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The ristretto255 and decaf448 Groups

Abstract

This memo specifies two prime-order groups, ristretto255 and decaf448, suitable for safely implementing higher-level and complex cryptographic protocols. The ristretto255 group can be implemented using Curve25519, allowing existing Curve25519 implementations to be reused and extended to provide a prime-order group. Likewise, the decaf448 group can be implemented using edwards448.

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1. Introduction

Decaf [Decaf] is a technique for constructing prime-order groups with nonmalleable encodings from non-prime-order elliptic curves. Ristretto extends this technique to support cofactor-8 curves such as Curve25519 [RFC7748]. In particular, this allows an existing Curve25519 library to provide a prime-order group with only a thin abstraction layer.

Many group-based cryptographic protocols require the number of elements in the group (the group order) to be prime. Prime-order groups are useful because every non-identity element of the group is

a generator of the entire group. This means the group has a cofactor of 1, and all elements are equivalent from the perspective of hardness of the discrete logarithm problem.

Edwards curves provide a number of implementation benefits for cryptography. These benefits include formulas for curve operations that are among the fastest currently known, and for which the addition formulas are complete with no exceptional points. However, the group of points on the curve is not of prime order, i.e., it has a cofactor larger than 1. This abstraction mismatch is usually handled, if it is handled at all, by means of ad hoc protocol tweaks such as multiplying by the cofactor in an appropriate place.

Even for simple protocols such as signatures, these tweaks can cause subtle issues. For instance, Ed25519 implementations may have different validation behavior between batched and singleton verification, and at least as specified in [RFC8032], the set of valid signatures is not defined precisely [Ed25519ValidCrit].

For more complex protocols, careful analysis is required as the original security proofs may no longer apply, and the tweaks for one protocol may have disastrous effects when applied to another (for instance, the octuple-spend vulnerability described in [MoneroVuln]).

Decaf and Ristretto fix this abstraction mismatch in one place for all protocols, providing an abstraction to protocol implementors that matches the abstraction commonly assumed in protocol specifications while still allowing the use of high-performance curve implementations internally. The abstraction layer imposes minor overhead but only in the encoding and decoding phases.

While Ristretto is a general method and can be used in conjunction with any Edwards curve with cofactor 4 or 8, this document specifies the ristretto255 group, which can be implemented using Curve25519, and the decaf448 group, which can be implemented using edwards448.

There are other elliptic curves that can be used internally to implement ristretto255 or decaf448; those implementations would be interoperable with one based on Curve25519 or edwards448, but those constructions are out of scope for this document.

The Ristretto construction is described and justified in detail at [RistrettoGroup].

This document represents the consensus of the Crypto Forum Research Group (CFRG). This document is not an IETF product and is not a standard.

2. Notation and Conventions Used in This Document

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "NOT RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in BCP 14 [RFC2119] [RFC8174] when, and only when, they appear in all capitals, as shown here.

Readers are cautioned that the term "Curve25519" has varying interpretations in the literature and that the canonical meaning of the term has shifted over time. Originally, it referred to a specific Diffie-Hellman key exchange mechanism. Use shifted over time, and "Curve25519" has been used to refer to the abstract underlying curve, its concrete representation in Montgomery form, or the specific Diffie-Hellman mechanism. This document uses the term "Curve25519" to refer to the abstract underlying curve, as recommended in [Naming]. The abstract Edwards form of the curve we refer to here as "Curve25519" is referred to in [RFC7748] as "edwards25519", and the Montgomery form that is isogenous to the Edwards form is referred to in [RFC7748] as "curve25519".

Elliptic curve points in this document are represented in extended Edwards coordinates in the (x, y, z, t) format [Twisted], also called extended homogeneous coordinates in Section 5.1.4 of [RFC8032]. Field elements are values modulo p , the Curve25519 prime $2^{255} - 19$ or the edwards448 prime $2^{448} - 2^{224} - 1$, as specified in Sections 4.1 and 4.2 of [RFC7748], respectively. All formulas specify field operations unless otherwise noted. The symbol $^$ denotes exponentiation.

The $|$ symbol represents a constant-time logical OR.

The notation `array[A:B]` means the elements of array from A to B-1. That is, it is exclusive of B. Arrays are indexed starting from 0.

A byte is an 8-bit entity (also known as "octet"), and a byte string is an ordered sequence of bytes. An N-byte string is a byte string of N bytes in length.

Element encodings are presented as hex-encoded byte strings with whitespace added for readability.

2.1. Negative Field Elements

As in [RFC8032], given a field element e , define `IS_NEGATIVE(e)` as TRUE if the least nonnegative integer representing e is odd and FALSE if it is even. This SHOULD be implemented in constant time.

2.2. Constant-Time Operations

We assume that the field element implementation supports the following operations, which SHOULD be implemented in constant time:

- * `CT_EQ(u, v)`: return TRUE if $u = v$, FALSE otherwise.
- * `CT_SELECT(v IF cond ELSE u)`: return v if `cond` is TRUE, else return u .
- * `CT_ABS(u)`: return $-u$ if `IS_NEGATIVE(u)`, else return u .

Note that `CT_ABS` MAY be implemented as:

`CT_SELECT(-u IF IS_NEGATIVE(u) ELSE u)`

3. The Group Abstraction

Ristretto and Decaf implement an abstract prime-order group interface that exposes only the behavior that is useful to higher-level protocols, without leaking curve-related details and pitfalls.

Each abstract group exposes operations on abstract element and abstract scalar types. The operations defined on these types include: decoding, encoding, equality, addition, negation, subtraction, and (multi-)scalar multiplication. Each abstract group also exposes a deterministic function to derive abstract elements from fixed-length byte strings. A description of each of these operations is below.

Decoding is a function from byte strings to abstract elements with built-in validation, so that only the canonical encodings of valid elements are accepted. The built-in validation avoids the need for explicit invalid curve checks.

Encoding is a function from abstract elements to byte strings. Internally, an abstract element might have more than one possible representation; for example, the implementation might use projective coordinates. When encoding, all equivalent representations of the same element are encoded as identical byte strings. Decoding the output of the encoding function always succeeds and returns an element equivalent to the encoding input.

The equality check reports whether two representations of an abstract element are equivalent.

The element derivation function maps deterministically from byte strings of a fixed length to abstract elements. It has two important properties. First, if the input is a uniformly random byte string, then the output is (within a negligible statistical distance of) a uniformly random abstract group element. This means the function is suitable for selecting random group elements.

