

# Bayesian multi-level modelling for predicting single and double feature visual search

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## Abstract

Performance in visual search tasks is frequently summarised by “search slopes” - the additional cost in reaction time for each additional distractor. While search tasks with a shallow search slopes are termed efficient (pop-out, parallel, feature), there is no clear dichotomy between efficient and inefficient (serial, conjunction) search. Indeed, a range of search slopes are observed in empirical data. The Target Contrast Signal (TCS) Theory is a rare example of quantitative model that attempts to predict search slopes for efficient visual search. One study using the TCS framework has shown that the search slope in a double-feature search (where the target differs in both colour and shape from the distractors) can be estimated from the slopes of the associated single-feature searches. This estimation is done using a contrast combination model, and a collinear contrast integration model was shown to outperform other options. In our work, we extend TCS to a Bayesian multi-level framework. We investigate modelling using normal and shifted-lognormal distributions, and show that the latter allows for a better fit to previously published data. We propose running a new fully within-subjects experiment to attempt to replicate the key original findings, with some changes to help distinguish between theories.

*Keywords:* Visual search, Efficient search, Parallel processing

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## 1. Introduction

Visual search, where participants are asked to find a target within a cluttered scene, has been extensively studied within psychology. Several models have been developed that can generate testable predictions about how different types of distractors and targets affect search efficiency. One of the key distinctions in the field

6 has been between efficient (also referred to as parallel or pop-out) and inefficient  
7 (serial) search. These are often studied in the context of the regression slope be-  
8 tween the number of distractors and mean reaction time, which has been termed  
9 the *search slope*. When the search slope is shallow (usually positive, but occasion-  
10 ally negative e.g. (Rangelov et al., 2017)), the search is called efficient or parallel,  
11 and the addition of more non-target distractors has little impact on an observers  
12 difficulty in finding a target. When the slope is steeper, each additional distractor  
13 has a noticeable impact on increasing difficulty, and the search is described as in-  
14 efficient or serial. However, the distinction between these types of search is often  
15 less clear in real experimental data, with a range of different search slopes being  
16 seen for different types of targets and distractors (Cave and Wolfe, 1990).

17 In the current study, we are interested in what has traditionally been termed  
18 efficient or parallel search, and the factors that affect search slope in these condi-  
19 tions. Recent work has suggested that for efficient search, there is a logarithmic  
20 relationship between distractor set size and reaction time, and that this relation-  
21 ship can be modified by target-distractor similarity (Buetti et al., 2016), providing  
22 evidence that search behaviour in parallel search is more complex than has pre-  
23 viously been assumed. This observation has formed the basis of the ‘Target Con-  
24 trast Signal (TCS) Theory’ (Lleras et al., 2020), which aims to provide a means  
25 of predicting observer search slopes for new search arrays by quantifying target-  
26 distractor differences. For example, by measuring search slopes for conditions in  
27 which the distractors differ from the target along a *single feature* (e.g. colour *or*  
28 shape), it has been shown that you can predict search times for arrays in which  
29 the target differs from the distractors along two features (e.g., colour *and* shape)  
30 which we refer to here as *double feature* search. (Buetti et al., 2019). Here, we  
31 aim to replicate and extend this work both theoretically and empirically, to test the  
32 generalisability of the TCS model, and to suggest ways in which the TCS model  
33 could be improved to generate better predictions.

### 34 1.1. Previous Work

35 Many different forms of visual search models have been proposed. One well  
36 developed class of models are the saliency models, which aim to predict eye move-  
37 ments during scene viewing, including visual search. They rest on the assump-  
38 tion that fixations are directed to objects or locations that are most dissimilar to  
39 the background or other objects in the visual display (Itti and Koch, 2000; Itti  
40 et al., 1998; Koch and Ullman, 1987). While the original saliency model was  
41 able to predict fixation allocation in a visual search task above chance (Parkhurst  
42 et al., 2002), further research demonstrated that a comparable level of performance

43 could be achieved using a simple central fixation bias heuristic (Tatler, 2007). The  
44 saliency models have since been extended and improved (see for example Zhang  
45 et al. (2008)): however, the main issue with this family of models remains their  
46 limited usability in complex real-life search arrays (Tatler et al., 2011; Koehler  
47 et al., 2014). In addition, in most instances of visual search, the target is clearly  
48 defined (i.e. the goal is to find a specific object) and inspecting the most salient  
49 areas of the display may in these cases be inefficient. Finally, by focusing on eye  
50 movements, these models do not necessarily provide a theoretical framework for  
51 the cognitive processes underlying visual search.

