

# Dynamic General Equilibrium Model for Climate Resilient Economic Development (DGE-CRED)

Technical Report  
Preliminary Draft

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April 2020

## 1 Introduction

Projections by the international panel on climate change (IPCC) show that the global average temperature, the sea level and the frequency of weather extremes are likely to change as a consequence of higher greenhouse gas concentration in the atmosphere Stocker et al. (2013). Climate change has the potential to affect the further economic development of Vietnam. Previous studies (e.g. Arndt et al. 2015, Chen et al. 2012, Wassmann et al. 2004) show that an increase in temperature, sea level rise and a higher frequency of weather extremes (e.g. cyclones and droughts) are hazards to the future economic development. Vietnam belongs to the group of highly vulnerable countries to climate change.

For economic adaptation measures a regional dimension is important because the impact of climate change on Vietnamese economy will be different across regions. National statistics differentiate between six different statistical regions in Vietnam: Red River Delta, Northern Midlands and Mountain Areas (North East and North West), North Central and Central Coastal area (North Central Coast and South Central Coast), Central Highlands, South East, and Mekong River Delta. The map in Figure 1 shows that four of the six regions are located at the coast. Hence, the impact of sea level rise will be different for coastal and non-coastal regions in Vietnam.

Further, climate change will affect economic activities like agriculture, forestry and fishery differently than manufacturing. Climate variables have different effects on the production factors labour and capital used in the different economic sectors. Adaptation measures can target different sectors and different production factors. Building a dam will reduce the damage by sea level rise on land use. Early warning systems for cyclones are able to reduce the damage on capital. Water management systems are able to tackle the issue of water scarcity due to higher temperatures. Labour productivity will be affected by heatwaves as well. Adaptation measures replacing labour intensive tasks using more capital intensive production processes are potential adaptation measures. To prioritize and evaluate different adaptation measures a cost benefit analysis is necessary. A cost benefit analysis needs to account for the dynamic nature of the problem. It is also necessary to evaluate the sensitivity of the results to different assumptions made in order to get robust policy decisions. Further, the analysis needs to be transparent and all the assumptions made are explicitly stated. Structural mathematical models are a suitable tool for this task.

Dynamic general equilibrium models with optimizing agents are a standard tool to assess the impact of different policy measures. All adaptation measures will either reduce productivity in the short-run by relocating economic activity or reduce available public funds for other development measures. Therefore, a general equilibrium framework is necessary to assess the economic implications of different adaptation measures. Investment decisions today will affect the future development of specific sectors. This implies path dependency and requires a dynamic framework. We need to differentiate between different regions and economic activities to account for different regional climate developments.

Our model is implemented in the open source environment Dynare and can be run using Matlab or Octave. An open source environment allows low costs to acquire the necessary skills and experience to work with the model. The model is calibrated to represent the current economic structure. Sectors in the model correspond to economic activities and the classification by the General Statistical Office

(GSO). Regions are based on the statistical regions depicted in Figure 1. It is possible to modify the number of sectors and regions by aggregating the official data. This allows to reduce the size of the model and makes it easier to test new modifications and features of the model. The core of the model can be extended to feature different aspects of the economy.

We extend the approach by Nordhaus (1993) to model the impact of climate change through damage functions. The link between climate and the economy is modeled using sector and region specific damage functions. Damage functions will affect the productivity of all production factors, or only labour productivity, or the formation of capital. We know that the impact of Vietnamese economic variables on average annual temperature, precipitation, wind speed, average intensity of cyclones and droughts are negligible. Our cost benefit analysis will use the results of meteorology models to define paths for climate variables.

We will define different scenarios to evaluate the costs and benefits associated with different climate variables. Therefore, we first need to describe a *Baseline* scenario. The Baseline scenario is necessary to define the evolution of the Vietnamese economy without any climate change. Costs associated with climate change are defined as the difference between the Baseline path and another scenario with climate change for any target variable like gross domestic product. The model is a laboratory for policy makers and researchers to conduct experiments by alternating different climate variables and adaption measures. Data is required to set up the experiments and to get plausible results. Reporting the structural equations of the model is equivalent to a protocol and ensures replication of the experiment. Only replication and transparency ensures that the results can be judged by experts and the public. The model simulates long-run developments. The simulations are not meant to predict bumps in the road, e.g. the economic downturn caused by the coronavirus disease 2019 (COVID-19). But, it is possible to include the impact of the COVID-19 on the economy. One easy way to do this is to use latest economic forecasts as conducted by e.g. the International Monetary Fund (IMF) in April 2020 in the World Economic Outlook to adjust the Baseline scenario to reflect recent developments. Model users are able to quantify upper limits for costs of adaptation measures to reduce damages by climate change. For instance, it is possible to evaluate the impact of temperature increases on different sectors and the overall impact on total gross value added. The discounted cumulative difference between a scenario without a temperature increase and with temperature increase can be used to determine the upper bound for the costs to reduce the damage caused by a temperature increase. To study the interaction between adaptation and mitigation measures it is also possible to extend the model to explicitly consider energy consumption.

In Section 2 the derivation of the model equations is explicitly described. Readers who are interested in directly using the model can skip the model description and can directly proceed with Section 4.

## 2 Model

This report is a guide on how to use the spatial small open economy dynamic general equilibrium model for climate change and adaptation simulations. In general the model belongs to the class of real business cycle models, because no nominal rigidities are explicitly considered. Nevertheless, it is possible to extend the model to feature also nominal rigidities. The model structure is depicted in Figure 2. Regional climate variables (precipitation, wind speed, temperature and sea level) are exogenous to economic variables. Regional sectoral production functions depend on regional climate variables. The model is meant to reflect small open economies and therefore the climate system is unaffected by the domestic economic system.

The model consists of an arbitrary number of regions ( $R$ ) and sectors ( $K$ ). Regional differentiation is only provided on the supply side and not on the demand side. Representative households consume sectoral goods and supply capital and labour to the firms in the regions. Households also demand goods and services from the rest of the world. Firms use capital and labour to produce sectoral goods with sectoral and regional specific constant elasticity of substitution production functions.

The government collects taxes, consumes and can use its funds to finance adaptation measures for specific regions and sectors. So far, adaptation measures will reduce overall damage by all climate variables at the same time. The effectiveness of government expenditure in one specific region and sector can vary.

Table 1 provides a comprehensive list of all variables and parameters. Appendix A reports all equations of the model.

Figure 1: Map of Vietnam



Source: The illustration is published in Boateng (2012).

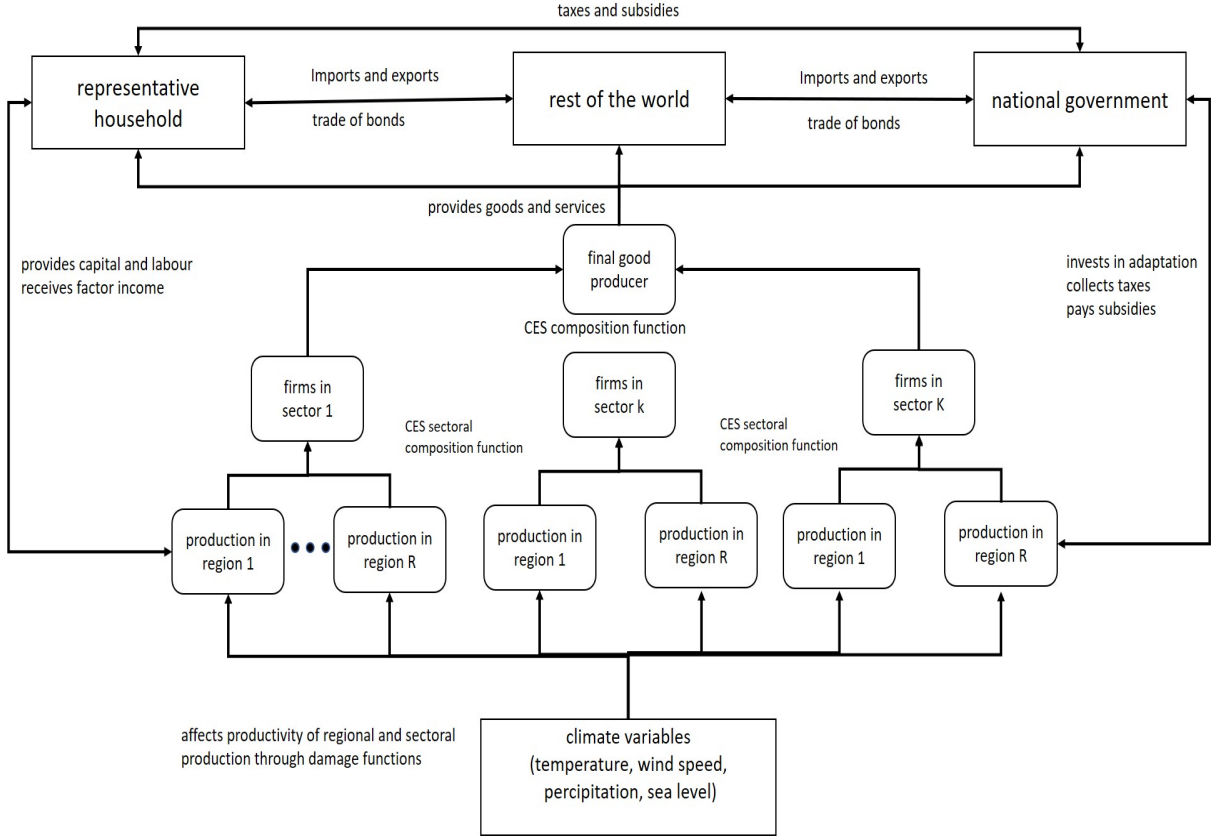
## 2.1 Climate variables

In order to capture the effect of climate change on the economy it is necessary to include climate variables into the model. A small open economy model does not need to include the impact of domestic economic activity on climate variables. Therefore, in contrast to Nordhaus (1993) we do not need to model the interaction between economic activity and climate change. Climate variables are independent of other endogenous variables in the model. We explicitly model the regional average annual temperature  $T_{r,t}$ , the average precipitation  $PREC_{r,t}$ , the average annual wind speed  $WS_{r,t}$ , the sea level  $SL_t$ , cyclones  $CYC_{r,t}$  and droughts  $DRO_{r,t}$ .

$$\begin{aligned}
 T_{r,t} &= T_{r,0} + \eta_{T,r,t} \\
 PREC_{r,t} &= PREC_{r,0} + \eta_{PREC,r,t} \\
 WS_{r,t} &= WS_{r,0} + \eta_{WS,r,t} \\
 SL_t &= SL_0 + \eta_{SL,r,t} \\
 CYC_{r,t} &= CYC_{r,0} + \eta_{CYC,r,t} \\
 DRO_{r,t} &= DRO_{r,0} + \eta_{DRO,r,t}
 \end{aligned} \tag{1}$$

The approach in eq. 1 allows to specify the evolution of climate variables according to the projections by meteorological models (e.g. Stocker et al. 2013).

