# Breast Cancer Prediction Case Study - Bayesian Logistic Regression with Comparison of Frequentist and Bayesian Variable Selection Methods

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```
library(readr); library(dplyr)
library(ggplot2); library(dplyr)
library(tidyr); library(corrplot)
library(caret); library(MCMCpack)
library(car); library(boot)
library(gridExtra); library(BAS)
```

# Introduction

This case study is based on the Breast Cancer Wisconsin (Diagnostic) Data Set (https://www.kaggle.com/datasets/uciml/breast-cancer-wisconsin-data). The data set contains 569 observations and 32 variables. The data set is available at the UCI Machine Learning Repository. The data set contains mean (and at times min and max) values of the patient for the following numeric (continious) variables:

- a) radius (mean of distances from center to points on the perimeter)
- b) texture (standard deviation of gray-scale values)
- c) perimeter
- d) area
- e) smoothness (local variation in radius lengths)
- f) compactness (perimeter<sup>2</sup> / area 1.0)
- g) concavity (severity of concave portions of the contour)
- h) concave points (number of concave portions of the contour)
- i) symmetry
- j) fractal dimension ("coastline approximation" 1)

The data set also contains the following Binary variables:

2) Diagnosis (M = malignant, B = benign)

Where Malignant (M) means the tumor is cancerous, while Benign (B): means that the tumor is non-cancerous.

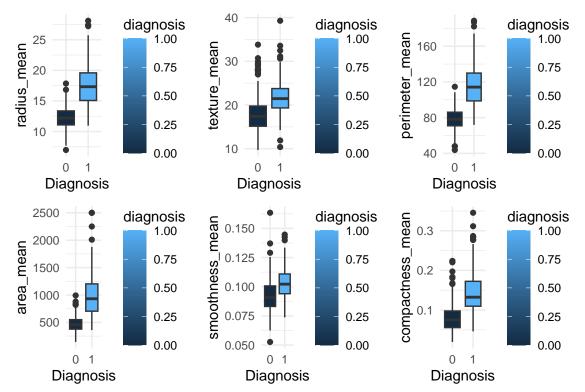
### Read Data

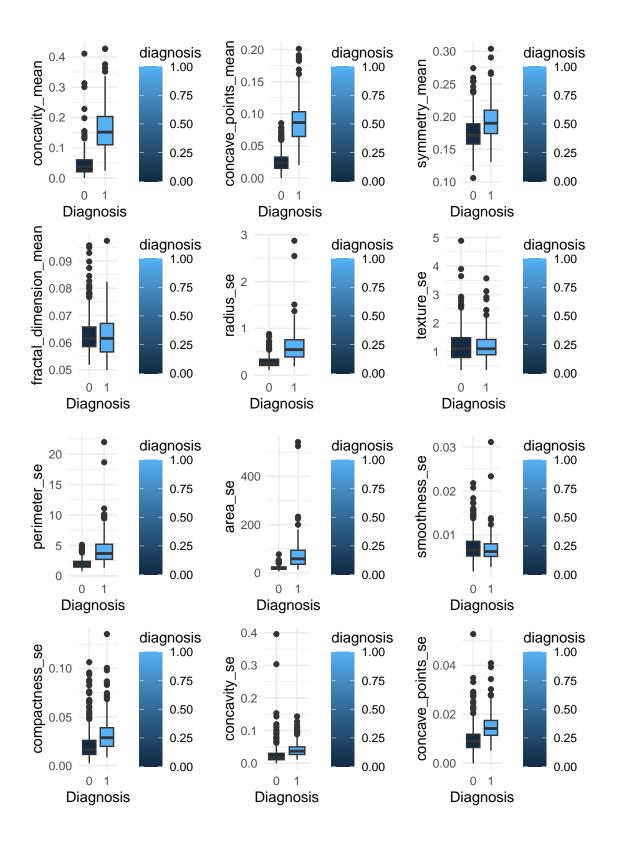
```
data <- read.csv("data.csv", header = TRUE, sep = ",")
data <- dplyr::select(data, -c(X,id))
names(data) <- gsub("\\.", "_", names(data))
data$diagnosis <- ifelse(data$diagnosis == "M", 1, 0)</pre>
```

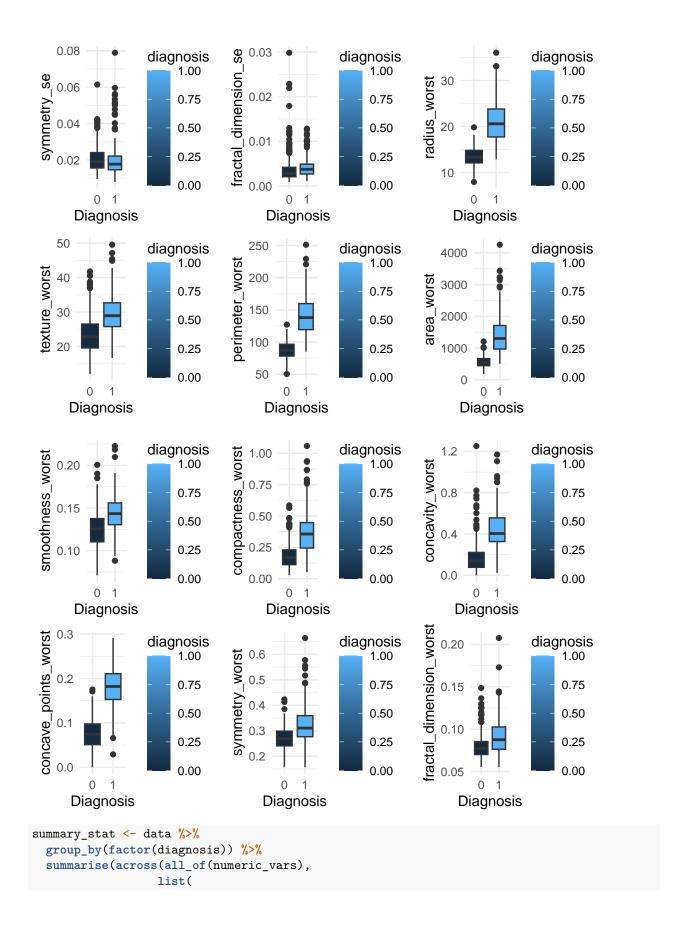
# **Exploratory Data Analysis**

# Relation with response var

