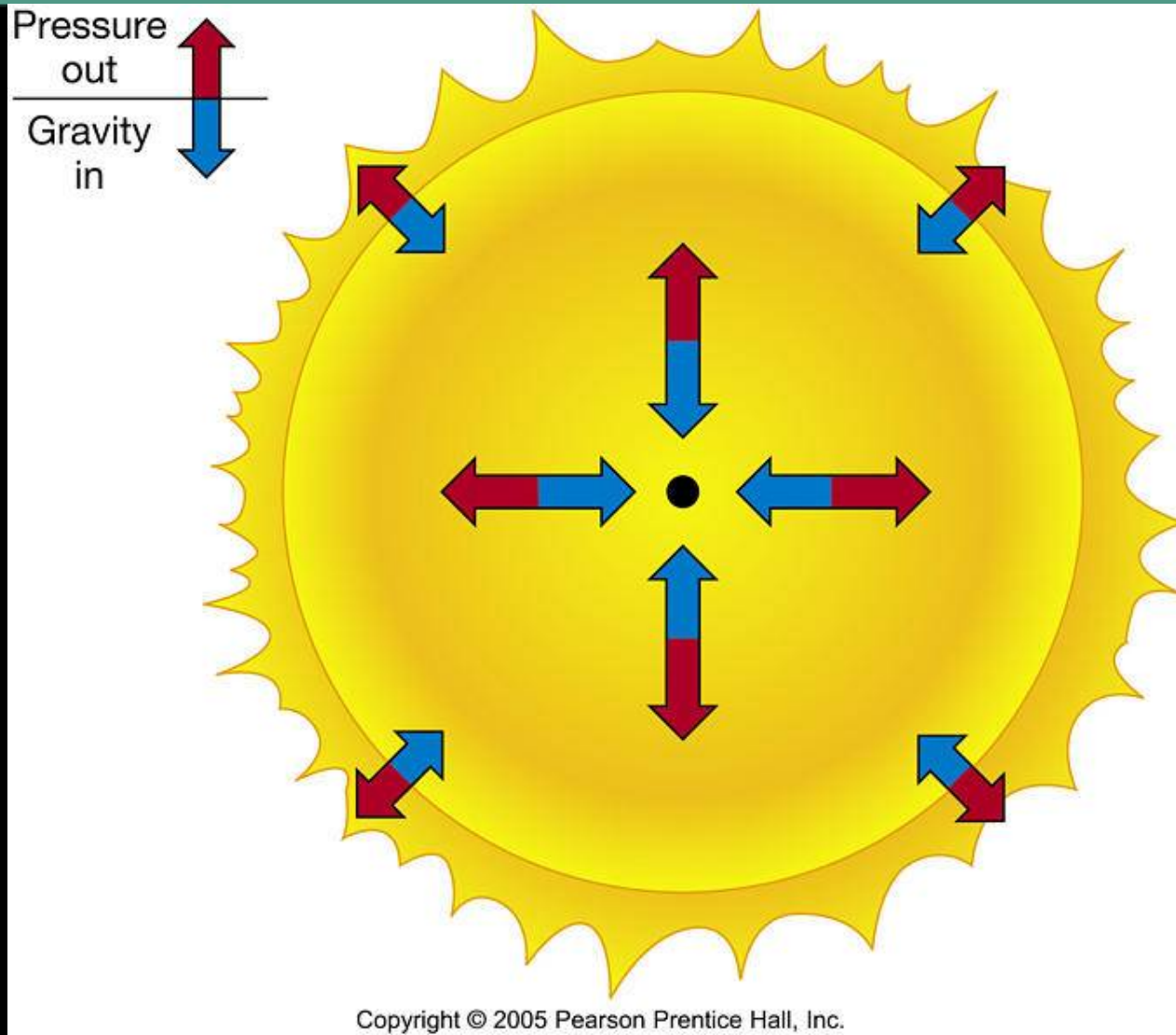


2. The Evolution of Stars (별의 진화)

2-1 Energy Generation (에너지 생성)



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Hydrostatic equilibrium (정 유체역학적 평형)

https://pages.uoregon.edu/jimbrau/BraulmNew/Chap16/FG16_06.jpg

김상철
(Sang Chul KIM)

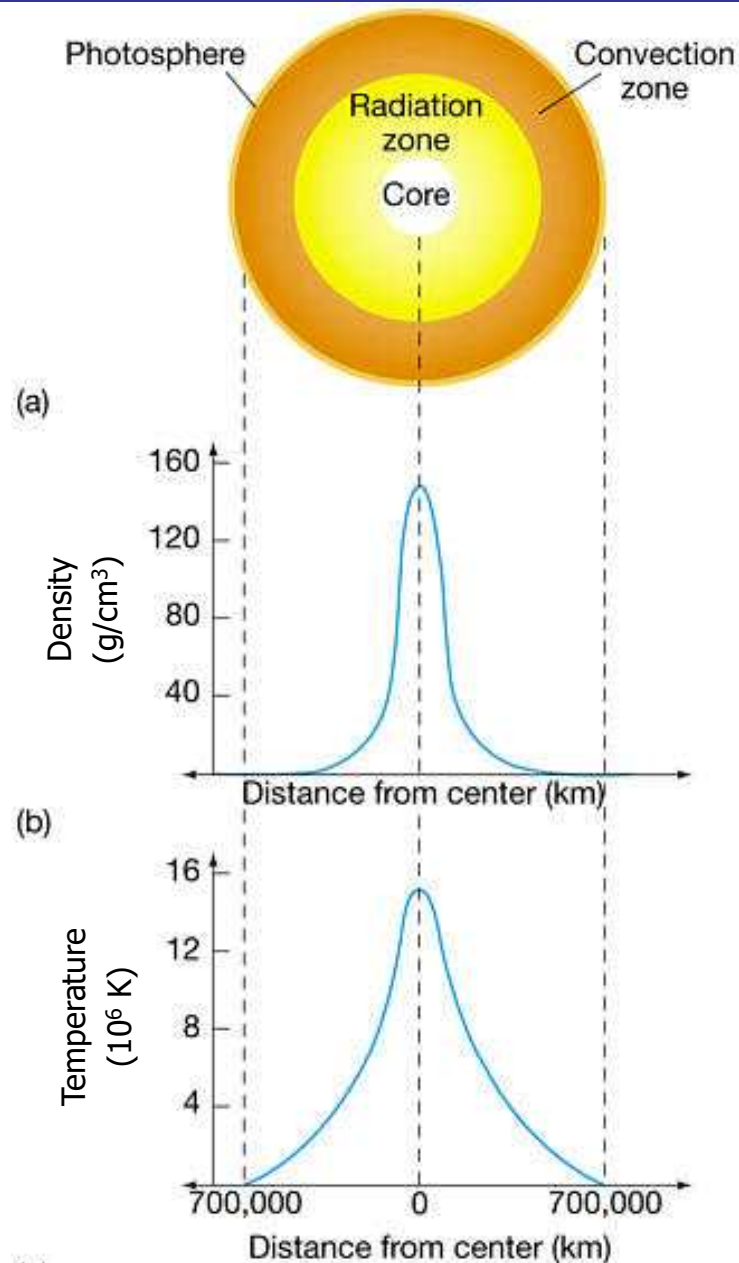
Main Sequence (MS, 주계열성)

- Equilibrium between pressure and gravity, almost constant luminosity
- Nuclear fusion
 - **proton-proton chain** (양성자-양성자 연쇄반응)
 - energy generation and radiation → mass decreases slowly
 - H burning by **CNO cycle** (탄소 순환반응) : $M > 1.5 M_{\odot}$, $T_{\text{center}} > 1.5 \times 10^7 \text{ K}$
- core : N(H) decreases, N(He) increases

Hydrostatic equilibrium (정 유체역학적 평형)

- If somehow core H-burning accelerates \rightarrow Core $T \uparrow$, $P \uparrow \rightarrow$ star expands
- Expansion makes $T \downarrow \rightarrow$ H-burning decelerates
- Hydrostatic equilibrium makes H-burning speed keep \sim constant
 \rightarrow constant luminosity

Interior structure of the Sun (태양의 내부 구조)



