

# Neural-network accelerated core-pedestal coupled simulations, and applications to ITER

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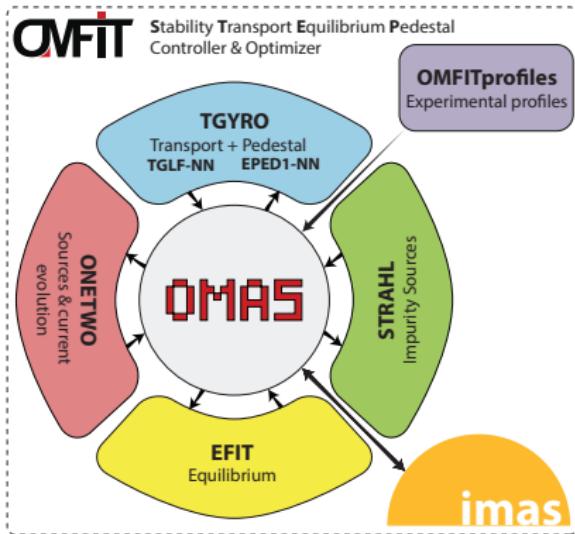
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Transport Task Force

March 18-21, 2019

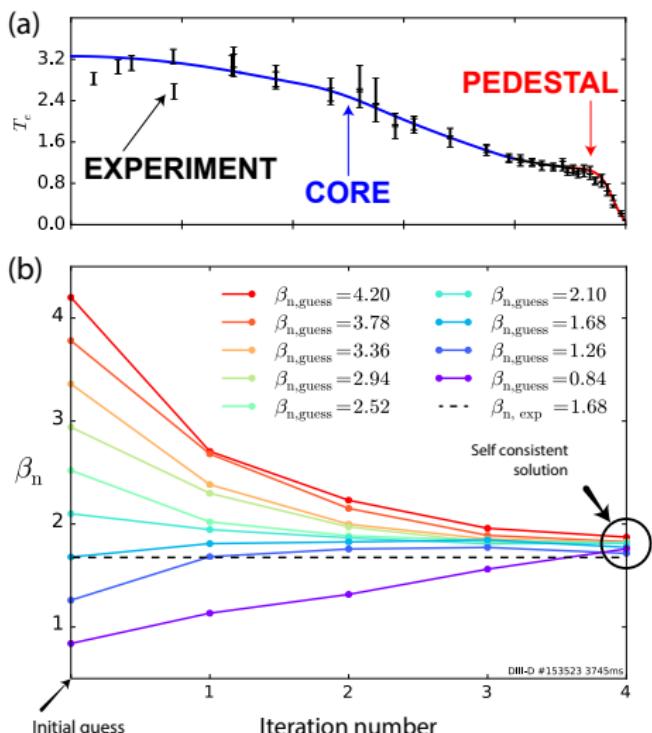


# Past core-pedestal coupled simulations developed within OMFIT assumed impurity profile to be known

O. Meneghini et al. NF 2017:

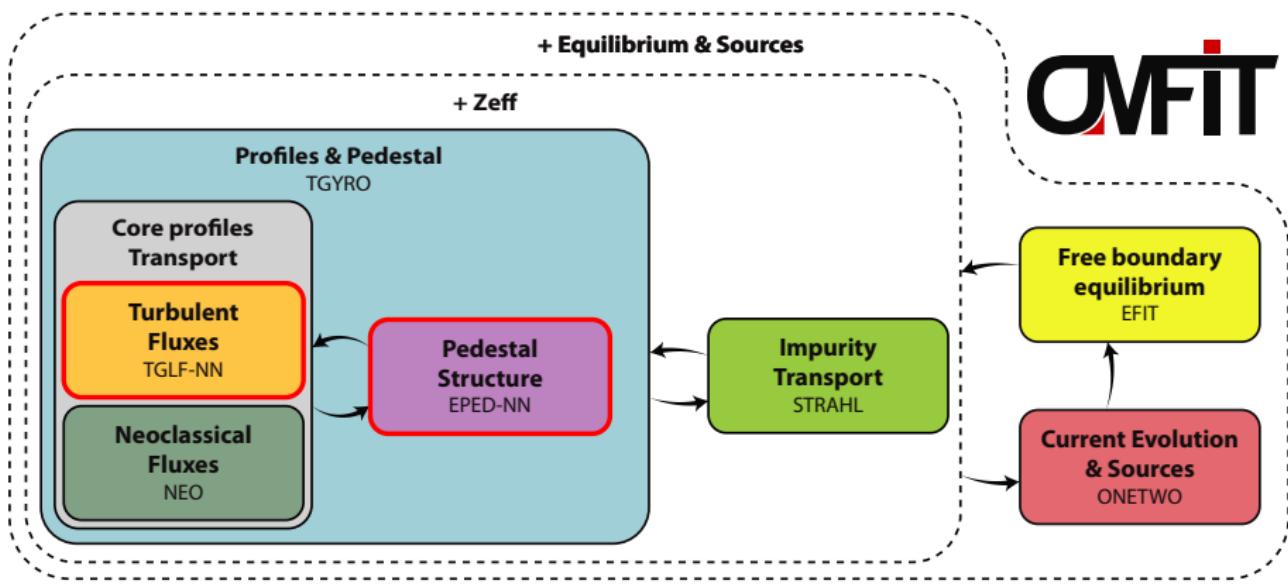
- Iterative workflow to couple core-pedestal solutions
- Speedup process by millions with neural networks
- Robustly finds self-consistent solution without pedestal height/width as free parameters
- ...**BUT**:  $Z_{eff}$  profile was assumed to be known

In this work, we lift this assumption, and **allow for self-consistent transport of impurities**



