# Dynamic General Equilibrium Model for Climate Resilient Economic Development

Andrej Drygalla, Katja Heinisch and Christoph Schult\* | July 2020 Halle Institute for Economic Research





On behalf of:



Federal Ministry for the Environment, Nature Conservation and Nuclear Safety

of the Federal Republic of Germany

<sup>\*</sup> Research assistance by Yoshiki Wiskamp is greatly acknowledged.

## Outline

- 1 Economic Models and Climate Change
- 2 Model building steps
- **10** Introduction to Dynare
- 4 DGE-CRED Model
- **6** Model Simulation and Calibration

## Outline

- 1 Economic Models and Climate Change
- 1.1 Motivation and Training Goals
- 1.2 Modeling Approaches
- 1.3 The Suggested Model
- 1.4 Advantages and Limitations of the Modeling Approach
- 1.5 Possible Applications

# 1.1 Training Goals

- Inclusion of climate change and potential adaptation measures as variables in macroeconomic models to assess the impact of climate change and evaluate adaptation policies
- A sustainable implementation of the developed model
- Relationship between climate and the economy needs to be continuously monitored
- Allow for model flexibility to address specific policy questions when needed



#### Outline

- 1 Economic Models and Climate Change
- 1.1 Motivation and Training Goals
- 1.2 Modeling Approaches
- 1.3 The Suggested Model
- 1.4 Advantages and Limitations of the Modeling Approach
- 1.5 Possible Applications

# 1.2 Overview of Modeling Approaches

- Commonly top-down approaches are used to model the economy
- Three broad categories of macroeconomic models are used for modeling the interaction between climate and the economy
  - 1. Input-output models
  - 2. Macroeconometric models
  - 3. General Equilibrium models



# 1.2.1 Input-output (I-O) Models (1)

- Basic idea underlying the concept of I-O models:
  - ▶ Interdependencies between different economic sectors are analyzed
  - $\blacktriangleright$  The output of sector i can be used as input of sector j and vice versa
  - ➤ The output of sector i can also be consumed in form of: consumption, investment, exports
  - ▶ Further refinements (e.g. environmental considerations) are possible



# 1.2.1 Input-output (I-O) Models (2)

- I-O models are based on national accounts and the respective supply and use tables
- I-O models are useful to study sectoral interdependencies
- I-O tables are not available on a sub-national level
- Long-term adjustment costs are overestimated using static I-O models
- See Miller and Blair 2009 for environmental input-output analysis



# 1.2.1 Input-output (I-O) Models (3)

#### Example:

- ▶ Consider an economy, in which two goods  $x = (x_1, x_2)'$  are produced
- ▶ The final consumption of each good is expressed by  $c = (c_1, c_2)'$
- ▶ Since each good can also be used as input in the production process:

$$x_1 = a_{11} x_1 + a_{12} x_2 + c_1$$
  
 $x_2 = a_{21} x_1 + a_{22} x_2 + c_2$ 

▶ In matrix notation this can be expressed as:

$$x = A x + c$$
, where  $A = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix}$ 



# 1.2.1 Input-output (I-O) Models (4)

- Literature:
  - ▶ Liping and Chen 2010
  - ▶ Lenzen 2011
  - ▶ Pan and Kraines 2001

# 1.2.2 Macroeconometric Models (1)

- Relationships between economic variables are:
  - estimated with econometric techniques or
  - ▶ follow from some definition (e.g. national accounts)
- Widely used in forecasting
- Examples include vector autoregressive (VAR) and (vector) error-correction (V)EC models

# 1.2.2 Macroeconometric Models (2)

- Simulation studies can be conducted for different scenarios, that can be quantified with the help of I-O models
- In contrast to I-O models: consideration of trends and prices that can amplify/mitigate effects on other variables
- Simulation results are less precise for longer simulation horizons as estimated parameters are constant
- Hsiang 2016 provides an excellent overview of climate econometrics



# 1.2.2 Macroeconometric Models (3)

#### Literature:

- ▶ Bloesch and Gourio 2015
- ► Colacito et al. 2018
- ▶ Dell et al. 2012
- ▶ Deryng et al. 2014
- ► Tol 1995
- ▶ Graff Zivin and Neidell 2014

# 1.2.3 General Equilibrium Models (CGE) (1)

- Basic idea underlying the concept of General Equilibrium Models:
  - ▶ Explain behavior of supply, demand, prices, etc. in a whole economy
  - ▶ Build up on microfoundations
  - ► Encompass different markets
  - ▶ Interaction of demand and supply leads to an overall general equilibrium for the entire economy

# 1.2.3 General Equilibrium Models (CGE) (2)

- The class of general equilibrium models relies on the principle of optimizing agents
  - ▶ The system of equations is derived from optimization problems of households and firms
  - ▶ Optimization is based on expectations about the future
- One can distinguish between static and dynamic general equilibrium models
- For a comprehensive introduction to the main principles of general equilibrium models, see Wing 2004



# 1.2.3 General Equilibrium Models (CGE) (3)

- See Arndt et al. 2015 for how to use CGE models to evaluate the impact of climate change on the economy
- This study uses a computational dynamic general equilibrium model for Vietnam
- Different climate change scenarios are simulated
- Climate change affects the evolution of sectoral productivity, increase in temperature e.g. has an adverse effect on rice crop yields

# 1.2.3 General Equilibrium Models (CGE) (4)

#### Literature:

- ► Acemoglu et al. 2012
- ▶ Berrittella et al. 2004
- ▶ Bosello et al. 2011
- ► Calzadilla et al. 2011
- ► Eboli et al. 2009
- ▶ Elshennawy et al. 2015
- ► Fankhauser and Tol 2005
- ▶ Heal 2017

- ▶ Kahn et al. 2019
- ▶ Lecocq and Shalizi 2007
- ▶ Manne et al. 1995
- ▶ Nordhaus and Yang 1996
- ▶ Popp 2004
  - ▶ Batten 2018
- ▶ Dietz and Stern 2015



## Outline

- 1 Economic Models and Climate Change
- 1.1 Motivation and Training Goals
- 1.2 Modeling Approaches
- 1.3 The Suggested Model
- 1.4 Advantages and Limitations of the Modeling Approach
- 1.5 Possible Applications

# 1.3 Our Approach

- We use a dynamic general equilibrium (DGE) framework, where
  - ▶ the model equations are explicitly derived from the optimization behaviour of representative agents
  - ▶ due to the dynamic nature of the model, the optimal decisions are derived at every point in time and thus show optimal reactions of agents to changing fundamentals
  - ▶ model provides a consistent framework for the interpretation of domestic and foreign economic shocks and the channels through which they affect variables

# 1.3.1 Key Characteristics of the Model (1)

- Small open-economy model
- Non-stationary model with direct mapping to statistical variables
- Regional and sectoral perspective:
  - ▶ Regional and sectoral shares of output, employment, wage bill
  - ▶ Regional and sectoral production functions
- National perspective: population, national output, taxes, government expenditure
- Three different agents: firms, households and government
- Climate variables are exogenous to economic variables: Temperature, wind speed, precipitation and sea level



# 1.3.1 Key Characteristics of the Model (2)

- The impact of climate (change) on the economy is modeled with the help of so-called "damage functions"
- These sector and/or region-specific equations link climate variables to economic outcomes
- "Damage" in that context refers to the fraction of potential production "lost" due to climate (change)
- Sectoral damage functions are calibrated based on particular sub-models that translate climate related events into economic impacts
- We will use results from the literature and econometric methods to calibrate the damage functions

# 1.3.1 Key Characteristics of the Model (3)

- DGE models can easily be built and run in Dynare, an open source pre-processor for Matlab (and its open source alternative Octave) that is continuously supported online and widely used
- Dynare allows the user to simulate and estimate the underlying structural model
- It is also possible to run Dynare with other open source software such as Julia, Python or R
- Translating model equations into Dynare code is intuitive

## Outline

- 1 Economic Models and Climate Change
- 1.1 Motivation and Training Goals
- 1.2 Modeling Approaches
- 1.3 The Suggested Model
- 1.4 Advantages and Limitations of the Modeling Approach
- 1.5 Possible Applications

# 1.4.1 Advantages of General Equilibrium Models (1)

- Parameters can either be calibrated based on comparable studies, economic theory as well as period averages of actual data or be estimated using data up to the most recent period
- It is possible to track the transition dynamics from the initial state to the final state
  - ▶ It shows precisely how the economy "reacts" to the induced changes
- GE models allow for the possibility of (transitory) disequilibria, e.g. unemployment or under-utilization of installed capital
- GE models are parsimonious and more frequent updates are possible with respect to data requirements
- GE models can be estimated (and simulated) with a subset of the data

adaptation policies come into effect, timelier and more precisely

GE models are estimated on the basis of national accounts data, and hence, they are capable to gauge the initial state of the economy, i.e. before climate change or

# 1.4.1 Advantages of General Equilibrium Models (2)

- The number of regions and sectors can be easily modified
- Extensions to the baseline model can be tested easily
- Our damage functions allow a transparent and replicable approach to include climate into the model
- Expectations are formed in a model consistent way



# 1.4.2 Limitations of the Modeling Approach

- Demand for computational power increases tremendously with the number of regions and sectors
- The number of factors is smaller compared to I-O models and static CGE models
- Deviations from perfect foresight setup is not straightforward
- Specifying a functional relationship between climate and sectoral productivity restricts the functional form considered

## Outline

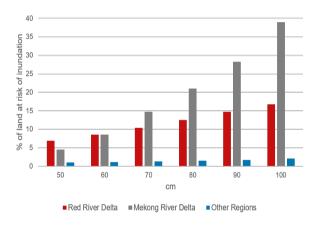
- Economic Models and Climate Change
- 1.1 Motivation and Training Goals
- 1.2 Modeling Approaches
- 1.3 The Suggested Model
- 1.4 Advantages and Limitations of the Modeling Approach
- 1.5 Possible Applications

# 1.5 Possible Applications

- Simulation of different climate change scenarios to determine upper bounds for costs of adaptation policies
- Decompose general equilibrium effects to identify relative contributions by individual climate variables
- Evaluate the impact of different tax rates for different sectors and regions to foster the transition process
- Cost-Benefit analysis example: building of a dike



# 1.5.1 Cost-Benefit of Building a Dike in the Mekong River Delta (1)



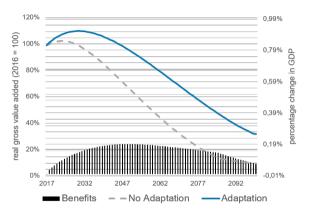
Source: Thuc et al. 2016

# 1.5.1 Cost-Benefit of Building a Dike in the Mekong River Delta (2)

- Facts and assumptions
  - ▶ Coast line of Mekong River Delta is 600 km
  - ▶ Dike needs to be of the same height along the entire coastline
  - ▶ Estimated costs: 40,000 EUR for one meter height and one meter length
  - ▶ Height increases with sea level each year
  - ▶ Damages associated with sea level rise in Mekong Delta River are zero, if and only if the height of the dike exceeds the sea level rise
- Benefit is defined as: difference between a scenario with dike (Adaptation) and without dike (Sea Level) relative to the Baseline scenario



# 1.5.1 Cost-Benefit of Building a Dike in the Mekong River Delta (3)



Source: own exhibition.

Note: Lines depict simulation of agricultural production and bars indicate the difference between

Adaptation and No-Adaptation scenario for total GDP.



## Outline

- 2 Model building steps
- 2.1 Definition of Scenarios
- 2.2 Identification of Climate Hazards
- 2.3 Calibration of Model Parameters

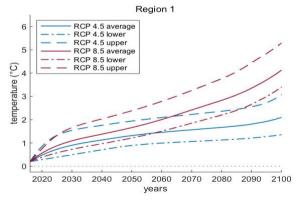
# 2.1 Definition of Climate Change Scenarios (1)

- Determine climate change scenarios
- We use results from Thuc et al. 2016 to define regional specific climate change variables
- Scenarios are based on the IPCC scenarios RCP 4.5 and 8.5.
- It is possible to define regional specific paths for:
  - ▶ annual average temperature
  - ▶ annual average precipitation
  - ▶ sea level rise



# 2.1 Definition of Climate Change Scenarios (2)

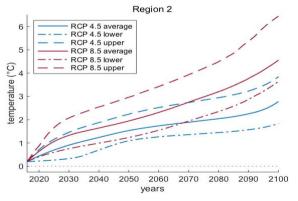
■ The following region specific scenarios for the climate variable temperature can be obtained using the results from Thuc et al. 2016:



Region 1: Mekong River Delta

# 2.1 Definition of Climate Change Scenarios (2)

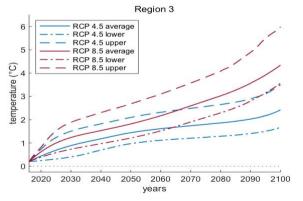
■ The following region specific scenarios for the climate variable temperature can be obtained using the results from Thuc et al. 2016:



Region 2: Red River Delta

# 2.1 Definition of Climate Change Scenarios (2)

■ The following region specific scenarios for the climate variable temperature can be obtained using the results from Thuc et al. 2016:



Region 3: North Central and Central Coast, Southeast, Central Highlands, Northern Midlands and Mountains



#### 2.1.1 Weather Extremes

- Thuc et al. 2016 do not explicitly report results for the frequency of weather extremes
- Define the relationship between annual averages and the frequency of weather extremes, e.g.
  - cyclones
  - ▶ droughts
- Previous studies report changes in the frequency of weather extremes for different climate change scenarios (see e.g. Arndt et al. 2015)

#### 2.1.2 Baseline Scenario (1)

- Determine a hypothetical reference path
- For this path no further change in climate variables
- Define the evolution of sectoral TFP
- Disentangle the impact of different impact chains on the economy

#### 2.1.2 Baseline Scenario (2)

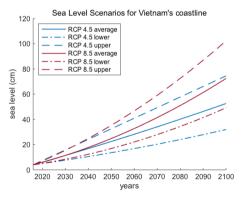
- Model parameters are set to match characteristics of Vietnamese economy in 2016
- Catch-up process and transition to developed economy (Japan selected as plausible benchmark)
  - ▶ Geometric average annual growth rate set to 4%
  - ▶ Determine sectoral TFP shocks to match an assumed new long-run composition of gross value added by economic activity (agriculture 1%, industry 35%, services 65%)
  - ▶ Long-run dynamics of labour productivity to ensure employment shares converge to values observed for developed economies
  - ► Exogenous evolution of sectoral labour and total factor productivity is completed after 120 periods
- No consideration of climate (change) effects on economic development

#### Outline

- 2 Model building steps
- 2.1 Definition of Scenarios
- 2.2 Identification of Climate Hazards
- 2.3 Calibration of Model Parameters

## 2.2 Climate Hazards (1)

- There are several Climate Hazards, potentially affecting Vietnam in the future
- Vietnam is expected to suffer from a rise in the sea level:



Source: Own computation based on results from Thuc et al. 2016.