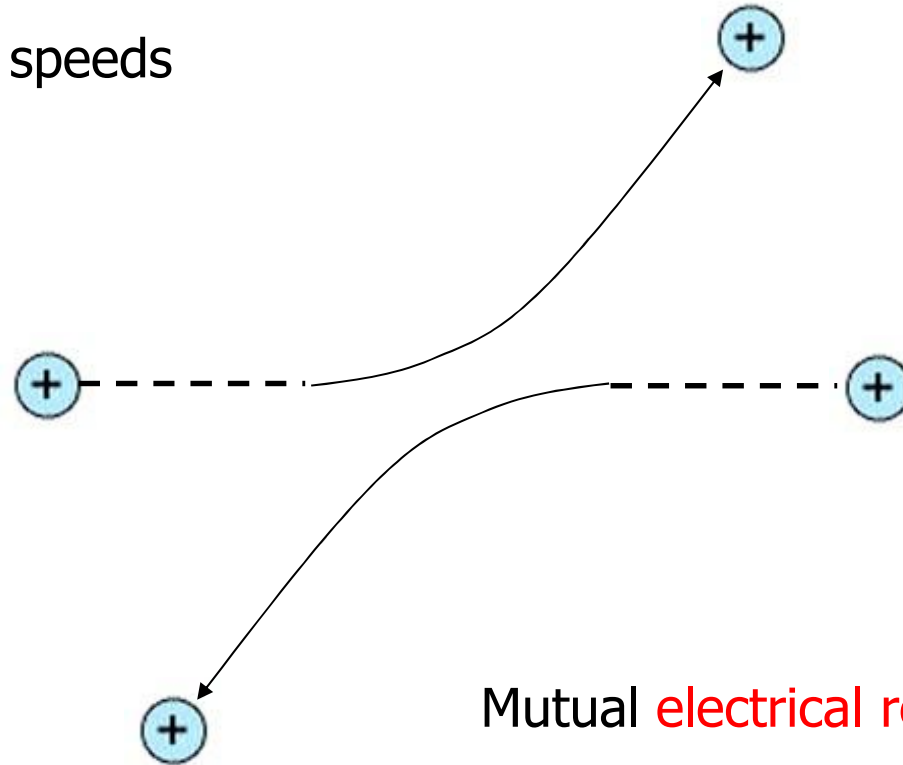
Why H-burning occurs at the core - 1

Low temperature :
small speeds



Why H-burning occurs at the core - 1

Low temperature :
small speeds



Mutual **electrical repulsion**
prevents fusion

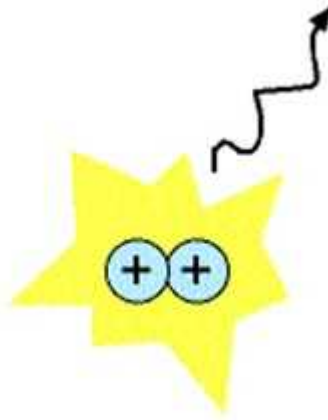
Why H-burning occurs at the core - 1

High temperature :
large speeds



Why H-burning occurs at the core - 1

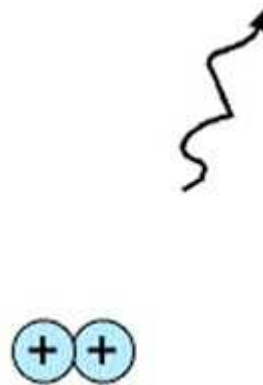
High temperature :
large speeds



Nuclei able to get close enough for **strong nuclear force** (강한 핵력)
to act

Why H-burning occurs at the core - 1

High temperature :
large speeds



Nuclei able to get close enough for **strong nuclear force** (강한 핵력) to act

→ Nuclei fuse & **energy** released

Chemical element - symbol



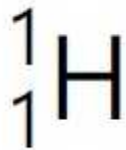
X : chemical symbol (e.g. : H, He, ...)

Z : number of protons (total positive charge, in units of e) 원자번호

A : mass number (total number of nucleons) = atomic weight 원자량(原子量)

$A = Z + N$ = number of protons + number of neutrons

(e.g.)



Energy from proton-proton chain

※ $^{12}\text{C} \rightarrow 12$ ($1.998467052 \times 10^{-23}$ g) (since 1962)

H atomic weight (원자량, 原子量) : 1.0078

4 H \rightarrow 4.0312

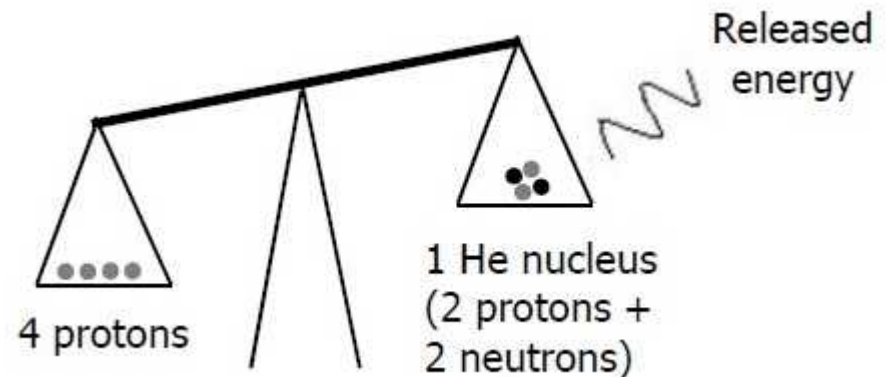
1 He \rightarrow 4.0026

$\Delta m = 4 \times m(\text{p}) - m(\text{He}) = 0.0286$ (mass deficit/defect, 질량 결손)

$$\begin{aligned} E &= \Delta m c^2 \\ &= (0.0286 \times 1.67 \times 10^{-24} \text{g}) \times (3 \times 10^{10} \text{ cm/s})^2 \\ &= 4.3 \times 10^{-5} \text{ erg} \\ &= 4.3 \times 10^{-12} \text{ J} \end{aligned}$$

$E = mc^2$ (Einstein's equation for the equivalence of mass and energy)

1 Joule = 1 kg·m²/s²
= 1 N·m
= **10⁷ erg**
= 6.24×10^{18} eV
= 0.2390 cal
= 2.78×10^{-7} kW·h



Energy from proton-proton chain

- Energy from coal 1 kg $\sim 5000 \text{ kcal} = 2.1 \times 10^7 \text{ J}$
- Use H 1 kg to produce He
 - 0.993 kg He produces, 0.007 kg changes into E
 - $E = mc^2 = 7 \text{ g} \times (3 \times 10^{10} \text{ cm/s})^2 = 7 \times 9 \times 10^{20} \text{ g cm}^2/\text{s}^2$
 $= 6.3 \times 10^{21} \text{ erg} = 6.3 \times 10^{14} \text{ J}$
 - same as E from $3 \times 10^7 \text{ kg} = 30,000 \text{ tons of coal}$

Sun : $4 \times 10^{38} \text{ protons/sec} = 6.68 \times 10^{14} \text{ g/sec}$ are consumed.

Energy from proton-proton chain

$$1 L_{\odot} = 3.9 \times 10^{33} \text{ erg/s} = 3.9 \times 10^{26} \text{ J/s}$$

= amount of electricity for all human beings can use for 10^7 years


Assuming :

Mankind populations = $5 \times 10^9 \rightarrow 10^9$ families (assume 1 family = 5 members)

Monthly family electricity uses, home use : 200~250 kW·h

Let's assume ~ 1000 kW·h/month including commercial use, etc

$$= 10^6 \text{ W} \times 3600 \text{ s/month} = 10^6 \text{ J/s} \times 3600 \text{ s/month} = 3.6 \times 10^9 \text{ J/month}$$


$$1 \text{ W} = 1 \text{ J/s}$$

Monthly mankind electricity uses $\sim 3.6 \times 10^9 \text{ J} \times 10^9 \text{ families/month} = 3.6 \times 10^{18} \text{ J/month}$

$$\rightarrow \frac{3.9 \times 10^{26} \text{ J}}{3.6 \times 10^{18} \text{ J}} = 1.1 \times 10^8 \text{ months} = 9.2 \times 10^6 \text{ years} \sim 10^7 \text{ years}$$

Terminology and β (beta)-decay

α -ray, α -particle : He nucleus

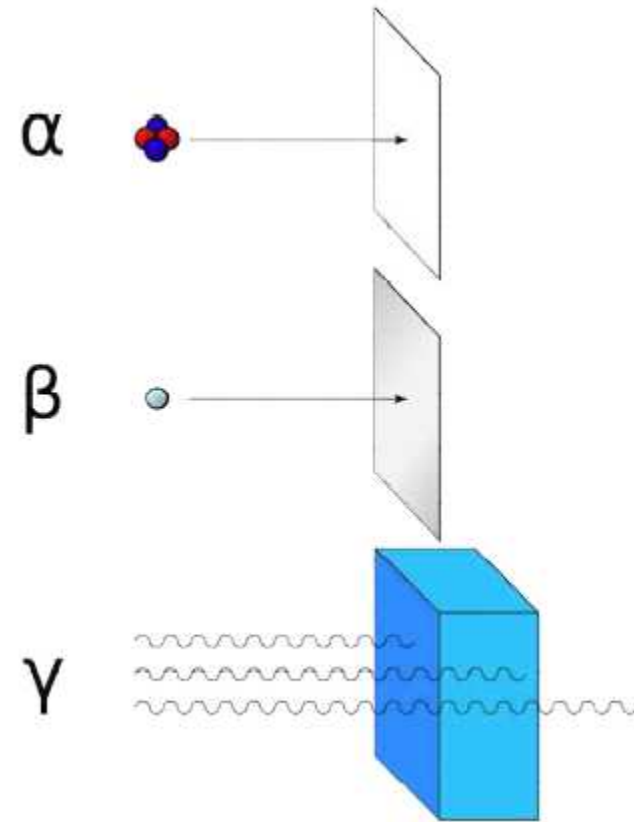
→ cannot penetrate a paper

β -ray : electron

→ cannot penetrate aluminum

γ -ray : high-energy photon

→ absorbed by dense materials (water, lead)



β^- decay : $n \rightarrow p + \beta^- + \overline{\nu}_e$

β^+ decay : $p \rightarrow n + \beta^+ + \nu_e$

※ $\beta^- = e^-$ (electron) 전자

※ $\beta^+ = e^+$ (positron) 양전자

inverse β decay : $p + e \rightarrow n + \nu$
(IBD)

