## 13.2 Simulation

June 27, 2018

## 0.0.1 Question 13.2

In this problem, you will simulate a simplified airport security system at a busy airport. Passengers arrive according to a Poisson distribution with  $\lambda_1=5$  per minute (i.e., mean interarrival rate  $\mu_1=0.2$  minutes) to the ID/boarding-pass check queue, where there are several servers who each have exponential service time with mean rate  $\mu_2=0.75$  minutes. [Hint: model them as one block that has more than one resource.] After that, the passengers are assigned to the shortest of the several personal-check queues, where they go through the personal scanner (time is uniformly distributed between 0.5 minutes and 1 minute).

Use the Arena software (PC users) or Python with SimPy (PC or Mac users) to build a simulation of the system, and then vary the number of ID/boarding-pass checkers and personal-check queues to determine how many are needed to keep average wait times below 15 minutes. Note: If you're using SimPy, or if you have access to a non-student version of Arena, you can use  $\lambda_1=50$  to simulate a busier airport.

## 0.0.2 Results summary

For the simulation where the mean passenger arrival rate is 5, we find that the optimal configuration yielding mean wait time just below 15 minutes was with 5 id scanners and 9 personal checkers (time of 14.639845305).

For the simulation where the mean passenger arrival rate is 50, we find that the optimal configuration yielding mean wait time just below 15 minutes was with 35 id scanners and 31 personal checkers (time of 14.9797373981).

However, we would need to include costs in our final analysis as well. If personal checkers are twice as expensive as id scanners, we would choose a solution that has fewer personal checkers (for example num\_id= 36 and num\_pc= 20 yields a time of 14.7139433891).

## 0.0.3 References

Example with analogous arrival processes and queues:

