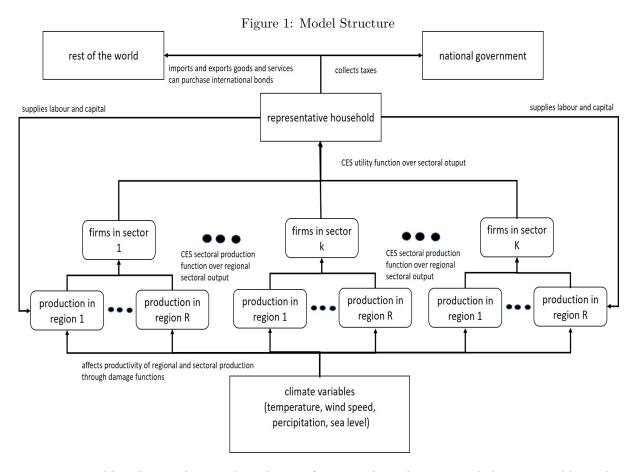
Dynamic General Equilibrium Model for Climate Resilient Economic Development (DGE-CRED) Technical Report

Christoph Schult and Andrej Drygalla Halle Institute for Economic Research

March 2020

1 Introduction

This report is a guide on how to use the spatial small open economy dynamic general equilibrium model for climate change and adaptation simulations. In general the model belongs to the class of real business cycle models, because no nominal rigidities are explicitly considered. Nevertheless, it is possible to extend the model to feature also nominal rigidities. The model structure is depicted in Figure 1. Regional climate variables (precipitation, wind speed, temperature and sea level) are exogenous to



economic variables. Regional sectoral production functions depend on regional climate variables. The model is meant to reflect small open economies and therefore the climate system is unaffected by the domestic economic system.

The model consists of an arbitrary number of regions and sectors. Regional differentiation is only provided on the supply side and not on the demand side. Representative households consume sectoral goods and supply capital and labour to the firms in the regions. Households also demand goods and services from the rest of the world. Firms use capital and labour to produce sectoral goods with sectoral and regional specific constant elasticity of substitution production functions.

The government collects taxes, consumes and can use its funds to finance adaptation measures for specific regions and sectors. So far, adaptation measures will reduce overall damage by all climate variables at the same time. The effectiveness of government expenditure in one specific region and sector can vary.

One can use the model to conduct scenario simulations to evaluate the costs and benefits for different adaptation measures. It is important to understand that the model is not meant to produce explicit forecasts for an economy. The model is meant to simulate long-run developments considering the impact of potential changes in climate variables and their effect on the supply side of the economy. the user is able to define scenarios for different climate variables and adaptation measures. Therefore, it is possible to disentangle the effect of specific climate variable changes on the economy. Further, the model is able to quantify upper limits for costs of adaptation measures to reduce damages by climate change. E.g., it is possible to evaluate the impact of temperature increases on different sectors and the overall impact on total gross value added. The discounted cumulative difference between a scenario without a temperature increase and with temperature increase can be used to determine the upper bound for the costs to reduce the damage caused by a temperature increase.

In the following Section 2 the derivation of the model equations is explicitly described. Readers who are interested in using the model can skip the model section and can directly go to Section 3.

2 Model

2.1 Households

As depicted in Figure 1 the demand side is represented by representative households h providing labour N and capital K to domestic firms f. Households maximize discounted utility over an infinite horizon by choosing consumption $C_t(h)$, capital $K_{k,r,t+1}(h)$, investments $I_{k,r,t}(h)$, labour $N_{k,r,t}(h)$ and foreign net bond holdings B_{t+1} to maximize utility constrained by the budget constraint and the law of motion for sectoral and regional capital. Therefore, the Lagrangian eq. 1 of the representative household is

