

# Spatial Light Modulator Based Propagation of Partially Coherent Speckle Fields in a 4f setup

Bachelor Thesis

Paul Schulze

- Motivation
- Hypotheses
- The Theory of the Propagation of Light
- Experimental and Numerical Methods
- Results from the Experiment and the Simulation
- Conclusion

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# Motivation

- Measuring micro parts  
(size ~ 1mm)
- Requirements:
  - High accuracy
  - High speed
  - Robustness
  - Extended depth of field
- State of the art:  
No current method can fulfill all the requirements at the same time



# Motivation

- Measuring micro parts  
(size ~ 1mm)



	Phase evaluation	SWLI and OCT	SCP
High accuracy	✗	✓	✓
High speed	✓	✗	✓
Robustness	✗	✗	✗
Extended depth of field	✓	✓	✗

# Outline

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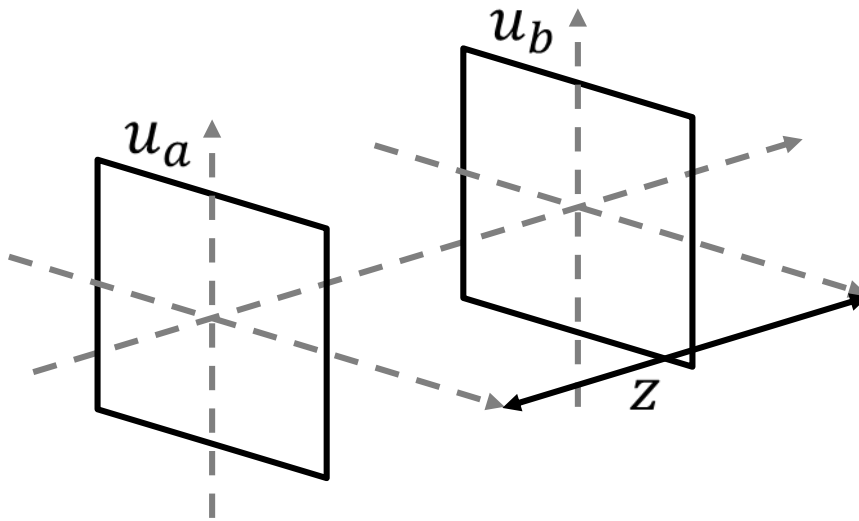
# Hypotheses

- I. The 4f setup can be simulated on the basis of Fourier optics.
- I. The Speckle size can be predicted from parameters of the light source and the 4f setup
- I. The spatial light modulator can move the focal plane in the 4f setup
- I. The depth of focus can be predicted from parameters of the light source and the 4f setup

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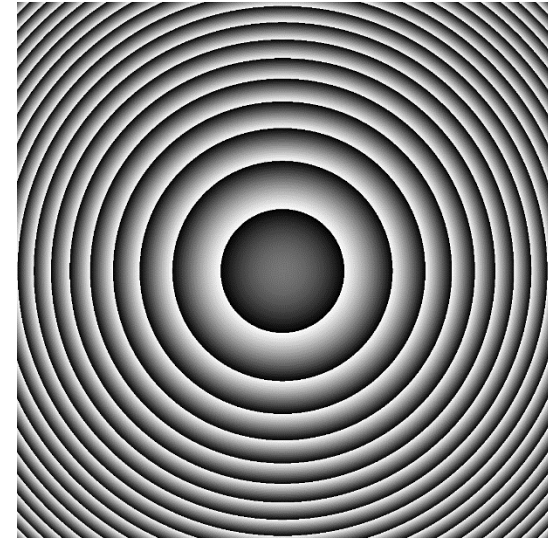