Figure 2: Model Structure



Source: own exhibition.

## 2.2 Demand

### 2.2.1 Households

As depicted in Figure 2, the demand side is represented by representative households  $h$  providing labour  $N$  and capital  $K$  to domestic firms  $f$ . Households maximize discounted utility over an infinite horizon by choosing consumption  $C_t(h)$ , capital  $K_{k,r,t+1}(h)$ , investments  $I_{k,r,t}(h)$ , labour  $N_{k,r,t}(h)$  and foreign net bond holdings  $B_{t+1}$  to maximize utility constrained by the budget constraint and the law of motion for sectoral and regional capital. Therefore, the Lagrangian eq. 2 of the representative household is

$$\begin{aligned}
 \sum_{t=0}^{\infty} \beta^t & \left[ \left( \frac{C_t(h)^{1-\sigma^C}}{1-\sigma^C} - \sum_{k=1}^K \sum_{r=1}^R \phi_{k,r}^L \frac{N_{k,r,t}(h)^{1+\sigma^L}}{1+\sigma^L} \right) \right. \\
 & - \lambda_t(h) \left( P_t C_t(h) (1 + \tau^C) + \sum_{k=1}^K \sum_{r=1}^R P_{k,r,t} I_{k,r,t}(h) + S_t^f \phi_t^B (1 + r_t^f) B_t(h) \right. \\
 & - \sum_{k=1}^K \sum_{r=1}^R (1 - \tau^N) W_{k,r,t} N_{k,r,t}(h) - \sum_{k=1}^K \sum_{r=1}^R P_{k,r,t} r_{k,r,t} (1 - \tau^K) K_{k,r,t}(h) - B_{t+1}(h) \Big) \\
 & \left. - \sum_{k=1}^K \sum_{r=1}^R \lambda_t(h) \omega_{k,r,t}^I \left\{ K_{k,r,t+1} - (1 - \delta) K_{k,r,t} - I_{k,r,t} S \left( \frac{I_{k,r,t}}{I_{k,r,t-1}} \right) \right\} \right]. \quad (2)
 \end{aligned}$$

Households receive utility by consuming goods, where the intertemporal elasticity of consumption is defined by  $\sigma^C$ . Disutility from labour is sector and region specific  $\phi_{k,r}^L$ , the inverse Frisch elasticity  $\sigma^L$  is

identical for all sectors and regions. Households spent money either on consumption goods  $P_t C_t(h) (1 + \tau^C)$ , regional and sector specific investment  $P_{k,r,t} I_{k,r,t}(h)$  and need to repay foreign bonds  $B_{t+1}(h)$ . They receive income from labour  $W_{k,r,t} N_{k,r,t}(h) (1 - \tau^L)$ , capital renting  $P_{k,r,t} r_{k,r,t} K_{k,r,t}(h) (1 - \tau^K)$  and can use their borrowed money from the foreign economy  $B_t(h)$ . The first order conditions to the problem are the behavioural equations. Following the literature, we replace the Lagrange multiplier  $\lambda_t$  by the marginal utility of consumption  $\frac{C_t(h)^{-\sigma^C}}{P_t (1 + \tau^C)}$  derived from the first order condition (FOC) of the above problem with respect to (w.r.t.) consumption. Households supply labour according to the FOC w.r.t. labour eq. 3 for each sector and region depending on the wage  $W_{k,r,t}$  and the marginal disutility of labour for the specific sector and region

$$\phi_{k,r}^L A_{k,r,t}^N N_{k,r,t}(h)^{\sigma^L} = \lambda_t(h) W_{k,r,t} (1 - \tau^N). \quad (3)$$

Households also need to decide how much of their income they want to consume or invest into capital. The famous Euler equation eq. 4 is obtained by taking the first derivative of the Lagrangian w.r.t. sector and region specific capital

$$\lambda_{t+1}(h) \beta (P_{k,r,t+1} r_{k,r,t+1} + (1 - \delta) \omega_{k,r,t+1}^I) = \lambda_t(h) \omega_{k,r,t}^I. \quad (4)$$

Further, households also face investment adjustment cost  $\Gamma(\frac{I_{k,r,t}}{I_{k,r,t-1}}) = 3 - \exp\left\{\sqrt{\phi^K/2} \left(\frac{I_{k,r,t}}{I_{k,r,t-1}} - 1\right)\right\} - \exp\left\{-\sqrt{\phi^K/2} \left(\frac{I_{k,r,t}}{I_{k,r,t-1}} - 1\right)\right\}$ , which are sector and region specific. The specification of the investment adjustment cost function is the same as proposed and estimated by Christiano et al. (2014) for the US. The marginal value of sectoral and regional investment  $\omega_{k,r,t}^I$  is determined by

$$P_{k,r,t} \lambda_t(h) = \lambda_t(h) \omega_{k,r,t}^I \left( \Gamma\left(\frac{I_{k,r,t}}{I_{k,r,t-1}}\right) - \frac{\partial \Gamma\left(\frac{I_{k,r,t}}{I_{k,r,t-1}}\right)}{\partial I_{k,r,t}} \frac{I_{k,r,t}}{I_{k,r,t-1}} \right) + \beta \lambda_{t+1}(h) \omega_{k,r,t+1}^I \frac{\partial \Gamma\left(\frac{I_{k,r,t+1}}{I_{k,r,t}}\right)}{\partial I_{k,r,t}} \left( \frac{I_{k,r,t+1}}{I_{k,r,t}} \right)^2 \quad (5)$$

### 2.2.2 Rest of the world

Households have access to the international financial market to purchase and sell internationally-traded bonds. However, we only consider net foreign positions

$$\lambda_{t+1} \beta S_{t+1}^f \phi_{t+1}^B (1 + r_{t+1}^f) = \lambda_t \quad (6)$$

with effective exchange rate  $S^f$  and the world interest rate  $r^f$ . The required interest rate is above the world interest rate if the foreign debt ( $B_{t+1} < 0$ )/ foreign claims ( $B_{t+1} > 0$ ) relative to GDP increases/decreases and future net exports relative to GDP will decrease.

$$\phi_{t+1}^B = \exp\left(-\phi^B (S_{t+1}^f r_{t+1}^f \frac{B_{t+1}}{Y_{t+1}} + \frac{NX_{t+1}}{Y_{t+1}})\right) \quad (7)$$

Here we introduce  $\phi_{t+1}^B$  to ensure stability of the system as discussed in Schmitt-Grohé & Uribe (2003).

### 2.2.3 Government

We are interested in different policy measures taken by the government to adapt to a new climate regime. Government behaviour is not a result of an optimization problem. The government collects taxes from consumption  $\tau^C C_t$ , labour income  $\sum_k^K \sum_r^R (\tau^N + \tau_{k,r,t}^N) W_{k,r,t} N_{k,r,t}$  and capital income  $\sum_k^K \sum_r^R (\tau^K + \tau_{k,r,t}^K) P_{k,r,t} r_{k,r,t} K_{k,r,t}$ . In order to finance its activities the government can receive loans from the rest of the world  $B_{t+1}^G$  and has to repay loans and interest from the previous period denominated

in foreign currency  $(1 + r_t^f)$  identical to the interest rates paid by households. The government budget constraint boils down to eq. 8.

$$G_t + \sum_k^K \sum_r^R G_{k,r,t}^A + B_t^G = \sum_k^K \sum_r^R \{(\tau^K + \tau_{r,k,t}^K) P_{k,r,t} r_{k,r,t} K_{k,r,t} + (\tau^N + \tau_{k,r,t}^N) W_{k,r,t} N_{k,r,t} Pop_t\} + (1 + r_t^f) S_t^f \phi_t^B B_{t-1}^G \quad (8)$$

Government expenditures can be used to finance adaptation measures in specific sectors and regions  $G_{k,n,t}^A$ . Government expenditures on adaptation measures, taxes on regional and sectoral capital expenditure, and government debt are independent of other variables or to formulate it differently are discretionary. This allows us to evaluate different policy paths for the future and to model the variables by exogenous processes as stated in eq. 9.

$$\begin{aligned} G_{k,r,t}^A &= G_{k,r,0}^A + \eta_{k,r,t}^A \\ \tau_{k,r,t}^K &= \tau_{k,r,0}^K + \eta_{k,r,t}^{\tau^K} \\ \tau_{k,r,t}^N &= \tau_{k,r,0}^N + \eta_{k,r,t}^{\tau^N} \\ B_t^G &= B_0^G + \eta_t^{B^G} \end{aligned} \quad (9)$$

#### 2.2.4 Resource constraint

Households and government use domestic final goods  $Y_t$  produced by firms for consumption, investment and for exports  $X_t$  and can also use imports  $M_t$  for consumption and investment. This gives rise to the well known resource constraint or the expenditure approach to define GDP

$$Y_t = C_t + I_t + G_t + \underbrace{X_t - M_t}_{NX_t} \quad (10)$$

### 2.3 Production

Households demand final domestic goods  $Y_t$  combining goods from different sectors  $Y_{k,t}$  using a CES production function. They minimize expenditures subject to the production function

$$\min_{Y_{k,t}} \sum_k Y_{k,t} P_{k,t} \quad (11)$$

$$Y_t = \left( \sum_k \omega_k^Q \frac{1}{\eta_k^Q} Y_{k,t}^{\frac{\eta_k^Q - 1}{\eta_k^Q}} \right)^{\frac{\eta_k^Q}{\eta_k^Q - 1}} \quad (12)$$

Therefore, the demand for sectoral products correspond to the first order conditions of the above optimization problem. The Lagrange multiplier is the price level  $P_t$  of domestic products.

$$\frac{P_{k,t}}{P_t} = \omega_k^Q \frac{1}{\eta_k^Q} \left( \frac{Y_{k,t}}{Y_t} \right)^{\frac{-1}{\eta_k^Q}} \quad (13)$$

In order to model regional economic activity we further decompose the production process on a regional level. One can either think about this approach as modeling the optimization problem of a representative firm operating in one sector on a national level allocating production activity across the nation. Another way is to consider that households make direct purchases from regional operating firms in one sector. In this case the following optimization problem would be part of the above optimization problem.

$$\min_{Y_{k,r,t}} \sum_k Y_{k,r,t} P_{k,r,t} \quad (14)$$

$$Y_{k,t} = \left( \sum_k \omega_{k,r}^Q \frac{1}{\eta_k^Q} Y_{k,r,t}^{\frac{\eta_k^Q - 1}{\eta_k^Q}} \right)^{\frac{\eta_k^Q}{\eta_k^Q - 1}} \quad (15)$$