$$\sum_{t=0}^{\infty} \beta^{t} \left[\left(\frac{C_{t}(h)^{1-\sigma^{C}}}{1-\sigma^{C}} - \sum_{k=1}^{K} \sum_{r=1}^{R} \phi_{k,r}^{L} \frac{N_{k,r,t}(h)^{1+\sigma^{L}}}{1+\sigma^{L}} \right) - \lambda_{t}(h) \left(P_{t} C_{t}(h) \left(1 + \tau^{C} \right) + \sum_{k=1}^{K} \sum_{r=1}^{R} P_{k,r,t} I_{k,r,t}(h) \right) \right. \\
\left. + P_{t}^{f} B_{t}(h) - \sum_{k=1}^{K} \sum_{r=1}^{R} \left(1 - \tau^{L} \right) W_{k,r,t} N_{k,r,t}(h) - \sum_{k=1}^{K} \sum_{r=1}^{R} P_{k,r,t} r_{k,r,t} \left(1 - \tau^{K} \right) K_{k,r,t}(h) - B_{t+1}(h) \right) \\
\left. - \sum_{k=1}^{K} \sum_{r=1}^{R} \lambda_{t}(h) \omega_{k,r,t}^{I}(h) \left\{ K_{k,r,t+1} - \left(1 - \delta \right) K_{k,r,t} - I_{k,r,t} S \left(\frac{I_{k,r,t}}{I_{k,r,t-1}} \right) \right\} \right]. \tag{1}$$

Households receive utility by consuming goods, where the inter temporal elasticity of consumption is defined by σ^C . Dis-utility from labour is sector and region specific $\phi_{k,r}^L$, the inverse Frisch elasticity σ^L is identical for all sectors and regions. Households spent money either on consumption goods $P_t C_t(h)$ (1 + τ^C), regional and sector specific investment $P_{k,r,t}I_{k,r,t}(h)$ and need to repay foreign bonds $B_{t+1}(h)$. They receive income from labour $W_{k,r,t} N_{k,r,t}(h)$ (1 - τ^L), capital renting $P_{k,r,t} r_{k,r,t} K_{k,r,t}(h)$ (1 - τ^K) and can use their borrowed money from the foreign economy $B_t(h)$. The first order conditions to the problem are the behavioral equations. As is standard in teh literature we replace the Lagrange multiplier λ_t by the marginal utility of consumption $\frac{C_t(h)^{-\sigma^C}}{P_t(1+\tau^C)}$ derived from the first order condition (FOC) of the above problem with respect to (w.r.t.) consumption. Households supply labour according to the FOC w.r.t. labour eq. 2 for each sector and region depending on the wage $W_{k,r,t}$ and the marginal dis-utility of labour for the specific sector and region

$$\phi_{k,r}^{L} N_{k,r,t}(h)^{\sigma^{L}} = \lambda_{t}(h) W_{k,r,t} (1 - \tau_{k,r,t}^{L}).$$
(2)

The household also needs to decide how much of its income it wants to consume or invest into capital. The famous Euler equation eq. 3 is obtained by taking the first derivative of the Lagrangian w.r.t. sector and region specific capital

$$\lambda_{t+1}(h) \beta \left(P_{k,r,t+1} \, r_{k,r,t+1} + (1-\delta) \, \omega_{k,r,t+1}^{I} \right) = \lambda_{t}(h) \, \omega_{k,r,t}^{I}. \tag{3}$$

Further, the household also faces investment adjustment cost $S(\frac{I_{k,r,t}}{I_{k,r,t-1}}) = 3 - exp\left\{\sqrt{\phi^K/2}\left(\frac{I_{k,r,t}}{I_{k,r,t-1}} - 1\right)\right\}$ exp $\left\{-\sqrt{\phi^K/2}\left(\frac{I_{k,r,t}}{I_{k,r,t-1}} - 1\right)\right\}$, which are sector and region specific. The specification of the investment adjustment cost function is the same as proposed and estimated by Christiano et al. (2014) for the US. The marginal value of sectoral and regional investment $\omega^I_{k,r,t}$ is determined by

$$P_{k,r,t} \lambda_{t}(h) = \lambda_{t}(h) \omega_{k,r,t}^{I} \left(S(\frac{I_{k,r,t}}{I_{k,r,t-1}}) - \frac{\partial S(\frac{I_{k,r,t}}{I_{k,r,t-1}})}{\partial I_{k,r,t}} \frac{I_{k,r,t}}{I_{k,r,t-1}} \right) + \beta \lambda_{t+1}(h) \omega_{k,r,t+1}^{I} \frac{\partial S(\frac{I_{k,r,t+1}}{I_{k,r,t}})}{\partial I_{k,r,t}} \left(\frac{I_{k,r,t+1}}{I_{k,r,t}} \right)^{2}$$
(4)

Households have access to the international financial market to purchase and sell internationally traded bonds. We only consider net foreign positions.