# Theory of Propagation of light



$$u_b = u_a * h_z$$

$$\mathcal{F}^{-1}\{U_b\} = \boxed{u_b = \mathcal{F}^{-1}\{U_a \cdot H_z\}}$$

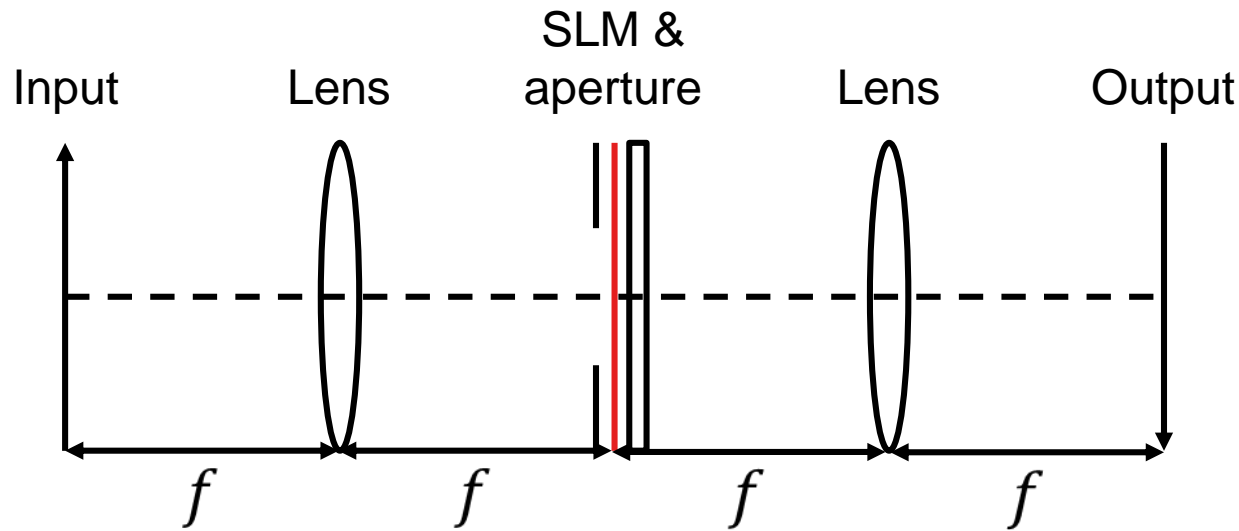


Transfer Function

$$H_z = e^{ikz\sqrt{1-\lambda^2\xi^2}}$$

⇒ The transfer function of propagation  $H_z$  is a phase modulating function in the Fourier domain