https://pythonhosted.org/SimPy/Tutorials/TheBank.html

TA carwash example: http://simpy.readthedocs.io/en/latest/examples/carwash.html

```
import numpy as np
RANDOM\_SEED = 42
TOTAL WAIT=[]
                 #Total wait time to use both IDboarding and PersonalCheck stations
REPLICATIONS=5 #Number of replications for which to repeat the experiment
MU 1 = 0.2
                #Mean interarrival rate for passenger generation
MU 2 = 0.75
                 #Mean service time (IDboarding check time)
#IDboarding parameters. One queue for all passengers:
            # Number of stations in the IDboarding check system
NUM_ID = 5
SIM_TIME = 100
                 # Simulation time in minutes (100 minutes was suggested in TA vide
# When the passengers are done at the IDboarding station, they enter the
# PersonalCheck station where there is a queue for each PersonalCheck machine
#PersonalCheck parameters
NUM_PC = 5 #Number of PersonalCheck stations
MIN_PC = 0.5 #Lower bound on PersonalCheck time
MAX_PC = 1.0 #Upper bound on PersonalCheck time
#Resource queue counter
def NoInSystem(R):
    """ Total number of customers in the resource R"""
   return (len(R.queue)+R.count)
#Define IDboarding class
class IDboarding(object):
    """An IDboarding has a limited number of stations (``NUM_ID``) to
    check passenger ID's in parallel.
    Passengers have to request one of the machines. When they get one,
    they can start the checking processes and wait for it to finish
    (which takes an average of ``mu_2`` minutes).
    def __init__(self, env, num_id, mu_2):
        self.env = env
        self.machine = simpy.Resource(env, num_id)
        self.mu_2 = mu_2
    def IDcheck(self, passenger):
        """Takes a passenger and checks their ID and boarding pass"""
        yield self.env.timeout(random.expovariate(1.0/self.mu_2))
class PersonalCheck(object):
```

```
"""Final passenger processing station. When a passenger arrives,
    they join the shortest queue. When it is their turn to be
    processed, the time it takes is Uniform(min_pc, max_pc)"""
    def __init__(self, env, NUM_PC, min_pc, max_pc):
        self.env = env
        self.machine = []
        for i in range(NUM PC):
            self.machine.append(simpy.Resource(env, 1))
        self.min_pc = min_pc
        self.max_pc = max_pc
    def pcheck(self, passenger):
        """The PersonalCheck processes. It takes a passenger and processes them."""
        yield self.env.timeout(random.uniform(self.min_pc,self.max_pc))
def passenger(env, name, cw, ew):
    """The passenger process arrives and requests
    an IDboarding machine. They then start the checking process,
    waits for it to finish and leaves. They then enter the
    PersonalCheck station to receive final processing."""
    arrive_id=env.now
    with cw.machine.request() as request:
        yield request
        wait_id=env.now-arrive_id
        #print('%s waited %.2f minutes to begin using the IDcheck'% (name, wait id))
        yield env.process(cw.IDcheck(name))
    arrive_pc=env.now
    #Find the shortest wax queue
   minq=0
    for i in range(len(ew.machine)):
        if (ew.machine[i].count < ew.machine[minq].count):</pre>
            minq=i
    with ew.machine[minq].request() as request:
        yield request
        wait_pc=env.now-arrive_pc
        #print('%s waited %.2f minutes to begin using the Personal Check'% (name, wai
        yield env.process(ew.pcheck(name))
        total_wait=wait_id+wait_pc
        TOTAL_WAIT.append(total_wait)
def setup(env, num_id, mu_2, mu_1, num_pc, min_pc, max_pc):
    """Create an idcheck, with passengers approx.
    every ``mu_1`` minutes."""
    # Create the idcheck and carwax stations
    idcheck = IDboarding(env, num_id, mu_2)
    personalcheck = PersonalCheck(env, num_pc, min_pc, max_pc)
```

```
# Create more passengers while the simulation is running
            i=0
            while True:
                yield env.timeout(np.random.poisson(mu_1))
                 env.process(passenger(env, 'Passenger %d' % i, idcheck, personalcheck))
        #Calculations and Analysis
In [7]: #Set up a loop to calculate the average over REPLICATIONS:
       TOTAL_WAIT=[]
       for num_id in range(1,10):
            for num_pc in range(1,10):
               reps=[]
               for i in range(REPLICATIONS):
                   random.seed(RANDOM_SEED) # This helps reproducing the results
                   env = simpy.Environment()
                   env.process(setup(env, num_id, MU_2, MU_1, num_pc, MIN_PC, MAX_PC))
                   env.run(until=SIM TIME)
                   TOTAL_WAIT
                   reps.append(np.mean(TOTAL WAIT))
               print('Average wait time over ', REPLICATIONS, ' replications with num_id=',
                     num id, "and num pc=", num pc, ":", np.mean(reps))
                           replications with num_id= 1
                                                        and num_pc=1:34.3010667369
Average wait time over 10
Average wait time over 10
                           replications with num_id= 1
                                                        and num_pc= 2 : 34.0633257641
Average wait time over 10
                           replications with num_id= 1
                                                        and num_pc=3:34.0044374835
                           replications with num_id= 1
                                                        and num pc= 4 : 34.4733403157
Average wait time over 10
Average wait time over 10
                           replications with num_id= 1
                                                        and num_pc = 5 : 34.9509757571
                           replications with num_id= 1
                                                        and num_pc = 6 : 35.2423608078
Average wait time over 10
Average wait time over 10
                           replications with num_id= 1
                                                        and num_pc=7:35.5699376097
Average wait time over 10
                           replications with num_id= 1
                                                        and num_pc = 8 : 35.6766993712
                           replications with num_id= 1
                                                        and num_pc = 9 : 35.7173722404
Average wait time over 10
Average wait time over 10
                           replications with num_id= 2
                                                        and num_pc = 1 : 35.7842448908
                                                        and num_pc= 2 : 34.9993070731
Average wait time over 10
                           replications with num_id= 2
                           replications with num_id= 2
Average wait time over 10
                                                        and num_pc=3:33.6204918788
Average wait time over 10
                           replications with num id= 2
                                                        and num_pc = 4 : 32.1152695072
                           replications with num_id= 2
                                                        and num_pc = 5 : 30.7438949344
Average wait time over 10
                           replications with num_id= 2
Average wait time over 10
                                                        and num_pc= 6 : 29.709688136
                           replications with num_id= 2
                                                        and num_pc=7:29.1588798281
Average wait time over 10
                           replications with num id= 2
                                                        and num pc= 8 : 28.5715998657
Average wait time over 10
                           replications with num_id= 2
                                                        and num_pc= 9 : 28.2210467464
Average wait time over 10
Average wait time over 10
                           replications with num_id= 3
                                                        and num pc= 1 : 28.2784940556
Average wait time over 10
                           replications with num_id= 3
                                                        and num_pc= 2 : 28.1561222315
Average wait time over 10
                           replications with num_id= 3
                                                        and num_pc=3:27.5328005098
                           replications with num_id= 3
                                                        and num_pc= 4 : 26.5794988151
Average wait time over 10
```

```
Average wait time over
                        10
                            replications with num_id= 3
                                                          and num_pc = 5 : 25.6059062758
Average wait time over
                        10
                            replications with num_id= 3
                                                          and num_pc = 6 : 24.6199248793
                            replications with num_id= 3
                                                          and num_pc = 7 : 23.7643383745
Average wait time over
                        10
                                                          and num_pc=8:23.0715408291
                        10
                            replications with num_id= 3
Average wait time over
Average wait time over
                        10
                            replications with num id= 3
                                                          and num pc= 9 : 22.5445537493
                                                          and num pc= 1 : 22.4717473932
Average wait time over
                            replications with num id= 4
                        10
                            replications with num id= 4
                                                          and num pc= 2 : 22.5230681753
Average wait time over
Average wait time over
                        10
                            replications with num_id= 4
                                                          and num_pc= 3 : 22.2457832222
                        10
Average wait time over
                            replications with num_id= 4
                                                          and num_pc = 4 : 21.6540215025
Average wait time over
                        10
                            replications with num_id= 4
                                                          and num_pc = 5 : 20.8315624962
                                                          and num_pc = 6 : 20.0090927727
Average wait time over
                        10
                            replications with num_id= 4
Average wait time over
                        10
                            replications with num_id= 4
                                                          and num_pc = 7 : 19.1662047312
                                                          and num_pc= 8 : 18.3915894139
Average wait time over
                        10
                            replications with num_id= 4
                        10
                            replications with num_id= 4
                                                          and num_pc = 9 : 17.7411202509
Average wait time over
Average wait time over
                        10
                            replications with num_id= 5
                                                          and num_pc = 1 : 17.5756307455
Average wait time over
                        10
                            replications with num_id= 5
                                                          and num_pc= 2 : 17.6982433862
                        10
                            replications with num_id= 5
                                                          and num_pc= 3 : 17.6177566948
Average wait time over
                                                          and num_pc = 4 : 17.3230791031
Average wait time over
                        10
                            replications with num_id= 5
                                                          and num_pc= 5 : 16.8759821719
Average wait time over
                        10
                            replications with num_id= 5
                            replications with num id= 5
                                                          and num pc= 6:16.3010224897
Average wait time over
                        10
Average wait time over
                        10
                            replications with num id= 5
                                                          and num pc= 7 : 15.7179822899
Average wait time over
                            replications with num id= 5
                                                          and num pc= 8 : 15.1510781939
                        10
Average wait time over
                        10
                            replications with num_id= 5
                                                          and num_pc = 9 : 14.639845305
                                                          and num_pc=1:14.5425208534
Average wait time over
                        10
                            replications with num_id= 6
                            replications with num_id= 6
                                                          and num_pc= 2 : 14.6749267993
Average wait time over
                        10
                            replications with num_id= 6
                                                          and num_pc=3:14.6634043898
Average wait time over
                        10
                                                          and num_pc = 4 : 14.4908967796
                            replications with num_id= 6
Average wait time over
                        10
Average wait time over
                        10
                            replications with num_id= 6
                                                          and num_pc= 5 : 14.2116574571
Average wait time over
                        10
                            replications with num_id= 6
                                                          and num_pc= 6 : 13.8683966234
                            replications with num_id= 6
                                                          and num_pc = 7 : 13.4864336733
Average wait time over
                        10
                                                          and num_pc = 8 : 13.1039662177
Average wait time over
                        10
                            replications with num_id= 6
                        10
                            replications with num_id= 6
                                                          and num_pc=9:12.7242905693
Average wait time over
Average wait time over
                        10
                            replications with num_id= 7
                                                          and num_pc = 1 : 12.6630253373
                                                          and num_pc= 2 : 12.8059257652
                        10
                            replications with num_id= 7
Average wait time over
                            replications with num id= 7
                                                          and num pc= 3 : 12.8394084524
Average wait time over
                        10
Average wait time over
                        10
                            replications with num id= 7
                                                          and num pc= 4 : 12.7483292866
Average wait time over
                            replications with num id= 7
                                                          and num pc= 5 : 12.5540425252
                            replications with num_id= 7
                                                          and num_pc= 6 : 12.2990141909
Average wait time over
                        10
Average wait time over
                        10
                            replications with num_id= 7
                                                          and num_pc = 7 : 12.0254904144
                            replications with num_id= 7
                                                          and num_pc= 8 : 11.7413435523
Average wait time over
                        10
Average wait time over
                        10
                            replications with num_id= 7
                                                          and num_pc= 9 : 11.470877571
                                                          and num_pc= 1 : 11.4214654186
                            replications with num_id= 8
Average wait time over
                        10
                                                          and num_pc= 2 : 11.5412133581
Average wait time over
                        10
                            replications with num_id= 8
Average wait time over