Periodic Table of the Elements

Periodic Table of the Elements

1

H

Hydrogen

1.01

2

3

Li

Lithium

6.94

4

Be

Beryllium

9.01

5

B

Boron

10.81

6

C

Carbon

12.01

7

N

Nitrogen

14.01

8

O

Oxygen

16.00

9

F

Fluorine

19.00

10

Ne

Neon

20.18

11

Na

Sodium

22.99

12

Mg

Magnesium

24.31

13

Al

Aluminum

26.98

14

Si

Silicon

28.09

15

P

Phosphorus

30.97

16

S

Sulfur

32.06

17

Cl

Chlorine

35.45

18

Ar

Argon

39.95

19

K

Potassium

39.10

20

Ca

Calcium

40.08

21

Sc

Scandium

44.96

22

Ti

Titanium

47.88

23

V

Vanadium

50.94

24

Cr

Chromium

51.99

25

Mn

Manganese

54.94

26

Fe

Iron

55.85

27

Co

Cobalt

58.93

28

Ni

Nickel

58.69

29

Cu

Copper

63.55

30

Zn

Zinc

65.38

31

Ga

Gallium

69.72

32

Ge

Germanium

72.63

33

As

Arsenic

74.92

34

Se

Selenium

78.97

35

Br

Bromine

79.90

36

Kr

Krypton

84.80

37

Rb

Rubidium

85.47

38

Sr

Strontium

87.62

39

Y

Yttrium

88.91

40

Zr

Zirconium

91.22

41

Nb

Niobium

92.91

42

Mo

Molybdenum

95.95

43

Tc

Technetium

98.91

44

Ru

Ruthenium

101.07

45

Rh

Rhodium

102.91

46

Pd

Palladium

106.42

47

Ag

Silver

107.87

48

Cd

Cadmium

112.41

49

In

Indium

114.82

50

Sn

Tin

118.71

51

Sb

Antimony

121.76

52

Te

Tellurium

127.6

53

I

Iodine

126.90

54

Xe

Xenon

131.29

55

Cs

Cesium

132.91

56

Ba

Barium

137.33

57-71

Lanthanides

72

Hf

Hafnium

178.49

73

Ta

Tantalum

180.95

74

W

Tungsten

183.85

75

Re

Rhenium

186.21

76

Os

Osmium

190.23

77

Ir

Iridium

192.22

78

Pt

Platinum

195.08

79

Au

Gold

196.97

80

Hg

Mercury

200.59

81

Tl

Thallium

204.38

82

Pb

Lead

207.20

83

Bi

Bismuth

208.98

84

Po

Polonium

[208.98]

85

At

Astatine

209.98

86

Rn

Radon

222.02

87

Fr

Francium

223.02

88

Ra

Radium

226.03

89-103

Actinides

104

Rf

Rutherfordium

[261]

105

Db

Dubnium

[262]

106

Sg

Seaborgium

[266]

107

Bh

Bohrium

[264]

108

Hs

Hassium

[269]

109

Mt

Meitnerium

[278]

110

Ds

Darmstadtium

[281]

111

Rg

Roentgenium

[280]

112

Cn

Copernicium

[285]

113

Nh

Nihonium

[286]

114

Fl

Flerovium

[289]

115

Mc

Moscovium

[289]

116

Lv

Livermorium

[293]

117

Ts

Tennessine

[294]

118

Og

Oganesson

[294]

Atomic Number

Symbol

Name

Atomic Mass

57 La Lanthanum 138.91	58 Ce Cerium 140.12	59 Pr Praseodymium 140.91	60 Nd Neodymium 144.24	61 Pm Promethium 144.91	62 Sm Samarium 150.36	63 Eu Europium 151.96	64 Gd Gadolinium 157.25	65 Tb Terbium 158.93	66 Dy Dysprosium 162.50	67 Ho Holmium 164.93	68 Er Erbium 167.26	69 Tm Thulium 168.93	70 Yb Ytterbium 173.06	71 Lu Lutetium 174.97
89 Ac Actinium 227.03	90 Th Thorium 232.04	91 Pa Protactinium 231.04	92 U Uranium 238.03	93 Np Neptunium 237.05	94 Pu Plutonium 244.06	95 Am Americium 243.06	96 Cm Curium 247.07	97 Bk Berkelium 247.07	98 Cf Californium 251.08	99 Es Einsteinium [254]	100 Fm Fermium 257.10	101 Md Mendelevium 258.10	102 No Nobelium 259.10	103 Lr Lawrencium [262]

Alkali Metal	Alkaline Earth	Transition Metal	Basic Metal	Metalloid	Nonmetal	Halogen	Noble Gas	Lanthanide	Actinide
--------------	----------------	------------------	-------------	-----------	----------	---------	-----------	------------	----------

Energy generation rate

- H atomic weight : 1.0078

4 H → 4.0312

1 He → 4.0026

$\Delta m = 0.0286$

- $0.0286/4.0312 = 0.0071 \rightarrow 0.71\%$
- Only H in the core → T, P high enough to permit nuclear reactions → $\sim 10\%$ of the mass of the Sun is available for energy conversion
- Thermonuclear energy available in the Sun :

$$\begin{aligned}
 E_{Total} = mc^2 &= \left(\frac{4^1H - ^4He}{4^1H} \times 0.1M_{\odot} \right) \times (c^2) \\
 &= 0.0071 \times (1.99 \times 10^{32} \text{ g}) \times (3 \times 10^{10} \text{ cm/s})^2 \\
 &\approx 10^{51} \text{ g} \cdot \text{cm}^2/\text{s}^2 \\
 &\approx 10^{51} \text{ erg} \\
 &\approx 10^{44} \text{ J}
 \end{aligned}$$

1 J = 10^7 erg

$$1 L_{\odot} = 3.90 \times 10^{33} \text{ erg/s} = 3.90 \times 10^{26} \text{ J/s}$$

$$\rightarrow E/L_{\odot} = \text{Solar lifetime} = 8.11 \times 10^9 \text{ yr} \sim 10 \text{ Gyr}$$

Energy generation rate

※ **AGN** → efficiency of conversion from mass to energy $\sim 10\%$ ($\eta=0.1$)
 (see, e.g., Fabian & Rees 1995, MNRAS, 277, L55,
http://phys.huji.ac.il/~joaw/winterschool/heckman_1.pdf)

※ **Gravitational wave** (e.g, by merging of two identical black holes) → conversion efficiency $\sim 30\%$ ($\eta \sim 0.3$)
 (『Black Hole Physics』 1991, Edited by Venzo de Sabbata, Zhenjiu Zhang, NATO ASI Series, Vol. 364, p. 139)

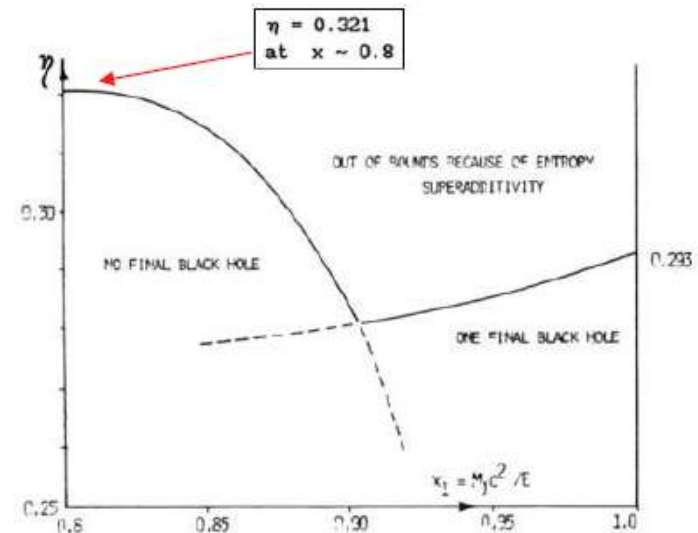
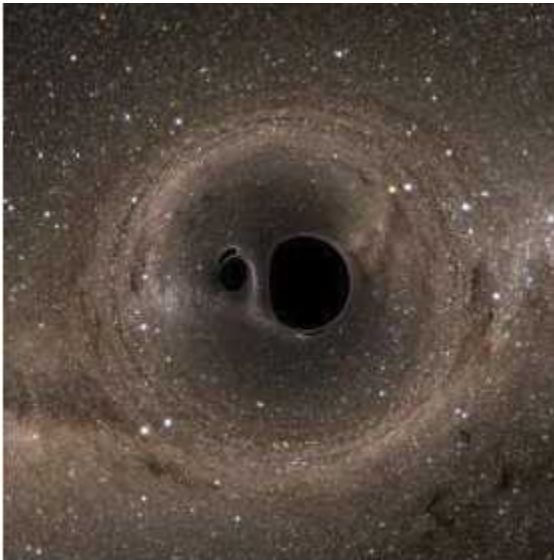
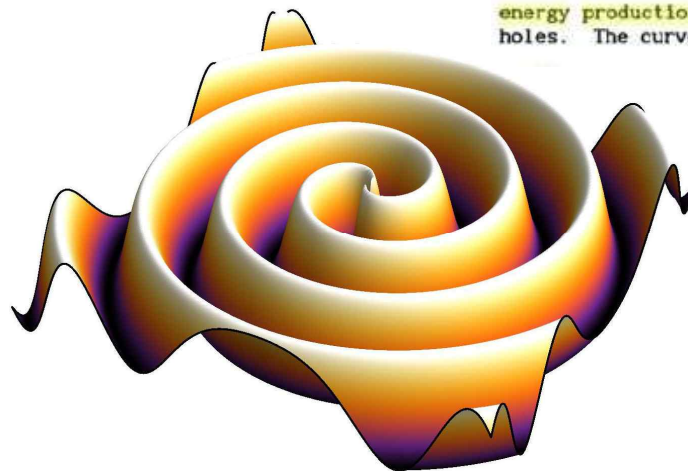


Figure 8. The maximum possible efficiency of gravitational wave energy production by the merging of two identical Schwarzschild black holes. The curves intersect at $x_1 \sim 0.903$, $\eta \sim 0.281$.



