

# COMBINATIONAL LOGIC

`combinational-logic:~#` digital systems where the outputs are determined solely by the current states of the inputs to the circuit.



`binary-states-convention:~#` Throughout the exploration, black-filled LEDs correspond to a HIGH digital state while white-filled LEDs correspond to a LOW digital state

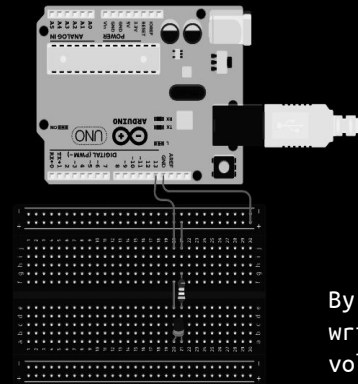
**blink-exercise:~#** To start the microcontroller learning, we are tasked to construct our first “Hello World” code. That is, we can start by doing the following tasks:

\$ construct a blinking LED sketch,

\$ adjust the frequency of the blink

\$ find out the critical frequency where rapid blinking approaches a steady state

\$ construct two alternately blinking LED system



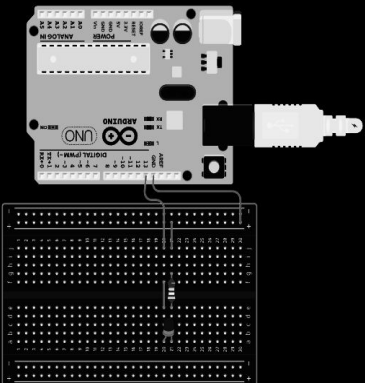
#### Basic blink

```
int led = 13;
void setup() {
  pinMode(led, OUTPUT);
}
void loop() {
  digitalWrite(led, HIGH);
  delay(1000);
  digitalWrite(led, LOW);
  delay(1000);
}
```

GitHub repo:

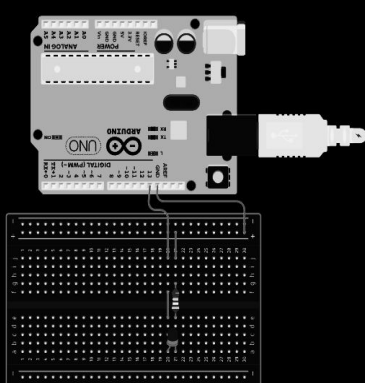
Raw data: <https://bit.ly/3ST7GTQ>  
 Data processing: <https://bit.ly/3TaGLCP>  
 Plots: <https://bit.ly/3q2bVyc>  
 Code repository: <https://bit.ly/3vsqFDq>

By constructing a simple LED-resistor circuit and writing a code with a delay from HIGH to LOW voltage, we have constructed our first blinking LED system.



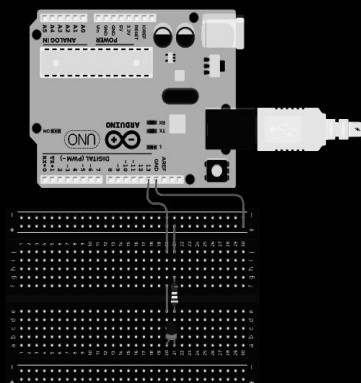
#### Slower blink

```
...
delay(2000);
...
```



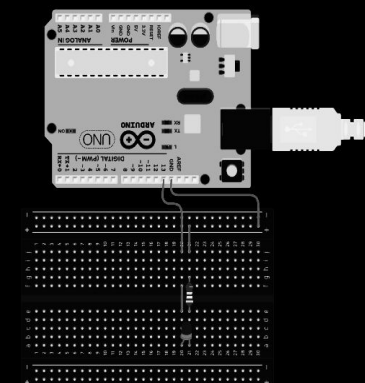
#### Slower blink (2)

```
...
delay(3000);
...
```



#### Faster blink

```
...
delay(500);
...
```

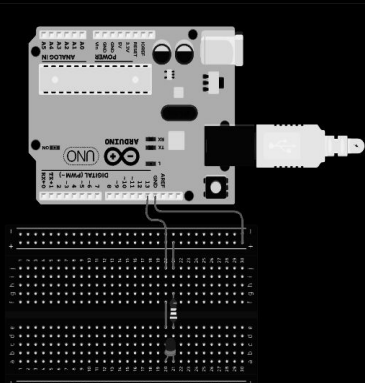


#### Faster blink (2)

```
...
delay(250);
...
```

One can make the blinking go faster or go slower by adjusting the delay() from HIGH to LOW voltage.

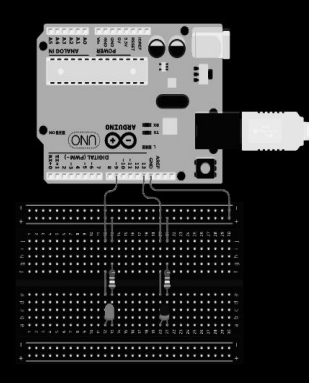
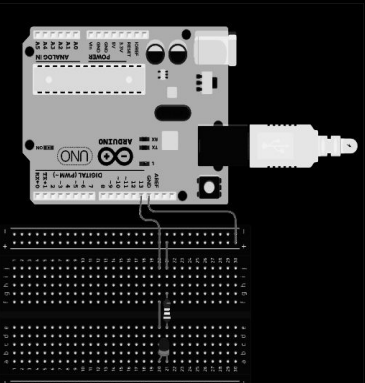
With these, an alternating blinking circuit can be constructed by simultaneously turning an LED to HIGH and another to LOW