52 Perhaps the most established class of models of visual search are based around  
53 Feature Integration Theory (Treisman and Gelade, 1980), which has been modi-  
54 fied and extended by Wolfe and colleagues in the Guided Search Model (Wolfe  
55 et al., 1989; Wolfe, 2014). These theories have been developed using data from  
56 visual search tasks with discrete sets of abstract items. These models combine  
57 top-down influences (how closely an item resembles the observer’s goal) with  
58 bottom-up image properties. For example, if one’s goal (top-down processing)  
59 is to find a red horizontal bar, all the red and horizontal items in a visual search  
60 display will be given greater weight than distractors (e.g. vertical and blue items)  
61 in the model. The salience of a given object in the display (how distinctive it is  
62 from the surrounding objects) also activates bottom-up processing. For instance, a  
63 blue item among red items is ranked higher than red among orange items. In such  
64 cases, a salient item can capture attention even without resembling the target.  
65 Combining bottom-up and top-down sources of activation generates an activation  
66 map which generates a prediction of the order in which stimuli are processed in  
67 visual search. Thus, these models aim to produce a representation of the visual  
68 properties of the distractors at each location in the visual field. However, these  
69 are predominantly qualitative models, and thus it is difficult to use them to make  
70 specific quantitative predictions.

71 TCS falls under a class of models that take a different approach, in that they  
72 focus solely on representing the difference between targets and distractors. For  
73 example, in work on eye movement patterns, it has been proposed that perfor-  
74 mance in inefficient (serial) visual search is mostly determined by the size of the  
75 ‘functional viewing field’, whose size varies as a function of target-distractor sim-  
76 ilarity (Hulleman and Olivers, 2017). Similarly, work on attention has proposed  
77 the notion of ‘relative features’, where attention is tuned to feature relationships  
78 i.e. the appearance of the target relative to distractors in the environment (Becker  
79 et al., 2014; Becker, 2010). TCS also has features in common with other models  
80 that propose parallel identification of all items in a scene, with diffusion based

mechanisms for identifying targets from distractors (Moran et al., 2013, 2016). However, TCS (Lleras et al., 2020) aims to provide a unifying framework that can make quantitative behavioural predictions for visual search based on this general assumption. As such, it is an attractive candidate model for a formal registered replication.

A key assumption of the TCS model is that behaviour is determined by comparing the target template (held in memory) with every element present in the scene in parallel. This allows the visual system to reject peripheral non-targets quickly; the speed at which items are evaluated is determined by how different the item is from the template through an evidence accumulation process (formally, the slope of the logarithmic function is assumed to be inversely proportional to the overall magnitude of the contrast signal between the target and distractor). The model thus focuses on an initial, efficient processing stage of search; if sufficient evidence is not accumulated during this process, the model posits that a second stage is entered, requiring a sequence of eye movements to search for the target in a serial manner. TCS has been successful in predicting a number of empirical results, including search performance in heterogeneous scenes based on parameters estimated in homogeneous scenes, both with artificial stimuli (Buetti et al., 2016; Lleras et al., 2019) and with real-world objects visualised on a computer display (Wang et al., 2017). Table 1 provides an overview of studies investigating the TCS framework to date.

The original version of the TCS model is essentially a (natural) log-linear model in the number of distractors. The full model contains a variable  $L$ , which represents the number of different types of distractors present in the display. However, in our paper, we will follow Buetti et al. (2019) and only consider the specific case of  $L = 1$ , of a target among a homogeneous set of distractors. In this case, the TCS model can be represented in the following way:

$$\hat{RT} = a + D \log(N_T + 1) \quad (1)$$

The intercept,  $a$ , corresponds to search arrays in which only the target is present and there are no distractors.  $N_T$  is the total number of distractors.

## 1.2. Rationale for proposed work

While many aspects of the TCS framework have been tested, with extremely promising results, there remains a great deal of scope for verification of some of the key findings to date, and extensions of aspects of the model. In all implementations of TCS so far, predictions of search efficiency (e.g. in heterogeneous scenes)

