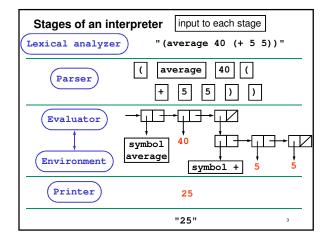
6.001 SICP Interpretation

- · Parts of an interpreter
- · Arithmetic calculator
- Names
- · Conditionals and if
- Storing procedures in the environment
- · Environment as explicit parameter
- Defining new procedures

Why do we need an interpreter?

- Abstractions let us bury details and focus on use of modules to solve large systems
- We need a process to unwind abstractions at execution time to deduce meaning
- We have already seen such a process the Environment Model
- · Now want to describe that process as a procedure

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Role of each part of the interpreter

- · Lexical analyzer
 - break up input string into "words" called tokens
- Parse
 - convert linear sequence of tokens to a tree
 - like diagramming sentences in elementary school
 - also convert self-evaluating tokens to their internal values
 - -e.g., #f is converted to the internal false value
- Evaluator
 - follow language rules to convert parse tree to a value
 - read and modify the environment as needed
- Printer
 - · convert value to human-readable output string

Goal of today's lecture

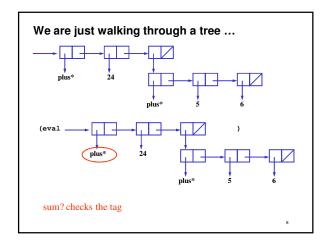
- Implement an interpreter
- · Only write evaluator and environment
 - Use Scheme's reader for lexical analysis and parsing
 - Use Scheme's printer for output
 - To do this, our language must resemble Scheme
- Call the language scheme*
 - All names end with a star to distinguish from Scheme names
- Start with interpreter for simple arithmetic expressions
 - · Progressively add more features

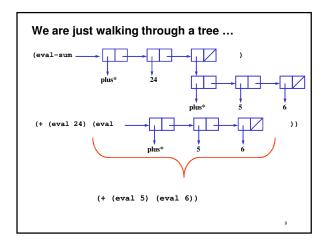
1. Arithmetic calculator

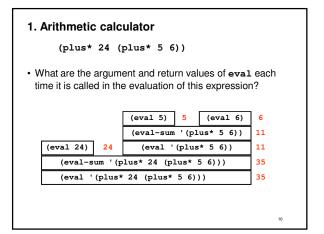
Want to evaluate arithmetic expressions of two arguments, like:

(plus* 24 (plus* 5 6))

1. Arithmetic calculator (define (tag-check e sym) (and (pair? e) (eq? (car e) sym))) (define (sum? e) (tag-check e 'plus*)) (define (eval exp) ((ound ((number? exp) exp) ((sum? exp) (eval-sum exp)) (else (error "unknown expression " exp)))) (define (eval-sum exp) (+ (eval (cadr exp)) (eval (caddr exp)))) (eval '(plus* 24 (plus* 5 6)))







1. Things to observe

- cond determines the expression type
- · No work to do on numbers
 - Scheme's reader has already done the work
 - It converts a sequence of characters like "24" to an internal binary representation of the number 24
- eval-sum recursively calls eval on both argument expressions

Store bindings between names and values in a table

• Extend the calculator to store intermediate results as

(define* x* (plus* 4 5))

2. Names

named values

(plus* x* 2)

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store result as x*

use that result

```
2. Names
 (define (define? exp) (tag-check exp 'define*))
 (define (eval exp)
   (cond
    ((number? exp) exp)
    ((sumper: exp) exp)
((sumper: exp) (eval-sum exp))
((symbol? exp) (lookup exp))
((define? exp) (eval-define exp))
     (error "unknown expression " exp))))
; table ADT from prior lecture:
                         void -> table
table, symbol -> (binding | null)
   make-table
  table-get
  table-put!
                         table, symbol, anytype -> undef
                     binding -> anytype
; binding-value
 (define environment (make-table))
                                                                       13
```

```
2. Names ...
(define (lookup name)
   (let ((binding (table-get environment name)))
    (if (null? binding)
        (error "unbound variable: " name)
        (binding-value binding))))
(define (eval-define exp)
        (let ((name (cadr exp)))
        (defined-to-be (caddr exp)))
        (table-put! environment name (eval defined-to-be))
        'undefined))

(eval '(define* x* (plus* 4 5)))
(eval '(plus* x* 2))
How many times is eval called in these two evaluations?
```

