# Engineering Calculator with KEyboard and Refined Tools

# **ECKERT**

Console User Interface

(Scientific stack calculator)

User's manual

For version 2017-01

January 14, 2017

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# 0. Introduction

#### 0-1. What is ECKERT

ECKERT is a calculator software with keyboard interface, whose name is short for Engineering Calculator with KEyboard and Refined Tools.

```
Engineering Calculator with KEyboard and Refined Tools
(C) 2014-2017 Yuishin Kikuchi
HOMURA: (FF) (Rad) (Hex) (Dword) [i.a/b]
Std: 9/15, Stack: 6, History: 0/9
 _____
  TYPE
                                           VALUE
6: Integer
                                             12
5: Floating
                                            1.5
4: Complex
                                     3/25 - i4/25
                                  [[2, 3], [3, 4]]
Z: Matrix
Y: Rational
X: Tuple(Col) :
                           (1 + i2, 2 + i3, 3 + i4)
MAKE COLUMN TUPLE
Ready to operate
              -----
```

Watching the display, type keywords or values to calculate. This software adopts RPN (Reverse Polish Notation), so you do not have to type parenthnesses to determine calculation priorities.

#### 0-2. Audiences

ECKERT is recommended for users following:

Physical or Chemical scientists, electrical scientists, machine engineer, architect, civil engineer, medical scientists, pharmacists, sologists and so on.

# 0-3. Supporting functions

ECKERT has many functions such as following:

Percent calculation	Logical calculations
Include/exclude tax	Vector calculations
Multiply/divide by prefix	Matrix calculations
Multiply/divide by $2\pi$	Register functions [2]
Decibel conversion	Unit conversions [3]
Base conversion	Math/sci constants [3]
	Include/exclude tax Multiply/divide by prefix Multiply/divide by $2\pi$ Decibel conversion

- [1] Numeric format such as '12k' (12 kilos) or '32u' (32 micros) and so on.
- [2] You can store data from stack to register, also can load/delete from register.
- [3] 2014 CODATA

#### 0-4. Operating environments

Windows 7, Windows 8, Windows 8.1 and the latter versions.

#### 0-5. Disclaimer

This software and the manual of this software is copyrighted to Yuishin Kikuchi.

ECKERT is free for use and no warranty.

If you find bugs or unnatural specifications, please send messages to me.

# ECKERT introduction page

http://sfoftime.web.fc2.com/eckert

E-mail to:

only.my.truth@gmail.com



#### I NEED YOUR HELP

This user's manual was translated from Japanese version. If you find the English in the document something wrong, please send reports to me, thanks.

これは日本語からの翻訳です。不自然な英語表現にお気づきの際はご連絡ください。

# 1. Preparation

#### 1-1. Installation and Uninstallation

You can find ekert86.exe and eckert64.exe in the package. The both are executable file. ekert86.exe is for 32-bit windows system and eckert64.exe is for 64-bit windows system. Please check your system.

Each exe file is independent so you can delete unnecessary one. This software doesn't change registories in your system thus this is portable.

The installation is just copy.

The uninstallation is just delete. You can also delete the config file.

#### 1-2. How to read this manual

This manual explains whole functions of ECKERT and it is just user's manual so the fundmental mathematical definitions are omitted.

If it is the first time to use RPN calculator, please read chapter 2 and 4. If you get used to the operations, read chapter 5, 6, 7 and 11.

If you know about RPN calculator, you can read chapter 4 diagonally to make comprehension of the operations of this software.

To configurate display digits or value format, please read chapter 3.

#### 1. Preparation

# 1-3. Format of this manual

This manual uses following format:

 IMPORTANT
 Important thngs

 NOTICE
 Things to notice

Input> (Notation)

Type the right text and press enter.

This software uses stack concept, which is one of data storage structures. (Please read chapter 3 to get more information about stack). This manual uses tables following to describe a state of a stack.

#	TYPE	VALUE	
4			
Z			Suuplementary
Υ	Integer	12	explanation
Х	Floating	1.5	4

The column TYPE means data type and the column VALUE means data value.

This document uses list following to show functions.

Function	Keyword	R	D	Computation
Add	ADD	2	2	V + V
Add	+	2	2	Y + X
Cysletmo at	SUB	2 2	2	Y - X
Subtract	-		] 2   '	2   2

The column Function means function name and the column Keyword means command to call corresponding function.

Please refer chapter 4 to get more information about reading list above.

#### 2-1. Launch and End

Just double click the executable file to launch.

Type 'EXIT', 'QUIT', or 'Q' and press enter to terminate. Inputs are non-capital-sensitive except for numerical value input.

Function	Keyword
	EXIT
Terminate	QUIT
	Q

Special start up is available. Please refer chapter 15.

#### 2-2. Display of calculation mode

The chart following is the display of calculation mode:

```
Engineering Calculator with KEyboard and Refined Tools
(C) 2014-2017 Yuishin Kikuchi
HOMURA: (FF) (Rad) (Hex) (Dword) [i.a/b]
Std: 9/15, Stack: 6, History: 0/9
  -----
# TYPE
                                              VALUE
                                                 12
6: Integer
5: Floating
                                                1.5
4: Complex
                                        3/25 - i4/25
                                    [[2, 3], [3, 4]]
Z: Matrix
Y: Rational
                             (1 + i2, 2 + i3, 3 + i4)
X: Tuple(Col) :
MAKE COLUMN TUPLE
Ready to operate
```

The first two lines mean name of this software and the copyright of it.

```
Engineering Calculator with KEyboard and Refined Tools (C) 2014-2017 Yuishin Kikuchi
```

Following a split line, calculation config and state display.

```
HOMURA: (FF) (Rad) (Hex) (Dword) [i.a/b]
Std: 9/15, Stack: 6, History: 0/9
```

Then below a doubly split line, stack display there.

```
# TYPE : VALUE

6: Integer : 12
5: Floating : 1.5
4: Complex : 3/25 - i4/25
Z: Rational : 2.1/4
Y: Matrix : [[2, 3], [3, 4]]
X: Tuple(Col) : (1 + i2, 2 + i3, 3 + i4)
```

The right column is data number, the center is data type, and the left is value.

Below the stack display, 2-line message area there.

```
TRANSPOSE
Ready to operate
```

The bottom of the display is input field.

```
> _
```

Go on to the next section to make comprehension of reading the display.

# 2-3. Calculation mode and states display

You can find 2-line calculation mode and states display.

HOMURA: (FF) (Rad) (Hex) (Dword) [i.a/b] Std: 9/15, Stack: 6, History: 0/9

In the first line, you can notice symbols in the following list:

Symbol	Meaning	Class
(AD)	Auto Decimal display	Danimal
(FD)	Force Decimal display	Decimal
(FF)	Force Fractional display	display
(Deg)	Degree mode	
(Rad)	Radian mode	Angle mode
(Gra)	Grade mode	
(Bin)	Binary display	
(0ct)	Octal display	Ungianad
(Sdec)	Signed decimal display	Unsigned integer display
(Udec)	Unsigned decimal display	integer display
(Hex)	Hexadecimal display	
(Byte)	8-bit mode	
(Word)	16-bit mode	Logical
(Dword)	32-bit mode	calculation
(Qword)	64-bit mode	
[Reg]	Register display	
[Eul]	Euler display	
[i.a/b]	Mixed fractional display	

(Symbol) selected in each class is always displayed.

[Symbol] is displayed if the mode is enabled.

You can see display above and you get force fractional display, radian, hexadecimal display, 32-bit and mixed fractional display mode.

There are three displays in the second line. The first is decimal display mode and display digits.

Symbol	Mode
Std	Standard display
Fix	Fixed display
Sci	Scientific display
Eng	Engineering display

The fraction "Int/Int" means this: the first means the current display digits and the second is max digits you can set in the selected display mode. To change digits, please read chapter 3.

If you see above, you get that the settings are standard display mode and the current number of standard display digits is 6 and the maximum number of digits you can set is 15.

The second is the number of elements in the stack. If the number is zero, Empty is displayed.

If you see like above, there are 11 elements in the stack.

The third is history display.

Display	Meaning
OFF	History is disabled
Init	Initial state
Int/Int	(Discribed later)

'Int/int' display means this: the first integer is the times that you have called undo and the second integer is the items in the history.

You see above and you get that you have undo 4 times and the number of items in the stack is 10, so you can redo 10 times totally.

# 2-4. Stack display

Let's learn the concept of stack.

# TYPE	:	VALUE
-:	:	
-:	:	
-:	:	
<b>Z</b> :	:	
Y: Integer	:	12
X: Floating	:	1.5

Stack is one of the data container. This software has one stack.

In each line in the stack display contains item number, data type and value. A data type means a kind of number. If the type is integer, Integer is displayed and if the type is rational number, Rational is displayed.

And more, this manual shows the stack like below:

#	TYPE	VALUE
4		
Z		
Υ	Integer	12
Х	Floating	1.5

# **IMPORTANT**

The stack size is unlimited.

X is the bottom of the stack. Y is the second bottom and Z is the third bottom. After that the data number is displayed as integer such as 4, 5.... And the data in X is called just X, the datain Y is just Y, and so on.

Go on to the next page and make comprehension of stack graphically.

You can see a stack like a pile of cards. You draw one by one from the top of the pile and you put into the pile one by one.



Please look at the left chart. There are some cards. You put a card '1' and card '2' in turn.

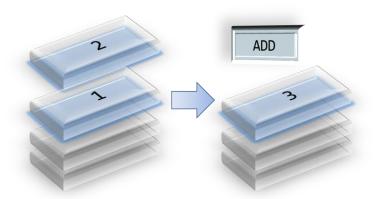
This situation is expressed like below:

#	TYPE	VALUE
Z		
Υ	Integer	1
Х	Integer	2



The left chart means the top of the pile is removed from the previous chart. In other words, X is dropped from the stack.

#	TYPE	VALUE
Z		
Υ		
Х	Integer	1



Let's see addition with stack.

You draw 2 cards from the top and you put the additional value on the top.

This is the fundamental flow of calculation with stack.

#	TYPE	VALUE
Z		
Υ	Integer	1
Х	Integer	2

Addition operated

#	TYPE	VALUE
Z		
Υ		
Х	Integer	3

There are 3 fundamental operations: add (push), remove (drop) and execution.

# Data-type list here:

Display	Meaning
Error	String value means error
String	String value
Integer	Integer
Floating	Floating point number
Rational	Rational number
Infinity	Infinity
Complex	Complex number
Boolean	Boolean (true of false)
Byte	8-bit unsigned integer
Word	16-bit unsigned integer
Dword	32-bit unsigned integer
Qword	64-bit unsigned integer
Tuple[Row]	Row vector
Tuple(Col)	Column vector
Matrix	Matrix

# 2-5. Message display

In the message display, called function and error / notice / confirm message are displayed.

TRANSPOSE
Ready to operate

In the first line is called function and the second line is the other messages.

If unoperatable commands such as division by zero is input, the operation is stopped and the error message is displayed in the second line.

[!] ADD Y+X Error: Too few arguments

If there is error or notice message, the message is displayed second line with a symbol in the first line.

Symbol	Meaning
[!]	Operation is terminated by error
[i]	Unordinal operation
[C]	Waiting input or confirm

For more information, please read chapter 16.

If [?] is displayed, it means software bugs. Please send me a bug report.

# 2-6. Configuration mode display

Type 'config' to go to configuration display.

```
Engineering Calculator with KEyboard and Refined Tools
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CONFIGURATION MODE

Interface
   History size (hist): 10
   Display width (width): 60
   Display lines (lines): 6

Management
   Load config (load)
   Save config (save)
   Reset config (reset)

ECKERT Config
To quit config, type "calc", "homura"
```

```
Interface
History size (hist): 10
Display width (width): 60
Display lines (lines): 6
```

Maximum history size, display width and the number of stack display lines are shown. Please read chapter 3 to configurate.

```
Management
Load config (load)
Save config (save)
Reset config (reset)
```

Those are command for config management.

# 2-7. Fundamental operation

Input keywords or values to operate. Only half-width characters are supported.

Type one or several space-splitted keywords or values and hit enter to calculate or configurate. If the number of tokens, which are keywords or numerical values, is not single, each token is processed in turn.

This way, "type and enter" is the flow of the operations. Please notice that the display changes only pressing enter. And then, only SI or binary prefixes are case-sensitive, the others are not.

This software supports only printable characters input.

For instance, type like below to operate 'add' and 'multiply' in turn.

Some keywords are aliases, in other words, some ones are connected with the same function. And more, there are some keywords depend on calculation modes.

Type numerical values to input. You can put space-splitted values in order.

You can even mix values and keywords.

Go on to the next section to get how to input numeric values.

# 2-8. Input numeric values

This section shows how to input numeric values in this software.

#### 2-8-1. Integer

Just type an integer value.

#### 2-8-2. Decimal

Type a value with decimal point.

You can omit integer part (like ".2") or decimal part (like "1.").

#### 2-8-3. Exponential

Type a decimal value and append 'E' and a decimal exponent.

For instance,  $6.02 \times 10^{-23}$  is expressed like "6.02E-23" and  $1.01325 \times 10^5$  is expressed like "1.01325E5".

#### 2-8-4. Imaginary unit

Positive imaginary unit is "i" or "+i" and negative imaginary unit is "-i".

Non-case-sensitive.

#### 2-8-5. Imaginary number

Type integer, decimal or exponential with prefix 'i'.

Non-case-sensitive.

#### 2-8-6. Infinity

Positive infinity is "INF", "+INF" or "+INFINITY".

Negative infinity is "-INF" or "-INFINITY".

#### 2-8-7. Boolean

True value is "TRUE" or "T" and false value is "FALSE" or "F".

#### 2-8-8. Unsigned decimal value

Type "u" and postfix non-signed integer.

#### 2-8-9. Binary value

Type "0b" and postfix binary expression using 0 and 1.

# 2-8-10. Octal value

Type "00" and postfix octal expression using 0 to 7.

#### 2-8-11. Hexadecimal value

Type "0x" and postfix hexadecimal expression using 0 to 9 and A to F.

# 2-8-12. Value with SI or binary prefix

You can append SI or binary prefix to integer, decimal, exponential and imaginary value. SI and binary prefixes are case-sensitive.

Symbol	Name	Value			Value	Name	Symbol
da	DECA	1.0E+01	SI	IS	1.0E-01	DECI	d
h	НЕСТО	1.0E+02	SI prefix greater than 1	SI prefix less than 1	1.0E-02	CENTI	С
K, k	KILO	1.0E+03	x gr	x les	1.0E-03	MILLI	m
М	MEGA	1.0E+06	eater	ss tha	1.0E-06	MICRO	u
G	GIGA	1.0E+09	· thai	an 1	1.0E-09	NANO	n
Т	TERA	1.0E+12	1 1		1.0E-12	PICO	р
Р	PETA	1.0E+15			1.0E-15	FEMTO	f
Е	EXA	1.0E+18			1.0E-18	ATTO	а
Z	ZETTA	1.0E+21			1.0E-21	ZEPTO	z
Υ	YOTTA	1.0E+24			1.0E-24	<b>YOCTO</b>	у
Ki, ki	KIBI	1024^1	Bir			_	
Mi, mi	MEBI	1024^2	Binary prefix				
Gi, gi	GIBI	1024^3	pref				
Ti, ti	TEBI	1024^4	ΪΧ				
Pi, pi	PEBI	1024^5					
Ei, ei	EXBI	1024^6					
Zi, zi	ZEBI	1024^7					
Yi, yi	YOBI	1024^8					

You can binary prefixes alias.