$$\lambda_{t+1} \,\beta \, S_{t+1}^f \,\phi_{t+1}^B \, \left(1 + r^f_{t+1}\right) = \lambda_t \tag{5}$$

The required interest rate will increase if the foreign debt relative to GDP increases and current net exports relative to GDP will decrease.

$$\phi_{t+1}^{B} = exp\left(-\phi^{B}\left(S_{t+1}^{f} r_{t+1}^{f} \frac{B_{t}}{Y_{t+1}} + \frac{NX_{t}}{Y_{t}}\right)\right)$$
 (6)

- 2.2 Firms
- 2.3 Government
- 2.4 Climate variables
- 2.5 Rest of the world

3 How to use the model?

3.1 Usage

- 1. In order to use the model you need to install Dynare (at least version 4.5.5) and Matlab (at least 2018b) or Octave on your computing machine.
- 2. You need to download the repository from Github.
- 3. The script RunSimulations.m has to be executed in order to run simulations for different scenarios. Make sure that the scenarios and model parameters are defined in the file Model Simulation and Calibration K Sectors and R Regions.xlsx. We need to adopt the number of sectors and regions in the file IWH_CRED_Model.mod.
- 4. The simulation results are stored in the file Results Scenarios K Sectors and R Regions.xlsx.

4 Folder structure

- 1. The main file containing all necessary mod files is IWH_CRED_Model.mod. This file includes the following files stored in the ModFiles folder:
 - (a) IWH_CRED_Model_Declarations.mod declares all endogenous and exogenous variables if the model and structural parameters.
 - (b) IWH_CRED_Model_Parameters.mod assigns values to the structural parameters of the model.
 - (c) IWH_CRED_Model_Equations.mod contains the equations of the model.
 - (d) IWH_CRED_Model_LatexOutput.mod produces latex output for documentation of the declared variables and model equations.
 - (e) IWH_CRED_Model_SteadyState.mod computes initial and terminal condition for the dynamic simulation.
 - (f) IWH_CRED_Model_Simulations.mod starts the dynamic simulation.
- 2. Subroutines responsible for finding the initial and terminal conditions are located in the subfolder Functions:
 - (a) Calibration.mat finds the initial conditions to reflect a specific year of the economy.
 - (b) FIndA.mat looks for exogenous productivity shocks across sectors and regions to meet the terminal conditions.
 - (c) FIndK.mat looks for a capital allocation across sectors and regions to fulfill the static equations of the model.
 - (d) rng.mat random number generator function necessary for Octave users.
- 3. To define scenarios and structural parameters one needs to create an Excel workbook located in the subfolder ExcelFiles:
 - (a) Model Simulation and Calibration for K Sectors and R regions.xlsx has multiple sheets:
 - i. initial Start
 - ii. terminal Terminal
 - iii. parameters to define rigidity parameters Dynamics
 - iv. elasticity parameters and tax rates Structural Parameters
 - v. coefficients for regional and sector specific damage functions Climate Damage Functions
 - vi. Baseline scenario and other optional scenario sheets defining long-run values of climate variables
 - (b) Results Scenarios K Sectors and R regions.xlsx has as many sheets as Scenarios defined in the previous Excel file.

- 4. The latex files produced by IWH_CRED_Model_LatexOutput.mod are stored in LatexFiles.
 - $(a) \ \ the \ system \ of \ dynamic \ equations \ as \ implemented \ in \ Matlab \ \verb|IWH_CRED_Model_Dynamic|, \ \ \verb|IWH_CRED_Model_Dynamic|, \ \ \verb|IWH_CRED_Mod$
 - (b) names of endogenous, exogenous variables and parameters IWH_CRED_Model_latex_definitions
 - (c) the system of dynamic equations in original form without auxiliary variables for leads and lags IWH_CRED_Model_original, IWH_CRED_Model_original_content
- 5. The file to run different simulations is RunSimulations.m.
- 6. A Matlab function to find solutions to the static system of equations is IWH_CRED_Model_steady_state.m.

References

Christiano, L. J., Motto, R. & Rostagno, M. (2014), 'Risk shocks', American Economic Review 104(1), 27–65.

