Transmission Type Fuel Efficiency Analysis

2014-10-26

Executive Summary

Using the Motor Trends data this report endeavours to find out whether automatic or manual transmission is better for MPG. This report will further more attempt to quantify the MPG difference between automatic and manual transmissions. In an effort to keep the report concise most of the R code is not shown, please feel free to visit this GitHub Repository for the complete R Markdown code.

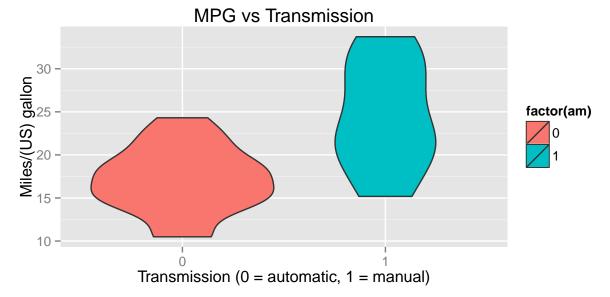
Data Dictionary

The Motor Trends data consists of 32 observations spanning 11 variables. For a full description of the data definition please refer to the Motor Trends Data Documentation.

Field	Definition	Field	Definition
mpg	Miles/(US) gallon	cyl	Number of cylinders
disp	Displacement (cu.in.)	hp	Gross horsepower
drat	Rear axle ratio	wt	Weight $(lb/1000)$
qsec	1/4 mile time in seconds	vs	V/S (0 = V-engine, 1 = straight engine)
am	Transmission (0 = automatic, $1 = \text{manual}$)	gear	Number of forward gears
carb	Number of carburetors		

Exploring the Data

We start with a violin plot of MPG vs Transmission to explore the relatioship between transmission type and MPG. Next we run summary() on a few of the more interesting fields in the data to get a feel of what the data is telling us.



```
##
       cars.mpg
                        cars.cvl
                                       cars.disp
                                                         cars.hp
                            :4.00
                                            : 71.1
                                                              : 52.0
##
    Min.
            :10.4
                    Min.
                                    Min.
                                                      Min.
    1st Qu.:15.4
                    1st Qu.:4.00
##
                                    1st Qu.:120.8
                                                      1st Qu.: 96.5
                                    Median :196.3
    Median:19.2
                    Median:6.00
                                                      Median :123.0
##
##
    Mean
            :20.1
                    Mean
                            :6.19
                                    Mean
                                            :230.7
                                                      Mean
                                                              :146.7
    3rd Qu.:22.8
                    3rd Qu.:8.00
                                    3rd Qu.:326.0
##
                                                      3rd Qu.:180.0
##
    Max.
            :33.9
                    Max.
                            :8.00
                                    Max.
                                            :472.0
                                                      Max.
                                                              :335.0
##
      cars.drat
                        cars.wt
                                       cars.qsec
                                                       cars.carb
##
    Min.
            :2.76
                            :1.51
                                    Min.
                                            :14.5
                                                     Min.
                                                             :1.00
                    Min.
##
    1st Qu.:3.08
                    1st Qu.:2.58
                                    1st Qu.:16.9
                                                     1st Qu.:2.00
##
    Median:3.69
                    Median:3.33
                                    Median:17.7
                                                     Median:2.00
            :3.60
                            :3.22
                                            :17.8
                                                             :2.81
##
    Mean
                    Mean
                                    Mean
                                                     Mean
##
    3rd Qu.:3.92
                    3rd Qu.:3.61
                                    3rd Qu.:18.9
                                                     3rd Qu.:4.00
            :4.93
                            :5.42
                                            :22.9
##
    Max.
                    Max.
                                    Max.
                                                     Max.
                                                             :8.00
```

We find that the mean MPG for our Automatic transmissions is 17.1474 and for Manual transmissions is 24.3923. This is a mean MPG difference of 7.2449 with the Automatic transmission being less efficient. This extremely simple comparison is just the beginning of our journey.

Regression Modelling

We iteratively run linear regressions starting with summary(lm(mpg ~ cyl + disp + hp + drat + wt + qsec + vs + am + gear + carb, data = cars))\$coef, in each subsequent run we remove the entry (field) with the largest Pr(>|t|) score until we have only one left, namely wt. Next we use the anova() function to find the cut-off point in terms regression variables. We find that including the gear is not beneficial to our regression model and when it is not specified the Transmission type am scrapes in just under 5%.

Field	$\Pr(>F)$ for (mpg ~ wt, qsec, am)	$\Pr(>F) \text{ for (mpg} \sim \text{wt, qsec, am, gear)}$
wt	NA	NA
qsec	$9.2862 \times 10-4$	0.0011
am	0.0467	0.0508
gear		0.8897

The fields wt, qsec and am feel like the right set of variables to be looking at but a linear coefficient against qsec seems odd. One would expect diminishing returns for the fuel consumed as the qsec gets smaller (i.e. increased acceleration). In an effort to model these diminishing returns I introduce a new variable named qsec.2.I which represents the inverse of the square of qsec $(1/qsec^2)$. The following two tables detail the coefficients of the respective linear regression models. We see that using the variable qsec.2.I as opposed to qsec yields a tighter fit to our data as evidenced by every single Pr(>|t|) being almost halved.

```
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  9.618
                             6.9596
                                      1.382 1.779e-01
## wt
                  -3.917
                             0.7112
                                     -5.507 6.953e-06
## qsec
                  1.226
                             0.2887
                                      4.247 2.162e-04
## am
                  2.936
                             1.4109
                                      2.081 4.672e-02
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  42.806
                              2.6020
                                      16.451 6.347e-16
## wt
                   -3.845
                              0.6806
                                      -5.649 4.719e-06
```

```
## qsec.2.I -3603.694 767.4360 -4.696 6.370e-05
## am 3.191 1.3612 2.344 2.639e-02
```

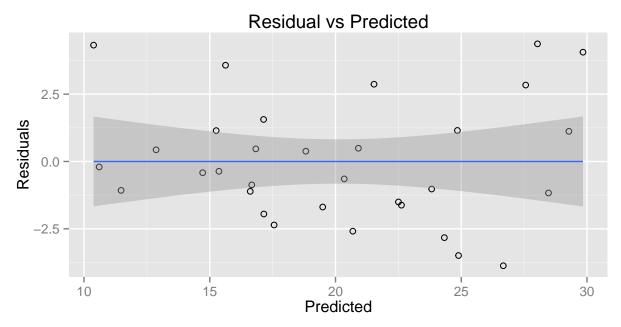
Interpreting the Coefficients

Using the qsec based regression we arrive at following model. For each additional wt (1000 lb) our MPG decreases by 3.9165. For each additional second needed to complete qsec (1/4 mile time in seconds) our MPG increases by 1.2259. Lastly, Manual transmissions yield a 2.9358 MPG benefit (increase) over Automatic transmissions.

Confidence

The R^2 for the qsec and qsec.2.I regression models are 0.8497 and 0.8617 respectively. The R^2 for the qsec.2.I based regression model is marginally stronger (by 0.0121) and with this model explaining 0.8617 of the variability it is a highly predictive model. We opt to use the qsec.2.I based regression model going forward.

Residuals



The Residuals vs. Predicted look good for this model and I believe we can in good conscience use it.

Conclusion

Using our qsec.2.I based regression model we find that Manual transmissions yield better MPG in the amount of 3.1909 MPG.