# 2-9. Examples of value input

Examples here:

Integer	Input> -3	Infinity	Input> -inf
Prefixed	Input> 3k	Boolean	Input> t
Exponential	Input> 2.998e8	Unsigned	Input> u65536
Imaginary unit	Input> -i	Binary	Input> 0b1010
Imaginary num	Input> i12	Octal	Input> 0o100
Imag with sign	Input> -i5	Hexadecimal	<pre>Input&gt; 0xFFFE</pre>

You can also input math or scientific constants with keywords. Please read chapter 14 to get more information.

Name	Keyword	Value		
PI	PI	3.141 592 653 589 79		
Napier's constant	Е	2.718 281 828 459 05		
Euler-Mascheroni constant	EG	0.577 215 664 901 533		

In addition to these you can input string value. Use double quotation to input string value.

You can use string to put memos in the register or use macro function.

2-10. When the error message is displayed

When the error occurs while operating some functions, the operating and the left unoperated functions are cancelled. This means, the state is the before one cancelled operation. And then, the error

messages are shown.

If you see error messages, you can operate as usual. Input commands and if the operations are

successful, error messages are disappeared.

Even if operating space-splitted tokens, the functions called one by one, so this software do not stop

the operations if no errors.

Input> 5 0 /

(You can make sense the notation if you read chapter 4.)

For instance, if you input like above, the error "division by zero" occurs. But the push operations

are done, so the value 5 and the value 0 is added into the stack and the division cancelled with the

stack remaining.

If the error messages are shown, undo and redo are recommended. Please read chapter 15 to get

more information.

If you look at the list of error messages, please read chapter 16.

When unsupported inputs are detected, the error message below is displayed:

[!] OPERATIONAL ERROR Error: Unsupported operation or notation

If you see this, please check the spelling.

And then, even if the keyword is supported, you can see this when the calculation mode or state is

not inappropriate, or greater than one settings-changing keywords.

17

# 3. Settings

#### IMPORTANT

Please read this chapter after making comprehension of fundamental operations.

#### 3-1. Settings in configuration mode

You can set max history size, display width and the number of lines of stack display in configuration mode.

Please type the keyword 'CONFIG' to go to config mode. Input keyword "HOMURA" or "CALC" to return to calculation mode.

#### 3-1-1. Max history size

Type "HIST" and an integer. You can input splited-tokens like "hist 10". You can set the size to 0 to disable history function.

The default max history size is 10.

Type below to set the max history size to 20.

#### 3-1-2. Display width

Type "WIDTH" and an integer. You can input splited-tokens like "width 79". If the value is less than the least width, the least width is set.

The default display width is 79 and the least size is 60.

Type below to set the display width to 69.

#### 3-1-3. Number of stack lines

Type "LINES" and an integer. You can input splited-tokens like "lines 11". If the value is less than the least number, the least number is set.

The default number of stack lines is 11 and the least is 4.

Type below to set the number of stack lines to 20.

# 3-1-4. Management of config

You can save configurations as config file. You can use the functions following to manage config file.

Function	Keyword
Load config file	LOAD
Save config file	SAVE
Deset config	RESET
Reset config	RST

If the config file exists, this software loads it on startup. So the max history size and display width are restored automatically.

You can load config file explicitly with "LOAD" function.

The function "RESET" sets all settings in config mode to default. But this function does not save or change a config file.

# 3-1-5. Functions in configuration mode

List of keywords for configuration mode is following:

Function	Keyword
Config mode	CONFIG
Calculation mode	CALC
Calculation mode	HOMURA
History size	HIST
Display width	WIDTH
Number of stack lines	LINES
Load config file	LOAD
Save config file	SAVE
Pagat config	RESET
Reset config	RST

# 3-2. Settings in calculation mode

Angle mode, type display and number of display digits can be changed in calculation mode.

#### 3-2-1. Rational display mode

When the decimal display is set to standard, you can choose rational number display following:

Audo Decimal display

If a rational number can be displayed as finite decimal display, show a decimal. In other cases, show a fraction.

■ Force Decimal display

All rational numbers are displayed as decimal.

Force Fractional display

All rational numbers are displayed as fraction.

To choose mode, use keywords below:

Mode	Keyword	Symbol
Auto Decimal display	AD	(AD)
Force Decimal display	FD	(FD)
Force Fractional display	FF	(FF)

The default rational display mode is Force Decimal.

#### 3-2-2. Angle mode

You can choose angle unit with setting angle mode. Angle mode affects trigonometric functions. To choose mode, use the keywords below:

Mode	Keyword	Symbol
Degree	DEG	(Deg)
Radian	RAD	(Rad)
Grade	GRAD	(Cn2)
Grade	GRA	(Gra)

This mode is connected with "SIN" and "ARG" and so on.

The default angle mode is Radian.

#### 3-2-3. N-ary number display mode

You can select the display of 8-bit, 16-bit, 32-bit and 64-bit data.

To choose mode, use the keywords below:

Mode	Keyword	Symbol
Binary display	BIN	(Bin)
Octal display	ОСТ	(0ct)
Signed decimal display	SDEC	(Sdec)
Unsigned decimal display	UDEC	(Udec)
Hexadecimal display	HEX	(Hex)

The default n-ary number display mode is Hexadecimal.

# 3-2-4. N-bit input mode

You can choose the binary size to input from 8, 16, 32 or 64 bits. If unsigned decimal with 'u' is detected, the value is generated as selected bit mode.

To choose mode, use the keywords below:

Mode	Keyword	Symbol	
8-bit mode	BYTE	(Byte)	
(byte)	DITE	(byte)	
16-bit mode	WORD	(Word)	
(word)	WORD	(wor'd)	
32-bit mode	DWORD	(Dword)	
(dword)	DWORD	(DWOI d)	
64-bit mode	QWORD	(Qword)	
(qword)	QNOND	(Qword)	

The default size is 32-bit.

# 3-2-5. Type display

You can switch the type display in the stack display on/off. Input "TYPE" without any other keywords to switch.

The default type display is enabled.

#### 3-2-6. Register display

You can enable or disable the register display. Use the keyword "REG" or "REGISTER" to switch the display. Register is displayed above the stack. If the register display is enabled, the stack display gets smaller.

When register display is enabled, the symbol [Reg] is displayed.

The default setting is disabled.

#### 3-2-7. Euler display

You can switch the complex number display: a + ib (rectangular) or  $r \exp(i\theta)$  (polar) style. Use the keyword "EULER" or "EUL" to switch.

If the Euler display is enabled, the symbol [Eul] is displayed.

The argument of euler display is depends on angle mode.

Mode	Expression	Display	
Rectangular	2 + 3 <i>i</i>	2 + i3	
Polar	12∠56[deg]	12 ovn(1356 d)	
(Degree)	12230[ueg]	12 exp(+i56.d)	
Polar	12∠0.9[rad]	12 exp(+i0.9)	
(Radian)	1220.9[1au]	12 exp(+10.9)	
Polar	12 (62[gra]	12 exp(+i62.g)	
(Grade)	12∠62[gra]	12 exp(+102.g)	

The default setting is disabled.

# 3-2-8. Mixed fractional display

You can get mixed fractional display. Use "FRACTION" or "FRAC" to enable/disable mixed fractional display.

The display of rational number is below:

Value	Provisional	Mixed	Decimal
+3/2	3/2	1.1/2	1.5
-6/5	-6/5	-1.1/5	-1.2

If the mode is enabled, the symbol [i.a/b] is displayed.

The default setting is disabled.

#### 3-2-9. Decimal display

You can choose decimal display mode. There are four modes: standard, fixed, exponential, engineering.

# ■ Standard display

Value display changes flexibly.

Rational number display depends on the rational display mode.

#### ■ Fixed display

Fix the digits of decimal part.

Integer and rational number is displayed as decimal.

#### ■ Scientific display

All scalars are displayed as scientific notation such as "1.2E+10". The range of mantissa m is  $0 \le m < 10$ .

Integer and rational number is displayed as decimal.

#### ■ Engineering display

All scalars are displayed as scientific notation such as "12E+10". The range of mantissa m is  $0 \le m < 1000$ .

Integer and rational number is displayed as decimal.

To choose display mode, use the keywords following:

Display	Keyword	Symbol
Standard display	STD	Std
Fixed display	FIX	Fix
Scientific display	SCI	Sci
Engineering display	ENG	Eng

Rational number is displayed as decimal without in standard mode.

The default display mode is standard.

#### 3-2-10. Decimal digits

You can change the digits of decimal. Here is the list of "digit" meaning:

Mode	Meaning of "digits"
Standard	Significant digits
Fixed	Digits of decimal part
Scientific	Significant digits
Engineering	Significant digits

Use the keyword "DISP" or "DIGIT" and input an integer to set the number of digits.

If you would set to 3 digits, type below:

You can set digits in each mode.

The maximum number of digits exists in each mode. Too large number is read as max and too small number does as minimum.

Mode	Minimum	Maximum
Standard	1	15
Fixed	0	15
Scientific	1	15
Engineering	1	15

Example: 10 times of  $\pi$  (31.4159265358979)

Std: 5/15 31.416 Fix: 5/15 31.41593 Sci: 5/15 3.1416E+01 Eng: 5/15 31.416E+00

The default numbers of digits are all 9.

And then, if you put other tokens after digit settings like "disp 10 36", these are ignored.

3-2-11. Keywords of settings in calculation mode Here is the list of keywords of settings in calculation mode:

Mode	Keyword	Symbol
Auto Decimal display	AD	(AD)
Force Decimal display	FD	(FD)
Force Fractional display	FF	(FF)
Degree mode	DEG	(Deg)
Radian mode	RAD	(Rad)
Grade mode	GRA	(Cn2)
Grade mode	GRAD	(Gra)
Binary display	BIN	(Bin)
Octal display	ОСТ	(0ct)
Signed decimal display	SDEC	(Sdec)
Unsigned decimal display	UDEC	(Udec)
Hexadecimal display	HEX	(Hex)
8-bit mode	BYTE	(Byte)
16-bit mode	WORD	(Word)
32-bit mode	DWORD	(Dword)
64-bit mode	QWORD	(Qword)
Type display	TYPE	
Register display	REG	[Reg]
Eular dignley	EULER	[[]]
Euler display	EUL	[Eul]
Mixed fraction display	FRACTION	[i.a/b]
Whited fraction display	FRAC	[1.a/U]
Standard decimal display	STD	Std
Fixed decimal display	FIX	Fix
Scientific decimal display	SCI	Sci
Engineering decimal display	ENG	Eng
Set number of digits	DISP	
bet number of digits	DIGIT	

# 3-3. Next/previous pages in stack

If there are many elements in the stack, you cannot see the all data.

Std: 9/15	, Stack: 11,	History: 0/10	
# TYPE ^ 6: Intege 5: Intege 4: Intege Z: Intege Y: Intege X: Intege	r : r : r : r :		VALUE ^ 6 7 8 9 10
PUSH Integ Ready to o			

If you need to see unshown data, use stack page function. There are 8 data in stack but only 6 is shown in the chart above.

Use the keyword "NEXT" or "N" to turn to the next page.

Std	: 9/15,	Stack: 11,	History: 0/10		
#	TYPE	:		VALUE	
-:		:			
11:	Integer	:		1	
10:	Integer	:		2	
9:	Integer	:		3	
8:	Integer	:		4	
7:	Integer	:		5	
V				v	
NEXT PAGE of STACK					
Rea	dy to ope	rate 			

Use the keyword "PREV" or "P" to turn to the previous page.

If you would like to return to first page, use the keyword "FIRST" or "FST".

If a stack-changing function is called, the page is set to first.

Here is the list of stack page-flipping:

Function	Keyword
Next page of steels	NEXT
Next page of stack	N
Dravious page of steels	PREV
Previous page of stack	Р
First page of steels	FIRST
First page of stack	FST

# 3-4. Next/previous pages in register

This software has registers which is used for saving location of data. There are 26 registers in this software: RA to RZ. You can not view all registers at once without changing the number of stack lines. Look at the following chart. RA to RC are displayed but the others are not.

Std: 9	/15,	Stack: 3	History:	0/10	
# TYP	:===== E	:		======	VALUE
RA: Flo	ating	:			3.14159265
RB:	_	:			
RC:		:			
Z: Int	eger	:			4
Y: Int	eger	:			5
X: Int	eger	:			6
PUSH Integer Ready to operate					

You can change the register page.

Type "REGNEXT" or "RN" to change to next page of registers.

Std: 9/15,	Stack: 3,	History: 0/3			
# TYPE	:	VALUE			
RD:	:				
RE:	:				
RF:	:				
Z: Integer	:	4			
Y: Integer	:	5			
X: Integer	:	6			
NEXT PAGE of REGISTERS Ready to operate					

On the other hand, type "REGPREV" or "RP" to change to previous page of registers. The keyword "REGFIRST" or "RF" is for returning to first page of the registers.

Here is the list of register page functions:

Function	Keyword
Novt page of registers	REGNEXT
Next page of registers	RN
Dravious page of registers	REGPREV
Previous page of registers	RP
First made of magistans	REGFIRST
First page of registers	RF

#### 3. Settings

### 3-5. View full string of data

In case of the value display is too long, only the left part is displayed. The following chart is the stack which has a complex number consists of 2 rationals but the right part is omited.

# TYPE	:	VALUE
·		
	:	
-:	•	
7:	:	
Y:	:	
X: Complex	: 2432902008176640000/2432902008176	64000

To view full data, use the keyword "VIEW" or "V".

Function	Keyword
View full data	VIEW
view full data	V

View mode shows data which are displayed in calculation mode.

Press Enter to return to calculation mode.

## 3. Settings

# 3-6. Version display

Type the keyword "VER" or "VERSION" to display current version.

Function	Keyword
Varsion display	VERSION
Version display	VER

If you find bugs in this app, please send reports to me with the version.

# **IMPORTANT**

This chapter includes the most important things about operating this software, such as RPN. So please read carefully.

## 4-1. Elementary stack operation

First of all, let's input an integer.

## Input> 12

#	TYPE	VALUE			
4					
Z					$\supset$
Υ				Added into	
Х	Integer	12	$\leq$	the bottom	ل

12 is added into X in the stack display area.

Next, type one more integer.

# Input> 9

#	TYPE	VALUE			
4					
Z				A 44-4 :4-	7
Υ	Integer	12		Added into the bottom	
Х	Integer	9	4	ine bottom	ل

The data 9 is added into X.

This way, addition is executed into X.

The next, input decimals.

Input> 1.6 6.0e-23

#	TYPE	VALUE	
4	Integer	12	
Z	Integer	9	
Υ	Floating	1.6	Added in turn
Х	Floating	6E-23	

This way, just write numbers to add into the stack. The addition into the bottom of the stack is called push.

Type "DROP" or "\(\frac{1}{2}\)" to remove the data at the bottom of the stack. The removal of the bottom of the bottom of the stack is called drop.

# Input> ¥

#	TYPE	VALUE	
4			
Z	Integer	12	The bettern is
Υ	Integer	9	The bottom is
Х	Floating	1.6	removed

Just hit enter without any input to duplicate the bottom of the stack (X) and push.

The keywords "COPY", "C" and "DUP" call the same function.

Input> (Just hit Enter)

#	TYPE	VALUE	
4	Integer	12	
Z	Integer	9	
Υ	Floating	1.6	Duplicated
Χ	Floating	1.6	

Type "CLEAR" or "CLR" to empty the stack.

## Input> clear

#	TYPE	VALUE	
4			
Z			
Υ			Emptied
Х			

Here is the list of keywords described in this section:

Function	Keyword	R	D
Push		0	0
Dron	DROP	1	1
Drop	¥	1	
Duplicate [1]	COPY		
	С	1	1
	DUP		
Clear steels	CLEAR	N <sub>2</sub> O	NI
Clear stack	CLR	N>0	N

[1] You can call the function just hitting enter without any input.