Second, although the element derivation function is many-to-one and therefore not strictly invertible, it is not pre-image resistant. On the contrary, given an arbitrary abstract group element P , there is an efficient algorithm to randomly sample from byte strings that map to P . In some contexts, this property would be a weakness, but it is important in some contexts: in particular, it means that a combination of a cryptographic hash function and the element derivation function is suitable to define encoding functions such as `hash_to_ristretto255` (Appendix B of [RFC9380]) and `hash_to_decaf448` (Appendix C of [RFC9380]).

Addition is the group operation. The group has an identity element and prime order l . Adding together l copies of the same element gives the identity. Adding the identity element to any element returns that element unchanged. Negation returns an element that, when added to the negation input, gives the identity element. Subtraction is the addition of a negated element, and scalar multiplication is the repeated addition of an element.

4. ristretto255

ristretto255 is an instantiation of the abstract prime-order group interface defined in Section 3. This document describes how to implement the ristretto255 prime-order group using Curve25519 points as internal representations.

A "ristretto255 group element" is the abstract element of the prime-order group. An "element encoding" is the unique reversible encoding of a group element. An "internal representation" is a point on the curve used to implement ristretto255. Each group element can have multiple equivalent internal representations.

Encoding, decoding, equality, and the element derivation function are defined in Section 4.3. Element addition, subtraction, negation, and scalar multiplication are implemented by applying the corresponding operations directly to the internal representation.

The group order is the same as the order of the Curve25519 prime-order subgroup:

$$l = 2^{252} + 27742317777372353535851937790883648493$$

Since ristretto255 is a prime-order group, every element except the identity is a generator. However, for interoperability, a canonical generator is selected, which can be internally represented by the Curve25519 base point, enabling reuse of existing precomputation for scalar multiplication. The encoding of this canonical generator, as produced by the function specified in Section 4.3.2, is:

e2f2ae0a 6abc4e71 a884a961 c500515f 58e30b6a a582dd8d b6a65945 e08d2d76

4.1. Implementation Constants

This document references the following constant field element values that are used for the implementation of group operations.

- * D = 37095705934669439343138083508754565189542113879843219016388785533085940283555
- This is the Edwards d parameter for Curve25519, as specified in Section 4.1 of [RFC7748].
- * Sqrt_M1 = 19681161376707505956807079304988542015446066515923890162744021073123829784752
- * Sqrt_AD_MINUS_ONE = 25063068953384623474111414158702152701244531502492656460079210482610430750235
- * InverseSqrt_A_MINUS_D = 54469307008909316920995813868745141605393597292927456921205312896311721017578
- * ONE_MINUS_D_SQ = 1159843021668779879193775521855586647937357759715417654439879720876111806838
- * D_MINUS_ONE_SQ = 40440834346308536858101042469323190826248399146238708352240133220865137265952

4.2. Square Root of a Ratio of Field Elements

The following function is defined on field elements and is used to implement other ristretto255 functions. This function is only used internally to implement some of the group operations.

On input field elements u and v , the function $\text{SQRT_RATIO_M1}(u, v)$ returns:

- * $(\text{TRUE}, +\text{sqrt}(u/v))$ if u and v are nonzero and u/v is square in the field;
- * $(\text{TRUE}, \text{zero})$ if u is zero;
- * $(\text{FALSE}, \text{zero})$ if v is zero and u is nonzero; and
- * $(\text{FALSE}, +\text{sqrt}(\text{SQRT_M1}(u/v)))$ if u and v are nonzero and u/v is non-square in the field (so $\text{SQRT_M1}(u/v)$ is square in the field),

where $+\text{sqrt}(x)$ indicates the nonnegative square root of x in the field.

The computation is similar to what is described in Section 5.1.3 of [RFC8032], with the difference that, if the input is non-square, the function returns a result with a defined relationship to the inputs. This result is used for efficient implementation of the derivation function. The function can be refactored from an existing Ed25519 implementation.

$\text{SQRT_RATIO_M1}(u, v)$ is defined as follows:

```
r = (u * v^3) * (u * v^7)^((p-5)/8) // Note: (p - 5) / 8 is an integer.
check = v * r^2

correct_sign_sqrt    = CT_EQ(check, u)
flipped_sign_sqrt    = CT_EQ(check, -u)
flipped_sign_sqrt_i  = CT_EQ(check, -u*SQRT_M1)

r_prime = SQRT_M1 * r
r = CT_SELECT(r_prime IF flipped_sign_sqrt | flipped_sign_sqrt_i ELSE r)

// Choose the nonnegative square root.
r = CT_ABS(r)

was_square = correct_sign_sqrt | flipped_sign_sqrt

return (was_square, r)
```

4.3. ristretto255 Group Operations

This section describes the implementation of the external functions exposed by the ristretto255 prime-order group.

4.3.1. Decode

All elements are encoded as 32-byte strings. Decoding proceeds as follows:

1. Interpret the string as an unsigned integer s in little-endian representation. If the length of the string is not 32 bytes or if the resulting value is $\geq p$, decoding fails.

Note: Unlike the field element decoding described in [RFC7748], the most significant bit is not masked, and non-canonical values are rejected. The test vectors in Appendix A.2 exercise

| these edge cases.

2. If `IS_NEGATIVE(s)` returns `TRUE`, decoding fails.
3. Process `s` as follows:

```
ss = s^2
u1 = 1 - ss
u2 = 1 + ss
u2_sqr = u2^2
```

```
v = -(D * u1^2) - u2_sqr
```

```
(was_square, invsqrt) = Sqrt_Ratio_M1(1, v * u2_sqr)
```

```
den_x = invsqrt * u2
den_y = invsqrt * den_x * v
```

```
x = CT_ABS(2 * s * den_x)
y = u1 * den_y
t = x * y
```

4. If `was_square` is `FALSE`, `IS_NEGATIVE(t)` returns `TRUE`, or `y = 0`, decoding fails. Otherwise, return the group element represented by the internal representation `(x, y, 1, t)` as the result of decoding.

