

2020 Winter Midterm - PRACTICE

Introduction to Theoretical Computer Science (Concordia University)



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Part A There are 8 multiple-choice questions in this part.

You **must** use the supplied multiple-choice answer sheet to record your answers for this part (Part A). Only answers on that sheet will be considered (answers on the exam booklet itself will be **discarded**). You must highlight your ID on that multiple-choice sheet as well. A correct choice for one question will get you 4 points. An incorrect answer, marking several answers or selecting nothing for a question will get you 0. If you believe that more than one answer is correct, select the best answer.

1. What is the best asymptotic ("big-O") characterization of the following function:

$$f(n) = (14\log n)^2 + \log(3^n)$$

- a) $O(3^n)$
- b) $O(n^2)$
- c) O(n)
- d) $O(2^n)$
- e) O(logn)
- 2. Give the best asymptotic ("big-Oh") characterization of the worst case and the best case time complexities of the algorithm DoAgain(A, n).

Algorithm DoAgain(A, n)Input: Array A storing integers and of size n > 1. $sum \leftarrow 0$ for $c \leftarrow 0$ to n^2 do if A[0] < 0 then for $k \leftarrow 0$ to n - 1 do $sum \leftarrow sum + c \cdot A[k]$

- (a) Best case O(n) and worst case $O(n^2)$
- (b) Best case O(n) and worst case $O(n^3)$
- (c) Best case $O(n^2)$ and worst case $O(n^3)$
- (d) Best case O(n) and worst case $O(n^4)$
- (e) Best case $O(n^3)$ and worst case $O(n^4)$
- 3. You have implemented the queue with a linked list, keeping track of a front node and a rear node with two reference variables. Which of these reference variables will change during an insertion into a NONEMPTY queue?
 - a) Neither changes
 - b) Only front changes.
 - c) Only rear changes.
 - d) Both change.

4. Here is an incorrect kind of pseudo code a student provided for the algorithm which is supposed to determine whether a sequence of parentheses is balanced:

```
declare a character stack
while ( more input is available)
{
   read a character
   if ( the character is a '(' )
        push it on the stack
   else if ( the character is a ')' and the stack is not empty )
        pop a character off the stack
   else
        print "unbalanced" and exit
}
print "balanced"
```

Which of these unbalanced sequences does the above code think is balanced?

```
a) ((())
b) ())(()
c) (()()))
d) (()))()
```

5. Consider the algorithm *Multiply*(*A*,*n*) below. *A* is an array of size *n* storing integer values. What is the best characterization of the best and worst case asymptotic time complexity of the following algorithm?

```
Algorithm Multiply(A, n)

result = 0

for i = 0 to \frac{n}{2} do

j = 0

while A[j] < 0 and j < \frac{n}{2} do

result = result + A[i] * A[j]

j = j + 1

return result
```

```
a) Best case O(1), worst case O(n).
```

```
b) Best case O(\log n), worst case O(n).
```

- c) Best case O(n), worst case O(n).
- d) Best case O(1), worst case $O(n^2)$.
- e) Best case O(n), worst case $O(n^2)$.

- 6. Consider the following pairs of functions: f(n), g(n). For which pair, the functions are such that f(n) is O(g(n)) and g(n) is **not** O(f(n))?
 - (a) $f(n) = n^2, g(n) = 2n^2 + 7$
 - (b) $f(n) = \log n, g(n) = \log(n^2)$
 - (c) f(n) = 17, g(n) = n + 1
 - (d) f(n) = n, g(n) = 3000n + 1
 - (e) $f(n) = \log n, g(n) = 1/n$
- 7. What is the best asymptotic ("big-O") characterization of the following function:

$$f(n) = 6n \log \log(n^2) + 2n\log^2 n + n\log n$$

- a) $O(nlog^2n)$
- b) O(nlogn)
- c) $O(n^2 log n)$
- d) $O(n^3 log n)$
- e) $O(nlog(n^2))$
- 8. Suppose we have a circular array implementation of the queue class, with ten items in the queue stored at data [2] through data [11]. The current capacity is 42. Where does the insert method place the new entry in the array?
 - a) data[1]
 - b) data[2]
 - c) data[11]
 - d) data[12]

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Part B

Important Note

- ***** Efficiency refers to <u>time and memory.</u>
- ❖ You will be graded as follows:
 - A mark (100%) if you provide a **correct and most efficient** algorithm.
 - A mark (%80) if you provide a **correct and second efficient** algorithm.
 - A mark (%50) if you provide a **correct** and missed to consider the efficiency of the algorithm.

B.1 [33 Points] A palindrome is a string that reads the same forward and backward, capitalization and space are ignored. For example *deed*, *go dog*, *level*.... are palindromes.

a) [10 Points] Write an iterative algorithm in pseudo code that tests whether a string is a palindrome.

b) [10 Points] Write a recursive algorithm in pseudocode that tests whether a string is a palindrome.

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c) **[8 Points]** Describe how you could use a *Stack* or *Queue* to check whether a string is a palindrome, and write the pseudo code for that.

d) [5 Points] What are the worst-case runtimes of above algorithms (a), (b), (c) (use the big-Oh notation). Justify your answers.

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Part C [24 Points]

For each of the 4 questions in this part, mark T if the given statement is **ALWAYS** true. Otherwise mark F and **justify** your answer. If you do not justify the FALSE case you will lose $\frac{4}{6}$ of the mark. There is **no penalty** for selecting a wrong answer. **Hint**: a correct counter example and/or correct specification will give you better marks. A correct answer will get you **6** points.

1. If $f(n) = 5n^2$ then $f(n) \in \Omega(2^n)$

 $\Box T$ $\Box F$

2. The worst-case asymptotic running time for the best algorithm for finding something in a sorted array? is O(n) $\Box T$ $\Box F$

3. The worst-case asymptotic running time of finding and removing all values greater than 12 from a stack implemented with a linked-list (leaving the rest of the stack in its original order) is O(1) $\Box T$ $\Box F$

4. Performing a remove operation at the tail in a list ADT implemented as a singly LinkedList that keeps track of the head, is very efficient: performed in a constant time O(1).

 $\Box T \qquad \quad \Box F$