# 2.2 Climate Hazards (2)

- The sea level rise will come along with a higher inundation risk in coastal regions
- Example: According to Thuc et al. 2016, a sea level rise of 50mm (100mm) is expected to lead to an inundation (% area) of
  - $\blacktriangleright$  6.93% (16.8%) in the Red River Delta
  - $\blacktriangleright$  4.48% (38.9%) in the Mekong Delta
- Increases in the average temperature are expected to cause:
  - ▶ Decline of crop yield
  - ▶ Reduction of total factor productivity
- Other potential hazards: Increased frequency of cyclones, storm surges, etc.



#### Outline

- 2 Model building steps
- 2.1 Definition of Scenarios
- 2.2 Identification of Climate Hazards
- 2.3 Calibration of Model Parameters

#### 2.3.1 Calibration

- It is necessary to define structural parameters of the model to reflect the Vietnamese economy
- Based on identified damages and potential losses in previous studies one can calibrate functional forms of the damage functions
- Climate change will affect economic sectors to a different extent:
  - ▶ Previous studies show a high potential impact of agriculture, electricity markets and transportation

## 2.3.2 Scenario Analysis

- In order to gauge the impact of climate change on economic outcomes, deterministic simulations are conducted
- Different climate change scenarios need to be defined first, e.g. long-term projections for temperature or the sea level
- The model is simulated from its initial condition along the assumed climate change path
- Simulation results then show the adjustment processes to climate change in the economy
- Further, it is possible to specify adaptation measures reducing the impact of climate change on the damage function



#### Outline

- 3 Introduction to Dynare
- 3.1 What is Dynare?
- 3.2 Implementing a Model in Dynare
- 3.3 Steady State in Dynare
- 3.4 Deterministic Simulations in Dynare
- 3.5 Perfect Foresight Setup in Dynare
- 3.6 Remarks and Examples
- 3.7 Macro Processor

## 3.1 What is Dynare?

- Dynare is an open-source program for dynamic general equilibrium modeling:
  - ▶ mainly a collection of different functions written for MATLAB
  - ▶ pre-processor translates Dynare files (.mod files) into MATLAB code



#### Outline

- 3 Introduction to Dynare
- 3.1 What is Dynare?
- 3.2 Implementing a Model in Dynare
- 3.3 Steady State in Dynare
- 3.4 Deterministic Simulations in Dynare
- 3.5 Perfect Foresight Setup in Dynare
- 3.6 Remarks and Examples
- 3.7 Macro Processor



## 3.2.1 Implementing a Model in Dynare

Neoclassical Growth Model (1)

■ Households maximize lifetime utility subject to their budget constraint

$$\max_{\{c_t, k_{t+1}\}_{t=1}^{\infty}} = \sum_{t=1}^{\infty} \beta^{t-1} \frac{c_t^{1-\sigma}}{1-\sigma}$$
s.t.  $c_t + k_{t+1} = A_t k_t^{\alpha} + (1-\delta) k_t$ 

■ It follows from the first order condition of the above problem with respect to consumption that the Lagrange multiplier is defined as

$$\lambda_t = \beta^{t-1} c_t^{-\sigma},$$

representing the marginal utility of consumption

## 3.2.1 Implementing a Model in Dynare

Neoclassical Growth Model (2)

■ The resulting first order conditions are:

$$c_{t}^{-\sigma} = \beta c_{t+1}^{-\sigma} (\alpha A_{t+1} k_{t+1}^{\alpha-1} + 1 - \delta)$$
$$c_{t} + k_{t+1} = A_{t} k_{t}^{\alpha} + (1 - \delta) k_{t}$$

- By the definition  $c_t = c_{t+1} = \bar{c}$ ,  $k_t = k_{t+1} = \bar{k}$  and  $A_t = A_{t+1} = \bar{A}$  has to hold in the steady state
- Therefore, the first order conditions in the steady state case become:

$$\bar{\mathbf{c}}^{-\sigma} = \beta \, \bar{\mathbf{c}}^{-\sigma} (\alpha \, \bar{\mathbf{A}} \, \bar{\mathbf{k}}^{\alpha-1} + 1 - \delta)$$
$$\bar{\mathbf{c}} + \bar{\mathbf{k}} = \bar{\mathbf{A}} \, \bar{\mathbf{k}}^{\alpha} + (1 - \delta) \, \bar{\mathbf{k}}$$

## 3.2.1 Implementing a Model in Dynare

Neoclassical Growth Model (3)

■ The steady state can be obtained analytically by solving the first equation for  $\bar{k}$  and the second equation for  $\bar{c}$ :

$$\bar{\mathbf{k}} = \left(\frac{1 - \beta(1 - \delta)}{\beta \alpha \bar{\mathbf{A}}}\right)^{\frac{1}{\alpha - 1}}$$
$$\bar{\mathbf{c}} = \bar{\mathbf{A}} \bar{\mathbf{k}}^{\alpha} - \delta \bar{\mathbf{k}}$$

- The neoclassical growth model considered in these slides, as well as the DGE-CRED model are deterministic models
  - ▶ No stochastic elements requiring expectancy terms or probability distributions
  - ▶ The remainder of this introduction to Dynare focuses on this class of models

## 3.2.2 Model File (1)

- A model file or mod-file (filename.mod) contains commands and blocks
  - ▶ Each command and each element of a block is terminated by a semicolon (;)
  - ▶ Blocks are terminated by end;
- The model file complementary to these slides is Introduction\_Dynare.mod
- $\blacksquare$  Code lines within the mode file can be deactivated using %, // or /\* ... \*/
- In order to run a model file:
  - ➤ The Dynare path has to be added to the search path of MATLAB addpath('C:\dynare\4.6.1\matlab')
  - ▶ Dynare executed to run the model in MATLAB dynare filename



## 3.2.3 Model File (2)

- To set up a model in Dynare the following componets are needed:
  - ▶ var: Used to declare the endogenous variables
  - ▶ varexo: Used to declare the endogenous variables
  - ▶ parameters: Used to declare the parameters
  - ▶ model block: The model equations must be provided in this block

#### 3.2.4 Variables and Parameters (1)

■ At the beginning of each model file, the endogenous (var) and exogenous (varexo) variables as well as parameters (parameters) have to be defined:

```
var = c k;
varexo = A;
parameters alpha_p beta_p gamma_p delta_p;
```

■ Then, the parameter values have to be assigned:

```
alpha_p = 0.5;
beta_p = 0.95;
gamma_p = 0.5;
delta_p = 0.02;
```

## 3.2.4 Variables and Parameters (2)

■ Optionally, a LaTeX name and long name can be assigned to a variable using the convention:

```
variable_name $tex_name$ (long_name = 'quoted_string')
```

► Example:

```
var
k $k$ (long_name = 'capital'),
c $c$ (long_name = 'consumption');
varexo
A $A$ (long_name = 'technology');
```

## 3.2.4 Variables and Parameters (3)

- There are some restrictions to be kept in mind, when choosing variable and parameter names in Dynare:
  - ▶ Avoid names of built-in functions and commands
  - ▶ Minimize interface with Matlab or Octave functions
  - ► Example: Do not use correctly-spelled greek letters like beta, instead e.g. betta

## 3.2.4 Variables and Parameters (4)

- In Dynare a leading/lagging variable is denoted by adding (+1)/(-1) after the variable
- Note that by convention in Dynare, the time indice of a variable refers to the period when its value is determined. In the context of the neoclassical growth model:
  - ightharpoonup c refers to  $c_t$ , c(+1) to  $c_{t+1}$  and c(-1) to  $c_{t-1}$
  - Since the capital stock entering the production function in the current period is determined in the previous period, the capital stock  $k_t$  becomes k(-1), and the law of motion of capital must be written as: k = i + (1-delta) \*k(-1)
  - ➤ This convention can be modified using the predetermined\_variables setting



## 3.2.5 The model block (1)

- A model is declared inside a model block
- In general, there must be as many equations as there are endogenous variables in the model
- A great advantage of using Dynare is that the equations can be written almost as on paper

```
model;
c + k = A*k(-1)^alpha_p + (1-delta_p)*k(-1);
c^(-gamma_p) = beta_p*c(+1)^(-gamma_p)
            *(alpha_p*A(+1)*k^(alpha_p-1) + 1 - delta_p);
end;
```

## 3.2.5 The model block (2)

- Inside the model block, model-local variables can be used
  - ▶ Simple way to share a common expression between several equations
  - ▶ Syntax: # name\_of\_the\_model\_local\_variable = expression
  - ▶ Scope of this variable is restricted to the model block
- Therefore, the Neoclassical growth model can also be expressed as:

#### Outline

- 3 Introduction to Dynare
- 3.1 What is Dynare
- 3.2 Implementing a Model in Dynare
- 3.3 Steady State in Dynare
- 3.4 Deterministic Simulations in Dynare
- 3.5 Perfect Foresight Setup in Dynare
- 3.6 Remarks and Examples
- 3.7 Macro Processor



## 3.3 Steady State (1)

■ By definition a steady state of a model satisfies:

$$y_t = y_{t+1} = \bar{y} \text{ and } u_t = u_{t+1} = \bar{u},$$

where y is the vector of endogenous variables and u the vector of exogenous shocks

- ▶ In the context of the neoclassical growth model:  $y_t = (c_t k_t)'$  and  $u_t = A_t$
- Note that a steady state is conditional to:
  - $\blacktriangleright$  The steady state values of exogenous variables  $\bar{\mathbf{u}}$
  - ▶ The values of parameters (implicit in the above definition)
- Even for a given set of exogenous and parameter values, some (nonlinear) models have several steady states

# 3.3 Steady State (2)

- The steady state is an important concept in the framework of the DGE-CRED model:
  - ▶ In this model it is assumed that the economy is in steady state at the beginning of the initial period and then transits towards a new steady state, reached in the terminal period
  - ▶ While the trajectories of the exogenous variables are given, those of the endogenous variables are determined within the model
- There are three approaches to calculate the steady state in Dynare
- The steady state values are stored in the MATLAB matrix oo\_.steady\_state



## 3.3.1 Steady State: Approach 1

- Idea: Provide an initial guess for the steady state in the initval block and then conduct the steady state calculation using steady
- Example, considering the neoclassical growth model:

```
initval;
c = 2;
k = 30;
A = 1;
end;
steady;
```

## 3.3.2 Steady State: Approach 2 (1)

- Idea: Use a steady\_state\_model block, in which the steady state values are calculated
- Example, considering the neoclassical growth model:

# 3.3.2 Steady State: Approach 2 (2)

- Note that the steady state values of the exogenous variables have to be assigned in an initval block
- In cases where the steady state can be solved analytically, using a steady\_state\_model block is a suitable approach

# 3.3.3 Steady State: Approach 3 (1)

- Idea: Use an explicit steady state file, which is an external MATLAB-file that must conform with a certain structure and naming convention:
  - ${\tt NAME} of {\tt MODfile\_steady state.m}$
- In this steady state file, you must provide the exact steady state values as in the case of the steady\_state\_model block
- Note: A steady state file is used in the DGE-CRED model



# 3.3.3 Steady State: Approach 3 (2)

■ Before typing the command steady, the steady state values of the exogenous variables have to be assigned in an initval block

```
initval;
A = 1;
end;
steady;
```

# 3.3.3 Steady State: Approach 3 (3)

- Advantage:
  - ▶ Flexibility, can call build-in MATLAB functions
  - ▶ Allows for changing parameters to take parameter dependencies into account without resorting to model-local variables
- Drawback:
  - ▶ Additional flexibility offered by a steady state file increases the scope for errors

#### Outline

- 3 Introduction to Dynare
- 3.1 What is Dynare?
- 3.2 Implementing a Model in Dynare
- 3.3 Steady State in Dynare
- 3.4 Deterministic Simulations in Dynare
- 3.5 Perfect Foresight Setup in Dynare
- 3.6 Remarks and Examples
- 3.7 Macro Processor

#### 3.4.1 Deterministic Simulation (1)

- The deterministic simulation builds up on the concept of perfect foresight, in which agents have full knowledge and perfectly anticipate all future shocks
- More precisely, we assume that:
  - ▶ Agents learn the value of all future shocks
  - ▶ Since there is shared knowledge of the model and of future shocks, agents can compute their optimal plans for all future periods
  - ▶ optimal plans are not adjusted in periods 2 and later
    - $\Rightarrow$  the model behaves as if it were deterministic
- Cost of this approach: The effect of future uncertainty is not taken into account
- Advantage: Numerical solutions can be computed exactly (up to rounding errors) and nonlinearities are fully taken into account



#### 3.4.1 Deterministic Simulation (2)

■ The general problem in the deterministic, perfect foresight, case can be expressed as:

$$f(y_{t+1}, y_t, y_{t-1}, u_t) = 0,$$

where y is the vector of endogenous variables and u the vector of exogenous shocks