4.3.2. Encode

A group element with internal representation `(x0, y0, z0, t0)` is encoded as follows:

1. Process the internal representation into a field element `s` as follows:

```
u1 = (z0 + y0) * (z0 - y0)
u2 = x0 * y0
```

```
// Ignore was_square since this is always square.
(_, invsqrt) = Sqrt_Ratio_M1(1, u1 * u2^2)
```

```
den1 = invsqrt * u1
den2 = invsqrt * u2
z_inv = den1 * den2 * t0
```

```
ix0 = x0 * Sqrt_M1
iy0 = y0 * Sqrt_M1
enchanted_denominator = den1 * INVSqrt_A_Minus_D
```

```
rotate = IS_NEGATIVE(t0 * z_inv)
```

```
// Conditionally rotate x and y.
x = CT_SELECT(iy0 IF rotate ELSE x0)
y = CT_SELECT(ix0 IF rotate ELSE y0)
z = z0
den_inv = CT_SELECT(enchanted_denominator IF rotate ELSE den2)
```


$y = \text{CT_SELECT}(-y \text{ IF } \text{IS_NEGATIVE}(x * z_inv) \text{ ELSE } y)$

$s = \text{CT_ABS}(\text{den_inv} * (z - y))$

2. Return the 32-byte little-endian encoding of s . More specifically, this is the encoding of the canonical representation of s as an integer between 0 and $p-1$, inclusive.

Note that decoding and then re-encoding a valid group element will yield an identical byte string.

4.3.3. Equals

The equality function returns TRUE when two internal representations correspond to the same group element. Note that internal representations MUST NOT be compared in any way other than specified here.

For two internal representations $(x1, y1, z1, t1)$ and $(x2, y2, z2, t2)$, if

$\text{CT_EQ}(x1 * y2, y1 * x2) \mid \text{CT_EQ}(y1 * y2, x1 * x2)$

evaluates to TRUE, then return TRUE. Otherwise, return FALSE.

Note that the equality function always returns TRUE when applied to an internal representation and to the internal representation obtained by encoding and then re-decoding it. However, the internal representations themselves might not be identical.

Implementations MAY also perform constant-time byte comparisons on the encodings of group elements (produced by Section 4.3.2) for an equivalent, although less efficient, result.

4.3.4. Element Derivation

The element derivation function operates on 64-byte strings. To obtain such an input from an arbitrary-length byte string, applications should use a domain-separated hash construction, the choice of which is out of scope for this document.

The element derivation function on an input string b proceeds as follows:

1. Compute $P1$ as $\text{MAP}(b[0:32])$.
2. Compute $P2$ as $\text{MAP}(b[32:64])$.
3. Return $P1 + P2$.

The MAP function is defined on 32-byte strings as:

1. Mask the most significant bit in the final byte of the string, and interpret the string as an unsigned integer r in little-endian representation. Reduce r modulo p to obtain a field element t .
 - * Masking the most significant bit is equivalent to interpreting the whole string as an unsigned integer in little-endian

representation and then reducing it modulo 2^{255} .

Note: Similar to the field element decoding described in [RFC7748], and unlike the field element decoding described in Section 4.3.1, the most significant bit is masked, and non-canonical values are accepted.

2. Process t as follows:

```
r = Sqrt_M1 * t^2
u = (r + 1) * ONE_MINUS_D_SQ
v = (-1 - r*D) * (r + D)

(was_square, s) = Sqrt_Ratio_M1(u, v)
s_prime = -CT_ABS(s*t)
s = CT_SELECT(s IF was_square ELSE s_prime)
c = CT_SELECT(-1 IF was_square ELSE r)

N = c * (r - 1) * D_MINUS_ONE_SQ - v

w0 = 2 * s * v
w1 = N * Sqrt_AD_MINUS_ONE
w2 = 1 - s^2
w3 = 1 + s^2
```

3. Return the group element represented by the internal representation ($w0*w3$, $w2*w1$, $w1*w3$, $w0*w2$).

4.4. Scalar Field

The scalars for the ristretto255 group are integers modulo the order l of the ristretto255 group. Note that this is the same scalar field as Curve25519, allowing existing implementations to be reused.

Scalars are encoded as 32-byte strings in little-endian order. Implementations SHOULD check that any scalar s falls in the range $0 \leq s < l$ when parsing them and reject non-canonical scalar encodings. Implementations SHOULD reduce scalars modulo l when encoding them as byte strings. Omitting these strict range checks is NOT RECOMMENDED but is allowed to enable reuse of scalar arithmetic implementations in existing Curve25519 libraries.

Given a uniformly distributed 64-byte string b , implementations can obtain a uniformly distributed scalar by interpreting the 64-byte string as a 512-bit unsigned integer in little-endian order and reducing the integer modulo l , as in [RFC8032]. To obtain such an input from an arbitrary-length byte string, applications should use a domain-separated hash construction, the choice of which is out of scope for this document.

5. decaf448

decaf448 is an instantiation of the abstract prime-order group interface defined in Section 3. This document describes how to implement the decaf448 prime-order group using edwards448 points as internal representations.

A "decaf448 group element" is the abstract element of the prime-order group. An "element encoding" is the unique reversible encoding of a group element. An "internal representation" is a point on the curve used to implement decaf448. Each group element can have multiple equivalent internal representations.

Encoding, decoding, equality, and the element derivation functions are defined in Section 5.3. Element addition, subtraction, negation, and scalar multiplication are implemented by applying the corresponding operations directly to the internal representation.

The group order is the same as the order of the edwards448 prime-order subgroup:

```
l = 2^446 -  
13818066809895115352007386748515426880336692474882178609894547503885
```

Since decaf448 is a prime-order group, every element except the identity is a generator; however, for interoperability, a canonical generator is selected. This generator can be internally represented by $2*B$, where B is the edwards448 base point, enabling reuse of existing precomputation for scalar multiplication. The encoding of this canonical generator, as produced by the function specified in Section 5.3.2, is:

```
66666666 66666666 66666666 66666666 66666666 66666666 66666666  
33333333 33333333 33333333 33333333 33333333 33333333 33333333
```

This repetitive constant is equal to $1/\sqrt{5}$ in decaf448's field, corresponding to the curve448 base point with $x = 5$.

5.1. Implementation Constants

This document references the following constant field element values that are used for the implementation of group operations.

```
* D = 72683872429560689054932380788800453435364136068731806028149019  
918061232816673077268639638369867654593008888446184363736105349801  
8326358  
- This is the Edwards d parameter for edwards448, as specified in  
  Section 4.2 of [RFC7748], and is equal to -39081 in the field.  
* ONE_MINUS_D = 39082  
* ONE_MINUS_TWO_D = 78163  
* Sqrt_MINUS_D = 989442336477322197691770048769290191284175762955299  
010740998895980437021160012578568021315638965153739277122320928458  
83226922417596214  
* INVSqrt_MINUS_D = 315019913931389607337177038330951043522456072897  
266928557328499619017160722351061360252776265186336876723201881398  
623946864393857820716
```

5.2. Square Root of a Ratio of Field Elements

The following function is defined on field elements and is used to implement other decaf448 functions. This function is only used internally to implement some of the group operations.