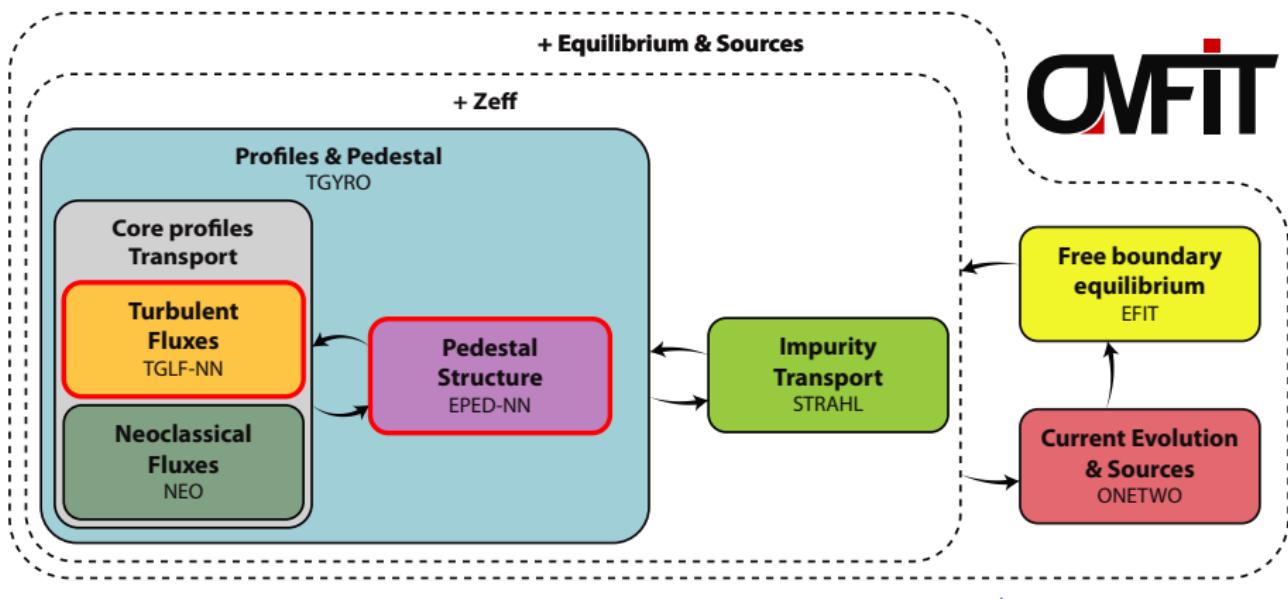
# Developed workflow for coupled core-pedestal simulations with self-consistent transport of impurities

- Three nested self-consistency loops
  - core profiles + pedestal + impurities + equilibrium & sources
- Used NN models to speedup the most critical bottlenecks
- Compatible with ITER IMAS data structure (leveraging OMAS)



# Used neural network models EPED1-NN and TGLF-NN to speedup the most critical bottlenecks in the workflow

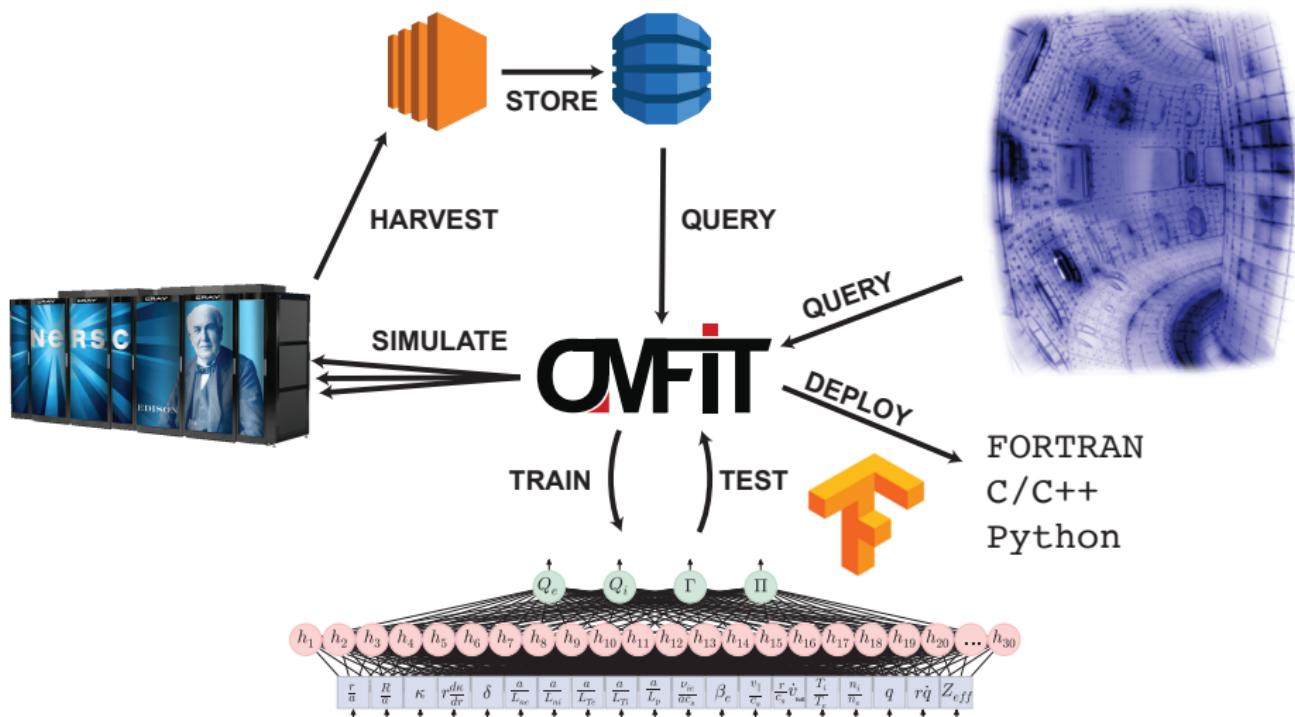
- EPED1 pedestal model  $\sim 20$  CPU/h  $\rightarrow$  EPED1-NN  $\sim$ ms
  - EPED1-NN pedestal coupling moved within core-profiles calculation
- TGLF transport model called  $1000 \times \sim 10$  CPU/s  $\rightarrow$  TGLF-NN  $\sim$ ms
  - TGLF-NN embedded as part of orginal TGLF code



# Neural-network accelerated core-pedestal coupled simulations, and applications to ITER

- 1 EPED-NN and TGLF-NN models**
- 2 STEP workflow for core-pedestal predictive simulations with transport of impurities**
- 3 Theory-based machine confinement scaling**
- 4 Conclusions**

# OMFIT provides a convenient environment to support machine learning applications



# OMFIT module ‘BRAINFUSE’ gathers data, trains, tests and deploys neural network for multiple applications

Three main domains:

## 1 Pedestal

- EPED1-NN
- RMPED-NN

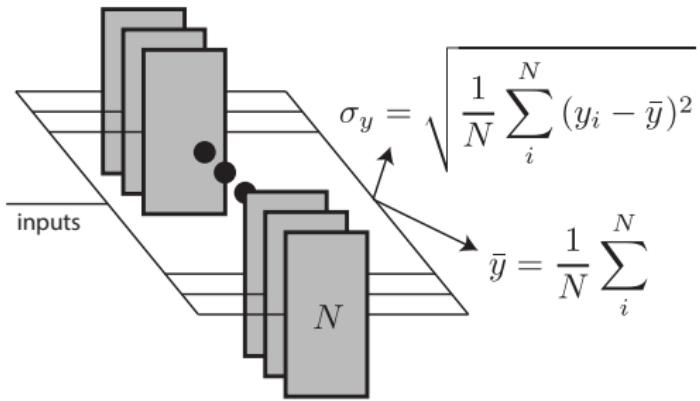
- Regularization to avoid over-training
- Ensemble of NNs used to estimate the error in NN models prediction
  - random NN initialization
  - each NN trained on a subset of the training DB ( $k$ -fold)

