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100

5% annual growth.

over 20 years.

$$A = 100(1.05)^{20} = 265.33$$

165.33% growth.

- \$100 growing at nominal rate of 20%.
- after 1 year:
- compounding annually $\rightarrow \$200$
 - compounding semi-annually: $100\left(1 + \frac{100}{2}\right)^{2(1)}$
 $= 225 \Rightarrow 125\% \text{ effective yield}$
 - compounding quarterly: $100\left(1 + \frac{100}{4}\right)^{4(1 \text{ year})}$
 $= 244$
 $144\% \text{ eff yield}$
 - compounding daily: $100\left(1 + \frac{100}{365}\right)^{365} = 271.46$
 - compounding hourly: $100\left(1 + \frac{1}{8760}\right)^{8760} = 271.81$
 - compounding second: $100\left(1 + \frac{1}{3153600}\right)^{3153600} = 271.83$

Define e - fundamental constant in mathematics.

$$e = \left(1 + \frac{1}{x}\right)^x \text{ as } x \rightarrow \infty$$

$\approx 2.7183 \dots$

In science and math, we replace $y = ab^x$ with $y = ae^{kx}$

- ① a is still y-intercept
- ② $e^k = b$
- ③ k is the continuous growth/decay rate

Ex

$$y = [e^{0.20}]^x$$

\updownarrow

$$y = ab^x$$

$$y = b^x$$

$b = e^{0.20} \approx 1.2214$

20% continuous growth.

Ex

$$y = e^{-0.20x}$$

$$y = ab^x$$

$$y = b^x$$

$e^{-0.20} = b$

0.819 $\approx b$

22% growth

Ex