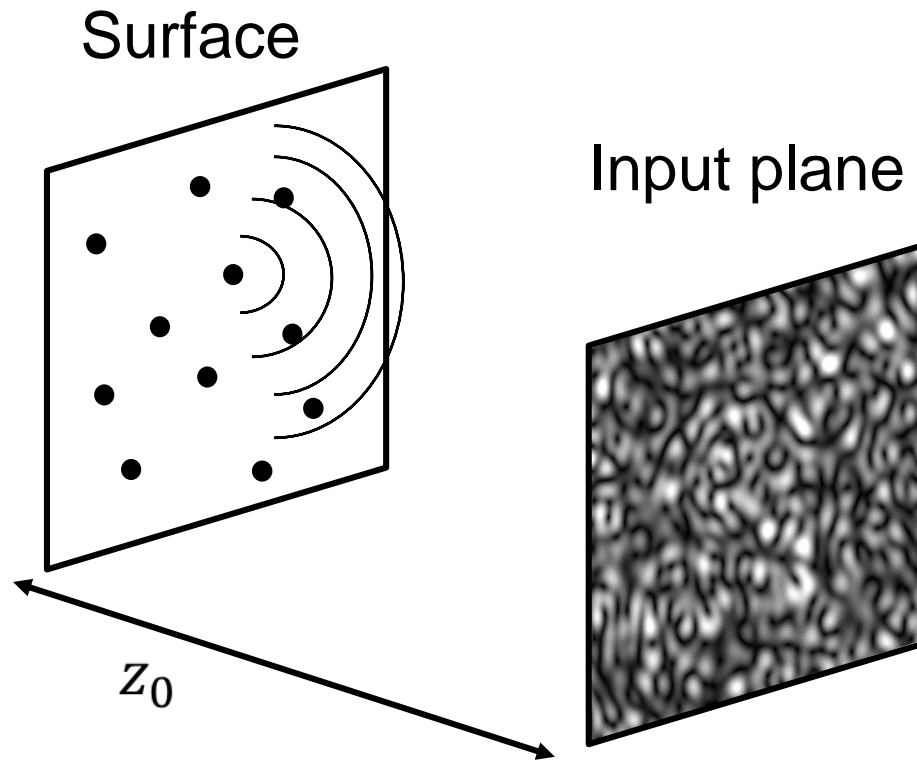
# The 4f setup



- A **Fourier representation** is created in the center
- The SLM utilizes the transfer function  $H_z$  to create a propagated representation in the output plane