- Identification rule: There must be as many equations in f(...) as there are endogeneous variables in y
- The general perfect foresight problem for the neoclassical growth model is:

$$f(y_{t+1}, y_t, y_{t-1}, u_t) = \begin{pmatrix} c_t^{-\sigma} - \beta c_{t+1}^{-\sigma} (\alpha A_{t+1} k_{t+1}^{\alpha-1} + 1 - \delta) \\ c_t + k_{t+1} - A_t k_t^{\alpha} - (1 - \delta) k_t \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix},$$

where  $y_t = (c_t k_{t+1})'$  and  $u_t = A_t$ 



## 3.4.1 Deterministic Simulation (3)

- The aim of a deterministic simulation is to examine the trajectories of the model variables over the time period t = 1, ..., T
- Consequently, the stacked system for a perfect foresight simulation over T periods becomes a two-boundary value problem:

$$\begin{cases} f(y_2, y_1, \mathbf{y_0}, \mathbf{u_1}) = 0 \\ f(y_3, y_2, y_1, \mathbf{u_2}) = 0 \\ \vdots \\ f(\mathbf{y_{T+1}}, y_T, y_{T-1}, \mathbf{u_T}) = 0 \end{cases}$$

where  $y_0$  and  $y_{T+1}$  as well as  $u_1, ..., u_T$  are given

■ Dynare uses a Newton-type methode to solve this stacked system

#### 3.4.1 Deterministic Simulation (4)

- The Newton method numerically solves the two-boundary value problem and hence computes trajectories for given shocks over a finite number of periods
- If one is rather interested in solving an infinite-horizon problem:
  - ▶ The easiest way is to approximate the solution by a finite-horizon problem (large T)
  - ▶ Drawback: The solution is specific to a given sequence of shocks, and not generic

### 3.4.1 Deterministic Simulation (5)

- In case there is more than one lead or lag, Dynare automatically transforms the model in the form with one lead and one lag using auxiliary variables
- For example, if there is a variable with two leads  $x_{t+2}$ :
  - create a new auxiliary variable a
  - ightharpoonup replace all occurrences of  $x_{t+2}$  by  $a_{t+1}$
  - $\blacktriangleright$  add a new equation:  $a_t = x_{t+1}$

#### 3.4.2 Newton Method (1)

- The following slides aim to provide an intuition for the Newton method used by the perfect foresight solver in Dynare
- Start from an initial guess  $Y^{(0)}$ , where  $Y = [y'_1 \ y'_2 \ \dots \ y'_T]'$
- Iterate: Updated solutions  $Y^{(k+1)}$  are obtained by solving a linear system

$$F(Y^{k}) + \left[\frac{\partial F}{\partial Y}\right](Y^{(k+1)} - Y^{(k)}) = 0$$

#### 3.4.2 Newton Method (2)

■ Terminal condition for the solver:

$$\|Y^{(k+1)} - Y^{(k)}\| < \epsilon_Y$$

or

$$\|F(Y^{(k)})\| < \epsilon_F$$

- $\blacksquare$  Convergence may never happen if function is ill-behaved or initial guess  $Y^{(0)}$  is too far from solution
  - $\Rightarrow$  to avoid an infinite loop, abort after a given number of iterations

### 3.4.2 Newton Method (3)

- The following options to the perfect\_foresight\_solver can be used to control the Newton algorithm:
  - ▶ maxit: Maximum number of iterations before aborting (default: 50)
  - ▶ tolf: Convergence criterion based on function value ( $\epsilon_{\rm F}$ ) (default:  $10^{-5}$
  - ▶ tolx: Convergence criterion based on change in function argument  $(\epsilon_Y)$  (default:  $10^{-5}$ )
  - ► stack\_solver\_algo: Select between the different flavors of Newton algorithms

#### Outline

- 3 Introduction to Dynare
- 3.1 What is Dynare's
- 3.2 Implementing a Model in Dynare
- 3.3 Steady State in Dynare
- 3.4 Deterministic Simulations in Dynare
- 3.5 Perfect Foresight Setup in Dynare
- 3.6 Remarks and Examples
- 3.7 Macro Processor

#### 3.5.1 Introduction

- In order to perform the deterministic simulation, one has to specify:
  - $\blacktriangleright$  The constraints of the stacked system  $y_0, y_{T+1}$  and  $u_1, \dots, u_T$
  - ightharpoonup Provide an initial guess  $y_1, \dots, y_T$  for the Newton algorithm
- The path for the endogenous and exogenous variables are stored in two MATLAB/Octave matrices:
  - ightharpoonup oo\_.endo\_simul =  $(y_0 \ y_1 \ \dots \ y_T \ y_{T+1})$
  - ightharpoonup oo\_.exo\_simul' =  $(y_0 \ y_1 \ \dots \ y_T \ y_{T+1})$
- The perfect\_foresight\_setup initializes those matrices, given the shocks, initval, endval and histval blocks
- Then, the perfect\_foresight\_solver replaces  $y_1, \ldots, y_T$  by the solution



### 3.5.2 Transition from an Initial to a Terminal Steady State (1)

- The following slides examine a specific type of deterministic simulation, which is needed in the DGE-CRED framework
- The DGE-CRED Model allows its user to investigate:
  - ▶ The trajectories of the endogenous variables
  - ▶ Given the parameter values and pathways of the exogenous variables
- It is assumed that the economy is:
  - ▶ In an inital steady state at the beginning of the model period (t = 0)
  - ▶ Transits towards a new steady state in the terminal period (t = T + 1)

### 3.5.2 Transition from an Initial to a Terminal Steady State (2)

- In order to implement this specific type of deterministic simulation, the following can be conducted in Dynare:
  - ▶ Use a steady state file. This enables a steady state computation for varying values of the exogenous variables and allows using numeric solvers.
  - ▶ Declare the initial values of the exogenous variables in an initval block followed by steady.
  - ▶ Declare the terminal values of the exogenous variables in an endval block followed by steady.
  - ▶ Note: This is basically the same idea as presented in "approach 3" of the section covering the steady state calculation.



### 3.5.2 Transition from an Initial to a Terminal Steady State (3)

- The initial steady state values are determined based on the values of the exogenous variables assigned in the initval block
  - ► These values are then stored as initial values in oo\_.endo\_simul and oo\_.exo\_simul
- The terminal steady state values are determined based on the values of the exogenous variables assigned in the endval block
  - ► These values are then stored as terminal values as well as initial guess for the numerial solver in oo\_.endo\_simul and oo\_.exo\_simul



### 3.5.2 Transition from an Initial to a Terminal Steady State (4)

Example: The economy starts from the initial steady state, where  $A_0 = 1$ . In the terminal steady state, the total factory productivity is 10% ( $A_{T+1} = 1.1$ ) higher.

```
initval;
A = 1;
end;
steady:
endval;
A = 1.1;
end;
steady;
```

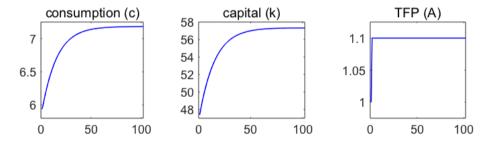
3.5.2 Transition from an Initial to a Terminal Steady State (5)

■ In order to run the deterministic simulation for T = 100 periods, enter:

```
perfect_foresight_setup(periods=100);
perfect_foresight_solver;
```

### 3.5.2 Transition from an Initial to a Terminal Steady State (6)

■ The following trajectories are obtained:





#### 3.5.3 The initval Block (1)

- While the previous slides examined the usage of the initval and endval block in combination with steady, these blocks have more functionalities than encountered so far
- In presence of the initval and absence of other blocks:
  - ▶ oo\_.endo\_simul and oo\_.exo\_simul variables storing the endogenous and exogenous variables will be filled with the values provided by this block
  - ▶ It will therefore provide the initial and terminal conditions for all the endogenous and exogenous variables
  - ▶ For the intermediate simulation periods it provides the starting values for the solver
- It is important to be aware that if some variables, endogenous or exogenous, are not mentioned in the initval block, a zero value is assumed



#### 3.5.3 The initval Block (2)

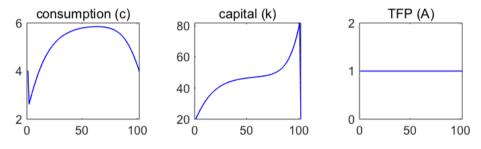
Example: Let us assume that we want to set  $c_0 = c_{T+1} = 4$  and  $k_0 = k_{T+1} = 20$  in the neoclassical growth model. Furthermore, we assume that TFP is constant at  $A_t = 1$ .

```
initval;
c = 4;
k = 20;
A = 1;
end;
```

■ Note that the purpose of this example is to illustrate the usage of the initval block, rather than addressing a meaningful question.

### 3.5.3 The initval Block (3)

■ The following trajectories are obtained:



- Comments:
  - $\blacktriangleright$  As consumption is a forward looking variable in this model, its initialization  $c_0$  does not affect the trajectory. However, its terminal value does.
  - ▶ The opposite holds for capital.



#### 3.5.4 The endval Block (1)

- In the absence of an initval block, the endval block fills both oo\_.endo\_simul and oo\_.exo\_simul
  - ▶ In this case it, therefore, has the same effect as if only an initval block was present
- However, if an initval and endval block are both present:
  - ▶ The former assigns the initial conditions in t = 0
    - While the latter provides the terminal conditions in t = T + 1 as well as the initial guess for the perfect foresight solver
- Example: Let us assume that we want to set  $c_0 = 4$ ,  $c_{T+1} = 6$ ,  $k_0 = 20$ ,  $k_{T+1} = 30$  and  $A_t = 1$
- As before, the purpose of this example is to illustrate the usage of the endval block, rather than addressing a meaningful question

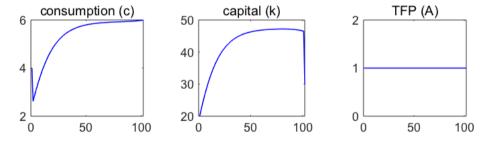
## 3.5.4 The endval Block (2)

■ Leading the following code:

```
initval;
c = 4;
k = 20;
A = 1;
end;
endval;
c = 6;
k = 30;
A = 1;
end;
```

### 3.5.4 The endval Block (3)

■ The following trajectories are obtained:



■ Comment: As in the previous example, consumption is forward looking, while capital is backward looking.



#### 3.5.5 The histval Block (1)

- The histval block assigns the initial condition, while the initval block provides the terminal condition and inital guess for the perfect foresight solver
- The usage of the histval block is particularly interesting, if there are variables with more than one lead or lag
- In a deterministic simulation the histval block must be combined with an initval block
- A histval and endval block cannot be combined



#### 3.5.5 The histval Block (2)

■ The previous example can, therefore, also be implemented by:

```
histval;
c(0) = 4;
k(0) = 20;
A(0) = 1;
end;
initval;
c = 6;
k = 30;
A = 1;
end;
```

#### Introduction (1)

- For deterministic simulations, the shocks block specifies temporary changes in the value of exogenous variables
- For permanent shocks, use an endval block
- It is possible to specify shocks which last several periods and which can vary over time
  - ▶ The periods keyword accepts a list of several dates or date ranges, which must be matched by as many shock values in the values keyword
- Note that a range in the periods keyword can be matched by only one value in the values keyword
  - ▶ If values represents a scalar, the same value applies to the whole range
  - ▶ If values represents a vector, it must have as many elements as there are periods in the range —

Introduction (2)

■ The shock block has the following structure:

```
shocks;
var ...;
periods ...;
values ...;
end;
```

Example No. 1 (1)

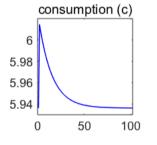
Scenario: The economy starts from the steady state. There is an unexpected temporary positive productivity shock at the beginning of period 1:  $A_1 = 1.1$ .

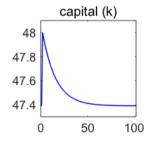
```
A = 1;
end:
steady;
shocks;
var A;
periods 1;
values 1.1;
end:
```

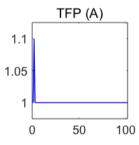
initval;

Example No. 1 (2)

■ The following trajectories are obtained:







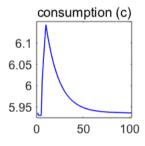
Example No. 2 (1)

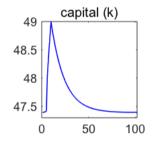
■ Scenario: The economy starts from the steady state. There is a sequence of shocks to  $A_t$ : 10% in period 5 and an 5% during the 4 following periods.