                            replications with num_id= 8
                                                          and num_pc= 3 : 11.5738059085
                                                          and num_pc = 4 : 11.5425982138
Average wait time over
                        10
                            replications with num_id= 8
                        10
                            replications with num_id= 8
                                                          and num_pc= 5 : 11.431127783
Average wait time over
                        10
                            replications with num_id= 8
                                                          and num_pc= 6 : 11.2513691014
Average wait time over
                            replications with num_id= 8
                                                          and num_pc = 7 : 11.0343546501
Average wait time over
                        10
```

```
replications with num_id= 8
                                                         and num_pc = 8 : 10.8085105122
Average wait time over
                        10
Average wait time over
                        10
                            replications with num_id= 8
                                                         and num_pc = 9 : 10.5893528995
                            replications with num_id= 9
                                                         and num_pc = 1 : 10.5726116305
Average wait time over
                        10
                            replications with num_id= 9
                                                         and num_pc= 2 : 10.677973346
Average wait time over
                        10
                            replications with num id= 9
Average wait time over
                        10
                                                         and num pc= 3 : 10.7177820643
                            replications with num id= 9
                                                         and num pc = 4 : 10.6914793823
Average wait time over
Average wait time over
                            replications with num id= 9
                                                         and num pc= 5 : 10.6088982025
Average wait time over
                        10
                            replications with num id= 9
                                                         and num_pc = 6 : 10.4803032225
                            replications with num id= 9
                                                         and num pc= 7 : 10.3146144141
Average wait time over
                        10
Average wait time over
                        10
                            replications with num_id= 9
                                                         and num_pc= 8 : 10.134287626
                                                         and num_pc = 9 : 9.95585675125
                            replications with num_id= 9
Average wait time over
                        10
In [15]: #Do the same as above but with the passenger arrival rate of 50 instead of 5
         TOTAL_WAIT=[]
         for num_id in range(20,40):
             for num_pc in range(20,40):
                 reps=[]
                 for i in range(REPLICATIONS):
                     random.seed(RANDOM_SEED)
                                               # This helps reproducing the results
                     env = simpy.Environment()
                     env.process(setup(env, num_id, MU_2, 0.02, num_pc, MIN_PC, MAX_PC))
                     env.run(until=SIM TIME)
                     reps.append(np.mean(TOTAL_WAIT))
                 print('Average wait time over ', REPLICATIONS, ' replications with num id=',
                       num_id, " and num_pc=", num_pc, ":", np.mean(reps))
                           replications with num_id= 20
                                                         and num pc= 20 : 27.0983600861
Average wait time over 5
                           replications with num_id= 20
                                                         and num_pc= 21 : 24.6715140189
Average wait time over
                           replications with num_id= 20
                                                         and num pc= 22 : 24.2441508481
Average wait time over
Average wait time over
                           replications with num_id= 20
                                                         and num_pc = 23 : 23.4947245061
                           replications with num_id= 20
                                                         and num_pc = 24 : 23.4004827367
Average wait time over 5
Average wait time over 5
                           replications with num_id= 20
                                                         and num_pc= 25 : 23.6365827429
                        5
                           replications with num_id= 20
                                                         and num_pc= 26 : 23.680136894
Average wait time over
Average wait time over 5
                                                         and num_pc = 27 : 23.5650581524
                           replications with num_id= 20
Average wait time over 5
                           replications with num_id= 20
                                                         and num_pc= 28 : 23.1972113687
                                                         and num_pc= 29 : 23.2234931525
                        5
                           replications with num_id= 20
Average wait time over
                           replications with num_id= 20
                                                         and num_pc= 30 : 23.035271559
Average wait time over
Average wait time over 5
                           replications with num id= 20
                                                         and num pc= 31 : 23.1343926179
                           replications with num_id= 20
                                                         and num_pc= 32 : 23.2634235325
Average wait time over
Average wait time over
                        5
                           replications with num id= 20
                                                         and num pc= 33 : 23.3967426204
                           replications with num_id= 20
                                                         and num_pc = 34 : 23.438824033
Average wait time over 5
                           replications with num id= 20
                                                         and num pc= 35 : 23.5073329559
Average wait time over 5
                                                         and num_pc=36:23.4701869071
                           replications with num_id= 20
Average wait time over
                        5
                           replications with num id= 20
                                                         and num pc= 37 : 23.3156690976
Average wait time over
Average wait time over
                        5
                           replications with num_id= 20
                                                         and num_pc= 38 : 23.3585832113
                           replications with num_id= 20
                                                         and num_pc= 39 : 23.4011274188
Average wait time over
                                                         and num_pc= 20 : 23.3045938305
                           replications with num_id= 21
Average wait time over
                        5
```

```
Average wait time over
                        5
                           replications with num_id= 21
                                                          and num_pc= 21 : 23.3334054555
Average wait time over
                           replications with num_id= 21
                                                          and num_pc= 22 : 23.3796679947
                           replications with num_id= 21
                                                          and num_pc = 23 : 23.4059489227
Average wait time over
                                                          and num_pc= 24 : 23.2188125683
                           replications with num_id= 21
Average wait time over
Average wait time over
                           replications with num id= 21
                                                          and num pc= 25 : 23.2683661835
                                                          and num pc= 26 : 23.3588290015
Average wait time over
                           replications with num_id= 21
                           replications with num id= 21
                                                          and num pc= 27 : 23.316656013
Average wait time over
Average wait time over
                        5
                           replications with num_id= 21
                                                          and num_pc= 28 : 23.3103796555
                                                          and num pc= 29 : 23.3362462643
Average wait time over
                           replications with num_id= 21
                        5
Average wait time over
                        5
                           replications with num_id= 21
                                                          and num_pc= 30 : 23.3988097886
                                                          and num_pc= 31 : 23.3447697923
                           replications with num_id= 21
Average wait time over
                                                          and num_pc= 32 : 23.248103658
Average wait time over
                           replications with num_id= 21
                                                          and num_pc= 33 : 23.2145478231
Average wait time over
                        5
                           replications with num_id= 21
                           replications with num_id= 21
                                                          and num_pc= 34 : 23.2279691905
Average wait time over
Average wait time over
                        5
                           replications with num_id= 21
                                                          and num_pc= 35 : 23.2083091538
Average wait time over
                                                          and num_pc= 36 : 23.1930860591
                           replications with num_id= 21
                        5
                           replications with num_id= 21
                                                          and num_pc = 37 : 23.1491455769
Average wait time over
                                                          and num_pc = 38 : 23.0678429275
Average wait time over
                        5
                           replications with num_id= 21
                                                          and num_pc= 39 : 23.1008536971
Average wait time over
                        5
                           replications with num_id= 21
                           replications with num id= 22
                                                          and num pc= 20 : 23.0805337699
Average wait time over
                        5
Average wait time over
                           replications with num id= 22
                                                          and num pc= 21 : 23.1050027347
                                                          and num pc= 22 : 23.0751595102
Average wait time over
                        5
                           replications with num id= 22
Average wait time over
                           replications with num_id= 22
                                                          and num_pc= 23 : 23.0808380888
Average wait time over
                        5
                           replications with num_id= 22
                                                          and num_pc= 24 : 23.0642174663
                           replications with num_id= 22
                                                          and num_pc= 25 : 23.0062820893
Average wait time over
                           replications with num_id= 22
                                                          and num_pc= 26 : 22.9987711901
Average wait time over
                                                          and num_pc = 27 : 22.9498183618
Average wait time over
                           replications with num_id= 22
                        5
Average wait time over
                           replications with num_id= 22
                                                          and num_pc= 28 : 22.9377935261
                                                          and num_pc= 29 : 22.8480283222
                           replications with num_id= 22
Average wait time over
                           replications with num_id= 22
                                                          and num_pc = 30 : 22.8007617328
Average wait time over
                                                          and num_pc = 31 : 22.7507281683
Average wait time over
                        5
                           replications with num_id= 22
                                                          and num_pc= 32 : 22.7552348012
                        5
                           replications with num_id= 22
Average wait time over
Average wait time over
                        5
                           replications with num_id= 22
                                                          and num_pc= 33 : 22.7171164828
                                                          and num_pc= 34 : 22.6595952545
                        5
                           replications with num_id= 22
Average wait time over
                           replications with num id= 22
                                                          and num pc= 35 : 22.6044520684
Average wait time over
Average wait time over
                        5
                           replications with num id= 22
                                                          and num pc= 36 : 22.5925563541
Average wait time over
                           replications with num id= 22
                                                          and num pc= 37 : 22.5681655277
                           replications with num_id= 22
                                                          and num_pc= 38 : 22.4765805217
Average wait time over
                        5
                                                          and num_pc = 39 : 22.4505570922
Average wait time over
                           replications with num_id= 22
                        5
                           replications with num_id= 23
                                                          and num_pc= 20 : 22.4400812545
Average wait time over
                                                          and num_pc= 21 : 22.3817277654
Average wait time over
                        5
                           replications with num_id= 23
                                                          and num_pc= 22 : 22.330936651
                           replications with num_id= 23
Average wait time over
                           replications with num_id= 23
                                                          and num_pc= 23 : 22.2710782796
Average wait time over
                        5
Average wait time over
                           replications with num_id= 23
                                                          and num_pc= 24 : 22.2427962451
                        5
                           replications with num_id= 23
                                                          and num_pc= 25 : 22.222031126
Average wait time over
                           replications with num_id= 23
                                                          and num_pc= 26 : 22.1893228924
Average wait time over
                        5
                           replications with num_id= 23
                                                          and num_pc= 27 : 22.1608378036
Average wait time over
                           replications with num_id= 23
                                                          and num_pc= 28 : 22.1609808101
Average wait time over
```

```
Average wait time over
                        5
                           replications with num_id= 23
                                                          and num_pc= 29 : 22.1014789322
Average wait time over
                           replications with num_id= 23
                                                          and num_pc = 30 : 22.0451137445
                           replications with num_id= 23
                                                          and num_pc= 31 : 22.0131131904
Average wait time over
                                                          and num_pc= 32 : 21.9875053189
                           replications with num_id= 23
Average wait time over
