An introduction to Reinforcement Learning

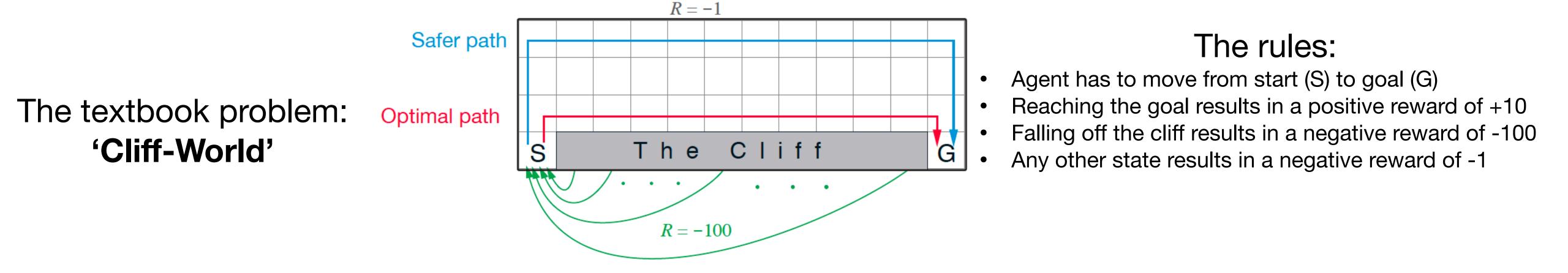
05th of July 2022

Q-Learning

Limitation of multi-armed bandit problems

Your current action does not influence what happens next!!

How can we solve sequential problems?

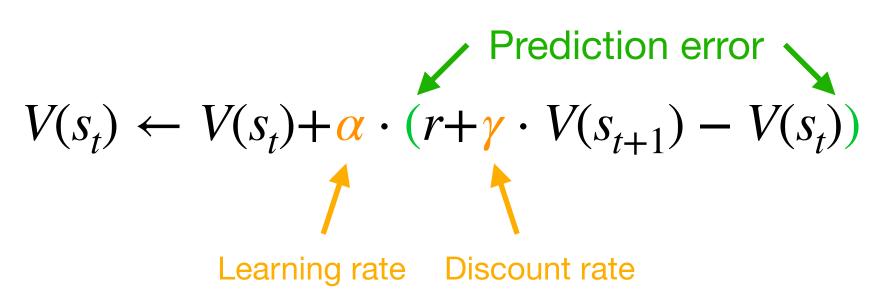


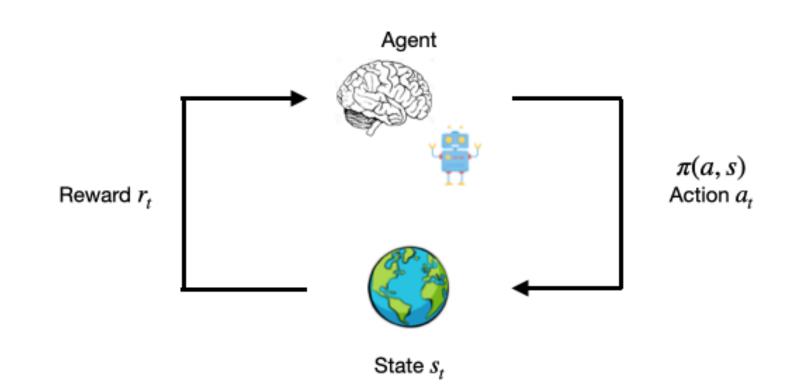
What's the problem the agent has to solve here??