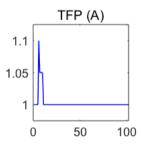
```
initval;
A = 1;
end:
steady;
shocks;
var A;
periods 5, 6:9;
values 1.1, 1.05;
end:
```

Example No. 2 (2)

■ The following trajectories are obtained:







#### Outline

- 3 Introduction to Dynare
- 3.1 What is Dynare?
- 3.2 Implementing a Model in Dynare
- 3.3 Steady State in Dynare
- 3.4 Deterministic Simulations in Dynare
- 3.5 Perfect Foresight Setup in Dynare
- 3.6 Remarks and Examples
- 3.7 Macro Processor



#### 3.6.1 Remarks

- Because of the various functions of the initval, endval and histval blocks, it is strongly recommended to check the constructed oo\_.endo\_simul and oo\_.exo\_simul variables after running perfect\_foresight\_setup and before running perfect\_foresight\_solver
- simul (periods = T) executes both, perfect\_foresight\_setup and perfect\_foresight\_solver at the same time and can also be used
- The following slides cover two examples based on the neoclassical growth model
  - ▶ It is recommendable to take a look at the file Introduction\_Dynare.mod while proceeding with these examples



#### 3.6.2 Example No. 1 (1)

■ Scenario: Return to equilibrium starting from  $k_0 = 0.5\bar{k}$  and  $c_0 = 0.5\bar{c}$ .

```
initval;
A = 1:
end;
steady;
ik = varlist indices('k', M .endo names);
ic = varlist_indices('c', M_.endo_names);
kstar = oo .steady state(ik);
cstar = oo .steady state(ic);
```

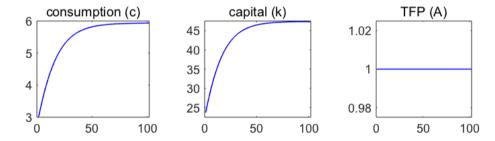
### 3.6.2 Example No. 1 (2)

#### **...** continued:

```
histval;
A(0) = 1;
k(0) = kstar/2;
c(0) = cstar/2;
end;
```

## 3.6.2 Example No. 1 (3)

■ The following trajectories are obtained:



#### 3.6.2 Example No. 2 (1)

■ Scenario: The economy starts from the initial steady state. In period 6, TFP increases by 10% permanently.

```
initval;
A = 1:
end;
steady;
endval;
A = 1.1;
end;
steady;
```

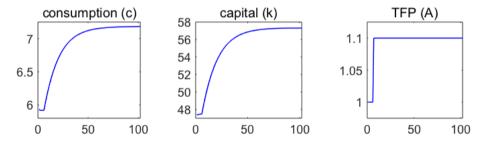
#### 3.6.2 Example No. 2 (2)

■ A shock block is used to maintain TFP at its initial level during periods 1-5.

```
shocks;
var A;
periods 1:5;
values 1;
end;
```

#### 3.6.2 Example No. 2 (3)

■ The following trajectories are obtained:



#### Outline

- 3 Introduction to Dynare
- 3.1 What is Dynare's
- 3.2 Implementing a Model in Dynare
- 3.3 Steady State in Dynare
- 3.4 Deterministic Simulations in Dynare
- 3.5 Perfect Foresight Setup in Dynare
- 3.6 Remarks and Examples
- 3.7 Macro Processor

# 3.7.1 Macro-processing Language (1)

- So far, we have encountered the Dynare language (used in mod-files), which is well suited for many economic models.
  - ▶ The Dynare language is a markup language for MATLAB/Octave that defines models,
  - ▶ but itself lacks a programmatic element.
- The Dynare macro language adds a programmatic element to Dynare.
  - ▶ It allows to replicate blocks of equations through loops (for structure), conditionally executing some code (if/then/else structure), writing indexed sums or products inside equations, etc.
  - ▶ It is used to speed model development,
  - ▶ and useful in various situations. Examples: Multi-region models, creation of modular mod-files, variable flipping, conditional inclusion of equations, etc.

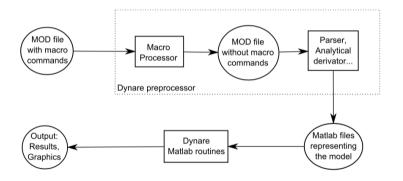
# 3.7.1 Macro-processing Language (2)

- The Dynare macro language provides a new set of macro commands that can be used in mod-files
- Technically, this macro language is totally independent of the basic Dynare language, and is processed by a seperate component of the Dynare pre-processor
- This macro processor transforms a mod-file with macros into a mod-file without macros (doing text expansion/inclusions) and then feeds it to the Dynare parser
- The key point is to understand that the macro processor only does text substitution (like the C preprocessor or the PHP language)



# 3.7.1 Macro-processing Language (3)

■ The flowchart below illustrates the relation between the Dynare macro language, macro processor, Dynare language and MATLAB/Octave



# 3.7.2 Introduction to the Syntax (1)

- The macro-processor is invoked by placing macro directives in the mod-file
- Directives begin with: @#
- The main directives are:
  - ▶ @#include: file inclusion
  - ▶ @#define: definition of a macro processor variable
  - ▶ @#if, @#ifdef, @#ifndef, @#else, @#endif: conditional statements
  - ▶ @#for/@#endfor: loop statements
- Most directives fit on one line
- If needed however, two backslashes at the end of a line indicate that the directive is continued on the next line



## 3.7.2 Introduction to the Syntax (2)

- The macro processor has its own list of variables which are different than model variables and MATLAB/Octave variables
- There are 4 types of macro-variables:
  - integer
  - ▶ string
  - ▶ integer array
  - ▶ string array
- Note that there is no boolean type:
  - ▶ false is represented by integer zero
  - ▶ true is any non-zero integer
- As the macro-processor cannot handle non-integer real numbers, integer division results in the quotient with the fractional part truncated (hence,

$$5/3 = 3/3 = 1$$

# 3.7.2 Introduction to the Syntax (3)

- The following slides introduce the directives used in the DGE-CRED model
  - ▶ In order to be able to use and modify the DGE-CRED, it is sufficient to master these commands
- The sources listed below encompass a comprehensive explanation of the entire syntax of the macro language:
  - ▶ Villemot, S. and H. Bastani: "The Dynare Macro Processor Dynare Summer School 2019"
  - ▶ Chapter 4.24 in Dynare Reference Manual Version 4



# 3.7.2 Introduction to the Syntax (4)

■ The value of a macro-variable can be defined with the @#define directive @#define Regions = 3

- Macro-expressions can be used in two places:
  - ▶ Inside a macro directive; no special markup is required (as in the example above)
  - ▶ In the body of the mod-file, between an at sign and curly braces (like @expr); the macro processor will substitute the expression with its value:

```
parameters z;
z = @{Regions};
```

In the example above the value of 3 is assigned to parameter z



# 3.7.2 Introduction to the Syntax (5)

- The include directive simply inserts the text of another file in its place @#include "ModFiles/DGE\_CRED\_Model\_Equations.mod"
- It is equivalent to copy/paste of the content of the included file
- Note that it is possible to nest includes (i.e. to include a file with an include file)
- Files to include are searched for in the current directory. Other directories can be added with the @#includepath directive

# 3.7.2 Introduction to the Syntax (6)

- Loops can be implemented using the @#for...@#endfor directive
- In a model encompassing multiple regions, loops can faciliate setting up a model block:

# 3.7.2 Introduction to the Syntax (7)

- The previous example also illustrates a great advantage of the macro language compared to the MATLAB/Ocatve syntax
  - ▶ In MATLAB it is not possible to change the index of a variable, for example  $Y_r, K_r, L_r$
  - ▶ Intuition: The Dynare macro as well as basic language rather have the character of a text than code, which is then transforemed by Dynare and MATLAB into a code
  - ▶ It is also possible to use the MATLAB syntax directly in a mod-file. Dynare simply does not have to translate this part of the file further



# 3.7.2 Introduction to the Syntax (8)

- The most basic conditional directive is the if-statement
  - ▶ It is executed by the directive @#if, ..., @#else, @#endif

```
@#define RCP_scenario = 4.5 // choose: 4.5 or 8.5
parameters Temp_2100;
...
@#if RCP_scenario == 4.5
    Temp_2100 = 2.3;
@#else
    Temp_2100 = 3.9;
@#endif
```

## 3.7.2 Introduction to the Syntax (9)

- In the example on the previous slide, Temp\_2100 is a parameter representing the temperature in 2100
  - ▶ Its value is assigned using a conditional statement
- The lines between @#if, @#else or @#endif are executed only if the condition evaluates to a non-null integer (i.e. is true)
- The @#else branch is optional and, if present, is only evaluated if all other conditions evaluate to 0 (i.e. do not hold)

## Outline

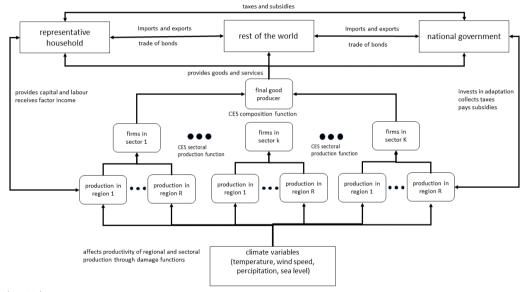
- **1** DGE-CRED Model
- 4.1 Introduction
- 4.2 Folder Structure
- 4.3 Demand
- 4.4 Production
- 4.5 Climate Variables
- 4.6 Aggregation and Identities

## 4.1 Introduction

- Dynamic general equilibrium (DGE) model with optimizing agents.
- Differentiates between several regions and main economic activities.
- Our model is implemented in the open source environment Dynare and can be run using Matlab or Octave.
  - ▶ Sectors in the model correspond to economic activities and the classification by the General Statistical Office (GSO).
  - ▶ Regions are based on the statistical regions.
- We extend the approach by Nordhaus 1993 to model the impact of climate change through damage functions.



## 4.1 Model Structure



## Outline

- **1** DGE-CRED Model
- 4.1 Introduction
- 4.2 Folder Structure
- 4.3 Demand
- 4.4 Production
- 4.5 Climate Variables
- 4.6 Aggregation and Identities

### 4.2.1 Main Folder Structure

- The main file containing all necessary mod-files is DGE\_CRED\_Model.mod.

  This file includes the following files stored in the ModFiles folder
- Subroutines responsible for finding the initial and terminal conditions are located in the subfolder Functions
- To define scenarios and structural parameters you need to create an Excel file located in the subfolder ExcelFiles

#### 4.2.2 Mod Files

- The main file containing all necessary mod-files is DGE\_CRED\_Model.mod. This file includes the following files stored in the ModFiles folder:
  - ▶ DGE\_CRED\_Model\_Declarations.mod declares all endogenous and exogenous variables of the model and structural parameters.
  - ▶ DGE\_CRED\_Model\_Parameters.mod assigns values to the structural parameters of the model.
  - ▶ DGE\_CRED\_Model\_Equations.mod contains the equations of the model.
  - ▶ DGE\_CRED\_Model\_LatexOutput.mod produces latex output for documentation of the declared variables and model equations.
  - ▶ DGE\_CRED\_Model\_SteadyState.mod computes initial and terminal condition for the dynamic simulation.
  - ▶ DGE\_CRED\_Model\_Simulations.mod starts the dynamic simulation.



#### 4.2.3 Functions

- Subroutines responsible for finding the initial and terminal conditions are located in the subfolder Functions:
  - ▶ Calibration.mat finds the initial conditions to reflect a specific year of the economy.
  - ► FindA.mat looks for exogenous productivity shocks across sectors and regions to meet the terminal conditions.
  - ▶ FindK.mat looks for a capital allocation across sectors and regions to fulfill the static equations of the model.
  - ▶ rng.mat random number generator function necessary for Octave users.
  - ▶ LoadExogenous.mat reads exogenous variables for different scenarios.



#### 4.2.4 Excel Files

- To define scenarios and structural parameters you need to create an Excel file located in the subfolder ExcelFiles:
  - ► ModelSimulationandCalibrationforKSectorsandRregions.xlsx has multiple sheets:
    - ▶ initial Start
    - terminal Terminal
    - parameters to define rigidity parameters Dynamics
    - elasticity parameters and tax rates Structural Parameters
    - coefficients for regional and sector specific damage functions Climate Damage Functions (Labour, Capital, TFP)
    - ► Baseline scenario and other optional scenario sheets Adaptation and Extremes defining paths for exogenous variables
    - ▶ Data to load external data sources



#### 4.2.5 Mod Files

- We will now define and implement all model equations into Dynare.
- For each Equation we will explain its derivation and how to implement it.
- The folder ModFiles contains the file DGE\_CRED\_Model\_Equations.mod.
- DGE\_CRED\_Model\_Equations.mod contains all model equations.
- We need to use the symbols defined in DGE\_CRED\_Model\_Declarations.mod.
- Please add the missing equations in DGE\_CRED\_Model\_Equations\_missing.mod.



## Outline

- **4** DGE-CRED Model
- 4.1 Introduction
- 4.2 Folder Structure
- 4.3 Demand
- 4.4 Production
- 4.5 Climate Variables
- 4.6 Aggregation and Identities

### 4.3.1 Households

- Representative households h providing labour N and capital K to domestic firms f
- Maximize discounted utility over an infinite horizon by choosing consumption  $C_t(h)$ , capital  $K_{k,r,t+1}(h)$ , investments  $I_{k,r,t}(h)$ , labour  $N_{k,r,t}(h)$  and foreign net wealth  $B_{t+1}$
- Optimization problem of the representative household is

$$\begin{split} \max_{C_{t}(h),\,K_{k,r,t+1}(h),\,I_{k,r,t}(h),\,N_{k,r,t}(h),\,B_{t+1}} \sum_{t=0}^{\infty} \beta^{t} \left( \frac{C_{t}(h)^{1-\sigma^{C}}}{1-\sigma^{C}} - \sum_{k=1}^{K} \sum_{r=1}^{R} A_{k,r,t}^{N} \phi_{k,r}^{L} \frac{N_{k,r,t}(h)^{1+\sigma^{L}}}{1+\sigma^{L}} \right) \\ \text{s.t.} \quad P_{t} \, C_{t}(h) \, (1+\tau^{C}) + \sum_{k=1}^{K} \sum_{r=1}^{R} P_{k,r,t} I_{k,r,t}(h) + B_{t+1}(h) = \\ \sum_{k=1}^{K} \sum_{r=1}^{R} (1-\tau^{N}) \, W_{k,r,t} N_{k,r,t}(h) + \sum_{k=1}^{K} \sum_{r=1}^{R} P_{k,r,t} \, r_{k,r,t} \, (1-\tau^{K}) \, K_{k,r,t}(h) + S_{t}^{f} \, \phi_{t}^{B} \, (1+r_{t}^{f}) \, B_{t}(h) \\ \text{and} \quad K_{k,r,t+1} = (1-\delta-D_{k,r,t}^{K}) \, K_{k,r,t} - I_{k,r,t} \, \Gamma\left(\frac{I_{k,r,t}}{I_{k,r,t-1}}\right). \end{split}$$

## 4.3.2 Households Lagrangian

■ We set-up the Lagrangian for the optimization problem to derive the first order conditions.