## 2 Transport fluxes

- TGLF-NN

## 3 Bootstrap current

- NEOjbs-NN



# EPED1-NN to predict pedestal structure for H and Super-H mode plasma regimes

Trained to reproduce results of **IPS-EPED1** model

**10** input parameters to predict **12** outputs:

- ① **normal H mode** solution
- ② **Super-H mode** solution

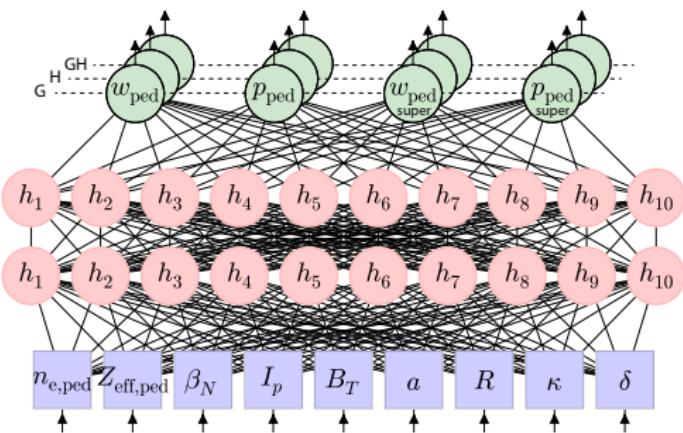
H and Super-H set to be equal  
when there is only one root

Extended NN model so that  
each root is evaluated for 3  
different diamagnetic  
stabilization models:

$$\mathbf{G} \quad \gamma/\omega_A > 0.03$$

$$\mathbf{H} \quad \gamma/(\omega^*/2) > 1$$

$$\mathbf{GH} \quad \gamma^2/(\omega_A\omega^*/2) > 0.03$$



# EPED1-NN model closely reproduces EPED1 predictions Trained across input parameter range of multiple devices

Built database of  
~20,000 EPED1 runs  
(2 million CPU hours)

**DIII-D:** 3,000 runs

**KSTAR:** 700 runs

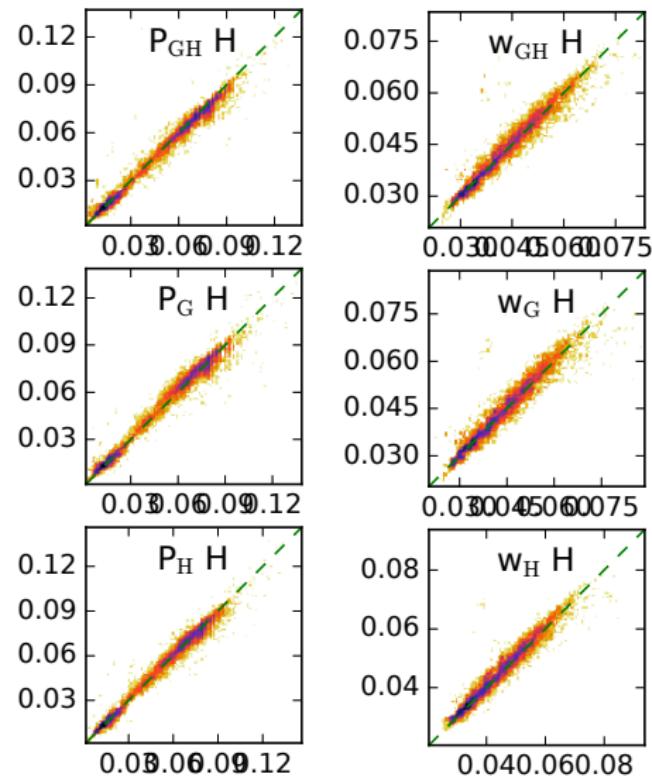
**JET:** 200 runs

**ITER:** 15,000 runs

**CFETR:** 1,200 runs

Same EPED1 runs  
reprocessed with  
different  
diamagnetic  
stabilization rules

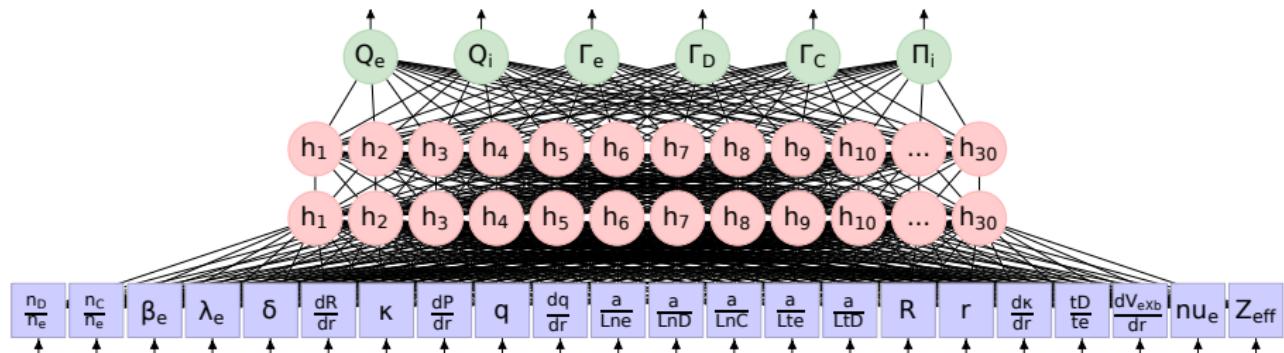
$\times 10^9$  speedup



# TGLF-NN predicts core turbulent fluxes

Trained to reproduce results of **TGLF** model

NOTE: TGLF is itself a reduced model of gyrokinetic simulations



For 2 ion species plasma (eg. Deuterium & Carbon for DIII-D):

- 23 dimensionless input parameters
- to predict 6 gyro-Bohm fluxes  $Q_e, Q_i, \Gamma_e, \Gamma_D, \Gamma_C, \Pi_i$

+2 inputs and +1 output for every additional ion species:

- 25 inputs, 7 outputs for DT, He4, Ne plasma (eg. ITER)