#### Steady blink

```
...
delay(20); // left
delay(10); // right
...
```

Observe that at delay(20), we can still see the flicker; such flicker converges to a steady state at delay(10)



#### Alternating Blink

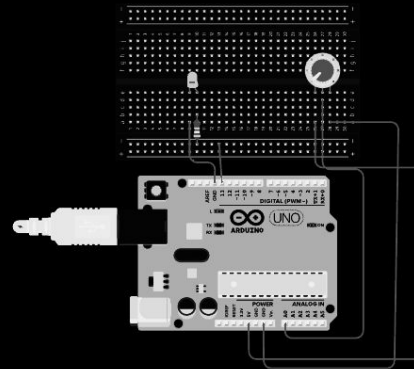
```
int led1 = 13;
int led2 = 9;
void setup() {
  pinMode(led1, OUTPUT);
  pinMode(led2, OUTPUT);
}
void loop() {
  digitalWrite(led1, HIGH);
  delay(10);
  digitalWrite(led1, LOW);
  digitalWrite(led2, HIGH);
  delay(10);
  digitalWrite(led2, LOW);
}
```

**blinking-through-analog-input:~#** Potentiometers can be used to act like an adjustable voltage dividers. Here, we can explore one of its application to control sensor values by doing the following tasks:

\$ adjust LED blinking rate via a potentiometer,

\$ display sensor value from the analog input,

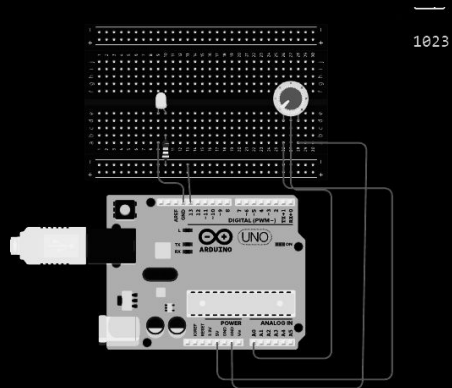
\$ display actual voltages value



#### Blinking Rate via Potentiometer

```
...
sensorValue = analogRead(sensorPin);
digitalWrite(ledPin, HIGH);
delay(sensorValue);
digitalWrite(ledPin, LOW);
delay(sensorValue);
...
```

Blinking rate can be adjusted manually by incorporating a potentiometer to adjust the analog voltage read from AnalogRead() function. By setting the value to correspond with the delay between HIGH and LOW LED states, blinking rate can be directly controlled by rotating the potentiometer

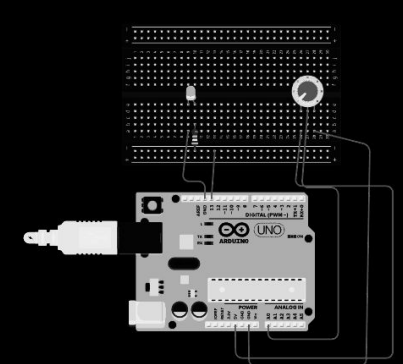


#### Blinking Rate via potentiometer

```
...
void setup()
{
  Serial.begin(9600);
  ...
}

void loop()
{
  sensorValue = analogRead(sensorPin);
  voltage = sensorValue;
  Serial.println(voltage);
  ...
}
```

The serial monitor allows us to visualize the range of analog values being controlled by the potentiometer.



#### True voltage from analogRead()

```
...
sensorValue = analogRead(sensorPin);
voltage = sensorValue * 5.0/1023;
Serial.println(voltage);
...
```

Note that the operating voltage of Arduino UNO is 5V. We can scale the displayed sensor values to portray the actual voltages from analogRead().

Observe that the values displayed at the serial monitor ranges from 1023 to 0. Programming these values to correspond to the delay() between both digitalWrite() functions, the delays adjusted by this circuit ranges from 1023 milliseconds to 0 millisecond (no delay, static LED)

This scaling gives us an idea that the analogRead() function maps out the voltage range 0V to 5V into corresponding integer values 0 to 1023. As we have seen, one of such applications is to control delay times between switching digital states.

blinking-through-analog-input:~# code it up!

```
    scrollHeight = scrollHeight + 1000;
    window.scrollTo(0, scrollHeight);

function() {
  function s_setFocus() {
    var form = null;
    if (document.getElementById
```

codes-used

#### Blinking Rate via potentiometer

```
int sensorPin = A0;
int ledPin = 13;
int sensorValue = 0;

void setup()
{
  pinMode(ledPin, OUTPUT);
}

void loop()
{
  sensorValue = analogRead(sensorPin); //read the value from the sensor
  digitalWrite(ledPin, HIGH);
  delay(sensorValue);
  digitalWrite(ledPin, LOW);
  delay(sensorValue);
}
```

#### Serial monitor

```
int sensorPin = A0;
int ledPin = 13;
int sensorValue = 0;
int voltage = 0;

void setup()
{
  Serial.begin(9600);
  pinMode(ledPin, OUTPUT);
}

void loop()
{
  sensorValue = analogRead(sensorPin); // read the value from the sensor
  voltage = sensorValue * 5.0/1023; // scaling to display true voltage value
  Serial.println(voltage);
  digitalWrite(ledPin, HIGH);
  delay(sensorValue);
  digitalWrite(ledPin, LOW);
  delay(sensorValue);
}
```