<http://news.nationalgeographic.com/2016/02/160211-gravitational-waves-found-spacetime-science/>



<http://www.universetoday.com/127329/gravitational-wave-sources/>

Energy generation rate

MS Lifetime : $\tau = 10^{10}(M/L)$ yr

(M=stellar mass, L=stellar luminosity)

※ Mass-Luminosity Relation :

$$L/L_{\odot} = (M/M_{\odot})^4 \quad \text{for } M > 0.4M_{\odot}$$

$$L/L_{\odot} = (M/M_{\odot})^{2.3} \quad \text{for } M < 0.4M_{\odot}$$

→ $\tau = 10^{10} (M/M_{\odot})^4$ yr = $10^{10} / [M(M_{\odot})]^3$ yr

1 M_{\odot} → 10^{10} yr

10 M_{\odot} → 10^7 yr

O stars (the most massive stars) → **a million** years

"we are seeing some O stars!" = SF is still occurring in the MW

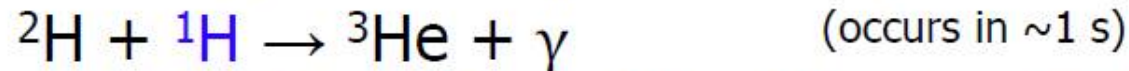
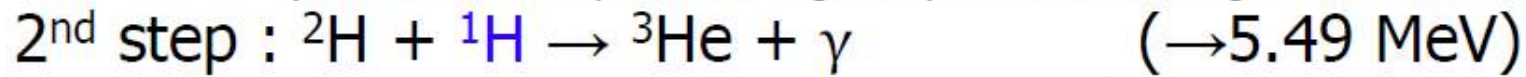
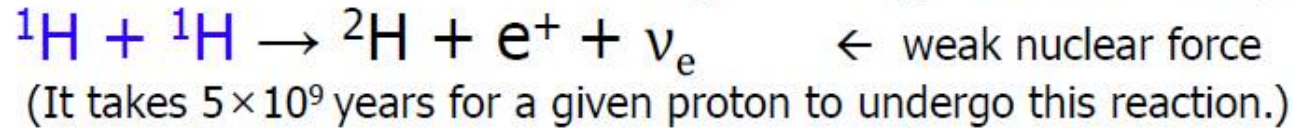
Main-sequence Lifetimes

<http://www.ifa.hawaii.edu/~szapudi/astro110/2007/ch21.pdf>

Mass (M_{\odot})	Effective Temperature (K)	Spectral Class	Luminosity (L_{\odot})	MS Lifetime (10^6 yr)
25	35,000	O	80,000	3
15	30,000	B	10,000	15
3	11,000	A	60	500
1.5	7000	F	5	3000
1.0	6000	G	1	10,000
0.75	5000	K	0.5	15,000
0.50	4000	M	0.03	200,000

http://ircamera.as.arizona.edu/astr_250/Lectures/Lecture_20.htm

Proton-proton (PP) fusion chain process



\leftarrow strong nuclear force

(It takes $\sim 3 \times 10^5$ years.)

${}^1\text{H} = \text{p}$: proton

${}^2\text{H}$: deuterium (중수소) = $\text{p} + \text{n}$

e^+ : positron (e^- 의 반물질 antimatter, same mass,
positive charge)

ν : neutrino (energy, spin, very small mass)

ν_e : electron neutrino

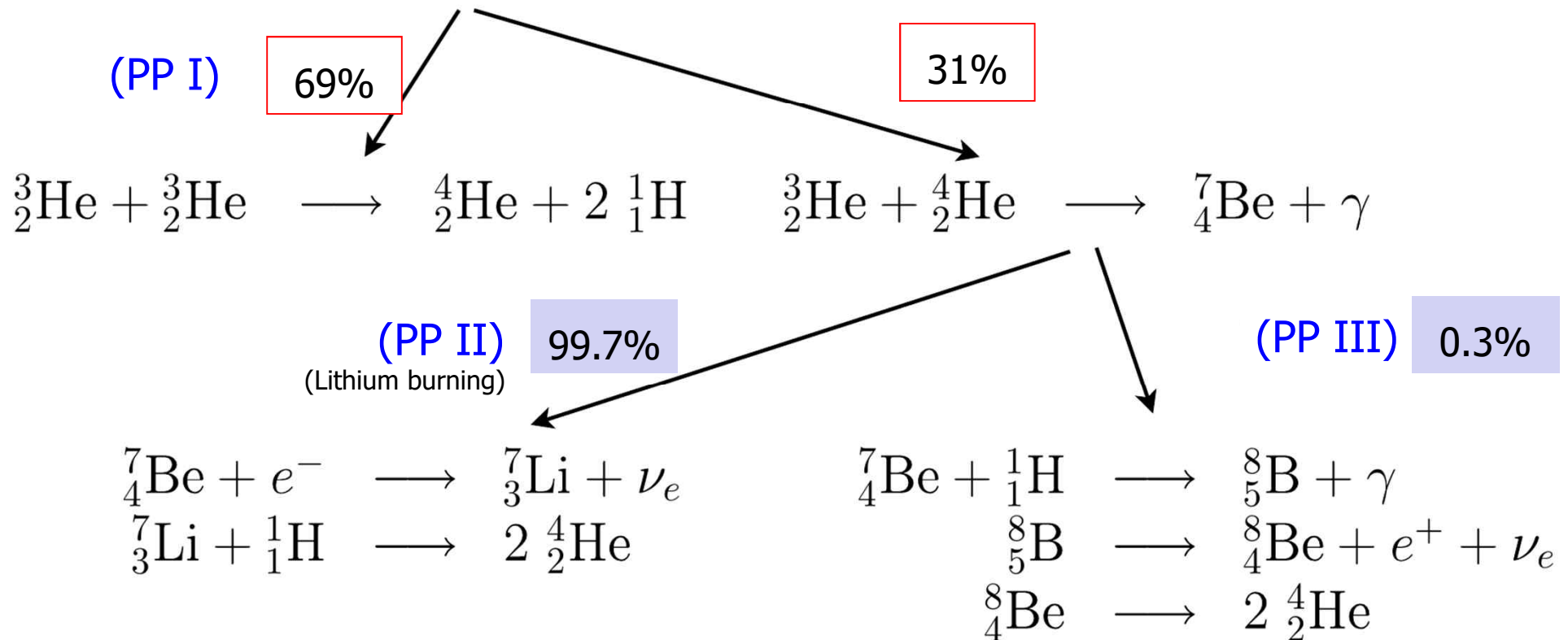
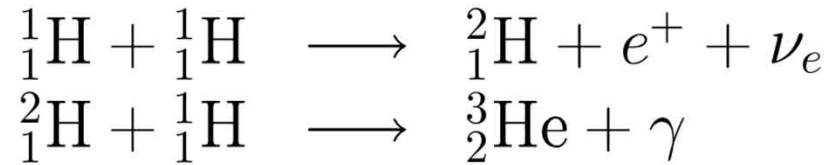
${}^3\text{He}$: helium-3 nucleus = $2\text{p} + 1\text{n}$