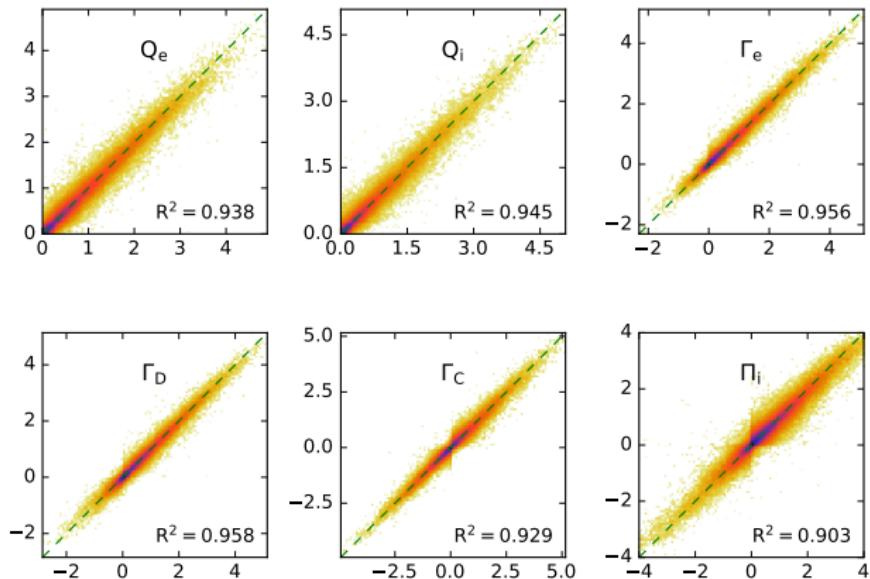
# TGLF-NN model closely reproduces TGLF predictions

Training data  
generated making  
random variations  
around points of  
interest

DIII-D: 1M runs

ITER: 500k runs

$\times 10^5$  speedup

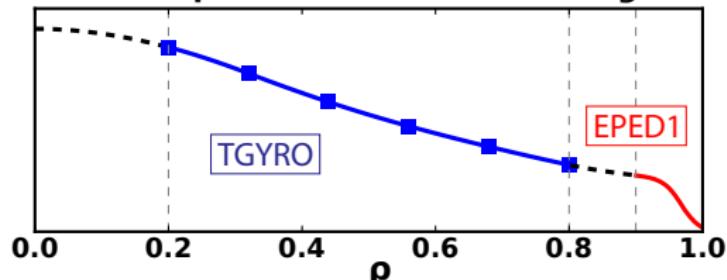


# Neural-network accelerated core-pedestal coupled simulations, and applications to ITER

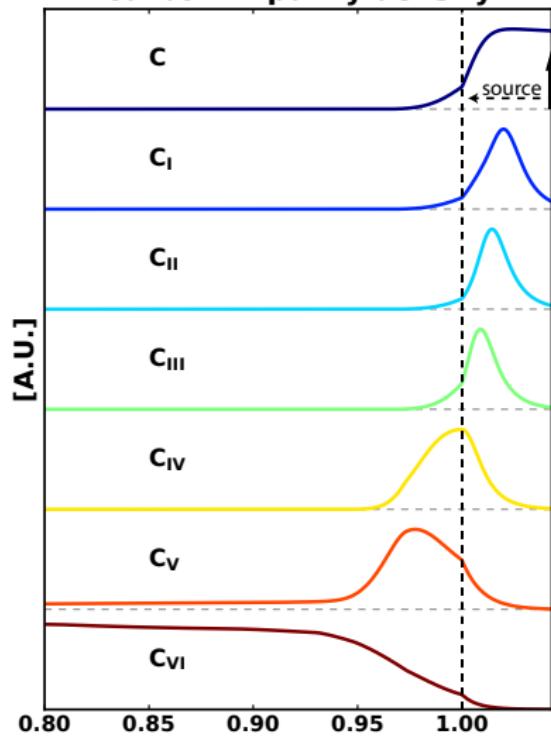
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# Self-consistent impurity transport done with STRAHL

Core-pedestal solution stitching



Carbon impurity density



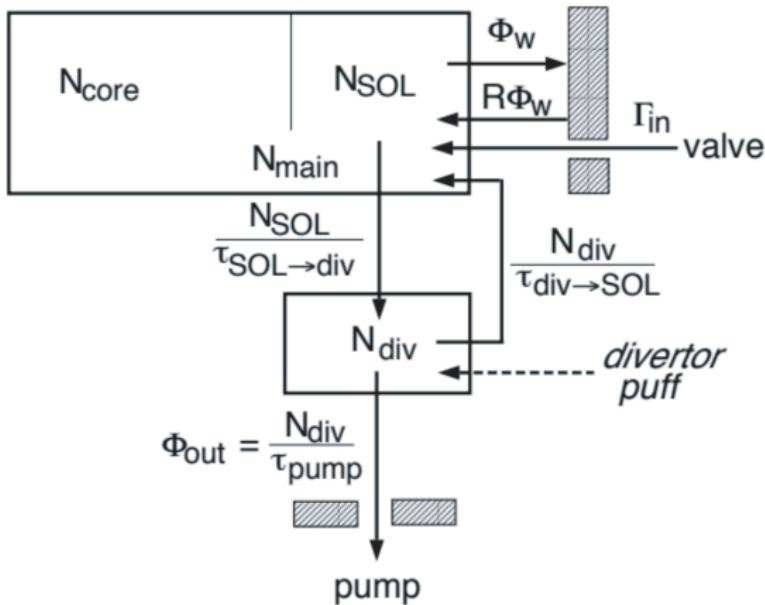
**STRAHL** is a 1D impurity transport code:

- IN** Influx of neutral species  
(rate and energy)
- IN** Transport coefficients
- IN** Background plasma density and temperature
- OUT** Profiles for each ionized state of the impurity