Demand for sectoral and regional products correspond to the first order conditions of the above optimization problem. The Lagrange multiplier is the sectoral price level  $P_{k,t}$  of domestic products.

$$\frac{P_{k,r,t}}{P_{k,t}} = \omega_{k,r}^Q \frac{1}{\eta_k^Q} \left( \frac{Y_{k,r,t}}{Y_{k,t}} \right)^{\frac{-1}{\eta_k^Q}} \quad (16)$$

At the regional and sectoral level are representative firms maximizing profits using capital  $K_{k,r,t}$  and labour  $L_{k,r,t} = N_{k,r,t} \text{Pop}_t$  provided by households to produce products. They charge a price  $P_{k,r,t}$  for their products and have to pay households wages  $W_{k,r,t}$ , interest on rented capital  $P_{r,k,t} r_{r,k,t}$ , taxes related to the wage bill  $\tau_{r,k,t}^N$  and on capital expenditure  $\tau_{r,k,t}^K$ . Representative firms have access to a regional and sector specific constant elasticity of substitution production function. The productivity of capital and labour of a firm in one sector and region depends on the climate variables, and the adaption measures by the government represented by a damage function affecting total factor productivity  $A_{k,r,t}$  by  $D_{k,r,t} = D_{k,r} \left( T_{r,t}, PREC_{r,t}, WS_{r,t}, SL_{r,t}, CYC_{r,t}, DRO_{r,t}, G_{r,k,t}^A \right)$ . Further, we explicitly differentiate between climate induced damages affecting labour productivity  $D_{N,k,r,t}$  and capital depreciation  $D_{K,k,r,t}$ . As in Nordhaus (1993), we assume a polynomial functional form of the damage functions, but the damages are different across regions and sectors (eq. 17).

$$D_{k,r,t} = \exp \left( -\phi^{G_{k,r}^A} G_{k,r,t}^A \right) \left( \underbrace{a_{T,1,k,r} T_{r,t} + a_{T,2,k,r} (T_{r,t})^{a_{T,3,k,r}}}_{\text{impact of temperature}} + \underbrace{a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}}}_{\text{impact of sea level}} \right. \\ + \underbrace{a_{WS,1,k,r} WS_{r,t} + a_{WS,2,k,r} (WS_{r,t})^{a_{WS,3,k,r}}}_{\text{impact of wind speed}} + \underbrace{a_{PREC,1,k,r} PREC_{r,t} + a_{PREC,2,k,r} (PREC_{r,t})^{a_{PREC,3,k,r}}}_{\text{impact of precipitation}} \\ + \underbrace{a_{CYC,1,k,r} CYC_{r,t} + a_{CYC,2,k,r} (CYC_{r,t})^{a_{CYC,3,k,r}}}_{\text{impact of cyclones}} + \underbrace{a_{DRO,1,k,r} DRO_{r,t} + a_{DRO,2,k,r} (DRO_{r,t})^{a_{DRO,3,k,r}}}_{\text{impact of droughts}} \left. \right). \quad (17)$$

$$D_{k,r,t}^N = \exp \left( -\phi^{G_{k,r}^A} G_{k,r,t}^A \right) \left( \underbrace{a_{T,1,k,r}^N T_{r,t} + a_{T,2,k,r}^N (T_{r,t})^{a_{T,3,k,r}^N}}_{\text{impact of temperature}} + \underbrace{a_{SL,1,k,r}^N SL_t + a_{SL,2,k,r}^N (SL_t)^{a_{SL,3,k,r}^N}}_{\text{impact of sea level}} \right. \\ + \underbrace{a_{WS,1,k,r}^N WS_{r,t} + a_{WS,2,k,r}^N (WS_{r,t})^{a_{WS,3,k,r}^N}}_{\text{impact of wind speed}} + \underbrace{a_{PREC,1,k,r}^N PREC_{r,t} + a_{PREC,2,k,r}^N (PREC_{r,t})^{a_{PREC,3,k,r}^N}}_{\text{impact of precipitation}} \\ + \underbrace{a_{CYC,1,k,r}^N CYC_{r,t} + a_{CYC,2,k,r}^N (CYC_{r,t})^{a_{CYC,3,k,r}^N}}_{\text{impact of cyclones}} + \underbrace{a_{DRO,1,k,r}^N DRO_{r,t} + a_{DRO,2,k,r}^N (DRO_{r,t})^{a_{DRO,3,k,r}^N}}_{\text{impact of droughts}} \left. \right). \quad (18)$$

$$D_{k,r,t}^K = \exp \left( -\phi^{G_{k,r}^A} G_{k,r,t}^A \right) \left( \underbrace{a_{T,1,k,r}^K T_{r,t} + a_{T,2,k,r}^K (T_{r,t})^{a_{T,3,k,r}^K}}_{\text{impact of temperature}} + \underbrace{a_{SL,1,k,r}^K SL_t + a_{SL,2,k,r}^K (SL_t)^{a_{SL,3,k,r}^K}}_{\text{impact of sea level}} \right. \\ + \underbrace{a_{WS,1,k,r}^K WS_{r,t} + a_{WS,2,k,r}^K (WS_{r,t})^{a_{WS,3,k,r}^K}}_{\text{impact of wind speed}} + \underbrace{a_{PREC,1,k,r}^K PREC_{r,t} + a_{PREC,2,k,r}^K (PREC_{r,t})^{a_{PREC,3,k,r}^K}}_{\text{impact of precipitation}} \\ + \underbrace{a_{CYC,1,k,r}^K CYC_{r,t} + a_{CYC,2,k,r}^K (CYC_{r,t})^{a_{CYC,3,k,r}^K}}_{\text{impact of cyclones}} + \underbrace{a_{DRO,1,k,r}^K DRO_{r,t} + a_{DRO,2,k,r}^K (DRO_{r,t})^{a_{DRO,3,k,r}^K}}_{\text{impact of droughts}} \left. \right). \quad (19)$$

Firms in each region and sector have access to a constant elasticity of substitution production function with production factors labour and capital. Eq. 20 states the optimization problem of the firm.

$$\begin{aligned}
& \max_{Y_{k,r,t}, N_{k,r,t}, K_{k,r,t}} P_{k,r,t} Y_{k,r,t} - W_{k,r,t} N_{k,r,t} - r_{k,r,t} P_{k,r,t} K_{k,r,t} \\
& \text{s.t. } Y_{k,r,t} = A_{k,r,t} (1 - D_{k,r,t}) \left[ \alpha_{k,r}^N \frac{1}{\eta_{k,r}^{NK}} (A_{k,r,t}^N (1 - D_{k,r,t}^N) Pop_t N_{k,r,t})^{\rho_{k,r}} + \alpha_{k,r}^K \frac{1}{\eta_{k,r}^{NK}} (K_{k,r,t})^{\rho_{k,r}} \right]^{\frac{1}{\rho_{k,r}}}, \\
& \text{where } \rho_{k,r} = \frac{\eta_k^{NK} - 1}{\eta_k^{NK}}.
\end{aligned} \tag{20}$$

Demand for production factors are given by the first order condition of the above optimization problem. The Lagrange multiplier is equal to the price charged by companies.

$$\begin{aligned}
\frac{W_{k,r,t}}{P_{k,r,t}} &= \alpha_{k,r}^N \frac{1}{\eta_{k,r}^{NK}} (A_{k,r,t} (1 - D_{k,r,t}) A_{k,r,t}^N (1 - D_{k,r,t}^N))^{\rho_{k,r}} \left( \frac{Pop_t N_{k,r,t}}{Y_{k,r,t}} \right)^{-\frac{1}{\eta_{k,r}^{NK}}} \\
r_{k,r,t} &= \alpha_{k,r}^K \frac{1}{\eta_{k,r}^{NK}} (A_{k,r,t} (1 - D_{k,r,t}))^{\rho_{k,r}} \left( \frac{K_{k,r,t}}{Y_{k,r,t}} \right)^{-\frac{1}{\eta_{k,r}^{NK}}}
\end{aligned} \tag{21}$$

$$\tag{22}$$

We use the more general case of the CES production function rather than the more commonly used Cobb-Douglas production function. The parameter  $\eta_{k,r}^{NK}$  allows us to control the response of capital and labour demand to temporary productivity shocks. Temporary productivity shocks are in our set-up also weather extremes. Cyclones can destroy the capital stock. Firms can either substitute capital using more labour in the period, e.g. using more labour to replace tractors. Or they need to layoff workers because they are useless without machines, e.g. destruction of factories. The parameter  $\eta_{k,r}^{NK}$  allows to specify the reaction of firms according to the data.

## 2.4 Rest of the world

The demand for domestic exports and foreign imports is not explicitly modeled in this version of the model. We assume that net exports follow an auto-regressive process of order one and that the long-run value of net exports depend on the long-run development of gross domestic product. We therefore assume that imports and exports will grow at the same speed as GDP. Sluggish adjustments in export and import behaviour of companies is captured by an auto-regressive process.

$$NX_t = \rho^{NX} NX_{t-1} + (1 - \rho^{NX}) \omega^{NX} P_t Y_t \tag{23}$$

The effective exchange rate  $S_t^f$  and the world interest rate  $r_t^f$  determine how much governments and households have to pay back in domestic currency as net lender or how much they receive as net borrower to the rest of the world. Here the world interest rate is independent of domestic developments and only the effective exchange rate adjusts according to eq. 6.

## 2.5 Model extension: intermediate consumption and sectoral trade

Table 2 provides a list of all additional variables and parameters included for the extension. Appendix B reports all additional and modified equations associated with the respective extension.