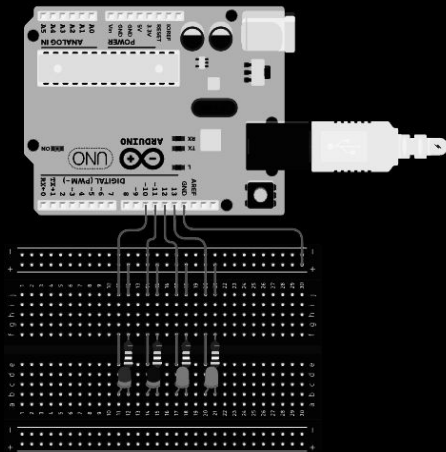
**scrolling-led:~#** By programming conditional statements on Arduino microcontroller one can create visual effects such as the illusion of a scrolling LED; these can be sometimes be seen on premium keyboards with RGB features. To get our hands dirty with conditional statements, we aim to do the following tasks:

\$ construct a scrolling LED circuit,

\$ demonstrate the utility of the reset button,

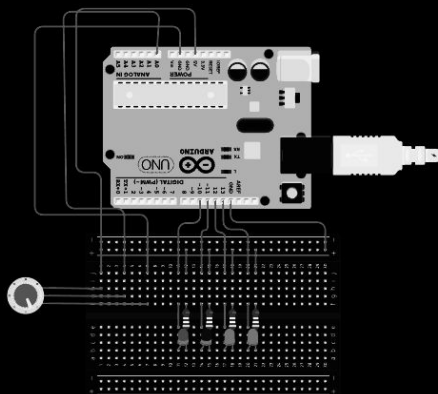
\$ increase the rate of scrolling

\$ control the rate of scrolling via a potentiometer



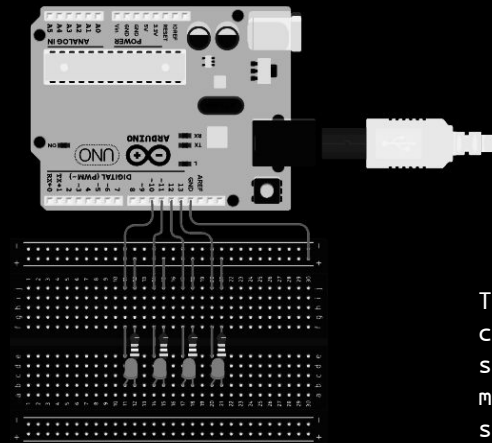
Incrementally increasing scrolling rate

```
-----  
...  
digitalWrite(led1, HIGH);  
delay(init_del - inc);  
digitalWrite(led1, LOW);  
digitalWrite(led2, HIGH);  
...  
inc = inc + inc_change;  
...  
-----
```



Potentiometer-adjusted scrolling rate

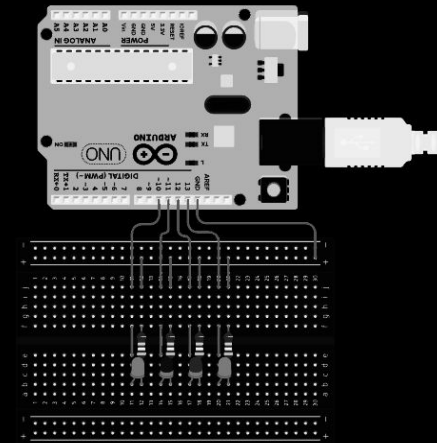
```
-----  
...  
digitalWrite(led1, HIGH);  
delay(1050-sensorValue);  
digitalWrite(led1, LOW);  
digitalWrite(led2, HIGH);  
...  
-----
```



Scrolling LED

```
-----  
...  
digitalWrite(led1, HIGH);  
delay(500);  
digitalWrite(led1, LOW);  
digitalWrite(led2, HIGH);  
delay(500);  
digitalWrite(led2, LOW);  
digitalWrite(led3, HIGH);  
...  
-----
```

The alternating blink circuit can be modified such that blinking is modified into a scrolling behavior.



One can write up a code where, at each looping instance, the delay is being increased (or decreased) by a constant value. This gives the scrolling-LED circuit to have an increasing rate after each full scrolling cycle.

The rate of scrolling can be further modified such that the constant change after each scrolling cycle is replaced by a variable rate dictated by the a potentiometer. This way, one can control the rate of LED scrolling as necessary.

scrolling-led:~# code it up!

## Incrementally increasing scrolling rate

```

int led1 = 13;
int led2 = 12;
int led3 = 11;
int led4 = 10;
int inc = 0;
int inc_change = 100;
int init_del = 500;

void setup() {
  pinMode(led1, OUTPUT);
  pinMode(led2, OUTPUT);
  pinMode(led3, OUTPUT);
  pinMode(led4, OUTPUT);
}

void loop() {
  // left to right
  digitalWrite(led1, HIGH);
  delay(init_del - inc);
  digitalWrite(led1, LOW);
  digitalWrite(led2, HIGH);
  delay(init_del - inc);
  digitalWrite(led2, LOW);
  digitalWrite(led3, HIGH);
  delay(init_del - inc);
  digitalWrite(led3, LOW);
  digitalWrite(led4, HIGH);
  delay(init_del - inc);
  digitalWrite(led4, LOW);
  // right to left
  digitalWrite(led3, HIGH);
  delay(init_del - inc);
  digitalWrite(led3, LOW);
  digitalWrite(led2, HIGH);
  delay(init_del - inc);
  digitalWrite(led2, LOW);
  digitalWrite(led1, HIGH);
  inc = inc + inc_change;
}