# For the purpose of core impurity transport we are not focusing on physics of the divertor chamber in STRAHL

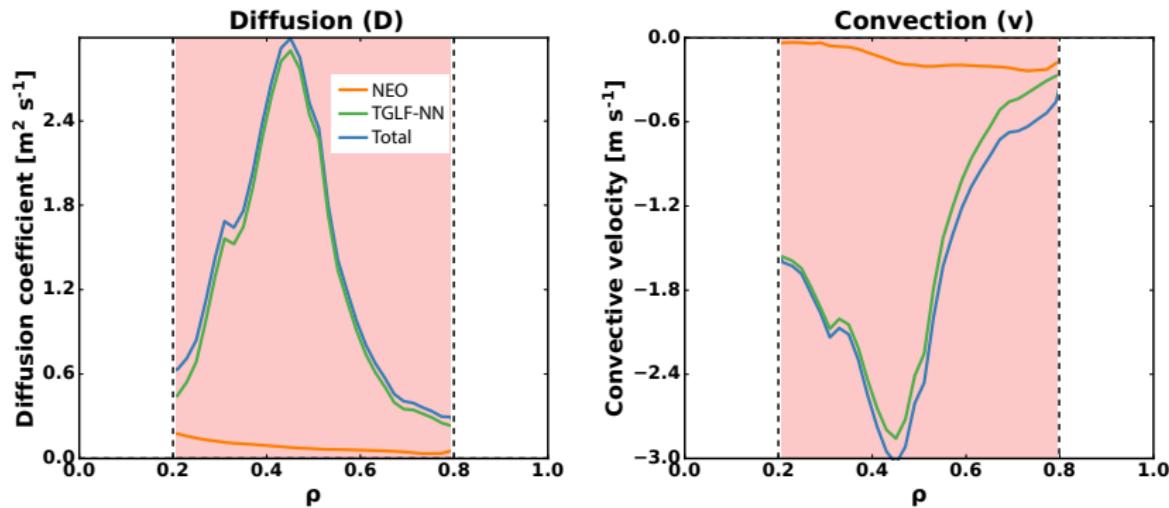
- Set artificially short SOL/divertor/pump confinement times for simulations to reach steady-state fast
- **Neutrals source scaled** to match  $Z_{eff}$  at one radial location, or total plasma impurity particle content
- **STRAHL uses a diffusive and convective transport ansatz:**

$$\Gamma_I = -D \frac{\partial n_I}{\partial r} + v n_I$$



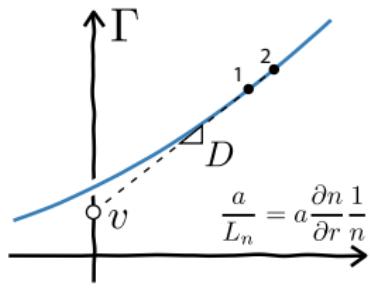
# Diffusion and convection coefficients for impurity transport

## CORE region:

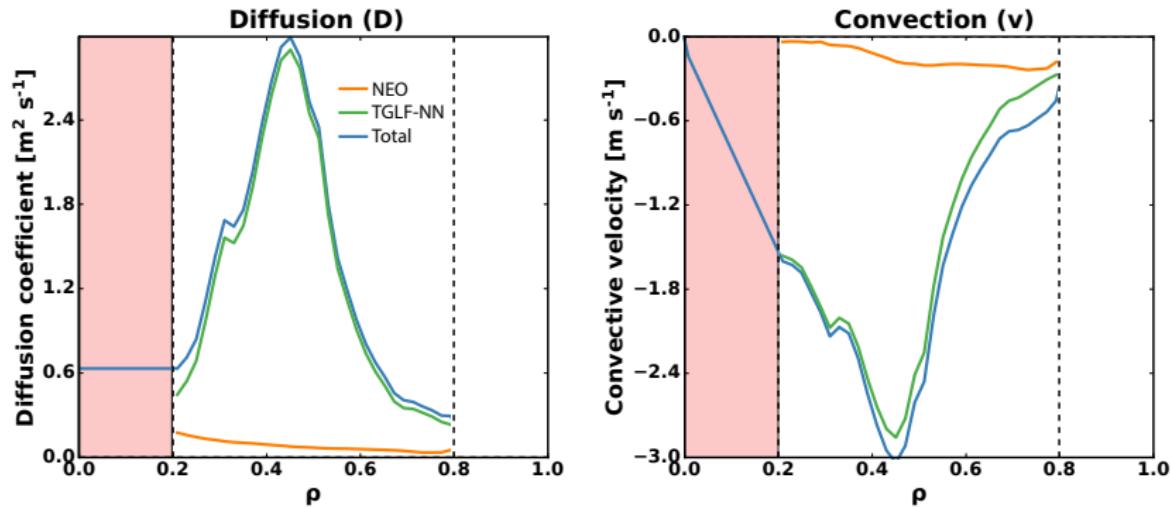


In the core  $D$  and  $v$  can be calculated from TGLF(-NN) and NEO fluxes:

$$D = \frac{\Gamma_1 n_2 - \Gamma_2 n_1}{n'_2 n_1 - n'_1 n_2} \quad v = \frac{\Gamma_1 n'_2 - \Gamma_2 n'_1}{n'_2 n_1 - n'_1 n_2}$$



# Diffusion and convection coefficients for impurity transport AXIS region:

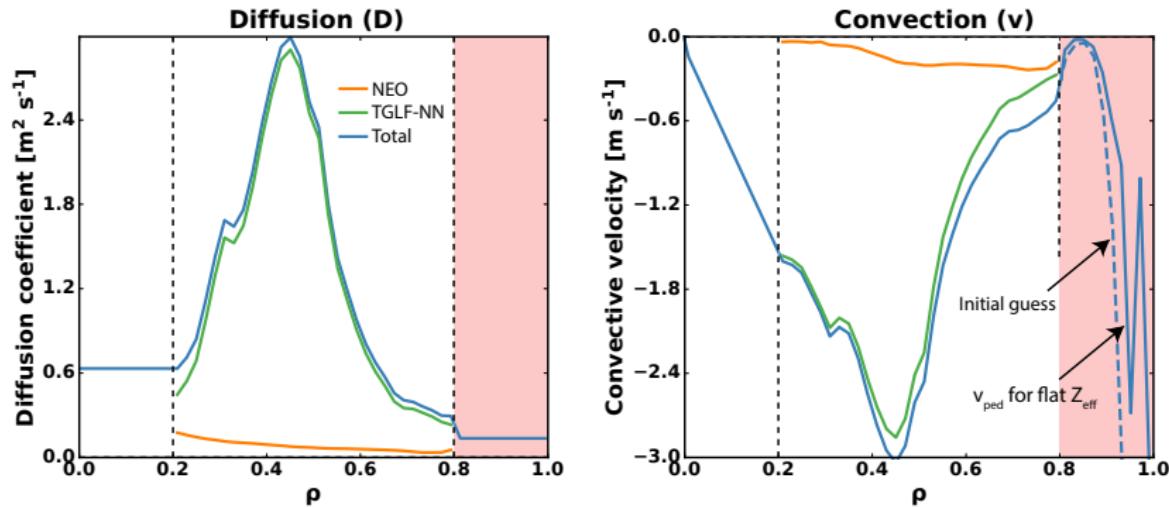


Near the axis impurity particle source is zero, thus in stationary regime:

$$\frac{\partial n_I}{\partial r} \frac{1}{n_I} = \frac{v}{D}$$

- Fix  $D_{axis} = D|_{\rho=0.2}$
- Set  $v_{axis}$  such that  $v_{axis}/D_{axis}$  linearly goes to zero at  $\rho = 0$