Evaluation of page 2 lines 36 and 37

- · Show argument and return values of eval for each call
- Show the environment each time it changes

2. Things to observe

- Use scheme function symbol? to check for a name
 - the reader converts sequences of characters like "x*" to symbols in the parse tree
- Can use any implementation of the table ADT
- eval-define recursively calls eval on the second subtree but not on the first one
- eval-define returns a special undefined value

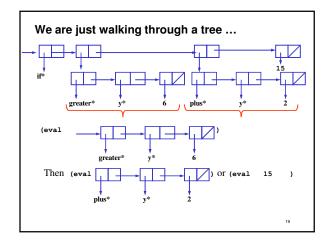
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3. Conditionals and if

Extend the calculator to handle predicates and if:
 (if* (greater* y* 6) (plus* y* 2) 15)

• What are the argument and return values of eval each time it is called in the expression above?

```
(define (greater? exp) (tag-check exp 'greater*))
(define (if? exp) (tag-check exp 'if*))
(define (eval exp)
                                             3. Conditionals and If
  (cond ...
    ((greater? exp) (eval-greater exp))
    ((if? exp) (eval-if exp))
(else (error "unknown expression " exp))))
(define (eval-greater exp)
   (> (eval (cadr exp)) (eval (caddr exp))))
(define (eval-if exp)
  (let ((predicate (cadr exp))
(consequent (caddr exp))
(alternative (caddr exp)))
                                                        Note: if* is stricter
                                                         than Scheme's if
     (let ((test (eval predicate)))
        (cond
         ((eq? test #t) (eval consequent))
((eq? test #f) (eval alternative))
         (else
                               (error "predicate not boolean: "
                                       predicate))))))
(eval '(define* y* 9))
(eval '(if* (greater* y* 6) (plus* y* 2) 15))
```



```
Evaluation of page 3 line 32
(eval '(if* (greater* y* 6) (plus* y* 2) 15))
  (eval '(greater* y* 6))
    (eval 'y*) ==> 9
    (eval 6) ==> 6
    ==> #t
  (eval '(plus* y* 2))
    (eval 'y*) ==> 9
    (eval 2) ==> 2
    ==> 11
==> 11
```

3. Things to observe

- eval-greater is just like eval-sum from page 1
 - recursively call eval on both argument expressions
 - call Scheme > to compute value
- eval-if does not call eval on all argument expressions:
 - call eval on the predicate
 - call eval either on the consequent or on the alternative but not both
 - this is the mechanism that makes if*

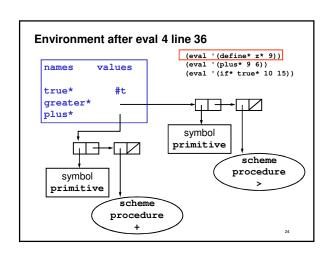
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4. Store operators in the environment

- Want to add lots of operators but keep eval short
- Operations like plus* and greater* are similar
 - evaluate all the argument subexpressions
 - perform the operation on the resulting values
- Call this standard pattern an application
 - Implement a single case in eval for all applications
- Approach:
 - eval the first subexpression of an application
 - put a name in the environment for each operation
 - value of that name is a procedure
 - apply the procedure to the operands

```
(define (application? e) (pair? e))

(define (eval exp)
(cond
((number? exp) exp)
((sokup exp))
((define fexp) (eval-define exp))
((if? exp)
((application? exp) (eval-define exp))
((ief) exp)
((application? exp) (eval-define exp))
((application? exp) (epply (eval (car exp)))
((else
(error "unknown expression" exp))))
(define scheme-apply apply);; rename scheme's apply so we can reuse the name
(define (apply operator operands)
(if (primitive? operator)
(scheme-apply (get-scheme-procedure operator) operands)
(error "operator not a procedure: "operator)))
;; primitive: an ADT that stores scheme procedures
(define prim-tag 'primitive)
(define (application explication explin
```



```
Evaluation of eval 4 line 38

(eval '(if* true* 10 15))
  (eval-if '(if* true* 10 15))
  (let ((test (eval 'true*))) (cond ...))
  (let ((test (lookup 'true*))) (cond ...))
  (let ((test #t)) (cond ...))
  (eval 10)
  10

Apply is never called!
```

