

# ZIMPL

(Zuse Institute Mathematical Programming Language)

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## Abstract

ZIMPL is a little language to translate the mathematical model of a problem into a linear or (mixed-)integer mathematical program expressed in `lp` or `mps` file format which can be read by a LP or MIP solver.

*May the source be with you, Luke!*

## 1 Introduction

Most of the things in ZIMPL (and a lot more) can be found in the wonderful book about the modelling language AMPL from Robert Fourer, David N. Gay and Brian W. Kernighan [FGK93]. Indeed if not the guys at ILOG had needed more than three months just to tell me the price of AMPL for CPLEX, I would probably use AMPL today. On the other hand, having the source code of a program has its advantages. The possibility to run it regardless of architecture and operating system, the ability to modify it to suite the needs and not having to hassle with license managers may make a much less powerful program the better choice. And so ZIMPL came into being.

A linear program (LP) might look like this:

$$\begin{array}{ll} \min & 2x + 3y \\ \text{subject to} & x + y \leq 6 \\ & x, y \geq 0 \end{array}$$

The usual format to store the description of such a problem is `mps` invented by IBM [IBM97] long ago. Nearly all available LP and MIP solvers can read this format. While `mps` is a nice format to punch into a punch card and at least a reasonable format to read for a computer it is quite unreadable for humans.

```
NAME          ex1.mps
ROWS
  N  OBJECTIV
  L  c0
COLUMNS
      x          OBJECTIV          2
      x          c0                1
      y          OBJECTIV          3
      y          c0                1
RHS
      RHS        c0                6
ENDATA
```

Another possibility is the `lp` format [ILO00], which is more readable but is only supported by a few solvers.

```
Minimize
  cost:  +2 x +3 y
Subject to
  c0:  +1 x +1 y <= 6
End
```

But since each coefficient of the matrix  $A$  must be stated explicitly it is also not a desirable choice to develop a mathematical model.

Now, with ZIMPL it is possible to write this:

```
var x;
var y;
minimize cost: 2 * x + 3 * y;
subto c0: x + y <= 6;
```

and have it automatically translated into `mps` or `lp` format. While this looks not much different from what is in the `lp` format, the difference can be seen, if we use indexed variables. Here is an example. This is the LP

$$\begin{array}{ll}\min & 2x_1 + 3x_2 + 1.5x_3 \\ \text{subject to} & \sum_{i=1}^3 x_i \leq 6 \\ & x_i \geq 0\end{array}$$

And this is how to tell it ZIMPL

```
set I      := { 1 to 3 };
param c[I] := <1> 2, <2> 3, <3> 1.5;
var  x[I] >= 0;
minimize value: sum <i> in I : c[i] * x[i];
subto  cons: sum <i> in I : x[i] <= 6;
```

## 2 Invocation

To run ZIMPL on the model given in the file `ex1.zpl` type the command

```
zimpl ex1.zpl
```

The general case is `zimpl [options] <input-files>`. It is possible to give more than one input file. They are read one after the other and then executed as if they were all in one big file. The result of running ZIMPL will be either an error message or two files.

The two files are the problem generated from the model in either `lp` or `mps` format with extension `.lp` or `.mps` and a file with the extension `.tbl` which lists all variable and constraint names used in the model and there corresponding name in the problem file. The reason for this name translation is that the `mps` format can only handle names up to eight characters long. And in `LP` format the length of the names is also restricted to 16 characters.

The following options are possible (only the first two are normally of interest):

- `-t format` Selects the output format. Can be either `lp` which is default or `mps`.
- `-o name` Sets the base-name for the output files.  
Defaults to the first input file striped of the extension.
- `-n cform` Select the format for the generation of constraint names. Can be either `cm` which will number them  $1 \dots n$  with a 'c' in front. `cn` will use the name supplied in the `subto` statement and number them  $1 \dots n$  within the statement. `cf` will use the name of given with the `subto`, then a  $1 \dots n$  number like in `cm` and then append all the local variables from the `forall` statements.
- `-b` Enables bison debugging output.
- `-d` Enables zimpl debugging output.
- `-f` Enables flex debugging output.
- `-h` Prints a usage message.
- `-v` Enables verbose mode.

