# The GAPic Package

Lukas Schnelle

GAPDays Spring 2024

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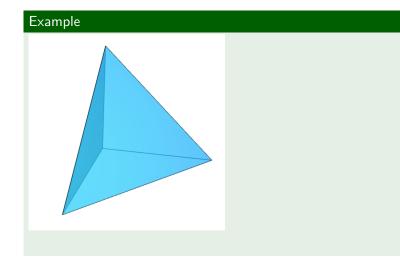
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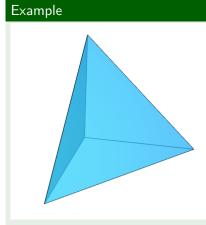
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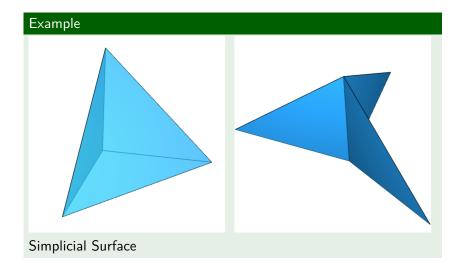
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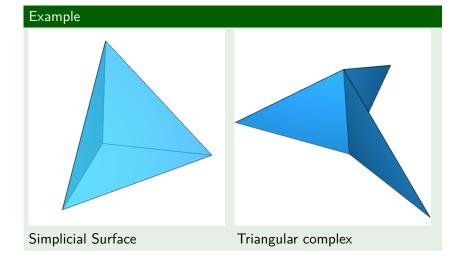
Condition (iii) is called the umbrella condition.





Simplicial Surface





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## Example



**Embedded** triangular complex

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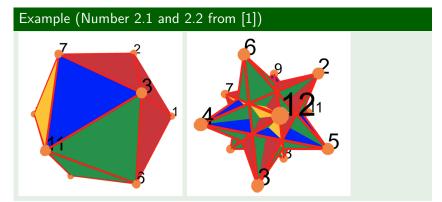
Embedded simplicial surface

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- Has functionality for displaying simplicial surfaces
  - Generates a .html file
  - Uses three.js

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## THREE.Geometry will be removed from core with r125

Discussion

geometry





The upcoming release r125 will contain a major, potentially breaking change. The class THREE.Geometry will be no longer part of the core but moved to jsm/deprecated/Geometry.js. It will only be available as an ES6 module and not as a global script.

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3 🥒 Jan '21

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→ Decided to rewrite whole functionality

### Advancements after rewrite

- New security requirements of JavaScript and modern browsers: need to load the code from some server  $\rightarrow$  way smaller file sizes (for small examples 9kB vs. 539kB)

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- More efficient Animations, faster loading, less memory (Demo in Browser)
- Also works for triangular complexes
  - ightarrow Does not depend on umbrella condition for visualization (Demo in Browser)

GAPic ●00

Afterwards decided to roll this feature into new package:

GAP image creator

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Goal is to divide up working with triangular complexes/simplicial surfaces in SimplicialSurfaces and to visualize them in GAPic.

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- Parameterized coordinates
  - ightarrow allows coordinates to be defined as any equation JavaScript can evaluate

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# Thank you for your attention

Want to get involved?  $\rightarrow$  github.com/GAP-ART-RWTH/GAPic

### References:

[1] Karl-Heinz Brakhage et al. *The icosahedra of edge length 1*. 2019. DOI: 10.48550/ARXIV.1903.08278. URL: https://arxiv.org/abs/1903.08278.