Reference	Overview
Buetti et al. (2016)	For efficient search with a specific target, there is a logarithmic relationship between distractor set size and reaction time. The steepness of this relationship is modulated by distractor-target similarity, with steeper slopes for more similar distractors.
Wang et al. (2017)	Data from homogeneous search arrays can be used to predict search reaction times in heterogeneous displays containing images of real-world objects, using an equation assuming parallel, unlimited capacity, exhaustive processing, and independence of inter-item processing.
Madison et al. (2018)	Logarithmic efficiency in efficient search cannot be explained by crowding in peripheral vision.
Ng et al. (2018)	Logarithmic efficiency in efficient search cannot be explained by eye movements.
Lleras et al. (2019)	Validation of previous results showing data from homogeneous search arrays can be used to predict reaction times in heterogeneous displays. Distractor-distractor interactions can also facilitate processing when nearby items are similar to each other.
<b>Buetti et al. (2019)</b>	Data from search arrays where the distractors are distinguished from the target by one feature can be used to predict search reaction times in displays with compound stimuli, defined by two features. Reaction times can be predicted using a collinear contrast integration model, which assumes that the overall target-distractor contrast is the sum of the contrasts from the two feature vectors separately.
Lleras et al. (2020)	Full proposal of the Target Contrast Signal Theory, proposing that the initial stage of processing computes a difference signal between each item in the scene and the target template, using this to determine which items in the scene are unlikely to be the target.
Ng et al. (2020)	Attention works in a two stage process, first discarding target-dissimilar distractors in a distributed, parallel way. Focused spatial attention then visits target-similar items at random.
Xu et al. (2021)	Extension of Buetti et al. (2019) to new features (shape and texture), which combine according to a Euclidean metric (orthogonal contrast integration model).

Table 1: An overview of work on the Target Contrast Signal Theory. The key paper for our replication is highlighted.

115 have been made on the average of a group of participants, using data from a dif-  
116 ferent group performing a different task (e.g. searching in homogeneous scenes).  
117 Thus, we know that TCS can replicate group-level averages between subjects in  
118 search well, but we do not know to what extent it is also able to make predictions  
119 at the individual level. This is particularly important given that conclusions based  
120 on aggregate data can be different from those that take individual differences into  
121 account; in one study where participants searched for a target in an array of ran-  
122 domly oriented line segments, aggregating the data suggested that participants  
123 were using a stochastic search model (Nowakowska et al., 2017). However, when  
124 considering each participant individually, it became clear that there was a high  
125 level of heterogeneity in responses, with some participants performing close to  
126 optimally, and others actually performing worse than chance (Nowakowska et al.,  
127 2017). Similarly striking variability has also been reported in other search studies  
128 (Irons and Leber, 2016, 2018; Clarke et al., 2020).

129 Taking search time distributions into account is also important for constrain-  
130 ing theories of visual search (Wolfe et al., 2010; Liesefeld and Müller, 2020): for  
131 example, they have been used to help distinguish between models that make sim-  
132 ilar predictions at the level of average reaction times (Moran et al., 2016, 2017).  
133 Including subject and trial level data into our implementation of the TCS will  
134 therefore further aid model development and assumption testing.

135 We also extend the TCS model into a Bayesian framework, where we begin  
136 with existing 'prior' beliefs that are updated with data to give 'posterior' beliefs  
137 that can be used for inference (McElreath, 2020). We think this has a number  
138 of advantages over frequentist approaches. Perhaps most importantly, Bayesian  
139 models are highly flexible. We demonstrate how we are able to specify a model  
140 that is able to more accurately represent the distribution of responses (for exam-  
141 ple, by specifying a response distribution that avoids predicting negative reaction  
142 times) with a relatively complex model structure, that can be fit to a relatively  
143 small amount of pilot data: something that would be challenging within a fre-  
144 quentist framework. We also believe that Bayesian models offer very intuitive  
145 methods for model testing and comparison and straightforward interpretation of  
146 results, and we hope that this manuscript can act as a demonstration of these ben-  
147 efits, showing how they can be applied to real scientific questions beyond the  
148 simplified examples often found in textbooks or tutorials.

149 In the current manuscript, we focus on replicating and extending findings from  
150 Buetti et al. (2019). In their study, participants searched for a target in a scene of  
151 homogeneous distractors (see Figure 1). First, parallel search efficiency (mea-  
152 sured by the logarithmic search slope) was estimated for cases where the distrac-

153 tors varied from the target in one dimension: either colour (e.g. a cyan target being  
 154 searched for in either yellow, blue or orange distractors) or shape (e.g. a semicir-  
 155 cle target in either circle, diamond or triangle distractors). New participants then  
 156 searched for the same targets in displays where the distractors were compounds,  
 157 differing from the target in both colour and shape (e.g. searching for a cyan semi-  
 158 circle in either blue circles, orange diamonds or yellow triangles). The logarithmic  
 159 search slopes in the initial experiments were then used to predict the logarithmic  
 160 slopes and reaction times using a number of models. The authors found that the  
 161 best model was a ‘collinear contrast integration model’ where the distinctiveness  
 162 scores were summed along each attribute in the unidimensional experiments, cre-  
 163 ating an overall contrast score that was used for compound stimuli predictions.  
 164 In our registered replication, we will attempt to verify the conclusions of Buetti  
 165 et al. (2019), that the collinear contrast integration model does indeed offer the  
 166 best characterisation of contrast signal combinations in visual search within the  
 167 TCS framework.