```
numeric_vars <- data %>%select_if(is.numeric) %>% colnames()
numeric_vars <- setdiff(numeric_vars, "diagnosis")</pre>
plots <- lapply(numeric_vars, function(var) {</pre>
  ggplot(data, aes(x = factor(diagnosis), y = .data[[var]], fill = diagnosis)) +
    geom_boxplot() +
    labs(x = "Diagnosis", y = var) +
    theme_minimal()
})
# Print all plots
# Display plots in batches of 6 (2 rows × 3 columns)
num_plots <- length(plots)</pre>
batch_size <- 6
for(i in seq(1, num_plots, batch_size)) {
  end_idx <- min(i + batch_size - 1, num_plots)</pre>
  batch_plots <- plots[i:end_idx]</pre>
  grid.arrange(grobs = batch_plots, ncol = 3)
}
```



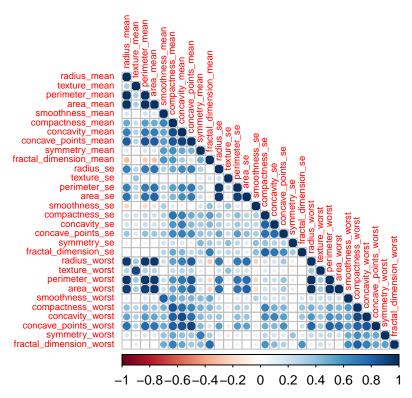




```
## # A tibble: 300 x 4
##
     `factor(diagnosis)` variable
                                            value
                                     stat
##
     <fct>
                         <chr>
                                     <chr> <dbl>
## 1 0
                                            12.1
                        radius_mean mean
## 2 0
                        radius_mean sd
                                            1.78
## 3 0
                        radius_mean median 12.2
## 4 0
                        radius_mean min
                                           6.98
## 5 0
                        radius_mean max
                                            17.8
## 6 0
                        texture_mean mean
                                          17.9
## 7 0
                        texture mean sd
                                            4.00
## 8 0
                        texture_mean median 17.4
## 9 0
                        texture_mean min
                                            9.71
## 10 0
                        texture_mean max
                                            33.8
## # i 290 more rows
```

### Correlation

```
# Check correlation between numeric variables
cor_matrix <- cor(data[, numeric_vars])
corrplot(cor_matrix, method = "circle",type="lower",tl.cex = 0.6)</pre>
```



```
# Or find highly correlated variables
high cor <- findCorrelation(cor matrix, cutoff = 0.8)
problematic_vars <- numeric_vars[high_cor]</pre>
print(problematic_vars)
    [1] "concavity_mean"
##
                                "concave_points_mean"
                                                        "compactness_mean"
##
    [4] "concave_points_worst"
                                "concavity_worst"
                                                        "perimeter_worst"
##
   [7] "radius_worst"
                                "perimeter_mean"
                                                        "compactness_worst"
## [10] "area_worst"
                                "radius_mean"
                                                        "perimeter_se"
## [13] "compactness_se"
                                "area_se"
                                                        "smoothness_mean"
## [16] "texture_mean"
```

# Variable Selection

### Frequentist Approach

Check VIF and remove variables with extremely high values