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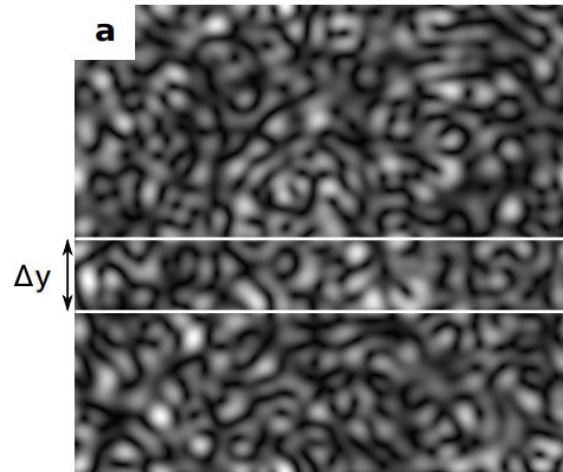
# Simulation of the Object



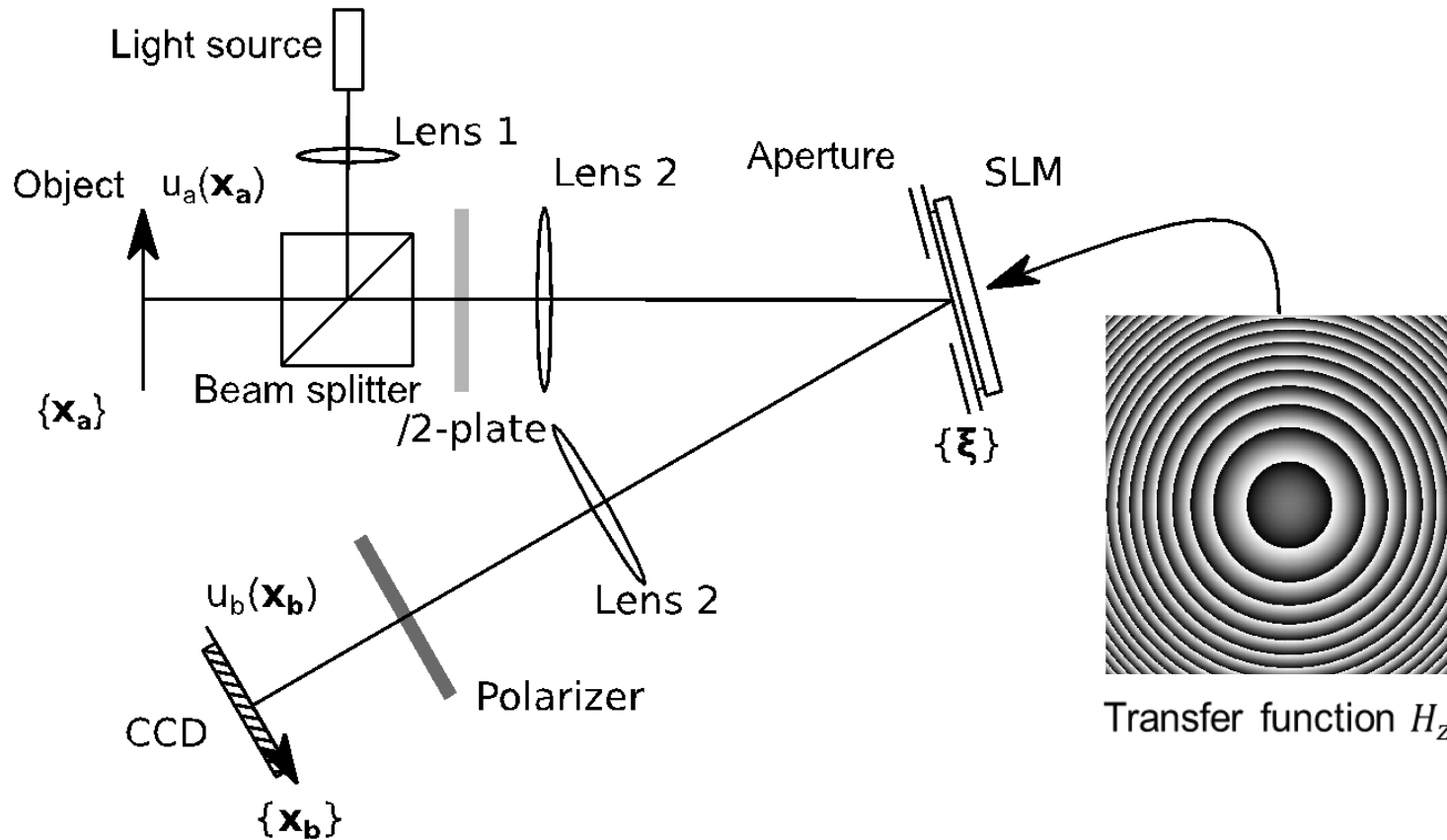
- The rough surface is approximated by a set of points
- The superposition of the spherical waves create the speckle pattern