Average wait time over
                           replications with num id= 23
                                                          and num pc= 33 : 21.9445865388
                                                          and num pc= 34 : 21.9200087985
Average wait time over
                           replications with num id= 23
                           replications with num id= 23
                                                          and num pc= 35 : 21.8860978105
Average wait time over
Average wait time over
                        5
                           replications with num_id= 23
                                                          and num_pc= 36 : 21.8438415043
                                                          and num pc= 37 : 21.7753112392
Average wait time over
                           replications with num_id= 23
                        5
Average wait time over
                        5
                           replications with num_id= 23
                                                          and num_pc= 38 : 21.7430756966
                                                          and num_pc= 39 : 21.7256116561
                           replications with num_id= 23
Average wait time over
                                                          and num_pc= 20 : 21.6823136411
Average wait time over
                           replications with num_id= 24
                                                          and num_pc= 21 : 21.6746683171
Average wait time over
                        5
                           replications with num_id= 24
                                                          and num_pc= 22 : 21.6591305578
                           replications with num_id= 24
Average wait time over
Average wait time over
                        5
                           replications with num_id= 24
                                                          and num_pc = 23 : 21.655403524
Average wait time over
                                                          and num_pc= 24 : 21.6525058069
                           replications with num_id= 24
                        5
                           replications with num_id= 24
                                                          and num_pc = 25 : 21.6230023107
Average wait time over
                                                          and num_pc= 26 : 21.5963866303
Average wait time over
                        5
                           replications with num_id= 24
                           replications with num_id= 24
                                                          and num_pc= 27 : 21.559509991
Average wait time over
                        5
                           replications with num id= 24
                                                          and num pc= 28 : 21.521307219
Average wait time over
                        5
                                                          and num pc= 29 : 21.5239500831
Average wait time over
                           replications with num id= 24
Average wait time over
                        5
                           replications with num id= 24
                                                          and num pc= 30 : 21.4903795179
Average wait time over
                           replications with num_id= 24
                                                          and num_pc= 31 : 21.446197386
                                                          and num_pc = 32 : 21.3930530442
Average wait time over
                        5
                           replications with num_id= 24
                           replications with num_id= 24
                                                          and num_pc= 33 : 21.3656656699
Average wait time over
                           replications with num_id= 24
                                                          and num_pc= 34 : 21.3339562624
Average wait time over
                                                          and num_pc = 35 : 21.3084722132
Average wait time over
                           replications with num_id= 24
                        5
Average wait time over
                           replications with num_id= 24
                                                          and num_pc= 36 : 21.2711444719
                                                          and num_pc= 37 : 21.2246929902
                           replications with num_id= 24
Average wait time over
                           replications with num_id= 24
                                                          and num_pc= 38 : 21.1785725558
Average wait time over
                                                          and num_pc= 39 : 21.1729538231
Average wait time over
                        5
                           replications with num_id= 24
                        5
                           replications with num_id= 25
                                                          and num_pc = 20 : 21.155393537
Average wait time over
Average wait time over
                        5
                           replications with num_id= 25
                                                          and num_pc= 21 : 21.1291893039
                                                          and num_pc= 22 : 21.1019961017
                        5
                           replications with num_id= 25
Average wait time over
                           replications with num id= 25
                                                          and num pc= 23 : 21.1017888354
Average wait time over
Average wait time over
                        5
                           replications with num id= 25
                                                          and num pc= 24 : 21.084172553
Average wait time over
                           replications with num id= 25
                                                          and num pc= 25 : 21.0423934578
                           replications with num_id= 25
                                                          and num_pc= 26 : 20.9985163342
Average wait time over
                        5
                                                          and num_pc = 27 : 20.9264487124
Average wait time over
                           replications with num_id= 25
                        5
                           replications with num_id= 25
                                                          and num_pc= 28 : 20.8677088337
Average wait time over
                                                          and num_pc= 29 : 20.8122241161
Average wait time over
                        5
                           replications with num_id= 25
                                                          and num_pc = 30 : 20.7771230115
                           replications with num_id= 25
Average wait time over
                           replications with num_id= 25
                                                          and num_pc= 31 : 20.7536521535
Average wait time over
                        5
Average wait time over
                           replications with num_id= 25
                                                          and num_pc= 32 : 20.7115827127
                        5
                           replications with num_id= 25
                                                          and num_pc = 33 : 20.6424420091
Average wait time over
                           replications with num_id= 25
                                                          and num_pc = 34 : 20.6041456828
Average wait time over
                        5
                           replications with num_id= 25
                                                          and num_pc= 35 : 20.5859233329
Average wait time over
                           replications with num_id= 25
                                                          and num_pc= 36 : 20.5685520003
Average wait time over
```

```
Average wait time over
                        5
                           replications with num_id= 25
                                                          and num_pc= 37 : 20.5420515981
Average wait time over
                           replications with num_id= 25
                                                          and num_pc= 38 : 20.5180139665
                           replications with num_id= 25
                                                          and num_pc = 39 : 20.5034706514
Average wait time over
                        5
                                                          and num_pc= 20 : 20.5015383311
                        5
                           replications with num_id= 26
Average wait time over
Average wait time over
                           replications with num id= 26
                                                          and num pc= 21 : 20.4739061078
                                                          and num pc= 22 : 20.4418718139
Average wait time over
                           replications with num_id= 26
                           replications with num id= 26
                                                          and num pc= 23 : 20.4320167488
Average wait time over
Average wait time over
                        5
                           replications with num_id= 26
                                                          and num_pc= 24 : 20.4204141465
Average wait time over
                           replications with num_id= 26
                                                          and num_pc= 25 : 20.3946834665
                        5
Average wait time over
                        5
                           replications with num_id= 26
                                                          and num_pc= 26 : 20.3644111507
                                                          and num_pc = 27 : 20.3259020243
                           replications with num_id= 26
Average wait time over
                        5
                                                          and num_pc= 28 : 20.3120048943
Average wait time over
                           replications with num_id= 26
                                                          and num_pc= 29 : 20.2852412301
Average wait time over
                        5
                           replications with num_id= 26
                           replications with num_id= 26
                                                          and num_pc= 30 : 20.2415193163
Average wait time over
Average wait time over
                        5
                           replications with num_id= 26
                                                          and num_pc= 31 : 20.2123781583
Average wait time over
                                                          and num_pc = 32 : 20.2070382736
                           replications with num_id= 26
                        5
                           replications with num_id= 26
                                                          and num_pc= 33 : 20.1697162461
Average wait time over
                                                          and num_pc = 34 : 20.1347955886
Average wait time over
                        5
                           replications with num_id= 26
                                                          and num_pc= 35 : 20.0818716405
Average wait time over
                        5
                           replications with num_id= 26
                           replications with num id= 26
                                                          and num pc= 36 : 20.0408625913
Average wait time over
                        5
                                                          and num pc= 37 : 20.0146406017
Average wait time over
                           replications with num id= 26
                        5
                           replications with num id= 26
                                                          and num pc= 38 : 19.9694255872
Average wait time over
Average wait time over
                           replications with num_id= 26
                                                          and num_pc= 39 : 19.9403774141
Average wait time over
                        5
                           replications with num_id= 27
                                                          and num_pc= 20 : 19.9136882689
                           replications with num_id= 27
                                                          and num_pc= 21 : 19.8958291494
Average wait time over
                        5
                           replications with num_id= 27
                                                          and num_pc= 22 : 19.8655490058
Average wait time over
                                                          and num_pc= 23 : 19.8301915275
Average wait time over
                           replications with num_id= 27
                        5
Average wait time over
                           replications with num_id= 27
                                                          and num_pc= 24 : 19.8017132488
                           replications with num_id= 27
                                                          and num_pc= 25 : 19.7665464342
Average wait time over
                           replications with num_id= 27
                                                          and num_pc= 26 : 19.7335121751
Average wait time over
                                                          and num_pc = 27 : 19.703309562
Average wait time over
                        5
                           replications with num_id= 27
                        5
                           replications with num_id= 27
                                                          and num_pc= 28 : 19.6834725678
Average wait time over
Average wait time over
                        5
                           replications with num_id= 27
                                                          and num_pc= 29 : 19.6525768352
                                                          and num_pc= 30 : 19.6059459063
                        5
                           replications with num_id= 27
Average wait time over
                           replications with num id= 27
                                                          and num pc= 31 : 19.5740017353
Average wait time over
Average wait time over
                        5
                           replications with num id= 27
                                                          and num pc= 32 : 19.5347762975
                           replications with num id= 27
                                                          and num pc= 33 : 19.5107378835
Average wait time over
                           replications with num_id= 27
                                                          and num_pc= 34 : 19.4970651551
Average wait time over
                        5
                                                          and num_pc= 35 : 19.4557974774
                        5
                           replications with num_id= 27
Average wait time over
                        5
                           replications with num_id= 27
                                                          and num_pc= 36 : 19.4258482289
Average wait time over
                                                          and num_pc= 37 : 19.3937153873
Average wait time over
                        5
                           replications with num_id= 27
                                                          and num_pc= 38 : 19.3727063172
                           replications with num_id= 27
Average wait time over
                                                          and num_pc= 39 : 19.3391854918
Average wait time over
                        5
                           replications with num_id= 27
Average wait time over
                           replications with num_id= 28
                                                          and num_pc= 20 : 19.3109240745
                        5
                           replications with num_id= 28
                                                          and num_pc= 21 : 19.2944676078
Average wait time over
                           replications with num_id= 28
                                                          and num_pc= 22 : 19.2617372804
Average wait time over
                        5
                           replications with num_id= 28
                                                          and num_pc= 23 : 19.2337774708
Average wait time over
                           replications with num_id= 28
                                                          and num_pc= 24 : 19.1960164701
Average wait time over
```