A typical invocation is for example:

```
zimpl -o hardone -t mps data.zpl model.zpl
```

This reads the files `data.zpl` and `model.zpl` and produces `hardone.mps` and `hardone.tbl`.

## 3 Format

Each ZPL-file consists of five types of statements: Sets, parameters, variables, an objective and constraints. Each statement ends with a semicolon (;). Everything from a number-sign (#) to the end of the line is treated as a comment and is ignored.

If a line starts with the word `include` followed by a filename in double quotation marks, this file is read instead of this line.

ZIMPL works on the lowest level with two types of data: Strings and numbers. A string is delimited by double quotation marks ("). A number can be given as 2, -6.5 or 5.234e-12. Wherever a number or string is required, it is also possible to give a parameter of the right value type. Also numeric expressions are allowed instead of just a number. The precedence of numeric, boolean and set operators should be the usual one. If in doubt use parenthesis to be save.

### Numeric expressions

The following functions are currently implemented:  $\wedge$ , +, -, \*, /, mod, div, abs, floor, ceil, log (logarithm with base 10), ln (logarithm with base  $e$ ), exp ( $e^x$ ), !.  $\wedge$  stands for *to the power of*. mod is the modulo function and div gives the integer part of a division. \*\* can be used as synonym for  $\wedge$ . With min and max it is possible to find the minimum/maximum member of an one dimensional set of numeric values. card gives the cardinality of a set.

The following is also a numeric expression:

*if boolean-expression then numeric-expression else numeric-expression end.*

### Boolean expressions

For numbers <, <=, ==, !=, >=, > are defined. For strings only == and != are available. The expression *tuple in set-expression* can be used to test set membership of a tuple. Combinations of boolean-expressions with and, or and negation with not are possible.

### Sets

The elements of a set are tuples. Each tuple of a set has the same number of components. The components are either numbers or strings. The type of the n-th component of each tuple must be the same. A tuple starts and ends with < and >, resp. The components are separated by commas. If tuples are one-dimensional, it is possible to omit the braces in a list of elements, but then they must be omitted from all tuples of the set.

**Set functions**

A cross B	Cross product	$\{(x, y)   x \in A \wedge y \in B\}$
A union B	Union	$\{x   x \in A \vee x \in B\}$
A inter B	Intersection	$\{x   x \in A \wedge x \in B\}$
A without B	Difference	$\{x   x \in A \wedge x \notin B\}$
A symdiff B	Symmetric difference	$\{x   (x \in A \wedge x \notin B) \vee (x \in B \wedge x \notin A)\}$
{n to m by s}	Generate, (default s = 1)	$\{x   x = n + is \leq m, i \in \mathbb{N}_0\}$
proj(A, t)	Projection $t = (e_1, \dots, e_n)$	The new set will consist of $n$ -tuples, with the $i$ -th component being the $e_i$ -th component of $A$ .

It is possible to write `*` instead of `cross`, `+` instead of `union`, `\` or `-` instead of `without` and `..` instead of `to`.

**Examples**

```
set A := { 1, 2, 3 };
set B := { "hi", "ha", "ho" };
set C := { <1,2,"x">, <6,5,"y">, <787,12.6,"oh"> };
set D := A cross B;
set E := { 6 to 9 } union A without { <2>, <3> };
set F := <i,j> in Q with i > j and i < 5;
set G := { 1 to 9 } * { 10 to 19 } * { "A", "B" };
set H := proj(G, <3,1>)
# will give: <"A",1>, <"A",2"> ... <"B",9>
```

**Parameters**

Parameters can be declared with or without an indexing set. Without indexing the parameter is just one value, which is either a number or a string. For indexed parameters there is one value for each member of the set. There are not much uses for string valued parameters, so normally they are all numbers.

