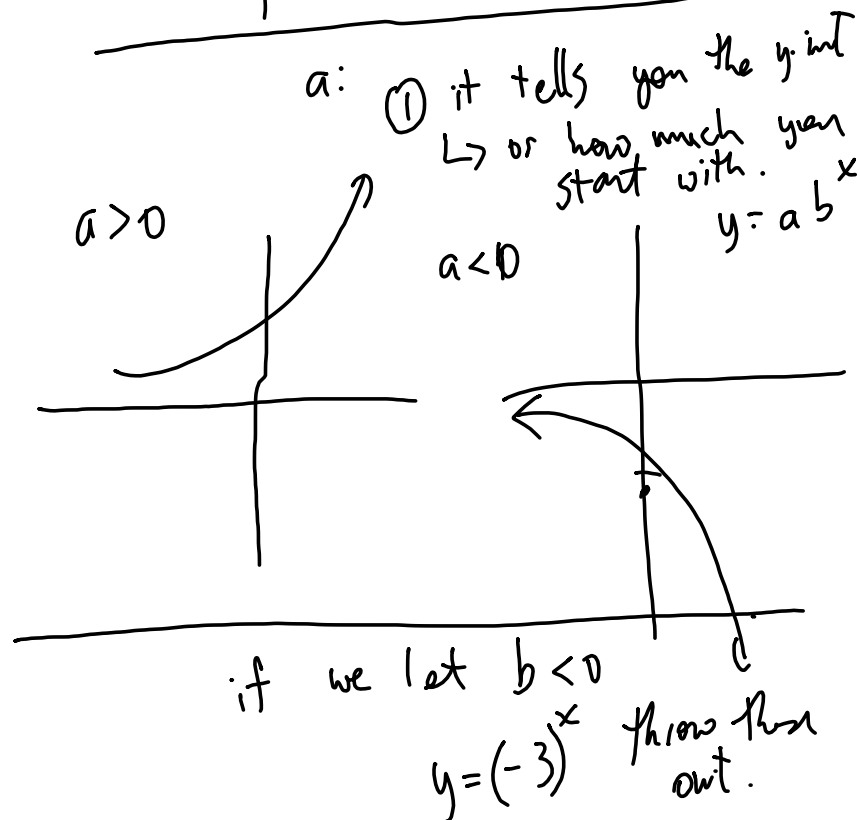
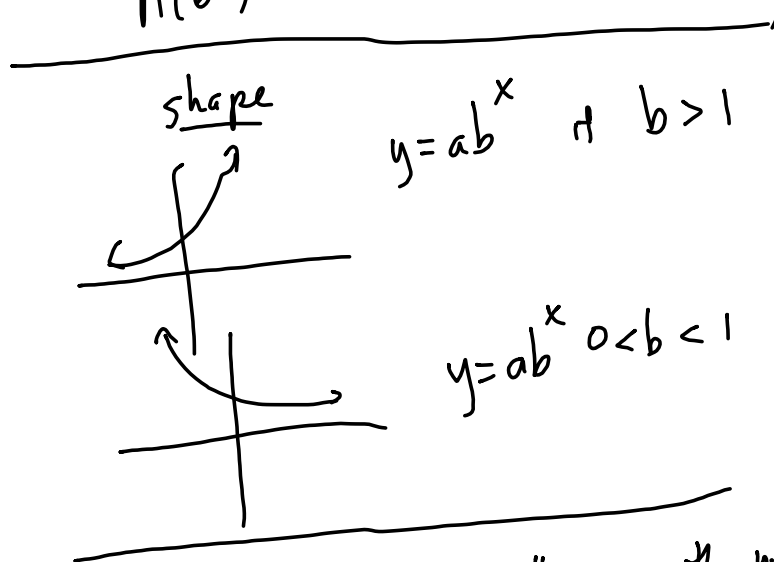


$A_0 = 10,000$  annual growth of 9%.

