

$$\begin{aligned}
 \text{Poisson : } P(y, \lambda) &= \frac{\lambda^y \cdot e^{-\lambda}}{y!} \\
 &= \exp\left(\ln\left(\frac{\lambda^y \cdot e^{-\lambda}}{y!}\right)\right) \\
 &= \exp\left(\ln \lambda^y - \ln y! - \lambda\right) \\
 &= b(y) \exp\left[y^T T(y) - a(\eta)\right]
 \end{aligned}$$

$$\text{with } b(y) = 1 \quad a(\eta) = \lambda \quad \eta = 1$$

$$T(y) = \ln \lambda^y - \ln y!$$

T does not have this form in an exponential family. The $y!$ should be pulled out front into b