Parameters are declared in the following way: The keyword `param` is followed by the name of the parameter optionally followed by the indexing set. Then after the assignment sign comes a list of pairs. The first element of each pair is a tuple from the index set, the second element is the value of the parameter for this index.

**Examples**

```
param q := 5;
param u[A] := <1> 17, <2> 29, <3> 12;
```

```
param w[C] := <1,2,"x"> 1/2, <6,5,"y"> 2/3;
```

In the example, no value is given for index `<787,12.6,"oh">` of parameter `w`, that is assignments need not to be complete. This is correct as long as it is never referenced.

## Variables

Like parameters, variables can be indexed. A variable has to be one out of three possible types: Continuous (called *real*), binary or integer. The default is real. Variables may have lower and upper bounds. Defaults are zero as lower and infinity as upper bound. Binary variables are always bounded between zero and one. It is possible to compute the value of the lower or upper bounds depending on the index for the variable (see last declaration in the example).

## Examples

```
var x1;  
var x2 binary;  
var y[A] real >= 2 <= 18;  
var z[<a,b,c> in C] integer  
    >= a * 10  
    <= if b <= 3 then p[b] else 10 end;
```

## Objective

There must be exactly one objective statement in a model. The objective can be either minimize or maximize. Following the keyword is a name, a colon (:) and then a term consisting of variables.

## Example

```
minimize cost: 12 * x1 -4.4 * x2  
    + sum <a> in A : u[a] * y[a]  
    + sum <a,b,c> in C with a in E and b > 3 : -a/2 * z[a,b,c];
```

## Constraints

The general format for a constraint is `subto name: term sense term`. Name can be any name starting with a letter. The term is defined as in the objective. Sense is one of `<=`, `>=` and `==`. Many constraints can be generated with one statement by the use of the `forall` instruction, see below.

## Examples

```
subto time : 3 * x1 + 4 * x2 <= 7;
subto space: sum <a> in A : 2 * u[a] * y[a] >= 50;
subto weird: forall <a> in A :
    sum <a,b,c> in C : z[a,b,c] == 55;
subto c21: 6 * (sum <i> in A : x[i]
    + sum <j> in B : y[j]) >= 2;
subto c40: x[1] == a[1] +
    2 * sum <i> in A do 2*a[i]*x[i]*3 + 4;
```

## Details on `sum` and `forall`

The general forms are

`forall index do term` and `sum index do term`.

It is possible to nest several `forall` instructions. The general form of *index* is

*tuple* in *set* with *boolean-expression*.

It is allowed to write a colon (:) instead of `do` and a vertical bar (|) instead of `with`.

The number of components in the *tuple* and in the components of the members of the *set* must match. The *with* part of an *index* is optional. The *set* can be any expression giving a set.

## Examples

```
forall <i,j> in X cross { 1 to 5 } without { <2,3> }
    with i > 5 and j < 2 do
        sum <i,j,k> in X cross { 1 to 3 } cross Z do
            p[i] * q[j] * w[j,k] >= if i == 2 then 17 else 53;
```

Note that in the example *i* and *j* are set by the `forall` instruction. So they are fixed for all invocations of `sum`.

## Initialising sets and parameters from a file

It is possible to load the values for a set or a parameter from a file. The syntax is

```
read filename as template [skip n] [use n] [fs s] [comment s]
```

*filename* is the name of the file to read.

*template* is a string with a template for the tuples to generate. Each input line from the file is split in fields. The splitting is done according to the following rules: Whenever a space, tab, comma, semicolon or double colon is encountered a new field is started. Text that is enclosed in double quotes is not split, the quotes are always removed. When a field is split all space and tab characters around the splitting are removed. If the split is due to a comma, semicolon or double colon, each occurrence of these characters starts a new field.