γ : photon

${}^4\text{He}$: helium-4 nucleus = $2\text{p} + 2\text{n}$

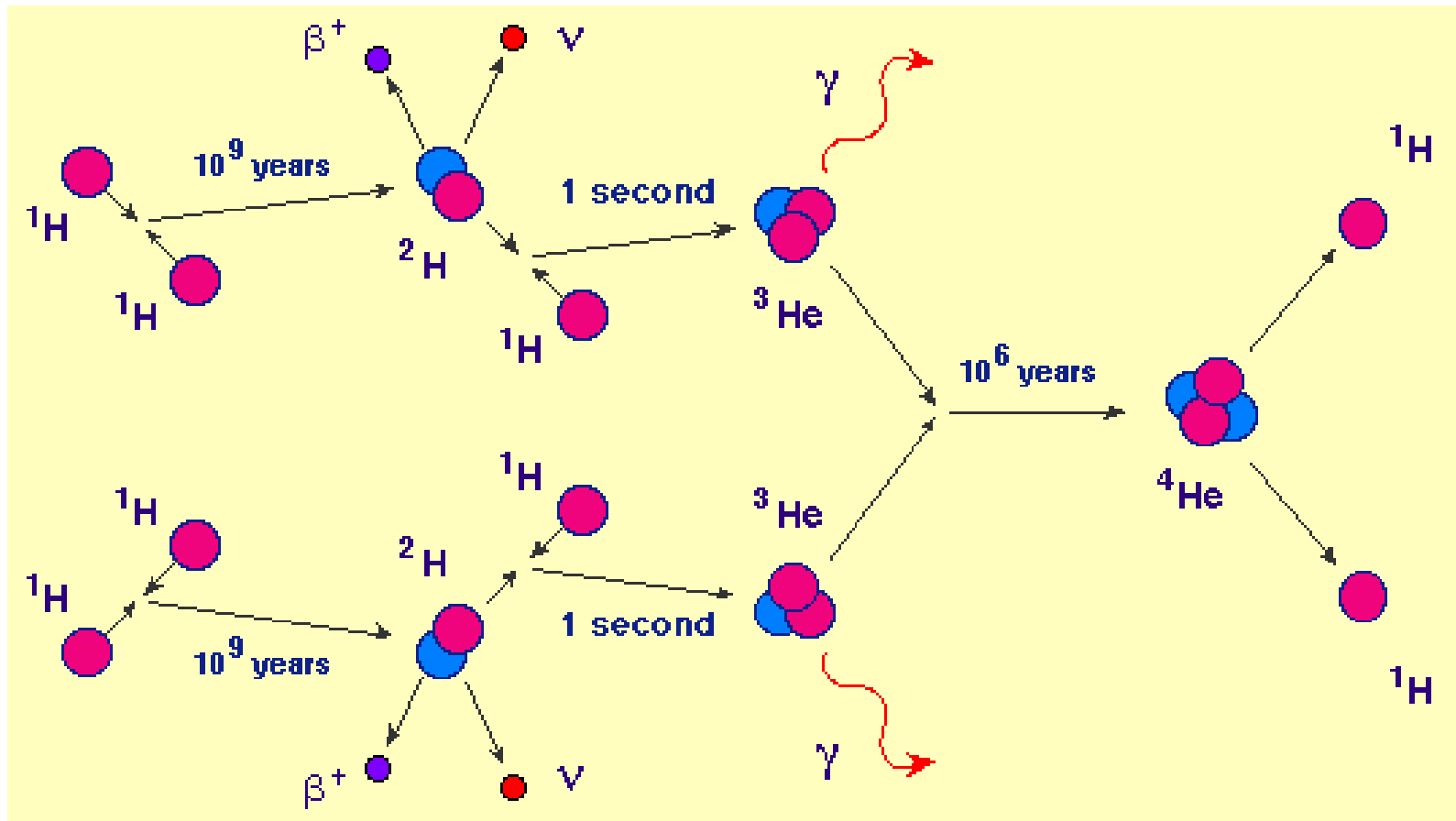
$\rightarrow 91\%$ of the time in the Sun

Proton-proton (**PP**) fusion **chain** process



Why this complicated process?

- Direct collision of 4 H atoms to produce He \rightarrow probability is very low
- Relatively, 2-body collision is more often !



Photon, neutrino – escape from the Sun

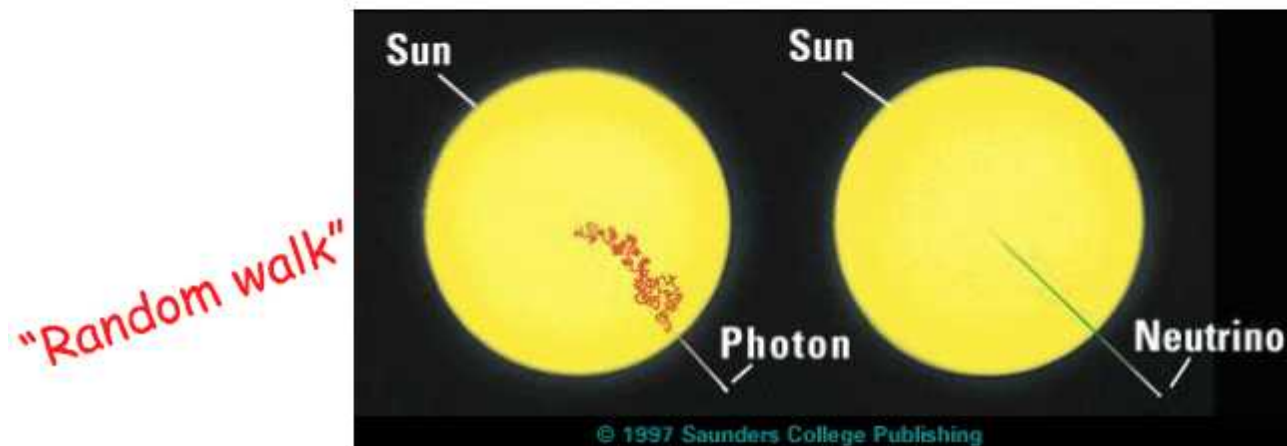
Sun : 2×10^{38} **neutrinos**/sec are generated

※ Solar neutrino problem

Super-Kamiokande (50,000 ton water)
: neutrino oscillation, mass \neq 0
→ [Takaaki KAJITA](#) (2015 Nobel prize)

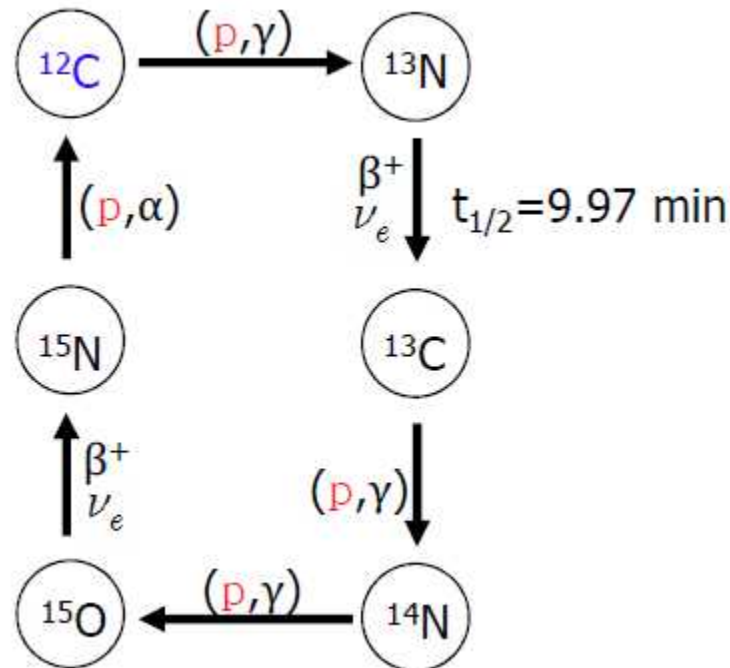
Photon and neutrino – **travel times** out of the center of the Sun

$10^4 - 10^5$ yr 2 sec



CNO Cycle

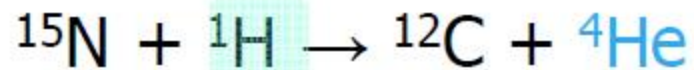
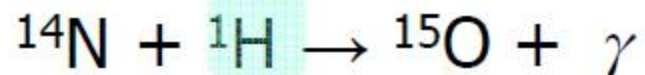
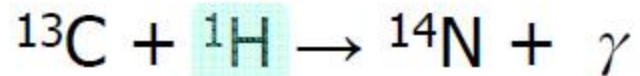
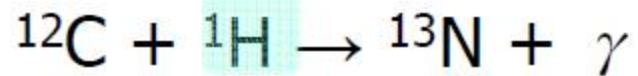
- Carbon = catalyst : a substance that causes a chemical reaction to happen **more quickly**, while the substance **not consumed** and remain unchanged
- 촉매(觸媒) : 반응과정에서 **소모되거나 변화되지 않으면서** 반응속도를 **빠르거나 느리게** 변화시키는 물질



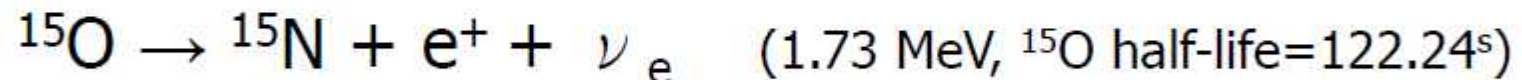
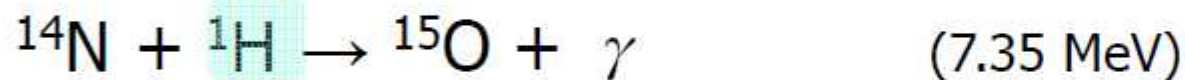
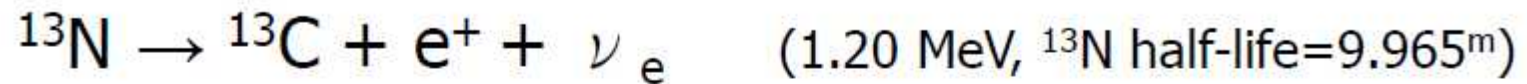
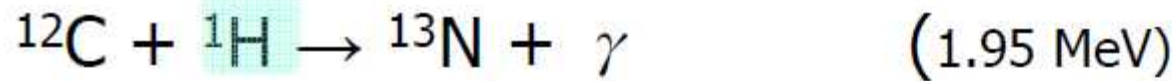
β^+ decay : $p \rightarrow n + \beta^+ + \nu_e$
 ※ $\beta^+ = e^+$ (positron) 양전자

- Start : $\text{C} + \text{p}$
- At high-temp stars : $T > 1.6 \times 10^7 \text{ K}$, $M > 1.5 M_{\odot}$