Let us calculate four arithmetics after getting this section.

### 4-2. Four arithmetics

The four arithmetics are the basics of calculating with this software.

Use following keywords to calculate the four arithmetics:

Function	Keyword	R	D	Computation						
Add	ADD	2		•	2 2					V + V
Add	+	2	2	Y + X						
Subctract	SUB	2	2	Y - X						
Subctract	1			2   2	$I - \lambda$					
Multiply	MUL	2	<u> </u>	2	2 2	1	$Y \times X$			
Multiply	*		_	ΙΧΛ						
Divide	DIV	2	2	Y/X						
Divide	/	2	2   2		Ι/Λ					
Modulo	MOD	] ,	2 2	2 2 <i>Y</i>	Y mod X					
Modulo	%					i iiiou x				

Let us try following the tutlrial.

The first step is a simple addition. Challenge "2 + 3". Push 2 numbers as following:

# Input> 2 3

#	TYPE	VALUE	
4			
Z			
Υ	Integer	2	Added in turn
Х	Integer	3	Added in turn

Input> +

#	TYPE	VALUE	
4			Addition requires
Z			2 data.
Υ			2 dropped. 1 result
Х	Integer	5	pushed.

You can see X is 5, which is the tresult of Y+X (2+3). The previous Y and X are removed. Your inputs mean the pushing 2 and 3 before adding.

Following this, try this:

Input> 9 -

#	TYPE	VALUE		
4			/	
Z				Push and
Υ				subtraction at
Х	Integer	-4	4	one time.

You get X is -4. You have pushed 9 and called subtraction. You can see this software calculates with using the bottom of the stack.

Function	Keyword	R	D	Computation	
٨٩٩	ADD	,	1	V + V	
Add	+	2   2		Y + X	

This manual uses tables like above one. The column R is the number of required data. If you call the function without the stack containing enough data, error messages are displayed. The column D is the number of dropped data.

Addition requires 2 data. Once the function is called, 2 data are dropped and the result of Y + X is pushed. The other arithmetics are similar with addition.

In the case of not-enough data, you see error messages like following:

Engineering Calculator with KEyboard and Refined Tools (C) 2014-2017 Yuishin Kikuchi
HOMURA: (AD) (Rad) (Hex) (Dword) Std: 9/15, Stack: 1, History: 0/10
# TYPE : VALUE
-: :
-: :
-: :
Z: :
Y: :
X: Integer : 5
[!] ADD Y+X Error: Too few arguments
-

### 4-3. Multiple arithmetics

Let us try higher-level.

Calculate the area of the trapezoid: the upper base is 2, the lower is 1, the hight is 5. The formula of of calculating this is:

$$5 \times (2 + 1) \div 2$$

You can read this like the multiplication of 5 and (2 + 1). First, push 5 and the result of 2 + 1, and call multiply. The final step is halfing.

Type as following to calculate at one time.

However, this expression is difficult for the beginners. I divided this into the steps:  $(1) \sim (5)$ . Read carefully and operate to understand easily.

#### (1) Push 5, 2 and 1

Input> 5 2 1

#	TYPE	VALUE	
4			
Z	Integer	5	
Υ	Integer	2	Pushed in
Х	Integer	1	turn

#### (2) Add

Input> +

#	TYPE	VALUE		Unused value
4				remains
Z				
Υ	Integer	5		Addition
Х	Integer	3	$\leq$	requires 2.

(3) Multiply

Input> \*

#	TYPE	VALUE	
4			
Z			
Υ			Multiplication
Х	Integer	15	requires 2.

(4) Push 2

Input> 2

#	TYPE	VALUE	
4			
Z			
Υ	Integer	15	Pushed into
Х	Integer	2	$\leftarrow$ the bottom

(5) Divide

Input> /

			1
#	TYPE	VALUE	
4			
Z			
Υ			Division
Х	Rational	15/2	requires 2.

You can calculate with pushing and calling functions in appropriate order without parentheses.

# 4-4. Elementary functions

Here is the list of elementary functions without 4 arithmetics:

Function	Keyword	R	D	Computation
Quotient and	OM	,	_	$Y \leftarrow Y \div X$
remainder	QM	2	2	$X \leftarrow Y \mod X$
Increment	INC	1	1	V . 1
merement	++	1	1	X+1
Decrement	DEC	1	1	<i>X</i> – 1
Decrement				$\lambda = 1$
Absolute value	ABS	1	1	X
Nagata	PM	1	1	-X
Negate	NEG	1	1	<i>−∧</i>
Invert (incl. matrix)	INV	1	1	$X^{-1}$

You can increment or decrement only integers. Increment is adding 1 and decrement is adding -1. For example, type this to find the inverse of 5:

These functions require 1 artument.

#### 5-1. How to use math functions

This software supports many math functions. Please notice that the usage of these functions is similar with the usage of 4 arithmetics. Push first and call functions.

Some functions have restricted domains.

#### 5-2. Exponent and logarithm

Please use following keywords with operating exponents and logarithms.

Function	Keyword	R	D	Computation
Square	SQ	1	1	X <sup>2</sup>
Square root	SQRT	1	1	$\sqrt{X}$
Cubic root	CBRT	1	1	<sup>3</sup> √ <i>X</i>
Hypotenuse	НҮРОТ	2	2	$\sqrt{Y^2 + X^2}$
	POW			
Power	۸	2	2	$Y^X$
	**			
N-th root	NRT	2	2	$\sqrt[X]{Y}$
Exponent	EXP	1	1	$\exp(X)$
Power of 10	TPOW	1	1	10 <sup>X</sup>
Power of 2	BPOW	1	1	$2^X$
Logarithm of X to base Y	LOGB	2	2	$\log_Y(X)$
Natural logarithm	LN	1	1	$\log_e(X)$
Common logarithm	LOG	1	1	$\log_{10}(X)$
Binary logarithm	LB	1	1	$\log_2(X)$

EX 1 
$$\log_{10} 3000$$
 EX 3  $\log_3 22$  Input> 3000  $\log$  Input> 3 22  $\log b$  EX 2  $\sqrt{5^2 + 12^2}$  EX 4  $\exp(-3^2/2)$  Input> 5 sq 12 sq + sqrt Input> 3 sq 2 / pm exp

# 5-3. Trigonometric functions

Here is the list of trigonometric and inverse trigonometric functions:

Function	Keyword	R	D	Computation
Sine	SIN	1	1	sin(X)
Cosine	cos	1	1	cos(X)
Tangent	TAN	1	1	tan(X)
Arcsine	ASIN	1	1	arcsin(X)
Arccosine	ACOS	1	1	arccos(X)
Arctangent	ATAN	1	1	arctan(X)

These keywords depend on the angle mode. If you input "sin" in degree mode, this software calls "sin (degree)".

The radian trigonometric functions are here:

Function	Keyword	R	D	Computation
Sine (Radian)	SINR	1	1	sin(X[rad])
Cosine (Radian)	COSR	1	1	cos(X[rad])
Tangent (Radian)	TANR	1	1	tan(X[rad])
Arcsine (Radian)	ASINR	1	1	arcsin(X)[rad]
Arccosine (Radian)	ACOSR	1	1	arccos(X) [rad]
Arctangent (Radian)	ATANR	1	1	arctan(X) [rad]

The degree trigonometric functions are here:

Function	Keyword	R	D	Computation
Sine (Degree)	SIND	1	1	sin(X[deg])
Cosine (Degree)	COSD	1	1	cos(X[deg])
Tangent (Degree)	TAND	1	1	tan(X[deg])
Arcsine (Degree)	ASIND	1	1	arcsin(X)[deg]
Arccosine (Degree)	ACOSD	1	1	arccos(X) [deg]
Arctangent (Degree)	ATAND	1	1	arctan(X) [deg]

The grade trigonometric functions are here:

Function	Keyword	R	D	Computation
Sine (Grade)	SING	1	1	sin(X[gra])
Cosine (Grade)	COSG	1	1	cos(X[gra])
Tangent (Grade)	TANG	1	1	tan(X[gra])
Arcsine (Grade)	ASING	1	1	arcsin(X)[gra]
Arccosine (Grade)	ACOSG	1	1	arccos(X) [gra]
Arctangent (Grade)	ATANG	1	1	arctan(X) [gra]

EX 1 sin(30) (mode dependent)

Input> 30 sin

EX 2 cos(52[deg])

Input> 52 tand

## 5-4. Hyperbolic functions

Use following keywords to calculate hyperbolic functions:

Function	Keyword	R	D	Computation
Hyperbolic sine	SINH	1	1	sinh(X)
Hyperbolic cosine	COSH	1	1	cosh(X)
Hyperbolic tangent	TANH	1	1	tanh(X)
Inverse hyperbolic sine	ASINH	1	1	asinh(X)
Inverse hyperbolic cosine	ACOSH	1	1	acosh(X)
Inverse hyperbolic tangent	ATANH	1	1	atanh(X)

EX 
$$cosh(1.2)$$

Input> 1.2 cosh

### 5-5. Stats functions

Stats functions are here:

Function	Keyword	R	D	Computation
Beta function	ВЕТА	2	2	B(Y,X)
Gamma function	GAMMA	1	1	Γ( <i>X</i> )
Logarithm of gamma function	LNGAMMA	1	1	$\log_{\mathrm{e}} \Gamma(X) $
Error function	ERF	1	1	erf(X)
Complementary error function	ERFC	1	1	$1 - \operatorname{erf}(X)$

Input> 0.5 1.6 beta

Input> 2 gamma

## 5-6. Integer roundings

Integer roundings are here:

Function	Keyword	R	D	Computation
Elear function	FLOOR	1	1	[X]
Floor function	FLR	1		
Ceiling function	CEIL	1	1	[X]
Round	ROUND	1	1	IV + 0.51
	RND	1	1	[X + 0.5]

Input> -2.2 flr

EX 2 
$$[\pi]$$

Input> pi ceil

# 5-7. Functions for integers

Functions for integers such as GCD and LCM are here:

Function	Keyword	R	D	Computation
Factorial	FACT	1	1	<i>X</i> !
ractoriai	!	] 1	1	
Greatest common divisor	GCD	1	1	GCD(Y,X)
Least common multiple	LCM	1	1	LCM(Y, X)
Permutation	PERM	1	1	$_{Y}P_{X}$
Combination	СОМВ	1	1	$_{Y}C_{X}$

 $EX 1 _5P_2$  Input> 5 2 perm

EX 2 LCM(12,50)

Input> 12 50 lcm

#### 6-1. Percent calculation

Percent calculations such as including tax are here:

Function	Keyword	R	D	Computation
V margant of V	PERC	2	1	$Y \times \frac{X}{100}$
X percent of Y PC	PC	2		
Dalta paraant batwaan V and V	DPERC	2	2	$\frac{X-Y}{Y} \times 100$
Delta percent between Y and X  DP	DP		۷	
Include tax	INTAX	2	2	$Y \times \frac{100 + X}{100}$
Exclude tax	EXTAX	2	2	$Y \times \frac{100}{100 + X}$

These functions support only scalars.

6-2. Time conversion

Conversions between sec, min, hour, day and week.

Function	Keyword	R	D	Computation
Seconds to ninutes	STOM	1	1	X/60
Seconds to hours	STOH	1	1	X/3600
Seconds to days	STOD	1	1	X/86400
Seconds to weeks	STOW	1	1	X/604800
Minutes to seconds	MTOS	1	1	$X \times 60$
Minutes to hours	МТОН	1	1	X/60
Minutes to days	MTOD	1	1	X/1440
Minutes to weeks	MTOW	1	1	X/10080
Hours to seconds	HTOS	1	1	<i>X</i> × 3600
Hours to minutes	НТОМ	1	1	$X \times 60$
Hours to days	HTOD	1	1	X/24
Hours to weeks	HTOW	1	1	X/168
Days to seconds	DTOS	1	1	X × 86400
Days to minutes	DTOM	1	1	<i>X</i> × 1440
Days to hours	DTOH	1	1	X × 24
Days to weeks	DTOW	1	1	X/7
Weeks to seconds	WTOS	1	1	<i>X</i> × 604800
Weeks to minutes	WTOM	1	1	X × 10080
Weeks to hours	WTOH	1	1	X × 168
Weeks to days	WTOD	1	1	$X \times 7$

These functions support only scalars.

EX 2 45 min to hours

Input> 45 mtoh

EX 1 65536 sec to days

Input> 65536 stod

#### 6-3. DMS conversion

DMS conversion divides a scalar value into degrees / minutes / seconds.

Inverse DMS conversion combines degrees / minutes / seconds into a value.

Function	Keyword	R	D	Computation
Decimal deg to deg/min/sec	TODMS	1	1	$Z \leftarrow D$ $Y \leftarrow M$
Decimal deg to deg immissee	mar deg to deg/mm/see		-	$X \leftarrow S$
Deg/min/sec to decimal deg	DMSTO	3	3	$Z + \frac{Y}{60} + \frac{X}{3600}$

These functions support only scalars.

EX 1 4096 sec to h:m:s

EX 2 30°20′10″ to degrees

Input> 4096 stoh todms

Input> 30 20 10 dmsto

#### 6-4. Whole stack calculations

You can find sum or infinite product in the stack.

Function	Keyword	R	D	Computation
Sum	SUM	N>1	N	$\sum\nolimits_{i=1}^{n}x_{i}$
Infinite product	PROD	N>1	N	$\prod\nolimits_{i=1}^{n} x_{i}$
Arithmetic average	AVR	N>1	N	$\frac{1}{n} \sum_{i=1}^{n} x_i$
Geometric average	GAVR	N>1	N	$\sqrt[n]{\prod_{i=1}^n x_i}$
Harmonic average	HAVR	N>1	N	$\frac{n}{\sum_{i=1}^{n} x_i^{-1}}$

If there are errors in the process of the functions, the calculation is cancelled and the stack keeps on.

### Other versions available:

Function	Keyword	R	D	Computation
Partial sum	PSUM	N>2	M+1	
Partial product	PPROD	N>2	M+1	
Partial arithmetic average	PAVR	N>2	M+1	
Partial geometric average	PGAVR	N>2	M+1	
Partial harmonic average	PHAVR	N>2	M+1	
Sum without drop	SUMW	N>1	0	
Infinite product without drop	PRODW	N>1	0	
Arithmetic average without drop	AVRW	N>1	0	
Geometric average without drop	GAVRW	N>1	0	
Harmonic average without drop	HAVRW	N>1	0	
Partial sum without drop	PSUMW	N>2	1	
Partial product without drop	PPRODW	N>2	1	
Partial arithmetic average without drop	PAVRW	N>2	1	
Partial geometric average without drop	PGAVRW	N>2	1	
Partial harmonic average without drop	PHAVRW	N>2	1	

# 6-5. Multiply by prefix

Multiplication by prefix means the removal of prefix. For instance, if you have to get meter from kilometer, multiply by 1000, which means kilo.