On input field elements u and v , the function `SQRT_RATIO_M1(u, v)` returns:

- * `(TRUE, +sqrt(u/v))` if u and v are nonzero and u/v is square in the field;
- * `(TRUE, zero)` if u is zero;
- * `(FALSE, zero)` if v is zero and u is nonzero; and
- * `(FALSE, +sqrt(-u/v))` if u and v are nonzero and u/v is non-square in the field (so $-(u/v)$ is square in the field),

where `+sqrt(x)` indicates the nonnegative square root of x in the field.

The computation is similar to what is described in Section 5.2.3 of [RFC8032], with the difference that, if the input is non-square, the function returns a result with a defined relationship to the inputs. This result is used for efficient implementation of the derivation function. The function can be refactored from an existing `edwards448` implementation.

`SQRT_RATIO_M1(u, v)` is defined as follows:

```
r = u * (u * v)^((p - 3) / 4) // Note: (p - 3) / 4 is an integer.
```

```
check = v * r^2
was_square = CT_EQ(check, u)
```

```
// Choose the nonnegative square root.
r = CT_ABS(r)
```

```
return (was_square, r)
```

5.3. decaf448 Group Operations

This section describes the implementation of the external functions exposed by the `decaf448` prime-order group.

5.3.1. Decode

All elements are encoded as 56-byte strings. Decoding proceeds as follows:

1. Interpret the string as an unsigned integer s in little-endian representation. If the length of the string is not 56 bytes or if the resulting value is $\geq p$, decoding fails.

Note: Unlike the field element decoding described in [RFC7748], non-canonical values are rejected. The test vectors in Appendix B.2 exercise these edge cases.

2. If `IS_NEGATIVE(s)` returns `TRUE`, decoding fails.
3. Process s as follows:

```
ss = s^2
u1 = 1 + ss
```

```
u2 = u1^2 - 4 * D * ss
```

```
(was_square, invsqrt) = Sqrt_Ratio_M1(1, u2 * u1^2)
```

```
u3 = CT_ABS(2 * s * invsqrt * u1 * Sqrt_Minus_D)
```

```
x = u3 * invsqrt * u2 * Invsqrt_Minus_D
```

```
y = (1 - ss) * invsqrt * u1
```

```
t = x * y
```

4. If `was_square` is `FALSE`, then decoding fails. Otherwise, return the group element represented by the internal representation $(x, y, 1, t)$ as the result of decoding.

5.3.2. Encode

A group element with internal representation (x_0, y_0, z_0, t_0) is encoded as follows:

1. Process the internal representation into a field element s as follows:

```
u1 = (x0 + t0) * (x0 - t0)
```

```
// Ignore was_square since this is always square.
```

```
(_, invsqrt) = Sqrt_Ratio_M1(1, u1 * ONE_MINUS_D * x0^2)
```

```
ratio = CT_ABS(invsqrt * u1 * Sqrt_Minus_D)
```

```
u2 = Invsqrt_Minus_D * ratio * z0 - t0
```

```
s = CT_ABS(ONE_MINUS_D * invsqrt * x0 * u2)
```

2. Return the 56-byte little-endian encoding of s . More specifically, this is the encoding of the canonical representation of s as an integer between 0 and $p-1$, inclusive.

Note that decoding and then re-encoding a valid group element will yield an identical byte string.

5.3.3. Equals

The equality function returns `TRUE` when two internal representations correspond to the same group element. Note that internal representations **MUST NOT** be compared in any way other than specified here.

For two internal representations (x_1, y_1, z_1, t_1) and (x_2, y_2, z_2, t_2) , if

```
CT_EQ(x1 * y2, y1 * x2)
```

evaluates to `TRUE`, then return `TRUE`. Otherwise, return `FALSE`.

Note that the equality function always returns `TRUE` when applied to an internal representation and to the internal representation obtained by encoding and then re-decoding it. However, the internal

representations themselves might not be identical.

Implementations MAY also perform constant-time byte comparisons on the encodings of group elements (produced by Section 5.3.2) for an equivalent, although less efficient, result.

5.3.4. Element Derivation

The element derivation function operates on 112-byte strings. To obtain such an input from an arbitrary-length byte string, applications should use a domain-separated hash construction, the choice of which is out of scope for this document.

The element derivation function on an input string b proceeds as follows:

1. Compute $P1$ as $\text{MAP}(b[0:56])$.
2. Compute $P2$ as $\text{MAP}(b[56:112])$.
3. Return $P1 + P2$.

The MAP function is defined on 56-byte strings as:

1. Interpret the string as an unsigned integer r in little-endian representation. Reduce r modulo p to obtain a field element t .

Note: Similar to the field element decoding described in [RFC7748], and unlike the field element decoding described in Section 5.3.1, non-canonical values are accepted.

2. Process t as follows:

```
r = -t^2
u0 = d * (r-1)
u1 = (u0 + 1) * (u0 - r)

(was_square, v) = SqrtRatioM1(ONE_MINUS_TWO_D, (r + 1) * u1)
v_prime = CT_SELECT(v IF was_square ELSE t * v)
sgn      = CT_SELECT(1 IF was_square ELSE -1)
s = v_prime * (r + 1)
```

```
w0 = 2 * CT_ABS(s)
w1 = s^2 + 1
w2 = s^2 - 1
w3 = v_prime * s * (r - 1) * ONE_MINUS_TWO_D + sgn
```

3. Return the group element represented by the internal representation $(w0*w3, w2*w1, w1*w3, w0*w2)$.

5.4. Scalar Field

The scalars for the decaf448 group are integers modulo the order l of the decaf448 group. Note that this is the same scalar field as edwards448, allowing existing implementations to be reused.

Scalars are encoded as 56-byte strings in little-endian order. Implementations SHOULD check that any scalar s falls in the range 0

$s \leq s < l$ when parsing them and reject non-canonical scalar encodings. Implementations SHOULD reduce scalars modulo l when encoding them as byte strings. Omitting these strict range checks is NOT RECOMMENDED but is allowed to enable reuse of scalar arithmetic implementations in existing edwards448 libraries.