```

## Potentiometer-adjusted scrolling rate

```

int sensorPin = A0;
int led1 = 13;
int led2 = 12;
int led3 = 11;
int led4 = 10;
int sensorValue = 0;

void setup() {
  Serial.begin(9600);
  pinMode(led1, OUTPUT);
  pinMode(led2, OUTPUT);
  pinMode(led3, OUTPUT);
  pinMode(led4, OUTPUT);
}

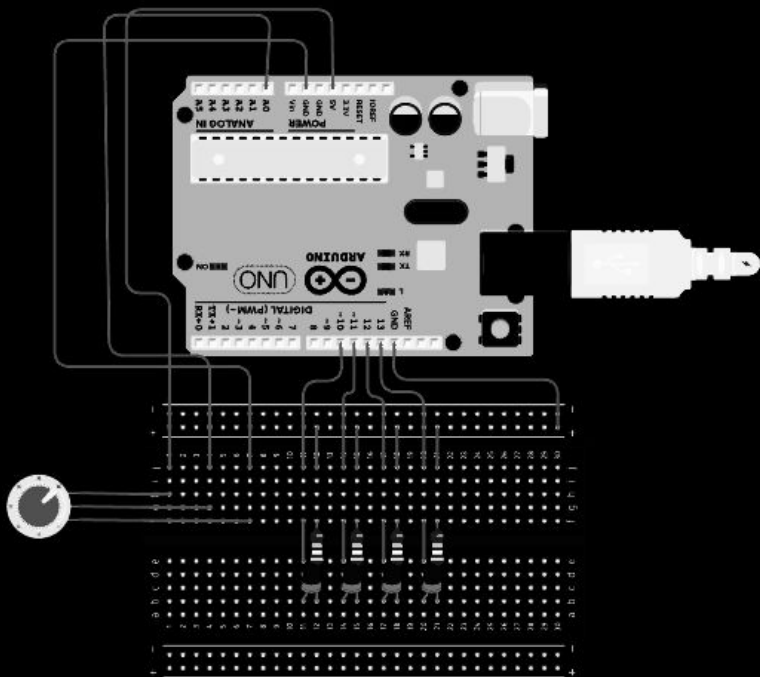
void loop() {
  sensorValue = analogRead(sensorPin);
  Serial.println(sensorValue);
  // left to right
  digitalWrite(led1, HIGH);
  delay(1050-sensorValue);
  digitalWrite(led1, LOW);
  digitalWrite(led2, HIGH);
  delay(1050-sensorValue);
  digitalWrite(led2, LOW);
  digitalWrite(led3, HIGH);
  delay(1050-sensorValue);
  digitalWrite(led3, LOW);
  digitalWrite(led4, HIGH);
  delay(1050-sensorValue);
  digitalWrite(led4, LOW);
  // right to left
  digitalWrite(led3, HIGH);
  delay(1050-sensorValue);
  digitalWrite(led3, LOW);
  digitalWrite(led2, HIGH);
  delay(1050-sensorValue);
  digitalWrite(led2, LOW);
  digitalWrite(led1, HIGH);
}

```

codes-used

**pot-multiple-leds:~#** As a natural extension, it would be interesting to write some conditional statements that depend on some adjustable input parameters (such as values given by a potentiometer). Here, we aim to do the following:

\$ construct an LED-based progress bar graph following the levels of the potentiometer as input



#### LED Progress Bar

```
-----  
...  
if (sensorValue < 256)  
{...}  
if (sensorValue > 256)  
{...}  
if (sensorValue < 512)  
{...}  
if (sensorValue < 768)  
{...}  
if (sensorValue < 1020)  
{...}  
...  
-----
```

Conditional statements can be written to the code referring to different circuit states. Here, five such states were programmed depending on the input values of adjusted by the potentiometer. Dividing the analog range of 0 to 1023 into five different states, we have the ranges 0 to 256, 257 to 512, 513 to 768, and 769 to 1020.

The respective five different states correspond the progress bar level of the LED array. Respectively, the states are: (i) 0 LED activated, (ii) 1 LED activated ,..., (v) ALL LEDs activated.



pot-multiple-leds:~#

```

        scrollHeight + 0.1 *
        window.scroll(0, scrollHeight)

function() {
  function s_setFocus() {
    var form = null;
    if (document.getElement