Here is the list of multiplications by prefix:

Function	Keyword	R	D	Computation
Multiply by yocto	<b>УОСТО</b>	1	1	$X \times 10^{-24}$
Multiply by zepto	ZEPTO	1	1	$X \times 10^{-21}$
Multiply by atto	ATTO	1	1	$X \times 10^{-18}$
Multiply by femto	FEMTO	1	1	$X \times 10^{-15}$
Multiply by pico	PICO	1	1	$X \times 10^{-12}$
Multiply by nano	NANO	1	1	$X \times 10^{-09}$
Multiply by micro	MICRO	1	1	$X \times 10^{-06}$
Multiply by milli	MILLI	1	1	$X \times 10^{-03}$
Multiply by centi	CENTI	1	1	$X \times 10^{-02}$
Multiply by deci	DECI	1	1	$X \times 10^{-01}$
Multiply by deca	DECA	1	1	$X \times 10^{+01}$
Multiply by hecto	НЕСТО	1	1	$X \times 10^{+02}$
Multiply by kilo	KILO	1	1	$X \times 10^{+03}$
Multiply by mega	MEGA	1	1	$X \times 10^{+06}$
Multiply by giga	GIGA	1	1	$X \times 10^{+09}$
Multiply by tera	TERA	1	1	$X \times 10^{+12}$
Multiply by peta	PETA	1	1	$X \times 10^{+15}$
Multiply by exa	EXA	1	1	$X \times 10^{+18}$
Multiply by zetta	ZETTA	1	1	$X \times 10^{+21}$
Multiply by yotta	YOTTA	1	1	$X \times 10^{+24}$
Multiply by kibi	KIBI	1	1	$X \times 2^{10}$
Multiply by mebi	MEBI	1	1	$X \times 2^{20}$
Multiply by gibi	GIBI	1	1	$X \times 2^{30}$
Multiply by tebi	TEBI	1	1	$X \times 2^{40}$
Multiply by pebi	PEBI	1	1	$X \times 2^{50}$
Multiply by exbi	EXBI	1	1	$X \times 2^{60}$
Multiply by zebi	ZEBI	1	1	$X \times 2^{70}$
Multiply by yobi	YOBI	1	1	$X \times 2^{80}$

# 6-6. Divide by prefix

Division by prefix means the addition of prefix. For instance, if you have to get millimeter from meter, divide by 0.001, which means milli.

Here is the list of divisions by prefix:

Function	Keyword	R	D	Computation
Divide by yocto	тоуосто	1	1	$X/10^{-24}$
Divide by zepto	TOZEPTO	1	1	$X/10^{-21}$
Divide by atto	TOATTO	1	1	$X/10^{-18}$
Divide by femto	TOFEMTO	1	1	$X/10^{-15}$
Divide by pico	TOPICO	1	1	$X/10^{-12}$
Divide by nano	TONANO	1	1	$X/10^{-09}$
Divide by micro	TOMICRO	1	1	$X/10^{-06}$
Divide by milli	TOMILLI	1	1	$X/10^{-03}$
Divide by centi	TOCENTI	1	1	$X/10^{-02}$
Divide by deci	TODECI	1	1	$X/10^{-01}$
Divide by deca	TODECA	1	1	$X/10^{+01}$
Divide by hecto	ТОНЕСТО	1	1	$X/10^{+02}$
Divide by kilo	TOKILO	1	1	$X/10^{+03}$
Divide by mega	TOMEGA	1	1	$X/10^{+06}$
Divide by giga	TOGIGA	1	1	$X/10^{+09}$
Divide by tera	TOTERA	1	1	$X/10^{+12}$
Divide by peta	TOPETA	1	1	$X/10^{+15}$
Divide by exa	TOEXA	1	1	$X/10^{+18}$
Divide by zetta	TOZETTA	1	1	$X/10^{+21}$
Divide by yotta	TOYOTTA	1	1	$X/10^{+24}$
Divide by kibi	TOKIBI	1	1	$X/2^{10}$
Divide by mebi	TOMEBI	1	1	$X/2^{20}$
Divide by gibi	TOGIBI	1	1	$X/2^{30}$
Divide by tebi	TOTEBI	1	1	X/2 <sup>40</sup>
Divide by pebi	TOPEBI	1	1	$X/2^{50}$
Divide by exbi	TOEXBI	1	1	$X/2^{60}$
Divide by zebi	TOZEBI	1	1	$X/2^{70}$
Divide by yobi	TOYOBI	1	1	X/2 <sup>80</sup>

# 6-7. Angle conversion

Angle conversions here:

Function	Keyword	R	D	Computation
Radian to degree	RTOD	1	1	$180X/\pi$
Radian to grace	RTOG	1	1	$200X/\pi$
Degree to radian	DTOR	1	1	$\pi X / 180$
Degree to grade	DTOG	1	1	10 <i>X</i> /9
Grade to radian	GTOR	1	1	$\pi X/200$
Grade to degree	GTOD	1	1	9X/10

# 6-8. Angle calculation

Complementary / supprementaly angle:

Function	Keyword	R	D	Computation
Complementary angle [1]	CANG	1	1	
Complementary angle (Radian)	CANGR	1	1	$\pi/2-X$
Complementary angle (Degree)	CANGD	1	1	90 – X
Complementary angle (Grade)	CANGG	1	1	100 – X
Supplementary angle [1]	SANG	1	1	
Supplementary angle (Radian)	SANGR	1	1	$\pi - X$
Supplementary angle (Degree)	SANGD	1	1	180 – X
Supplementary angle (Grade)	SANGG	1	1	200 – X

# [1] Depends on angle mode

### 6-9. Ratio

Convert a rational number into two integers.

Function	Keyword	R	D	Computation
Datio	RATIO	1	1	$Y \leftarrow Numerator$
Ratio	KATIU	1	1	$X \leftarrow Denominator$

#### 6-10. Random numbers

You can generate random numbers:

Function	Keyword	R	D	Computation
Random integer	RAND	0	0	Push Int
Random floating	FRAND	0	0	Push Flt

# IMPORTANT

A random integer has 63 bits and random floating is generated from one.

The algorithm of random generator is mersenne twister.

6-11. Cast

You can cast data types:

Function	Keyword	R	D	Computation
Cast into integer	TOINT	1	1	
Cast into floating	TOFLT	1	1	
Cast into rational	TORAT	1	1	
Cast into bool	TOBOOL	1	1	
Cast into byte	TOBYTE	1	1	
Cast into word	TOWORD	1	1	
Cast into dword	TODWORD	1	1	
Cast into qword	TOQWORD	1	1	

# IMPORTANT

You can approximate floating to rational with "cast into rational".

The approximation is using continued fraction.

# 6-12. Calculations for engineers

These are useful calculations for engineers:

Function	Keyword	R	D	Computation
Multiply by $2\pi$	TPIX	1	1	$2\pi X$
Divide by $2\pi$	DTPI	1	1	$X/2\pi$
Parallel	PARA	1	1	$(Y^{-1} + X^{-1})^{-1}$
To decibel	TODB	1	1	$10\log_{10} X $
Decibel to	DBTO	1	1	$10^{\frac{X}{10}}$

## 6-13. Health calculations

These calculations are extras:

Function	Keyword	R	D	Computation
Discomfort index	DISCOM	2	2	$0.81Y - 0.01X \times (0.99Y - 14.3) + 46.3$
Body mass index	BMI	2	2	$X/(Y/100)^2$

## 7-1. Display of complex numbers

This software displays complex numbers as following:

Mode	Expression	Display
Default	2 + 3 <i>i</i>	2 + i3
Euler	12∠56[deg]	12 exp(+i56.d)
(degree)	12230[ueg]	12 exp(+130.u)
Euler	12∠0.9[rad]	12 ovr(+i0 0)
(radian)	1220.9[rau]	12 exp(+i0.9)
Euler	12 (62[ama]	12 ovn/1362 g)
(grade)	12∠62[gra]	12 exp(+i62.g)

Type "EULER" or "EUL" to toggle Euler mode. If Euler mode is enabled, complex numbers are shown as polar display.

The argument display depends on angle mode. Use the keywords "DEG", "RAD" or "GRA" to change angle mode.

Function	Keyword
Eular diaplay	EULER
Euler display	EUL
Degree mode	DEG
Radian mode	RAD
Grade mode	GRAD
	GRA

When Euler display is on, even scalars are treated as complex numbers so its argument is displayed if its value is not 0.

## 7-2. How to make complex numbers

There are three ways to make complex numbers.

## IMPORTANT

Real and imaginary part accept only scalars.

7-2-1. Input imaginary and add or subtract

Try to make "2+i3".

Input> 2 i3 +

#### 7-2-2. Make complex from real and imaginary part

Push real and imaginary part in turn and make complex. Use the keyword "MKCMP" or "MKC" to make complex from rectangular.

# Input> 2 3

#	TYPE	VALUE	
4			
Z			Real
Υ	Integer	2	
Х	Integer	3	Imaginary

## Input> mkc

	1	T	7		
#	TYPE	VALUE			
4					
Z				C1	
Υ				Complex	
Х	Complex	2 + i3	4	generated	

### 7-2-3. Make complex from absolute value and argument

Push absolute value and argument in turn and make complex. Use the keyword "MKE" to make complex from polar.

This keyword depends on angle mode. For example, make 1.5∠30° in degree mode.

Input> 1.5 30

#	TYPE	VALUE	
4			
Z			Absolute
Υ	Floating	1.5	
Х	Integer	30	Argument

## Input> mke

#	TYPE	VALUE		
4				
Z			C 1	
Υ			Complex	
Х	Complex	1.29903811 + i0.75	generated	ل

Radian version is "MKER".

Degree version is "MKED".

Grade version is "MKEG".

You can generate complex with following keywords:

Function	Keyword	R	D	Computation
Make complete from necton cycles	MKCMP	1	_	Y + iX
Make complex from rectangular	MKC	2	2	
Make complex from polar	MKE	2	2	$Y \angle X$
Make complex from polar (radian)	MKER	2	2	<i>Y∠X</i> [rad]
Make complex from polar (degree)	MKED	2	2	<i>Y∠X</i> [deg]
Make complex from polar (grade)	MKEG	2	2	<i>Y∠X</i> [gra]

# 7-3. Complex calculations

You can operate complex calculations:

Function	Keyword	R	D	Computation
Real part	RE	1	1	Re(X)
Imaginary part	IM	1	1	Im(X)
Complex argument	ARG	1	1	arg X
Complex argument (radian)	ARGR	1	1	arg X [rad]
Complex argument (degree)	ARGD	1	1	arg X [deg]
Complex argument (grade)	ARGG	1	1	arg X [gra]
Complex conjugation	CONJ	1	1	conj(X)

Complex magnitude is "ABS".

EX 1 
$$arg(1+i2)$$
 EX 3  $conj(6+i3)$  Input> 1 2 mkc arg Input> 6 3 mkc conj EX 2  $Re(15 \angle 32^\circ)$  Input> 15 32 mked re

## 7-4. Disassemble complex

You can disassemble complex numbers:

Function	Keyword	R	D	Computation
Real and imaginary	DETM	1	1	$Y \leftarrow \operatorname{Re}(X)$
Kear and imaginary	REIM		1	$X \leftarrow \operatorname{Im}(X)$
Magnitude and argument	MAGA	1	1	$Y \leftarrow  X $
Magnitude and argument	MAGA	1	1	$X \leftarrow \arg X$
Magnitude and argument (radian)	MAGAR	1	1	$Y \leftarrow  X $
wagiitude and argument (radian)			_	$X \leftarrow \arg X [\text{rad}]$
Magnitude and argument (degree)	MAGAD	1	1	$Y \leftarrow  X $ $X \leftarrow \arg X [\deg]$
wagintude and argument (degree)			1	$X \leftarrow \arg X [\deg]$
Magnitude and argument (grade)	MAGAG	1	1	$Y \leftarrow  X $
iviagintude and argument (grade)		_	_	$X \leftarrow \arg X [\operatorname{gra}]$

EX 1  $15\angle32^{\circ}$  to Re/Im part

Input> 15 32 mked reim

EX 2 5 + i3 to magnitude and arg (deg)

Input> 5 3 mkc magad

## 7-5. Complex functions

This software supports complex functions:

- Square root, cubic root
- Power, logarithm
- Trigonometric functions
- Hyperbolic functions

Complex trigonometric functions are available only in radian.

### 8-1. Unsigned decimal and Boolean

This software displays unsigned decimal and Boolean as following:

Type/mode	Value	Display
Daalaan	TRUE	Т
Boolean	FALSE	F
Binary mode	255	0b11111111
Octal mode	255	0377
Signed decimal mode	255	-1
Unsigned decimal mode	255	255
Hexadecimal mode	255	0xFF

### 8-2. Bit length

You can operate logical calculations in calculation mode.

This software supports 8, 16, 32, 64 bits. The bit length setting is shown in the display. Switch the mode to change the bit length.

Mode	Keyword	Symbol	
8-bit mode	BYTE	(Byta)	
(byte)	DITE	(Byte)	
16-bit mode	WORD	(Word)	
(word)	WORD	(word)	
32-bit mode	DWORD	(Duand)	
(dword)	DWOND	(Dword)	
64-bit mode	OHORD	(Owond)	
(qword)	QWORD	(Qword)	

Set bit length and the bit length symbol changes.

Please notice that if you input too large value for selected bit length, the software masks its lower N-bit (N is selected length) and push the result.

#### 8-3. N-ary number switching

進数表示の設定は、計算設定・状態表示領域で確認できます。下表の画面表示のいずれか が表示されています。

表示を切り替えたい場合、下表のキーワードを用います。

Mode	Keyword	Symbol
Binary display	BIN	(Bin)
Octal display	ОСТ	(0ct)
Signed decimal display	SDEC	(Sdec)
Unsigned decimal display	UDEC	(Udec)
Hexadecimal display	HEX	(Hex)

Set N-ary and the N-ary symbol changes.

#### 8-4. Input binary and Boolean

Input value as binary (unsigned integer) to operate logical calculations.

Boolean: True value is "TRUE" or "T" and false value is "FALSE" or "F".

Unsigned: Type "u" and postfix non-signed integer.

Binary: Type "0b" and postfix binary expression using 0 and 1.

Octal value: Type "0o" and postfix octal expression using 0 to 7.

Hex value: Type "0x" and postfix hexadecimal expression using 0 to 9 and A to F.

The input data is shown as selected N-ary display mode. For example, input binary "0b1010" and the display is "0x000000A" in hexadecimal mode.

## Input> 0b1010

#	TYPE	VALUE
4		
Z		
Υ		
Х	Dword	0x0000000A

You can push binaries and Booleans at one time.

# Input> t f

#	TYPE	VALUE
4		
Z	Dword	0x0000000A
Υ	Boolean	Т
Х	Boolean	F

# 8-5. Fundamental logical calculations

Here is the list of fundamental logical calculations:

Function	Keyword	R	D	Computation
Bitwise NOT	NOT	1	1	$ar{X}$
Ditwise NOT	~	1		Λ
Bitwise AND	AND	2	2	$Y \wedge X$
Ditwise AND	&			$I \wedge X$
Bitwise OR	OR	2	2 2	$Y \vee X$
Ditwise OK				IVA
Bitwise XOR	XOR	2	2	$Y \oplus X$
Bitwise NAND	NAND	2	2	$\overline{Y \wedge X}$
Bitwise NOR	NOR	2	2	$\overline{Y \vee X}$

EX 1 0x1234 & 0b0111

Input> 0x1234 0b0111 and

EX 2 not(65535)

Input> u65535 not

8-6. Bit shift Bit shifts are here:

Function	Keyword	R	D	Computation	
Shift left	SHL	1	1	V 1	
	<b>&lt;&lt;</b>	1		X << 1	
Shift logical right	SHR	1	1	X >> 1	
	>>			X >> 1	
Shift arithmetic right	SAR	1	1	X >>> 1	
	>>>			X >>> I	
Shift byte left	SBL	1	1	X << 8	
Shift byte right	SBR	1	1	X >> 8	
Shift nibble left	SNL	1	1	X << 4	
Shift nibble right	SNR	1	1	X >> 4	

EX 1 0x1234 & 0b0111

Input> 0x1234 0b0111 and

EX 2 not(65535)

Input> u65535 not

## 8-7. Rotate

Bit rotates are here:

Function	Keyword	R	D	Computation
Rotate left	ROL	1	1	Rotate X Left
Rotate right	ROR	1	1	Rotate X Right

EX rol(31)

Input> u31 rol

# 8-8. Other functions that support unsigned integer

Function	Keyword	R	D	Computation
Increment	INC	1	1	<i>X</i> + 1
	++	1	4	Λ T I
Decrement	DEC	1	1	X-1
		1		
Add	ADD	2	2	Y + X
	+			
Subtract	SUB	2	2	Y - X
	-			
Multiply	MUL	2	2	$Y \times X$
	*			
Divide	DIV	2	2	Y/X
	/			
Negate	NEG	1	1	-X
	PM			

# IMPORTANT

The addition of 2 Booleans is XOR, and the multiplication of 2 Booleans is AND. If you increment Boolean, the result is always true.