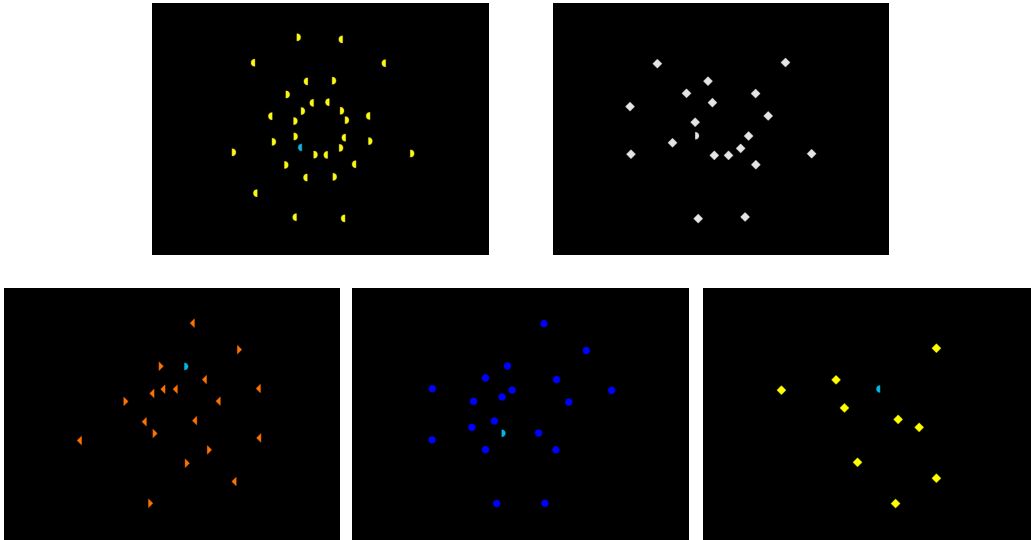


Figure 1: Example stimuli from Buetti et al. (2019) Top left: Expt 1A. Here, the target is a blue semicircle within a set of homogeneous (yellow semicircle) distractors. Top right: Expt 1B. The target is a grey semicircle in circular grey distractors. Bottom left: Expt 2A. The target is a blue semicircle in orange diamond distractors. Bottom middle: Expt 2B. The target is a blue semicircle in dark blue triangle distractors. Bottom right: Expt 2C. The target is a blue semicircle in yellow circular distractors.

168 We begin by verifying the analysis of Buetti et al. (2019). We then describe  
169 our proposed replication study, showing with pilot data how we are able to extend  
170 their model of how multi-dimensional contrasts are calculated, both by incorpo-  
171 rating a multi-level design to predict within-subjects effects and by utilising a  
172 Bayesian generalised linear model framework to better represent the distribution  
173 of responses (e.g. avoiding predicting negative reaction times, accounting for un-  
174 certainty in model predictions).

## 175 2. The Target Contrast Model

176 We first describe the original Target Contrast Model, as presented in Buetti  
177 et al. (2019) and verify that we can successfully replicate the original analysis  
178 (both using frequentist modelling and Bayesian modelling; see Supplementary  
179 Materials).

### 180 2.1. TCS modelling overview

181 In Experiment 1a of Buetti et al. (2019), participants searched for a cyan  
182 semicircle target among blue, yellow or orange semicircular distractors i.e. they  
183 searched for a target that differed from the distractors by a *single feature* (colour).  
184 The experiment was then repeated (1b) using a different single feature (shape,  
185 with participants searching for the semicircular target within triangle, circle or di-  
186 amond distractors). In Experiments 2a, 2b and 2c, participants again searched for  
187 a cyan semicircle, but this time, the distractors differed in both shape and colour.  
188 We will refer to these conditions as *double features*. Note, unlike in standard con-  
189 junction searches, in this paradigm, the distractors are all identical with respect to  
190 these features (i.e, orange triangles). Examples of all these stimuli are shown in  
191 Figure 1. Buetti et al. (2019) also carried out a replication of their basic results  
192 using slightly different target and distractor stimuli (Experiments 3 and 4).