```
predictors <- setdiff(names(data), c("diagnosis"))
formula_str <- paste("diagnosis ~", paste(predictors, collapse = " + "))
formula <- as.formula(formula_str)

l_reg = lm(formula, data)
vif_values <- vif(l_reg)

vif_df <- data.frame(
    Variable = names(vif_values),</pre>
```

```
VIF = vif_values
)
vif df <- vif df %>% arrange(desc(VIF))
print(head(vif_df,5))
##
                           Variable
                                           VIF
## radius mean
                        radius mean 3806.1153
## perimeter_mean
                     perimeter_mean 3786.4004
## radius_worst
                       radius_worst 799.1059
## perimeter_worst perimeter_worst
                                      405.0233
## area mean
                          area_mean
                                      347.8787
vars_to_exclude <- c(head(vif_df,15)$Variable)</pre>
Check correlations after excluding x VIF, variables to pay attention if something does not work.
# Check correlation between numeric variables
cor_matrix_f <- cor(data[, setdiff(numeric_vars, vars_to_exclude)])</pre>
# corrplot(cor_matrix, method = "circle")
# Or find highly correlated variables
high_cor_f <- findCorrelation(cor_matrix_f, cutoff = 0.8)
problematic_vars_f <- setdiff(numeric_vars, vars_to_exclude)[high_cor_f]</pre>
print(problematic_vars_f)
```

```
## [1] "compactness_se" "smoothness_mean" "texture_mean"
selected_freq <- setdiff(numeric_vars, vars_to_exclude)</pre>
```

### Bayesian Approach

We obtain the posterior probability of including each beta, and also, some statistics for different models in order to select which one is the better. Then, we select the variables that compound the model with highest BF and lower logmang.

```
##
                          P(B != 0 | Y)
                                            model 1 model 2
                                                                 model 3
## symmetry_worst
                                 0.5695
                                          1.0000000
                                                     1.0000
                                                               0.0000000
                                                     0.0000
                                 0.3568
## fractal_dimension_worst
                                          1.0000000
                                                               0.000000
## BF
                                          0.9935745
                                                      1.0000
                                                               0.1810987
                                     NA
## PostProbs
                                     NA
                                          0.0031000
                                                      0.0027
                                                               0.0024000
## R2
                                          0.9431000
                                                      0.9216
                                                               0.9053000
                                     NA
                                                      9.0000
## dim
                                     NA 13.000000
                                                               7.0000000
                                     NA -51.6464504 -51.6400 -53.3487174
## logmarg
##
                              model 4
                                          model 5
                                        0.0000000
## symmetry_worst
                            1.0000000
                                       0.0000000
## fractal_dimension_worst
                            0.0000000
```

```
## BF
                              0.3408087 0.1458783
                              0.0024000 0.0023000
## PostProbs
## R2
                              0.9299000 0.9108000
## dim
                             11.0000000 8.0000000
## logmarg
                            -52.7164382 -53.5649865
# Posterior inclusion probabilities
pip <- model_bas$probne0</pre>
variable_names <- names(pip)</pre>
#pip_df <- data.frame(Variable = numeric_vars,</pre>
                       InclusionProb = pip)
#pip_df <- pip_df[order(pip_df$InclusionProb, decreasing = TRUE),]</pre>
#print(pip_df)
selected_bayes <- c( "perimeter_mean", "concave_points_mean", "compactness_mean",</pre>
                      "concavity_mean", "area_se", "smoothness_se", "concave_points_se",
                      "fractal_dimension_se", "radius_worst", "texture_worst",
                      "fractal_dimension_worst")
```

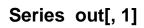
# Logistic Models

Then we fit the models for the variable selected in each case, evaluate the autocorrelation and fix the thinning parameter and starting point. This second one is selected as the beta estimation of a regular linear model.

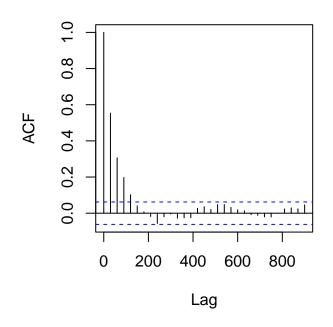
### Freq var selection

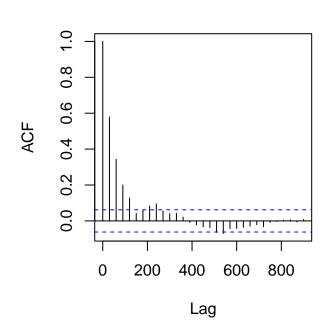
```
formula_str <- paste("diagnosis ~", paste(selected_freq, collapse = " + "))</pre>
formula <- as.formula(formula_str)</pre>
freq model1<-lm(formula, data = data)</pre>
beta.start1 <- coef(freq_model1)</pre>
out = MCMClogit(formula, data, burnin=1000, mcmc=21000, beta.start = beta.start1)
# summary(out)
# acf(out[,1])
# acf(out[,2])
# Correct autocorrelation
out = MCMClogit(formula, data, burnin=5000, mcmc=30000, thin = 30,
                beta.start = beta.start1)
summary(out)
##
## Iterations = 5001:34971
## Thinning interval = 30
## Number of chains = 1
## Sample size per chain = 1000
##
## 1. Empirical mean and standard deviation for each variable,
      plus standard error of the mean:
##
##
##
                                 Mean
                                            SD Naive SE Time-series SE
                              -6.9619 2.9564 0.093488
## (Intercept)
                                                             0.174505
```