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Average wait time over
                        5
                           replications with num_id= 28
                                                          and num_pc= 25 : 19.1561153799
Average wait time over
                           replications with num_id= 28
                                                          and num_pc= 26 : 19.1302112723
                           replications with num_id= 28
                                                          and num_pc= 27 : 19.1133241221
Average wait time over
                                                          and num_pc= 28 : 19.0787076947
                           replications with num_id= 28
Average wait time over
Average wait time over
                           replications with num id= 28
                                                          and num pc= 29 : 19.0396136795
                                                          and num pc= 30 : 18.9986180113
Average wait time over
                           replications with num id= 28
                           replications with num id= 28
                                                          and num pc= 31 : 18.9661261565
Average wait time over
Average wait time over
                        5
                           replications with num_id= 28
                                                          and num_pc= 32 : 18.933724324
                                                          and num pc= 33 : 18.8827884308
Average wait time over
                           replications with num_id= 28
Average wait time over
                        5
                           replications with num_id= 28
                                                          and num_pc= 34 : 18.853481718
                           replications with num_id= 28
                                                          and num_pc = 35 : 18.8207423763
Average wait time over
                                                          and num_pc= 36 : 18.7917620781
Average wait time over
                           replications with num_id= 28
                                                          and num_pc= 37 : 18.7582227464
Average wait time over
                        5
                           replications with num_id= 28
                           replications with num_id= 28
                                                          and num_pc= 38 : 18.708571072
Average wait time over
Average wait time over
                        5
                           replications with num_id= 28
                                                          and num_pc = 39 : 18.6607705543
Average wait time over
                                                          and num_pc = 20 : 18.6343779252
                           replications with num_id= 29
                        5
                           replications with num_id= 29
                                                          and num_pc= 21 : 18.606145659
Average wait time over
                                                          and num_pc= 22 : 18.588959098
Average wait time over
                        5
                           replications with num_id= 29
                                                          and num_pc= 23 : 18.575426849
Average wait time over
                        5
                           replications with num_id= 29
                           replications with num id= 29
                                                          and num pc= 24 : 18.5640195862
Average wait time over
                        5
Average wait time over
                           replications with num id= 29
                                                          and num pc= 25 : 18.5308860704
                        5
                           replications with num id= 29
                                                          and num pc= 26 : 18.5074265294
Average wait time over
Average wait time over
                           replications with num_id= 29
                                                          and num_pc= 27 : 18.4707440255
Average wait time over
                        5
                           replications with num_id= 29
                                                          and num pc= 28 : 18.4419737046
                           replications with num_id= 29
                                                          and num_pc= 29 : 18.4173147091
Average wait time over
                           replications with num_id= 29
                                                          and num_pc= 30 : 18.3892125268
Average wait time over
                                                          and num_pc= 31 : 18.3755771884
Average wait time over
                           replications with num_id= 29
                        5
Average wait time over
                           replications with num_id= 29
                                                          and num_pc= 32 : 18.3329177962
                           replications with num_id= 29
                                                          and num_pc= 33 : 18.3010654924
Average wait time over
                           replications with num_id= 29
                                                          and num_pc= 34 : 18.2807021386
Average wait time over
                                                          and num_pc = 35 : 18.2528807027
Average wait time over
                        5
                           replications with num_id= 29
                        5
                           replications with num_id= 29
                                                          and num_pc= 36 : 18.2183883772
Average wait time over
Average wait time over
                        5
                           replications with num_id= 29
                                                          and num_pc= 37 : 18.1936795379
                                                          and num_pc= 38 : 18.1488679785
                        5
                           replications with num_id= 29
Average wait time over
                           replications with num id= 29
                                                          and num pc= 39 : 18.1141125306
Average wait time over
Average wait time over
                        5
                           replications with num id= 30
                                                          and num pc= 20 : 18.1026136923
                           replications with num id= 30
                                                          and num pc= 21 : 18.0761775862
Average wait time over
                           replications with num_id= 30
                                                          and num_pc= 22 : 18.0574437844
Average wait time over
                        5
                                                          and num_pc= 23 : 18.0436783858
Average wait time over
                           replications with num_id= 30
                        5
                           replications with num_id= 30
                                                          and num_pc= 24 : 18.0079773369
Average wait time over
                                                          and num_pc= 25 : 17.9985620673
Average wait time over
                        5
                           replications with num_id= 30
                                                          and num_pc= 26 : 17.9812733889
                           replications with num_id= 30
Average wait time over
                           replications with num_id= 30
                                                          and num_pc= 27 : 17.9617425642
Average wait time over
                        5
Average wait time over
                           replications with num_id= 30
                                                          and num_pc= 28 : 17.9403830989
                        5
                           replications with num_id= 30
                                                          and num_pc = 29 : 17.903743526
Average wait time over
                           replications with num_id= 30
                                                          and num_pc = 30 : 17.8628023103
Average wait time over
                        5
                           replications with num_id= 30
                                                          and num_pc= 31 : 17.8213103395
Average wait time over
                           replications with num_id= 30
                                                          and num_pc= 32 : 17.7733930336
Average wait time over
```

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Average wait time over
                        5
                           replications with num_id= 30
                                                          and num_pc= 33 : 17.7342110025
Average wait time over
                           replications with num_id= 30
                                                          and num_pc = 34 : 17.7029306379
                           replications with num_id= 30
                                                          and num_pc = 35 : 17.6740691969
Average wait time over
                                                          and num_pc = 36 : 17.6549527179
                           replications with num_id= 30
Average wait time over
Average wait time over
                           replications with num id= 30
                                                          and num pc= 37 : 17.6305801457
                                                          and num pc= 38 : 17.6007068019
Average wait time over
                           replications with num id= 30
                           replications with num id= 30
                                                          and num pc= 39 : 17.572518585
Average wait time over
Average wait time over
                        5
                           replications with num_id= 31
                                                          and num_pc= 20 : 17.5368869189
                           replications with num_id= 31
                                                          and num_pc= 21 : 17.5110586509
Average wait time over
Average wait time over
                        5
                           replications with num_id= 31
                                                          and num_pc= 22 : 17.4945240867
                           replications with num_id= 31
                                                          and num_pc= 23 : 17.4642131081
Average wait time over
                                                          and num_pc= 24 : 17.439875632
Average wait time over
                           replications with num_id= 31
                                                          and num_pc= 25 : 17.4168252904
Average wait time over
                        5
                           replications with num_id= 31
                           replications with num_id= 31
                                                          and num_pc= 26 : 17.395900705
Average wait time over
Average wait time over
                        5
                           replications with num_id= 31
                                                          and num_pc = 27 : 17.3614607758
Average wait time over
                                                          and num_pc= 28 : 17.3202597498
                           replications with num_id= 31
                        5
                           replications with num_id= 31
                                                          and num_pc= 29 : 17.2789732222
Average wait time over
                                                          and num_pc = 30 : 17.2427029834
Average wait time over
                        5
                           replications with num_id= 31
                                                          and num_pc= 31 : 17.2135933076
Average wait time over
                        5
                           replications with num_id= 31
                           replications with num id= 31
                                                          and num pc= 32 : 17.1782137314
Average wait time over
                        5
Average wait time over
                           replications with num id= 31
                                                          and num pc= 33 : 17.1416389026
                        5
                           replications with num id= 31
                                                          and num pc= 34 : 17.1119449687
Average wait time over
Average wait time over
                           replications with num_id= 31
                                                          and num_pc= 35 : 17.0771977839
Average wait time over
                        5
                           replications with num_id= 31
                                                          and num_pc= 36 : 17.037793326
                           replications with num_id= 31
                                                          and num_pc= 37 : 16.998773281
Average wait time over
                           replications with num_id= 31
                                                          and num_pc= 38 : 16.9776132068
Average wait time over
                                                          and num_pc = 39 : 16.9552494003
Average wait time over
                           replications with num_id= 31
                        5
Average wait time over
                           replications with num_id= 32
                                                          and num_pc= 20 : 16.9229444082
                           replications with num_id= 32
                                                          and num_pc= 21 : 16.8938015655
Average wait time over
                           replications with num_id= 32
                                                          and num_pc= 22 : 16.8645251297
Average wait time over
Average wait time over
                                                          and num_pc = 23 : 16.8394660555
                        5
                           replications with num_id= 32
                        5
                           replications with num_id= 32
                                                          and num_pc= 24 : 16.8136932787
Average wait time over
Average wait time over
                        5
                           replications with num_id= 32
                                                          and num_pc = 25 : 16.7865005374
                                                          and num_pc= 26 : 16.7681205855
                        5
                           replications with num_id= 32
Average wait time over
                           replications with num id= 32
                                                          and num pc= 27 : 16.7357948208
Average wait time over
Average wait time over
                        5
                           replications with num id= 32
                                                          and num pc= 28 : 16.712011993
                           replications with num id= 32
                                                          and num pc= 29 : 16.6757299082
Average wait time over
                                                          and num_pc= 30 : 16.6508186945
                           replications with num_id= 32
Average wait time over
                        5
                                                          and num_pc= 31 : 16.619716939
                           replications with num_id= 32
Average wait time over
                        5
                           replications with num_id= 32
                                                          and num_pc= 32 : 16.5835562633
Average wait time over
                                                          and num_pc = 33 : 16.5497371707
Average wait time over
                        5
                           replications with num_id= 32
                                                          and num_pc= 34 : 16.5252348405
                           replications with num_id= 32
Average wait time over
                                                          and num_pc = 35 : 16.4990741191
Average wait time over
                        5
                           replications with num_id= 32
Average wait time over
                           replications with num_id= 32
                                                          and num_pc= 36 : 16.4667095409
                        5
                           replications with num_id= 32
                                                          and num_pc = 37 : 16.422656763
Average wait time over
                           replications with num_id= 32
                                                          and num_pc= 38 : 16.3843811493
Average wait time over
                        5
                           replications with num_id= 32
                                                          and num_pc= 39 : 16.350837696
Average wait time over
                           replications with num_id= 33
                                                          and num_pc= 20 : 16.3313636109
Average wait time over
```