CNO cycle process



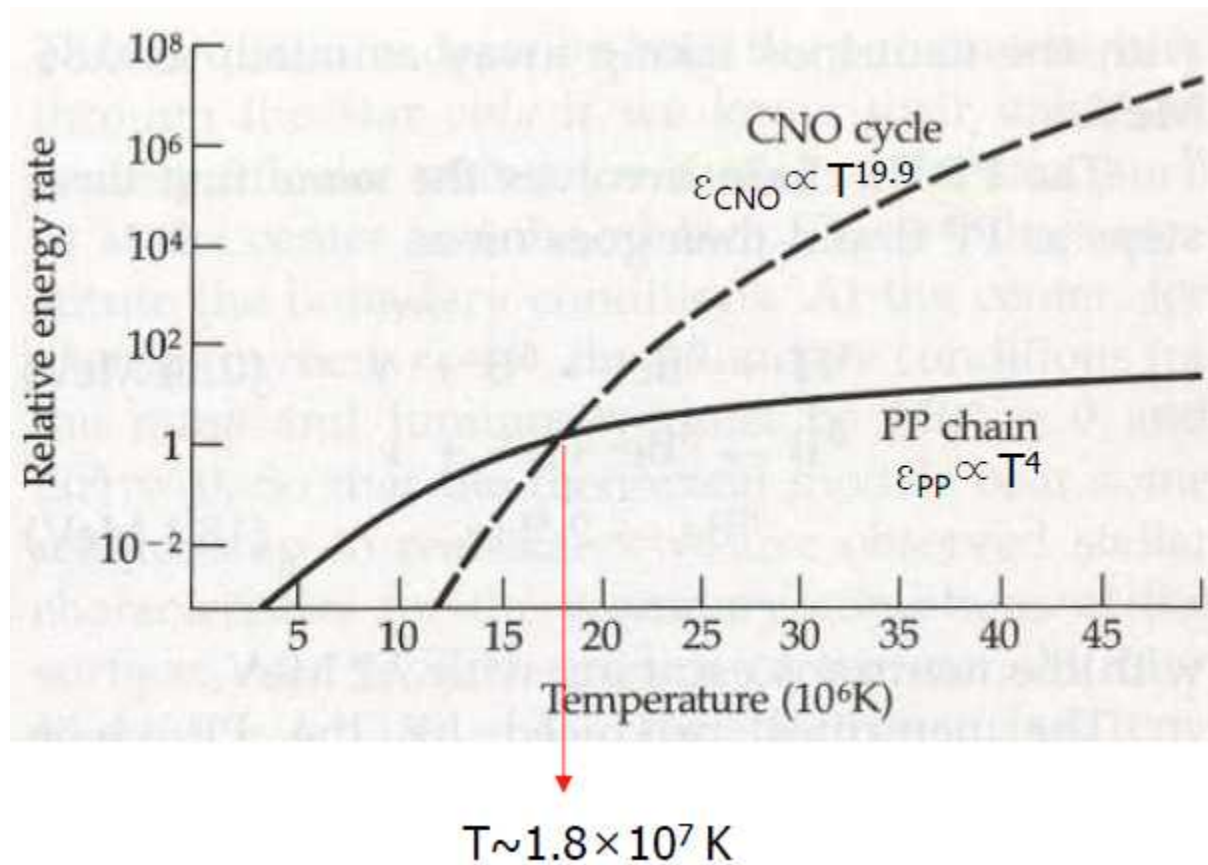
CNO cycle process



※ 2 positrons annihilate with 2 ambient electrons → produce 2.04 MeV

Total 24.73 + 2.04 = 26.73 MeV

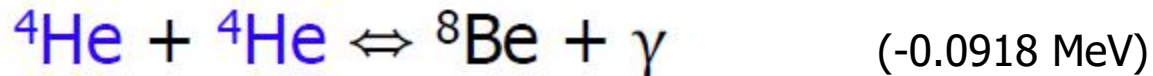
Energy-generation rates



Triple-alpha (3α) process

Nucleosynthesis using **He** :

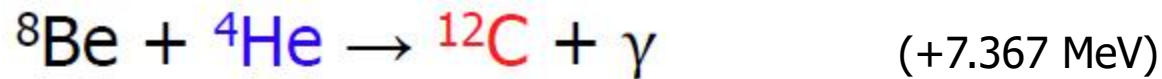
$T \geq 10^8 \text{ K}$, $\rho \geq 10^5 \text{ g cm}^{-3}$: He \rightarrow heavier elements



※ ${}^8\text{Be}$ lifetime $\sim 2.6 \times 10^{-16} \text{ s}$

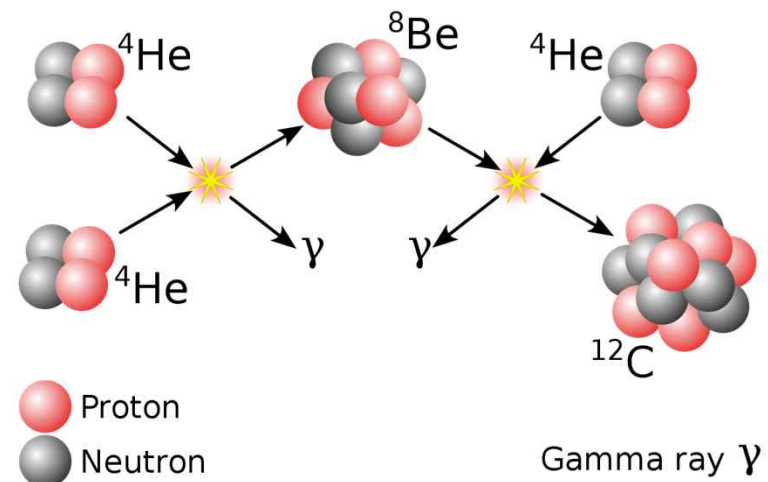
> mean collision (scattering) time of α -particle ($T_{\text{scattering}}$)

Huge amount of He, $n({}^8\text{Be}) : n({}^4\text{He}) = 1 : 10^9$



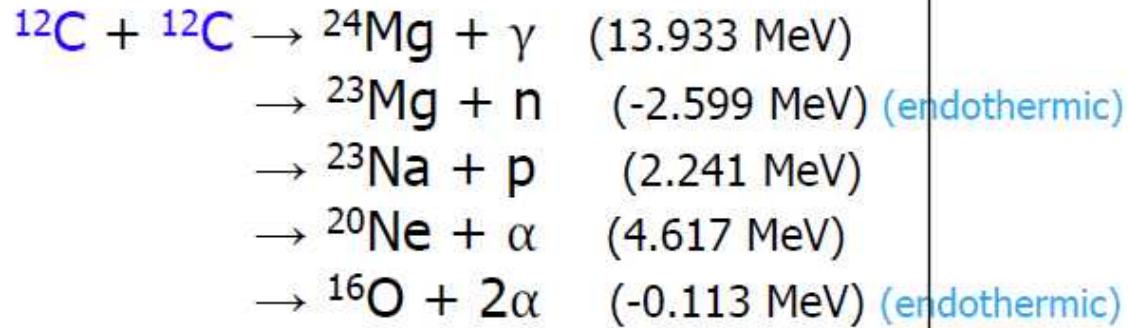
$\langle \text{Emitted energy} \rangle = +7.275 \text{ MeV}$

“Triple- α process”