193 The *Target Signal Contrast* theory is built around a linear model for predicting  
194 mean reaction times from the logarithm of the number of distractors (see Equation  
195 1). In particular, the TCS theory allows us to predict the value of the logarithmic  
196 slope,  $D_{c,s}$ , in this condition based on the corresponding  $D_i$  in the single feature  
197 search experiments.

#### 198 2.1.1. Calculating the intercept, $a$ , and the logarithmic slope parameter, $D_i$

199 Experiments 1a and 1b and 3a and 3b were used to calculate the logarithmic  
200 slope parameter  $D_i$ . In all experiments, the number of distractors varied, allowing  
201 the data to be used to fit a log-linear model for reaction times, where reaction



times increase logarithmically with  $N_T$ , the number of distractors (see Equation 1). In the original model the error distribution was assumed to be normal. Thus the results of Experiments 1 and 3 were used to calculate  $D_i$ , for each type of distractor. When colour varied, we will refer to  $D_c$ , for  $c = 1, 2, 3$ . Similarly for shape we will denote this ( $D_s$ ), and the compound features are denoted as ( $D_{c,s}$ ).

Fitting the model specified in Equation 1 to the data, we obtain the values for  $D_c$  and  $D_s$  given in Table 2. As can be seen, the more similar the distractors are to the target, the steeper the slope parameter is.

feature	$D_c$	feature	$D_s$
blue	76.8	triangle	141.1
yellow	16.0	diamond	77.2
orange	9.8	circle	62.1

Table 2: A table of  $D_i$  values for Experiment 1a and 1b. See Supplementary Material for full values for all experiments.

### 2.1.2. Estimating $D_{c,s}$ , the logarithmic slope parameter for compound features

In the context of the current experiments, the core idea of TCS theory is that we can estimate the (natural) logarithmic slope parameter for a double feature visual search from the slopes parameters in the two independent single feature searches i.e.,  $D_{c,s} = f(D_c, D_s)$ . Buetti et al. (2019) tested three different models for predicting  $D$  for compound colour-shape stimuli. The best feature guidance model (Equation 2) suggests that when the target and lures differ in two dimensions, participants will choose to attend to whichever feature dimension is the most discriminable (i.e. has the smallest  $D$  value):

$$D_{c,s} = \min(D_c, D_s) \quad (2)$$

The orthogonal contrast combination model instead suggests that independent feature dimensions comprise a multidimensional space, where an object can be described by the overall vector in this space, and thus  $D_{c,s}$  can be represented as:

$$D_{c,s} = \frac{1}{\sqrt{(\frac{1}{D_c})^2 + (\frac{1}{D_s})^2}} \quad (3)$$

Finally, the collinear contrast integration model also assumes independence of feature dimensions, but assumes that while the visual features create a multidimensional space, the overall vector is the sum of the individual feature vectors.

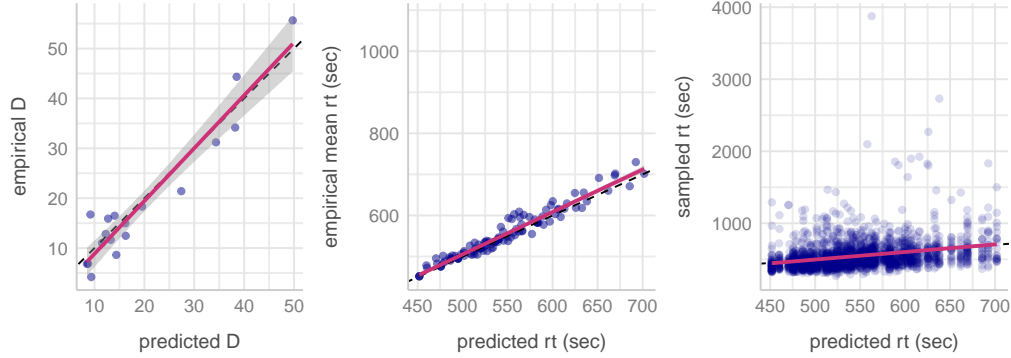


Figure 2: (left) The collinear method for calculating  $D$  offers a good prediction. (centre) Using the TCS to predict reaction times. (right) Each dot now represents a randomly sampled reaction time from an observer. Note that there is greater spread in the data points here, due to the fact that there will be trial-to-trial variability due to target position, inter-item distances, observer differences and so on.