```

codes-used

## LED Progress Bar

```

int sensorPin = A0;
int led1 = 13;
int led2 = 12;
int led3 = 11;
int led4 = 10;
int inc = 0;
int inc_change = 100;
int init_del = 500;
int sensorValue = 0;

void setup() {
  Serial.begin(9600);
  pinMode(led1, OUTPUT);
  pinMode(led2, OUTPUT);
  pinMode(led3, OUTPUT);
  pinMode(led4, OUTPUT);
}

void loop() {
  sensorValue = analogRead(sensorPin);
  Serial.println(sensorValue);

  if (sensorValue < 256) {
    digitalWrite(led1, LOW);
    digitalWrite(led2, LOW);
    digitalWrite(led3, LOW);
    digitalWrite(led4, LOW);
  }

  if (sensorValue > 256) {
    digitalWrite(led1, LOW);
    digitalWrite(led2, LOW);
    digitalWrite(led3, LOW);
    digitalWrite(led4, LOW);
    digitalWrite(led1, HIGH);
  }

  if (sensorValue > 512) {
    digitalWrite(led1, LOW);
    digitalWrite(led2, LOW);
    digitalWrite(led3, LOW);
    digitalWrite(led4, LOW);
    digitalWrite(led1, HIGH);
    digitalWrite(led2, HIGH);
  }

  if (sensorValue > 768) {
    digitalWrite(led1, LOW);
    digitalWrite(led2, LOW);
    digitalWrite(led3, LOW);
    digitalWrite(led4, LOW);
    digitalWrite(led1, HIGH);
    digitalWrite(led2, HIGH);
    digitalWrite(led3, HIGH);
  }

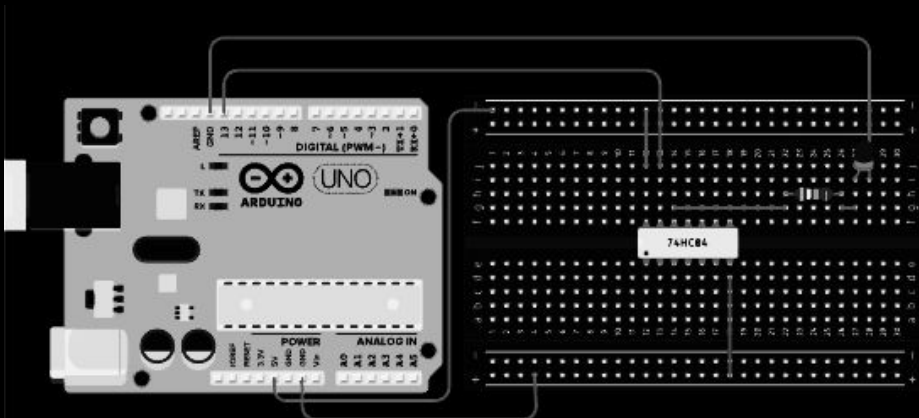
  if (sensorValue > 1020) {
    digitalWrite(led1, LOW);
    digitalWrite(led2, LOW);
    digitalWrite(led3, LOW);
    digitalWrite(led4, LOW);
    digitalWrite(led1, HIGH);
    digitalWrite(led2, HIGH);
    digitalWrite(led3, HIGH);
    digitalWrite(led4, HIGH);
  }
}

```



**logic-gate-1:~#** Now, we enter the area of logic gates - the main element to design a circuit based on some carefully-designed logic conditions. One such gate is the NOT gate. Given a binary state (1) or (0), the output must be the inverse of the input (0) or (1), respectively. To see this, aim to do the following:

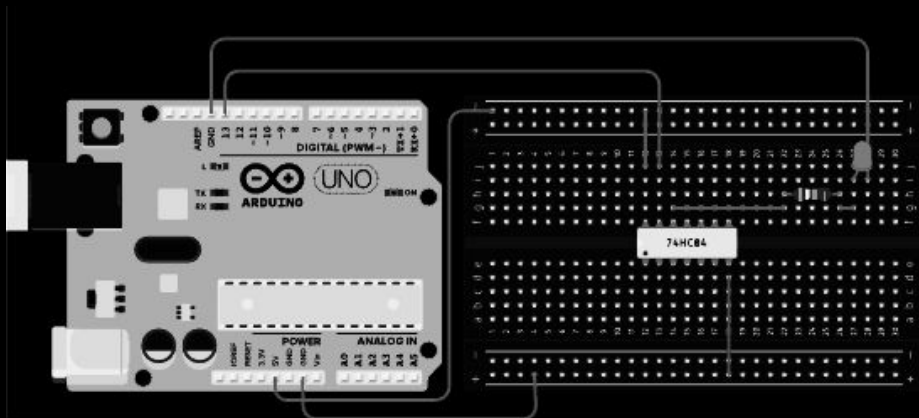
**\$** verify and demonstrate the validity of the NOT gate truth values



#### NOT gate LED states test I

```
...  
digitalWrite(ledPin, LOW);  
delay(2000);  
digitalWrite(ledPin, HIGH);  
delay(300);  
...
```

To test the validity of the truth values of the constructed NOT gates, we employ to equivalent tests. In the first test, we set the input to LOW for 2000 milliseconds and to HIGH for 300 milliseconds. The resulting LED must have an inverted output: 2000 milliseconds HIGH state and 300 milliseconds LOW state.



#### NOT gate LED states test II

```
...  
digitalWrite(ledPin, HIGH);  
delay(2000);  
digitalWrite(ledPin, LOW);  
delay(300);  
...
```

Another test shows that inverting the input also inverts the output. In both cases, truth values that of a NOT gate.

Geraldez-LK-2019-11336 184-WFU-FX-2 ~ (combinational-logic)

logic-gate-1:~# code it up!

```
        scrollHeight + 0.1);
        window.scrollTo(0, scrollHeight);

function() {
function s.setFocus() {
var form = null;
if (document.getElementById
```

codes-used

NOT gate LED states test

```
-----
int ledPin = 13;
int sensorValue = 0;

void setup(){
  pinMode(ledPin, OUTPUT);
}
void loop(){
  digitalWrite(ledPin, LOW);
  delay(2000);
  digitalWrite(ledPin, HIGH);
  delay(300);
}
-----
```