A Model Equations

A.1 Regional Industries

Damage function

$$D_{k,r_{t}} = exp\left(-\phi^{G_{k,n}^{A}} G_{k,n}^{A}\right) \left(a_{1,k,r} T_{rt} + a_{2,k,r} (T_{rt})^{a_{3,k,r}} + a_{1,k,r} SL_{t} + a_{2,k,r} (SL_{t})^{a_{3,k,r}} + a_{1,k,r} W_{rt}^{S} + a_{2,k,r} (W_{rt}^{S})^{a_{3,k,r}} + a_{1,k,r} PERC_{rt} + a_{2,k,r} (PERC_{rt})^{a_{3,k,r}}\right)$$

$$(7)$$

TFP

$$A_{k,r_t} = \rho_{k,r}^A A_{k,r_{t-1}} + (1 - \rho_{k,r}^A) \exp\left(\eta_{A,k,r_t}\right)$$
(8)

capital specific productivity

$$A_{k,r_{t}}^{K} = \rho_{k,r}^{A^{K}} \, A_{k,r_{t-1}}^{K} + (1 - \rho_{k,r}^{A^{K}}) \exp \left(\eta_{A^{K},k,n_{t}} \right) \tag{9}$$

labour specific productivity

$$A_{k,r_{t}}^{N} = \rho_{k,r}^{A^{N}} \, A_{k,r_{t-1}}^{N} + (1 - \rho_{k,r}^{A^{N}}) \exp \left(\eta_{A^{N},k,n_{t}} \right) \tag{10} \label{eq:10}$$

Price of regional sectoral goods

$$\frac{P_{k,r_t}}{P_{k_t}} = \omega_{k,r}^{\frac{1}{\eta^C}} \left(\frac{Y_{k,r_t}}{Y_{k_t}}\right)^{\frac{(-1)}{\eta^C}} \tag{11}$$

Production function

$$Y_{k,r_{t}} = A_{k,r_{t}} \left(1 - D_{k,r_{t}} \right) \left(\alpha_{k,r}^{K} \frac{\frac{1}{\eta_{k,r}^{N,K}}} \left(A_{k,r_{t}}^{K} K_{k,r_{t-1}} \right) \frac{\eta_{k,r}^{N,K} - 1}{\eta_{k,r}^{N,K}} + \alpha_{k,r}^{N} \frac{\frac{1}{\eta_{k,r}^{N,K}}}{\eta_{k,r}^{N,K}} \left(A_{k,r_{t}}^{N} PoP_{t} N_{k,r_{t}} \right) \frac{\eta_{k,r}^{N,K} - 1}{\eta_{k,r}^{N,K}} \right) \frac{\eta_{k,r}^{N,K} - 1}{\eta_{k,r}^{N,K}}$$

$$(12)$$

Firms FOC capital

$$r_{k,r_t} = \alpha_{k,r}^{K} \frac{\frac{1}{N,K}}{\eta_{k,r}^{K}} A_{k,r_t}^{K} \frac{\eta_{k,r}^{N,K-1}}{\eta_{k,r}^{N,K}} \left(\frac{K_{k,r_{t-1}}}{Y_{k,r_t}}\right)^{\frac{-1}{N,K}}$$

$$(13)$$

Firms FOC labour

$$\frac{W_{k,r_t}}{P_{k,r_t}} = \alpha_{k,r}^N \frac{\frac{1}{\eta_{k,r}^{N,K}}}{Y_{k,r_t}} \left(\frac{A_{k,r_t}^N PoP_t N_{k,r_t}}{Y_{k,r_t}} \right)^{\frac{-1}{\eta_{k,r}^{N,K}}}$$
(14)

A.2 Retailer for Aggregation

Relative price of sectoral output

$$\frac{P_{kt}}{P_t} = \omega_k^{\frac{1}{\eta^C}} \left(\frac{Y_{kt}}{Y_t}\right)^{\frac{(-1)}{\eta^C}} \tag{15}$$

Sectoral CES aggregation

$$Y_{kt} = \left(\sum_{r}^{R} \omega_{k,r} \frac{\frac{1}{\eta_{k}^{C}}}{\eta_{k}^{C}} Y_{k,r_{t}} \frac{\eta_{k}^{C-1}}{\eta_{k}^{C}}\right)^{\frac{\eta_{k}^{C}}{\eta_{k}^{C-1}}}$$
(16)

A.3 Households

Households FOC labour

$$\frac{W_{k,r_t} \left(1 - \tau^N\right) \left(\frac{C_t}{PoP_t}\right)^{\left(-\sigma^C\right)}}{1 + \tau^C} = \phi^L N_{kt}^{\sigma^L}$$
(17)