In order to consider the impact of climate change on exports and imports, we need to extend the model to feature sectoral exports  $X_{k,t}$  and imports  $M_{k,t}$ . It is also necessary to include intermediate consumption  $Q_{k,r,t}^I$  by firms to ensure that the model can be calibrated to match export and import ratios for different sectors. In contrast to the baseline version imports are used to produce final domestically used output  $Q_t^U$ . The later is provided by a representative firm using domestic output from different sectors and regions  $Q_{k,t}^D$  and sectoral imports. Imports and domestic products from different sectors



are combined using a CES production function. The production function of the firm is a nested CES function:

$$Q_t^U = \left( (1 - \omega^F)^{\frac{1}{\eta^F}} Q_t^{D\rho^F} + \omega^F \frac{1}{\eta^F} M_t^{\rho^F} \right)^{\frac{1}{\rho^F}}, \text{ where } \rho^F = \frac{\eta^F - 1}{\eta^F} \quad (24)$$

$$M_t = \left( \sum_k^K \omega_k^M \frac{1}{\eta^M} M_{k,t}^{\rho^M} \right)^{\frac{1}{\rho^M}}, \text{ where } \rho^M = \frac{\eta^M - 1}{\eta^M} \quad (25)$$

$$Q_t^D = \left( \sum_k^K \omega_k^Q \frac{1}{\eta^Q} Q_{k,t}^{\rho^Q} \right)^{\frac{1}{\rho^Q}}, \text{ where } \rho^Q = \frac{\eta^Q - 1}{\eta^Q} \quad (26)$$

$$Q_{k,t}^D = Q_{k,t} - X_{k,t}$$

$$Q_{k,t} = \left( \sum_k^K \omega_{k,r}^Q \frac{1}{\eta_k^Q} Q_{k,r,t}^{\rho_k^Q} \right)^{\frac{1}{\rho_k^Q}}, \text{ where } \rho_k^Q = \frac{\eta_k^Q - 1}{\eta_k^Q}$$

Prices of sectoral imports  $P_{k,t}^M$  are exogenous (eq. (90)) as well as the export demand (eq. (89)) for domestic produced sectoral products. The optimization problem of the final goods producer can be split up into different parts. According to eq. (24) they first choose the amount of imports (eq. (78)) and domestically used and produced products (eq. (77)). In the next layer the final goods producer minimizes costs for a given level of imports (eq. (25)) and domestically used and produced output (eq. (26)). This leads to demand functions for sectoral domestic output (eq. (74)) and sectoral imports (eq. (79)).

Further, imports and domestic production are used to consume, invest and for intermediate goods  $Q_{k,r,t}^I$  in the domestic production process. Therefore, firms are using labour and capital, but also intermediate input to produce goods and services. The production function of firms operating in different regions is now modified to feature another layer of the CES production function. The firm is now maximizing profits combining value-added  $Y_{k,r,t}$  and intermediate products  $Q_{k,r,t}^I$  to produce output  $Q_{k,r,t}$ . They sell their products under perfect competition for the price  $P_{k,r,t}^D$ . The optimization problem is

$$\begin{aligned} & \min_{Q_{k,r,t}^I, Y_{k,r,t}} P_{k,r,t}^D Q_{k,r,t} - P_t Q_{k,r,t}^I - P_{k,r,t} Y_{k,r,t} \\ Q_{k,r,t} &= \left( \omega_{k,r}^{Q^I} \frac{1}{\eta_{k,r}^I} Q_{k,r,t}^{I\rho_{k,r}^I} + (1 - \omega_{k,r}^{Q^I}) \frac{1}{\eta_{k,r}^I} Y_{k,r,t}^{\rho_{k,r}^I} \right)^{\frac{1}{\rho_{k,r}^I}}, \text{ where } \rho_{k,r}^I = \frac{\eta_{k,r}^I - 1}{\eta_{k,r}^I} \end{aligned} \quad (27)$$

Therefore, we obtain equations determining the demand for value added (eq. (28)) and intermediate products (eq. (29)) by one sector in a region depending on the relative prices of labour, capital and intermediate products.

$$\frac{P_{k,r,t}}{P_{k,r,t}^D} = \left( 1 - \omega_{k,r}^{Q^I} \right)^{\frac{1}{\eta_{k,r}^I}} \left( \frac{Y_{k,r,t}}{Q_{k,r,t}} \right)^{\frac{(-1)}{\eta_{k,r}^I}} \quad (28)$$

$$\frac{P_t}{P_{k,r,t}^D} = \omega_{k,r}^{Q^I} \frac{1}{\eta_{k,r}^I} \left( \frac{Q_{k,r,t}^I}{Q_{k,r,t}} \right)^{\frac{(-1)}{\eta_{k,r}^I}} \quad (29)$$

Net exports (eq. (88)) are now the difference between aggregate export expenditures  $P_t^D X_t$  and aggregate import expenditures  $P_t^M M_t$ . The resource constraint now equates total domestic production with domestic consumption, investment, government consumption, net exports and intermediate products (eq. (80)). Gross value added is total domestic output less total intermediate consumption.

## 2.6 Model extension: energy consumption

Table 3 provides a list of all additional variables and parameters included for the extension. Appendix C reports all additional and modified equations associated with the respective extension.

To model the impact of mitigation policy on the economy we define an energy sector  $k^E$ . We add two new layers to the production function in the energy sector. The energy sector uses intermediate

products  $Q_{k,r,t}^I$  and a composite energy product  $E_{k,r,t}$  to produce a composite intermediate product  $Q_{k,r,t}^{I,E}$  (eq. (92)). The composite energy input is a combination of different energy carriers  $c \in \{1, \dots, EC\}$  using a CES production function (eq. (93)). The price of an energy carrier is the same across regions and exogenous to other variables (eq. (99)). Aggregate consumption of energy carriers (eq. (98)) is necessary to compute emissions associated with different energy carriers. Total intermediate input  $Q_t^I$  expenditures is the sum over all intermediate inputs demanded by different sectors including expenditures on energy carriers (eq. (97)).

### 3 Scenario Analysis

For simulations it is necessary to specify a direct mapping between sectors in the model and the available data. The analysis in the following paragraphs will differentiate between three economic sectors:

1. A - agriculture, forestry and fishing
2. B-F: industrial sectors (mining and quarrying, manufacturing, electricity, gas, steam and air conditioning supply, water supply, sewerage, waste management and remediation activities) and construction
3. G-S: services

It is also necessary to define the regions. Therefore, we will explicitly model three regions:

1. Mekong river delta
2. Red river delta
3. North Central and Central Coast, Southeast, Central Highlands, Northern Midlands and Mountains

We calibrate the model to reflect the economic structure of Vietnam for the year 2016. The year 2016 is our base year, because the latest supply and use table is available for this year. We calibrate the production function parameters  $\alpha_{k,r,n}^K$ ,  $\alpha_{k,r,n}^N$  such that we match for a given elasticity of substitution  $\eta_{k,r}^{NK}$  the observed share of the wage bill on gross value added  $\frac{W_{k,r,0} N_{k,r,0}}{P_{k,r,0} Y_{k,r,0}}$  and ensure a correct accounting of factor income by economic activity. Further, we calibrate the sectoral composition production function parameters  $\omega_{k,r}^Q$ ,  $\omega_k^Q$  for a given elasticity of substitutions  $\eta^Q$ ,  $\eta_k^Q$  to meet the initial gross value added shares  $\phi_{k,r,0}^Y = \frac{P_{k,r,0} Y_{k,r,0}}{P_0 Y_0}$  for the year 2016.

A scenario defines paths for variables exogenous to the economic system. In the standard version of the model we need to define how exogenous total factor productivity  $\eta_{A,k,r,t}$ , labour productivity  $\eta_{k,r,t}^{AN}$ , climate variables  $\{\eta_{r,t}^T, \eta_{r,t}^{PREC}, \eta_{r,t}^{WS}, \eta_{r,t}^{CYC}, \eta_{r,t}^{DRO}, \eta_t^{SL}\}$ , population  $\eta_t^{Pop}$ , price level  $\eta_t^P$ , taxes  $\eta_{k,r,t}^{TK,N}$ ,  $\eta_t^{TK,N}$ ,  $\eta_t^{TC}$ , the government deficit  $\eta_t^{BG}$ , adaptation measures  $\eta_{k,r,t}^{GA}$  and the trade balance  $\eta_t^{NX}$  evolve over time.

#### 3.1 Baseline

Vietnam is a developing economy with a GDP per inhabitant in constant 2010 US Dollar of 1,752 USD equivalent to roughly 4 percent of Japan's GDP per inhabitant in 2016. Japan was the first Asian country becoming a developed economy in the 20th century. We will use the development of the Japanese economy in the 20th century as a benchmark for a counter-factual development of Vietnam without climate change in the 21st century. Japan is the best benchmark among other developed economies, which are either the United States of America or countries from Europe. Japan's GDP grew annually from 1960 to 2018 by 3 percent according to the World Bank. In the Baseline scenario Vietnam's geometric average annual growth rate will be 4 percent for the next century.

It is common for developing economies to face also a change in the composition of their economic structure. The agricultural sector in Vietnam is still an important employer (40% of all employees worked in the agricultural sector) and is responsible for roughly 15% of total gross value added in Vietnam. In developed countries (e.g. Japan, Germany, United Kingdom etc.) the share of agriculture on total gross value added is approximately 1% and the share of employees is roughly the same. Services contribute

64% and mining, manufacturing, water supply and waste management, energy supply, and construction contribute 35% to GDP. We therefore determine sectoral total productivity shocks  $\eta_{A,k,r,t}$  to match an assumed new long-run composition of gross value added by economic activity  $\phi_{k,r,T}^Y = \frac{P_{k,r,T} Y_{k,r,T}}{P_T Y_T}$ . We also define the long-run development on the labour market. The long-run development of labour productivity  $\eta_{A^N,k,r,t}$  ensures that employment shares  $\phi_{k,r,T}^Y = \frac{Pop_T N_{k,r,T}}{Pop_T N_T}$  will converge to observed shares for other industrial countries. The evolution of sector specific labour productivity and total factor productivity is determined such that the initial simulated sectoral growth rates of labour share  $g_{k,r,1}^N = \frac{N_{k,r,1}/N_1}{N_{k,r,0}/N_0}$  and real gross value added  $g_{k,r,1}^Y = \frac{Y_{k,r,1}}{Y_{k,r,0}}$  match the observed growth rates of different sectors in Vietnam over the last decade. Growth rates follow an auto-regressive process of order one, where the auto-correlation parameter is determined such that growth rates are approximately zero after 120 periods. We ensure that the exogenous evolution of sectoral labour and total factor productivity is completed after 120 periods.

The evolution of the population is given by the projection of the GSO. The GSO published four different projections with different fertility rates of the Vietnamese population. We use the medium variant population projection. The population is expected to grow from roughly 95 million people in 2016 to 108 million people by 2050. After 2050 the population stays constant. In our simulation we do not consider potential feedback between the economic development of Vietnam and the development of the population. Potential interdependence between the population and climate change through higher mortality caused by weather extremes (e.g. droughts, heat waves, cyclones) are not considered. It is hard to find studies on the effects of temperature increases on the services sector regarding TFP. Therefore, we will assume that the productivity of the services sector is unaffected by annual average increase in temperature.

### 3.2 Temperature

Average annual temperature change will not exceed 6 degree Celsius with a probability of 90% according to down scaling techniques of the RCP 8.5 scenario from the IPCC conducted by Thuc et al. (2016). We consider the upper bound to estimate the maximum expected damage associated with a change in temperature. The average annual temperature will follow a linear trend. According to the results published in Thuc et al. (2016) the average annual temperature in the Mekong delta river, Red River Delta, and the remaining regions will increase by 4.4, 5.4, and 5 degree Celsius until the end of the 21st century, respectively.