4. Things to observe

- applications must be the last case in eval
 - · no tag check
- apply is never called in line 38
 - · applications evaluate all subexpressions
 - expressions that need special handling, like if*, gets their own case in eval

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```
5. Environment as explicit parameter
```

· Change from

```
(eval '(plus* 6 4))
to
     (eval '(plus* 6 4) environment)
```

- All procedures that call ${\tt eval}$ now have extra argument
- \bullet ${\tt lookup}$ and ${\tt define}$ use environment from argument
- No other change from evaluator 4
- Only nontrivial code: case for application? in eval

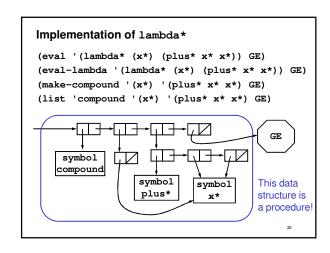
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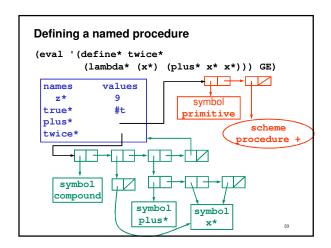
6. Defining new procedures

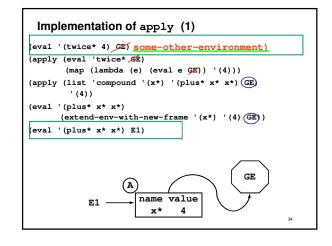
- · Want to add new procedures
- For example, a scheme* procedure:

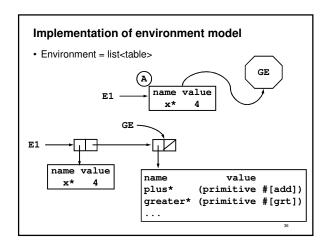
```
(define* twice* (lambda* (x*) (plus* x* x*)))
(twice* 4)
```

- · Strategy:
 - Add a case for lambda* to eval
 - -the value of lambda* is a compound procedure
 - Extend apply to handle compound procedures
 - · Implement environment model









```
; Environment model code (part of eval 6)

; Environment = list ctable>
(define (extend-env-with-nev-frame names values env)
(latt ((new-frame (make-table)))
(come new-frame env) values new-frame)
(define (make-bindings' names values table)
(come new-frame env) (table-put' table name value))
names values))

the initial global environment
(define GE
(lambda (name value) (table-put' table name value))
names values));

; lookup searches the list of frames for the first match
(define (Lookup name env)
(int (make-primitive +) (make-primitive >))
name)
(int (binding (table-get (car env) name)))
(if (mill') binding)
(if (mill') binding)
(if (mill') binding))
(if (mill') binding))
; define changes the first frame in the environment
(define (eval-define eng env)
(itt (linding-value binding))))
(table-put-define eng env)
(itable-put-define eng env)
(itable-put-define eng env)
(undefined))
(carl (defined-to-be (cadde exp)))
(table-put-(car env) name (eval defined-to-be env))
'undefined))
(carl (defined-to-be (lambde* (x*) (plue* x* x*))) GE)
```

Summary

- · Cycle between eval and apply is the core of the evaluator
 - eval calls apply with operator and argument values
 - · apply calls eval with expression and environment
 - no pending operations on either call
 - an iterative algorithm if the expression is iterative
- What is still missing from scheme*?
 - · ability to evaluate a sequence of expressions
 - data types other than numbers and booleans

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Cute Punchline

- Everything in these lectures would still work if you deleted the stars from the names.
- We just wrote (most of) a Scheme interpreter in Scheme.
- · Seriously nerdly, eh?
 - · The language makes things explicit
 - e.g., procedures and procedure app in environment
 - · More generally
 - Writing a precise definition for what the Scheme language means
 - Describing computation in a computer language forces precision and completeness
 - Sets the foundation for exploring variants of Scheme