$$\begin{split} &\sum_{t=0}^{\infty} \beta^t \Bigg[ \left( \frac{C_t(h)^{1-\sigma^C}}{1-\sigma^C} - \sum_{k=1}^K \sum_{r=1}^R A_{k,r,t}^N \phi_{k,r}^L \frac{N_{k,r,t}(h)^{1+\sigma^L}}{1+\sigma^L} \right) \\ &- \lambda_t(h) \Big( P_t \, C_t(h) \, (1+\tau^C) + \sum_{k=1}^K \sum_{r=1}^R P_{k,r,t} I_{k,r,t}(h) + B_{t+1}(h) - \sum_{k=1}^K \sum_{r=1}^R (1-\tau^N) \, W_{k,r,t} N_{k,r,t}(h) \\ &- \sum_{k=1}^K \sum_{r=1}^R P_{k,r,t} \, r_{k,r,t} \, (1-\tau^K) \, K_{k,r,t}(h) - S_t^f \, \phi_t^B \, (1+r_t^f) \, B_t(h) \Big) \\ &- \sum_{k=1}^K \sum_{r=1}^R \lambda_t(h) \omega_{k,r,t}^I(h) \, \bigg\{ K_{k,r,t+1} - (1-\delta - D_{k,r,t}^K) \, K_{k,r,t} - I_{k,r,t} \, \Gamma \left( \frac{I_{k,r,t}}{I_{k,r,t-1}} \right) \bigg\} \, \Bigg]. \end{split}$$

## 4.3.3 Households First Order Conditions – Intratemporal

■ Marginal utility of consumption

$$\lambda_{\rm t} = \frac{C_{\rm t}(h)^{-\sigma^{\rm C}}}{P_{\rm t}(1+\tau^{\rm C})}$$

Labour supply curve

$$\phi_{k,r}^{L}\,A_{k,r,t}^{N}\,N_{k,r,t}(h)^{\sigma^{L}} = \lambda_{t}(h)\,W_{k,r,t}\,(1-\tau^{N})$$

# 4.3.4 Implementation of Households First Order Conditions – Intratemporal

```
model;
...

@# for sec in 1:Sectors

@# for reg in 1:Regions
...

[name = 'HH FOC labour', mcp = 'N_@{sec}_@{reg}>0']

(1 - tauN_p)*W_@{sec}_@{reg}*(P*C/PoP)^(-sigmaC_p)/(1+tauC_p) =

A_N_@{sec}_@{reg}*phiL_@{sec}_@{reg}_p*(N_@{sec}_@{reg})^(sigmaL_p);
...

@# endfor // end loop over regions

@# endfor // end loop over sectors
...
end;
```

## 4.3.5 Households First Order Conditions – Intertemporal

Euler equation for capital

$$\lambda_{t+1}(h)\beta\left(P_{k,r,t+1} r_{k,r,t+1} (1-\tau^K) + (1-\delta - D_{k,r,t+1}^K) \omega_{k,r,t+1}^I\right) = \lambda_t(h)\omega_{k,r,t}^I$$

Euler equation for investment

$$P_{k,r,t} \lambda_t(h) = \lambda_t(h) \omega_{k,r,t}^I \left( \Gamma(\frac{I_{k,r,t}}{I_{k,r,t-1}}) + \frac{\partial \Gamma(\frac{I_{k,r,t}}{I_{k,r,t-1}})}{\partial (\frac{I_{k,r,t}}{I_{k,r,t-1}})} \frac{I_{k,r,t}}{I_{k,r,t-1}} \right) - \beta \lambda_{t+1}(h) \omega_{k,r,t+1}^I \frac{\partial \Gamma(\frac{I_{k,r,t+1}}{I_{k,r,t}})}{\partial (\frac{I_{k,r,t+1}}{I_{k,r,t}})} \left( \frac{I_{k,r,t+1}}{I_{k,r,t}} \right)$$

■ Investment adjustment cost

$$\Gamma(\frac{I_{k,r,t}}{I_{k,r,t-1}}) = 3 - \exp\left\{\sqrt{\phi^{K}/2} \left(\frac{I_{k,r,t}}{I_{k,r,t-1}} - 1\right)\right) - \exp\left\{-\sqrt{\phi^{K}/2} \left(\frac{I_{k,r,t}}{I_{k,r,t-1}} - 1\right)\right\}$$



# 4.3.6 Implementation of Households First Order Conditions – Intertemporal (1)

```
# Gamma @\{sec\} @\{reg\} = (3 - (exp(sqrt(phiK p/2)*(I @\{sec}) @\{reg\}/I @\{sec}) @\{reg\}(-1)-1))
                                            +\exp(-\operatorname{sqrt}(\operatorname{phiK} p/2)*(I @{\sec} @{\operatorname{reg}}/I @{\sec} @{\operatorname{reg}}(-1)-1))));
\# Gammapr @\{sec\} @\{reg\} = -I @\{sec\} @\{reg\}/I @\{sec\} @\{reg\}(-1)*sqrt(phiK p/2)*
                                                   (\exp(\operatorname{sqrt}(\operatorname{phiK} \ p/2)*(I \ @\{\sec\} \ @\{\operatorname{reg}\}/I \ @\{\sec\} \ @\{\operatorname{reg}\}(-1)-1))
                                                   -\exp(-\operatorname{sqrt}(\operatorname{phiK} \ p/2)*(I \ @\{\sec\} \ @\{\operatorname{reg}\}/I \ @\{\sec\} \ @\{\operatorname{reg}\}(-1)-1)));
# Gammaprp1 @{sec} @{reg} = I @{sec} @{reg}(+1)^2/(I @{sec} @{reg})^2*sqrt(phiK p/2)*
                                                         (\exp(\operatorname{sqrt}(\operatorname{phiK} p/2)*(I @{\operatorname{sec}} @{\operatorname{reg}}(+1)/I @{\operatorname{sec}} @{\operatorname{reg}}-1))
                                                         -\exp(-\operatorname{sqrt}(\operatorname{phiK} \ p/2)*(I \ @\{\sec\} \ @\{\operatorname{reg}\}(+1)/I \ @\{\sec\} \ @\{\operatorname{reg}\}-1))
\# \text{ Gammapl @} \{ \sec \} \ @ \{ \operatorname{reg} \} \ = \ (3 - (\exp(\operatorname{sqrt}(\operatorname{phi} K \ p/2) * (I \ @ \{ \operatorname{sec} \} \ @ \{ \operatorname{reg} \} / I \ @ \{ \operatorname{sec} \} \ @ \{ \operatorname{reg} \} (-1) - 1)
                                                 +\exp(-\operatorname{sqrt}(\operatorname{phiK} \ p/2)*(I \ @\{\operatorname{sec}\} \ @\{\operatorname{reg}\}/I \ @\{\operatorname{sec}\} \ @\{\operatorname{reg}\}(-1)-1))));
```

# 4.3.6 Implementation of Households First Order Conditions – Intertemporal (2)

```
[name = 'HH FOC capital', mcp = 'K @{sec} @{reg} > 0']
  (C(+1)/PoP(+1))^{-(-sigmaC-p)/(P(+1)*(1+tauC-p))*beta-p*r @{sec} @{reg}(+1)*P @{reg}(+1)*P @{reg}(+1)*P @{reg}(+1)*P @{reg}
                 \{(+1)*(1 - \text{tauK p})\}
+ (C(+1)/PoP(+1))^{-sigmaC} p)/(P(+1)*(1+tauC p))*omegaI @{sec} @{reg}(+1)
* beta p*(1 - delta p - D K @{sec} @{reg}(+1))
= omegaI @{sec} @{reg}*(C/PoP)^(-sigmaC p)/(P*(1+tauC p));
 [name = 'HH FOC investment', mcp = 'I @{sec} @{reg} > 0']
 (C/PoP)^{-(-sigmaC p)/(P*(1+tauC p))*P @{sec} @{reg} =
 (C/PoP)^{-sigmaC} p)/(P*(1+tauC p))*omegaI @{sec} @{reg}*(Gamma @{sec} @{reg}+Gammapr @{sec})
                 } @{reg})
+ \text{ beta } p*(C(+1)/PoP(+1))^(-sigmaC p)/(P(+1)*(1+tauC p))*omegaI @{sec} @{reg}(+1)*
                 Gammaprp1 @{sec} @{reg}:
 [name = 'LOM \ capital', mcp = 'I \ @{sec} \ @{reg} > 0']
```

## 4.3.7 Rest of the world

■ Euler equation foreign bonds

$$\lambda_{t+1} \, \beta \, S_{t+1}^{f} \, \phi_{t+1}^{B} \left(1 + r^{f}_{t+1}\right) = \lambda_{t}$$

- Effective exchange rate S<sup>f</sup> and the world interest rate r<sup>f</sup>.
- The required interest rate is above the world interest rate if the foreign debt  $(B_{t+1} < 0)$  foreign claims  $(B_{t+1} > 0)$  relative to GDP increases/decreases and future net exports relative to GDP will decrease.

$$\phi_{t+1}^{B} = \exp\left(-\phi^{B}\left(S_{t+1}^{f}\,r_{t+1}^{f}\,\frac{B_{t+1}}{Y_{t+1}} + \frac{NX_{t+1}}{Y_{t+1}}\right)\right)$$



# 4.3.8 Implementation Rest of the World

```
... [name = 'Foreign Assets'] ...
```

## 4.3.9 Government Budget Constraint

- We are interested in different policy measures taken by the government to adapt to a new climate regime.
- Government behaviour is not a result of an optimization problem.

$$G_{t} + \sum_{k}^{K} \sum_{r}^{R} \sum_{z}^{Z} G_{k,r,t}^{A,z} + B_{t+1}^{G} = \sum_{k}^{K} \sum_{r}^{R} \left\{ (\tau^{K} + \tau_{r,k,t}^{K}) P_{k,r,t} r_{k,r,t} K_{k,r,t} + (\tau^{N} + \tau_{k,r,t}^{N}) W_{k,r,t} N_{k,r,t} Pop_{t} \right\} + (1 + r_{t}^{f}) S_{t}^{f} \phi_{t}^{B} B_{t}^{G}$$

# 4.3.10 Implementation of Government Budget Constraint

```
[name = 'Government Budget Constraint']
G+BG
@# for sec in 1:Sectors
@# endfor
= (1+rf)*Sf*exp(-phiB p*((Sf*rf*B(-1)/Y+NX/Y)))*BG (-1)+tauC p*C
@# for sec in 1:Sectors
@# endfor
[name = 'Government Budget Deficit']
BG = exo BG;
```

## 4.3.11 Government Policy Instruments

■ Governments can invest into adaptation capital stocks

$$K_{k,r,t+1}^{A,z} = \eta_{k,r,t}^{A,z}$$

■ Evolution of adaptation capital stocks

$$K_{k,r,t+1}^{A,z} = (1 - \delta_{K^{A,z},k,r}) K_{k,r,t}^{A,z} + G_{k,r,t}^{A,z}$$

■ Tax on capital expenditures paid by firms

$$\tau_{k,r,t}^K = \tau_{k,r,0}^K + \eta_{k,r,t}^{\tau^K}$$

■ Tax rate on wage bill paid by firms

$$\tau_{k,r,t}^N = \tau_{k,r,0}^N + \eta_{k,r,t}^{\tau^N}$$

## 4.3.12 Implementation of Government Policy Instruments

```
@# for z in ["T", "WS", "PREC", "SL", "CYC", "DRO"]
 [name = 'sector specific adaptation expenditures by the government against sea level rise
 [name = 'sector specific adaptation capital against sea level rise ']
@# endfor
[name = 'sector specific corporate tax rate paid by firms']
[name = 'sector specific labour tax rate paid by firms']
```

## 4.3.13 Resource constraint

Households and government use domestic final goods  $Y_t$  produced by firms for consumption, investment and for exports  $X_t$  and can also use imports  $M_t$  for consumption and investment

$$Y_t = C_t + I_t + G_t + \underbrace{X_t - M_t}_{NX_t} \tag{1}$$

■ The aggregation of the budget constraints of the representative households also states that positive net exports are used to increase net financial wealth to the rest of the world.

$$NX_{t} = B_{t+1} - (1 + r_{t}^{f})S_{t}^{f}\phi_{t}^{B}B_{t}$$
 (2)

### 4.3.14 Implementation of Resource Constraint

```
...

[name = 'Resource Constraint']

Y = C + I + G + NX

@# for sec in 1:Sectors

@# endfor

;

[name = 'Net Exports']

NX = (B - (1 + rf) * exp(-phiB_p*((Sf*rf*B(-1)/Y+NX/Y))) * Sf * B(-1));

...
```

#### Outline

- **1** DGE-CRED Model
- 4.1 Introduction
- 4.2 Folder Structure
- 4.3 Demand
- 4.4 Production
- 4.5 Climate Variables
- 4.6 Aggregation and Identities

### 4.4.1 Sectoral Decomposition

Final domestic goods  $Y_t$  are created combining goods from different sectors  $Y_{k,t}$  using a CES production function.

$$\min_{\mathbf{Y}_{\mathbf{k},\mathbf{t}}} \sum_{\mathbf{k}} \mathbf{Y}_{\mathbf{k},\mathbf{t}} \, \mathbf{P}_{\mathbf{k},\mathbf{t}} \tag{3}$$

$$Y_{t} = \left(\sum_{k} \omega_{k}^{Q} \frac{1}{\eta^{Q}} Y_{k,t}^{\frac{\eta Q}{\eta Q}}\right)^{\frac{\eta^{Q}}{\eta^{Q} - 1}}$$

$$\tag{4}$$

■ Therefore, the demand for sectoral products correspond to the first order conditions of the above optimization problem.

$$\frac{P_{k,t}}{P_t} = \omega_k^{Q \frac{1}{\eta^{Q}}} \left( \frac{Y_{k,t}}{Y_t} \right)^{\frac{-1}{\eta^{Q}}}$$