To evaluate the impact of climate change on the economy in Vietnam we need to specify the parameters  $a_{T,\{1,2,3\},k,r}$ ,  $a_{T,\{1,2,3\},k,r}^N$ ,  $a_{T,\{1,2,3\},k,r}^K$  of the damage functions. We use the literature to define these parameters. We assume a linear relationship between total factor productivity of the agricultural sector and a change in temperature. The coefficient  $a_{T,1,1,r}$  is set to 0.045 based on Challinor et al. (2014) and the other parameters are set to zero for agriculture. Challinor et al. (2014) report a decline of crop yield of 4.5% as a response to a one degree Celsius increase in average annual temperature. This is a simplification of a complex causal mechanism between temperature and crop yield. Further, different crops will respond differently to a one degree Celsius increase of temperature. It is possible to explicitly model different crops and to define the damage functions differently for different crops.

For the industry sector we use the results of Zhang et al. (2018) for total factor productivity. The study estimates a reduction in TFP by 9% in the manufacturing sector in China as a response to a 2 degree Celsius increase of average annual temperature. Therefore, we calibrate the parameter to  $a_{T,1,2,r} = 0.045$ . The other parameters are set to zero regarding temperature.

### 3.3 Sea Level

The impact of sea level rise on Vietnam is well studied in the literature (). The impact will be mainly on the agricultural sector.

### 3.4 Extremes

### 3.5 Results

## 4 How to use the model?

### 4.1 Usage

1. In order to use the model you need to install Dynare (at least version 4.6.1) and Matlab (at least 2018b) or Octave on your computing machine. For Octave you need to have the version 5.2.0 as reported by the Dynare team. Furthermore, MS Excel is used to specify the parameters and to save the results. Result tables are saved additionally in Latex-format.
2. You need to download the repository from Github.
3. Open Octave or Matlab GUI and browse to the location of the folder in your computer. You have the right folder if the command `pwd()` returns `YourPath/DGE-CRED/DGE_CRED_Model`.
4. The script `RunSimulations.m` has to be executed in order to run simulations for different scenarios. Make sure that the scenarios and model parameters are defined in the file `ModelSimulationandCalibrationKSEctorsandRRRegions.xlsx`. You need to adopt the number of sectors and regions in the file `DGE_CRED_Model.mod`. All program files are described in the next section.
5. The simulation results are stored in the file `ResultsScenariosKSEctorsandRRRegions.xlsx`.

### 4.2 Folder structure

1. The main file containing all necessary mod-files is `DGE_CRED_Model.mod`. This file includes the following files stored in the `ModFiles` folder:
  - (a) `DGE_CRED_Model_Declarations.mod` declares all endogenous and exogenous variables of the model and structural parameters.
  - (b) `DGE_CRED_Model_Parameters.mod` assigns values to the structural parameters of the model.
  - (c) `DGE_CRED_Model_Equations.mod` contains the equations of the model.
  - (d) `DGE_CRED_Model_LatexOutput.mod` produces latex output for documentation of the declared variables and model equations.
  - (e) `DGE_CRED_Model_SteadyState.mod` computes initial and terminal condition for the dynamic simulation.
  - (f) `DGE_CRED_Model_Simulations.mod` starts the dynamic simulation.
2. Subroutines responsible for finding the initial and terminal conditions are located in the subfolder `Functions`:
  - (a) `Calibration.mat` finds the initial conditions to reflect a specific year of the economy.
  - (b) `FindA.mat` looks for exogenous productivity shocks across sectors and regions to meet the terminal conditions.
  - (c) `FindK.mat` looks for a capital allocation across sectors and regions to fulfill the static equations of the model.
  - (d) `rng.mat` random number generator function necessary for Octave users.
  - (e) `LoadExogenous.mat` reads exogenous variables for different scenarios.
3. To define scenarios and structural parameters you need to create an Excel file located in the subfolder `ExcelFiles`:
  - (a) `ModelSimulationandCalibrationforKSEctorsandRRRegions.xlsx` has multiple sheets:
    - i. initial `Start`
    - ii. terminal `Terminal`
    - iii. parameters to define rigidity parameters `Dynamics`
    - iv. elasticity parameters and tax rates `Structural Parameters`

- v. coefficients for regional and sector specific damage functions `Climate Damage Functions (Labour, Capital, TFP)`
  - vi. `Baseline` scenario and other optional scenario sheets `Adaptation` and `Extremes` defining paths for exogenous variables
  - vii. `Data` to load external data sources
- (b) `ResultsScenariosKSEctorsandRregions.xlsx` has as many sheets as scenarios defined in the previous Excel file.
4. The latex files produced by `DGE_CRED_Model_LatexOutput.mod` are stored in the sub-folder `LatexFiles`:
    - (a) the system of dynamic equations as implemented in Matlab `DGE_CRED_Model_Dynamic`, `DGE_CRED_Model_Dynamic_content`
    - (b) names of endogenous, exogenous variables and parameters `DGE_CRED_Model_latex_definitions`
    - (c) the system of dynamic equations in original form without auxiliary variables for leads and lags `DGE_CRED_Model_original`, `DGE_CRED_Model_original_content`
  5. The file to run different simulations is `RunSimulations.m`.
  6. A Matlab function to find solutions to the static system of equations is `DGE_CRED_Model_steady_state.m`.

## References

- Arndt, C., Tarp, F. & Thurlow, J. (2015), ‘The economic costs of climate change: a multi-sector impact assessment for Vietnam’, *Sustainability* **7**(4), 4131–4145.
- Boateng, I. (2012), ‘Gis assessment of coastal vulnerability to climate change and coastal adaption planning in Vietnam’, *Journal of Coastal Conservation* **16**(1), 25–36.
- Challinor, A. J., Watson, J., Lobell, D. B., Howden, S., Smith, D. & Chhetri, N. (2014), ‘A meta-analysis of crop yield under climate change and adaptation’, *Nature Climate Change* **4**(4), 287–291.
- Chen, C.-C., McCarl, B. & Chang, C.-C. (2012), ‘Climate change, sea level rise and rice: global market implications’, *Climatic Change* **110**(3-4), 543–560.
- Christiano, L. J., Motto, R. & Rostagno, M. (2014), ‘Risk shocks’, *American Economic Review* **104**(1), 27–65.
- Nordhaus, W. D. (1993), ‘Optimal greenhouse-gas reductions and tax policy in the “dice” model’, *American Economic Review* **83**(2), 313–317.
- Schmitt-Grohé, S. & Uribe, M. (2003), ‘Closing small open economy models’, *Journal of International Economics* **61**(1), 163–185.
- Stocker, T. F., Qin, D., Plattner, G.-K., Tignor, M., Allen, S. K., Boschung, J., Nauels, A., Xia, Y., Bex, V., Midgley, P. M. et al. (2013), ‘Climate change 2013: The physical science basis’, *Contribution of working group I to the fifth assessment report of the intergovernmental panel on climate change* **1535**.
- Thuc, T., Thang, N., Huong, H., Kien, M., Hien, N. & Phong, D. (2016), ‘Climate change and sea level rise scenarios for vietnam’, *Ministry of Natural resources and Environment. Hanoi, Vietnam*.
- Wassmann, R., Hien, N. X., Hoanh, C. T. & Tuong, T. P. (2004), ‘Sea level rise affecting the Vietnamese Mekong Delta: water elevation in the flood season and implications for rice production’, *Climatic Change* **66**(1-2), 89–107.
- Zhang, P., Deschenes, O., Meng, K. & Zhang, J. (2018), ‘Temperature effects on productivity and factor reallocation: Evidence from a half million chinese manufacturing plants’, *Journal of Environmental Economics and Management* **88**, 1–17.

## A Model equations for CRED baseline version

## A.1 Regional Industries

damage function TFP

$$D_{k,r_t} = \exp \left( -\phi^{G_{k,r}^A} G_{k,r,t}^A \right) \left( a_{T,1,k,r} T_{rt} + a_{T,2,k,r} (T_{rt})^{a_{T,3,k,r}} + a_{SL,1,k,r} SL_t + a_{SL,2,k,r} (SL_t)^{a_{SL,3,k,r}} \right. \\ \left. + a_{W,1,k,r} WS_{rt} + a_{W,2,k,r} (WS_{rt})^{a_{W,3,k,r}} + a_{P,1,k,r} PREC_{rt} + a_{P,2,k,r} (PREC_{rt})^{a_{P,3,k,r}} + a_{C,1,k,r} CYC_{rt} \right. \\ \left. + a_{C,2,k,r} (CYC_{rt})^{a_{C,3,k,r}} + a_{D,1,k,r} DRO_{rt} + a_{D,2,k,r} (DRO_{rt})^{a_{D,3,k,r}} \right) \quad (30)$$

damage function capital

$$D_{k,r_t}^K = \exp \left( -\phi^{G_{k,r}^A} G_{k,r,t}^A \right) \left( a_{T,1,k,r}^K T_{rt} + a_{T,2,k,r}^K (T_{rt})^{a_{T,3,k,r}^K} + a_{SL,1,k,r}^K SL_t + a_{SL,2,k,r}^K (SL_t)^{a_{SL,3,k,r}^K} \right. \\ \left. + a_{W,1,k,r}^K WS_{rt} + a_{W,2,k,r}^K (WS_{rt})^{a_{W,3,k,r}^K} + a_{P,1,k,r}^K PREC_{rt} + a_{P,2,k,r}^K (PREC_{rt})^{a_{P,3,k,r}^K} + a_{C,1,k,r}^K CYC_{rt} \right. \\ \left. + a_{C,2,k,r}^K (CYC_{rt})^{a_{C,3,k,r}^K} + a_{D,1,k,r}^K DRO_{rt} + a_{D,2,k,r}^K (DRO_{rt})^{a_{D,3,k,r}^K} \right) \quad (31)$$

damage function labour productivity

$$D_{k,r_t}^N = \exp \left( -\phi^{G_{k,r}^A} G_{k,r,t}^A \right) \left( a_{T,1,k,r}^N T_{rt} + a_{T,2,k,r}^N (T_{rt})^{a_{T,3,k,r}^N} + a_{SL,1,k,r}^N SL_t + a_{SL,2,k,r}^N (SL_t)^{a_{SL,3,k,r}^N} \right. \\ \left. + a_{W,1,k,r}^N WS_{rt} + a_{W,2,k,r}^N (WS_{rt})^{a_{W,3,k,r}^N} + a_{P,1,k,r}^N PREC_{rt} + a_{P,2,k,r}^N (PREC_{rt})^{a_{P,3,k,r}^N} + a_{C,1,k,r}^N CYC_{rt} \right. \\ \left. + a_{C,2,k,r}^N (CYC_{rt})^{a_{C,3,k,r}^N} + a_{D,1,k,r}^N DRO_{rt} + a_{D,2,k,r}^N (DRO_{rt})^{a_{D,3,k,r}^N} \right) \quad (32)$$