Given a uniformly distributed 64-byte string b , implementations can obtain a uniformly distributed scalar by interpreting the 64-byte string as a 512-bit unsigned integer in little-endian order and reducing the integer modulo l . To obtain such an input from an arbitrary-length byte string, applications should use a domain-separated hash construction, the choice of which is out of scope for this document.

6. API Considerations

`ristretto255` and `decaf448` are abstractions that implement two prime-order groups. Their elements are represented by curve points, but are not curve points, and implementations SHOULD reflect that fact. That is, the type representing an element of the group SHOULD be opaque to the caller, meaning they do not expose the underlying curve point or field elements. Moreover, implementations SHOULD NOT expose any internal constants or functions used in the implementation of the group operations.

The reason for this encapsulation is that `ristretto255` and `decaf448` implementations can change their underlying curve without causing any breaking change. The `ristretto255` and `decaf448` constructions are carefully designed so that this will be the case, as long as implementations do not expose internal representations or operate on them except as described in this document. In particular, implementations SHOULD NOT define any external `ristretto255` or `decaf448` interface as operating on arbitrary curve points, and they SHOULD NOT construct group elements except via decoding, the element derivation function, or group operations on other valid group elements per Section 3. However, they are allowed to apply any optimization strategy to the internal representations as long as it doesn't change the exposed behavior of the API.

It is RECOMMENDED that implementations not perform a decoding and encoding operation for each group operation, as it is inefficient and unnecessary. Implementations SHOULD instead provide an opaque type to hold the internal representation through multiple operations.

7. IANA Considerations

This document has no IANA actions.

8. Security Considerations

The `ristretto255` and `decaf448` groups provide higher-level protocols with the abstraction they expect: a prime-order group. Therefore, it's expected to be safer for use in any situation where `Curve25519` or `edwards448` is used to implement a protocol requiring a prime-order group. Note that the safety of the abstraction can be defeated by implementations that do not follow the guidance in Section 6.

There is no function to test whether an elliptic curve point is a valid internal representation of a group element. The decoding function always returns a valid internal representation or an error, and operations exposed by the group per Section 3 return valid internal representations when applied to valid internal representations. In this way, an implementation can maintain the invariant that an internal representation is always valid, so that checking is never necessary, and invalid states are unrepresentable.

9. References

9.1. Normative References

- [RFC2119] Bradner, S., "Key words for use in RFCs to Indicate Requirement Levels", BCP 14, RFC 2119, DOI 10.17487/RFC2119, March 1997, <<https://www.rfc-editor.org/info/rfc2119>>.
- [RFC8174] Leiba, B., "Ambiguity of Uppercase vs Lowercase in RFC 2119 Key Words", BCP 14, RFC 8174, DOI 10.17487/RFC8174, May 2017, <<https://www.rfc-editor.org/info/rfc8174>>.

9.2. Informative References

- [Decaf] Hamburg, M., "Decaf: Eliminating cofactors through point compression", 2015, <<https://www.shiftright.org/papers/decaf/decaf.pdf>>.
- [Ed25519ValidCrit] de Valence, H., "It's 255:19AM. Do you know what your validation criteria are?", 4 October 2020, <<https://hdevalence.ca/blog/2020-10-04-its-25519am>>.
- [MoneroVuln] Nick, J., "Exploiting Low Order Generators in One-Time Ring Signatures", May 2017, <<https://jonasnick.github.io/blog/2017/05/23/exploiting-low-order-generators-in-one-time-ring-signatures/>>.
- [Naming] Bernstein, D. J., "Subject: [Cfrg] 25519 naming", message to the Cfrg mailing list, 26 August 2014, <https://mailarchive.ietf.org/arch/msg/cfrg/-9LEdnzVrE5R0Rux30o_oDDRksU/>.
- [RFC7748] Langley, A., Hamburg, M., and S. Turner, "Elliptic Curves for Security", RFC 7748, DOI 10.17487/RFC7748, January 2016, <<https://www.rfc-editor.org/info/rfc7748>>.
- [RFC8032] Josefsson, S. and I. Liusvaara, "Edwards-Curve Digital Signature Algorithm (EdDSA)", RFC 8032, DOI 10.17487/RFC8032, January 2017, <<https://www.rfc-editor.org/info/rfc8032>>.
- [RFC9380] Faz-Hernandez, A., Scott, S., Sullivan, N., Wahby, R. S., and C. A. Wood, "Hashing to Elliptic Curves", RFC 9380,

[RistrettoGroup] de Valence, H., Lovecruft, I., Arcieri, T., and M. Hamburg, "The Ristretto Group", <<https://ristretto.group>>.

[Twisted] Hisil, H., Wong, K. K., Carter, G., and E. Dawson, "Twisted Edwards Curves Revisited", Cryptology ePrint Archive, Paper 2008/522, December 2008, <<https://eprint.iacr.org/2008/522>>.

Appendix A. Test Vectors for ristretto255

This section contains test vectors for ristretto255. The octets are hex encoded, and whitespace is inserted for readability.

A.1. Multiples of the Generator

The following are the encodings of the multiples 0 to 15 of the canonical generator, represented as an array of elements. That is, the first entry is the encoding of the identity element, and each successive entry is obtained by adding the generator to the previous entry.

B[0]:	00000000	00000000	00000000	00000000	00000000	00000000	00000000
B[1]:	e2f2ae0a	6abc4e71	a884a961	c500515f	58e30b6a	a582dd8d	b6a65945
B[2]:	6a493210	f7499cd1	7fecb510	ae0cea23	a110e8d5	b901f8ac	add3095c
B[3]:	94741f5d	5d52755e	ce4f23f0	44ee27d5	d1ea1e2b	d196b462	166b1615
B[4]:	da808627	73358b46	6ffadfe0	b3293ab3	d9fd53c5	ea6c9553	58f56832
B[5]:	e882b131	016b52c1	d3337080	187cf768	423efccb	b517bb49	5ab812c4
B[6]:	f64746d3	c92b1305	0ed8d802	36a7f000	7c3b3f96	2f5ba793	d19a601e
B[7]:	44f53520	926ec81f	bd5a3878	45beb7df	85a96a24	ece18738	bdcfa6a7
B[8]:	903293d8	f2287ebe	10e2374d	c1a53e0b	c887e592	699f02d0	77d5263c
B[9]:	02622ace	8f7303a3	1cafc63f	8fc48fdc	16e1c8c8	d234b2f0	d6685282
B[10]:	20706fd7	88b2720a	1ed2a5da	d4952b01	f413bcf0	e7564de8	cdc81668
B[11]:	bce83f8b	a5dd2fa5	72864c24	ba1810f9	522bc600	4afe9587	7ac73241
B[12]:	e4549ee1	6b9aa030	99ca208c	67adafca	fa4c3f3e	4e5303de	6026e3ca
B[13]:	aa52e000	df2e16f5	5fb1032f	c33bc427	42dad6bd	5a8fc0be	0167436c
B[14]:	46376b80	f409b29d	c2b5f6f0	c5259199	0896e571	6f41477c	d30085ab
B[15]:	e0c418f7	c8d9c4cd	d7395b93	ea124f3a	d99021bb	681dfc33	02a9d99a