Note the subtle introduction of the concept of 'transition probabilities' here - implicit, later: explicit

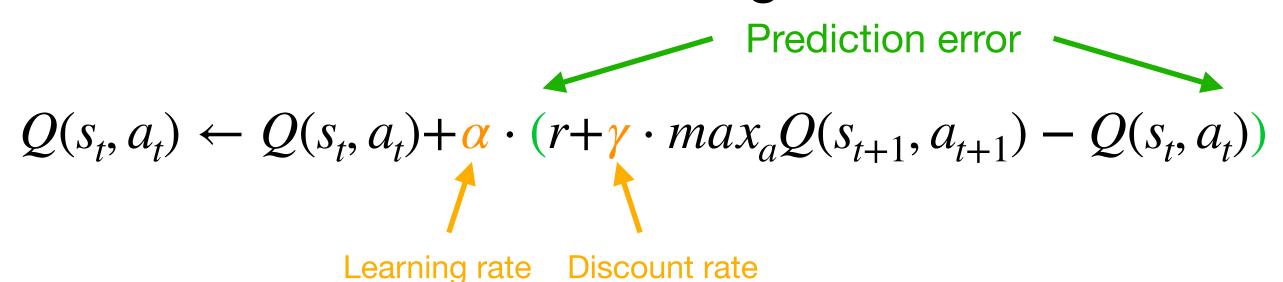
From classical to instrumental learning

TD Learning:





Q-Learning:



What's the difference between $V(s_t)$ and $Q(s_t, a_t)$?

What's is $max_aQ(s_t, a_t)$ doing?

Note that this is just an update rule - doesn't tell us how to select an action!

Coding: Q-Learning

https://github.com/schwartenbeckph/RL-Course/tree/main/2022_07_05

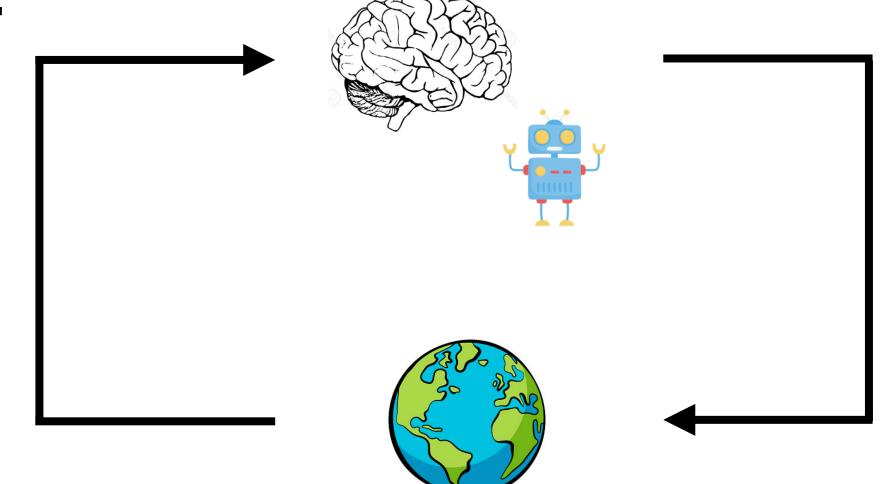
MDPs and model-based RL

Basic setup: how do agents learn to act?

Based on a reward signal, agents learn values of actions/states:



Reward r_t



Action is governed by a **policy**:

$$\pi(a,s) = P(a_t = a \mid s_t = s)$$

Action a_t

State S_t

Agents can learn a model of the environment to make smarter decisions, e.g.:

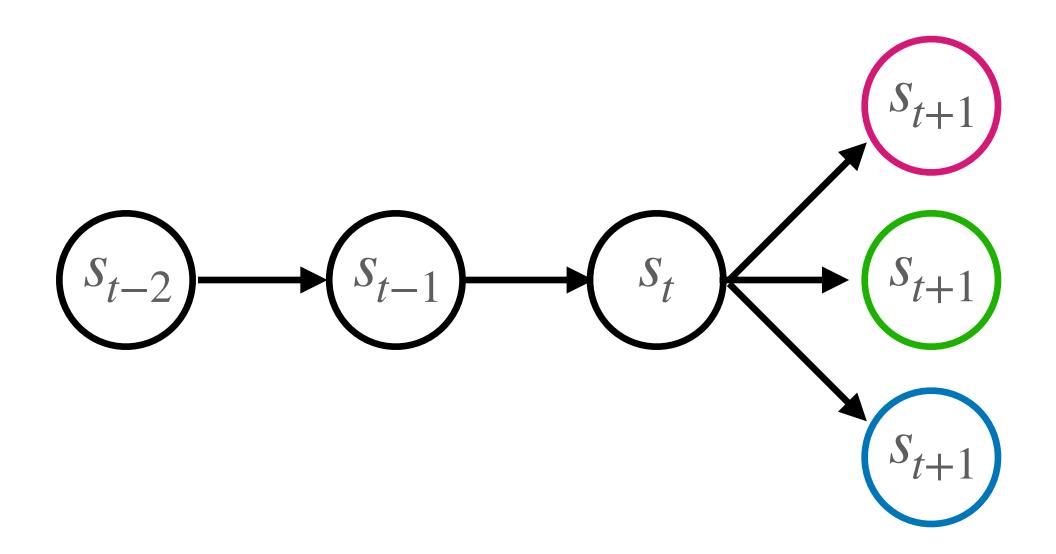
$$P(s_{t+1} = s | s_t = s, a_t = a)$$

Markov Process —

Markov Reward Process

Markov Decision Process (MDP)

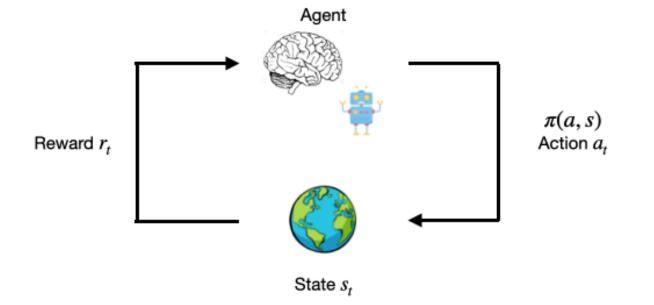
Most RL problems are problems where agents face sequences of states:



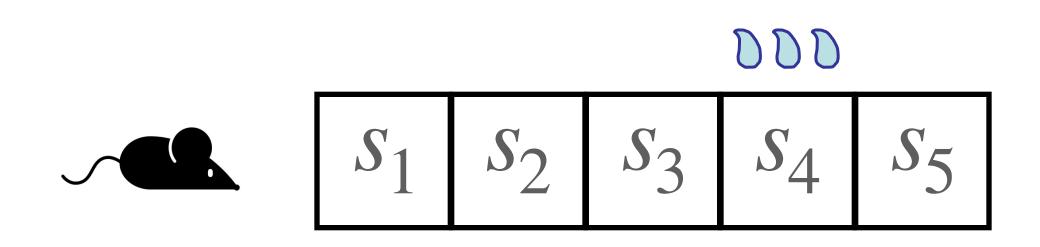
Fundamental property: Markov property

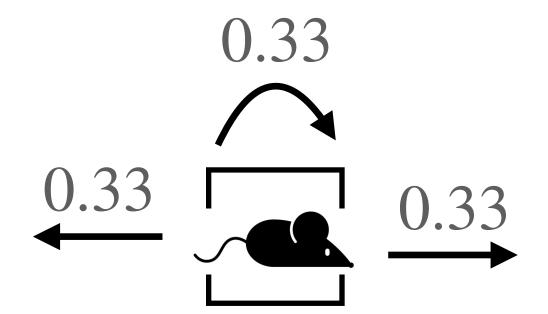
$$P(s_{t+1} = s \mid s_t, s_{t-1}, s_{t-2}, \dots) = P(s_{t+1} = s \mid s_t)$$

"The future is independent of the past given the present"

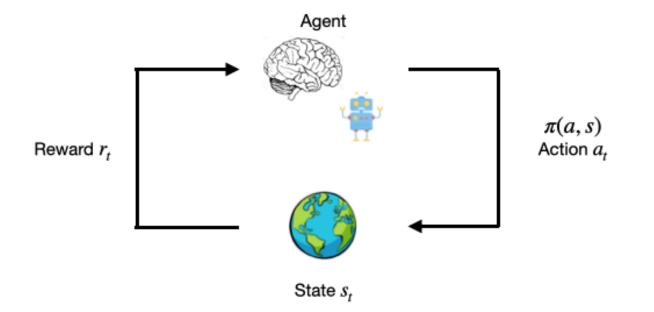


Let's assume a super simple problem:

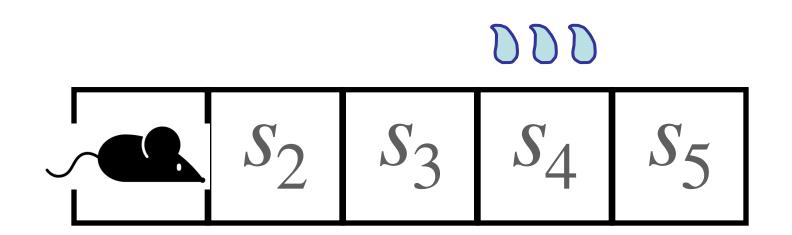


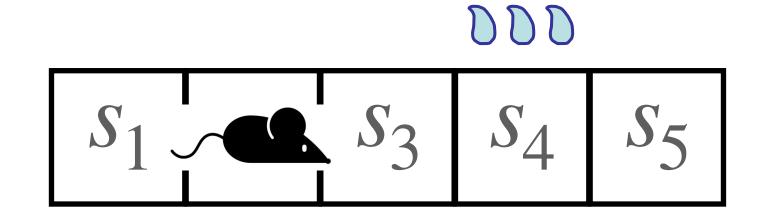


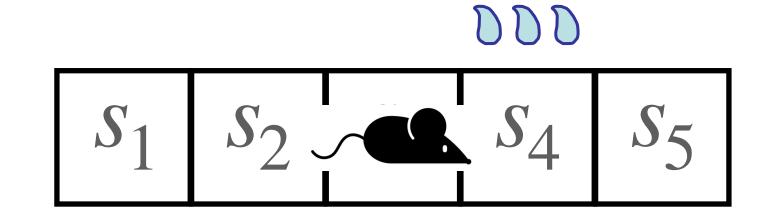
To define a Markov Process, we need to define a state space and transition probabilities

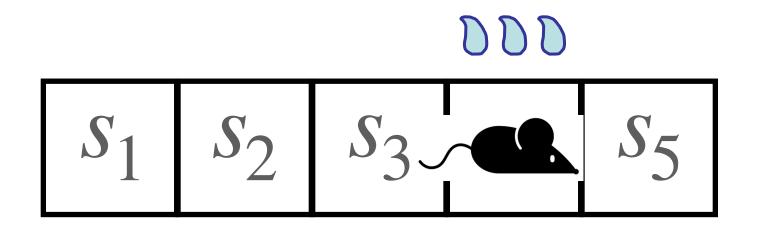


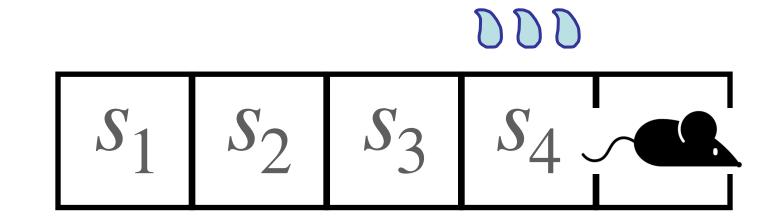
We can now define a state space S:

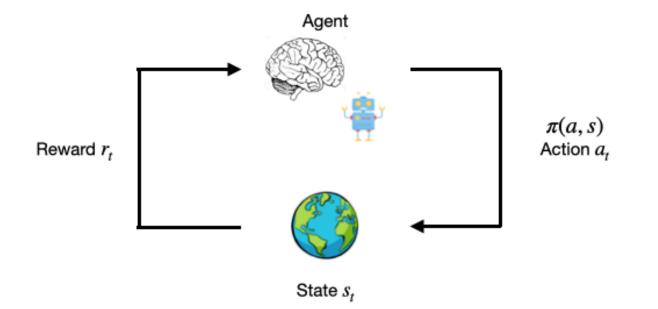




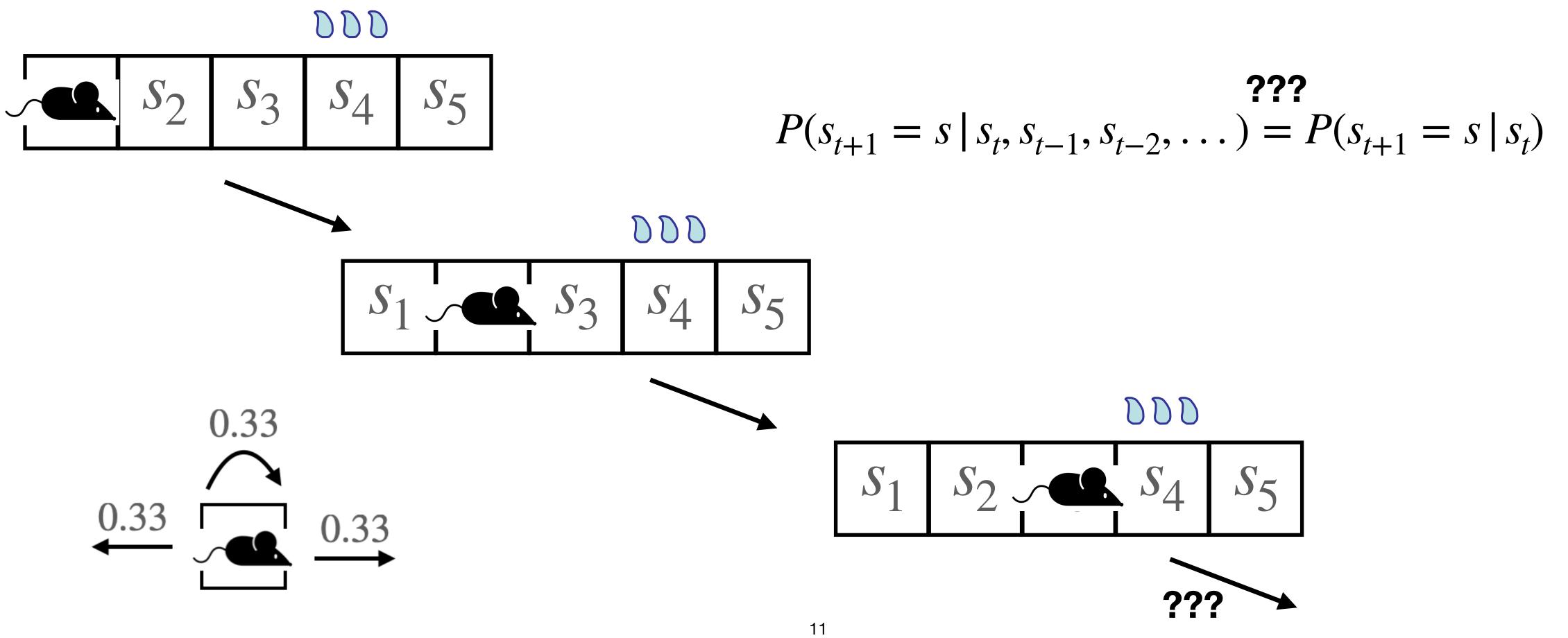


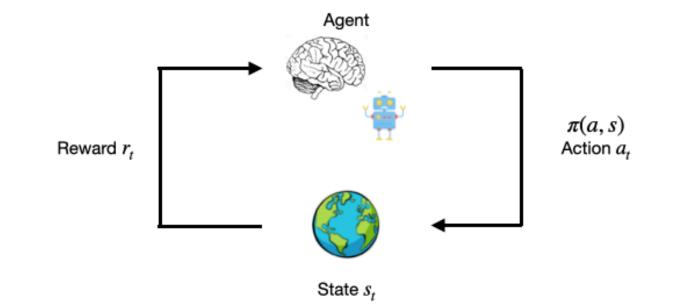




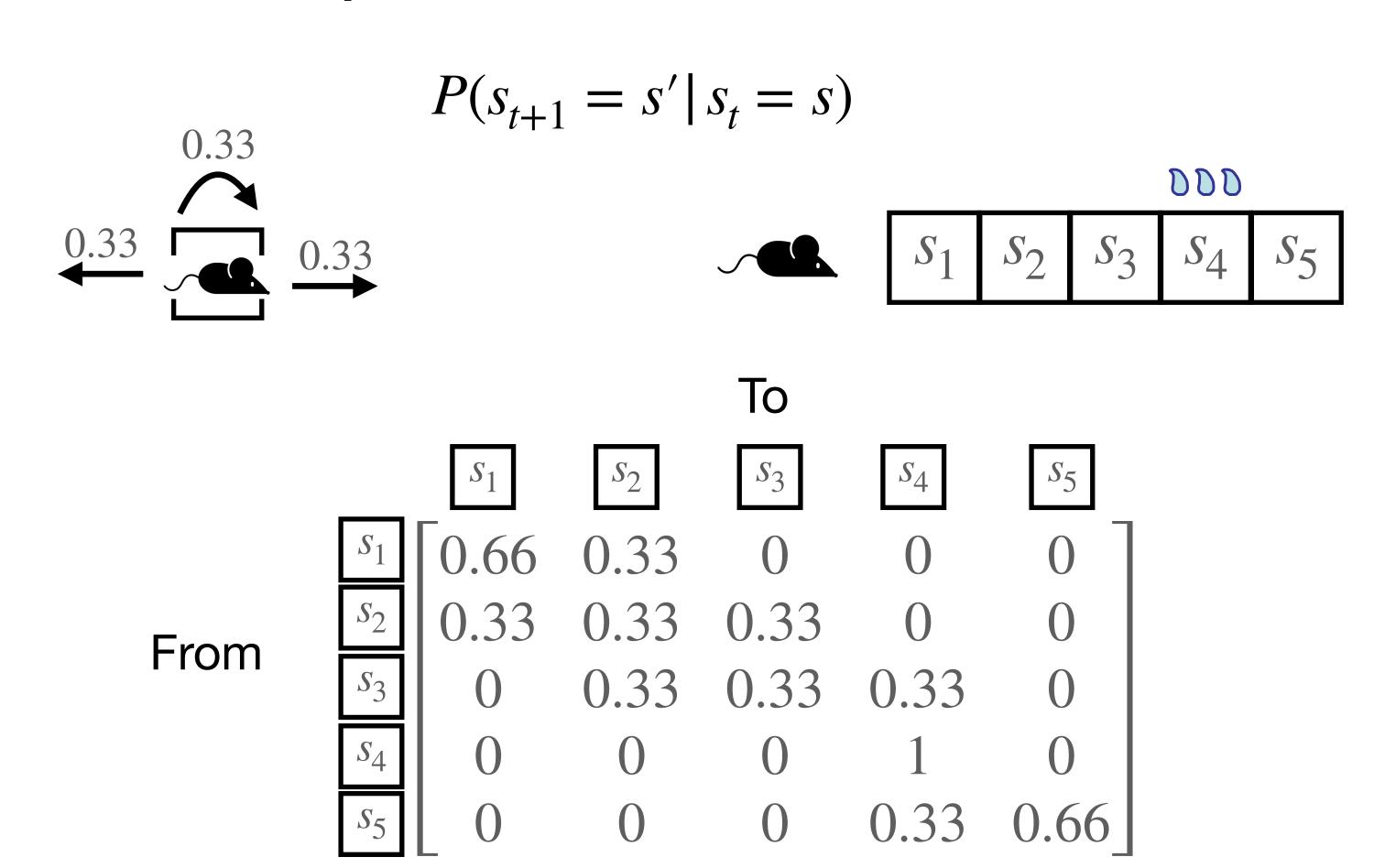


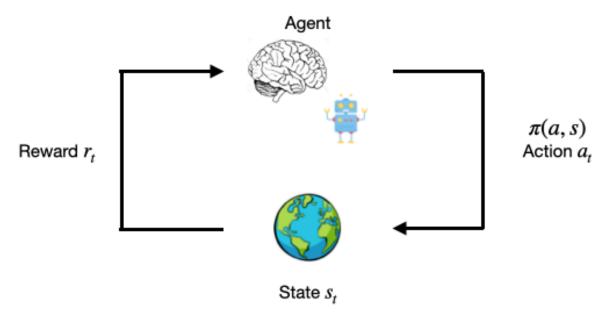
Does this problem have the Markov Property?





This allows us to define transition probabilities P:



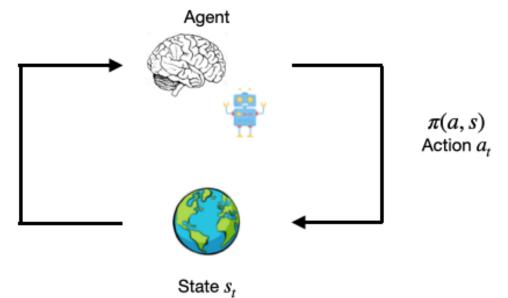


A Markov Process is defined based on