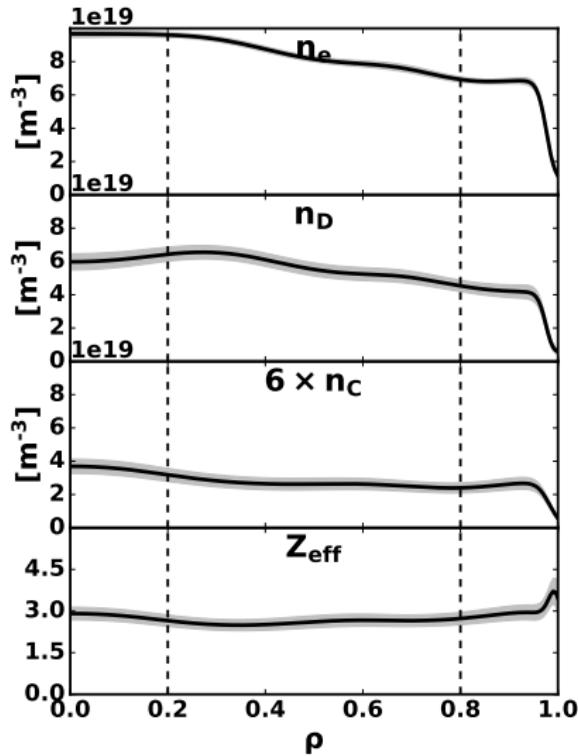
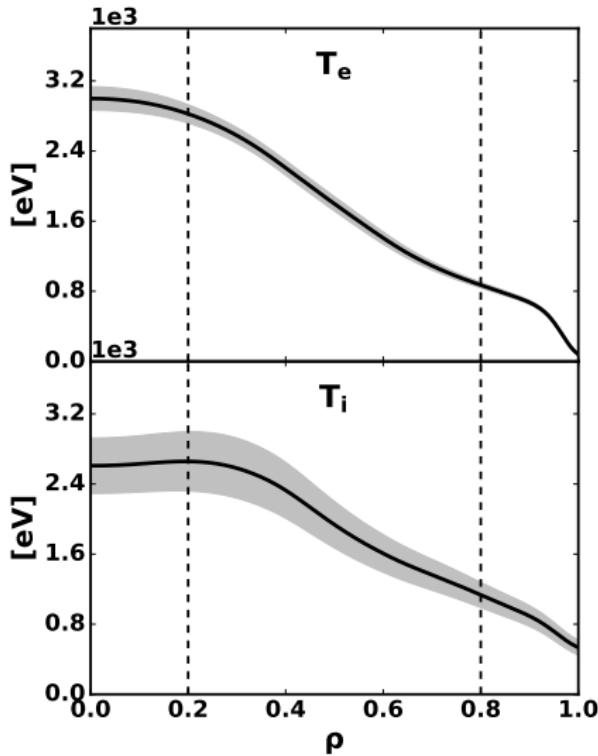
# Diffusion and convection coefficients for impurity transport PEDESTAL region:



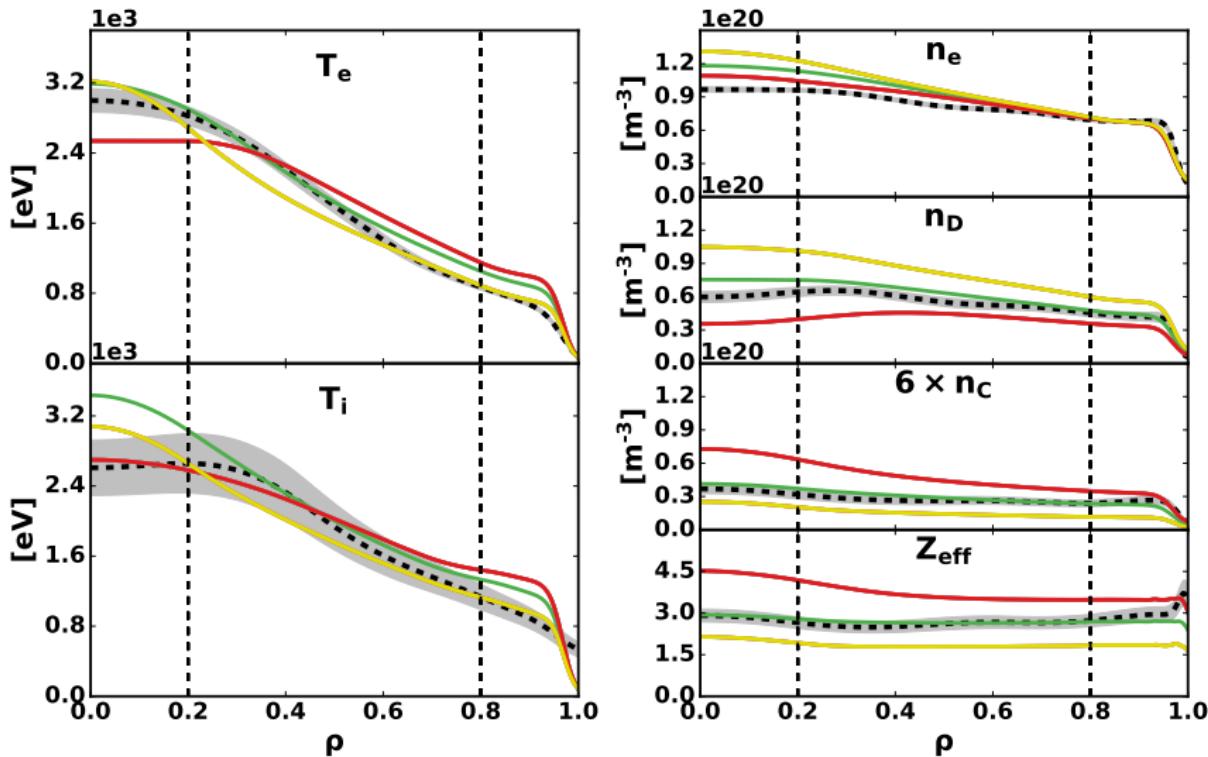
Alignment of impurity, main ion and electron density profiles  
(ie. flat  $Z_{eff}$ ) is a reasonable physical constraint for the pedestal region

