The GAPic Package

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GAPDays Spring 2024

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- (ii) $\forall v \in X_0 : def(v) := |\{f \in X_2 \mid v \prec f\}| < \infty$
- (iii) $\forall v \in X_0$: there is an ordering of $e_1, f_1, \dots, e_{deg(v)}, f_{deg(v)} \prec v$ such that

$$e_1 \prec f_1 \prec e_2 \prec f_2 \prec \cdots \prec f_{deg(v)} \prec e_{deg(v)}$$

with $e_1 = e_{deg}(v)$ if (i) is an equality.

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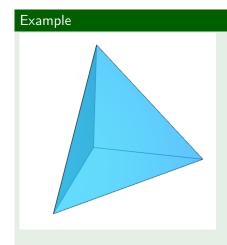
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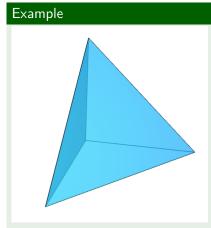
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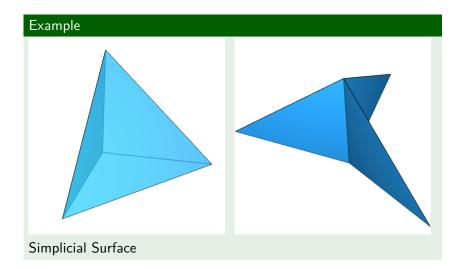
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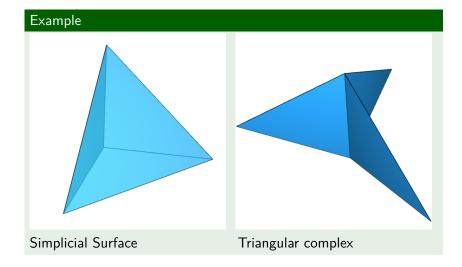
Condition (iii) is called the umbrella condition.





Simplicial Surface





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Embedded triangular complex

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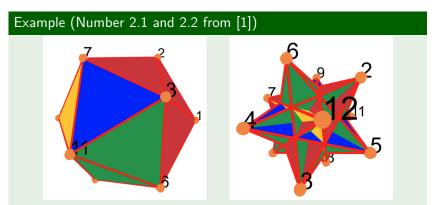
Embedded simplicial surface

Simplicial Surfaces Package

- Has functionality for displaying simplicial surfaces
 - Generates a .html file
 - Uses three.js

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Discussion geometry





The upcoming release r125 will contain a major, potentially breaking change. The class THREE.Geometry will be no longer part of the core but moved to jsm/deprecated/Geometry.js. It will only be available as an ES6 module and not as a global script.

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Discussion

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aeometry

3 🧳 Jan '21

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→ Decided to rewrite whole functionality

Advancements after rewrite

- New security requirements of JavaScript and modern browsers: need to load the code from some server \rightarrow way smaller file sizes (for small examples 9kB vs. 539kB)

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- New security requirements of JavaScript and modern browsers: need to load the code from some server → way smaller file sizes (for small examples 9kB vs. 539kB)
- More efficient Animations, faster loading, lower memory usage
- Also works for triangular complexes
 - ightarrowDoes not depend on umbrella condition for visualization

Afterwards decided to roll this feature into new package:

 $\mathsf{GAP}\ \mathbf{i}\mathsf{mage}\ \mathbf{c}\mathsf{reator}$

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GAP image creator

Goal is to divide up working with triangular complexes/simplicial surfaces in SimplicialSurfaces and to visualize them in GAPic.

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Time for Demonstrations

Time for Demonstrations

- Triangular complex
- Improved performance
- Normals material
- Intersection planes
- Parameterized coordinates

Thank you for your attention

Want to get involved? \rightarrow github.com/GAP-ART-RWTH/GAPic

References:

[1] Karl-Heinz Brakhage et al. *The icosahedra of edge length 1*. 2019. DOI: 10.48550/ARXIV.1903.08278. URL: https://arxiv.org/abs/1903.08278.