# 4.4.2 Implementation of Sectoral Decomposition

```
... [name = 'demand for sector output']
...
```

# 4.4.3 Regional Decomposition

In order to model regional economic activity we further decompose the production process on a regional level.

$$\begin{split} \min_{\mathbf{Y_{k,r,t}}} \sum_{\mathbf{k}} \mathbf{Y_{k,r,t}} \, \mathbf{P_{k,r,t}} \\ \mathbf{Y_{k,t}} &= \left( \sum_{\mathbf{k}} \omega_{\mathbf{k,r}}^{\mathbf{Q}} \frac{1}{\eta_{\mathbf{k}}^{\mathbf{Q}}} \mathbf{Y}_{\mathbf{k,r,t}}^{\frac{\mathbf{Q}-1}{\eta_{\mathbf{k}}^{\mathbf{Q}}}} \right)^{\frac{\eta_{\mathbf{k}}^{\mathbf{Q}}}{\eta_{\mathbf{k}}^{\mathbf{Q}-1}}} \end{split}$$

Demand for sectoral and regional products correspond to the first order conditions of the above optimization problem.

$$\frac{P_{k,r,t}}{P_{k,t}} = \omega_{k,r}^{Q} \frac{1}{\eta_{k}^{Q}} \left( \frac{Y_{k,r,t}}{Y_{k,t}} \right) \frac{1}{\eta_{k}^{Q}}$$

# 4.4.4 Implementation of Regional Decomposition

```
... [name = 'sector aggregate specific output']
```

### 4.4.5 Regional Production

- At the regional and sectoral level are representative firms maximizing profits using capital  $K_{k,r,t}$  and labour  $L_{k,r,t} = N_{k,r,t}$  Pop<sub>t</sub> provided by households to produce products.
- They charge a price  $P_{k,r,t}$  for their products and have to pay households wages  $W_{k,r,t}$ , interest on rented capital  $P_{r,k,t}$   $r_{r,k,t}$ , taxes related to the wage bill  $\tau_{r,k,t}^N$  and on capital expenditure  $\tau_{r,k,t}^K$ .
- Representative firms have access to a regional and sector specific constant elasticity of substitution production function.
- The productivity of capital and labour of a firm in one sector and region depends on the climate variables, and the adaption measures by the government represented by a damage function affecting total factor productivity  $A_{k,r,t}$  by

$$D_{k,r,t} = D_{k,r} \left( T_{r,t}, PREC_{r,t}, WS_{r,t}, SL_{r,t}, CYC_{r,t}, DRO_{r,t}, G_{r,k,t}^A \right).$$

- Further, we explicitly differentiate between climate induced damages affecting labour productivity  $D_{k,r,t}^N$  and capital depreciation  $D_{k,r,t}^K$ .
- As in Nordhaus 1993, we assume a polynomial functional form of the damage functions, but the damages are different across regions and sectors.



#### 4.4.6 Profit Maximization

Firms in each region and sector have access to a constant elasticity of substitution production function with production factors labour and capital.

$$\begin{split} \max_{Y_{k,r,t},N_{k,r,t},K_{k,r,t}} & P_{k,r,t} \, Y_{k,r,t} - W_{k,r,t} \, N_{k,r,t} \, \text{Pop}_t \left(1 + \tau_{k,r,t}^N \right) - r_{k,r,t} \, P_{k,r,t} \, K_{k,r,t} \left(1 + \tau_{k,r,t}^K \right) \\ \text{s.t.} \, Y_{k,r,t} &= A_{k,r,t} (1 - D_{k,r,t}) \left[ \alpha_{k,r}^N \, \frac{1}{\eta_{k,r}^{NK}} \, \left( A_{k,r,t}^N \left(1 - D_{k,r,t}^N \right) \, \text{Pop}_t \, N_{k,r,t} \right)^{\rho_{k,r}} + \alpha_{k,r}^K \, \frac{1}{\eta_{k,r}^{NK}} \, \left( K_{k,r,t} \right)^{\rho_{k,r}} \right]^{\frac{1}{\rho_{k,r}}}, \\ & \text{where } \rho_{k,r} &= \frac{\eta_k^{NK} - 1}{\eta_{NK}}. \end{split}$$

#### 4.4.7 Factor Demand

Demand for production factors are given by the first order condition of the above optimization problem. The Lagrange multiplier is equal to the price charged by companies.

$$\begin{split} \frac{W_{k,r,t}}{P_{k,r,t}} \left( 1 + \tau_{k,r,t}^N \right) &= \alpha_{k,r}^N \frac{\frac{1}{\eta_{k,r}^{NK}}}{\eta_{k,r}^{K}} \left( A_{k,r,t} \left( 1 - D_{k,r,t} \right) A_{k,r,t}^N \left( 1 - D_{k,r,t}^N \right) \right)^{\rho_{k,r}} \left( \frac{Pop_t N_{k,r,t}}{Y_{k,r,t}} \right)^{-\frac{1}{\eta_{k,r}^{NK}}} \\ r_{k,r,t} \left( 1 + \tau_{k,r,t}^K \right) &= \alpha_{k,r}^K \frac{\frac{1}{\eta_{k,r}^{NK}}}{\eta_{k,r}^{KK}} \left( A_{k,r,t} \left( 1 - D_{k,r,t} \right) \right)^{\rho_{k,r}} \left( \frac{K_{k,r,t}}{Y_{k,r,t}} \right)^{-\frac{1}{\eta_{k,r}^{NK}}} \end{split}$$

- We use the more general case of the CES production function rather than the more commonly used Cobb-Douglas production function.
- The parameter  $\eta_{k,r}^{NK}$  allows us to control the response of capital and labour demand to temporary productivity shocks.
- Temporary productivity shocks are in our set-up also weather extremes.



### 4.4.8 Implementation of Factor Demand

```
[name='sector specific output']
[name = 'Firms FOC capital', mcp = 'K_@{sec}_@{reg} > 0']
[name = 'Firms FOC labour', mcp = 'N_@{sec}_@{reg} > 0']
...
```



# 4.4.9 Damages on TFP

```
D_{k,r_t} = \left\{\right.
                       (a_{T,1,k,r} T_{rt} + a_{T,2,k,r} (T_{rt})^{a_{T,3,k,r}}) \exp(-\phi_{k,r}^{GA,T} K_{k,r,t}^{A,T}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) - I(SL > \frac{K_{k,r,t}^{A,SL}}{GA,SL}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) + (a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}) + (a_{SL,
                                                           impact of temperature
                                                                                                                                                                                                                                                                                                                                                           impact of sea level
                                                                                                                                                                                                   impact of adaptation
                          +(a_{WS,1,k,r}WS_{rt}+a_{WS,2,k,r}(WS_{rt})^{a_{WS,3,k,r}})\exp(-\phi_{k,r}^{GA,WS}K_{k,r,t}^{A,WS})
                                                                                             impact of wind speed
                                                                                                                                                                                                                                                          impact of adaptation
                           +\left(a_{\mathrm{PREC},1,k,r}\,\mathrm{PREC}_{\mathrm{rt}}+a_{\mathrm{PREC},2,k,r}\,\left(\mathrm{PREC}_{\mathrm{rt}}\right)^{a_{\mathrm{PREC},3,k,r}}\right)\,\exp(-\phi_{k,r}^{\mathrm{GA,PREC}}\mathrm{K}_{k,r}^{\mathrm{A,PREC}})
                                                                                                                      impact of precipitation
                                                                                                                                                                                                                                                                                                                                impact of adaptation
                          +\left(a_{\mathrm{CYC},1,k,r}\,\mathrm{CYC}_{\mathrm{rt}}+a_{\mathrm{CYC},2,k,r}\,\left(\mathrm{CYC}_{\mathrm{rt}}\right)^{a_{\mathrm{CYC},3,k,r}}\right)\,\exp(-\phi_{\nu,r}^{\mathrm{GA,CYC}}\,\mathrm{K}_{\nu,r}^{\mathrm{A,CYC}})
                                                                                                                  impact of cyclones
                                                                                                                                                                                                                                                                                             impact of adaptation
                          + (a_{DRO,1,k,r} DRO_{rt} + a_{DRO,2,k,r} (DRO_{rt})^{a_{DRO,3,k,r}}) \exp(-\phi_{k,r}^{GA,DRO} K_{k,r,t}^{A,DRO})
                                                                                                                  impact of droughts
                                                                                                                                                                                                                                                                                               impact of adaptation
```

impact of adaptation

# 4.4.10 Implementation of Damages on TFP

```
...
[name = 'sector specific damage function']
...
```

- Note: As  $D_{k,r,t} \in [0,1]$ , an upper bound has to be included in the code
  - $\blacktriangleright$  Due to computational constraints, the upper bound is set to 0.7 for  $D_{k,r,t}$



# 4.4.11 Damages on Labour Productivity

$$\begin{split} D_{k,r_{t}}^{N} = & \left( \underbrace{a_{T,1,k,r}^{N} T_{rt} + a_{T,2,k,r}^{N} \left( T_{rt} \right)^{a_{T,3,k,r}^{N}} + a_{SL,1,k,r}^{N} SL_{t} + a_{SL,2,k,r}^{N} \left( SL_{t} \right)^{a_{SL,3,k,r}^{N}}}_{impact of temperature} & impact of sea level \\ & + \underbrace{a_{WS,1,k,r}^{N} WS_{rt} + a_{WS,2,k,r}^{N} \left( WS_{rt} \right)^{a_{WS,3,k,r}^{N}} + \left( a_{PREC,1,k,r}^{N} PREC_{rt} + a_{PREC,2,k,r}^{N} \left( PREC_{rt} \right)^{a_{PREC,3,k,r}^{N}} \right)}_{impact of wind speed} & impact of precipitation \\ & + \underbrace{a_{CYC,1,k,r}^{N} CYC_{rt} + a_{CYC,2,k,r}^{N} \left( CYC_{rt} \right)^{a_{CYC,3,k,r}^{N}} + a_{DRO,1,k,r}^{N} DRO_{rt} + a_{DRO,2,k,r}^{N} \left( DRO_{rt} \right)^{a_{DRO,3,k,r}^{N}}}_{impact of cyclones} & impact of droughts \\ \end{pmatrix}. \end{split}$$

# 4.4.12 Implementation of Damages on Labour Productivity

```
[name = 'sector specific damage function on labour productivity']
 D N @\{sec\} @\{reg\} = min(1,aN T 1 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} + aN T 2 @\{sec\} @\{reg\} p * T @\{reg\} p
                                {reg}^(aN T 3 @{sec} @{reg} p) +
aN SL 1 @{sec} @{reg} p * SL + aN SL 2 @{sec} @{reg} p * SL^(aN SL 3 @{sec} @{reg} p) +
aN_W_1_@\{\sec\}_0\{reg\}_p * WS_0\{reg\} + aN_W_2_0\{\sec\}_0\{reg\}_p * WS_0\{reg\}^(aN_W_3_0\{\sec\}_0\{reg\}_p * WS_0[reg]^(aN_W_3_0\{\sec\}_0\{reg\}_p * WS_0[reg]^(aN_W_3_0\{\sec\}_0\{reg\}_p * WS_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]^(aN_W_3_0[reg]
                                  reg \} p) +
aN P 1 @\{sec\} @\{reg\} p * PREC @\{reg\} + aN P 2 @\{sec\} @\{reg\} p * PREC @\{reg\}^{(aN P 3 @\{sec)\}}
                              @{reg} p) +
aN DR 1 @{sec} @{reg} p * DRO @{reg} + aN DR 2 @{sec} @{reg} p * DRO @{reg}^(aN DR 3 @{sec
                                } @{reg} p) +
aN CY 1 @{sec} @{reg} p * CYC @{reg} + aN CY 2 @{sec} @{reg} p * CYC @{reg}^(aN CY 3 @{sec
                                } @{reg} p)
  );
```

■ Note: As  $D_{k,r,t}^N \in [0,1]$ , an upper bound has to be included in the code



# 4.4.13 Damages on Capital

$$\begin{split} D_{k,r_t}^K = & \left( \underbrace{ a_{T,1,k,r}^K T_{rt} + a_{T,2,k,r}^K \left( T_{rt} \right)^{a_{T,3,k,r}^K} + a_{SL,1,k,r}^K SL_t + a_{SL,2,k,r}^K \left( SL_t \right)^{a_{SL,3,k,r}^K}}_{impact of temperature} \right. \\ & \left. + a_{WS,1,k,r}^K WS_{rt} + a_{WS,2,k,r}^K \left( WS_{rt} \right)^{a_{WS,3,k,r}^K} + \underbrace{a_{PREC,1,k,r}^K PREC_{rt} + a_{PREC,2,k,r}^K \left( PREC_{rt} \right)^{a_{PREC,3,k,r}^K}}_{impact of wind speed} \right. \\ & \left. + \underbrace{a_{CYC,1,k,r}^K CYC_{rt} + a_{CYC,2,k,r}^K \left( CYC_{rt} \right)^{a_{CYC,3,k,r}^K} + a_{DRO,1,k,r}^K DRO_{rt} + a_{DRO,2,k,r}^K \left( DRO_{rt} \right)^{a_{DRO,3,k,r}^K}}_{impact of cyclones} \right. \end{split}$$

# 4.4.14 Implementation of Damages on Capital

```
[name = 'sector specific damage function on capital formation']
 D \ K \ @\{sec\} \ @\{reg\} = \min(1,aK \ T \ 1 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{sec\} \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ @\{reg\} \ p*T \ @\{reg\} + aK \ T \ 2 \ AK \ T \ 2 \ @\{reg\} + aK \ T \ 2 \ AK \ T \ 2 \ AK \ T \ 2 \ AK 
                  }^(aK T 3 @{sec} @{reg} p)+
aK SL 1 @{sec} @{reg} p*SL+aK SL 2 @{sec} @{reg} p*SL^(aK SL 3 @{sec} @{reg} p)+
aK_W_1_@\{\sec\}_0\{reg\}_p*WS_0\{reg\}_aK_W_2_0\{sec\}_0\{reg\}_p*WS_0\{reg\}^(aK_W_3_0\{sec\}_0\{reg\}_p)
aK P 1 @{sec} @{reg} p*PREC @{reg}+aK P 2 @{sec} @{reg} p*PREC @{reg}^(aK P 3 @{sec} @{reg}
                  } p)+
aK DR 1 @{sec} @{reg} p*DRO @{reg}+aK DR 2 @{sec} @{reg} p*DRO @{reg}^(aK DR 3 @{sec} @{
                     reg } p)+
aK CY 1 @{sec} @{reg} p*CYC @{reg}+aK CY 2 @{sec} @{reg} p*CYC @{reg}^(aK CY 3 @{sec} @{
                     reg} p)
);
```

■ Note: As  $D_{k,r,t}^{K} \in [0,1]$ , an upper bound has to be included in the code



#### 4.4.15 Trade with the Rest of the World

- The demand for domestic exports and foreign imports is not explicitly modeled in this version of the model.
- We assume that net exports follow an auto-regressive process of order one and that the long-run value of net exports depend on the long-run development of gross domestic product.

$$NX_{t} = \rho^{NX} NX_{t-1} + (1 - \rho^{NX}) \omega^{NX} P_{t} Y_{t} \exp(\eta_{NX_{t}})$$

- The effective exchange rate  $S_t^f$  and the world interest rate  $r_t^f$  determine how much governments and households have to pay back in domestic currency as net lender or how much they receive as net borrower to the rest of the world.
- The world interest rate is independent of domestic developments and only the effective exchange rate adjusts.



