

Traveling Salesperson Problem

- TSP. Given a set of n cities and a pairwise distance function $d(u, v)$, is there a tour of length $\leq D$?
- HAM-CYCLE: given a graph $G = (V, E)$, does there exist a simple cycle that contains every node in V .

- Claim. $\text{HAM-CYCLE} \leq_p \text{TSP}$.

- Pf.

- Given instance $G = (V, E)$ of HAM-CYCLE, create n cities with distance function

$$d(u, v) = \begin{cases} 1 & \text{if } (u, v) \in E \\ 2 & \text{if } (u, v) \notin E \end{cases}$$

- G is Hamiltonian iff TSP instance has tour of length $\leq D=n$. (proof is omitted)▪
 - Remark. TSP instance in reduction satisfies Δ -inequality.