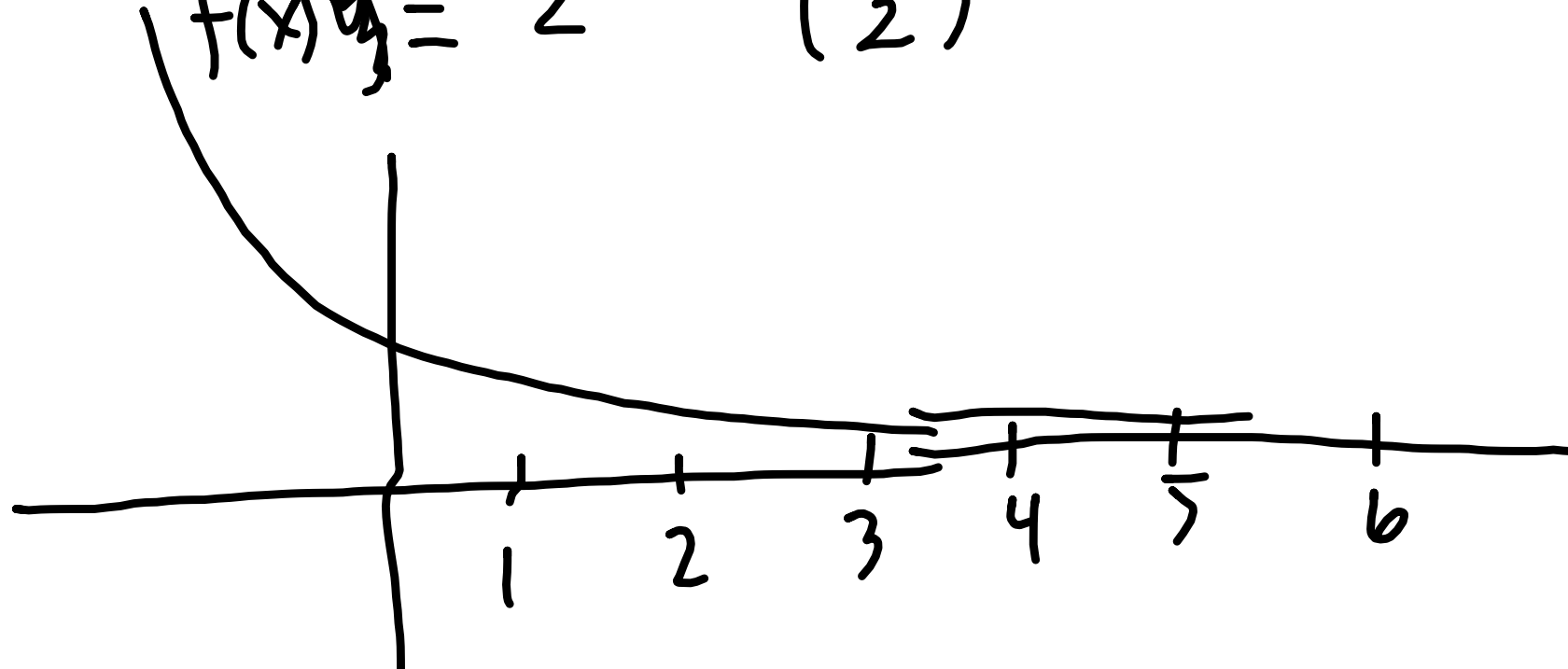
$$A_{65}$$

$$A(t) = 10,000 (1.09)^t$$

$$A(65) \approx 2.7 \times 10^6$$



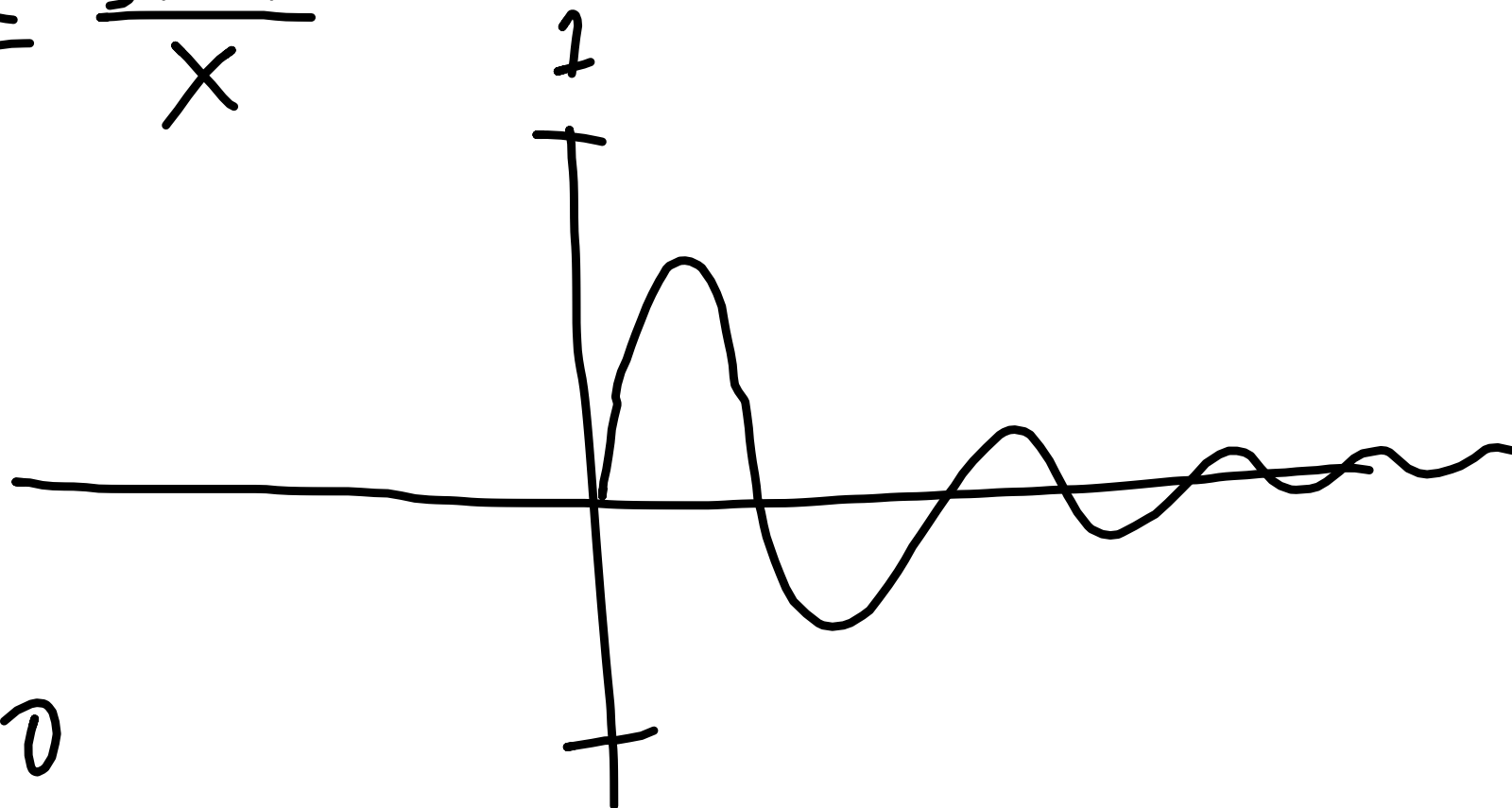
$$f(x) = 2^{-x} = \left(\frac{1}{2}\right)^x$$



$$\lim_{x \rightarrow \infty} f(x) = 0$$

$$\lim_{x \rightarrow -\infty} f(x) = +\infty$$

$$f(x) = \frac{\sin x}{x}$$



$$\lim_{x \rightarrow \infty} f(x) = 0$$

$$H.N. \quad y = 0$$

Ex  $A(t) = 100 (1.10)^t$

$$A(1) = 110$$

$$A(2) = 121 = 100 (1.10)(1.10)$$

$$A(3) = 100 (1.10)(1.10)(1.10)$$

if  $t$  is in years.

is compounding annually

---

ex \$100 to start at nominal rate  
of 10% compounded semiannually  
t

$$A(t) = 100 \left[ \left(1 + \frac{0.10}{2}\right) \left(1 + \frac{0.10}{2}\right) \right]$$
$$= 100 \left(1 + \frac{0.10}{2}\right)^{2t}$$

$$A(1) = 110.25$$

ex \$100. Nominal interest of  
10%  
(compounded monthly (like a mortgage))

$$A(t) = 100 \left( 1 + \frac{0.1}{12} \right)^{12t}$$

$$= 100 \left( 1 + \frac{0.1}{12} \right)^{12t}$$

$$A(1) = 110.47 \rightarrow \text{APR is } 10.47\%$$

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Generalize to compounding  $n$  times a  
year. at a nominal rate of  $r$ .

$$A(t) = A_0 \left( 1 + \frac{r}{n} \right)^{nt}$$

ex \$10,000 at birth you earn  
a nominal of 9% compounded daily.  
at age 65 how much do I have.

$$A(t) = 10,000 \left( 1 + \frac{0.09}{365} \right)^{365t}$$

$$A(65) = 10,000 \left( 1 + \frac{0.09}{365} \right)^{365(65)} \approx 3.47 \times 10^6$$