Households FOC capital

$$\frac{\left(\frac{P_{t+1} C_{t+1}}{P^{oP_{t+1}}}\right)^{\left(-\sigma^{C}\right)}}{1+\tau^{C}} \beta P_{k,r_{t+1}} r_{k,r_{t+1}} \left(1-\tau^{K}\right) + \beta \omega_{k,r_{t+1}}^{I} \left(1-\delta\right) = \omega_{k,r_{t}}^{I}$$
(18)

Households FOC investment

$$P_{k,r_{t}} \frac{\left(\frac{P_{t} C_{t}}{Po P_{t}}\right)^{\left(-\sigma^{C}\right)}}{1+\tau^{C}} = \omega_{k,r_{t}}^{I} \left(1 - \frac{\phi^{K}\left(\frac{I_{k,r_{t}}}{I_{k,r_{t-1}}} - 1\right)}{I_{k,r_{t-1}}}\right) + \frac{\phi^{K} \omega_{k,r_{t+1}}^{I} \beta P_{k,r_{t+1}} \left(\frac{I_{k,r_{t+1}}}{I_{k,r_{t}}} - 1\right) I_{k,r_{t+1}}^{2}}{I_{k,r_{t}}^{2}}$$
(19)

Households LOM capital

$$K_{k,r_t} = K_{k,r_{t-1}} (1 - \delta) + \max(0, I_{k,r_t} \left(1 - \frac{\phi^K}{2} \left(\frac{I_{k,r_t}}{I_{k,r_{t-1}}} - 1 \right)^2 \right))$$
 (20)

Households FOC foreign bonds

$$\left(\frac{P_{t+1} C_{t+1}}{PoP_{t+1}}\right)^{\left(-\sigma^{C}\right)} \beta \left(1 + r^{f}_{t+1}\right) = \left(\frac{P_{t} C_{t}}{PoP_{t}}\right)^{\left(-\sigma^{C}\right)} - \phi^{B} \left(B_{t} - (\bar{B})\right)$$

$$(21)$$

A.4 Climate Variables

Temperature
$$T_{rt} = T_{0,r} + \eta_{T,r_t} \tag{22}$$

Wind speed
$$W_{r\ t}^{S} = W_{0,r}^{S} + \eta_{W^{S},r,t} \tag{23} \label{eq:23}$$

Percipitation
$$PERC_{rt} = PERC_{0,r} + \eta_{PERC,r_t}$$
 (24)

Sea level
$$SL_t = SL_0 + \eta_{SL_t} \tag{25}$$

A.5 Trade

Trade balance $NX_{t} = \left(-\left(B_{t} - \left(1 + r^{f}_{t}\right) B_{t-1}\right)\right) \tag{26}$

Net exports
$$NX_t = \rho^{NX} NX_{t-1} + Y_t \left(1 - \rho^{NX}\right) \exp\left(\eta_{NX_t}\right) \omega^{NX} \tag{27}$$

A.6 Government

Budget constraint

$$P_{t}G_{t} + P_{t}\left(1 + r^{f}_{t}\right)BG_{t} = P_{t}BG_{t} + C_{t}P_{t}\tau^{C} + N_{k,r_{t}}W_{k,r_{t}}\tau^{N} + K_{k,r_{t}}r_{k,r_{t}}P_{k,r_{t}}\tau^{K}$$

$$\tag{28}$$

Government foreign debt $BG_t = \eta_{BG_t} \tag{29}$

A.7 Aggregates

National price level
$$P_{t} = exp\left(\eta_{P_{t}}\right) \tag{30}$$

National population $PoP_{t} = \rho^{PoP} \ PoP_{t-1} + \left(1 - \rho^{PoP}\right) \ PoP_{0} \exp\left(\eta_{PoP_{t}}\right) \tag{31}$

Resource constraint
$$Y_t = C_t + I_t + G_t - NX_t$$
 (32)

Sector labour

$$N_{kt} = \sum_{r}^{R} N_{k,r_t} \tag{33}$$

Sector wage bill

$$N_{kt} W_{kt} = \sum_{r}^{R} N_{k,r_t} W_{k,r_t}$$
(34)

Sector investment

$$P_{kt} I_{kt} = \sum_{r}^{R} P_{k,r_t} I_{k,r_t}$$
 (35)