224 mensional space, the contrast between them is unidimensional. As  $D$  is assumed  
 225 to be inversely proportional to contrast, the equation can be written as follows:

$$\frac{1}{D_{c,s}} = \frac{1}{D_c} + \frac{1}{D_s} \quad (4)$$

226 Buetti et al. (2019) found that with their dataset, the collinear contrast inte-  
 227 gration model was best able to predict  $D_{c,s}$  from  $D_c$  and  $D_s$ , with  $R^2 = 0.915$ .  
 228 We verified we were able to replicate this result using the dataset available on  
 229 OSF (<https://osf.io/f3m24/>)<sup>1</sup> and using the exclusion criteria originally applied;  
 230 see Figure 2 (left panel) and *Supplementary Materials* for details. We show that  
 231 we are able to do this using both the frequentist modelling approaches used in the  
 232 original paper, and using Bayesian modelling.

### 233 2.1.3. Estimating $a$ , the intercept parameter for compound features

234 As  $a$  is the intercept of the model, it represents how long observers take to find  
 235 a target when  $N_T = 0$ , i.e., there are no distractors. As such, it should be inde-  
 236 pendent of both shape and colour, and can be thought of as the role of non-search  
 237 processes (such as motivation, motor preparation etc.) that influence reaction time.

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<sup>1</sup>downloaded on 28th August 2020

238 In Buetti et al. (2019),  $a$  was calculated for each sub-experiment. Here, we follow  
239 that method in order to replicate their results exactly.

#### 240 2.1.4. *Estimating mean reaction times*

241 Finally, we can use Equation 1 to predict mean reaction times. As can be  
242 seen in Figure 2 (centre panel), these predictions are essentially identical to the  
243 empirical RT results:  $R^2 = 0.93\%$ .

#### 244 2.1.5. *Discussion*

245 While TCS theory offers a good prediction of search slopes and corresponding  
246 mean reaction times for double feature search, there are two related limitations.  
247 Firstly, it is unable to account for individual differences between observers, only  
248 the changes to the sample average. Secondly, it cannot account for the distribution  
249 of reaction times over multiple trials. Figure 2 (right panel) shows clearly that  
250 these factors generate high levels of variability within the individual trial-level  
251 data. To address these issues, we propose adapting TCS to make use of multi-  
252 level modelling techniques. Multi-level models allow us to take into account the  
253 hierarchical structure of the data (i.e. that each participant completes multiple  
254 trials) in a way that does not require averaging, meaning that we are able to model  
255 participant variability as well as group-level effects (Gelman and Hill, 2006).

#### 256 2.2. *A multi-level TCS*

257 Switching from a linear regression model to a multi-level model will allow  
258 us to compute  $D$  for each participant, while simultaneously estimating the trial-  
259 to-trial variance. We also switch from a frequentist to Bayesian framework, as  
260 this allows us to naturally account for the uncertainty in the model’s predictions.  
261 However, switching from linear regression to a multi-level model raises the prob-  
262 lem of which distribution to use for modelling reaction times. Using a normal  
263 distribution is unlikely to be satisfactory, as it is unable to account for the skew  
264 frequently seen in reaction time distributions, and also allows the possibility of  
265 negative reaction times. We can account for both of these problems by using a  
266 log-normal distribution. We will also test whether a slightly more complex ex-  
267 tension of this model, the shifted lognormal model (which allows the distribution  
268 to be offset to the right i.e. mimicking the patterns seen in reaction time data,  
269 where valid responses begin at around 100ms) offers any improvement in model  
270 fit. Note that a Wald, or inverse Gaussian distribution, would also be a reasonable  
271 distribution choice for this data given that TCS is based on a diffusion process  
272 e.g. (Moran et al., 2013): we chose not to use this distribution as it often leads to

273 computational issues, which would make it harder for others to reproduce or build  
274 on our approach later.

### 275 3. Hypotheses

276 We plan an experiment to test the extent to which the original results in Buetti  
277 et al. (2019) replicate and generalise, using our new modelling approach.

#### 278 3.1. Proposed Modifications to Experimental Design

279 In order to better test the above, and increases sensitivity, we propose to make  
280 the following changes to the experiment described in Buetti et al. (2019):

- 281 1. **Within-subjects design.** This modification should give us greater power to  
282 detect differences between different models, as well as allowing us to in-  
283 vestigate how individual differences in the single-feature task might explain  
284 differences in the double-feature task.
- 285 2. **Increase target-distractor similarity.** Our reanalysis of Buetti et al. (2019)  
286 indicates that if the distractors are a very different colour from the target,  
287 they not distinguish well between different contrast models. We will there-  
288 fore run a version of the experiment where the target is a red semicircle,  
289 with distractors being either orange, purple or pink.