government expenditure for adaptation measures

$$G_{k,r,t}^A = \eta_{G^A,k,r,t} \quad (33)$$

TFP

$$A_{k,r,t} = A_{k,r,0} \exp \left( \eta_{A,k,r,t} \right) \quad (34)$$

capital specific productivity

$$A_{k,r,t}^K = A_{k,r,0}^K \exp \left( \eta_{A^K,k,r,t} \right) \quad (35)$$

labour specific productivity

$$A_{k,r,t}^N = A_{k,r,0}^N \exp \left( \eta_{A^N,k,r,t} \right) \quad (36)$$

price of regional sectoral goods

$$\frac{P_{k,r_t}}{P_{k,t}} = \omega_{k,r}^Q \frac{1}{\eta_k^Q} \left( \frac{Y_{k,r_t}}{Y_{k,t}} \right)^{\frac{(-1)}{\eta_k^Q}} \quad (37)$$

production function

$$Y_{k,r_t} = A_{k,r_t} \left( 1 - D_{k,r_t} \right) \left( \alpha_{k,r}^K \frac{1}{\eta_{k,r}^{N,K}} \left( A_{k,r_t}^K K_{k,r_t-1} \right)^{\frac{\eta_{k,r}^{N,K}-1}{\eta_{k,r}^{N,K}}} + \alpha_{k,r}^N \frac{1}{\eta_{k,r}^{N,K}} \left( A_{k,r_t}^N (1 - Popt N_{k,r_t}) \right)^{\frac{\eta_{k,r}^{N,K}-1}{\eta_{k,r}^{N,K}}} \right)^{\frac{\eta_{k,r}^{N,K}}{\eta_{k,r}^{N,K}-1}} \quad (38)$$

firms FOC capital

$$r_{k,r_t} \left( 1 + \tau_{k,r,t}^K \right) = \alpha_{k,r}^K \frac{1}{\eta_{k,r}^{N,K}} A_{k,r_t}^K \frac{\eta_{k,r}^{N,K}-1}{\eta_{k,r}^{N,K}} \left( \frac{K_{k,r_t-1}}{Y_{k,r_t}} \right)^{\frac{-1}{\eta_{k,r}^{N,K}}} \quad (39)$$

firms FOC labour

$$\frac{W_{k,r_t} \left( 1 + \tau_{k,r,t}^N \right)}{P_{k,r_t}} = \alpha_{k,r}^N \frac{1}{\eta_{k,r}^{N,K}} \left( \frac{A_{k,r_t}^N Popt N_{k,r_t}}{Y_{k,r_t}} \right)^{\frac{-1}{\eta_{k,r}^{N,K}}} \quad (40)$$

## A.2 Aggregation

relative price of sectoral output

$$\frac{P_{k,t}}{P_t} = \omega_k^Q \frac{1}{\eta_k^Q} \left( \frac{Y_{k,t}}{Y_t} \right)^{\frac{(-1)}{\eta_k^Q}} \quad (41)$$

sectoral CES aggregation

$$Y_{k,t} = \left( \sum_r^R \omega_{k,r}^Q \frac{1}{\eta_k^Q} Y_{k,r,t} \frac{\eta_k^Q-1}{\eta_k^Q} \right)^{\frac{\eta_k^Q}{\eta_k^Q-1}} \quad (42)$$

### A.3 Households

households FOC labour

$$\frac{W_{k,r,t} (1 - \tau^N) \left( \frac{C_t}{Pop_t} \right)^{(-\sigma^C)}}{(1 + \tau^C) P_t} = \phi^L N_{k,t} \sigma^L \quad (43)$$

households FOC capital

$$\frac{\left( \frac{P_{t+1} C_{t+1}}{Pop_{t+1}} \right)^{(-\sigma^C)}}{(1 + \tau^C) P_{t+1}} \beta P_{k,r,t+1} r_{k,r,t+1} (1 - \tau^K) + \beta \omega_{k,r,t+1}^I (1 - \delta) = \omega_{k,r,t}^I \quad (44)$$

households FOC investment

$$\begin{aligned} P_{k,r,t} \frac{\left( \frac{C_t}{Pop_t} \right)^{(-\sigma^C)}}{P_t (1 + \tau^C)} &= \omega_{k,r,t}^I \frac{\left( \frac{C_t}{Pop_t} \right)^{(-\sigma^C)}}{P_t (1 + \tau^C)} \left( \Gamma \left( \frac{I_{k,r,t}}{I_{k,r,t-1}} \right) - \Gamma' \left( \frac{I_{k,r,t}}{I_{k,r,t-1}} \right) \left( \frac{I_{k,r,t}}{I_{k,r,t-1}} \right) \right) \\ &+ \omega_{k,r,t+1}^I \frac{\left( \frac{C_{t+1}}{Pop_{t+1}} \right)^{(-\sigma^C)}}{(1 + \tau^C) P_{t+1}} \beta \Gamma' \left( \frac{I_{k,r,t+1}}{I_{k,r,t}} \right) \frac{I_{k,r,t+1}^2}{I_{k,r,t}^2} \end{aligned} \quad (45)$$

households LOM capital

$$K_{k,r,t} = K_{k,r,t-1} (1 - \delta) + I_{k,r,t} \Gamma \left( \frac{I_{k,r,t}}{I_{k,r,t-1}} \right) \quad (46)$$

households FOC foreign bonds

$$\frac{\left( \frac{C_{t+1}}{Pop_{t+1}} \right)^{(-\sigma^C)}}{(1 + \tau^C) P_{t+1}} \beta S_{t+1}^f \exp \left( -\phi^B \left( \frac{B_t S_{t+1}^f r_{t+1}^f}{Y_{t+1}} + \frac{NX_t}{Y_t} \right) \right) (1 + r_{t+1}^f) = \frac{\left( \frac{C_t}{Pop_t} \right)^{(-\sigma^C)}}{P_t (1 + \tau^C)} \quad (47)$$

### A.4 Climate Variables

temperature

$$T_{r,t} = T_{0,r} + \eta_{T,r,t} \quad (48)$$

wind speed

$$WS_{r,t} = WS_{0,r} + \eta_{WS,r,t} \quad (49)$$

precipitation

$$PREC_{r,t} = PREC_{0,r} + \eta_{PREC,r,t} \quad (50)$$

sea level

$$SL_t = SL_0 + \eta_{SL,t} \quad (51)$$

### A.5 Trade

trade balance

$$NX_t = - \left( B_t - (1 + r_t^f) S_t^f B_{t-1} \right) \quad (52)$$

net exports

$$NX_t = \rho^{NX} NX_{t-1} + Y_t (1 - \rho^{NX}) \exp(\eta_{NX,t}) \omega^{NX} \quad (53)$$

foreign interest rates

$$r_t^f = \bar{r}^f \quad (54)$$

### A.6 Government

budget constraint

$$\begin{aligned} P_t G_t + \sum_r \sum_k P_t G_{k,r,t}^A + P_t S_t^f (1 + r_t^f) B_{G,t-1} &= P_t B_{G,t} + C_t P_t \tau^C + \sum_k \sum_r N_{k,r,t} W_{k,r,t} (\tau^N + \tau_{k,r,t}^N) \\ &+ K_{k,r,t} r_{k,r,t} P_{k,r,t} (\tau^K + \tau_{k,r,t}^K) \end{aligned} \quad (55)$$

government foreign debt

$$B_{G,t} = \eta_{B_{G,t}} \quad (56)$$

tax rates on capital expenditure

$$\tau_{k,r,t}^K = \tau_{k,r,0}^K + \eta_{k,r,t}^{\tau^K} \quad (57)$$

tax rates on labour compensation

$$\tau_{k,r,t}^N = \tau_{k,r,0}^N + \eta_{k,r,t}^{\tau^N} \quad (58)$$



## A.7 Aggregates

national price level

$$P_t = \exp(\eta_{P_t}) \quad (59)$$

national population

$$Pop_t = Pop_0 + \eta_{Pop,t} \quad (60)$$

resource constraint

$$Y_t = C_t + I_t + G_t + \sum_k^K \sum_r^R G_{k,r,t}^A + NX_t \quad (61)$$

sector labour

$$N_{kt} = \sum_r^R N_{k,r,t} \quad (62)$$

sector wage bill

$$N_{kt} W_{kt} = \sum_r^R N_{k,r,t} W_{k,r,t} \quad (63)$$

sector investment

$$P_{kt} I_{kt} = \sum_r^R P_{k,r,t} I_{k,r,t} \quad (64)$$

sector capital stock

$$P_{kt} K_{kt} = \sum_r^R P_{k,r,t} K_{k,r,t} \quad (65)$$

national investment

$$P_t I_t = \sum_k^K P_{kt} I_{kt} \quad (66)$$

national capital

$$P_t K_t = \sum_k^K P_{kt} K_{kt-1} \quad (67)$$

national output

$$P_t Y_t = \sum_k^K P_{kt} Y_{kt} \quad (68)$$

national labour share

$$N_t = \sum_k^K N_{kt} \quad (69)$$

## **B Additional and modified model equations for input-output extension**

## B.1 Regional Industries

demand for regional sector output

$$\frac{P_{k,r,t}^D}{P_{k,t}^D} = \omega_{k,r}^Q \frac{1}{\eta_k^Q} \left( \frac{Q_{k,r,t}}{Q_{k,t}} \right)^{\frac{(-1)}{\eta_k^Q}} \quad (70)$$

output production function

$$Q_{k,r,t} = \left( \omega_{k,r}^{Q^I} \frac{1}{\eta_{k,r}^{I^I}} \left( Q_{k,r,t}^I \right)^{\frac{\eta_{k,r}^{I^I} - 1}{\eta_{k,r}^{Q^I}}} + \left( 1 - \omega_{k,r}^{Q^I} \right) \frac{1}{\eta_{k,r}^{I^I}} \left( Y_{k,r,t} \right)^{\frac{\eta_{k,r}^{I^I} - 1}{\eta_{k,r}^{I^I}}} \right)^{\frac{\eta_{k,r}^{I^I}}{\eta_{k,r}^{I^I} - 1}} \quad (71)$$

demand for gross value added products

$$\frac{P_{k,r,t}}{P_{k,r,t}^D} = \left( 1 - \omega_{k,r}^{Q^I} \right) \frac{1}{\eta_k^I} \left( \frac{Y_{k,r,t}}{Q_{k,r,t}} \right)^{\frac{(-1)}{\eta_k^I}} \quad (72)$$

demand for intermediate products

$$\frac{P_t}{P_{k,r,t}^D} = \omega_{k,r}^{Q^I} \frac{1}{\eta_k^I} \left( \frac{Q_{k,r,t}^I}{Q_{k,r,t}} \right)^{\frac{(-1)}{\eta_k^I}} \quad (73)$$