## 8-9. Whole-stack logical calcultions

You can operate logical calculations for whole-stack.

Function	Keyword	R	D	Computation
All AND	ALLAND	N>1	N	$x_1 \wedge x_2 \dots$
All OR	ALLOR	N>1	N	$x_1 \lor x_2 \dots$
All XOR	ALLXOR	N>1	N	$x_1 \oplus x_2 \dots$

# 9. Vector calculations

### 9-1. Display of vectors

This software displays vectors as following:

Туре	Math expr.	Display
Horizontal [Row]	[1 2 3]	[1, 2, 3]
Vertical (Col)	$\begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix}$	(3, 2, 1)

#### 9-2. Making of vector

You can include scalars, complex or even binaries in vectors.

The input of vectors is complicated. I recommend using register function. Please read chapter 11 to get more information.

You can make vector with the following keywords:

Function	Keyword	R	D	Computation
Make row tuple	MRTUP	N	N	Push Tup.R
Make column tuple	MCTUP	N	N	Push Tup.C

There are three steps for making a vector:

- 1. Push elements of a vector
  - ... Push data in turn.
- 2. Push the number of elements the vector contains
  - ... Set the dimension of the vector.
- 3. Call making function
  - ... The vector is pushed.

#### NOTICE

You can include integers, floatings, rationals, complexes, Booleans and unsigned integers in a vector.

So, let us make row tuple [1 + i2 6].

### (1) Push elements

Input> 1 2 mkc 6

#	TYPE	VALUE	
4			
Z			
Υ	Complex	1 + i2	
Х	Integer	6	Push in turn

### (2) Push number of elements

Input> 2

#	TYPE	VALUE	
4			
Z	Complex	1 + i2	
Υ	Integer	6	
Х	Integer	2	Dimension

### (3) Make row tuple

Input> mrtup

#	TYPE	VALUE	
4			
Z			
Υ			Make row
Х	Tuple[Row]	[1 + i2, 6]	tuple

Making column tuple is similar with this case.

You can make unit vectors easily.

Function	Keyword	R	D	Computation
Make row unit tuple	MRUTUP	2	2	Push Tup.R
Make column unit tuple	MCUTUP	2	2	Push Tup.C

These functions requires 2 arguments: a dimension and a position.

- 1. Push a integer as a dimension
- 2. Push a integer as a position (starting with 1)
- 3. Call making function

Make (0 1 0).

### (1) Push the dimension

Input> 3

#	TYPE	VALUE	
4			
Z			
Υ			
Х	Integer	3	Dimension

### (2) Push the position

Input> 2

#	TYPE	VALUE	
4			
Z			
Υ	Integer	3	2
Х	Integer	2	Position

### (3) Make column unit tuple

Input> mcutup

#	TYPE	VALUE	
4			
Z			
Υ			
Х	Tuple(Col)	(0, 1, 0)	Generated

### 9-3. Extract element from tuple

Use the keyword "TGET" to extract one element from a tuple.

Please make sure Y is a tuple and X is an integer as a position (starting with 1) to extract.

Function	Keyword	R	D	Computation
Get element from tuple	TGET	2	2	Extract

This function drops 2 data, so the vector from that you extract is dropped. I recommend storing the tuple to a register and call to extract.

Please read chapter 11 to make comprehension of using register function.

You can crave a tuple into elements.

Function	Keyword	R	D	Computation
Chara	CUT	1	1	
Crave up	CRAVE	1	1	

The used tuple is dropped and the extracted elements are pushed in turn.

Let us extract the second element from (6 9 12).

### (0) Make sure that the tuple exists

#	TYPE	VALUE
4		
Z		
Υ		
Х	Tuple[Col]	(6, 9, 12)

### (1) Set a position.

### Input> 2

#	TYPE	VALUE	
4			
Z			
Υ	Tuple[Col]	(6, 9, 12)	
Х	Integer	2	Position

### (2) Extract

Input> tget

#	TYPE	VALUE	
4			
Z			
Υ			
Х	Integer	9	Extracted

#### 9-4. Four arithmetics of vectors

The four aritmetics keywords of vectors are same as those of scalars.

Please check that the calculations are defined.

#### 9-5. Inner / outer product

Use the keywords to calculate inner / outer product:

Function	Keyword	R	D	Computation
In more many divises	INNER	2	2	$\vec{Y}\cdot\vec{X}$
Inner product	DOT			
Outer product	OUTER	2	2	$\vec{Y}  imes \vec{X}$
Outer product	CROSS 2		$Y \times X$	

Outer product suppots only 3-dimensional tuples.

#### 9-6. Norms of vectors

Here is the keywords of norms of vectors:

Function	Keyword	R	D	Computation
Euclid norm	NORM	1	1	$\sqrt{\sum_{i=1}^{\infty}  x_i ^2}$
Euclid norm squared	NSQ	1	1	$\sum\nolimits_{i=1}^{\infty} \lvert x_i \rvert^2$
Lp-norm	PNORM	2	2	$\left(\sum_{i=1}^{\infty}  y_i ^x\right)^{1/x}$
Max norm	MAXNORM	1	1	$\max( x_1 ,  x_2 ,  x_n )$

Euclid norm, Euclid norm squared ana maxnorm require one vector.

For example, type following to find the Euclid norm of [3 5 7]:

Lp-norm requires one vector and an integer as a dimension.

Type following to find the third norm of [7 8 9]:

### 9-7. Transpose vectors

Use the keyword "TRANS" to transpose vectors.

Function	Keyword	R	D	Computation
Transpose	TRANS	1	1	$X^T$

This function supports matrices.

#### 10-1. Display of matrices

This software handles matrices as tuples of row tuples.

Math expr.	Display		
$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$	[[1, 2, 3], [4, 5, 6], [7, 8, 9]]		

#### 10-2. Making of matrices

This software supports matrix calculations. Matrices of this software can include scalars, complexes, Booleans and unsigned integers.

The input of matrices is complicated. I recommend using register function. Please read chapter 11 to get more information.

Use the keyword "MKMAT" to make a matrix.

Function	Keyword	R	D	Computation
Make matrix	MKMAT	N	N	Push Mat

There are three steps for making a vector:

- 1. Prepare same dimensional and directional vectors.
  - ... Make sure vectors are all row or all column.
- 2. Push an integer as a number of vectors.
  - ... The integer must be greater than zero.
- 3. Call making function
  - ... Make a matrix from vectors.

#### NOTICE

Matrices include row tuples. The data types that tuples cannot include are not supported in matrices.

Let us input matrix A:

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

#### (1-1) Make two row vectors

Input> 1 2 2 mrtup 3 4 2 mrtup

#	TYPE	VALUE	
4			
Z			
Υ	Tuple[Row]	[1, 2]	
Х	Tuple[Row]	[3, 4]	Added in turn

### (1-2) Set a number of vectors

Input> 2

#	TYPE	VALUE	
4			
Z	Tuple[Row]	[1, 2]	
Υ	Tuple[Row]	[3, 4]	
Х	Integer	2	Number

### (1-3) Make matrix

Input> mkmat

#	TYPE	VALUE	
4			
Z			
Υ			
Χ	Matrix	[[1, 2], [3, 4]]	Generated

### (2-1) Push two column tuple

Input> 1 3 2 mctup 2 4 2 mctup

#	TYPE	VALUE	
4			
Z			
Υ	Tuple(Col)	(1, 3)	
Х	Tuple(Col)	(2, 4)	Pushed in turn

### (2-2) Set a number of vectors

### Input> 2

#	TYPE	VALUE	
4			
Z	Tuple(Col)	(1, 3)	
Υ	Tuple(Col)	(2, 4)	
Х	Integer	2	Number

### (2-3) Make matrix

Input> mkmat

#	TYPE	VALUE	
4			
Z			
Υ			
Х	Matrix	[[1, 2], [3, 4]]	Generated

Make sure the sizes and directions of all vectors to make a matrix are same.

You can make a unit matrix easily. Use the keyword "MKUMAT".

Function	Keyword	R	D	Computation
Make unit matrix	MKUMAT	1	1	Push Mat

Set an integer as a dimension and call the function. For instance, input this to make 3-dim unit matrix:

Input> 3 mkumat

### 10-3. Get element or tuple from matrix

Get a tuple or a element from matrix to use following keywords:

Function	Keyword	R	D	Computation
Get element from matrix	MGET	3	3	Extract
Get row tuple from matrix	MGETR	2	2	Extract
Get column tuple from matrix	MGETC	2	2	Extract

These functions drop a matrix. I recommend using register function.

Please read chapter 11 to get more information about registers.

You can crave up matrices.

Function	Keyword	R	D	Computation
C	CUT	1	1	
Crave up	CRAVE	1	1	

A matrix is craved up into row tuples and they are pushed in turn.

Go on to the next pages to get usages of "MGET", "MGETR" and "MGETC".

#### 10-3-1. Get element from matrix

Use the keyword "MGET" to get an element from a matrix.

Make sure Z is matrix, Y is position i, X is position j. The position counting starts with 1.

Try to extract element (1,2) from matrix [[1, 2], [3, 4]].

### (0) Matrix is pushed

#	TYPE	VALUE
4		
Z		
Υ		
Х	Matrix	[[1, 2], [3, 4]]

### (1) Select a position of an element

Input> 1 2

#	TYPE	VALUE	
4			Position i
Z	Matrix	[[1, 2], [3, 4]]	T OSITION 1
Υ	Integer	1	
Х	Integer	2	Position j

### (2) Get an element from matrix

Input> mget

	<u> </u>		
#	TYPE	VALUE	
4			
Z			
Υ			
Х	Integer	2	Extracted

#### 10-3-2. Get tuple from matrix

You can get a tuple from a matrix. "MGETR" is the row tuple version and "MGETC" is the column tuple version.

Make sure Y is matrix and X is position. The position counting starts with 1.

Try to extract second column tuple from [[1, 2], [3, 4]].

#### (0) Matrix is pushed

#	TYPE	VALUE
4		
Z		
Υ		
Х	Matrix	[[1, 2], [3, 4]]

#### (1) Select a position

### Input> 2

#	TYPE	VALUE	
4			
Z			
Υ	Matrix	[[1, 2], [3, 4]]	
Х	Integer	2	Position

### (2) Get a column tuple from matrix

Input> mgetc

#	TYPE	VALUE	
4			
Z			
Υ			
Х	Tuple(Col)	(2, 4)	Extracted

### 10-4. Four arithmetics of matrices

The four arithmetics keywords are similar with those of scalars.

EX 1

$$\begin{bmatrix} 3 & 7 \\ 9 & 5 \end{bmatrix} - \begin{bmatrix} 2 & 6 \\ 2 & 4 \end{bmatrix}$$

Input> 3 7 2 mrtup 9 5 2 mrtup 2 mkmat
Input> 2 6 2 mrtup 2 4 2 mrtup 2 mkmat

Input> -

EX 2

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \begin{pmatrix} 5 \\ 6 \end{pmatrix}$$

Input> 1 2 2 mrtup 3 4 2 mrtup 2 mkmat

Input> 5 6 2 mctup

Input> \*

#### 10-5. Determinant and inverse matrix

Here is determinant and finding inverse matrix:

Function	Keyword	R	D	Computation
Determinant	DET	1	1	det X
Invert	INV	1	1	$X^{-1}$

These functions support only square matrices. You cannot find inverse matrix of A if the determinant of A is zero.

EX

$$\begin{bmatrix} \sqrt{2} & 1 \\ 1 & \sqrt{2} \end{bmatrix}^{-1}$$

Input> 2 sqrt 1 2 mrtup 1 2 sqrt 2 mrtup 2 mkmat inv

#### 10-6. Transpose matrix

Here is the list of transpose functions:

Function	Keyword	R	D	Computation
Transpose	TRANS	1	1	$X^T$
Homeitian transpaga	HTRANS	1	1	$conj(X^T)$
Hermitian transpose	НСОИЈ	1	1	Conj(x · )

Hermitian transpose function transposes matrix or vector and conjugate each element in it.

#### 10-7. Other matrix functions

Here is the list of other matrix functions:

Function	Keyword	R	D	Computation
Trace	TRACE	1	1	tr(X)

Trace function supports only square matrices.

#### 11-1. What is register

A register is kind of a memory. Each register in this software are independent of the stack. You can calculate more quickly with register function. There are 26 registers:  $RA \sim RZ$ .

Std: 15/15,	Stack: 3,	History: 0/10	
# TYPE RA: Floating RB: RC:	: : : :		VALUE 3.14159265358979
Z: Integer Y: Integer X: Integer	:		4 5 6
STORE to seld View / Undo			er / apx / json

You can store one data to each register and can load or delete any time.

Even if the stack is changed or cleared, registers keep on.

Registers can hold any data: scalars, vectors, errors even strings.

This manual uses following tables:

#	TYPE	VALUE		
RA				Registers
RB			4	RA - RZ
Z				
Υ				
Х				

This table shows X, Y and Z in stack and RA and RB in registers.

### 11-2. Register display

Type "REGISTER" or "REG" to switch register display.

If register display is enabled, the symbol [Reg] is displayed.

You can change display page of registers:

Function	Keyword
Creitale magistan digulary	REGISTER
Switch register display	REG
Nove many of magistans	REGNEXT
Next page of registers	RN
Dunning of an interes	REGPREV
Previous page of registers	RP
First naga of registers	REGFIRST
First page of registers	RF

See also chapter 3 and chapter 4.

### IMPORTANT

Switching register display function and register page changing functions do not affect registers. So you can use registers without displaying registers.

### 11-3. Store to selected register

You can store X to selected register. Then X is dropped.

Use the following keywords to storing functions:

Function	Keyword	R	D
Store to RA	STRA		
Store to RB	STRB	1	1
		1	1
Store to RZ	STRZ		

Use the format "STR?" and replace "?" by one alphabet.

Let us store the integer 5 to RA.

### (1) Push

### Input> 5

#	TYPE	VALUE	
RA			
RB			
Z			
Υ			Store from
Х	Integer	5	$\left\langle  \text{only X} \right\rangle$

# (2) Store to RA

Input> stra

#	TYPE	VALUE	
RA	Integer	5	Stored
RB			
Z			
Υ			
Х			

If the selected register has data, the data is overwritten.

### (1) Initial state

#	TYPE	VALUE	Already
RA	Integer	5	stored
RB			
Z			
Υ			
Х	Integer	7	

### (2) Push

## Input> 9

#	TYPE	VALUE	
RA	Integer	5	
RB			
Z			
Υ	Integer	7	Store from
Х	Integer	9	$\left  \left\langle \right  \right $ only X

# (3) Overwrite RA

Input> stra

#	TYPE	VALUE	
RA	Integer	9	Overwritten
RB			
Z			
Υ			
Х	Integer	7	

Cases of RB - RZ are similar with this.