#### 292 3.2. Registered Hypothesis

- 293 1. **Shifted lognormal model.** We hypothesise that a shifted lognormal model  
294 will give the best fit to our single-feature data, when compared to a lognor-  
295 mal and a normal model.
- 296 2. **Log-linear effect of  $N_T$ .** We will test the TCS model assumption that  $N_T$   
297 has a log-linear effect by testing models with and without the log of this  
298 term. We expect that this will confirm the results previously seen in papers  
299 testing TCS i.e. that the log-linear approach will be best.
- 300 3. **Contrast model comparisons.** We will test the hypothesis proposed by  
301 (Buetti et al., 2019): specifically, that the *collinear contrast ingratiation*  
302 *model* outperforms the *best feature guidance*, and *orthogonal contrast com-*  
303 *bination models* for the calculation of  $D$ , by calculating and comparing the  
304  
305

306 mean absolute prediction error for each model.

307

308 **4. Reaction time predictions.** We will further test the hypothesis proposed by  
309 (Buetti et al., 2019) by testing which model gives the best prediction at the  
310 trial-by-trial RT level.

311 We will test each of these hypotheses by calculating the marginal likelihood of  
312 the relevant models, and then calculating the poster probabilities. This will give  
313 us a probability for each model that represents the likelihood that the model gives  
314 the best prediction. We will consider there to be evidence for one model over  
315 the others if a given model has a probability above 90%. We will consider there  
316 to be strong evidence for one model over the others if that model has a posterior  
317 probability above 99%. This approach is most appropriate for our model: other  
318 measures of model fit, such as AIC, require an assumption of flat priors (which is  
319 not valid for multi-level models) and are based on point estimates (which is not  
320 valid for Bayesian models) (McElreath, 2020).

### 321 *3.3. Planned Explorations*

322 We plan to investigate the effect of individual differences in this paradigm:  
323 to what extent performance in the single-feature task can predict performance in  
324 the double-feature task for a given individual (Buetti et al. (2019) were not able  
325 to investigate this due to the between-subjects design of their study). We plan to  
326 do this by specifying a more complex random effects structure for the model, that  
327 allows for individual differences across different slopes for different features. This  
328 allows us to then study the random effect correlation structure. However, given  
329 these models can be challenging to fit, we will do this in an exploratory manner  
330 after carrying out our formally registered analysis.

331 One of the benefits of using a multi-level modelling approach is that it is rel-  
332 atively easy to extend to incorporate other factors that may contribute to reaction  
333 times, such as eccentricity and inter-item distance, which may help to explain  
334 behaviour further. To demonstrate this, we will also run exploratory analyses in-  
335 cluding a factor for which ring the target is in to assess whether this improves  
336 model fit or affects any of the conclusions that can be drawn from the model.

### 337 *3.4. Pilot Experiment*

338 Full details of a pilot experiment with  $n = 4$  participants (960 trials each) using  
339 our proposed analyses can be found in supplementary materials. This suggests that  
340 even with a small sample, we can convincingly demonstrate H1 and H2, however  
341 more data will be required to discriminate between the models in H3.

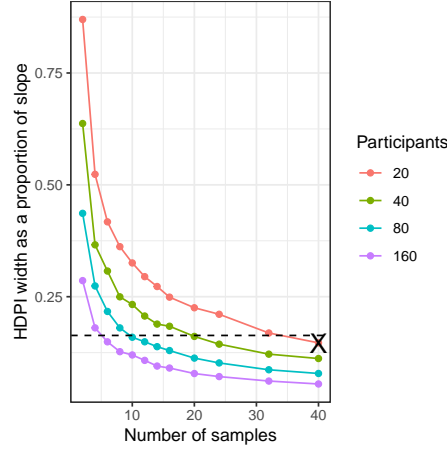


Figure 3: Simulation sensitivity analysis, showing the 97% HPDI width for the blue distractor condition in a shifted lognormal model, across different numbers of trials and participants. The X shows the real HPDI width as a proportion of slope for the blue distractor condition in Buetti et al. (2019).