## Examples

All these lines have three fields:

```
Hallo;12;3
Moin 7 2
"Hallo, Peter"; "Nice to meet you" 77
,,2
```

For each component of the tuple the number of the field to use for the value is given, followed by either a `n` if the field should be interpreted as a number or `s` for a string. Have a look at the example, it is quite obvious how it works. After the template some optional modifiers can be given. The order does not matter.

`skip n` instructs to skip the first  $n$  lines of the file.

`use n` limits the number of lines to use to  $n$ .

`comment s` sets a list of characters that start comments in the file. Each line is ended when any of the comment characters is found.

When a file is read, empty lines are skipped and not counted for the `use` clause. They are counted for the `skip` clause.

## Examples

```
set P := { read "nodes.txt" as <1s> };
```

nodes.txt:

```
Hamburg -> <"Hamburg">
München -> <"München">
Berlin -> <"Berlin">
```

```
set Q := { read "blabla.txt" as "<1s,5n,2n>" skip 1 use 2 };
```

blabla.txt:

```
Name;Nr;X;Y;No -> skip
Hamburg;12;x;y;7 -> <"Hamburg",7,12>
Bremen;4;x;y;5 -> <"Bremen",5,4>
Berlin;2;x;y;8 -> skip
```

```
param cost[P] := read "cost.txt" as "<1s> 4n" comment "#";
```

cost.txt:

```
# Name Price -> skip
Hamburg 1000 -> <"Hamburg"> 1000
München 1200 -> <"München"> 1200
Berlin 1400 -> <"Berlin"> 1400
```

```
param cost[Q] := read "haha.txt" as "<3s,1n,2n> 4s";
```



```
haha.txt:
  1:2:ab:con1    ->    <"ab",1,2> "con1"
  2:3:bc:con2    ->    <"bc",2,3> "con1"
  4:5:de:con3    ->    <"de",4,5> "con1"
```

## 4 Error messages

Here are some of the incomprehensible error messages ZIMPL can produce:

### **Comparison of different types**

It is not possible to compare a number with a string.

### **xxx of incompatible sets**

The members of the two sets involved in operation `xxx` have not the same number of components.

### **Illegal element xxx for symbol**

In the initialisation of a parameter, tuple `xxx` is not a member in the index set.

### **WITH not allowed here**

When initialising the bounds of variables by index, the `with` clause to exclude some of the elements is not allowed.

### **Comparison of different dimension tuples**

Two tuples were compared which have a different number of components. This is never a good idea, since such tuples are always different.

### **Comparison of elements with different types**

Two tuples were compared which have a different type for the `n`-th element. This is never a good idea, since such tuples are always different.

### **Type error, expected xxx got yyy**

In some context type `xxx` was expected, but the interpreter found type `yyy`. The meaning of the numbers could be looked up in `code.h`.

### **Duplicate constraint name "xxx"**

The name given to a `subto` statement was already used with another `subto` statement. Either change the name, or use `-n cm` or `-n cf`.

## 5 Remarks

ZIMPL is licensed under the GNU general public licence version 2. For more information on free software see <http://www.gnu.org>. The latest version of ZIMPL can be found at <http://www.zib.de/koch/zimpl>. If you find any bugs you can email me at <mailto:koch@zib.de>. Please include an example that shows the problem. If somebody extends ZIMPL, I am interested in getting patches to put them back in the main distribution.

## References

- [FGK93] R. Fourier, D. M. Gray, and B. W. Kernighan. *AMPL: A Modelling Language for Mathematical Programming*. boyd & fraser publishing company, Danvers, Massachusetts, 1993.
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- [ILO00] *ILOG CPLEX 7.0 Reference Manual*. ILOG, 2000.
- [vH99] Pascal van Hentenryck. *The OPL Optimization Programming Language*. MIT Press, Cambridge, Massachusetts, 1999.
- [XPR99] *XPRESS-MP Release 11 Reference Manual*. Dash Associates, 1999.