### 11-4. Load from selected register

You can load from selected register to X. The selected register keeps its data. If it has no data, error message is displayed.

Use the following keywors to load:

Function	Keyword	R	D
Load RA	LDRA		
Load RB	LDRB	۵	0
		0	0
Load RZ	LDRZ		

Use the format "LDR?" and replace "?" by one alphabet.

Try to add RA and RB.

### (1) Initial state

#	TYPE	VALUE	
RA	Integer	9	Stored
RB	Integer	4	
Z			
Υ			
Х			

### (2) Load RA

Input> ldra

#	TYPE	VALUE	
	111.5	VALUE	
RA	Integer	9	
RB	Integer	4	
Z			
Υ			Load RA
Х	Integer	9	$\left\langle \begin{array}{c} \text{to X} \end{array} \right\rangle$

## (3) Load RB

## Input> ldrb

#	TYPE	VALUE	
RA	Integer	9	
RB	Integer	4	
Z			(1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1
Υ	Integer	9	Load RB
Χ	Integer	4	to X

### (4) Add

## Input> +

#	TYPE	VALUE	
RA	Integer	9	
RB	Integer	4	
Z			
Υ			Addition
Х	Integer	13	requires 2.

Cases of RC - RZ are similar with this.

### 11-5. Delete selected register

You can remove data in selected register.

Use the following keywords to delete selected register:

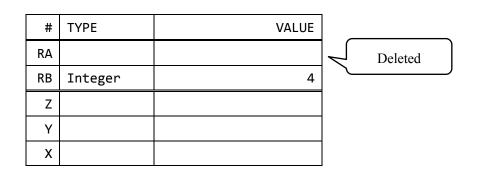
Function	Keyword	R	D
Delete RA	DELRA		
Delete RB	DELRB		0
		0	О
Delete RZ	DELRZ		

Use the format "DELR?" and replace "?" by one alphabet.

### (1) Initial state

#	TYPE	VALUE	
RA	Integer	9	Stored
RB	Integer	4	
Z			
Υ			
Х			

## (2) RA をデリート Input> delra



### 11-6. Register calculation

You can calculate with selected register and store the result to it.

Here is the list of register calculations:

Function	Keyword	R	D	Computation	
Docistor in successor	IR?	0	•	D . D . 1	
Register increment	++R?	0	0	$R \leftarrow R + 1$	
Dagistar dagrament	DR?	0	0	D , D 1	
Register decrement	R?	٥	0	$R \leftarrow R - 1$	
Decision of divisor	ADDR?	1	1	$R \leftarrow R + X$	
Register addition	+R?	1			
Decistor subtraction	SUBR?	1	1	$R \leftarrow R - X$	
Register subtraction	-R?	1		$K \leftarrow K - X$	
Docistan multiplication	MULR?		1	$R \leftarrow R \times X$	
Register multiplication	*R?	1	1	$K \leftarrow K \times X$	
Dociston division	DIVR?	1	1	D . D/V	
Register division	/R?	1		$R \leftarrow R/X$	

Operate register calculations to drop one data and overwrite selected register with the result.

Example: register addition and register increment

### (1) Initial state

#	TYPE	VALUE	
RA	Integer	9	Stored
RB	Integer	4	
Z			
Υ			
Х			

### (2) Increment RA

## Input> ira

#	TYPE	VALUE	
RA	Integer	10	Incremented
RB	Integer	4	
Z			
Υ			
Х			

### (3) Push

## Input> 1.2

#	TYPE	VALUE	
RA	Integer	10	
RB	Integer	4	
Z			
Υ			Operate with
Х	Floating	1.2	$\leq$ x

### (4) Increment RB

### Input> +rb

#	TYPE	VALUE	
RA	Integer	10	
RB	Floating	5.2	Added
Z			
Υ			
Х			

### 11-7. Register clear

You can clear all registers:

Function	Keyword	R	D	Computation
Danistan alaan	REGCLEAR		0	
Register clear	RCLR	0 0		

If you would like to delte one or some registers, use delete functions.

### IMPORTANT

You can clear registers and stack with the keyword "AC". It is all clear function.

### 11-8. Strings and registers

The registers accept strings. You can put a landmark to registers with strings.

The macro and registers combo is very affective.

See also chapter 15.

#### 12-1. Special stack operations

You can remove, insert or duplicate data or change the order of elements in the stack. There are many special stack operations.

#### 12-2. Fundamental stack operations

Here is the list of fundamental stack operations:

Function	Keyword	R	D	
Dron	DROP	1	1	
Drop	¥	1	1	
	COPY			
Duplicate [1]	С	1	1	
	DUP			
Claar	CLEAR	N <sub>2</sub> Q	N	
Clear	CLR	N>0	N	

[1] Press enter without any input to call the function

### 12-3. Order changing functions

Here is the list of order changing functions:

Function	Keyword	R	D
C.v.o.	SWAP	2	0
Swap	\$	2	О
Rotate	ROT	3	0
Unrotate	UNROT	3	0
Roll	ROLL	N	1
Roll D	ROLLD	N	1

The details are next pages:

### 12-3-1. Swap

Swap function swaps 2 data at bottom of the stack. This function requires 2 arguments. The keywords are "SWAP" and "\$".

### (1) Initial state

#	TYPE	VALUE
4		
Z	Integer	256
Υ	Integer	3
Х	Rational	9/4

### (2) Swap

### Input> swap

#	TYPE	VALUE
4		
Z	Integer	256
Υ	Rational	9/4
Х	Integer	3

### 12-3-2. Rotate

Rotate function rotates Z, Y and X. This function requires 3 arguments.

$$\begin{pmatrix} Z \\ Y \\ X \end{pmatrix} \to \begin{pmatrix} Y \\ X \\ Z \end{pmatrix}$$

The keyword is "ROT".

### (1) Initial state

#	TYPE	VALUE
4		
Z	Integer	256
Υ	Integer	3
Х	Rational	9/4

### (2) Rotate

Input> rot

#	TYPE	VALUE
4		
Z	Integer	256
Υ	Rational	9/4
Х	Integer	3

#### 12-3-3. Unrotate

Rotate function rotates Z, Y and X reversely. This function requires 3 arguments.

$$\begin{pmatrix} Z \\ Y \\ X \end{pmatrix} \to \begin{pmatrix} X \\ Z \\ Y \end{pmatrix}$$

The keyword is "UNROT".

#### 12-3-4. Roll

Roll function rotates data from selected position through X. The selected data is moved to X. The keyword is "ROLL".

#### (1) Initial state

#	TYPE	VALUE
4		
Z	Integer	256
Υ	Integer	3
Х	Rational	9/4

#### (2) Set a position

#	TYPE	VALUE
4	Integer	256
Z	Rational	9/4
Υ	Integer	3
Х	Integer	3

### (3) Roll

# Input> roll

#	TYPE	VALUE
4		
Z	Integer	3
Υ	Rational	9/4
Х	Integer	256

12-3-5. Roll D

Roll function rotates data from selected position through X reversely. X is moved to selected position.

The keyword is "ROLLD".

### 12-4. Duplicate and overwrite functions

Here is the list of duplicate and overwrite functions:

Function	Keyword	R	D
Over	OVER	2	0
Over	0	2	
Pick	PICK	N	0
Unpick	UNPICK	N	1
	XY		
Duplicate last 2 items	YX	2	0
	DUP2		
Dunlicate traige	DUPDUP	1	a
Duplicate twice	DD		ש
Duplicate last N-1 items and push N	NDUPN	1	1

The details are next pages:

12-4-1. Over

Over function duplicates Y and push it.

The keywords are "OVER" and "O".

### (1) Initial state

#	TYPE	VALUE
4		
Z		
Υ	Integer	16
Х	Integer	32

### (2) Over

### Input> o

#	TYPE	VALUE
4		
Z	Integer	16
Υ	Integer	32
Х	Integer	16

12-4-2. Pick

Pick function duplicates data in selected position.

The keyword is "PICK".

### (1) Initial state

#	TYPE	VALUE
4		
Z	Integer	256
Υ	Integer	3
Х	Rational	9/4

### (2) Set a position

## Input> 3

#	TYPE	VALUE
4	Integer	256
Z	Integer	3
Υ	Rational	9/4
Х	Integer	3

### (3) Pick

### Input> pick

#	TYPE	VALUE
4	Integer	256
Z	Integer	3
Υ	Rational	9/4
Х	Integer	256

12-4-3. Unpick

Unpick function replaces data in selected position X by Y.

The keyword is "UNPICK".

### (1) Initial state

#	TYPE	VALUE			
4					
Z					
Υ	Integer	256			
Х	Integer	3			

### (2) Push

### Input> 64

#	TYPE	VALUE
4		
Z	Integer	256
Υ	Integer	3
Х	Integer	64

### (3) Push a position

## Input> 2

#	TYPE	VALUE
4	Integer	256
Z	Integer	3
Υ	Integer	64
Х	Integer	2

### (4) Unpick

Input> unpick

#	TYPE	VALUE
4		
Z		
Υ	Integer	64
Х	Integer	3

### 12-4-4. Duplicate last 2 items

Duplicate last 2 items function duplicates  $\boldsymbol{Y}$  and  $\boldsymbol{X}$  and push them in turn.

The keywords are "XY", "YX" and "DUP2".

### (1) Initial state

#	TYPE	VALUE			
4					
Z					
Υ	Integer	16			
Х	Integer	32			

### (2) Duplicate last 2 items

Input> xy

#	TYPE	VALUE
4	Integer	16
Z	Integer	32
Υ	Integer	16
Х	Integer	32

### 12-4-5. Duplicate twice

Duplicate twice function operate duplicate function twice. The keywords are "dupdup" and "dd".

### 12-4-6. Duplicate last N-1 items and push N

Duplicate last N-1 items and push N function drops X and duplicate Y X times and then push X.

The keyword is "NDUPN".

### (1) Initial state

#	TYPE	VALUE			
4					
Z					
Υ	Integer	16			
Х	Integer	32			

### (2) Set a number of items

### Input> 2

#	TYPE	VALUE			
4					
Z	Integer	16			
Υ	Integer	32			
Х	Integer	2			

### (3) Duplicate last N-1 items and push N

Input> ndupn

#	TYPE	VALUE
4	Integer	16
Z	Integer	32
Υ	Integer	32
Х	Integer	2

### 12-5. Removal functions

Here is the list of removal functions:

Function	Keyword	R	D
Draw 2 itams	DROP2	2	2
Drop 2 items	¥¥		
Dran 2 itams	DROP3	3	3
Drop 3 items	¥¥¥		
Drop N items	DROPN	N+1	N+1
Nip	NIP	2	2
Nip N-th item	NIPN	N	2

The details are here:

12-5-1. Drop 2 items

Drop 2 items function drops 2 items.

The keywords are "DROP2" and "¥¥".

12-5-2. Drop 3 items

Drop 3 items function drops 3 items.

The keywords are "DROP3" and "\$\$\$\$".

# 12-5-3. Drop N items

Drop N items function drops X + 1 items.

The keyword is "DROPN".

## (1) Initial state

#	TYPE	VALUE
4		
Z	Integer	256
Υ	Integer	3
Х	Rational	9/4

# (2) Push a number of items to drop

# Input> 2

#	TYPE	VALUE
4	Integer	256
Z	Integer	3
Υ	Rational	9/4
Х	Integer	2

# (3) Drop N items

# Input> dropn

#	TYPE	VALUE
4		
Z		
Υ		
Х	Integer	256

12-5-4. Nip

Nip function removes Y.

The keyword is "NIP".

## (1) Initial state

#	TYPE	VALUE
4		
Z		
Υ	Integer	16
Х	Integer	32

# (2) Nip

Input> nip

#	TYPE	VALUE
4		
Z		
Υ		
Х	Integer	32

# 12-5-5. Nip N-th item

Nip N function removes data in the position X-1.

The keyword is "NIPN".

## (1) Initial state

#	TYPE	VALUE
4		
Z	Integer	64
Υ	Integer	16
Х	Integer	32

# (2) Set a position

# Input> 3

#	TYPE	VALUE
4	Integer	64
Z	Integer	16
Υ	Integer	32
Х	Integer	3

# (3) Nip N

# Input> nipn

#	TYPE	VALUE
4		
Z		
Υ	Integer	16
Х	Integer	32

# 12-6. Other stack operations

Here is the list of ther stack operations:

Function	Keyword	R	D
Number of stack items	DEPTH	0	0

Number of stack items function pushes the number of data in stack.

## IMPORTANT

See also chapter 6 to get more information about conversions.

## 13-1. Supporting units

This software supports the units as following:

	length		volume	mass	pressure
•	inv of length	•	inv of volume	velocity	energy
	area	•	time	acceleration	temperature
	inv of area		inv of time	force	

## NOTICE

These conversion functions support only scalars.

### 13-2. How to use unit conversion function

Type "CONV" or "CV" to call unit conversion. Then type 2 units to convert. The keyword "REC" calls previous conversion.

Function	Keyword	R	D	Computation	
Linit component	CONV	1	1	Unit conversion	
Unit conversion	CV				
Unit conversion (redo)	REC	1	1	Unit conversion	

You can convert X with calling the function and type "from unit" and "to unit".

For example, type this to convert inches into centimeter.

## **IMPORTANT**

If the each unit has different dimension, the combination is error.

13-3. Units of length

Here is the list of units of length:

Unit		Keyword	Ratio
Meter	[m]	М	1
Kilometer	[km]	KM	1 E+03
Centimeter	[cm]	СМ	1 E-02
Millimeter	[mm]	MM	1 E-03
Nautical mile [1]	[nmi]	NMI	1 852
Yard [1]	[yd]	YD	0.914 4
Feet [1]	[ft]	FT	0.304 8
Inch [1]	[in]	IN	0.025 4
Mile [1]	[mi]	MI	1 609.344
Fathom [2]	[fath]	FATH	1.828 8
Shaku [3]		SHAKU	10/33
<i>Sun</i> [3]		SUN	1/33
Ken [3]		KEN	20/11
Jou [3]		JOU	100/33
Chou [3]		CHOU	1200/11
<i>Ri</i> [3]		RI	43200/11

<sup>[1]</sup> International unit

<sup>[2]</sup> British fathom

<sup>[3]</sup> These are Japanese traditional units.