2e53e64e

Note that because

$$B[i+1] = B[i] + B[1]$$

these test vectors allow testing of the encoding function and the implementation of addition simultaneously.

A.2. Invalid Encodings

These are examples of encodings that MUST be rejected according to Section 4.3.1.

Non-canonical field encodings.

00ffffff ffffffff ffffffff ffffffff ffffffff ffffffff ffffffff
fffffff

fffffff ffffffff ffffffff ffffffff ffffffff ffffffff ffffffff
ffffff7f

f3ffffff ffffffff ffffffff ffffffff ffffffff ffffffff ffffffff
ffffff7f

edffffff ffffffff ffffffff ffffffff ffffffff ffffffff ffffffff
ffffff7f

Negative field elements.

01000000 00000000 00000000 00000000 00000000 00000000 00000000
00000000

01ffffff ffffffff ffffffff ffffffff ffffffff ffffffff ffffffff
ffffff7f

ed57ffd8 c914fb20 1471d1c3 d245ce3c 746fcbe6 3a3679d5 1b6a516e
bebe0e20

c34c4e18 26e5d403 b78e246e 88aa051c 36ccf0aa febffe13 7d148a2b
f9104562

c940e5a4 404157cf b1628b10 8db051a8 d439e1a4 21394ec4 ebccb9ec
92a8ac78

47cfc549 7c53dc8e 61c91d17 fd626ffb 1c49e2bc a94eed05 2281b510
b1117a24

f1c6165d 33367351 b0da8f6e 4511010c 68174a03 b6581212 c71c0e1d
026c3c72

87260f7a 2f124951 18360f02 c26a470f 450dadf3 4a413d21 042b43b9
d93e1309

Non-square x^2 .

26948d35 ca62e643 e26a8317 7332e6b6 afeb9d08 e4268b65 0f1f5bbd
8d81d371

4eac077a 713c57b4 f4397629 a4145982 c661f480 44dd3f96 427d40b1
47d9742f

de6a7b00 deadc788 eb6b6c8d 20c0ae96 c2f20190 78fa604f ee5b87d6
e989ad7b

bcab477b e20861e0 1e4a0e29 5284146a 510150d9 817763ca f1a6f4b4
22d67042

2a292df7 e32cabab bd9de088 d1d1abec 9fc0440f 637ed2fb a145094d
c14bea08

f4a9e534 fc0d216c 44b218fa 0c42d996 35a0127e e2e53c71 2f706096
49fdff22

8268436f 8c412619 6cf64b3c 7ddbda90 746a3786 25f9813d d9b84570
77256731

2810e5cb c2cc4d4e ece54f61 c6f69758 e289aa7a b440b3cb eaa21995
c2f4232b

Negative $x * y$ value.
3eb858e7 8f5a7254 d8c97311 74a94f76 755fd394 1c0ac937 35c07ba1
4579630e

a45fdc55 c76448c0 49a1ab33 f17023ed fb2be358 1e9c7aad e8a61252
15e04220

d483fe81 3c6ba647 ebbfd3ec 41adca1c 6130c2be eee9d9bf 065c8d15
1c5f396e

8a2e1d30 050198c6 5a544831 23960ccc 38aef684 8e1ec8f5 f780e852
3769ba32

32888462 f8b486c6 8ad7dd96 10be5192 bbeaf3b4 43951ac1 a8118419
d9fa097b

22714250 1b9d4355 ccba2904 04bde415 75b03769 3cef1f43 8c47f8fb
f35d1165

5c37cc49 1da847cf eb9281d4 07efc41e 15144c87 6e0170b4 99a96a22
ed31e01e

44542511 7cb8c90e dcbc7c1c c0e74f74 7f2c1efa 5630a967 c64f2877
92a48a4b

$s = -1$, which causes $y = 0$.
ecffffff ffffffff ffffffff ffffffff ffffffff ffffffff ffffffff
fffffff7f

A.3. Group Elements from Uniform Byte Strings

The following pairs are inputs to the element derivation function of Section 4.3.4 and their encoded outputs.

I: 5d1be09e3d0c82fc538112490e35701979d99e06ca3e2b5b54bffe8b4dc772c1

```

4d98b696a1bbfb5ca32c436cc61c16563790306c79eaca7705668b47dffe5bb6
0: 3066f82a 1a747d45 120d1740 f1435853 1a8f04bb ffe6a819 f86dfe50
f44a0a46

I: f116b34b8f17ceb56e8732a60d913dd10cce47a6d53bee9204be8b44f6678b27
0102a56902e2488c46120e9276cfe54638286b9e4b3cdb470b542d46c2068d38
0: f26e5b6f 7d362d2d 2a94c5d0 e7602cb4 773c95a2 e5c31a64 f133189f
a76ed61b

I: 8422e1bbdaab52938b81fd602effb6f89110e1e57208ad12d9ad767e2e25510c
27140775f9337088b982d83d7fcf0b2fa1edffe51952cbe7365e95c86eaf325c
0: 006ccd2a 9e6867e6 a2c5cea8 3d3302cc 9de128dd 2a9a57dd 8ee7b9d7
ffe02826

I: ac22415129b61427bf464e17baee8db65940c233b98afce8d17c57beeb7876c2
150d15af1cb1fb824bbd14955f2b57d08d388aab431a391cfc33d5bafb5dbbaf
0: f8f0c87c f237953c 5890aec3 99816900 5dae3eca 1fbb0454 8c635953
c817f92a

I: 165d697a1ef3d5cf3c38565beefcf88c0f282b8e7dbd28544c483432f1cec767
5debea8ebb4e5fe7d6f6e5db15f15587ac4d4d4a1de7191e0c1ca6664abcc413
0: ae81e7de df20a497 e10c304a 765c1767 a42d6e06 029758d2 d7e8ef7c
c4c41179

I: a836e6c9a9ca9f1e8d486273ad56a78c70cf18f0ce10abb1c7172ddd605d7fd2
979854f47ae1ccf204a33102095b4200e5befc0465accc263175485f0e17ea5c
0: e2705652 ff9f5e44 d3e841bf 1c251cf7 dddb77d1 40870d1a b2ed64f1
a9ce8628

I: 2cdc11eae95daf01189417cdddbf95952993aa9cb9c640eb5058d09702c7462
2c9965a697a3b345ec24ee56335b556e677b30e6f90ac77d781064f866a3c982
0: 80bd0726 2511cdde 4863f8a7 434cef69 6750681c b9510eea 557088f7
6d9e5065