### 4.4.16 Implementation of Trade with Rest of the World

```
...
[name = 'LOM Net Exports']

NX = rhoNX_p * NX(-1) + (1 - rhoNX_p) * exp(exo_NX) * omegaNX_p * Y * P;

[name = 'World interest rate']

rf = (1/beta_p-1);
...
```

#### Outline

- **1** DGE-CRED Model
- 4.1 Introduction
- 4.2 Folder Structure
- 4.3 Demand
- 4.4 Production
- 4.5 Climate Variables
- 4.6 Aggregation and Identities

#### 4.5.1 Climate Variables

■ Average annual regional temperature is given by:

$$T_{\mathrm{r,t}} = T_{\mathrm{r,0}} + \eta_{\mathrm{t}}^{\mathrm{T}}$$

Average annual regional wind speed is given by:

$$WS_{r,t} = WS_{r,0} + \eta_t^{WS}$$

Average annual regional precipitation is given by:

$$PREC_{r,t} = PREC_{r,0} + \eta_t^{PREC}$$

■ Sea level:

$$SL_t = SL_0 + \eta_t^{SL}$$

# 4.5.2 Implementation of Climate Variables

```
...
[name = 'Temperature']

T_@{reg} = T0_@{reg}_p + exo_T_@{reg};

[name = 'Wind speed']

WS_@{reg} = WS0_@{reg}_p + exo_WS_@{reg};

[name = 'Precipitation']

PREC_@{reg} = PREC0_@{reg}_p + exo_PREC_@{reg};

[name = 'Sea Level']

SL = SL0_p + exo_SL;
...
```

#### 4.5.3 Weather Extremes

■ A score reflecting the intensity and number of annual droughts in the region.

$$DRO_{r,t} = DRO_{r,0} + \eta_t^{DRO}$$

 $\blacksquare$  A score reflecting the intensity and number of annual cyclones in the region.

$$CYC_{r,t} = CYC_{r,0} + \eta_t^{CYC}$$

# 4.5.4 Implementation of Weather Extremes

```
...
[name = 'Drought']
DRO_@{reg} = DROO_@{reg}_p + exo_DRO_@{reg};

[name = 'Cyclones']
CYC_@{reg} = CYCO_@{reg}_p + exo_CYC_@{reg};
...
```

#### Outline

- **1** DGE-CRED Model
- 4.1 Introduction
- 4.2 Folder Structure
- 4.3 Demand
- 4.4 Production
- 4.5 Climate Variables
- 4.6 Aggregation and Identities

# 4.6.1 National Aggregates

■ National aggregate investment is given by:

$$P_t \, I_t = \sum_k^K P_{k,t} \, I_{k,t}$$

■ National aggregate capital stock is given by:

$$P_t K_t = \sum_{k}^{K} P_{k,t} K_{k,t}$$

■ National aggregate labour input:

$$N_{\mathrm{t}} = \sum_{k}^{K} N_{\mathrm{k,t}}$$

# 4.6.2 Implementation of National Aggregates

```
[name = 'aggregate investment']
P * I =
@# for sec in 1:Sectors
+ P @{sec} * I @{sec}
@# endfor
[name = 'aggregate capital']
P * K =
@# for sec in 1:Sectors
+ P @{sec} * K @{sec}(-1)
@# endfor
[name = 'aggregate labour']
O# for sec in 1: Sectors
   + N @{sec}
@# endfor
```

### 4.6.3 Sectoral Aggregates

Sector aggregate investment is given by:

$$P_{k,t} I_{k,t} = \sum_{r}^{R} P_{k,r,t} I_{k,r,t}$$

Sector aggregate capital stock is given by:

$$P_{k,t} K_{k,t} = \sum_r^R P_{k,r,t} K_{k,r,t}$$

Sector aggregate wage bill:

$$W_{k,t}N_{k,t} = \sum_{r}^{R} W_{k,r,t}N_{k,r,t}$$

Sector aggregate labour input:

$$N_{k,t} = \sum_{r}^{R} N_{k,r,t}$$

# 4.6.4 Implementation of Sectoral Aggregates (1)

# 4.6.5 Implementation of Sectoral Aggregates (2)

```
...
[name = 'aggregate sector investment']
P_@{sec} * I_@{sec} =
@# for reg in 1:Regions
+ P_@{sec}_@{reg} * I_@{sec}_@{reg}
@# endfor
;
[name = 'aggregate capital']
P_@{sec} * K_@{sec} =
@# for reg in 1:Regions
+ P_@{sec}_@{reg} * K_@{sec}_@{reg}
@#
;
...
```

### 4.6.6 National Aggregates

Sector aggregate investment is given by:

$$P_{k,t} I_{k,t} = \sum_{r}^{R} P_{k,r,t} I_{k,r,t}$$

Sector aggregate capital stock is given by:

$$P_{k,t} K_{k,t} = \sum_r^R P_{k,r,t} K_{k,r,t}$$

Sector aggregate wage bill:

$$W_{k,t}N_{k,t} = \sum_{r}^{R} W_{k,r,t}N_{k,r,t}$$

Sector aggregate labour input:

$$N_{k,t} = \sum_{r}^{R} N_{k,r,t}$$

# 4.6.7 Implementation of Sectoral Aggregates

```
[name = 'aggergate sector labour']
N \otimes \{sec\} =
@# for reg in 1:Regions
+ N @{sec} @{reg}
@# endfor
[name = 'aggergate sector labour income']
W @\{sec\} * N @\{sec\} =
@# for reg in 1: Regions
+ W @{sec} @{reg} * N @{sec} @{reg}
@# endfor
[name = 'aggregate sector investment']
P @{sec} * I @{sec} =
@# for reg in 1: Regions
+ P @{sec} @{reg} * I @{sec} @{reg}
@# endfor
[name = 'aggregate capital']
P @\{sec\} * K @\{sec\} =
@# for reg in 1: Regions
+ P @{sec} @{reg} * K @{sec} @{reg}
@#
|.p.150|
```

# 4.6.8 Population and Price Level

 $\blacksquare$  Population is independent of other variables in the model and is given by:

$$pop_t = pop_{0,t} + \eta_t^{pop}$$

National price level is given by:

$$P_t = P_{0,t} + \eta_t^P$$

# 4.6.9 Implementation of Population and Prices

```
...
[name = 'national price level']
P = P0_p * exp(exo_P);

[name = 'Population']
PoP = PoP0_p + exo_PoP;
...
```

### Outline

- 6 Model Simulation and Calibration
- 5.1 Definitions
- 5.2 Calibration
- 5.3 Scenario Analyses

### 5.1 Main model file DGE\_CRED\_Model.mod

- Define number of sectors and regions
- Define number of steps in steady state calculation and simulation process
- Define excel files that include:
  - ▶ Data used for calibration
  - ▶ Explicit parameter values for parameters
  - ► Assumption related to scenarios
  - ► Results
- Declare additional .mod files needed for simulation and documentation of results



# 5.1 Definition of Sectors and Regions

- Number of sectors: 3 or 9
  - ► Agriculture, industry, services
  - ▶ Agriculture, manufacturing, construction, transportation and storage, accommodation and food service activities, further production activities, services, state-related sectors and other service activities
- Number of regions: 2, 3 or 6
  - ► Coastal (Red River Delta, North Central and Central Coast, Southeast, Mekong river delta) and non-coastal regions
  - ▶ Red River Delta, Mekong river delta and remaining
  - ► All six individually



#### Outline

- 6 Model Simulation and Calibration
- 5.1 Definitions
- 5.2 Calibration
- 5.3 Scenario Analyses

#### 5.2.1 Calibration of Parameters

- Regional and sectoral shares of GDP, employment and wages calibrated to match actual data
- Assumptions about a baseline trajectory of the Vietnamese economy (without climate change effects)
  - ▶ Projections for population dynamics
  - ▶ Long-term growth projections, reflecting general economic catch-up process
  - ▶ Speed and scale of structural change (transition to service economy)
- Calibration of structural parameters unaffected by long-term growth and/or climate change



## 5.2.2 Calibration of Damage Function Parameters

- Distinct damage functions for every region-sector combination
- Consideration of six climate change phenomena:
  - ► Temperature (T)
  - ▶ Wind Speed (W)
  - ▶ Percipitation (P)
  - ► Sea Level (SL)
  - ▶ Drought (DR)
  - ► Cyclone (CY)
- Each damage function includes parameters measuring
  - ▶ Loss of labour productivity
  - ▶ Depreciation of capital
  - ► Loss of TFP

w.r.t. to each of the six climate change phenomena

## 5.2.3 Notation of Damage Function Parameters

■ Damage function parameters have the general form:

$$f\_c\_d\_s\_r\_p$$

- ▶ Input Factor (f): aN- labour, aK capital, a TFP
- ▶ Climate change phenomenon (c): T temperature, W wind speed, P percipitation, SL sea level, DR drought, CY cyclone
- ▶ Degree of polynomial (d): 1 linear, 2 quadratic, 3 quadratic exponent
- ▶ Sector (s): 1 agriculture, 2 industry, 3 services
- ▶ Region (r): 1 region 1, 2 region 2, 3 region 3



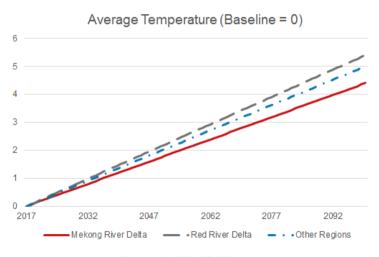
#### Outline

- 6 Model Simulation and Calibration
- 5.1 Definitions
- 5.2 Calibration
- 5.3 Scenario Analyses

## 5.3.1 Scenario 1 – "Temperature" (1)

- Assumes that average temperature increases by X degrees in a given region until the year 2100
- Three regions example (Thuc et al, 2016):
  - ▶ Mekong river delta: +4.4 degrees
  - $\triangleright$  Red river delta: +5.4 degrees
  - $\triangleright$  Other regions 3: +5.0 degrees
- Linear increases in average temperature every year until final value is reached

## 5.3.1 Scenario 1 – "Temperature" (2)



## 5.3.1 Scenario 1 – "Temperature" (3)

- Damage functions are calibrated to match results of relevant meta studies
- $\blacksquare$  Challinor et al. (2014):
  - $\blacktriangleright$  Crop yields on average decrease by 4.5% in response to a 1 degree increase in temperature
  - ► Parameter that governs loss in production from temperature increases (a\_T\_1\_1\_r\_p) is set to 0.045 for all regions
  - ► Can be set differently for different kinds of crop or, more generally, different regions (to reflect region-specific cultivation)



## 5.3.2 Scenario 2 – "Sea Level" (1)

- Increase in average temperature as defined in scenario 1
- In addition, assumes that the sea level rises by 100 cm until the year 2100
- Percentage of agricultural land at risk of inundation following a sea level rise by 100 cm (Thuc et al, 2016)
  - ▶ Mekong river delta: 39%
  - ▶ Red river delta: 16%
  - ▶ Other regions: 2%



## 5.3.2 Scenario 2 – "Sea Level" (2)

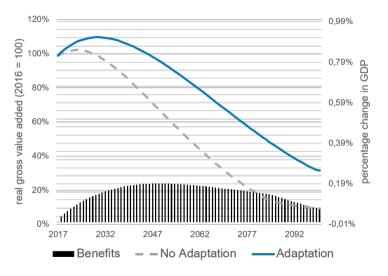
- Damage functions are calibrated to match percentage of agricultural land at risk of inundation
- Different calibration for different regions
  - ▶ Mekong river delta: a\_SL\_1\_1\_1\_p set to 0.39
  - ▶ Red river delta: a\_SL\_1\_1\_2\_p set to 0.16
  - $\blacktriangleright$  Other regions: a\_SL\_1\_1\_3\_p set to 0.02
- Effects of sea level rise on other sectors of production not yet included
- Can be extended e.g. to transportation (flooded/destroyed roads), energy etc.



