## A卷答案

一 填空题(每小题4分, 共32分)

|    |     | X | 0   | 1   | 2   |
|----|-----|---|-----|-----|-----|
| 2. | 答案: | p | 0.3 | 0.4 | 0.3 |

- 3. 答案:0.15
- 4. 答案: $\frac{1}{2}$

5. 答案:
$$\frac{1}{2}max\{X_1, X_2, \cdots, X_n\}$$

6. 答案: 
$$\frac{\pi}{12}(a^2+ab+b^2)$$

7. 答案: 
$$f_Y(y) = \begin{cases} \frac{1}{y^2}, y \ge 1\\ 0, y < 1 \end{cases}$$

8. 答案:
$$\frac{1}{50}$$

二 选择题(每小题4分, 共32分)

- 1. 答案:B
- 2. 答案:D
- 3. 答案:C
- 4. 答案:C
- 5. 答案:A
- 6. 答案:B
- 7. 答案:D
- 8. 答案:D

解答:(1)
$$f_X(x) = \begin{cases} \int_0^2 \left(x^2 + \frac{1}{3}xy\right) dy = 2x^2 + \frac{2}{3}x, & 0 \le x \le 1 \\ 0, & \text{其他} \end{cases}$$

$$f_Y(y) = \begin{cases} \int_0^1 \left(x^2 + \frac{1}{3}xy\right) dx = \frac{1}{3} + \frac{1}{6}y, & 0 \le y \le 2 \\ 0, & \text{其他} \end{cases}$$

$$(2)P(X + Y \le 2) = \int_0^1 \int_0^{2-x} \left(x^2 + \frac{1}{3}xy\right) dy dx = \int_0^1 \left(-\frac{5}{6}x^3 + \frac{4}{3}x^2 + \frac{2}{3}x\right) dx = \frac{41}{72}. \tag{12} \end{cases}$$

$$(12)f(X + Y \le 2) = \int_0^1 \int_0^{2-x} \left(x^2 + \frac{1}{3}xy\right) dy dx = \int_0^1 \left(-\frac{5}{6}x^3 + \frac{4}{3}x^2 + \frac{2}{3}x\right) dx = \frac{41}{72}. \tag{12} \end{cases}$$

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$$(12)f(X + Y \le 2) = \int_0^1 \int_0^{2-x} \left(x^2 + \frac{1}{3}xy\right) dy dx = \int_0^1 \left(-\frac{x}{3}xy\right) dy dx =$$

解答:(1) $EX = \int_0^\theta x \cdot \frac{6x}{\theta^3} (\theta - x) = \frac{\theta}{2}$  (3分)

2/3

$$EX^{2} = \int_{0}^{\theta} x^{2} \cdot \frac{6x}{\theta^{3}} (\theta - x) = \frac{3}{10} \theta^{2}$$

$$DX = \frac{1}{20} \theta^{2} \tag{6分}$$

$$(2)EX = \frac{\theta}{2} = \overline{X}, \hat{\theta} = 2\overline{X} \tag{9分}$$

$$(3)E\hat{\theta} = 2E\overline{X} = \theta,$$
无偏估计...
$$(12分)$$