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Average wait time over
                        5
                           replications with num_id= 33
                                                          and num_pc= 21 : 16.3126784869
Average wait time over
                           replications with num_id= 33
                                                          and num_pc= 22 : 16.2895430918
                           replications with num_id= 33
                                                          and num_pc= 23 : 16.2713594834
Average wait time over
                        5
                                                          and num_pc= 24 : 16.2531199964
                        5
                           replications with num_id= 33
Average wait time over
Average wait time over
                           replications with num id= 33
                                                          and num pc= 25 : 16.2258233011
                                                          and num pc= 26 : 16.1931907087
Average wait time over
                           replications with num id= 33
                           replications with num id= 33
                                                          and num pc= 27 : 16.1677668907
Average wait time over
Average wait time over
                        5
                           replications with num_id= 33
                                                          and num_pc= 28 : 16.1421996695
Average wait time over
                           replications with num_id= 33
                                                          and num_pc= 29 : 16.1126318957
                        5
Average wait time over
                        5
                           replications with num_id= 33
                                                          and num_pc = 30 : 16.0902074486
                           replications with num_id= 33
                                                          and num_pc= 31 : 16.0713888912
Average wait time over
                        5
                                                          and num_pc= 32 : 16.0459326807
Average wait time over
                           replications with num_id= 33
                                                          and num_pc= 33 : 16.0203201406
Average wait time over
                        5
                           replications with num_id= 33
                           replications with num_id= 33
                                                          and num_pc= 34 : 16.000702813
Average wait time over
Average wait time over
                        5
                           replications with num_id= 33
                                                          and num_pc= 35 : 15.9609283812
Average wait time over
                                                          and num_pc= 36 : 15.9169977726
                           replications with num_id= 33
                        5
                           replications with num_id= 33
                                                          and num_pc = 37 : 15.8757734243
Average wait time over
                                                          and num_pc= 38 : 15.8406394935
Average wait time over
                        5
                           replications with num_id= 33
                           replications with num_id= 33
                                                          and num_pc= 39 : 15.810926311
Average wait time over
                        5
                           replications with num id= 34
                                                          and num pc= 20 : 15.7856796893
Average wait time over
                        5
Average wait time over
                           replications with num id= 34
                                                          and num pc= 21 : 15.7628239347
                                                          and num pc= 22 : 15.7461136432
                        5
                           replications with num id= 34
Average wait time over
Average wait time over
                           replications with num_id= 34
                                                          and num_pc= 23 : 15.7225073524
Average wait time over
                        5
                           replications with num_id= 34
                                                          and num_pc= 24 : 15.7018309084
                           replications with num_id= 34
                                                          and num_pc= 25 : 15.6786593369
Average wait time over
                        5
                           replications with num_id= 34
                                                          and num_pc= 26 : 15.6617786721
Average wait time over
                                                          and num_pc = 27 : 15.635198351
Average wait time over
                           replications with num_id= 34
                        5
Average wait time over
                           replications with num_id= 34
                                                          and num_pc= 28 : 15.6069437157
                           replications with num_id= 34
                                                          and num_pc= 29 : 15.5865343189
Average wait time over
                           replications with num_id= 34
                                                          and num_pc = 30 : 15.5614498313
Average wait time over
                                                          and num_pc= 31 : 15.5288203733
Average wait time over
                        5
                           replications with num_id= 34
                        5
                           replications with num_id= 34
                                                          and num_pc = 32 : 15.4945897037
Average wait time over
Average wait time over
                        5
                           replications with num_id= 34
                                                          and num_pc= 33 : 15.4664381428
                                                          and num_pc = 34 : 15.436894029
                        5
                           replications with num_id= 34
Average wait time over
                           replications with num id= 34
                                                          and num pc= 35 : 15.4030344096
Average wait time over
Average wait time over
                        5
                           replications with num id= 34
                                                          and num pc= 36 : 15.363886604
                           replications with num id= 34
                                                          and num pc= 37 : 15.328400457
Average wait time over
                           replications with num_id= 34
                                                          and num_pc= 38 : 15.3076872878
Average wait time over
                        5
                                                          and num_pc= 39 : 15.2799759665
                        5
                           replications with num_id= 34
Average wait time over
                        5
                           replications with num_id= 35
                                                          and num_pc= 20 : 15.2565522528
Average wait time over
                                                          and num_pc= 21 : 15.2361026832
Average wait time over
                        5
                           replications with num_id= 35
                                                          and num_pc= 22 : 15.2167048111
                           replications with num_id= 35
Average wait time over
                           replications with num_id= 35
                                                          and num_pc= 23 : 15.1907588155
Average wait time over
                        5
Average wait time over
                           replications with num_id= 35
                                                          and num_pc= 24 : 15.1725225131
                        5
                           replications with num_id= 35
                                                          and num_pc= 25 : 15.1452259519
Average wait time over
                           replications with num_id= 35
                                                          and num_pc= 26 : 15.1181550684
Average wait time over
                        5
                           replications with num_id= 35
                                                          and num_pc= 27 : 15.0963895533
Average wait time over
                           replications with num_id= 35
                                                          and num_pc= 28 : 15.0685708947
Average wait time over
```

