6.001 SICP Further Variations on a Scheme

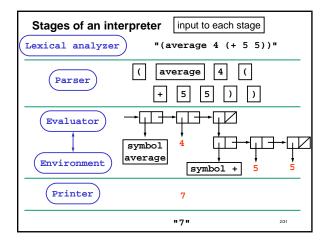
Beyond Scheme - more language variants

Lazy evaluation

- Complete conversion normal order evaluator
- Upward compatible extension lazy, lazy-memo

Punchline: Small edits to the interpreter give us a *new* programming language

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Evaluation model

Rules of evaluation:

- If expression is <u>self-evaluating</u> (e.g. a number), just return value
- If expression is a <u>name</u>, look up value associated with that name in environment
- If expression is a *lambda*, create procedure and return
- If expression is <u>special form</u> (e.g. if) follow specific rules for evaluating subexpressions
- If expression is a *compound expression*
 - Evaluate subexpressions in any order
 - If first subexpression is primitive (or built-in) procedure, just apply it to values of other subexpressions
 - If first subexpression is compound procedure (created by lambda), evaluate the body of the procedure in a new environment, which extends the environment of the procedure with a new frame in which the procedure's parameters are bound to the supplied arguments

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Alternative models for computation

- Applicative Order (aka Eager evaluation):
 - · evaluate all arguments, then apply operator
- Normal Order (aka Lazy evaluation):
 - go ahead and apply operator with unevaluated argument subexpressions
 - evaluate a subexpression only when value is needed
 to print
 - by primitive procedure (that is, primitive procedures are "strict" in their arguments)

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Applicative Order Example

```
Normal Order Example
(define (foo x)
  (write-line "inside foo")
  (+ \times \times)
(foo (begin (write-line "eval arg") 222))
 => (begin (write-line "inside foo")
                                                         From body
              (+ (begin (w-l "eval arg") 222)
(begin (w-l "eval arg") 222)))
                                                         of foo
                               As if we substituted the
inside foo
                            unevaluated expression in the
eval arg
                                body of the procedure
eval arg
 => 444
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```

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Applicative Order vs. Normal Order (write-line "inside foo") (+ x x)) (foo (begin (write-line "eval arg") 222)) Applicative order Normal order inside foo inside foo eval arg Think of as substituting eval arg values for variables in Think of as expanding expressions expressions until only involve primitive operations and data structures 7/31

```
Normal order (lazy evaluation) versus applicative order

How can we change our evaluator to use normal order?

Create "delayed objects" – expressions whose evaluation has been deferred

Change the evaluator to force evaluation only when needed

Why is normal order useful?

What kinds of computations does it make easier?
```

```
Mapply – the original version
(define (mapply procedure arguments)
 (cond ((primitive-procedure? procedure)
        (apply-primitive-procedure
           procedure
           arguments) Actual values
     ((compound-procedure? procedure)
      (eval-sequence
       (procedure-body procedure)
       (extend-environment
           (procedure-parameters procedure)
                          Actual valu
           arguments +
           (procedure-environment procedure))))
     (else (error "Unknown procedure" procedure))))
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```

```
How can we implement lazy evaluation?
  (define (1-apply procedure arguments env)
                                               ; changed
    (cond ((primitive-procedure? procedure)
            (apply-primitive-procedure
                                             Delayed
              procedure
                                             expression
Need to convert
               (list-of-arg-values arg
                                            s env)))
to actual values ((compound-procedure? procedure)
           (1-eval-sequence
              (procedure-body procedure)
                                              Delayed
Need to create
                                              Expressions
              extend-environment
delayed version
               (procedure-parameters procedure)
of arguments
               list-of-delayed-args argu
that will lead to
               (procedure-environment procedure))))
values
           (else (error "Unknown proc" procedure))))
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```


Representing Thunks • Abstractly – a thunk is a "promise" to return a value when later needed ("forced") • Concretely – our representation: thunk exp env

Memo-izing evaluation

- In lazy evaluation, if we reuse an argument, have to reevaluate each time
- In usual (applicative) evaluation, argument is evaluated once, and just referenced
- Can we keep track of values once we've obtained them, and avoid cost of reevaluation?

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Sidebar on memoization

- Idea of memoization is for a procedure to remember if it has been called with a particular argument(s) and if so to simply return the saved value
- Can have problems if mutation is allowed works best for functional programming