# Speckle Size Estimation in the Simulation

bias



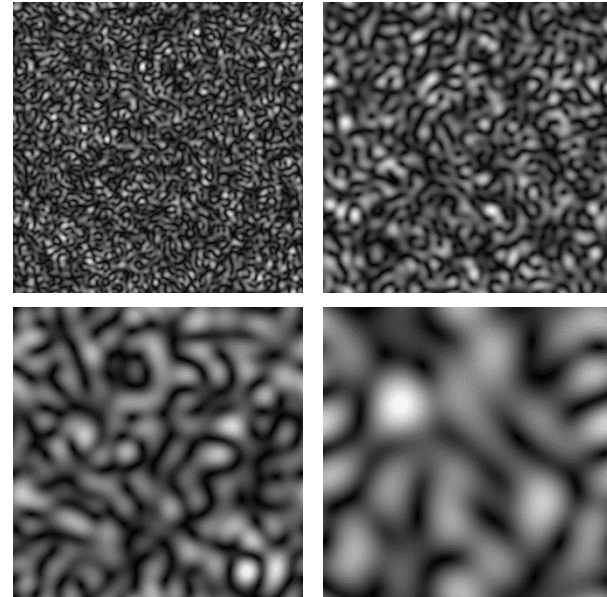
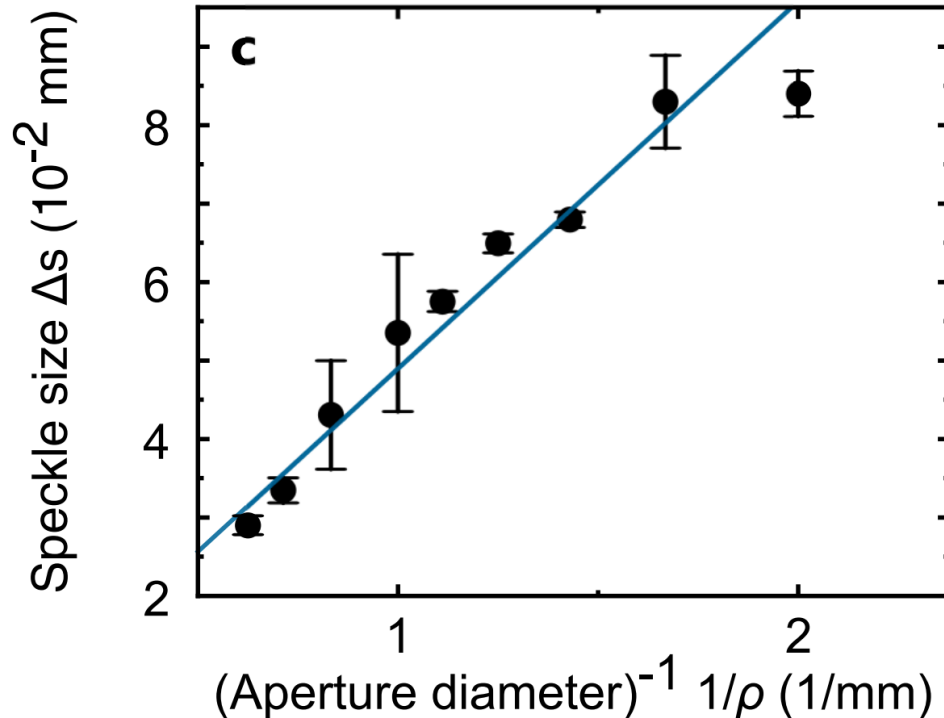
# Experimental Setup