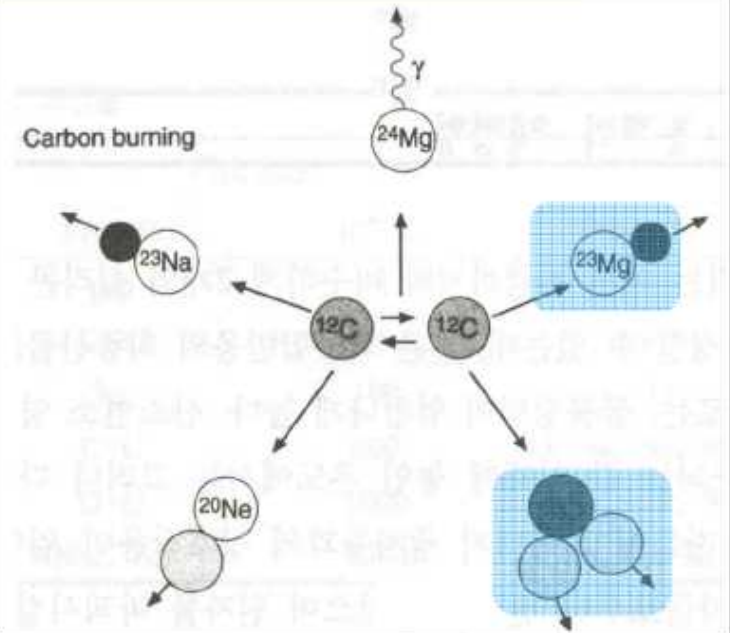
C, O-burning

$T \geq 5 \times 10^8 \text{ K} \rightarrow \text{C-burning}$

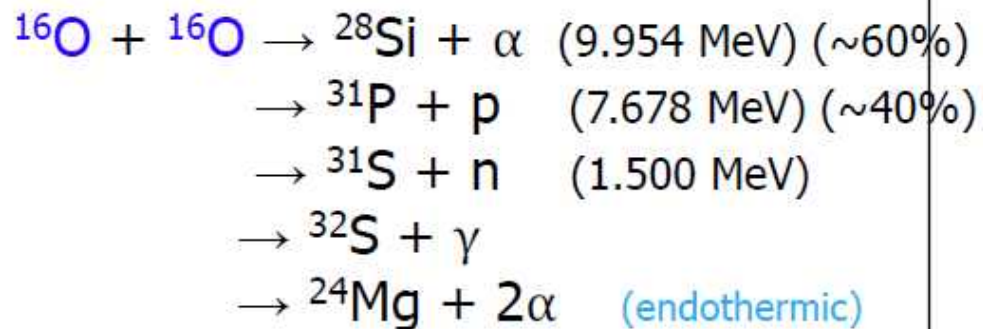


$\langle \text{Emitted energy} \rangle \approx 13 \text{ MeV}$

$\sim 5.2 \times 10^{13} \text{ J/kg} = 5.2 \times 10^{17} \text{ erg/g}$

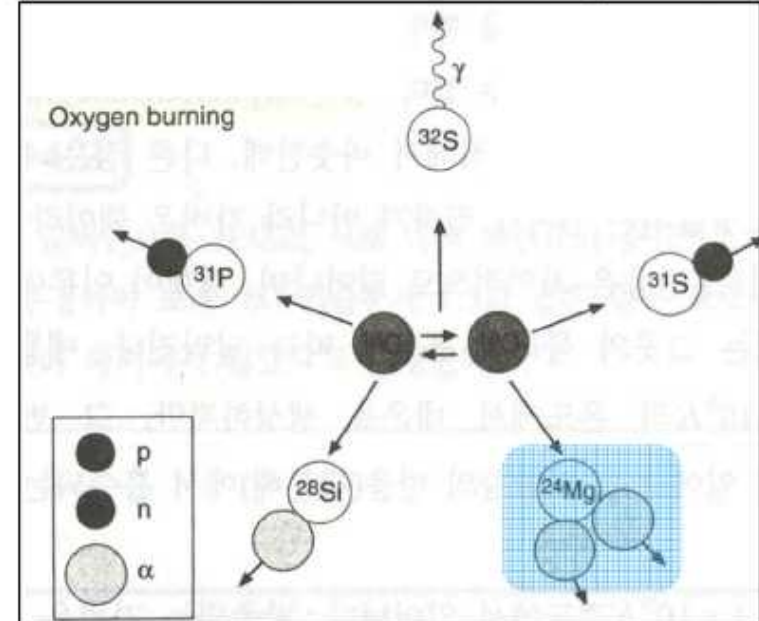


$T \geq 1 \times 10^9 \text{ K} \rightarrow \text{O-burning}$



$\langle \text{Emitted energy} \rangle \approx 16 \text{ MeV}$

$\sim 4.8 \times 10^{13} \text{ J/kg} = 4.8 \times 10^{17} \text{ erg/g}$



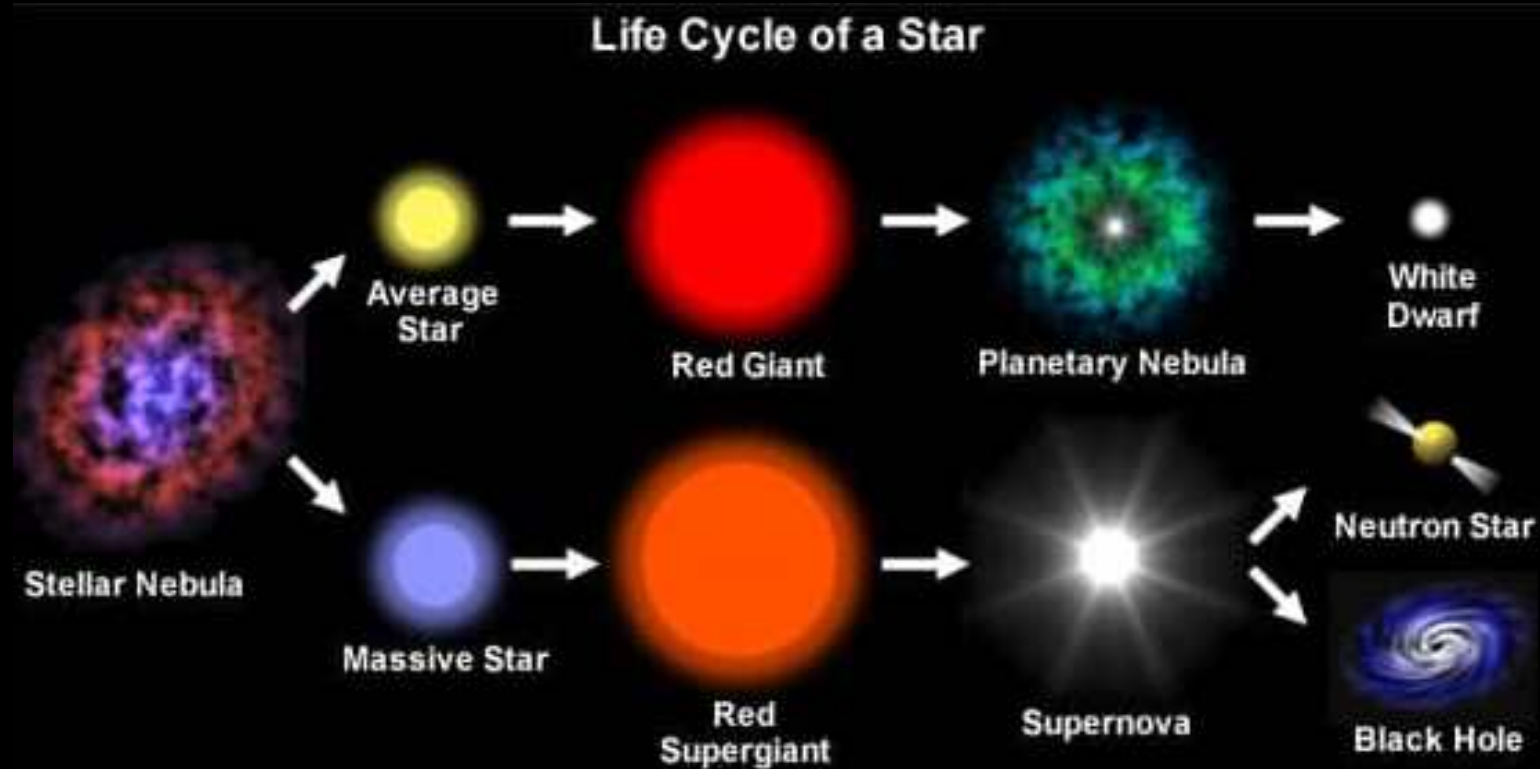
Si-burning

- After O-burning, core = Si + S
- $T \sim (2.7-3.5) \times 10^9 \text{ K}$ (depends on mass)
- Duration ~ 2 weeks
- No further fusion is possible.



2. The Evolution of Stars (별의 진화)

2-2 Stellar Evolution (항성 진화)