Sector capital stock

$$P_{kt} K_{kt} = \sum_{r}^{R} P_{k,r_t} K_{k,r_t}$$
(36)

National investment

$$P_t I_t = \sum_{k}^{K} P_{kt} I_{kt}$$
 (37)

National capital

$$P_t K_t = \sum_{k}^{K} P_{kt} K_{kt-1} \tag{38}$$

National output $P_t Y_t = P_{kt} Y_{kt}$ (39)

National labour share

$$N_t = \sum_{k}^{K} N_{kt} \tag{40}$$

Table 1: Endogenous

| Variable | IAT _E X | Description |
|----------------|---------------------|--|
| P | P | price level |
| K | K | capital stock |
| C | C | consumption |
| PoP | PoP | population |
| В | B | international traded bonds |
| BG | BG | government debt |
| NX | NX | net exports |
| rf | rf | foreign interest rate |
| G | G | government expenditure |
| I | I | private investment |
| Y | Y | GDP |
| N | N | labour |
| SL | SL | sea level |
| PERC_1 | $PERC_r$ | regional percipitation |
| T_1 | T_r | regional temperature |
| WS_1 | W_r^S | regional wind speed |
| Y_1 | Y_k | sector GDP |
| K_1 | K_k | sector capital |
| $N_{-}1$ | N_k | sector employment |
| $I_{-}1$ | I_k | sector private investment |
| P_1 | P_k | sector price index |
| W_{-1} | W_k | sector wage index |
| $Y_{-}1_{-}1$ | $Y_{k,n}$ | regional sector GDP |
| D_1_1 | $D_{k,n}$ | regional sector damages |
| K_1_1 | $K_{k,n}$ | regional sector capital |
| $N_{-}1_{-}1$ | $N_{k,n}$ | regional sector employment |
| $W_{-}1_{-}1$ | $W_{k,n}$ | regional sector wages |
| A_1_1 | $A_{k,n}$ | regional sector TFP |
| $A_N_1_1$ | $A_{k,n}^{N}$ | regional sector labour specific TFP |
| $A_K_1_1$ | $A_{k,n}^{K}$ | regional sector capital specific TFP |
| $I_{-}1_{-}1$ | $I_{k,n}$ | regional sector private investment |
| P_1_1 | $P_{k,n}$ | regional sector price index |
| $omegaI_1_1_1$ | $\omega_{k,n}^{I'}$ | shadow value of regional private sector investment |
| r_1_1 | $r_{k,n}$ | regional sector rental rate on capital |

Table 2: Exogenous

| Variable | L AT _E X | Description |
|--------------|----------------------------|----------------------------------|
| exo_P | η_P | exogeneous price index evolution |
| exo_PoP | η_{PoP} | exogeneous population |
| exo_SL | η_{SL} | exogeneous sea level |
| exo_NX | η_{NX} | exogenous net exports |
| exo_BG | η_{BG} | exogenous structural balance |
| exo_1_1 | $\eta_{A,k,n}$ | exogenus TFP |
| $exo_N_1_1$ | $\eta_{A^N,k,n}$ | exogenous labour specific TFP |
| $exo_K_1_1$ | $\eta_{A^K,k,n}$ | exogenous capital specific TFP |
| exo_T_1 | $\eta_{T,n}$ | exogenus regional temperature |
| exo_PERC_1 | $\eta_{PERC,n}$ | exogenus regional percipitation |
| exo_WS_1 | $\eta_{W^S,n}$ | exogenus regional wind speed |

Table 3: Parameters

| Variable | IATEX | Description |
|-----------------------|---|---|
| omega_1_p | ω_k | sector capital share |
| $etaC_1_p$ | η^C | intratemporal elasticity of substitution |
| $phiY_1_1_p$ | $\frac{P_{k,n,0} Y_{k,n,0}}{P_0 Y_0}$ | share of regional and sectoral output |
| $phiN_1_1_p$ | $N_{k,n,0}$ $W_{k,n,0}N_{k,n,0}$ | share of regional and sectoral employment |
| $\tt phiW_1_1_p$ | $\frac{W_{k,n,0} N_{k,n,0}}{P_{k,n,0} Y_{k,n,0}}$ $\frac{P_{k,n,0} Y_{k,n,0}}{P_{k,n,0}}$ | share of regional and sectoral employment |
| $phiP_{-}1_{-}1_{-}p$ | $\frac{P_{k,n,0}}{P_0}$ | share of regional and sectoral employment |