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- **Results from the Experiment and the Simulation**
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# Simulation: Speckle Size

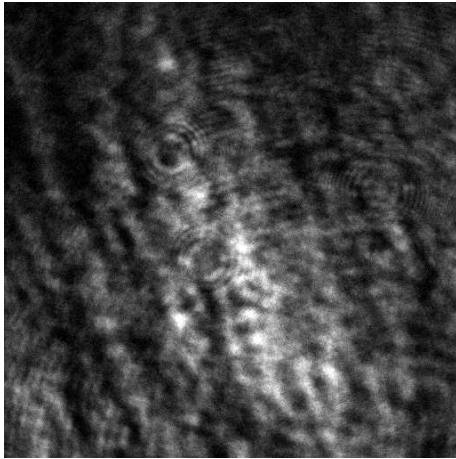


⇒ The Speckle size  $\Delta s$  is inversely proportional to the aperture diameter  $\rho$

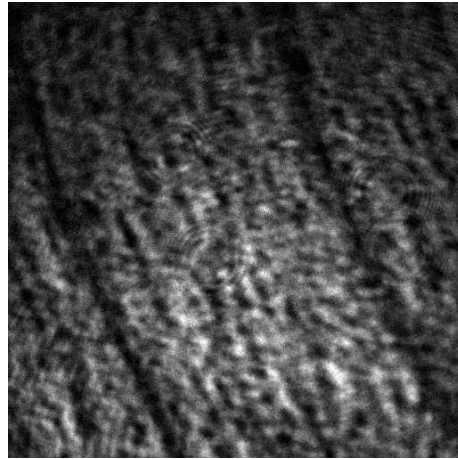
$$\Delta s \propto \frac{1}{\rho}$$



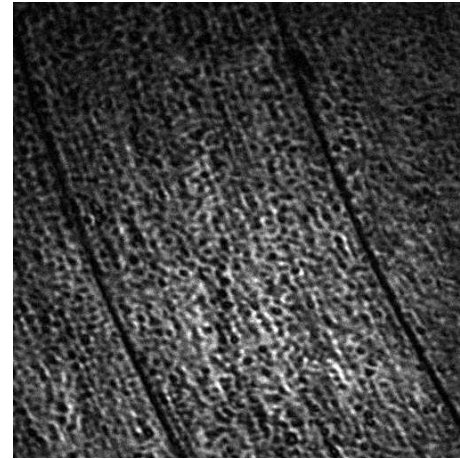
# Experiment: Speckle Size



$\rho = 3 \text{ mm}$  •



$\rho = 4.5 \text{ mm}$  •



$\rho = 6 \text{ mm}$  •

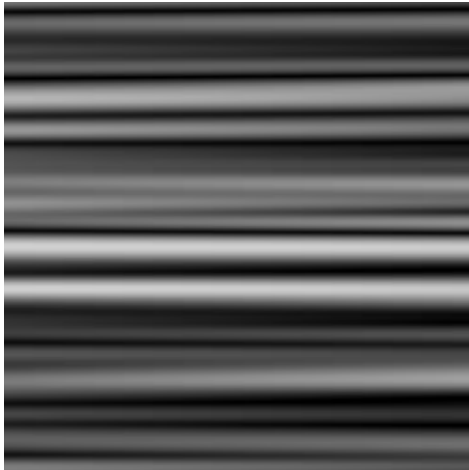
$\rho$ : Aperture diameter

⇒ Experimental validation of

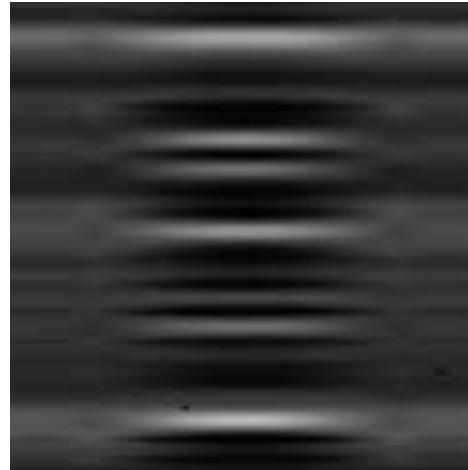
$$\Delta s \propto \frac{1}{\rho}$$

# Simulation: Partial Coherence

Amplitude cross sections of



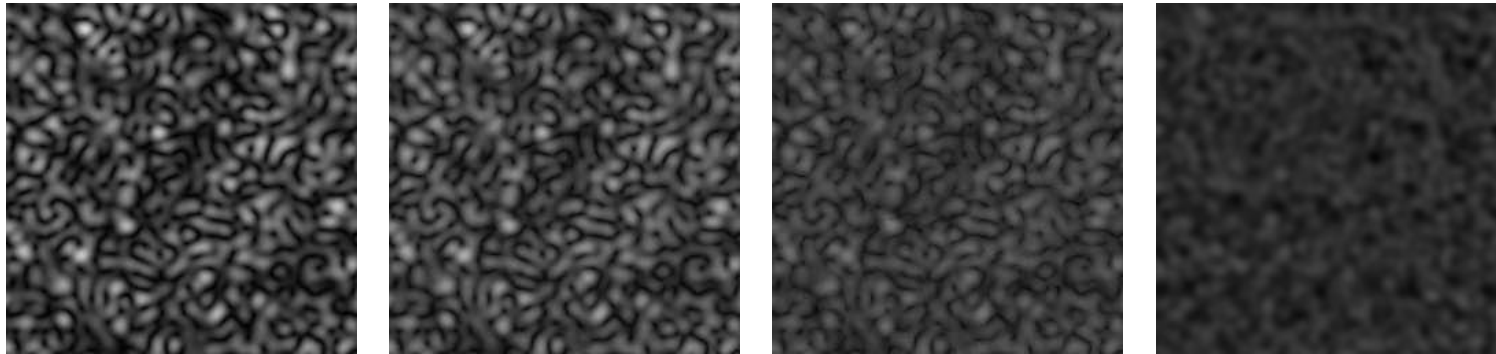
- a fully coherent wavefield



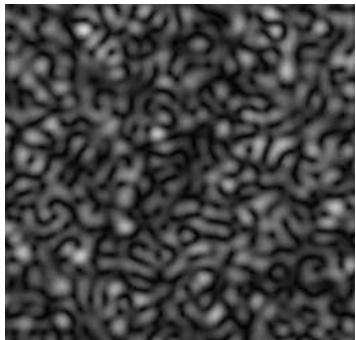
- a partially coherent wavefield

⇒ For partially coherent illumination, the area of high contrast is restricted to the vicinity of the surface

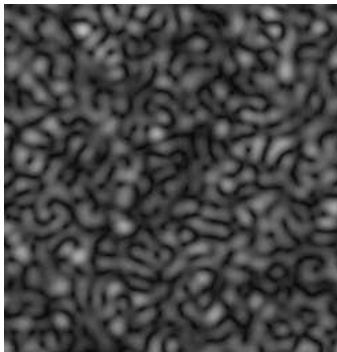
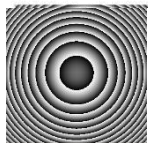
# Simulation: Partial Coherence