- Fix  $D_{axis} = D|_{\rho=0.8}$
- Initial guess  $v_{ped} = \frac{\partial n_e}{\partial r} \frac{1}{n_e} D_{ped}$  (inexact because sources are not zero)
- Iteratively run STRAHL and find  $v_{ped}$  so that  $Z_{ped} = Z|_{\rho=0.8}$

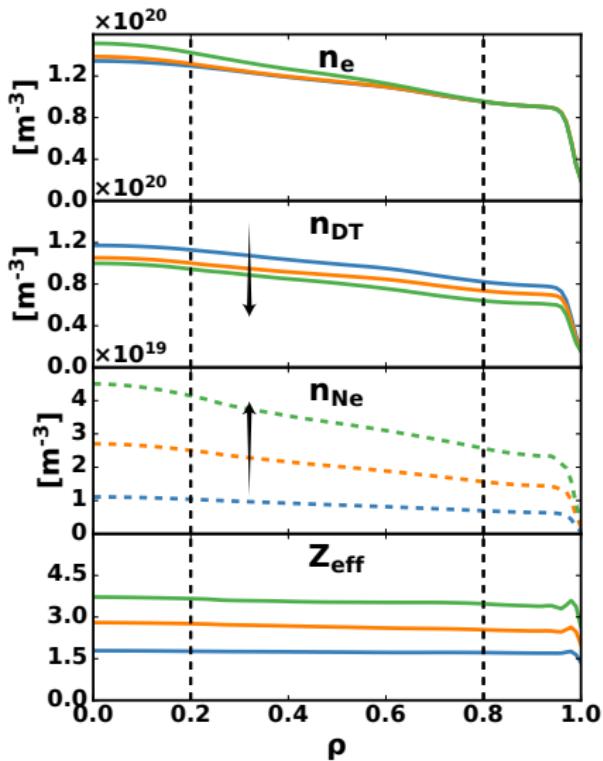
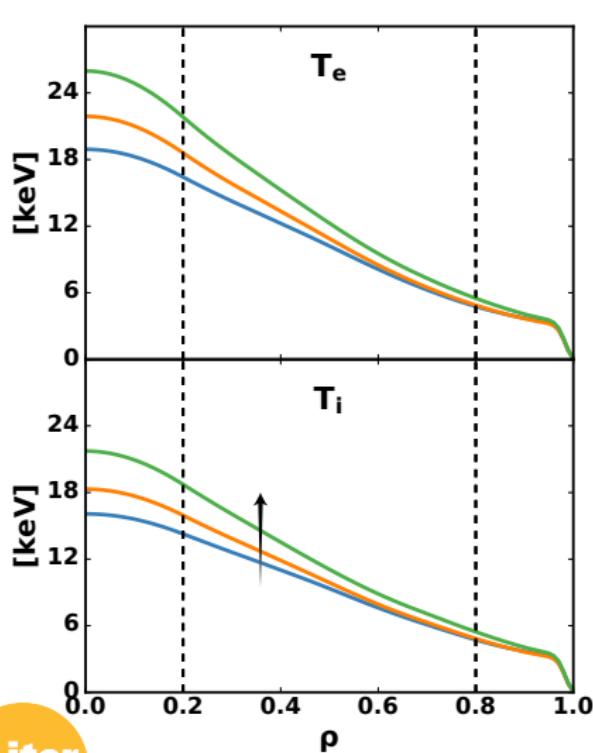
# Benchmark case: DIII-D H-mode discharge 168830



# Predictions for varying carbon content (0.5 , 1.0 , 1.5) shows how impurity seeding can improve pedestal



# Initial ITER simulations show small dependency of $Q$ on $Z_{eff}$ : increased $Z_{eff}$ benefits pedestal but adds to core dilution



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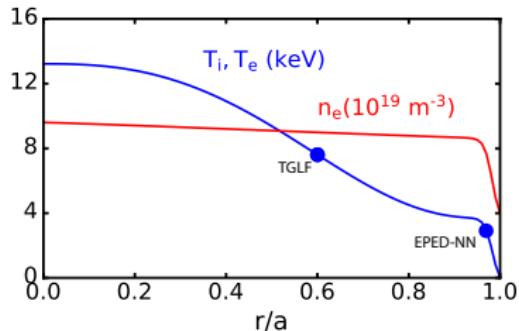
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# Minimal theory predictive model

## 0D → 1D profiles by assuming known functional form

J.McClenaghan APS 2018

- **Pedestal profiles** from EPED-NN prediction
- **Core profiles** from TGLF(-NN) prediction at one radial location
  - $T_e(r=0)$ ,  $T_i(r=0)$  iterated until flux matched at  $r/a=0.6$
- **Equilibrium and sources** based on input global parameters
  - $R, a, B_T, I_p, n_{e,ped}, P_{aux}, \kappa, \delta, q_0, Z_{eff}$



$$T_e(r) = T_{e,ped} + (T_{e,0} - T_{e,ped}) (1 + (r/a)^{2.6})^{2.6}$$

$$n_e(r) = n_{e,ped} + (n_{e,0} - n_{e,ped}) (1 + (r/a)^{1.1})^{1.1}$$

$$Z_{eff} = \text{const}$$

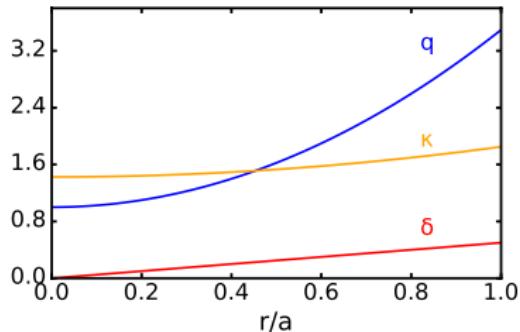
$$\omega_0 = 0$$

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$$q = q_0 + (q_{95} - q_0)r^2$$