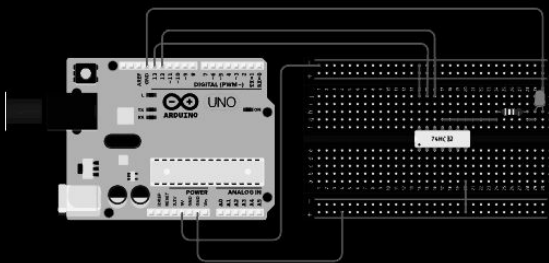
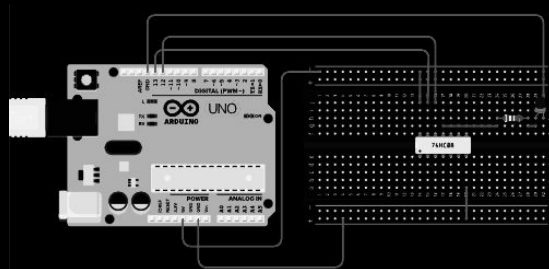
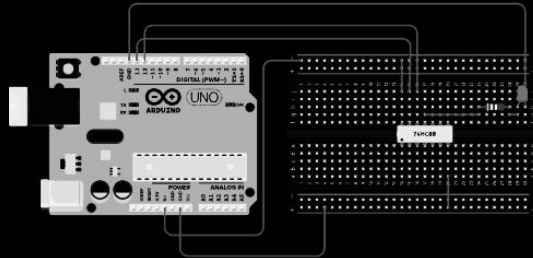
**logic-gate-2:~#** Several ICs contain different logic gates. We have already discussed the NOT gate using 7404). Here, we explore other kinds of logic gates using 7400, 7408, and 7432 by doing the following tasks:

\$ design, verify, and demonstrate the validity of the AND gate truth values

\$ design, verify, and demonstrate the validity of the NAND gate truth values

\$ design, verify, and demonstrate the validity of the OR gate truth values

The testing codes were programmed such that it cycles through all binary states in the following order (11) > (00) > (01) > (10). It was set up such that the first state (11) runs for 2000 milliseconds and while all other states run for 667 milliseconds



AND, NAND, and OR LED states test

```
...  
digitalWrite(ledPin1, HIGH);  
digitalWrite(ledPin2, HIGH);  
delay(2000);  
digitalWrite(ledPin1, LOW);  
digitalWrite(ledPin2, LOW);  
delay(667);  
digitalWrite(ledPin1, LOW);  
digitalWrite(ledPin2, HIGH);  
delay(667);  
digitalWrite(ledPin1, HIGH);  
digitalWrite(ledPin2, LOW);  
delay(667);  
...
```

The first circuit (7400) shows an initial 2 millisecond HIGH state followed by another 2 millisecond LOW state. This corresponds to an AND gate.

The second circuit (7408) corresponds to a 2 millisecond LOW state followed by another 2 millisecond HIGH state. This is simply an inverted AND gate, or a NAND gate.

The third circuit shows (7432) is active 3/4 of the times during the entire testing cycle. Upon careful observation, it goes into a LOW state at the second state. Hence, this is an OR gate.

logic-gate-2:~# code it up!

```
        document.getElementById("form").style.height = 100px;
        window.scrollTo(0, scrollHeight)

function() {
function s_setFocus() {
var form = null;
if (document.getElementById
```

codes-used

### AND, NAND, and OR LED states test

```
-----
int ledPin1 = 13;
int ledPin2 = 12;
int sensorValue = 0;

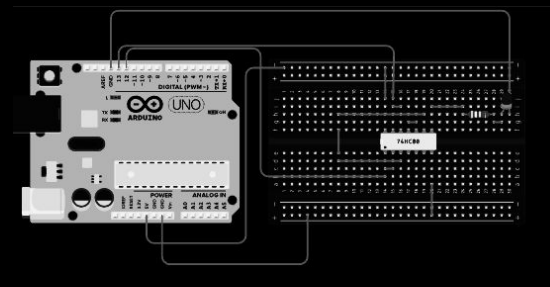
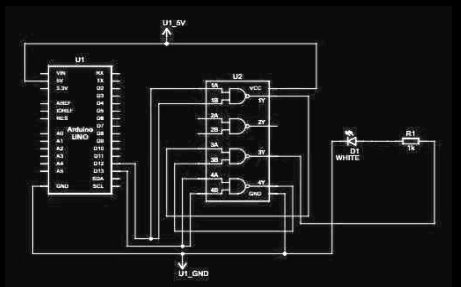
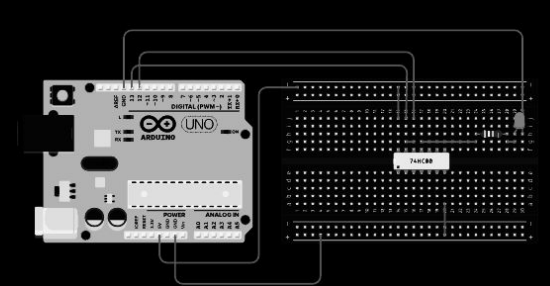
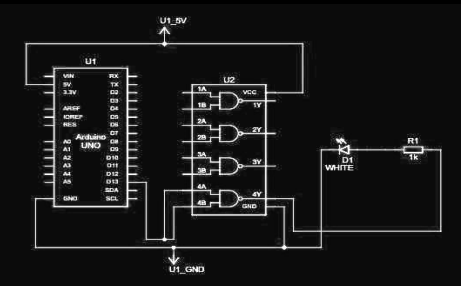
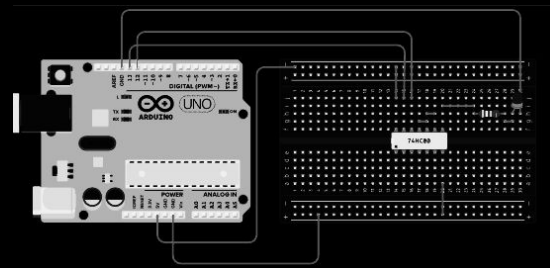
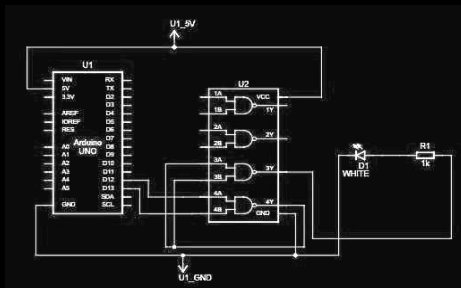
void setup(){
  pinMode(ledPin1, OUTPUT);
  pinMode(ledPin2, OUTPUT);
}
void loop(){
  digitalWrite(ledPin1, HIGH);
  digitalWrite(ledPin2, HIGH);
  delay(2000);
  digitalWrite(ledPin1, LOW);
  digitalWrite(ledPin2, LOW);
  delay(667);
  digitalWrite(ledPin1, LOW);
  digitalWrite(ledPin2, HIGH);
  delay(667);
  digitalWrite(ledPin1, HIGH);
  digitalWrite(ledPin2, LOW);
  delay(667);
}
-----
```

