

1.

$$\sum_{n=5}^{35} (5n - 8) = \sum_1^{35} (5n - 8) - \sum_1^4 (5n - 8)$$

note: $\sum_{n=1}^k a_n = \frac{(a_1 + a_k)k}{2}$

$$= \frac{(-3 + 167)35}{2} - \frac{(-3 + 12)4}{2}$$

$$= 2870 - 18$$

$$= 2852.$$

7. \$500 each month 3% annual rate,
compounded monthly.
in 5 years.

after 1 month. $500 \left(1 + \frac{0.03}{12}\right)$

after 2 months $500 \left(1 + \frac{0.03}{12}\right) + 500 \left(1 + \frac{0.03}{12}\right)^2$

after 3 mo. $500 \left(1 + \frac{0.03}{12}\right) + 500 \left(1 + \frac{0.03}{12}\right)^2 + 500 \left(1 + \frac{0.03}{12}\right)^3$

$$\sum_{n=1}^{60} 500 \left(1 + \frac{0.03}{12}\right)^n$$

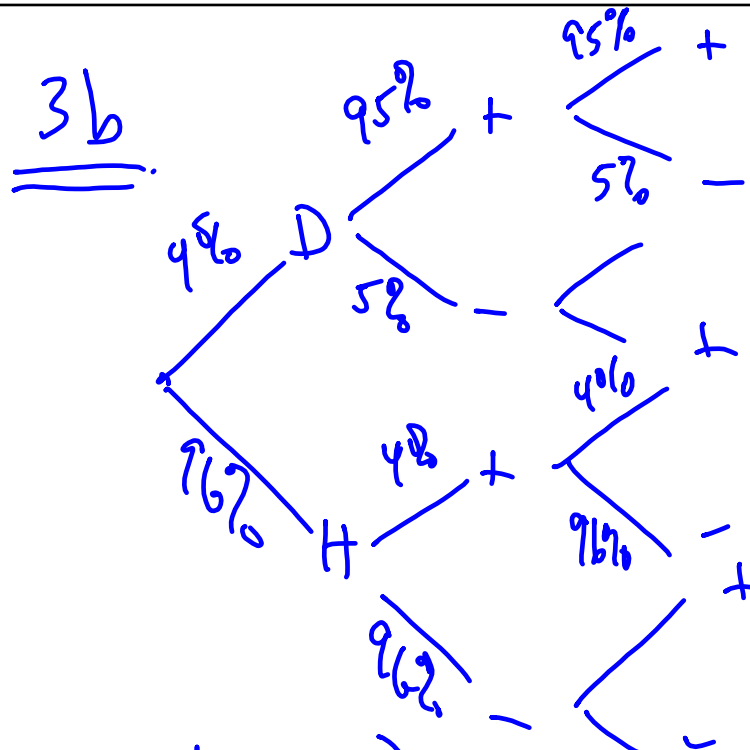
$$= 500 \left[1 + \frac{0.03}{12}\right] \left[\frac{1 - \left(1 + \frac{0.03}{12}\right)^{60}}{1 - \left(1 + \frac{0.03}{12}\right)} \right]$$

$$\sum_{n=1}^k ar^{n-1}$$

$$= \frac{501.25 \left[-0.16 \right]}{-0.0025}$$

$$= 32,404.16$$

$$\begin{aligned}\sum_{k=1}^{10} \ln\left(\frac{k+1}{k}\right) &= \ln(k+1) - \ln k \\ &= \ln 2 - \ln 1 + \ln 3 - \ln 2 + \dots - \ln 11 + \ln 10 \\ &= \ln 11 - \ln 1 = \ln 11\end{aligned}$$



$$P(D | + \cap +) = \frac{P(D \cap + \cap +)}{P(+ \cap +)}$$

$$= \frac{(0.04)(0.95)^2}{(0.04)(0.95)^2 + (0.96)(0.04)^2}$$

$$= \frac{0.0361}{0.037636} = 95.9188\%$$

Birthday Problem.

Q: How many people are necessary to ensure the Probability of 2 people having the same B-day is 50%?

A: 18? upper bound 366 lower bound: 2?

150?
182?
120?
90?
24?
97?

Complement Principle

$P(\text{no one having the same B-day})$

$P(\text{no one has same B-day})$ | $n = \# \text{ of people}$

$$91.7\% = \frac{365 \cdot 364}{365^2} \quad 2$$

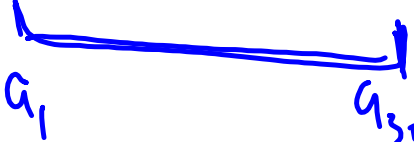
$$99.2\% = \frac{365 \cdot 364 \cdot 363}{365^3} \quad 3$$

$$98.4\% = \frac{365 \cdot 364 \cdot 363 \cdot 362}{365^4}$$

$$= \frac{365 P_4}{365^4}$$

$$\frac{365 P_n}{365^n} \quad n$$

$$f(n) = \frac{365 P_n}{(365)^n}$$

$$S_{n-8} : -3, 2, 7, 12, 17, \dots, 167$$

$$a_1$$
$$a_n = 5(n-1) + 17$$
$$a_{30} = 5(29) + 17$$