## 5.3.3 Scenario 3 – "Adaptation" (1)

- Increase in average temperature and sea level as defined in scenario 2
- In addition: government measures to reduce damage from (sea level rise), e.g. dike construction. Damage functions are calibrated to match percentage of agricultural land at risk of inundation
- Facts and assumptions
  - ► Coast line of Mekong River Delta is 600 km
  - ▶ Dike needs to be of the same height along the entire coastline
  - ▶ Estimated costs: 40,000 EUR for one meter height and one meter length
  - ▶ Height increases with sea level each year
  - ▶ Damages associated with sea level rise in Mekong Delta River are zero, if and only if the height of the dike exceeds the sea level rise
- Benefit calculated as difference in GDP between a scenario with dike (Adaptation) and without dike (Sea Level) relative to the Baseline

## 5.3.3 Scenario 3 – "Adaptation" (2)



#### 5.3.4 Scenario 4 – "Extremes"

- Increase in average temperature and sea level as defined in scenario 2
- In addition: occurrence of cyclones and droughts
- Occurrence of cyclones and droughts as well as their intensity is modeled as a random process

#### 5.3.5 Simulation Results

- Stored in Excel file
- **■** Include
  - ▶ Paths for all model variables, stored to individual sheets for every scenario
  - ▶ Figures comparing the outcomes of different simulated scenarios

## References



#### References I

Acemoglu, Daron, Philippe Aghion, Leonardo Bursztyn, and David Hemous (2012).

"The Environment and Directed Technical Change". In:

American Economic Review 102.1, pp. 131–66. DOI:

10.1257/aer.102.1.131. URL:

https://www.aeaweb.org/articles?id=10.1257/aer.102.1.131.

- Arndt, Channing, Finn Tarp, and James Thurlow (2015). "The economic costs of climate change: a multi-sector impact assessment for Vietnam". In: Sustainability 7.4, pp. 4131–4145.
  - Batten, Sandra (Jan. 2018). "Climate Change and the Macro-Economy: A Critical Review". In: SSRN Electronic Journal. DOI: 10.2139/ssrn.3104554.



#### References II

- Berrittella, Maria, Andrea Bigano, Roberto Roson, and Richard Tol (Nov. 2004).

  "A General Equilibrium Analysis of Climate Change Impacts on Tourism". In:

  Tourism Management 27, pp. 913–924. DOI:

  10.1016/j.tourman.2005.05.002.
- Bloesch, Justin and Francois Gourio (2015). "The Effect of Winter Weather on U.S. Economic Activity". In: <a href="mailto:Economic Perspectives">Economic Perspectives</a> Q I. URL: <a href="https://ideas.repec.org/a/fip/fedhep/00010.html">https://ideas.repec.org/a/fip/fedhep/00010.html</a>.
- Bosello, Francesco, Robert Nicholls, Julie Richards, Roberto Roson, and Richard Tol (May 2011). "Economic impacts of climate change in Europe: Sea-level rise". In: Climatic Change 112, pp. 63–81. DOI: 10.1007/s10584-011-0340-1.
  - Calzadilla, Alvaro, Katrin Rehdanz, and Richard Tol (Jan. 2011). "The GTAP-W model: accounting for water use in agriculture". In:

#### References III

Colacito, Riccardo, Bridget Hoffmann, and Toan Phan (Dec. 2018). "Temperature and Growth: A Panel Analysis of the United States". In:

Journal of Money, Credit and Banking. DOI: 10.1111/jmcb.12574.

Dell, Melissa, Benjamin F. Jones, and Benjamin A. Olken (2012). "Temperature Shocks and Economic Growth: Evidence from the Last Half Century". In:

<u>American Economic Journal: Macroeconomics</u> 4.3, pp. 66–95. DOI:

10.1257/mac.4.3.66. URL:

https://www.aeaweb.org/articles?id=10.1257/mac.4.3.66.

Deryng, Delphine, Declan Conway, Navin Ramankutty, J. Price, and Rachel Warren (Mar. 2014). "Global crop yield response to extreme heat stress under multiple climate change futures". In: <a href="mailto:Environmental Research Letters">Environmental Research Letters</a> 9, p. 034011. DOI: 10.1088/1748-9326/9/3/034011.



#### References IV

- Dietz, Simon and Nicholas Stern (Mar. 2015). "Endogenous Growth, Convexity of Damage and Climate Risk: How Nordhaus' Framework Supports Deep Cuts in Carbon Emissions". In: <a href="https://doi.org/10.1111/ecoj.12188">The Economic Journal 125</a>. DOI: 10.1111/ecoj.12188.
- Eboli, Fabio, Ramiro Parrado, and Roberto Roson (Aug. 2009). "Climate Change Feedback on Economic Growth: Explorations with a Dynamic General Equilibrium Model". In: <a href="mailto:Environment and Development Economics">Environment and Development Economics</a> 15, pp. 515–533. DOI: 10.2139/ssrn.1443885.
  - Elshennawy, Abeer, Sherman Robinson, and Dirk Willenbockel (Oct. 2015). "Climate change and economic growth: An intertemporal general equilibrium analysis for Egypt". In: <a href="mailto:Economic Modelling">Economic Modelling</a> 52. DOI: 10.1016/j.econmod.2015.10.008.

#### References V

- Fankhauser, Samuel and Richard Tol (Feb. 2005). "On climate change and economic growth". In: Resource and Energy Economics 27, pp. 1–17. DOI: 10.1016/j.reseneeco.2004.03.003.
- Graff Zivin, Joshua and Matthew Neidell (2014). "Temperature and the Allocation of Time: Implications for Climate Change". In: Journal of Labor Economics 32.1, pp. 1-26. URL: https://EconPapers.repec.org/RePEc:ucp:jlabec:
  - doi:10.1086/671766.
  - Heal, Geoffrey (2017). "The Economics of the Climate". In:
    - Journal of Economic Literature 55.3, pp. 1046–63. DOI:
    - 10.1257/jel.20151335. URL:
    - https://www.aeaweb.org/articles?id=10.1257/jel.20151335.
  - Hsiang, Solomon (2016). "Climate econometrics". In:
    - Annual Review of Resource Economics 8, pp. 43–75.

#### References VI

Kahn, Matthew E, Kamiar Mohaddes, Ryan N.C. Ng, M. Hashem Pesaran, Mehdi Raissi, and Jui-Chung Yang (2019).

Long-Term Macroeconomic Effects of Climate Change: A Cross-Country Analysis.

Working Paper 26167. National Bureau of Economic Research. DOI:

10.3386/w26167. URL: http://www.nber.org/papers/w26167.

Lecocq, Franck and Zmarak Shalizi (Sept. 2007). "How Might Climate Change Affect Economic Growth in Developing Countries? A Review of the Growth Literature with a Climate Lens". In:

Lenzen, Manfred (Mar. 2011). "Aggregation versus disaggregation in input-output analysis of the environment". In: Economic Systems Research 23, pp. 73–89. DOI: 10.1080/09535314.2010.548793.

#### References VII

Liping, Ju and Bin Chen (Dec. 2010). "An Input-output Model to Analyze Sector Linkages and CO2 Emissions". In: <a href="Environmental Sciences Procedia">Environmental Sciences Procedia</a> 2, pp. 1841–1845. DOI: 10.1016/j.proenv.2010.10.195.

Manne, Alan, Robert Mendelsohn, and Richard Richels (1995). "MERGE: A model for evaluating regional and global effects of GHG reduction policies". In:

Energy Policy 23.1, pp. 17–34. URL:

https://EconPapers.repec.org/RePEc:eee:enepol:v:23:y:1995:i:1:p:17-34.

Miller, Ronald E and Peter D Blair (2009).

Input-output analysis: foundations and extensions. Cambridge university press.



#### References VIII

- Nordhaus, William and Zili Yang (1996). "A Regional Dynamic
  - General-Equilibrium Model of Alternative Climate-Change Strategies". In:
  - American Economic Review 86.4, pp. 741–65. URL:
  - https://EconPapers.repec.org/RePEc:aea:aecrev:v:86:y:1996:
  - i:4:p:741-65.
- Nordhaus, William D (1993). "Optimal greenhouse-gas reductions and tax policy in the "DICE" model". In: American Economic Review 83.2, pp. 313–317.
- Pan, Xiaoming and Steven Kraines (Feb. 2001). "Environmental Input-Output
  - Models for Life-Cycle Analysis". In: <u>Environmental and Resource Economics</u> 20, pp. 61–72.



#### References IX

Popp, David (2004). "ENTICE: endogenous technological change in the DICE model of global warming". In:

Journal of Environmental Economics and Management 48.1, pp. 742-768. URL: https://EconPapers.repec.org/RePEc:eee:jeeman:v:48:y:2004:i:1:p:742-768.

Thuc, Tran, Nguyen Van Thang, Huynh Thi Lan Huong, Mai Van Khiem, Nguyen Xuan Hien, and Doan Ha Phong (2016). "Climate change and sea level rise scenarios for Vietnam". In:

Ministry of Natural resources and Environment, Hangi, Vietnam.

Ministry of Natural resources and Environment. Hanoi, Vietnam.

Tol, Richard (June 1995). "The Damage Costs of Climate Change Toward More Comprehensive Calculations". In: <a href="mailto:Environmental and Resource Economics">Environmental and Resource Economics</a> 5, pp. 353–374. DOI: 10.1007/BF00691574.



#### References X



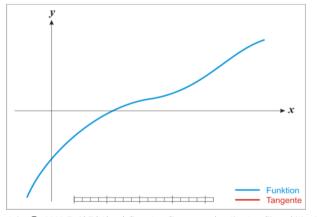
Wing, Ian Sue (2004). "Computable general equilibrium models and their use in economy-wide policy analysis". In:

Technical Note, Joint Program on the Science and Policy of Global Change, MIT.

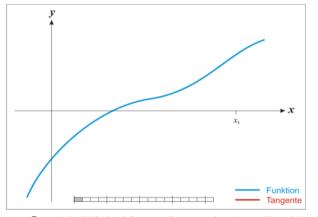


# Appendix

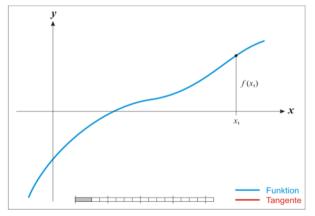




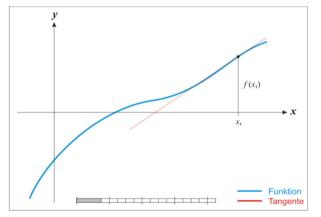
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



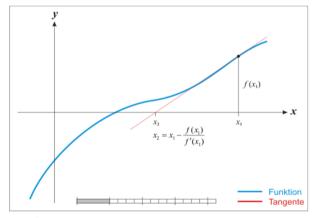
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



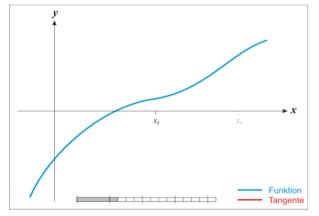
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



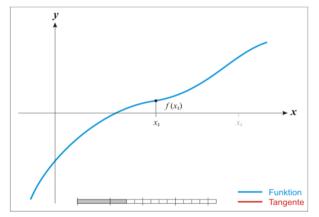
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



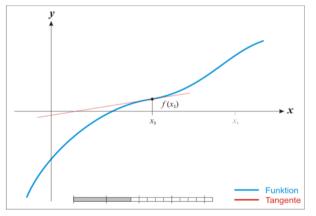
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



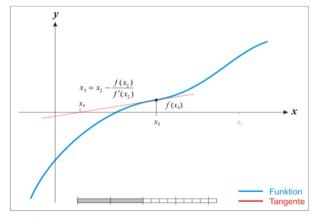
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



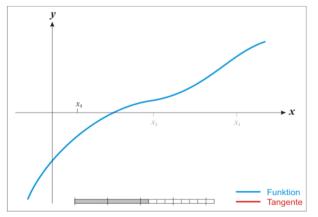
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



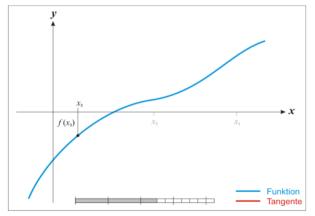
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



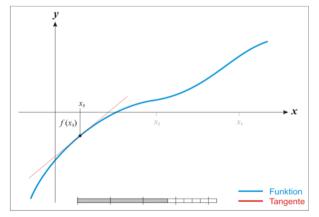
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



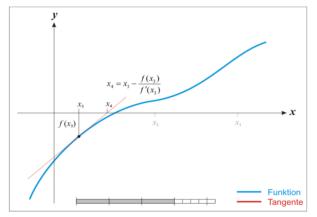
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike  $3.0\,$ 



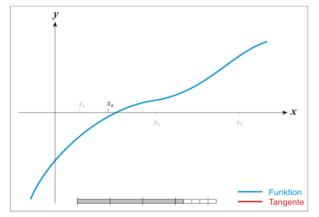
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



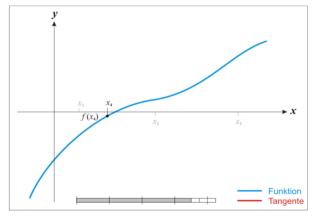
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



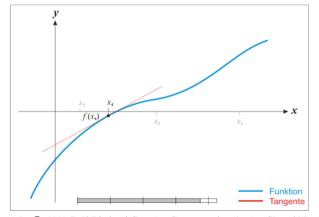
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



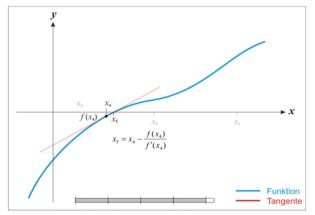
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike  $3.0\,$ 



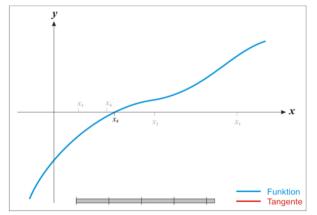
Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike  $3.0\,$ 



Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike  $3.0\,$ 



Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0



Copyright © 2005 Ralf Pfeifer / Creative Commons Attribution-Share Alike 3.0