```
and num_pc = 29 : 15.0405295258
Average wait time over
                        5
                           replications with num_id= 35
Average wait time over
                           replications with num_id= 35
                                                          and num_pc = 30 : 15.0111294853
                           replications with num_id= 35
                                                          and num_pc= 31 : 14.9797373981
Average wait time over
                        5
                                                          and num_pc= 32 : 14.9545247899
                        5
                           replications with num_id= 35
Average wait time over
Average wait time over
                           replications with num id= 35
                                                          and num pc= 33 : 14.9232842883
                                                          and num pc= 34 : 14.8901948735
Average wait time over
                           replications with num id= 35
                           replications with num id= 35
                                                          and num pc= 35 : 14.8625340637
Average wait time over
Average wait time over
                        5
                           replications with num_id= 35
                                                          and num_pc= 36 : 14.8360998464
                           replications with num_id= 35
                                                          and num pc= 37 : 14.8009567262
Average wait time over
                        5
Average wait time over
                        5
                           replications with num_id= 35
                                                          and num_pc= 38 : 14.7696092778
                           replications with num_id= 35
                                                          and num_pc = 39 : 14.7305173075
Average wait time over
                                                          and num_pc= 20 : 14.7139433891
Average wait time over
                           replications with num_id= 36
                                                          and num_pc= 21 : 14.6946133393
Average wait time over
                        5
                           replications with num_id= 36
                                                          and num_pc= 22 : 14.669369223
                           replications with num_id= 36
Average wait time over
Average wait time over
                        5
                           replications with num_id= 36
                                                          and num_pc = 23 : 14.6502042528
Average wait time over
                                                          and num_pc= 24 : 14.6236561191
                           replications with num_id= 36
                        5
                           replications with num_id= 36
                                                          and num_pc= 25 : 14.5962633613
Average wait time over
                                                          and num_pc = 26 : 14.574185935
Average wait time over
                        5
                           replications with num_id= 36
                                                          and num_pc= 27 : 14.5480466601
Average wait time over
                        5
                           replications with num_id= 36
                           replications with num id= 36
                                                          and num pc= 28 : 14.5205883238
Average wait time over
                        5
Average wait time over
                           replications with num id= 36
                                                          and num pc= 29 : 14.4987372008
                        5
                           replications with num id= 36
                                                          and num pc= 30 : 14.4836206648
Average wait time over
Average wait time over
                           replications with num_id= 36
                                                          and num_pc= 31 : 14.4605599984
                                                          and num_pc = 32 : 14.4323410953
Average wait time over
                        5
                           replications with num_id= 36
Average wait time over
                           replications with num_id= 36
                                                          and num_pc= 33 : 14.4015394457
                        5
                           replications with num_id= 36
                                                          and num_pc = 34 : 14.3660430743
Average wait time over
                                                          and num_pc= 35 : 14.3280492181
Average wait time over
                           replications with num_id= 36
                        5
Average wait time over
                           replications with num_id= 36
                                                          and num_pc= 36 : 14.2928185464
                                                          and num_pc= 37 : 14.2555793284
                           replications with num_id= 36
Average wait time over
                           replications with num_id= 36
                                                          and num_pc= 38 : 14.2256151588
Average wait time over
Average wait time over
                                                          and num_pc= 39 : 14.1932658986
                        5
                           replications with num_id= 36
                        5
                           replications with num_id= 37
                                                          and num_pc= 20 : 14.1638908983
Average wait time over
Average wait time over
                        5
                           replications with num_id= 37
                                                          and num_pc= 21 : 14.149947595
                                                          and num_pc= 22 : 14.1321241599
                        5
                           replications with num_id= 37
Average wait time over
                           replications with num id= 37
                                                          and num pc= 23 : 14.1099648772
Average wait time over
Average wait time over
                        5
                           replications with num id= 37
                                                          and num pc= 24 : 14.0875810522
                           replications with num id= 37
                                                          and num pc= 25 : 14.0644742574
Average wait time over
                           replications with num_id= 37
                                                          and num_pc= 26 : 14.04108899
Average wait time over
                        5
                        5
                           replications with num_id= 37
                                                          and num_pc= 27 : 14.0167979352
Average wait time over
                        5
                           replications with num_id= 37
                                                          and num_pc= 28 : 13.9935285152
Average wait time over
                                                          and num_pc= 29 : 13.9671207236
Average wait time over
                        5
                           replications with num_id= 37
                           replications with num_id= 37
                                                          and num_pc= 30 : 13.942224057
Average wait time over
                                                          and num_pc= 31 : 13.9135800256
Average wait time over
                        5
                           replications with num_id= 37
Average wait time over
                           replications with num_id= 37
                                                          and num_pc= 32 : 13.882653986
                                                          and num_pc= 33 : 13.8517300562
                        5
                           replications with num_id= 37
Average wait time over
                           replications with num_id= 37
                                                          and num_pc= 34 : 13.8264707597
Average wait time over
                        5
                           replications with num_id= 37
                                                          and num_pc= 35 : 13.7980185391
Average wait time over
                           replications with num_id= 37
                                                          and num_pc= 36 : 13.7757396833
Average wait time over
```