**logic-gate-3:~#** Some logic gates are considered to be universal. That is, one can design an appropriate circuit to repurpose an universal gate into any kind of logic gate (OR, AND, NOT, etc). A NAND gate is one example of a universal logic gate. To see this, we aim to do the following:

\$ construct a circuit to repurpose NAND universal gate as an OR gate

\$ construct a circuit to repurpose NAND universal gate as an AND gate

\$ construct a circuit to repurpose NAND universal gate as a NOT gate



To test the validity of the constructed NAND-based logic gates, we employ different tests by cycling through all states. The tests were designed with different delay times such that the respective states can be uniquely identified depending on how long it was activated.

#### NAND as AND test

```
...
digitalWrite(ledPin1, HIGH);
digitalWrite(ledPin2, HIGH);
delay(2000);
digitalWrite(ledPin1, LOW);
digitalWrite(ledPin2, LOW);
delay(667);
digitalWrite(ledPin1, LOW);
digitalWrite(ledPin2, HIGH);
delay(667);
digitalWrite(ledPin1, HIGH);
digitalWrite(ledPin2, LOW);
delay(667);
...
```

Circuit shows that, half of the time, LED enters a HIGH state. From the written code, 2000 millisecond is spend on a (11) state input. This is characteristic of an AND gate logic.

#### NAND as NOT test

```
...
digitalWrite(ledPin, LOW);
delay(2000);
digitalWrite(ledPin, HIGH);
delay(300);
...
```

Spending 2000 milliseconds on LOW input state and 300 milliseconds on HIGH input state gives us an inverted output state. This is characteristic of a NOT gate logic.

#### NAND as OR test

```
...
digitalWrite(ledPin1, HIGH);
digitalWrite(ledPin2, HIGH);
delay(2000);
digitalWrite(ledPin1, LOW);
digitalWrite(ledPin2, LOW);
delay(667);
digitalWrite(ledPin1, LOW);
digitalWrite(ledPin2, HIGH);
delay(667);
digitalWrite(ledPin1, HIGH);
digitalWrite(ledPin2, LOW);
delay(667);
...
```

Circuit enters only the LOW state for 667 milliseconds or 1/4 of the cycle entering. Looking at the test code, this corresponds to a (00) state input - characteristic of an OR gate logic.

logic-gate-3::~# code it up!

```

        height: scrollheight + 0.5em
        window.scroll(0, scrollheight)

function() {
  function s.setFocus() {
    var form = null;
    if (document.getElementById

```

codes-used

#### NAND as NOT test

```

-----
int ledPin = 13;
int sensorValue = 0;

void setup(){
  pinMode(ledPin, OUTPUT);
}

void loop(){
  digitalWrite(ledPin, LOW);
  delay(2000);
  digitalWrite(ledPin, HIGH);
  delay(300);
}
-----

```

#### NAND as AND test

```

-----
int ledPin1 = 13;
int ledPin2 = 12;
int sensorValue = 0;

void setup(){
  pinMode(ledPin1, OUTPUT);
  pinMode(ledPin2, OUTPUT);
}

void loop(){
  digitalWrite(ledPin1, HIGH);
  digitalWrite(ledPin2, HIGH);
  delay(2000);
  digitalWrite(ledPin1, LOW);
  digitalWrite(ledPin2, LOW);
  delay(667);
  digitalWrite(ledPin1, LOW);
  digitalWrite(ledPin2, HIGH);
  delay(667);
  digitalWrite(ledPin1, HIGH);
  digitalWrite(ledPin2, LOW);
  delay(667);
}
-----