13-4. Units of length inverse

Here is the list of units of length inverse:

Unit		Keyword	Ratio
Per meter	[1/m]	/M	1
Per kilometer	[1/km]	/KM	1 E-03
Per centimeter	[1/cm]	/CM	1 E+02
Per millimeter	[1/mm]	/MM	1 E+03
Per nautical mile	[1/nmi]	/NMI	1/1852
Per yard	[1/yd]	/YD	1250/1143
Per feet	[1/ft]	/FT	1250/381
Per inch	[1/in]	/IN	5000/127
Per mile	[1/mi]	/MI	125/201168
Per fathom	[1/fath]	/FATH	625/1143
Per Shaku		/SHAKU	3.3
Per Sun		/SUN	33
Per Ken		/KEN	0.55
Per Jou		/J0U	0.33
Per Chou		/CHOU	11/1200
Per Ri		/RI	11/43200

13-5. Units of area
Here is the list of units of area:

Unit		Keyword	Ratio
Square meter	$[m^2]$	M2	1
Square kilometer	[km <sup>2</sup> ]	KM2	1 E+06
Square centimeter	$[cm^2]$	CM2	1 E-04
Square millimeter	[mm <sup>2</sup> ]	MM2	1 E-06
Are	[a]	ARE	1 E+02
Hectare	[ha]	НА	1 E+04
Acre	[ac]	ACRE	4 046.856 422 4
Square yard	[yd <sup>2</sup> ]	YD2	0.836 127 36
Square feet	[ft <sup>2</sup> ]	FT2	9.290 304 E-02
Square inch	[in <sup>2</sup> ]	IN2	6.451 6 E-04
Square mile	[mi <sup>2</sup> ]	MI2	2 589 988.110 336
Tsubo		TSUB0	400/121
Isse		ISSE	12000/121
Ittan		ITTAN	120000/121
Choubu		CHOUBU	1200000/121

13-6. Units of are inverse

Here is the list of units of area inverse:

Unit		Keyword	Ratio
Per square meter	$[1/m^2]$	/M2	1
Per square kilometer	[1/km <sup>2</sup> ]	/KM2	1 E-06
Per square centimeter	$[1/cm^2]$	/CM2	1 E+04
Per square millimeter	$[1/\text{mm}^2]$	/MM2	1 E+06
Per are	[1/a]	/ARE	1 E-02
Per hectare	[1/ha]	/HA	1 E-04
Per acre	[1/ac]	/ACRE	78125/316160658
Per square yard	$[1/yd^2]$	/YD2	1562500/1306449
Per square feet	[1/ft <sup>2</sup> ]	/FT2	1562500/145161
Per square inch	$[1/in^2]$	/IN2	25000000/16129
Per square mile	$[1/mi^2]$	/MI2	15625/40468564224
Per Tsubo		/TSUBO	121/400
Per Isse		/ISSE	121/12000
Per Ittan		/ITTAN	121/120000
Per Choubu		/CHOUBU	121/1200000

13-7. Units of volume Here is the list of units of volume:

Unit		Keyword	Ratio
Cubic meter	[m <sup>3</sup> ]	M3	1
Cubic kilometer	[km <sup>3</sup> ]	KM3	1 E+09
Cubic centimeter	[cm <sup>3</sup> ]	CM3	1 E-06
Cubic millimeter	[mm <sup>3</sup> ]	MM3	1 E-09
Litter	[1]	L	1 E-03
(Cubic decimeter)	[L]	L	1 E-03
Kilolitter	[kL]	KL	1
Millilitter	[mL]	ML	1 E-06
Cubic yard	[yd³]	YD3	0.764 554 857 984
Cubic feet	[ft <sup>3</sup> ]	FT3	0.028 316 846 592
Cubic inch	[in <sup>3</sup> ]	IN3	1.638 706 4 E-05
Cubic mile	[mi <sup>3</sup> ]	MI3	4 168 181 825.440 579 584
Imperial gallon	$[gal_{imp}]$	IMG	4.546 09 E-03
US gallon	[gal <sub>us</sub> ]	USG	3.785 411 784 E-03
Gou		GOU	2401/13310000
Shou		SHOU	2401/1331000
Itto		ITTO	2401/133100
Koku		KOKU	2401/13310

13-8. Units of volume inverse

Here is the list of units of volume inverse:

Unit		Keyword	Ratio
Per cubic meter	$[1/m^3]$	/M3	1
Per cubic kilometer	[1/km <sup>3</sup> ]	/KM3	1 E-09
Per cubic centimeter	[1/cm <sup>3</sup> ]	/CM3	1 E+06
Per cubic millimeter	[1/mm <sup>3</sup> ]	/MM3	1 E+09
Per litter	[1/L]	/L	1 E+03
(Per cubic decimeter)	[1/L]	/ L	1 1+03
Per kilolitter	[1/kL]	/KL	1
Per millilitter	[1/mL]	/ML	1 E+06
Per cubic yard	$[1/yd^3]$	/YD3	1953125000/1493271207
Per cubic feet	[1/ft <sup>3</sup> ]	/FT3	1953125000/55306341
Per cubic inch	$[1/in^3]$	/IN3	125000000000/2048383
Per cubic mile	$[1/mi^3]$	/MI3	1953125/8140980127813632
Per imperial gallon	$[1/gal_{imp}]$	/IMG	100000000/454609
Per US gallon	$[1/gal_{us}]$	/USG	125000000000/473176473
Per Gou		/GOU	13310000/2401
Per Shou		/SHOU	1331000/2401
Per Itto		/ITTO	133100/2401
Per Koku		/KOKU	13310/2401

13-9. Units of time

Here is the list of units of time:

Unit		Keyword	Ratio	
Second	[s]	SEC	1	
Minute	[min]	MIN	60	
Hour	[h]	HOUR	3 600	
Day	[d]	DAY	86 400	
Week	[wk]	WEEK	604 800	
Normal year	[yr]	YEAR	31 536 000	
Gregolian year		GYEAR	31 556 952	
Julian year		JYEAR	31 557 600	

## 13-10. Units of time inverse

Here is the list of units of time inverse:

Unit		Keyword	Ratio	
Per second	[1 /2]	/SEC	1	
Per second	[1/s]	/S	1	
Per minute	[1/min]	/MIN	1/60	
Per hour	[1/h]	/HOUR	1/3600	
r et noui	[1/11]	/H	1/3000	
Per day	[1 /4]	/DAY	1/86400	
rei day	[1/d]	/D	1/00400	
Per week	[4 /]-]	[1 /]-]	/WEEK	1/604800
rei week	[1/wk]	/WK	1/004000	
Dar narmal waar	[4 / ]	/YEAR	1/21526000	
Per normal year [1/yr]		/YR	1/31536000	
Per Gregolian year		/GYEAR	1/31556952	
Per Julian year		/JYEAR	1/31557600	

13-11. Units of mass

Here is the list of units of mass:

Uni	it	Keyword	Ratio
Kilogram	[kg]	KG	1
Gram	[g]	G	1 E-03
Milligram	[mg]	MG	1 E-06
Metric ton	[t]	TON	1 E+03
Long ton	[l. t. ]	LTON	1 016.046 908 8
Short ton	[s. t. ]	STON	907.184 74
Ounce	[oz av]	OZ	0.028 349 523 125
Pound	[lb av]	LB	0.453 592 37
Kan		KAN	3.75
Ryou		RYOU	3.75 E-02
Momme		MOMME	3.75 E-03
Kin		KIN	0.6

# 13-12. Units of velocity

Here is the list of units of velocity:

Unit		Keyword	Ratio
Meter per second	[m/s]	M/S	1
Meter per minute	[m/min]	M/MIN	1/60
Kilometer per second	[km/s]	KM/S	1 E+03
Vilometer ner here	[]rm /h]	KM/H	5/18
Kilometer per hour	[km/h]	KPH	5/10
Inch per second	[ips]	IPS	0.025 4
Feet per second	[fps]	FPS	0.304 8
Mile per hour	[mph]	MPH	0.447 04
Knot (Nautical mile per hour)	[kn]	KN	463/900

13-13. Units of acceleration

Here is the list of units of acceleration:

Unit		Keyword	Ratio	
Meter per second per second	$[m/s^2]$	M/S2	1	
Kilometer per hour per second	[km/h/s]	KM/H/S	F /10	
Knometer per nour per second	[KIII/II/S]	KPH/S	5/18	
Gal / Galileo	[Gal]	GAL	1 E-02	
(Centimeter per second per second)	[Gai]	UAL	1 6-02	
Inch per second per second	[ips <sup>2</sup> ]	IPS2	0.025 4	
Feet per second per second	[fps <sup>2</sup> ]	FPS2	0.304 8	
Mile per hour per second	[mph/s]	MPH/S	0.447 04	
Knot per second	[kn/s]	KN/S	463/900	
(Nautical mile per hour per second)	[KII/ S]	KN/3	403/300	

# 13-14. Units of force

Here is the list of units of force:

Unit		Keyword	Ratio
Newton	[N]	NEWTON	1
(Kilogram meter per second per second)	[IN]	NEWTON	1
Dynne	[dyn]	DYN	1 E-05
(Gram centimeter per second per second)	[uyii]	DIN	1 6-03
Kilogram weight	[kgf]	KGF	9.806 65
Common visions	[æf]	GF	9.806 65
Gram weight	[gf]	GF.	E-03

13-15. Units of pressure

Here is the list of units of pressure:

Unit		Keyword	Ratio
Pascal	[Pa]	PA	1
(Newton per square meter)	լք Այ	173	_
Hectopascal	[hPa]	HPA	1 E+02
Kilopascal	[kPa]	KPA	1 E+03
Megapascal	[MPa]	MPA	1 E+06
Bar	[ban]	BAR	1 E+05
(Megadyne per square centimeter)	[bar]	DAN	1 2+03
Millimeter of mercury	[mmHg]	MMHG	101325/760
Inch of mercury	[inHg]	INHG	3 386.388 64

# 13-16. Units of energy

Here is the list of units of energy:

Unit		Keyword	Ratio
Joule (Newton meter)	[J]	J	1
Kilojoule	[kJ]	КЈ	1 E+03
Megajoule	[MJ]	МЈ	1 E+06
Electronvolt	[eV]	EV	1.602 176 620 8 E-19
Kilo-electronvolt	[keV]	KEV	1.602 176 620 8 E-16
Mega-electronvolt	[MeV]	MEV	1.602 176 620 8 E-13
Giga-electronvolt	[GeV]	GEV	1.602 176 620 8 E-10
Thermochemical calorie	[cal <sub>th</sub> ]	CAL	4.184
Kilocalorie	[kcal <sub>th</sub> ]	KCAL	4 184
Ton of TNT	[t <sub>TNT</sub> ]	TTNT	4.184 E+09
Kilowatt hour	[kWh]	KWH	3.6 E+06
British thermal unit	[Btu]	BTU	1055.06

# 13-17. Units of temperature

Here is the list of units of temperature:

Units		Keyword	Ratio	Zero
Kelvin	[K]	KEL	1	0
Celsius	[°C]	DEGC	1	-273.15
Rankine	[°R]	DEGR	5/9	0
Fahrenheit	[°F]	DEGF	5/9	-459.67

The values of absolute temperature of Celsius and Fahrenheit is not same. For instance, conversion from Celcius to Fahrenheit is following:

$$\theta$$
[°C] =  $(\theta + 273.15) \times \frac{9}{5} - 459.67$ [°F]

# 14. Math / Scientific constants

## 14-1. Input constants

This software supports many math / scientific constants. Type a keyword to push a constant.

# IMPORTANT

Scientific constants are from 2014 CODATA

### 14-2. Math constants

Here is the list of math constants:

Name	Keyword	Value
PI	PI	3.141 592 653 589 79
Napier's constant	Е	2.718 281 828 459 05
Euler-Mascheroni constant	EG	0.577 215 664 901 533

## 14-3. Fundamental physical constants

Here is the list of fundamental constants in physics:

Name		Symbol	Keyword	Value
Speed of light in vacum	$c_0$	[m/s]	LIGHT	299 792 458
Magnetic constant	$\mu_0$	[H/m]	MAGNETIC	1.256 637 061 436 E-06
Electric constant	$\varepsilon_0$	[F/m]	ELECTRIC	8.854 187 817 620 E-12
Characteristic impedance of vacum	$Z_0$	[Ω]	IMPEDANCE	376.730 313 461
Gravitation constant	$G_0$	$[m^3/kg/s^2]$	GRAVITATION	6.674 08 E-11
Planck constant	h	[J · s]	PLANCK	6.626 070 040 E-34
Reduced Planck constant	ħ	[J · s]	RPLANCK	1.054 571 800 E-34

14-4. Electromagnetics

Here is the list of constants in electromagnetics:

Name	S	ymbol	Keyword	Value
Elementary charge	e	[C]	ECHARGE	1.602 176 620 8
Elementary charge	ı	[O]	ECHARGE	E-19
Magnetic flux quantum	$\Phi_0$	[Wb]	Q.FLUX	2.067 833 831
Wagnetic flux quantum	$\Psi_0$	[wb]	Q.FLUX	E-15
Conductores quentum	(	[S]	Q.CONDUCT	7.748 091 731 0
Conductance quantum	$G_0$	[၁]	Q.CONDUCT	E-05
Resistance quantum	$R_0$	$[\Omega]$	Q.RESIST	12 906.403 727 8
Inganhaan aanatant	IV.	$K_J$ [Hz/V]	JOSEPHSON	483 597.852 5
Josephson constant	$\kappa_{j}$		JUSEPHSUN	E-09
von Klitzing constant	$R_K$	$[\Omega]$	KLITZING	25 812.807 455 5
Dalamananatan		[1 /m]	D MACNETON	927.400 999 4
Bohr magneton	$\mu_B$	[J/T]	B.MAGNETON	E-26
Neglesensesses		[r /m]	N. MACNETON	5.050 783 699
Nuclear magneton	$\mu_N$	[J/T]	N.MAGNETON	E-27

# 14-5. Nuclear physics

Here is the list of constants in nuclear physics:

Name	Sy	mbol	Keyword	Value
Eine atmostume constant			FSTRUCT	7.297 352 566 4
Fine-structure constant	α		FSTRUCT	E-03
Rydberg constant	$R_{\infty}$	$[m^{-1}]$	RYDBERG	10 973 731.568 508
Dalam and disca		r 1	D DADTIIC	0.529 177 210 67
Bohr radius	$a_0$	[m]	B.RADIUS	E-10
II-utus susus		[1]	HARTREE	4.359 744 650
Hartree energy	$E_h$	IJ	HAKIKEE	E-18

## 14. Math / Scientific constants

## Constants connected with electron:

Name	,	Symbol	Keyword	Value
Mass of electron		آادها	E.MASS	9.109 383 56
Ividss of electron	$m_e$	[kg]	E.MASS	E-31
Compton wavelength of electron	1	[m]	E.COMPTON	2.426 310 236 7
Compton wavelength of electron	$\lambda_e$	[m]	E.COMPTON	E-12
Classical electron radius	r	[m]	E.RADIUS	2.817 940 322 7
Classical electron facilis	$r_e$	[m]	E.RADIUS	E-15
Magnetic moment of electron		[ו /ת]	E.MAGNETIC	-928.476 462 0
Magnetic moment of electron	$\mu_e$	[J/T]	E.MAGNETIC	E-26
Camama amatia matia of alcotmom	4	[s <sup>-1</sup> T <sup>-1</sup> ]	E.GYRO	1.760 859 644
Gyromagnetic ratio of electron	$\gamma_e$	[8 -1 -]	E.GIKU	E+11

# Constants connected with proton:

Name	Symbol		Keyword	Value
Mass of proton	[1 ]	P.MASS	1.672 621 898	
iviass of proton	$m_p$	[kg]	r.III.33	E-27
Comments a syrval and the of must an	1	[]	P.COMPTON	1.321 409 853 96
Compton wavelength of proton	$\lambda_p$	$\lambda_p$ [m]	P.COMPTON	E-15
Magnetic moment of muton		[ו /ידי]	D. MACHETTC	1.410 606 787 3
Magnetic moment of proton	$\mu_p$	[J/T]	P.MAGNETIC	E-26
C	٠,	[1m-1]	D CVDO	2.675 221 900
Gyromagnetic ratio of proton	Υp	$[s^{-1}T^{-1}]$	P.GYRO	E+08

### 14. Math / Scientific constants

## Constants connected with neutron:

Name	Symbol		Keyword	Value
Mass of neutron	m	العما	N.MASS	1.674 927 471
iviass of fieudoff	$m_n$	[kg]	CCAIN.N	E-27
Compton wavelength of neutron	1	[m]	N.COMPTON	1.319 590 904 81
Compton wavelength of neutron	$\lambda_n$	[m]	N. COMPTON	E-15
Magnetic memort of neutron	<b></b>	[ɪ /亚]	N.MAGNETIC	-0.966 236 50
Magnetic moment of neutron	$\mu_n$	[J/T]	N.MAGNETIC	E-26
Cyromagnatic ratio of nautron		$[s^{-1}T^{-1}]$	N.GYRO	1.832 471 72
Gyromagnetic ratio of neutron	Υ'n	[S 1 -]	UAYD.NI	E+08

# Other constants in nuclear physics:

Name	Symbol		Keyword	Value		
Mass of muon	m	[]-a]	m []ra]	[]] MIL MACC	MU.MASS	1.883 531 594
Wass of fildon	$m_{\mu}$ [kg]		MU.MASS	E-28		
Magnetic moment of muon	μ <sub>μ</sub> [J/T]		MU.MAGNETIC	-4.490 448 26		
Wagnetic moment of muon			MO.MAGNETIC	E-26		
Mass of touon	222	D	TAU.MASS	3.167 47		
Mass of tauon	$m_{ au}$	[kg]	CCAITIONT	E-27		

14-6. Physicochemistry

Here is the list of constants in physicochemistry:

Name		Symbol	Keyword	Value
Boltzmann constant	k	[J/K]	BOLTZMANN	1.380 648 52 E-23
Avogadro constant	$N_A$	[mol <sup>-1</sup> ]	AVOGADRO	6.022 140 857 E+23
Atomic mass constant	$m_{ m u}$	[kg]	DALTON	1.660 539 040 E-27
Faraday constant	F	[C/mol]	FARADAY	96 485.332 89
Molar gas constant	R	$[J\cdot K^{-1}\cdot mol^{-1}]$	GAS	8.314 4598
Molar volume [1] (Cubic meter)	$V_{ m m}$	[m <sup>3</sup> /mol]	MOLV	22.413 962 E-03
Molar volume [1] (Litter)	V <sub>m</sub>	[L/mol]	MOLVL	22.413 962
Loschmidt's constant [1]	$n_0$	[m <sup>-3</sup> ]	LOSCHMIDT	2.686 7811 E+25

<sup>[1]</sup> In 0 degrees centigrade and standard atomospheric pressure (273.15K, 1 atm).