```

The following element derivation function inputs all produce the same encoded output.

```
I: edffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffff
1200000000000000000000000000000000000000000000000000000000000000
I: edffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffff7f
ffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffff
I: 0000000000000000000000000000000000000000000000000000000000000080
ffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffff7f
I: 00000000000000000000000000000000000000000000000000000000000000
120000000000000000000000000000000000000000000000000000000000080

0: 30428279 1023b731 28d277bd cb5c7746 ef2eac08 dde9f298 3379cb8e
5ef0517f
```

A.4. Square Root of a Ratio of Field Elements

The following are inputs and outputs of `SQRT_RATIO_M1(u, v)` defined in Section 4.2. The values are little-endian encodings of field elements.

[illegible]


```

B[ 7]: 502bcb68 42eb06f0 e49032ba e87c554c 031d6d4d 2d7694ef bf9c468d
        48220c50 f8ca2884 3364d70c ee92d6fe 246e6144 8f9db980 8b3b2408
B[ 8]: 0c9810f1 e2ebd389 caa78937 4d780079 74ef4d17 227316f4 0e578b33
        6827da3f 6b482a47 94eb6a39 75b971b5 e1388f52 e91ea2f1 bcb0f912
B[ 9]: 20d41d85 a18d5657 a2964032 1563bbd0 4c2ffbd0 a37a7ba4 3a4f7d26
        3ce26faf 4e1f74f9 f4b590c6 9229ae57 1fe37fa6 39b5b8eb 48bd9a55
B[10]: e6b4b8f4 08c7010d 0601e7ed a0c309a1 a42720d6 d06b5759 fdc4e1ef
        e22d076d 6c44d42f 508d67be 462914d2 8b8edce3 2e709430 5164af17
B[11]: be88bbb8 6c59c13d 8e9d09ab 98105f69 c2d1dd13 4dbcd3b0 863658f5
        3159db64 c0e139d1 80f3c89b 8296d0ae 324419c0 6fa87fc7 daaf34c1
B[12]: a456f936 9769e8f0 8902124a 0314c7a0 6537a06e 32411f4f 93415950
        a17badfa 7442b621 7434a3a0 5ef45be5 f10bd7b2 ef8ea00c 431edec5
B[13]: 186e452c 4466aa43 83b4c002 10d52e79 22dbf977 1e8b47e2 29a9b7b7
        3c8d10fd 7ef0b6e4 1530f91f 24a3ed9a b71fa38b 98b2fe47 46d51d68
B[14]: 4ae7fdca e9453f19 5a8ead5c be1a7b96 99673b52 c40ab279 27464887
        be53237f 7f3a21b9 38d40d0e c9e15b1d 5130b13f fed81373 a53e2b43
B[15]: 841981c3 bfeec3f6 0cfeca75 d9d8dc17 f46cf010 6f2422b5 9aec580a
        58f34227 2e3a5e57 5a055ddb 051390c5 4c24c6ec b1e0aceb 075f6056

```

B.2. Invalid Encodings

These are examples of encodings that **MUST** be rejected according to Section 5.3.1.

Non-canonical field encodings.

```

8e24f838 059ee9fe f1e20912 6defe53d cd74ef9b 6304601c 6966099e
ffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff

```

```

86fcc721 2bd4a0b9 80928666 dc28c444 a605ef38 e09fb569 e28d4443
ffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff

```

```

866d54bd 4c4ff41a 55d4eefd beca73cb d653c7bd 3135b383 708ec0bd
ffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff

```

```

4a380ccd ab9c8636 4a89e77a 464d64f9 157538cf dfa686ad c0d5ece4
ffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff

```

```

f22d9d4c 945dd44d 11e0b1d3 d3d358d9 59b4844d 83b08c44 e659d79f
ffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff

```

```

8cdfc68 1aa99e9c 818c8ef4 c3808b58 e86acdef 1ab68c84 77af185b
ffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff

```

```

0e1c12ac 7b5920ef fbd044e8 97c57634 e2d05b5c 27f8fa3d f8a086a1
ffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff ffffffffff

```

Negative field elements.

```

15141bd2 121837ef 71a0016b d11be757 507221c2 6542244f 23806f3f
d3496b7d 4c368262 76f3bf5d eea2c60c 4fa4cec6 9946876d a497e795

```

```

455d3802 38434ab7 40a56267 f4f46b7d 2eb2dd8e e905e51d 7b0ae8a6
cb2bae50 1e67df34 ab21fa45 946068c9 f233939b 1d9521a9 98b7cb93

```

```

810b1d8e 8bf3a9c0 23294bbf d3d905a9 7531709b dc0f4239 0feedd70
10f77e98 686d400c 9c86ed25 0ceecd9d e0a18888 ffecda0f 4ea1c60d