```
and num_pc= 37 : 13.7477627685
Average wait time over
                        5
                           replications with num_id= 37
Average wait time over
                           replications with num_id= 37
                                                          and num_pc= 38 : 13.7158168283
                           replications with num_id= 37
                                                          and num_pc = 39 : 13.6844606396
Average wait time over
                                                          and num_pc = 20 : 13.6594745495
Average wait time over
                           replications with num_id= 38
Average wait time over
                           replications with num id= 38
                                                          and num pc= 21 : 13.6428045264
                           replications with num id= 38
                                                          and num pc= 22 : 13.6264313178
Average wait time over
                           replications with num id= 38
                                                          and num pc= 23 : 13.6069755186
Average wait time over
Average wait time over
                        5
                           replications with num_id= 38
                                                          and num_pc= 24 : 13.5868823239
                                                          and num pc= 25 : 13.5643324839
Average wait time over
                           replications with num_id= 38
Average wait time over
                        5
                           replications with num_id= 38
                                                          and num_pc= 26 : 13.543689343
                                                          and num_pc= 27 : 13.522362385
                           replications with num_id= 38
Average wait time over
                                                          and num_pc= 28 : 13.4998710204
Average wait time over
                           replications with num_id= 38
                                                          and num_pc = 29 : 13.4781349847
Average wait time over
                        5
                           replications with num_id= 38
                           replications with num_id= 38
                                                          and num_pc= 30 : 13.460790531
Average wait time over
Average wait time over
                        5
                           replications with num_id= 38
                                                          and num_pc = 31 : 13.4393046666
Average wait time over
                                                          and num_pc = 32 : 13.4148320213
                           replications with num_id= 38
                        5
                           replications with num_id= 38
                                                          and num_pc = 33 : 13.3973814745
Average wait time over
                                                          and num_pc = 34 : 13.3698903478
Average wait time over
                        5
                           replications with num_id= 38
                           replications with num_id= 38
                                                          and num_pc= 35 : 13.3404689499
Average wait time over
                        5
                           replications with num id= 38
                                                          and num pc= 36 : 13.3153332236
Average wait time over
                        5
Average wait time over
                           replications with num id= 38
                                                          and num pc= 37 : 13.2889890123
Average wait time over
                           replications with num id= 38
                                                          and num pc= 38 : 13.2647634212
Average wait time over
                           replications with num_id= 38
                                                          and num_pc= 39 : 13.2435837515
                           replications with num_id= 39
Average wait time over
                        5
                                                          and num_pc= 20 : 13.2244284447
                           replications with num_id= 39
                                                          and num_pc= 21 : 13.2076003213
Average wait time over
                           replications with num_id= 39
                                                          and num_pc= 22 : 13.1887154064
Average wait time over
                                                          and num_pc = 23 : 13.1709570415
                           replications with num_id= 39
Average wait time over
                        5
Average wait time over
                           replications with num_id= 39
                                                          and num_pc= 24 : 13.1555231171
                                                          and num_pc= 25 : 13.1381529661
Average wait time over
                           replications with num_id= 39
                           replications with num_id= 39
                                                          and num_pc= 26 : 13.1163065216
Average wait time over
                           replications with num_id= 39
                                                          and num_pc = 27 : 13.0991492686
Average wait time over
                        5
                        5
                           replications with num_id= 39
                                                          and num_pc= 28 : 13.0789142385
Average wait time over
Average wait time over
                        5
                           replications with num_id= 39
                                                          and num_pc= 29 : 13.0570389921
                                                          and num_pc= 30 : 13.0368068443
Average wait time over
                        5
                           replications with num_id= 39
                                                          and num pc= 31 : 13.0135756211
                           replications with num id= 39
Average wait time over
Average wait time over
                        5
                           replications with num id= 39
                                                          and num pc= 32 : 12.9872564895
Average wait time over
                           replications with num id= 39
                                                          and num pc= 33 : 12.9600508022
                           replications with num_id= 39
                                                          and num_pc= 34 : 12.9372089177
Average wait time over
                        5
                                                          and num_pc = 35 : 12.913743339
Average wait time over
                        5
                           replications with num_id= 39
                        5
                           replications with num_id= 39
                                                          and num_pc= 36 : 12.8867530662
Average wait time over
                                                          and num_pc= 37 : 12.8563521226
Average wait time over
                        5
                           replications with num_id= 39
                           replications with num_id= 39
                                                          and num_pc= 38 : 12.8337899205
Average wait time over
                                                          and num_pc= 39 : 12.8047148237
                           replications with num_id= 39
Average wait time over
```