```
## texture mean
                              0.1449
                                       0.1338 0.004230
                                                             0.008603
## smoothness mean
                           210.3856 38.8092 1.227254
                                                             2.364636
## symmetry mean
                              6.7972 13.7695 0.435430
                                                             0.874829
## fractal_dimension_mean -692.9451 85.9090 2.716683
                                                             5.109411
## texture se
                            -1.4312
                                       0.7698 0.024345
                                                             0.043598
## smoothness se
                           -245.3894 120.4758 3.809779
                                                             6.431210
## compactness se
                             20.8806 28.9179 0.914463
                                                             1.881365
## concavity se
                            -2.1651 11.8429 0.374504
                                                             0.841066
## concave_points_se
                            419.8216
                                      68.7222 2.173187
                                                             4.788362
## symmetry_se
                              2.8399 51.6192 1.632341
                                                             3.064199
## fractal_dimension_se
                           -235.3213 230.1363 7.277549
                                                            12.459032
## texture_worst
                              0.2585
                                      0.1235 0.003904
                                                             0.008201
## smoothness_worst
                              0.4922 26.7191 0.844933
                                                             1.548509
## symmetry_worst
                             12.2236
                                      8.5569 0.270594
                                                             0.595713
## fractal_dimension_worst 153.6350 38.6341 1.221717
                                                             2.154905
##
## 2. Quantiles for each variable:
##
##
                                                       50%
                                                                 75%
                                                                          97.5%
                                 2.5%
                                             25%
## (Intercept)
                           -1.257e+01
                                        -8.82359
                                                   -7.1256
                                                             -4.9263
                                                                       -1.06303
## texture_mean
                           -1.264e-01
                                        0.05609
                                                    0.1493
                                                              0.2347
                                                                        0.42288
## smoothness_mean
                            1.346e+02 185.56985
                                                  207.4429
                                                            237.4691
                                                                      285.25906
## symmetry_mean
                                                                       33.46638
                           -2.133e+01
                                        -2.07081
                                                    7.2447
                                                             16.8415
## fractal dimension mean -8.685e+02 -748.06764 -687.5111 -638.0705 -535.08845
## texture se
                                                             -0.9116
                           -3.011e+00
                                        -1.90562
                                                   -1.3896
                                                                       -0.01158
## smoothness se
                           -4.695e+02 -329.76049 -253.4453 -166.7919
                                                                        2.89369
## compactness_se
                           -3.356e+01
                                         1.54953
                                                   21.3018
                                                             40.3877
                                                                       76.28100
                                      -10.76965
## concavity_se
                           -2.669e+01
                                                   -2.0245