- A State Space S
- Transition Probabilities P $P(s_{t+1} = s' | s_t = s)$

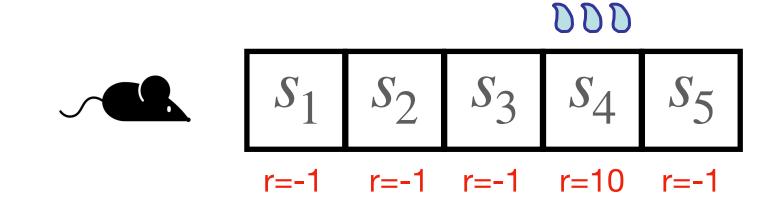
To define a Markov Reward Process, we need to add rewards

Markov Reward Process



A Markov Reward Process is defined based on

- A State Space S
- Transition Probabilities P
- A Reward Function $R_s = \mathbb{E}[r_t | s_t = s]$
- A Discount Factor $\gamma \in [0,1]$

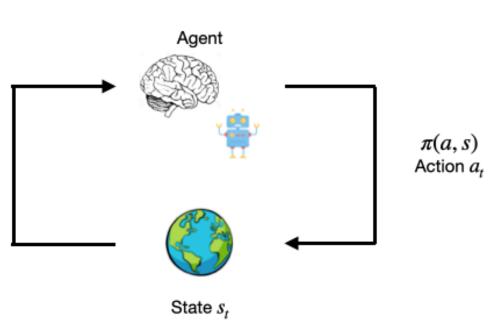


Allows to define Return

$$G_t = r_{t+1} + \gamma \cdot r_{t+2} + \gamma^2 \cdot r_{t+3} + \ldots = \sum_{k=0}^{\infty} \gamma^k \cdot r_{t+k+1}$$

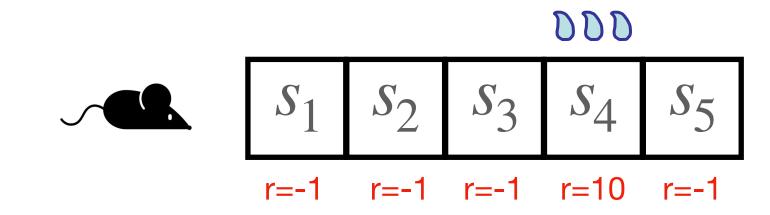
To define a Markov Decision Process, we need to add actions

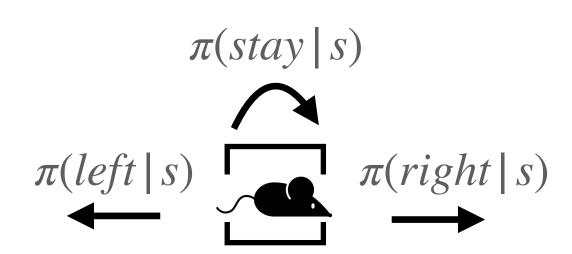
Markov Decision Process Reward r.