```

#### NAND as OR test

```

-----
int ledPin1 = 13;
int ledPin2 = 12;
int sensorValue = 0;

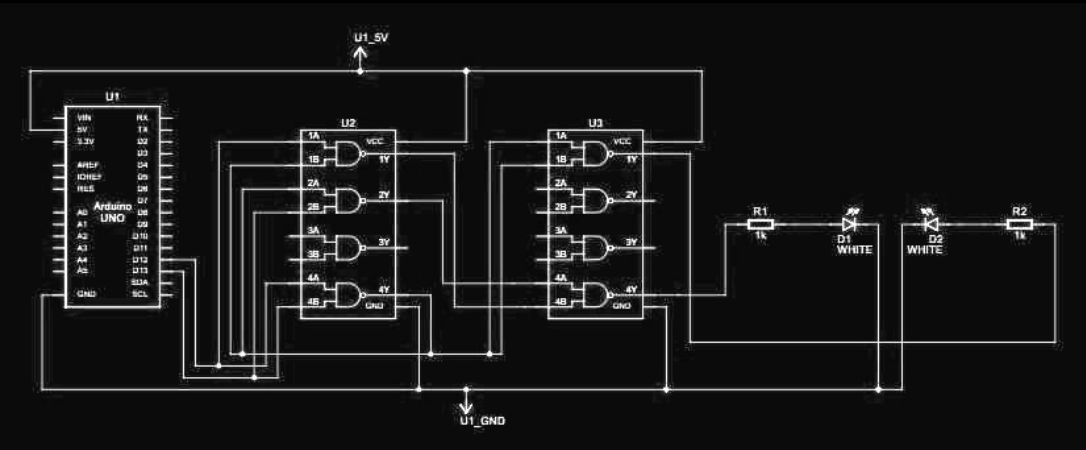
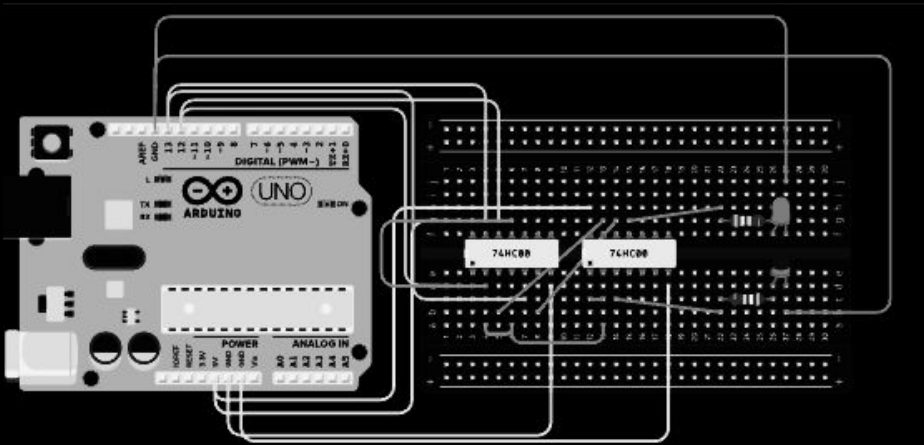
void setup(){
  pinMode(ledPin1, OUTPUT);
  pinMode(ledPin2, OUTPUT);
}

void loop(){
  digitalWrite(ledPin1, HIGH);
  digitalWrite(ledPin2, HIGH);
  delay(2000);
  digitalWrite(ledPin1, LOW);
  digitalWrite(ledPin2, LOW);
  delay(667);
  digitalWrite(ledPin1, LOW);
  digitalWrite(ledPin2, HIGH);
  delay(667);
  digitalWrite(ledPin1, HIGH);
  digitalWrite(ledPin2, LOW);
  delay(667);
}
-----

```

half-adder:~# We an appropriate circuit design, one can perform various arithmetic operations as desired. One of the simplets operations is to add two 1-bit numerical binary values. These can be easily carried out by a half-adder circuit. To see this, we aim to do the following:

\$ design a half-adder circuit using NAND gate and confirm its truth statements validity.



The half-adder circuit is constructed based on the following binary arithmetic logic displayed the following truth table.

Input 1	Input 2	Sum	Carry
1	1	0	1
1	0	1	0
0	0	0	0
0	1	1	0

```
Half-adder circuit using NAND gate
...
digitalWrite(ledPin1, HIGH);
digitalWrite(ledPin2, HIGH);
delay(2000);
digitalWrite(ledPin1, HIGH);
digitalWrite(ledPin2, LOW);
delay(2000);
digitalWrite(ledPin1, LOW);
digitalWrite(ledPin2, LOW);
delay(2000);
digitalWrite(ledPin1, LOW);
digitalWrite(ledPin2, HIGH);
delay(2000);
...

```

Observe the results of the written testing code, the input cycles through (11) > (10) > (00) > (01). This results to the following (Sum, Carry) states, respectively, as (01), (10), (00), (10), which is consistent with a half-adder truth table.



half-adder:~# code it up!

```
        scrollTop = scrollHeight - 1000;
        window.scrollTo(0, scrollTop);

function() {
function s_setFocus() {
var form = null;
if (document.getElementById
```

codes-used

### Half-adder circuit using NAND gate

```
int ledPin1 = 13;
int ledPin2 = 12;
int sensorValue = 0;

void setup(){
pinMode(ledPin1, OUTPUT);
pinMode(ledPin2, OUTPUT);
}
void loop(){
digitalWrite(ledPin1, HIGH);
digitalWrite(ledPin2, HIGH);
delay(2000);
digitalWrite(ledPin1, HIGH);
digitalWrite(ledPin2, LOW);
delay(2000);
digitalWrite(ledPin1, LOW);
digitalWrite(ledPin2, LOW);
delay(2000);
digitalWrite(ledPin1, LOW);
digitalWrite(ledPin2, HIGH);
delay(2000);
}
```