MASSACHVSETTS INSTITVTE OF TECHNOLOGY Department of Electrical Engineering and Computer Science 6.001—Structure and Interpretation of Computer Programs Fall 2007

Recitation 11 Solutions Tagged Data: Symbolic Manipulation

```
Tagging procedure:
(define (tagged-list? x tag)
  (and (pair? x) (eq? (car x) tag)))
A tagged abstraction for variables:
(define *variable-tag* 'variable)
(define (make-variable vname)
  (list *variable-tag* vname))
(define (variable? x)
  (tagged-list? x *variable-tag*))
(define (varname var)
  (if (variable? var)
      (cadr var)
      (error "not a variable: " var)))
(define (variable=? v1 v2)
  (eq? (varname v1) (varname v2)))
Tagged abstraction for constants:
(define *constant-tag* 'constant)
(define (make-constant c)
  (list *constant-tag* c))
(define (constant? c)
  (tagged-list? c *constant-tag*))
(define (constval c)
  (if (constant? c)
      (cadr c)
```

(error "not a constant: " c)))

Tagged abstraction for polynomials:

```
(define *poly-tag* 'poly)

(define (make-poly var terms)
   (list *poly-tag* var terms))

(define (poly? x)
    (tagged-list? x *poly-tag*))

(define (poly-get-var poly)
    (if (poly? poly)
        (cadr poly)
        (error "not a polynomial:" poly)))

(define (poly-get-terms poly)
   (caddr poly))
```

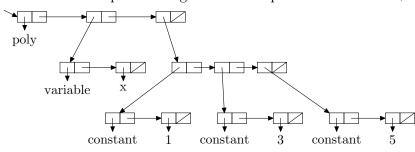
Problems

2. Write constant-add:

```
(define (constant-add c1 c2)
  (make-constant (+ (constval c1) (constval v2))))
```

3. Write a basic add, which works only on two constants or two polynomials, assuming you have a procedure poly-add which adds two polynomials:

4. Draw a box-and-pointer diagram of the representation of $5x^2 + 3x + 1$.



5. To actually build poly-add, which adds two polynomials:

(a) First write add-terms, which takes two lists of terms and returns a new list of sum terms:

(b) Then write poly-add using add-terms:

6. What happens (with add defined as above), if you try to evaluate the following sequence of expressions:

```
(define x (make-variable 'x))
(define 5x+1 (make-poly x (list (make-constant 1) (make-constant 5))))
(define five (make-constant 5))
(add 5x+1 5x+1)
(add five five)

(add 5x+1 five)
(add x 5x+1)
```

What goes wrong?

All of the add operations only deal with pairs of identical types: two constants or two polynomials. Expressions of mixed types aren't handled

7. Give the following procedures, var->poly and const->poly, which promote variables and constants to polynomials, write a general ->poly which promotes any of the three types to a polynomial.

8. Write a new version of add which uses promotion. Use the following procedure to guess what variable to use when promoting:

```
(define (find-var e1 e2)
  (cond ((poly? e1)
         (poly-get-var e1))
        ((poly? e2)
         (poly-get-var e2))
        ((variable? e1)
         e1)
        ((variable? e2)
         e2)
        (else
         (make-variable 'x))))
(define (add e1 e2)
  (if (and (constant? e1)
           (constant? e2))
      (constant-add e1 e2)
      (let ((var (find-var e1 e2)))
        (poly-add (->poly var e1)
                  (->poly var e2)))))
```