                                                              6.0901
                                                                       20.70983
## concave_points_se
                            2.861e+02 374.51992
                                                  416.7823
                                                           463.6432
                                                                      566.28489
## symmetry_se
                           -1.014e+02 -29.30766
                                                    2.0131
                                                             37.1225
                                                                       99.63610
## fractal_dimension_se
                           -7.050e+02 -385.97951 -235.5333
                                                            -66.6496
                                                                      194.69516
## texture_worst
                            2.987e-03
                                         0.17517
                                                    0.2570
                                                              0.3330
                                                                        0.52035
## smoothness_worst
                           -5.199e+01
                                       -17.05354
                                                   -0.2086
                                                             17.8640
                                                                       54.16787
## symmetry_worst
                           -2.732e+00
                                         6.80055
                                                   11.5672
                                                             17.4516
                                                                       30.08029
## fractal_dimension_worst 7.957e+01
                                       126.52236
                                                  155.9399
                                                            178.0914
                                                                      231.92666
par(mfrow=c(1,2))
acf(out[,1])
acf(out[,2])
```



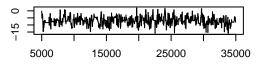
# Series out[, 2]





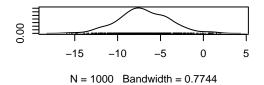
plot(out)

### Trace of (Intercept)

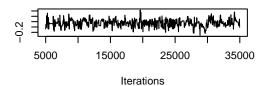


### Iterations

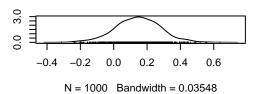
# **Density of (Intercept)**



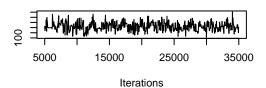
### Trace of texture\_mean



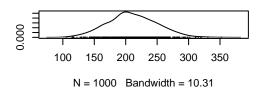
### Density of texture\_mean



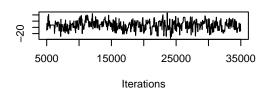
# Trace of smoothness\_mean



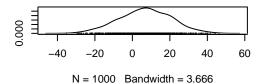
# Density of smoothness\_mean



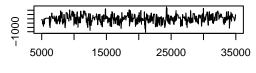
# Trace of symmetry\_mean



# Density of symmetry\_mean

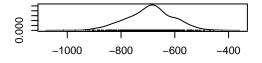


### Trace of fractal\_dimension\_mean



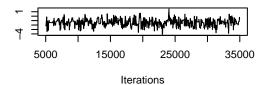
Iterations

### Density of fractal\_dimension\_mean

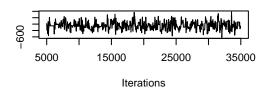


N = 1000 Bandwidth = 21.86

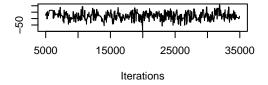
### Trace of texture\_se



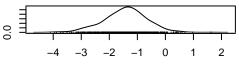
Trace of smoothness\_se



### Trace of compactness\_se

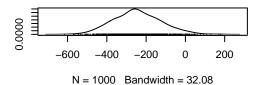


### Density of texture\_se

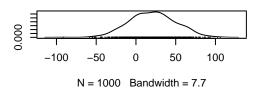


N = 1000 Bandwidth = 0.1975

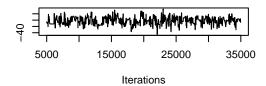
# Density of smoothness\_se



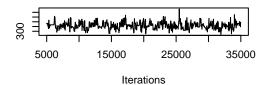
# Density of compactness\_se



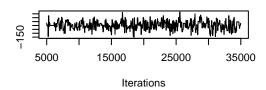
### Trace of concavity\_se



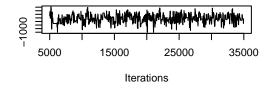
# Trace of concave\_points\_se



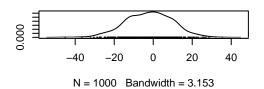
# Trace of symmetry\_se



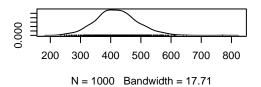
# Trace of fractal\_dimension\_se



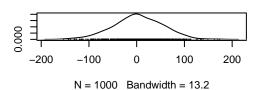
### Density of concavity\_se



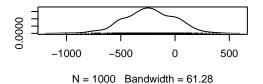
# Density of concave\_points\_se



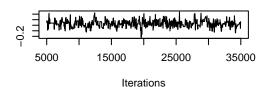
# Density of symmetry\_se



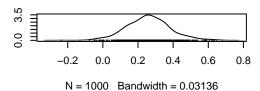
# Density of fractal\_dimension\_se



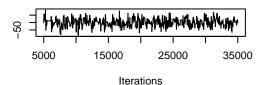
### Trace of texture worst



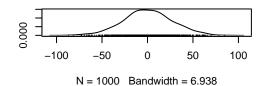
# Density of texture\_worst



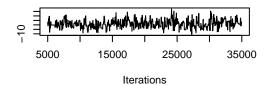
### Trace of smoothness worst



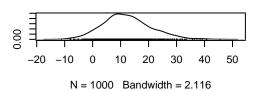
## Density of smoothness\_worst



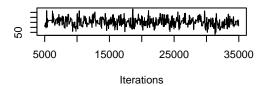
### Trace of symmetry\_worst



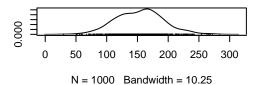
### **Density of symmetry\_worst**



### Trace of fractal\_dimension\_worst



### **Density of fractal\_dimension\_worst**



### Bayes var selection

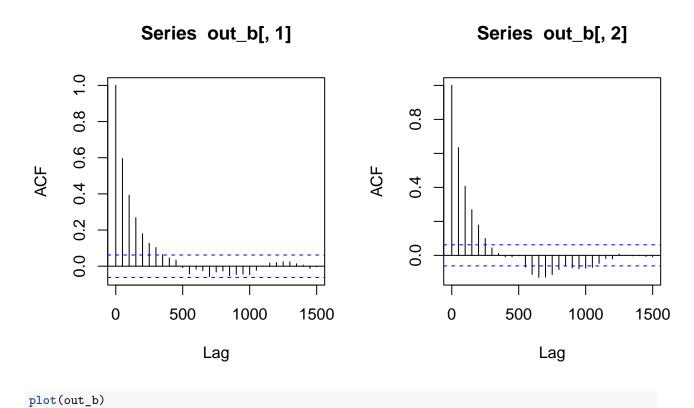
```
formula_str_b <- paste("diagnosis ~", paste(selected_bayes, collapse = " + "))
formula_b <- as.formula(formula_str_b)