$$q_{95} = \frac{5a^2 BS}{RI_p}$$

$$k = k_0 + (k_s - k_0)r^2$$

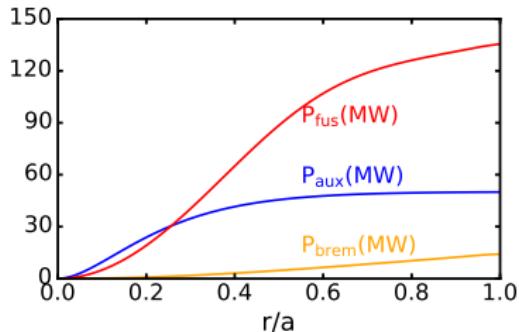
$$\delta = \delta_s r/a$$

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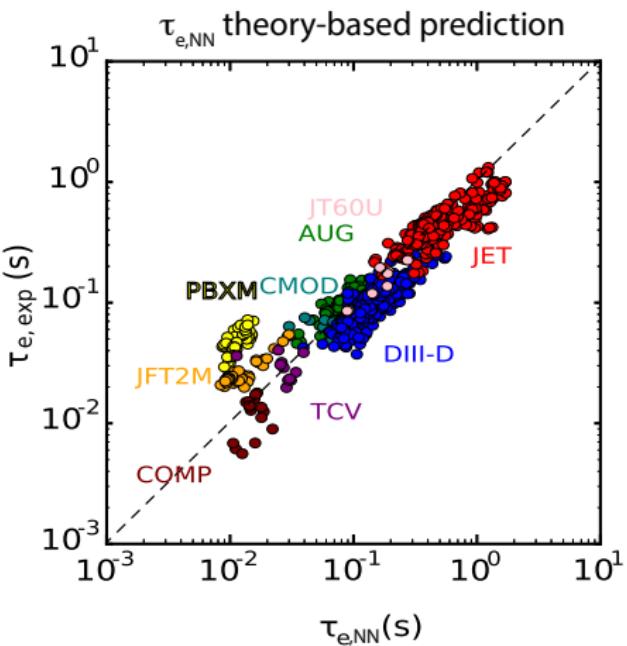
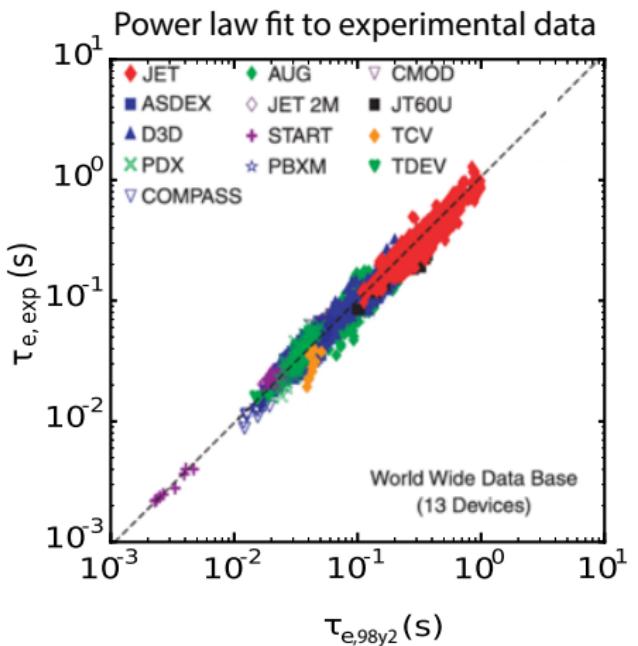
$$P_{aux} \propto \int \exp(-4r/a) dr$$

$$P_{fus} \propto \int n_i^2 r \exp(k_0 + k_1 \log(T_i) + \dots) dr$$

$$P_{brem} \propto Z_{eff} n_e^2 \sqrt{T_e} r dr$$

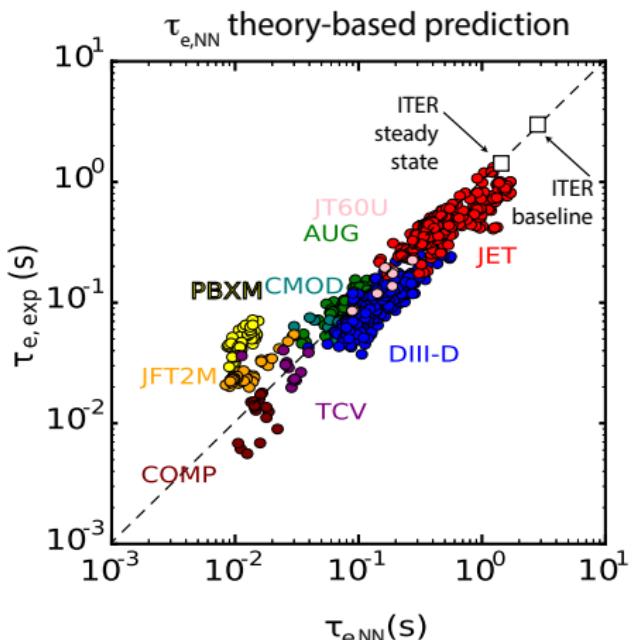
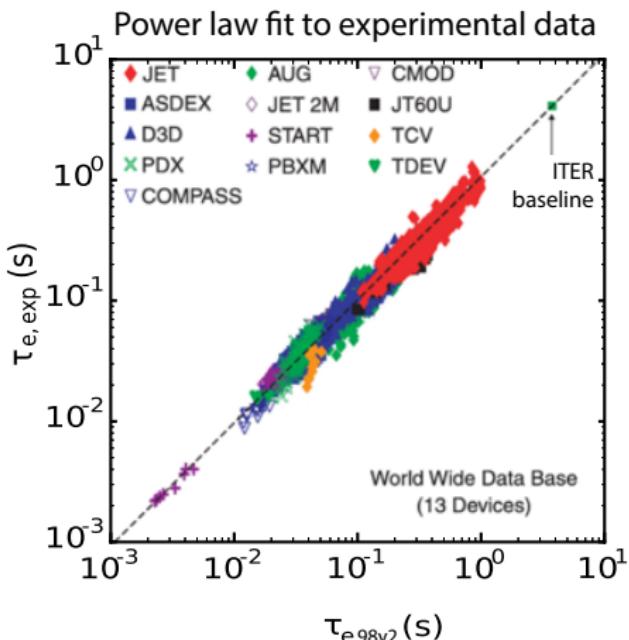
# Applied model for theory-based confinement scaling Showing good agreement with ITPA experimental database

J.McClenaghan APS 2018



# ITER prediction of theory-based model is slightly more pessimistic than $\tau_{98,y2}$ power law scaling

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- TGLF+EPED known to be more pessimistic than  $\tau_{98,y2}$  (Kinsey NF '11)
- Zero rotation and D-C TGLF-NN also more to pessimistic

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# EPED-NN and TGLF-NN accelerated models enable rapid core-pedestal coupled predictions, both applied to ITER

- ① Predictive simulations with self-consistent transport of impurities
  - STEP module in OMFIT, which leverages OMAS to combine codes ("steps") in arbitrary workflows
  - Novel coupling strategy for impurity transport
- ② Machine confinement scaling with minimal theory-based model
  - Good agreement with ITPA experimental database

Going forward:

- Apply higher fidelity predictive workflow to ITPA database
- Improve minimal theory-based predictive model to include rotation and DT-He4-Ne