## B.2 Aggregation

demand for domestically used sectoral products

$$\frac{P_{k,t}^D}{P_t^D} = \omega_k^Q \frac{1}{\eta_k^Q} \left( \frac{Q_{k,t}^D}{Q_t^D} \right)^{\frac{(-1)}{\eta_k^Q}} \quad (74)$$

use of domestically produced products

$$Q_{k,t} = Q_{k,t}^D + X_{k,t} \quad (75)$$

sectoral CES aggregation

$$Q_{k,t} = \left( \sum_r^R \omega_{k,r}^Q \frac{1}{\eta_k^Q} Q_{k,r,t}^{\frac{\eta_k^Q - 1}{\eta_k^Q}} \right)^{\frac{\eta_k^Q}{\eta_k^Q - 1}} \quad (76)$$

demand for domestically used and produced products

$$\frac{P_t^D}{P_t} = (1 - \omega^F) \frac{1}{\eta^F} \left( \frac{Q_t^D}{Q_t^U} \right)^{\frac{(-1)}{\eta^F}} \quad (77)$$

demand for imports

$$\frac{P_t^M}{P_t} = (\omega^F) \frac{1}{\eta^F} \left( \frac{M_t}{Q_t^U} \right)^{\frac{(-1)}{\eta^F}} \quad (78)$$

demand for sectoral imports

$$\frac{P_{k,t}^M}{P_t^M} = (\omega^F) \frac{1}{\eta^F} \left( \frac{M_{k,t}}{M_t} \right)^{\frac{(-1)}{\eta^F}} \quad (79)$$

## B.3 Aggregates

resource constraint

$$\frac{P_t^D}{P_t} Q_t = C_t + I_t + G_t + \sum_k^K \sum_r^R G_{k,r,t}^A + Q_t^I + NX_t \quad (80)$$

total demand for intermediate products

$$P_t Q_t^I = \sum_k^K \sum_r^R P_t Q_{k,r,t}^I \quad (81)$$

total sectoral demand for intermediate products

$$P_t Q_{k,t}^I = \sum_r^R P_t Q_{k,r,t}^I \quad (82)$$

definition of domestically used and produced products

$$P_t^D Q_t^D = \sum_k P_{k,t}^D Q_{k,t}^D \quad (83)$$

definition of domestic output

$$P_t Q_t = \sum_k^K P_{k,t}^D Q_{k,t}^D \quad (84)$$

definition of domestically used products

$$P_t Q_t^U = P_t^M M_t + P_t^D Q_t^D \quad (85)$$

exports

$$P_t^D X_t = \sum_k^K P_{k,t}^D X_{k,t} \quad (86)$$

imports

$$P_t^M M_t = \sum_k^K P_{k,t}^M M_{k,t} \quad (87)$$

net exports

$$P_t N X_t = P_t^D X_t - P_t^M M_t \quad (88)$$

## B.4 Trade

demand for sectoral exports

$$\begin{aligned} X_{k,t} &= D_{k,t}^X Q_{k,t} \\ D_{k,t}^X &= D_{k,0}^X + \eta_{k,t}^X \end{aligned} \quad (89)$$

price for sectoral imports

$$P_{k,t}^M = P_{k,0}^M + \eta_{k,t}^M \quad (90)$$

## C Additional and modified model equations for energy extension

## C.1 Regional Energy industries

output production function

$$Q_{k,r,t} = \left( \omega_{k,r}^{Q^I} \eta_{k,r}^{\frac{1}{\eta_k^I}} \left( Q_{k,r,t}^{I,E} \right)^{\frac{\eta_{k,r}^{Q^I} - 1}{\eta_k^I}} + \left( 1 - \omega_{k,r}^{Q^I} \right) \eta_{k,r}^{\frac{1}{\eta_k^I}} \left( Y_{k,r,t} \right)^{\frac{\eta_{k,r}^{Q^I} - 1}{\eta_k^I}} \right)^{\frac{\eta_{k,r}^I}{\eta_k^I - 1}} \quad (91)$$

nested composition function for intermediate energy and non-energy inputs

$$Q_{k,r,t}^{I,E} = \left( \left( 1 - \omega_{k,r}^{Q^E} \right) \eta_{k,r}^{\frac{1}{\eta_k^E}} \left( Q_{k,r,t}^{I,E} \right)^{\frac{\eta_{k,r}^{Q^E} - 1}{\eta_k^E}} + \left( \omega_{k,r}^{Q^E} \right) \eta_{k,r}^{\frac{1}{\eta_k^E}} \left( E_{k,r,t} \right)^{\frac{\eta_{k,r}^{Q^E} - 1}{\eta_k^E}} \right)^{\frac{\eta_{k,r}^E}{\eta_k^E - 1}} \quad (92)$$

nested composition function for energy inputs

$$E_{k,r,t} = \left( \sum_c^{EC} \omega_{k,r,c}^{Q^E} \eta_{k,r}^{\frac{1}{\eta_k^{EC}}} \left( E_{k,r,c,t} \right)^{\frac{\eta_{k,r}^{EC} - 1}{\eta_k^{EC}}} \right)^{\frac{\eta_{k,r}^{EC}}{\eta_k^{EC} - 1}} \quad (93)$$

demand for intermediate products

$$\frac{P_{k,r,t}^I}{P_{k,r,t}^D} = \omega_{k,r}^{Q^I} \eta_k^{\frac{1}{\eta_k^I}} \left( \frac{Q_{k,r,t}^I}{Q_{k,r,t}^{I,E}} \right)^{\frac{(-1)}{\eta_k^I}} \quad (94)$$

demand for energy as intermediate product

$$\frac{P_{k,r,t}^E}{P_{k,r,t}^I} = \omega_{k,r}^E \eta_{k,r}^{\frac{1}{\eta_k^E}} \left( \frac{E_{k,r,t}}{Q_{k,r,t}^{I,E}} \right)^{\frac{(-1)}{\eta_k^E}} \quad (95)$$

demand for non-energy intermediate products

$$\frac{P_t}{P_{k,r,t}^I} = \left( 1 - \omega_{k,r}^E \right) \eta_{k,r}^{\frac{1}{\eta_k^E}} \left( \frac{Q_{k,r,t}^I}{Q_{k,r,t}^{I,E}} \right)^{\frac{(-1)}{\eta_k^E}} \quad (96)$$

## C.2 Aggregates

total demand for intermediate products

$$P_t Q_t^I = \sum_k^K \sum_r^R \begin{cases} P_{k,r,t}^I Q_{k,r,t}^{I,E} & \text{if } k = k^E \\ P_t Q_{k,r,t}^I & \text{otherwise} \end{cases} \quad (97)$$

total consumption of energy carrier

$$E_{c,t} = \sum_r^R E_{k^E,r,c,t} \quad (98)$$

price of energy carrier

$$P_{c,t}^{EC} = P_{c,0}^{EC} + \eta_{c,t}^{EC} \quad (99)$$

Table 1: List of symbols for baseline version

Variable	L <sup>A</sup> T <sub>E</sub> X	Description
Endogenous		
P	$P$	price level
K	$K$	capital stock
C	$C$	consumption
PoP	$Pop$	population
B	$B$	international traded bonds
Sf	$S^f$	effective exchange rate with the rest of the world
BG	$BG$	government debt
NX	$NX$	net exports
rf	$r^f$	foreign interest rate
G	$G$	government expenditure
I	$I$	private investment
Y	$Y$	GDP
N	$N$	labour
SL	$SL$	sea level
PREC <sub>r</sub>	$PREC_r$	regional precipitation
T <sub>r</sub>	$T_r$	regional temperature
WS <sub>r</sub>	$W_r^S$	regional wind speed
Y <sub>k</sub>	$Y_k$	sector GDP
K <sub>k</sub>	$K_k$	sector capital
N <sub>k</sub>	$N_k$	sector employment
I <sub>k</sub>	$I_k$	sector private investment
P <sub>k</sub>	$P_k$	sector price index
W <sub>k</sub>	$W_k$	sector wage index
Y <sub>k,r</sub>	$Y_{k,r}$	regional sector GDP
D <sub>k,r</sub>	$D_{k,r}$	regional sector damages
K <sub>k,r</sub>	$K_{k,r}$	regional sector capital
N <sub>k,r</sub>	$N_{k,r}$	regional sector employment
W <sub>k,r</sub>	$W_{k,r}$	regional sector wages
A <sub>k,r</sub>	$A_{k,r}$	regional sector TFP
GA <sub>k,r</sub>	$G_{k,r}^A$	regional sector adaptation government expenditure
gA <sub>k,r</sub>	$g_{k,r}^A$	regional growth rate of sector TFP
AN <sub>k,r</sub>	$A_{k,r}^N$	regional sector labour specific TFP
AK <sub>k,r</sub>	$A_{k,r}^K$	regional sector capital specific TFP
I <sub>k,r</sub>	$I_{k,r}$	regional sector private investment
P <sub>k,r</sub>	$P_{k,r}$	regional sector price index
omegaI <sub>k,r</sub>	$\omega_{k,r}^I$	shadow value of regional private sector investment
r <sub>k,r</sub>	$r_{k,r}$	regional sector rental rate on capital
tauK <sub>k,r</sub>	$\tau_{k,r}^K$	regional sector corporate tax rate on capital
tauN <sub>k,r</sub>	$\tau_{k,r}^N$	regional sector labour tax rate on capital
Exogenous		
exo_P	$\eta_P$	exogenous price index evolution
exo_PoP	$\eta_{Pop}$	exogenous population
exo_SL	$\eta_{SL}$	exogenous sea level
exo_NX	$\eta_{NX}$	exogenous net exports
exo_BG	$\eta_{BG}$	exogenous structural balance
exo_tauK <sub>k,r</sub>	$\eta_{\tau^K,k,r}$	exogenous sector and region corporate tax rate
exo_tauN <sub>k,r</sub>	$\eta_{\tau^N,k,r}$	exogenous sector and region labour tax rate
exo_k <sub>r</sub>	$\eta_{A,k,r}$	exogenous TFP
exo_N <sub>k,r</sub>	$\eta_{A^N,k,r}$	exogenous labour specific TFP
exo_K <sub>k,r</sub>	$\eta_{A^K,k,r}$	exogenous capital specific TFP
exo_GA <sub>k,r</sub>	$\eta_{G^A,k,r}$	exogenous sector adaptation expenditure
exo_T <sub>r</sub>	$\eta_{T,r}$	exogenous regional temperature
exo_PREC <sub>r</sub>	$\eta_{PREC,r}$	exogenous regional precipitation
exo_WS <sub>r</sub>	$\eta_{WS,r}$	exogenous regional wind speed
Parameters		
omegaQ <sub>k,p</sub>	$\omega_{k,p}^Q$	distribution parameter for output from one sector
etaQ <sub>k,p</sub>	$\eta_{k,p}^Q$	elasticity of substitution between regional production
tauK <sub>k,r,p</sub>	$\tau_{k,r}^K$	region and sector specific tax rate on capital
tauN <sub>k,r,p</sub>	$\tau_{k,r}^N$	region and sector specific tax rate on labour
rhoA <sub>k,r,p</sub>	$\rho_{k,r}^A$	persistence productivity shock
rhoAN <sub>k,r,p</sub>	$\rho_{k,r}^{A,N}$	persistence labour specific productivity shock
rhoAK <sub>k,r,p</sub>	$\rho_{k,r}^{A,K}$	persistence capital specific productivity shock
phiY <sub>k,r,p</sub>	$\frac{P_{k,r,0} Y_{k,r,0}}{P_0 Y_0}$	long-run share of regional and sectoral output