# starting point
freq_model<-lm(formula_b, data = data)
beta.start <- coef(freq_model)

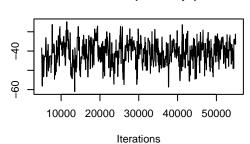
out_b = MCMClogit(formula_b, data, burnin=1000, mcmc=21000)

## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## summary(out_b)
# acf(out_b[,1])
# acf(out_b[,2])</pre>
```

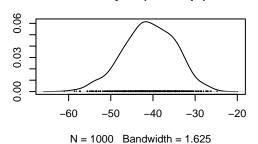
```
out_b = MCMClogit(formula_b, data, burnin=5000, mcmc=50000,
                 beta.start = beta.start, thin = 50, tune=0.5)
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
summary(out_b)
##
## Iterations = 5001:54951
## Thinning interval = 50
## Number of chains = 1
## Sample size per chain = 1000
##
## 1. Empirical mean and standard deviation for each variable,
     plus standard error of the mean:
##
##
##
                                            SD Naive SE Time-series SE
## (Intercept)
                          -4.089e+01
                                       6.10325 1.930e-01
                                                             4.069e-01
## perimeter_mean
                                                             5.462e-03
                          -8.767e-02
                                      0.08165 2.582e-03
## concave_points_mean
                          7.789e+01 33.64842 1.064e+00
                                                             2.578e+00
## compactness mean
                          -4.411e+01 20.79019 6.574e-01
                                                            1.713e+00
## concavity_mean
                          1.849e+01 10.76886 3.405e-01
                                                             8.339e-01
## area se
                          -7.147e-03
                                      0.01074 3.396e-04
                                                            5.185e-04
## smoothness_se
                          2.135e+02 150.05698 4.745e+00
                                                            1.353e+01
## concave points se
                           2.921e+02 101.48434 3.209e+00
                                                             5.821e+00
## fractal dimension se
                          -1.196e+03 340.24976 1.076e+01
                                                             1.952e+01
## radius worst
                                       0.44882 1.419e-02
                                                              2.645e-02
                           1.662e+00
                                       0.05205 1.646e-03
## texture_worst
                           2.749e-01
                                                              3.775e-03
## fractal_dimension_worst 1.559e+02 46.60596 1.474e+00
                                                              3.093e+00
##
## 2. Quantiles for each variable:
##
                                2.5%
##
                                            25%
                                                       50%
                                                                  75%
                                                                          97.5%
## (Intercept)
                          -5.348e+01 -4.504e+01 -4.084e+01 -3.637e+01
                                                                      -29.41492
## perimeter_mean
                          -2.363e-01 -1.449e-01 -9.337e-02 -3.226e-02
                                                                        0.08183
                           1.352e+01 5.524e+01 7.861e+01 1.017e+02 141.59098
## concave_points_mean
## compactness mean
                          -8.455e+01 -5.933e+01 -4.349e+01 -2.957e+01
                                                                       -4.49315