```
Sidebar on memoization
                                                         (define (square x) (* x x))
(define (memoize proc)
 (let ((history `()))
                                                         (define foo (memoize square))
    (lambda (arg)
      (let ((already-there (in-history? arg history))) Store pairings of
        (if already-there
                                                                 argument values and associated procedure
             (value already-there)
                                                                 values in history, e.g.
             (let ((return (proc arg)))
               (set! history
                      (insert-history return history))
                return))))))
  foo:
                             square:
                 proc:
                  history: '()
                                                       Calling foo will create a frame here which gives
```

Memo-izing Thunks • Idea: once thunk exp has been evaluated, remember it • If value is needed again, just return it rather than recompute W Concretely – mutate a thunk exp env thunk into an evaluated-thunk Why mutuate? evaluated because other result thunk

```
Thunks - Memoizing Implementation

(define (evaluated-thunk? obj)
```

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Lazy Evaluation - other changes needed

names or data structures may point to this thunk!

• Example – need actual predicate value in conditional if... (define (1-eval-if exp env)

```
(if (true? (actual-value (if-predicate exp) env))
  (1-eval (if-consequent exp) env)
  (1-eval (if-alternative exp) env)))
```

• Example – don't need actual value in assignment... (define (1-eval-assignment exp env)

(set-variable-value!
 (assignment-variable exp)
 (1-eval (assignment-value exp) env)
env)
'ok)

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Summary of lazy evaluation

- This completes changes to evaluator
 - Apply takes a set of expressions for arguments and an environment
 - Forces evaluation of arguments for primitive procedure application
 - Else defers evaluation and unwinds computation further
 - Need to pass in environment since don't know when it will be needed
 - Need to force evaluation on branching operations (e.g. if)
 - Otherwise small number of changes make big change in behavior of language

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Laziness and Language Design

- We have a dilemma with lazy evaluation
 - Advantage: only do work when value actually needed
 - Disadvantages
 - not sure when expression will be evaluated; can be very big issue in a language with side effects
 - -may evaluate same expression more than once
- Memoization doesn't fully resolve our dilemma
 - Advantage: Evaluate expression at most once
 - Disadvantage: What if we want evaluation on each use?
- Alternative approach: give programmer control!

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Variable Declarations: lazy and lazy-memo

 Handle lazy and lazy-memo extensions in an upwardcompatible fashion.;

(lambda (a (b lazy) c (d lazy-memo)) ...)

- "a", "c" are usual variables (evaluated before procedure application)
- "b" is lazy; it gets (re)-evaluated each time its value is actually needed
- "d" is lazy-memo; it gets evaluated the first time its value is needed, and then that value is returned again any other time it is needed again.

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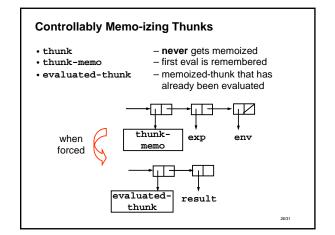
```
Syntax Extensions - Parameter Declarations

(define (first-variable var-decls) (car var-decls))
(define (rest-variables var-decls) (cdr var-decls))
(define declaration? pair?)

(define (parameter-name var-decl)
   (if (pair? var-decl) (car var-decl) var-decl))

(define (lazy? var-decl)
   (and (pair? var-decl) (eq? 'lazy (cadr var-decl))))

(define (memo? var-decl)
   (and (pair? var-decl)
   (eq? 'lazy-memo (cadr var-decl))))
```



A new version of delay-it

• Look at the variable declaration to do the right thing...

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Change to force-it

Changes to I-apply

- Key: in I-apply, only delay "lazy" or "lazy-memo" params
 - make thunks for "lazy" parameters
 - make memoized-thunks for "lazy-memo" parameters

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Deciding when to evaluate an argument...

 Process each variable declaration together with application subexpressions – delay as necessary:

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Summary

- Lazy evaluation control over evaluation models
 - Convert entire language to normal order
 - Upward compatible extension
 - lazy & lazy-memo parameter declarations
- We have created <u>a new language</u> (with <u>new syntax</u>), using only relatively small changes to the interpreter.

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