Table 1 – Continued

Variable	L <sup>A</sup> T <sub>E</sub> X	Description
phiN.k.r.p	$\frac{N_{k,r,0}}{P_{k,r,0} Y_{k,r,0}}$	long-run share of regional and sectoral employment
phiY0.k.r.p	$\frac{Y_{k,r,0}}{P_0 Y_0}$	terminal share of regional and sectoral output
phiN0.k.r.p	$\frac{N_{k,r,0}}{P_{k,r,0} Y_{k,r,0}}$	initial share of regional and sectoral employment
phiYT.k.r.p	$\frac{Y_{k,r,0}}{P_0 Y_0}$	terminal share of regional and sectoral output
phiNT.k.r.p	$\frac{N_{k,r,0}}{P_{k,r,0} Y_{k,r,0}}$	terminal share of regional and sectoral employment
phiW.k.r.p	$\frac{W_{k,r,0} N_{k,r,0}}{P_{k,r,0} Y_{k,r,0}}$	share of regional and sectoral employment
phiP.k.r.p	$\frac{P_{k,r,0}}{P_0}$	share of regional and sectoral employment
phiL.k.r.p	$\phi_{k,r}^L$	coefficient of disutility to work
omegaQ.k.r.p	$\omega_{k,r}^Q$	distribution parameter for regional production
alphaK.k.r.p	$\alpha_{k,r}^K$	distribution parameter capital share
alphaN.k.r.p	$\alpha_{k,r}^N$	distribution parameter labour share
etaNK.k.r.p	$\eta_{k,r}^{N,K}$	elasticity of substitution between labour and capital
A.k.r.p	$A_{k,r}$	sector long-run TFP
GAT.k.r.p	$G_{T,k,r}^A$	sector region specific government expenditure for adaptation
phiGA.k.r.p	$\phi_{k,r}^{G^A}$	coefficient of effectiveness of government expenditure on adaptation measures
gY0.k.r.p	$\frac{Y_{2,k,r}}{Y_{1,k,r}}$	initial sector growth
gN0.k.r.p	$\frac{N_{2,k,r}}{N_{1,k,r}}$	initial sector labour growth
omegaA.k.r.p	$\omega_{k,r}^A$	exponent for productivity growth
A.N.k.r.p	$A_{k,r}^N$	sector labour specific TFP
A.K.k.r.p	$A_{k,r}^K$	sector capital specific TFP
a.T.k.k.r.p	$a_{1,k,r}$	intercept of damage function temperature
a.T.2.k.r.p	$a_{2,k,r}$	slope of damage function temperature
a.T.3.k.r.p	$a_{3,k,r}$	exponent of damage function temperature
a.P.k.k.r.p	$a_{1,k,r}$	intercept of damage function precipitation
a.P.2.k.r.p	$a_{2,k,r}$	slope of damage function precipitation
a.P.3.k.r.p	$a_{3,k,r}$	exponent of damage function precipitation
a.W.k.k.r.p	$a_{1,k,r}$	intercept of damage function wind speed
a.W.2.k.r.p	$a_{2,k,r}$	slope of damage function wind speed
a.W.3.k.r.p	$a_{3,k,r}$	exponent of damage function wind speed
a.SL.k.k.r.p	$a_{1,k,r}$	intercept of damage function sea level
a.SL.2.k.r.p	$a_{2,k,r}$	slope of damage function sea level
a.SL.3.k.r.p	$a_{3,k,r}$	exponent of damage function sea level
beta.p	$\beta$	discount factor
delta.p	$\delta$	capital depreciation rate
sigmaL.p	$\sigma^L$	inverse Frisch elasticity
sigmaC.p	$\sigma^C$	intertemporal elasticity of substitution
etaQ.p	$\eta^Q$	elasticity of substitution between sectoral production
phiB.p	$\phi^B$	coefficient of foreign adjustment cost
phiK.p	$\phi^K$	coefficient of investment adjustment cost
tauC.p	$\tau^C$	consumption tax
tauN.p	$\tau^N$	labour tax
tauK.p	$\tau^K$	capital tax
omegaNX.p	$\omega^{NX}$	share of net exports relative to domestic GDP
omegaNX0.p	$\omega^{NX,0}$	initial share of net exports relative to domestic GDP
omegaNXT.p	$\omega^{NX,T}$	terminal share of net exports relative to domestic GDP
rhoNX.p	$\rho^{NX}$	persistence in net exports
rhoA.p	$\rho^A$	persistence in TFP
rhoPoP.p	$\rho^{Pop}$	persistence in population
rhoSL.p	$\rho^{SL}$	persistence in sea level
rhoT.p	$\rho^T$	persistence in temperature
rhoWS.p	$\rho^T$	persistence in wind speed
rhoPREC.p	$\rho^T$	persistence in precipitation
inbsectors.p	$K$	number of sectors
inbregions.p	$R$	number of regions
lCalibration.p	$l^{Calib}$	logical indicator whether model is calibrated or not
TO.r.p	$T_{0,n}$	initial regional temperature
PREC0.r.p	$PREC_{0,n}$	initial regional precipitation
WS0.r.p	$WS_{0,n}$	initial regional wind speed
TT.r.p	$T_{T,n}$	terminal regional temperature
PRECT.r.p	$PRECT_{T,n}$	terminal regional precipitation
WST.r.p	$WST_{T,n}$	terminal regional wind speed
SL0.p	$SL_0$	initial sea level



Table 1 – Continued

Variable	$\text{\LaTeX}$	Description
PoP0_p	$POP_0$	initial population
Y0_p	$Y_0$	initial output
P0_p	$P_0$	initial price level
N0_p	$N_0$	initial employment
SLT_p	$SL_T$	terminal sea level
PoPT_p	$Pop_T$	terminal population
YT_p	$Y_0$	terminal output
NT_p	$Y_0$	terminal employment

Table 2: List of symbols for input-output extension

Variable	L <sup>A</sup> T <sub>E</sub> X	Description
Endogenous		
P <sub>D</sub>	$P^D$	price level of domestic produced products
P <sub>M</sub>	$P^M$	price level of imports
Q <sub>U</sub>	$Q^U$	domestic used products
Q <sub>D</sub>	$Q^D$	domestic produced and used products
Q <sub>I</sub>	$Q^I$	intermediate products
Q	$Q$	domestic output
M	$M$	imports
X	$X$	exports
Q <sub>k</sub>	$Q_k$	sectoral exports
Q <sub>D.k</sub>	$Q_k^D$	domestic used and produced products
Q <sub>I.k</sub>	$Q_k^I$	domestic used intermediate products
M <sub>k</sub>	$M_k$	sectoral imports
X <sub>k</sub>	$X_k$	sectoral exports
P <sub>D.k</sub>	$P_k^D$	sectoral price index of domestic products
P <sub>M.k</sub>	$P_k^M$	sectoral price index of imports
Q <sub>k,r</sub>	$Q_{k,r}$	regional sector output
Q <sub>I.k,r</sub>	$Q_{k,r}^I$	regional sector demand for intermediate products
P <sub>D.k,r</sub>	$P_{k,r}^D$	sectoral and regional price index of domestic products
Exogenous		
exo <sub>X.k</sub>	$\eta_k^X$	exogenous demand for sectoral exports
exo <sub>M.k</sub>	$\eta_k^M$	exogenous sectoral price of imports
Parameters		
phi <sub>M.k.p</sub>	$\phi_k^M$	initial share of sectoral imports
phi <sub>X.k.p</sub>	$\phi_k^X$	initial share of sectoral exports
phi <sub>QI.k.p</sub>	$\phi_k^{QI}$	initial share of sectoral intermediate inputs
D <sub>X.k.p</sub>	$D_k^X$	initial demand for sectoral exports
P <sub>M.k.p</sub>	$P_k^M$	initial price level for sectoral imports
omega <sub>M.k.p</sub>	$\omega_k^M$	distribution parameter for imports
eta <sub>I.k.p</sub>	$\eta_k^I$	elasticity of substitution between intermediate products and value added
omega <sub>QI.k.r.p</sub>	$\omega_{k,r}^{QI}$	distribution parameter between intermediate products and value added
eta <sub>M.p</sub>	$\eta^M$	elasticity of substitution between sectoral imports
eta <sub>F.p</sub>	$\eta^F$	elasticity of substitution between imports and domestic products
omega <sub>F.p</sub>	$\omega^F$	distribution parameter for imports
phi <sub>M.p</sub>	$\phi^M$	initial share of imports on total output

Table 3: List of symbols for energy extension

Variable	L <sup>A</sup> T <sub>E</sub> X	Description
Endogenous		
P_EC_c	$P_c^E$	price of energy source
EC_c	$E_c$	consumption of energy source
E_k_r	$E_{k,r}$	composite energy consumption
Q_IE_k_r	$Q_{k,r}^{I,E}$	composite intermediate products for energy sector
P_I_k_r	$P_{k,r}^{E,Q^I}$	price of composite intermediate products for energy sector
P_E_k_r	$P_{k,r}^E$	price of composite energy
E_k_r_c	$E_{k,r,c}$	regional and sectoral consumption of energy source
Exogenous		
exo_E_c	$\eta_c^E$	exogenous price for energy source
Parameters		
phiE_k_r_p	$\phi_{k,r}^E$	initial share of energy on intermediate products
phiE_k_r_c_p	$\phi_{k,r,c}^E$	initial share of energy source on energy composite intermediate product
omegaE_k_r_p	$\phi_{k,r}^E$	distribution parameter for energy on intermediate products
omegaE_k_r_c_p	$\phi_{k,r,c}^E$	distribution parameter for energy source on energy as intermediate product
etaE_k_r_p	$\eta_{k,r}^E$	elasticity of substitution between energy and other intermediate products
etaEC_k_r_p	$\eta_{k,r}^{E,C}$	elasticity of substitution between energy carriers
P_EC_c_p	$P_{c,0}^E$	initial price for energy source