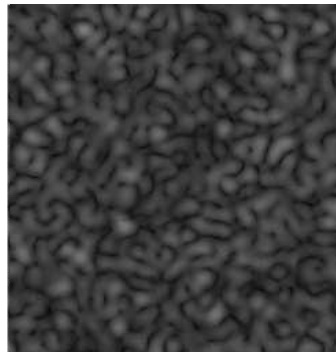
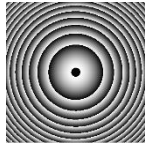
# Simulated Results



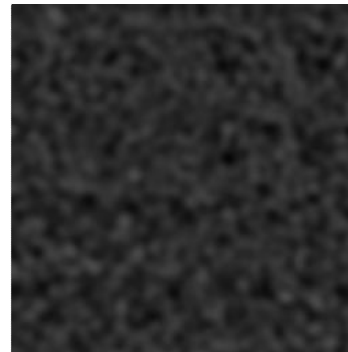
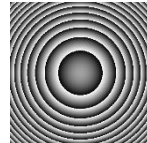
$z = 10 \text{ mm}$



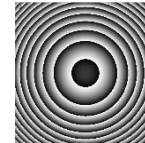
$z = 9.5 \text{ mm}$



$z = 9 \text{ mm}$

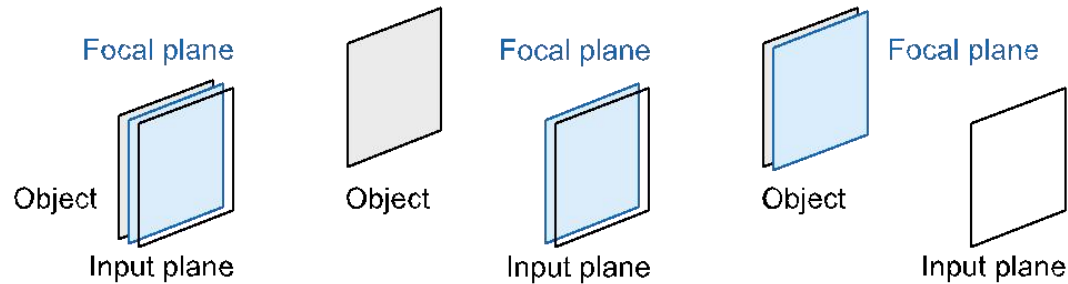
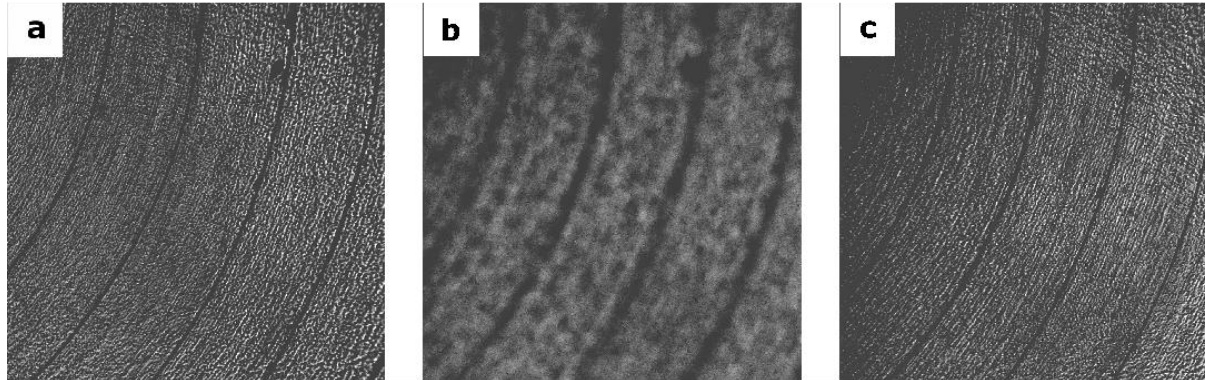