## concavity mean
                          -2.063e+00 1.172e+01 1.872e+01 2.589e+01
                                                                       39.71891
## area_se
                          -2.774e-02 -1.452e-02 -6.903e-03 -1.231e-04
                                                                        0.01324
## smoothness se
                          -8.381e+01 1.137e+02 2.063e+02 3.125e+02 512.29411
## concave_points_se
                           8.751e+01 2.252e+02 2.941e+02 3.573e+02 499.56987
## fractal dimension se
                          -1.905e+03 -1.411e+03 -1.177e+03 -9.488e+02 -589.19519
                           7.393e-01 1.375e+00 1.711e+00 1.994e+00
## radius worst
                                                                        2.41334
## texture worst
                           1.752e-01 2.396e-01 2.744e-01 3.086e-01
                                                                        0.37594
## fractal_dimension_worst 7.238e+01 1.237e+02 1.556e+02 1.866e+02 255.52220
par(mfrow=c(1,2))
acf(out b[,1])
acf(out_b[,2])
```



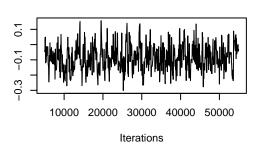
# Trace of (Intercept)



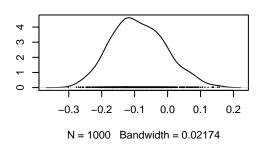
# **Density of (Intercept)**



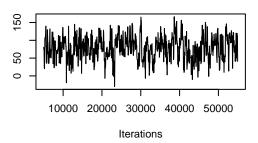
# Trace of perimeter\_mean



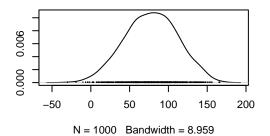
# Density of perimeter\_mean



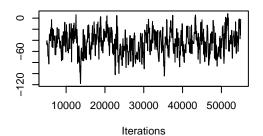
# Trace of concave\_points\_mean



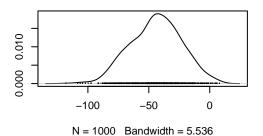
# Density of concave\_points\_mean



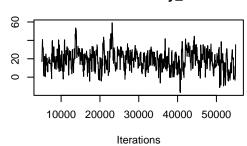
# Trace of compactness\_mean



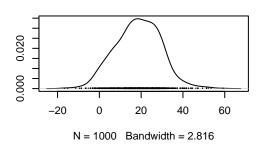
# Density of compactness\_mean



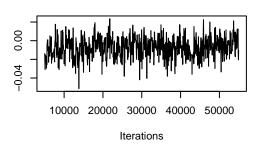
# Trace of concavity\_mean



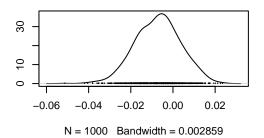
# Density of concavity\_mean

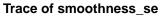


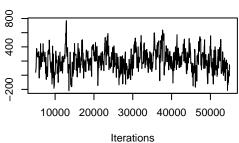
### Trace of area\_se



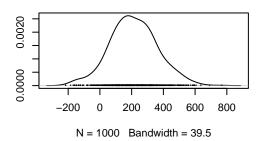
# Density of area\_se



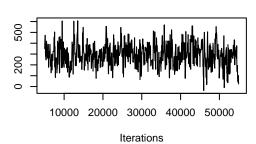




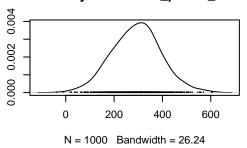
# Density of smoothness\_se



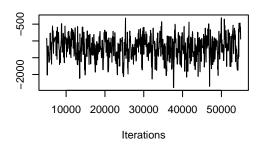
# Trace of concave\_points\_se



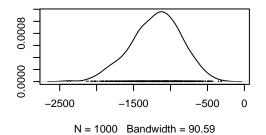
# Density of concave\_points\_se



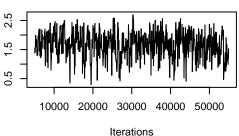
### Trace of fractal\_dimension\_se



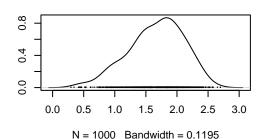
# Density of fractal\_dimension\_se



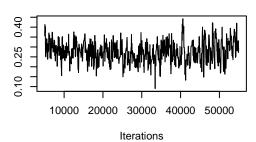




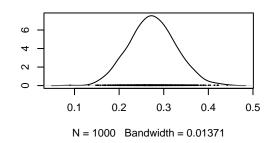
### Density of radius\_worst



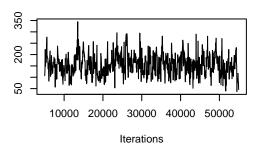
### Trace of texture\_worst



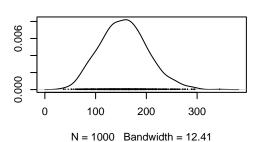
### Density of texture\_worst



# Trace of fractal\_dimension\_worst



### **Density of fractal\_dimension\_worst**



# Evaluate Models with Deviance Information Criterion (DIC)

In the following code, we will calculate the Deviance Information Criterion (DIC) for both the Frequentist and Bayesian models. The DIC is a measure of model fit that penalizes the complexity of the model. Lower values of DIC indicate better model fit. The DIC is calculated as follows:

$$DIC = \bar{D} + p_D$$

where:

-  $\bar{D}$  is the posterior mean deviance:

$$\bar{D} = \mathbb{E}[D(\theta) \mid \mathcal{D}]$$

with  $D(\theta) = -2 \log p(\mathcal{D} \mid \theta)$ , the deviance evaluated at parameter  $\theta$ . -  $p_D$  a penalization term (effective number of parameters to penalize model complexity):

$$p_D = \bar{D} - D(\hat{\theta})$$

where  $\hat{\theta}$  is the posterior mean of  $\theta$ .

The R implementation of the DIC function is as follows and was developed with help of Prof Michael Wiper:

```
# DIC Code
DIC = function(model, X, data, target) {
  dev = 0
  # Calculate Average Deviance of MCMC
  for (i in 1:nrow(model)) {
    params <- model[i,]</pre>
    p = inv.logit(X %*% params)
    p[data[target] == 0] = 1-p[data[target] == 0]
    dev = dev - 2 * sum(log(p)) # Negative log-likelihood
  D_bar = dev / nrow(model)
  # D_theta: Deviance at the posterior mean (using the average parameter values)
  posterior_means <- colMeans(model)</pre>
  linear_predictor <- X %*% posterior_means</pre>
  p_post <- inv.logit(linear_predictor)</pre>
  p_post[data[target] == 0] = 1-p_post[data[target] == 0]
  D theta = -2 * sum(log(p post)) # Deviance at the posterior mean
  # p D: Posterior deviance penalty
  p_D = D_bar - D_theta
  # DIC
 DIC = D_bar + p_D
  return(list(DIC=DIC, D_bar=D_bar, p_D=p_D))
}
```

We now continue with applying the DIC Score to the model derived from frequentist variable selection and the model derived from Bayesian variable selection. The straight forward conclusion is that the DIC is significantly better (lower) for the model that was set up with the Bayesian Variable Selection approach. Based on this result, we conclude this to be the best model and will use it for further analysis.

```
## [1] 229.9737
##
## $p D
## [1] 15.5509
# Bayesian
model = out b
X <- model.matrix(~ perimeter_mean + concave_points_mean + compactness_mean +
    concavity_mean + area_se + smoothness_se + concave_points_se +
   fractal_dimension_se + radius_worst + texture_worst + fractal_dimension_worst, data = data)
# model matrix
target = "diagnosis"
print("Bayesian Variable Selection DIC Score")
## [1] "Bayesian Variable Selection DIC Score"
DIC(model, X, data, target)
## $DIC
## [1] 89.86894
##
## $D_bar
## [1] 80.33019
##
## $p D
## [1] 9.538756
```

### Prediction

Since we already have our posterior coefficients from the MCMC samples, predicting is fairly straightforward. We will just have to turn the log odds back into probability space and choose a suitable threshold probability for the two classes (1 = malignant (cancer), 0 = benign)).

The standard threshold is 0.5. However, in the light of classifying cancer, one might choose this threshold more carefully. Assuming we are performing an initial cancer screening, we would prefer having a false positive than a false negative. In simpler words, we would rather initially classify something as cancer that later turns out as no cancer than missing a cancer diagnosis that actually is one. By lowering the threshold, we reduce our exposure to false negatives and increase sensitivity.

```
# posterior mean coefficients from MCMC samples
posterior_means <- colMeans(out_b)

# linear preds is in log odds space
linear_preds <- X %*% posterior_means

# inverse logit to get probabilities
prob_preds <- 1 / (1 + exp(-linear_preds))

# turn proba into binary prediction
test_preds <- ifelse(prob_preds >= 0.4, 1, 0)
```

Now that we have our predictions, let's analyze the outcome

```
positive = "1")
print(conf_matrix)
```

```
## Confusion Matrix and Statistics
##
##
             Reference
##
  Prediction
                0
                    5
##
            0 351
##
            1
                6 207
##
##
                  Accuracy: 0.9807
##
                    95% CI: (0.9657, 0.9903)
##
       No Information Rate: 0.6274
       P-Value [Acc > NIR] : <2e-16
##
##
##
                      Kappa: 0.9587
##
    Mcnemar's Test P-Value : 1
##
##
##
               Sensitivity: 0.9764
               Specificity: 0.9832
##
##
            Pos Pred Value: 0.9718
##
            Neg Pred Value: 0.9860
##
                Prevalence: 0.3726
##
            Detection Rate: 0.3638
      Detection Prevalence: 0.3743
##
##
         Balanced Accuracy: 0.9798
##
##
          'Positive' Class : 1
##
```

Overall, the model performs very well accurately classifying 98% of both malignant and benign cases. Our goal of achieving a high sensitivity was reached by correctly detecting 207 cancer cases out of 212 overall (97.6%). The specificity is also high with 98.3% of all benign cases correctly classified. Although false negatives might cause unnecessary medical procedures, we still prefer it this way. The model seems highly reliable as shown by the positive prediction value. When the model predicts cancer, it is correct 97.2% of the time. Overall, we have a more than solid classifier at hand.

### Conclusion

This report applied bayesian logistic regression to predict breast cancer by using a breast mass cell dataset made available by the University of Irvine. The exploratory data analysis revealed significant correlations among predictors, which required variable selection. A comparison between frequentist and bayesian variable selection methods was conducted which proved the bayesian approach as far superior when assessed on the Deviance Information Criterion. The final model was evaluated via a confusion matrix which yielded a highly reliable classifier for cancer detection