Here is the list of constants in thermal radiation:

Name	Symbol		Keyword	Value		
Stafon Daltzmann agnatunt	- FYAZ 2 1Z-41		STEFAN	5.670 367		
Stefan-Boltzmann constant	σ	$[W \cdot m^{-2} \cdot K^{-4}]$		E-08		
First radiation constant		$[W \cdot m^2]$	F.RAD	3.741 771 790		
First radiation constant	$c_1$		r.KAD	E-16		
Cooped modistion constant				[ IZ]	C DAD	1.438 777 36
Second radiation constant	$c_2$	$[\mathbf{m} \cdot \mathbf{K}]$	S.RAD	E-02		

# 14-7. Agreement value

Here is the list of agreement values:

Name	Symbol		Keyword	Value
Standard gravity	$g_n$	$[m/s^2]$	GRAVITY	9.806 65
Standard atmosphere	1 atm	[Pa]	ATM	10 1325
Zero degrees Celsius in Kelvin	0°C	[K]	ZEROD	273.15

## 14-8. Planck unit

Here is the list of Planck unit:

Name	Sy	mbol	Keyword	Value
Planck mass	222	[]+4]	PL.MASS	2.176 470
Planck mass	$m_{ m P}$	[kg]	PL.MA33	E-08
Planck energy	$E_{ m P}$	[CoV]	PL.ENERGY	1.220 910
Planck energy	Еp	[GeV]	PL.ENERGY	E+19
Planck temperature	т	[K]	PL.TEMP	1.416 808
Flanck temperature	$T_{ m P}$	[N]	F L . I LIMF	E+32
Dlandr lanath	1	[]	PL.LENGTH	1.616 229
Planck length	$l_{ m P}$	[m]	PL.LENGIH	E-35
Planck time		[a]	PL.TIME	5.391 16
Flanck unite	ck time $t_{\rm P}$ [s] PL.TIME		PL.IIME	E-44

## 14-9. Astronomy

Here is the list of constants of astronomy:

Name	Syr	nbol	Keyword	Value
Astronomical unit	AU	[m]	ASTRO	149 597 870 700
Parsec	рс	[m]	PARSEC	3.085 677 581 E+16
Light year	ly	[m]	LYEAR	9 460 730 472 580 800

### 15-1. All clear

You can clear stack and registers with all clear function.

Function	Keyword	
All clear	AC	
Stack clear	CLEAR	
Stack clear	CLR	
Dagiston alogn	REGCLEAR	
Register clear	RCLR	

You can use undo after you call clear functions.

## 15-2. All reset

Type "RESET" or "RST" to reset all settings without those in config mode. Call the function and type "YES" or "NO" to confirm.

### 15-3. Undo / redo

Undo and redo function is available:

Function	Keyword
Undo	UNDO
Undo	U
Redo	REDO
Keuo	R

See also chapter 2 and chapter 3.

## 15-4. JSON output

Type "JSON" or "OUT" to output JSON formatted text file.

Function	Keyword	R	D	Computation
ICON outsut	JSON	•	0	
JSON output	OUT	0	0	

This software output files to the directory it exists. The format of file name is following:

YYYY: Gregorian year MMDD: Month and day

HHMMSS: Hour, minute, second

Output JSON file and its file name is displayed in message area.

You can save stack and registers states.

### 15-5. Macro function

This software supports macro with strings.

Function	Keyword	R	D	Computation
Run macro	RUN	1	1	

Macro function reads X as a string and operate.

Here is an example of using macro function:

#	TYPE	VALUE
4		
Z		
Υ		
Х	String	2 3 +

### (2) Run macro

Input> run

#	TYPE	VALUE
4		
Z		
Υ		
Х	Integer	5

You can make easy user defined function with macro function.

For example, the macro string of RA +  $\sqrt{\text{RB} \times \text{RC}}$  is "ldra ldrb ldrc \* sqrt +". You store it to RE. Set RA, RB and RC. Then load RE and run macro to calculate RA +  $\sqrt{\text{RB} \times \text{RC}}$ .

## NOTICE

You cannot include keyword "RUN", which is macro, in a string for macro function. This specification is for avoiding infinite loop.

Similarly, you cannot include mode-changing, display-changing keywords.

## 15-6. Test precisions

You can test precisions of this software.

Function	Keyword	R	D	Computation
Radix of floating	RADIX	0	0	Push Int
Machine epsilon	EPS	0	0	Push Flt

These functions are for debugging.

## 15-7. Special startup

This software supports command line arguments.

Argument	Setting
-d	Do not clear display
-j	JSON file output
-jd	JSON display (console)
	Split for JSON expression

If you would like to keep display buffers, use -d option.

JSON file output and JSON display uses --. Write expressions after --. Example:

eckert64.exe -j -- 1 2 3 sum stra pi exp strz sum copy i mul 2

Replace -j into -jd to display upon console.

# 16. Messages

# 16-1. Error messages

The list of error messages in this software is below:

Message
Bad argument count
Bad argument type
Bad element
Bad matrix size
Bad tuple size
Determinant is zero
Division by zero
Empty input
Failed to output file
Final page of register
Final page of stack
First page of register
First page of stack
From to : INVALID
Invalid conversion
Invalid input
Invalid range
Invalid value
Latest history
Logarithm of zero
Maximum integer
Minimum integer
Negative-th power of zero
No history
No older history
Not a positive integer
Registers are empty

Display			
Selected register is empty			
Stack and registers are empty			
Stack is empty			
Too few arguments			
Too large or small input			
Too large to operate			
Unsupported in current version			
Unsupported operation or notation			
Zero-th power of zero			

# 16-2. Notice messages

The list of notice messages is following:

Display
Error calculation
Floating overflow
Integer overflow
Rational overflow

# 16-3. Confirm messages

The list of confirm messages is here:

Display
Cancelled
Done
From to
Input integer
Maximum value set
Minimum value set
OK? Y/N
Setting completed

# 17. Technical information

17-1. Data types

The list of data types this software supports is following:

Class		Type name	Explanation	Value range
Number	Scalar	Integer	Integer	64-bit integer
		Floating	Floating point number	long double
		Rational	Rational number	Pair of 64-bit integers
		Complex	Complex number	Pair of scalars
Binary (Unsigned decimal)		Boolean	Boolean	True, False
		Byte	Byte	Unsigned 8-bit
		Word	Word	Unsigned 16-bit
		Dword	Double word	Unsigned 32-bit
		Qword	Quad word	Unsigned 64-bit
Tuple		Tuple	Vector	Tuple of scalars or
				tuple of binaries
		Matrix	Matrix	Tuple of tuples
number	Not a	Infinity	Infinity	Positive, negative, complex
		String	String	String
er		Error	Error String	String

If integer overflow occurs, the calculation is retried as floating point number.

If floating-point overflow occurs, the result of calculation is handled as Infinity.

### 17-2. Calculation precision

The concept of this software is useful for engineers, but no accuracy assurances. So this software is not suitable for high precision calculations.

The internal precision of this software is displayed with calculation settings. The data are using binaries, so floating-point calculations cause calculation errors. Then, this software does not correct calculation errors.

### 17-3. Mathematical definitions

Mathematical definitions this software adopts is following:

### 17-3-1. Remainde of integers (Modulo)

Remainde of integers is defined as:

A/B	Quotient	Remainder
Neg / Neg	(-A)÷(-B)	-((-A) mod (-B))
Neg / Pos	-((-A)÷B)	-((-A) mod B)
Zero / Non-zero	0	0
Pos / Neg	-(A÷(-B))	(-A) mod B
Pos / Pos	A÷B	A mod B

### 17-3-2. Odd number-th root of negative value

The odd number-th root, such as cubic root or 5<sup>th</sup> root of negative value is not defined in range of real number. For instance, the cubic root of -1 is not -1.

The odd number-th root is defined in complex number:

$$\sqrt[N]{a+ib} = \sqrt[N]{r} \exp(i\theta/N)$$

$$= \sqrt[N]{r}(\cos\theta/N + i\sin\theta/N)$$

### 17-3-3. Definition of complex numbers

Complex absolution and argument are defined as:

$$abs(a+ib) = r = \sqrt{a^2 + b^2}$$

$$arg(a+ib) = \theta = \begin{cases} atan(b/a) & (a > 0) \\ \pi/2 & (a = 0, b > 0) \\ -\pi/2 & (a = 0, b < 0) \\ \pi - atan(b/a) & (a < 0, b > 0) \\ atan(b/a) - \pi & (a < 0, b < 0) \\ all real number & (a = b = 0) \end{cases}$$

This is the basics of complex functions.

17-3-4. Complex functions

The list of definitions of complex functions is following:

Function	Definition	
Square	$\sqrt{a+ib} = \sqrt{r} \exp(i\theta/2)$	
root	$= \sqrt{r}(\cos\theta/2 + i\sin\theta/2)$	
Cubic	$\sqrt[3]{a+ib} = \sqrt[3]{r} \exp(i\theta/3)$	
root	$= \sqrt[3]{r}(\cos\theta/3 + i\sin\theta/3)$	
Exponent	$\exp(a+ib) = \exp(a)(\cos b + i\sin b)$	
Natural $\ln(a+ib) = \ln r + i\theta$		
logarithm		
Power	$(a+ib)^{c+id} = r^c e^{-d\theta} \{\cos(c\theta + d\ln r)$	
Power.	$+i\sin(c\theta+d\ln r)$	
SIN	$\sin(a+ib) = \sin a \cosh b + i \cos a \sinh b$	
COS	$\cos(a+ib) = \cos a \cosh b - i \sin a \sinh b$	
TAN	$\tan(a+ib) = \frac{1}{2} \cdot \frac{\sin 2a}{\cos^2 a + \sinh^2 b} + i\frac{1}{2} \cdot \frac{\sinh 2b}{\cos^2 a + \sinh^2 b}$	
ASIN	$\arcsin(Z) = -i \ln \left( \sqrt{1 - Z^2} + Zi \right)$	
ACOS	$\arccos(Z) = -i \ln \left( Z + i \sqrt{1 - Z^2} \right)$	
ATAN	$\arctan(Z) = \frac{i}{2} \ln\left(\frac{i+Z}{i-Z}\right)  (Z \neq \pm i)$	
SINH	$\sinh(a+ib) = \sinh a \cos b + i \cosh a \sin b$	
COSH	$\cosh(a+ib) = \cosh a \cos b + i \sinh a \sin b$	
TANH $\tanh(a+ib) = \frac{\sinh 2a}{\cosh 2a + \cos 2b} + i \frac{\sin 2b}{\cosh 2a + \cos 2b}$		
ASINH	$\operatorname{asinh} Z = \ln \left( Z + \sqrt{Z^2 + 1} \right)$	
ACOSH	$\operatorname{acosh} Z = \ln \left( Z + \sqrt{Z+1} \sqrt{Z-1} \right)$	
ATANH	$\operatorname{atanh} Z = \frac{1}{2} \ln \left( \frac{1+Z}{1-Z} \right)  (Z \neq \pm 1)$	

# 18. Troubleshootings

### 18-1. I have no idea to operate this software

Please restart this software and read chapter 4.

This software adopts RPN-style (stack). You can make comprehension with reading chapter 4 so please read it carefully.

### 18-2. I'd like to view full data

If you find "..." in the display, type "v" to show full data (view mode). Press enter to return to calculation mode from view mode.

### 18-3. I'd like to change rational or floating display

Use the following keywords to change rational or floating display:

Mode	Keyword
Auto decimal display	AD
Force decimal display	FD
Force floating display	FF
Standard decimal display	STD
Fixed decimal display	FIX
Scientific decimal display	SCI
Engineering decimal display	ENG

Please read chapter 3 to get more information.

### 18-4. I'd like to change complex display

Type "EUL" to switch complex number display. The argument of complex display depends on angle mode.

Please read chapter 3 to get more information.

### 18-5. I'd like to view all values in the stack and the registers

JSON output function is recommended. Please read chapter 15.

If you would like to look at some data, try page-flipping function. Please read chapter 3 to get more information.

### 18-6. I saw doubtful calculation result

Restart the software and retry.

Supported numbers in this software are expressed in binary so the calculations may have small errors. I think the answer is 0.1 but this shows 0.0999... that is within the spec.

### 18-6-1. Check keywords

Did not you type wrong spelling? Check the keywords.

### 18-6-2. Check display mode

Were not you confused by display mode? Try another display mode and check the value.

Please read chapter 3 to change modes.

### 18-6-3. Check angle mode

Did you noticed the unit of angle in your calculation? Trigonometric functions depend on angle mode. So a called trigonometric function is determined by a keyword and angle mode.

Please read chapter 3 to change modes.

### 18-6-4. Check range of value

Some functions may cause large errors depending on range of value. For instance, input a large value to trigonometric functions to make unreliable results.

See also chapter 17.

### 18-6-5. Check the order of calculations

If the expression is changeable in math, calculators may make small errors. Please calculate by changing orders with consideration of less error.

### 18-7. Stopped by errors

Check types or values of data. For instance, the factorial of floating-point number is not defined.

### 18-7-1. Check types

You can check the type of data in the second left column in the stack display. If types are not shown, type "TYPE" to display. Check types of arguments of functions.

### 18-7-2. Check values

Did you input error value? Some functions have undefined input. For example, logarithm of 0 is undefined.

#### 18-7-3. Check sizes of vectors and matrices

Please notice that the calculations of vectors or matrices are defined.

### 18-7-4. Read error messages

The messages may help you to detect operational errors.

### 18-8. I found doubtful behaviors

If you find bugs or unnatural specifications, please send messages to me.

### ECKERT introduction page

http://sfoftime.web.fc2.com/eckert

### E-mail to:

only.my.truth@gmail.com



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