$z = 8.5 \text{ mm}$



# Experimental Results

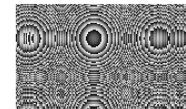
## SLM Propagation



No SLM Modulation

No SLM Modulation

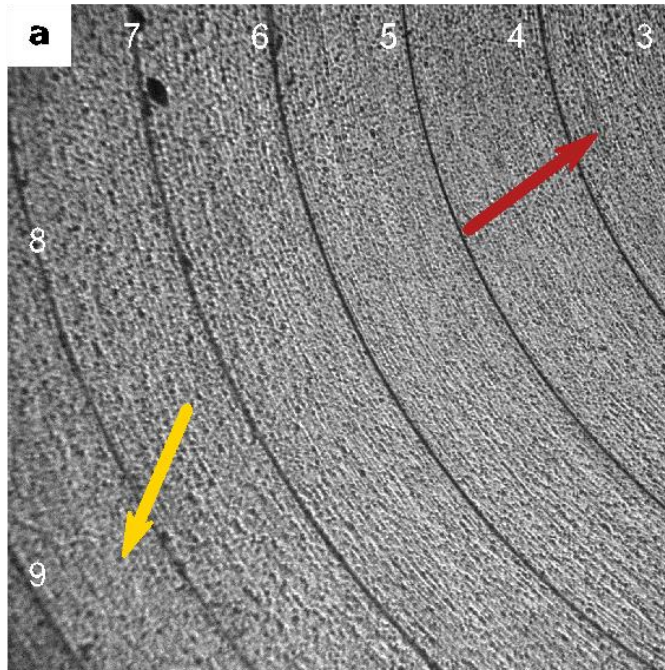
$z = 10 \text{ mm}$



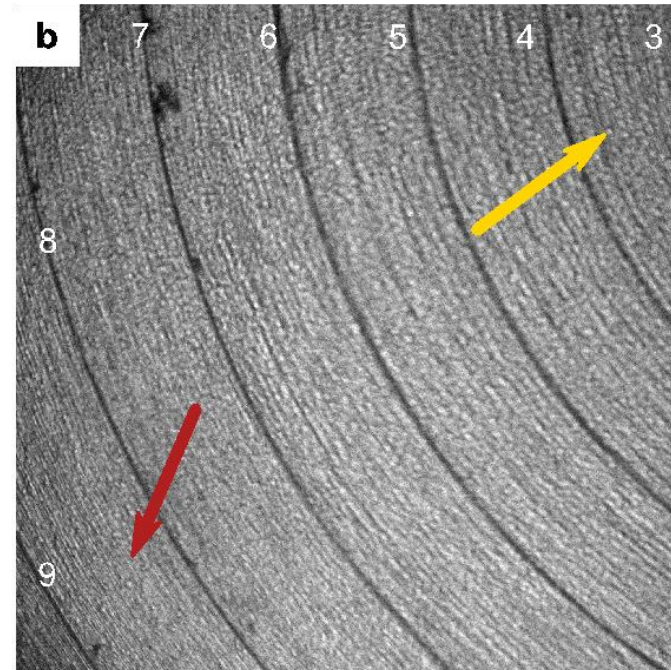


# Experimental Results

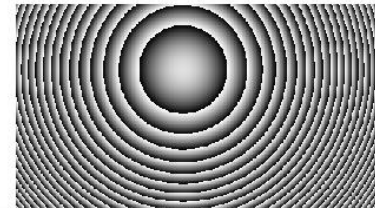
## Contrast Difference



No SLM Modulation



$z = 3 \text{ mm}$



# Conclusion

	Simulation	Experiment
I. Simulation of the 4f setup on the basis of Fourier optics	✓*	
II. Predictability of Speckle size from parameters of the 4f setup and the light source	✓	(✓)
III. Spatial light modulator based propagation	✓	✓
IV. Predictability of the area of high contrast for partially coherent illumination	✓	(✓)

# Conclusion

Hypotheses:

- I. Validation in part
- II. Full validation in simulation  
validation in part experimentally
- III. Full validation in simulation &  
experiment
- IV. Evidence strongly suggests validity