```

d3af9cc4	1be0e5de	83c0c627	3bedcb93	51970110	044a9a41	c7b9b226
7cdb9d7b	f4dc9c2f	db8bed32	87818460	4f1d9944	305a8df4	274ce301
9312bcab	09009e43	30ff89c4	bc1e9e00	0d863efc	3c863d3b	6c507a40
fd2cdefd	e1bf0892	b4b5ed97	80b91ed1	398fb4a7	344c605a	a5efda74
53d11bce	9e62a29d	63ed82ae	93761bdd	76e38c21	e2822d6e	bee5eb1c
5b8a03ea	f9df749e	2490eda9	d8ac27d1	f71150de	93668074	d18d1c3a
697c1aed	3cd88585	15d4be8a	c158b229	fe184d79	cb2b06e4	9210a6f3
a7cd537b	cd9bd390	d96c4ab6	a4406da5	d9364072	6285370c	fa95df80
# Non-square x^2 .						
58ad4871	5c9a1025	69b68b88	362a4b06	45781f5a	19eb7e59	c6a4686f
d0f0750f	f42e3d7a	f1ab38c2	9d69b670	f3125891	9c9fdbf6	093d06c0
8ca37ee2	b15693f0	6e910cf4	3c4e32f1	d5551dda	8b1e48cb	6ddd55e4
40dbc7b2	96b60191	9a4e4069	f59239ca	247ff693	f7daa42f	086122b1
982c0ec7	f43d9f97	c0a74b36	db0abd9c	a6bfb981	23a90782	787242c8
a523cdc7	6df14a91	0d544711	27e7662a	1059201f	902940cd	39d57af5
baa9ab82	d07ca282	b968a911	a6c3728d	74bf2fe2	58901925	787f03ee
4be7e3cb	6684fd1b	cfe5071a	9a974ad2	49a4aaa8	ca812642	16c68574
2ed9ffe2	ded67a37	2b181ac5	24996402	c4297062	9db03f5e	8636cbaf
6074b523	d154a7a8	c4472c4c	353ab88c	d6fec7da	7780834c	c5bd5242
f063769e	4241e76d	815800e4	933a3a14	4327a30e	c40758ad	3723a788
388399f7	b3f5d45b	6351eb8e	ddefda7d	5bff4ee9	20d338a8	b89d8b63
5a0104f1	f55d152c	eb68bc13	81824998	91d90ee8	f09b4003	8ccc1e07
cb621fd4	62f781d0	45732a4f	0bda73f0	b2acf943	55424ff0	388d4b9c

B.3. Group Elements from Uniform Byte Strings

The following pairs are inputs to the element derivation function of Section 5.3.4 and their encoded outputs.

I:	cbb8c991fd2f0b7e1913462d6463e4fd2ce4ccdd28274dc2ca1f4165 d5ee6cdccea57be3416e166fd06718a31af45a2f8e987e301be59ae6 673e963001dbbda80df47014a21a26d6c7eb4ebe0312aa6ffffb8d1b2 6bc62ca40ed51f8057a635a02c2b8c83f48fa6a2d70f58a1185902c0
0:	0c709c96 07dbb01c 94513358 745b7c23 953d03b3 3e39c723 4e268d1d 6e24f340 14ccbc22 16b965dd 231d5327 e591dc3c 0e8844cc fd568848
I:	b6d8da654b13c3101d6634a231569e6b85961c3f4b460a08ac4a5857 069576b64428676584baa45b97701be6d0b0ba18ac28d443403b4569 9ea0fbd1164f5893d39ad8f29e48e399aec5902508ea95e33bc1e9e4 620489d684eb5c26bc1ad1e09aba61fabcc2cdfee0b6b6862ffc8e55a
0:	76ab794e 28ff1224 c727fa10 16bf7f1d 329260b7 218a39ae a2fdb17d 8bd91190 17b093d6 41cedf74 328c3271 84dc6f2a 64bd90ed dccfcdab
I:	36a69976c3e5d74e4904776993cbac27d10f25f5626dd45c51d15dcf 7b3e6a5446a6649ec912a56895d6baa9dc395ce9e34b868d9fb2c1fc 72eb6495702ea4f446c9b7a188a4e0826b1506b0747a6709f37988ff

1aeb5e3788d5076ccbb01a4bc6623c92ff147a1e21b29cc3fdd0e0f4
0: c8d7ac38 4143500e 50890a1c 25d64334 3accce58 4caf2544 f9249b2b
f4a69210 82be0e7f 3669bb5e c24535e6 c45621e1 f6dec676 edd8b664

I: d5938acbbba432ecd5617c555a6a777734494f176259bff9dab844c81
aadcf8f7abd1a9001d89c7008c1957272c1786a4293bb0ee7cb37cf3
988e2513b14e1b75249a5343643d3c5e5545a0c1a2a4d3c685927c38
bc5e5879d68745464e2589e000b31301f1dfb7471a4f1300d6fd0f99
0: 62beffc6 b8ee11cc d79dbaac 8f0252c7 50eb052b 192f41ee ecb12f29
79713b56 3caf7d22 588eca5e 80995241 ef963e7a d7cb7962 f343a973

I: 4dec58199a35f531a5f0a9f71a53376d7b4bdd6bbd2904234a8ea65b
bacbce2a542291378157a8f4be7b6a092672a34d85e473b26ccfbd4c
dc6739783dc3f4f6ee3537b7aed81df898c7ea0ae89a15b5559596c2
a5eeacf8b2b362f3db2940e3798b63203cae77c4683ebaed71533e51
0: f4ccb31d 263731ab 88bed634 304956d2 603174c6 6da38742 053fa37d
d902346c 3862155d 68db63be 87439e3d 68758ad7 268e239d 39c4fd3b

I: df2aa1536abb4acab26efa538ce07fd7bca921b13e17bc5ebcba7d1b
6b733deda1d04c220f6b5ab35c61b6bcb15808251cab909a01465b8a
e3fc770850c66246d5a9eae9e2877e0826e2b8dc1bc08009590bc677
8a84e919fbd28e02a0f9c49b48dc689eb5d5d922dc01469968ee81b5
0: 7e79b00e 8e0a76a6 7c0040f6 2713b8b8 c6d6f05e 9c6d0259 2e8a22ea
896f5dea cc7c7df5 ed42beae 6fedb900 0285b482 aa504e27 9fd49c32

I: e9fb440282e07145f1f7f5ecf3c273212cd3d26b836b41b02f108431
488e5e84bd15f2418b3d92a3380dd66a374645c2a995976a015632d3
6a6c2189f202fc766e1c82f50ad9189be190a1f0e8f9b9e69c9c18cc
98fdd885608f68bf0fdded7b894081a63f70016a8abf04953affbfa
0: 20b171cb 16be977f 15e013b9 752cf86c 54c631c4 fc8cbf7c 03c4d3ac
9b8e8640 e7b0e930 0b987fe0 ab504466 9314f6ed 1650ae03 7db853f1

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