A Markov Decision Process is defined based on

- A State Space S
- An Action Space A
- Transition Probabilities P
- A Reward Function $R_s = \mathbb{E}[r_t | s_t = s]$
- A Discount Factor $\gamma \in [0,1]$





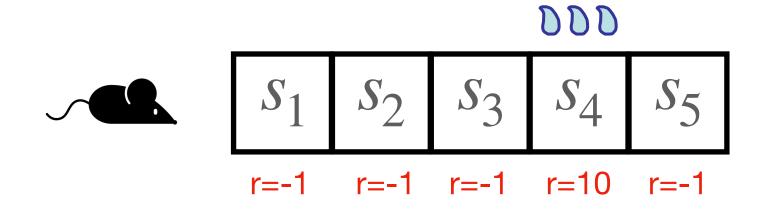
Actions are governed via a **policy**: $\pi(a, s) = P(a_t = a | s_t = s)$

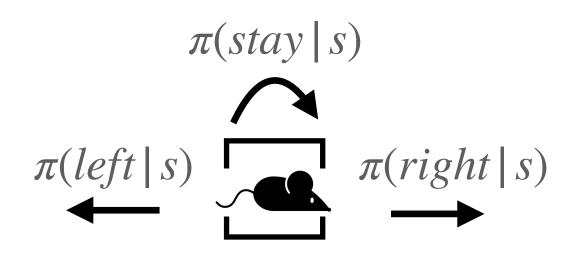
$$\pi(a, s) = P(a_t = a \mid s_t = s)$$

MDPs basis for model-based RL

Allows to specify all environment dynamics for RL problem:

$$P(s', r | s, a) = P(s_{t+1} = s', r_{t+1} = r | s_t = s, a_t = a)$$



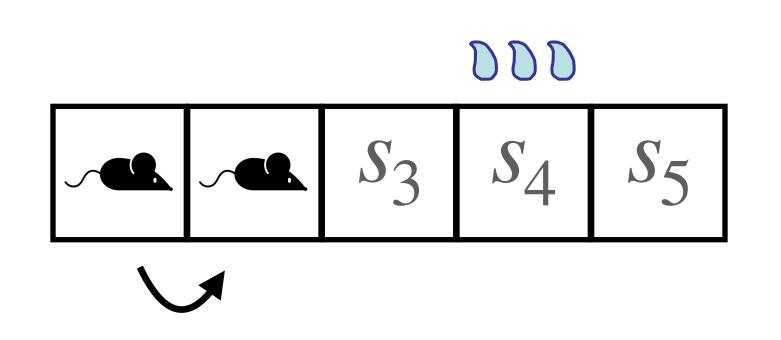


MDPs basis for model-based RL

$$P(s', r | s, a) = P(s_{t+1} = s', r_{t+1} = r | s_t = s, a_t = a)$$

Allows to specify useful things like state-transition probabilities (often T):

$$P(s'|s,a) = P(s_{t+1} = s'|s_t = s, a_t = a) = \sum_{r} P(s',r|s,a)$$



$$P(s'|s, right) = \begin{bmatrix} s_1 & s_2 & s_3 & s_4 & s_5 \\ \hline s_2 & 0 & 1 & 0 & 0 \\ \hline s_3 & 0 & 0 & 1 & 0 \\ \hline s_4 & 0 & 0 & 0 & 1 \\ \hline s_5 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

MDPs basis for model-based RL

$$P(s', r | s, a) = P(s_{t+1} = s', r_{t+1} = r | s_t = s, a_t = a)$$

How can we make use of such models of the world?

Planning and action selection (maybe later..)

Learning

- Key idea: store experiences in world model P(s', r | s, a)
- Sample from this model to generate extra learning data
- This is called **DYNA-Q...**

Coding: DYNA-Q

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