Table 3 – Continued

| Variable | ĿŒŢ | Description |
|--------------------------|--|--|
| phiL_1_1_p | $\phi_{k,n}^L$ | coefficient of disutility to work |
| omega_1_1_p | $\omega_{k,n}$ | sector capital share |
| alphaK_1_1_p | $\alpha_{k,n}^{K}$ | distribution parameter capital share |
| alphaN_1_1_p | $\alpha_{h,n}^{N}$ | distribution parameter labour share |
| etaNK_1_1_p | $rac{lpha_{k,n}^{N,K}}{\eta_{k,n}^{N,K}}$ | elasticity of substitution between labour and capital |
| A_1_1_p | $A_{k,n}$ | sector long-run TFP |
| A_N_1_1_p | $A_{k,n}^N$ | sector labour specific TFP |
| A_K_1_1_p | $A_{k,n}^{K,n}$ | sector capital specific TFP |
| a_T_1_1_p | | intercept of damage function temperature |
| a_T_1_1_p a_T_2_1_1_p | $a_{1,k,n}$ | slope of damage function temperature |
| a_T_3_1_1_p | $a_{2,k,n}$ $a_{3,k,n}$ | exponent of damage function temperature |
| a_P_1_1_1_p | $a_{1,k,n}$ | intercept of damage function percipitation |
| a_P_2_1_1_p | $a_{2,k,n}$ | slope of damage function percipitation |
| a_P_3_1_1_p | $a_{3,k,n}$ | exponent of damage function percipitation |
| a_W_1_1_1_p | $a_{1,k,n}$ | intercept of damage function wind speed |
| a_W_2_1_1_p | $a_{2,k,n}$ | slope of damage function wind speed |
| a_W_3_1_1_p | $a_{3,k,n}$ | exponent of damage function wind speed |
| a_SL_1_1_1_p | $a_{1,k,n}$ | intercept of damage function sea level |
| a_SL_2_1_1_p | $a_{2,k,n}$ | slope of damage function sea level |
| a_SL_3_1_1_p | $a_{3,k,n}$ | exponent of damage function sea level |
| beta_p | β | discount factor |
| delta_p | $rac{\delta}{\sigma^L}$ | capital depreciation rate |
| sigmaL_p | $\sigma^{C} = \sigma^{C}$ | inverse Frisch elasticity |
| sigmaC_p | η^C | intertemporal elasticity of substitution |
| etaC_p | ϕ^B | intratemporal elasticity of substitution coefficient of foreign adjustment cost |
| phiB_p | $\overset{arphi}{\phi}^{K}$ | coefficient of investment adjustment cost |
| phiK_p tauC_p | $	au^C_{	au^C}$ | consumption tax |
| tau0_p tauN_p | $	au^N$ | labour tax |
| tauK_p | $	au^K$ | capital tax |
| omegaNX_p | ω^{NX} | share of net exports relative to domestic GDP |
| rhoNX_p | ρ^{NX} | persistency in net exports |
| rhoA_p | o^A | persistency in TFP |
| rhoPoP_p | o^{PoP} | persistency in population |
| rhoSL_p | $ ho^{SL}$ | persistency in sea level |
| inbsectors_p | K | number of sectors |
| $inbregions_p$ | R | number of regions |
| ${\tt lCalibration_p}$ | l^{Calib} | logical indiactor whether model is calibrated or not |
| T0_1_p | $T_{0,n}$ | initial regional temperature |
| PERCO_1_p | $PERC_{0,n}$ | initial regional percipitation |
| WSO_1_p | $W_{0,n}^S$ | initial regional wind speed |
| TT_1_p | $T_{T,n}$ | terminal regional temperature |
| PERCT_1_p | $PERC_{T,n}$ | terminal regional percipitation |
| WST_1_p | $W_{T,n}^{S}$ | terminal regional wind speed |
| SLO_p | SL_0 | initial sea level |
| PoP0_p | POP_0 | initial population |
| Y0_p | Y_0 | initial output |
| PO_p | P_0 | initial price level initial employment |
| NO_p | $Y_0 \\ SL_0$ | terminal sea level |
| SLT_p PoPT_p | PoP_0 | terminal sea level terminal population |
| YT_p | Y_0 | terminal output |
| NT_p | Y_0 | terminal employment |
| | ± () | terminar employment |