## 4. General Methods

### 4.1. Sample Size: Participants and Trials

To determine our sample size, we carried out a simulation study to estimate the effect of reducing the number of trials and increasing the number of participants on our ability to accurately measure the  $D_i$ . While our reanalysis of Buetti et al. (2019)’s data is unable to distinguish between the three models of contrast combination, we believe that this is due to the feature values used in their study, rather than low statistical power from sampling (see above and Figure ??). Therefore, we will base our sensitivity analysis around the width of the 97% HPDI when estimating  $D_{\text{blue}}$ . We have chosen to look at this single feature level as the blue distractor trials offer the greatest discrimination between the three contrast models.

We carried out our simulation sensitivity analysis by generating synthetic data from the shifted lognormal model outlined in Section ??, Figure ??, for the blue distractor conditions. This was done for several different sample sizes, both in terms of number of trials and number of participants. For each synthetic dataset, we then refit the model and calculated the width of the 97% HPDI (see Figure 3).

As we are moving from the between-subjects design used by Buetti et al. (2019) to a within-subjects design in which each participant sees all combinations

of features, we prefer to decrease the number of trials per person  $\times$  condition from 40 to six. Increasing the number of participants from 20 to 150 will allow us to maintain sufficient accuracy in the estimating of logarithmic search slopes.

Ethical approval for the study was granted by the University of Aberdeen (application number PEC/4677/2021/2).

#### 4.2. *Stimuli*

The targets and distractors are randomly assigned to the display based on an invisible grid. Within each quadrant of the screen, there are three 'spokes' each with four possible target positions (starting from the centre of the screen and moving outwards), creating 36 different target positions in total, in three concentric circles. A small amount of jitter is added to each possible position to make the target locations less predictable.

**Distractor and target types:** we will replicate the distractor types used in Buetti et al. (2019), apart from that we will change one distractor colour (from blue to pink) to allow us to discriminate better between different models of the data (see above). There are six single-feature conditions (purple, orange and pink distractors and triangle, circle and diamond distractors) and nine double-feature conditions (all possible pairings of the single-feature conditions). The target is always a red semicircle, except in the trials where the distractors are single-feature shapes (triangles, circles and diamonds) in which case the target is a white semicircle.

**Set sizes:** we will run all the distractor set sizes used in Buetti et al. (2019) (1, 4, 9, 19 and 31). We will also run target-only 'zero distractor' trials (60 in total, with 12 being the white semicircle target and the remainder the red semicircle target).

The experiments were programmed in PsychoPy and Pavlovia (Peirce et al., 2019). Stimuli were pre-made to generate search array images with  $1920 \times 1080$  resolution.

#### 4.3. *Procedure*

Participants will complete the experiment in the laboratory, sitting at a viewing distance of 45cm from the screen. They will view a fixation cross before viewing a search array: they will press the space bar to continue to the trial. Participants will be told to search for the target among distractors (i.e. will be told to perform a singleton search) and report if the semicircle target points to the left or right, by pressing either the 'f' or 'j' key respectively on their keyboard. They

will first complete 16 practice trials where they will receive feedback immediately after completing each trial. In the real experimental trials, participants will receive feedback on their average accuracy and reaction time after each block of 120 trials. Participants will complete 8 blocks of trials (960 trials overall i.e. 192 trials in each of 5 experiments, consisting of 5 set sizes x 3 distractor conditions x 12 repeats + 12 zero distractor trials) with the order of the stimuli being fully randomised i.e. all different conditions will be completely intermixed (in the terminology of Buetti et al. (2019), participants will complete all of Experiments 1 and 2 in the same testing session, rather than having different participants complete each separate sub-experiment).

In both the practice and experimental trials, the search display will always remain on screen until a response is made, or until 5 seconds had passed.

#### 4.4. Data Pre-processing

Only participants who complete the full experiment will be considered candidates for inclusion in the data analysis. We will apply the same inclusion criteria as the original paper: participants will only be included if their search accuracy over 90% and their average response time is not smaller or larger than two standard deviations from the group average response time.

For participants included in the analysis, we will apply the data cleaning used in Section ?? i.e. removing the top and bottom 1% of their data.

#### 4.5. Analysis Plan

All analysis will be carried out using R (vx.xx)<sup>2</sup>, brms (v.xx.xx) and rStan (vx.xxxx) As discussed above, we will use a mixed-effect models with either normal, lognormal or shifted lognormal distributions.

Please see the analysis of our pilot data for a full implementation of our analysis pipeline, including all code (available on Github at [https://github.com/scienceanna/TCS\\_Bayesian](https://github.com/scienceanna/TCS_Bayesian)).

## 5. Results

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## 6. General Discussion

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<sup>2</sup>Version numbers will be recorded upon completion of final analysis.



427 **Conflict of interest**

428 The authors declare that they have no conflict of interest.

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