Sun + Star

Solar surface composition :
 $X=0.73, Y=0.25, Z=0.02$

Star = atmosphere + interior

Optical depth < 1

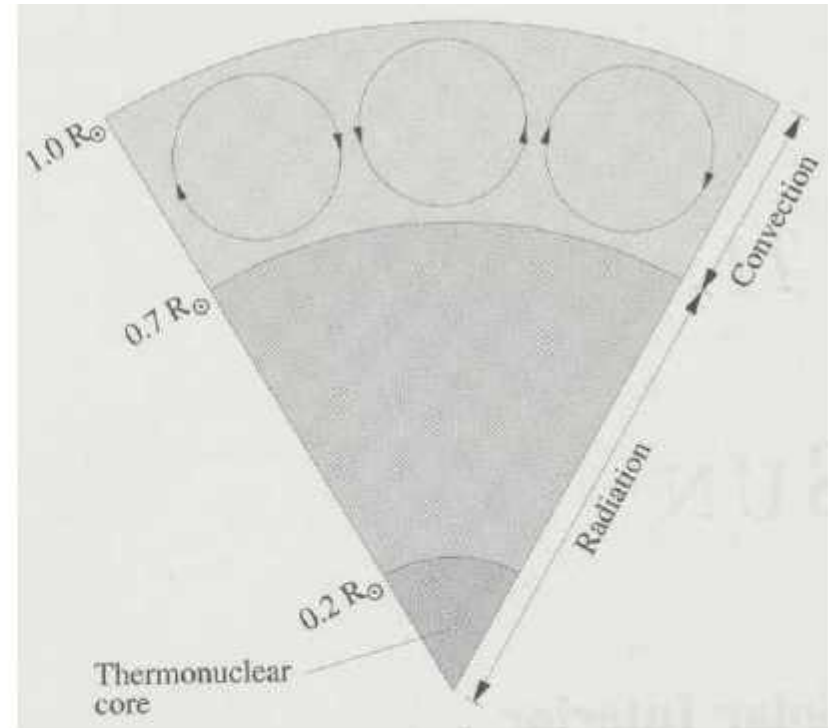
Optical depth > 1
 nuclear reaction

※ Optical depth, τ_λ : $d\tau_\lambda = -\kappa_\lambda \rho ds$

$\tau_\lambda \gg 1$: optically thick

$\tau_\lambda \ll 1$: optically thin

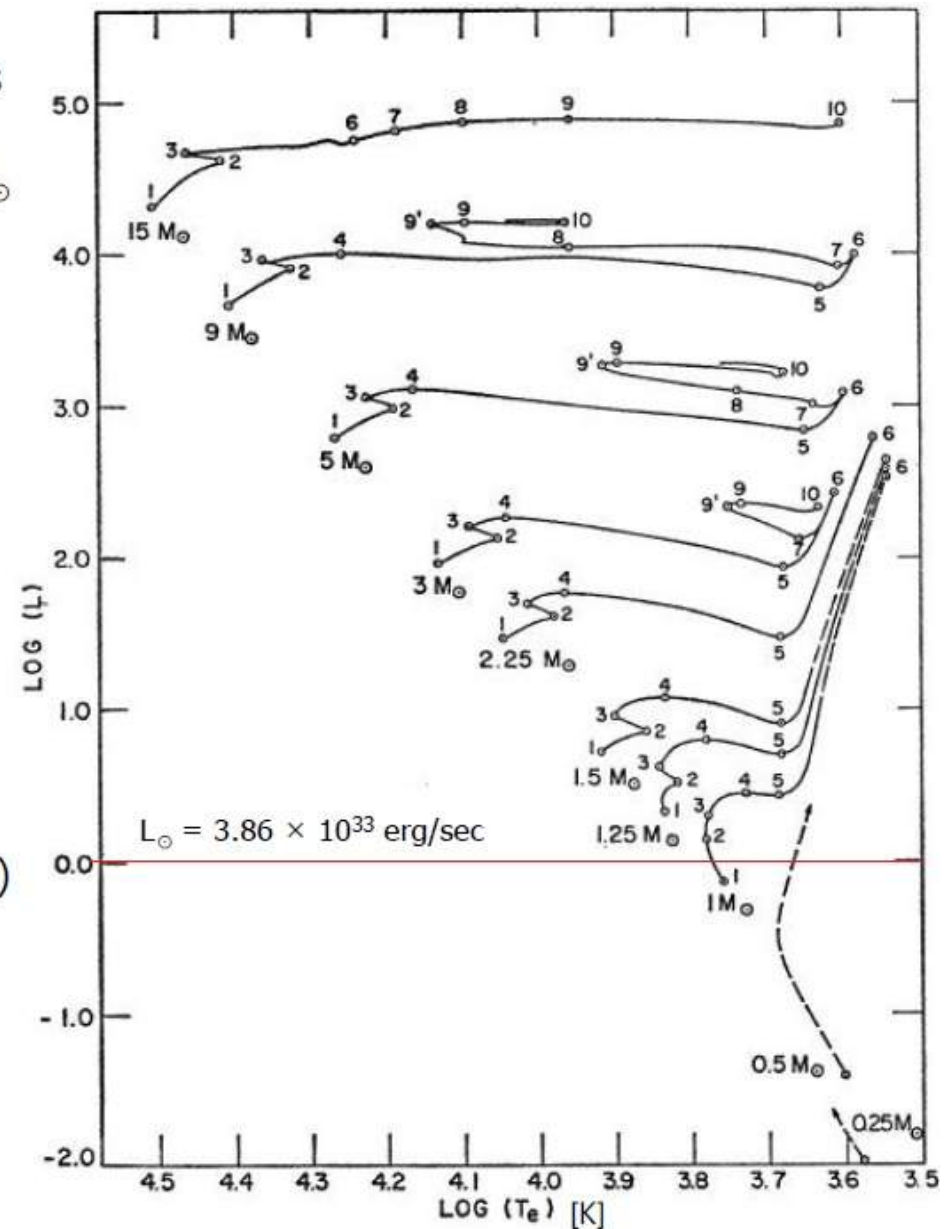
※ κ_λ : absorption coefficient (opacity)



Post-MS Stellar Evolution

Hertzsprung-Russell Diagram of Metal-rich stars
($X=0.708$, $Y=0.272$, $Z=0.020$)
 $M = 15, 9, 5, 3, 2.25, 1.5, 1.25, 1, 0.5, 0.25 M_{\odot}$
Dashed lines : estimates

- Sun's L, R, T : increased steadily since it reached the zero-age main sequence (ZAMS) ~4.5 Gyr ago



Iben (1967, ARA&A, 5, 571) Fig 3

Solar Evolution

Sun's center, during its lifetime :

X : 0.71 → 0.34

Y : 0.27 → 0.64

changing the composition and structure

The change in the Sun's **central composition**
→ direct influence on observable L, T_{eff} and R

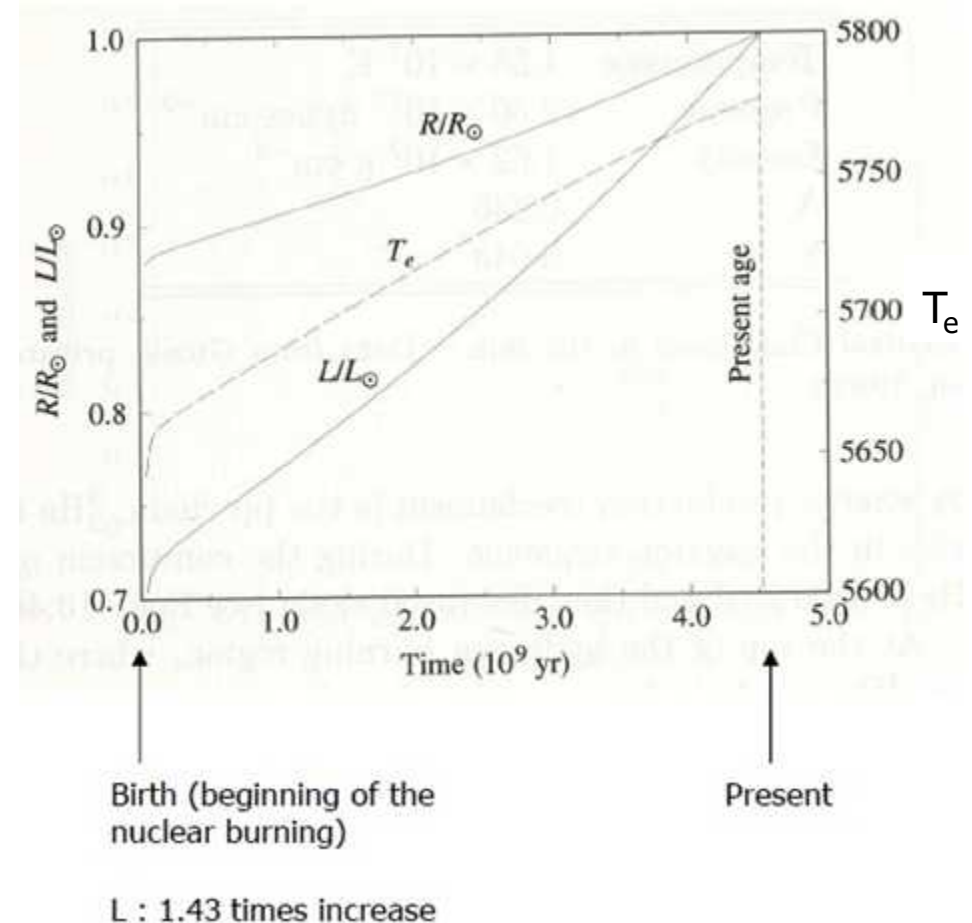
L increased by 40%

R increased by > 10%

※ Physical parameters of the Solar center
(standard solar model of Joyce Guzik)

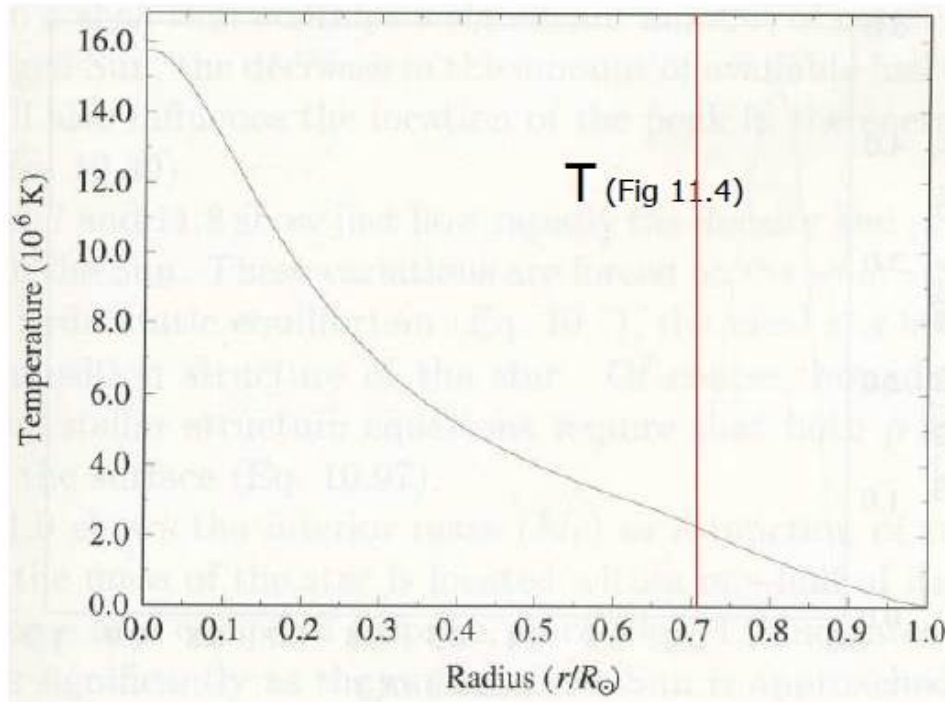
Central conditions in the Sun

T_C	(1.56~) 1.58×10^7 K
P_C	2.50×10^{17} dyne/cm ²
ρ_C	162 (150-160) g/cm ³
X_C	0.336
Y_C	0.643

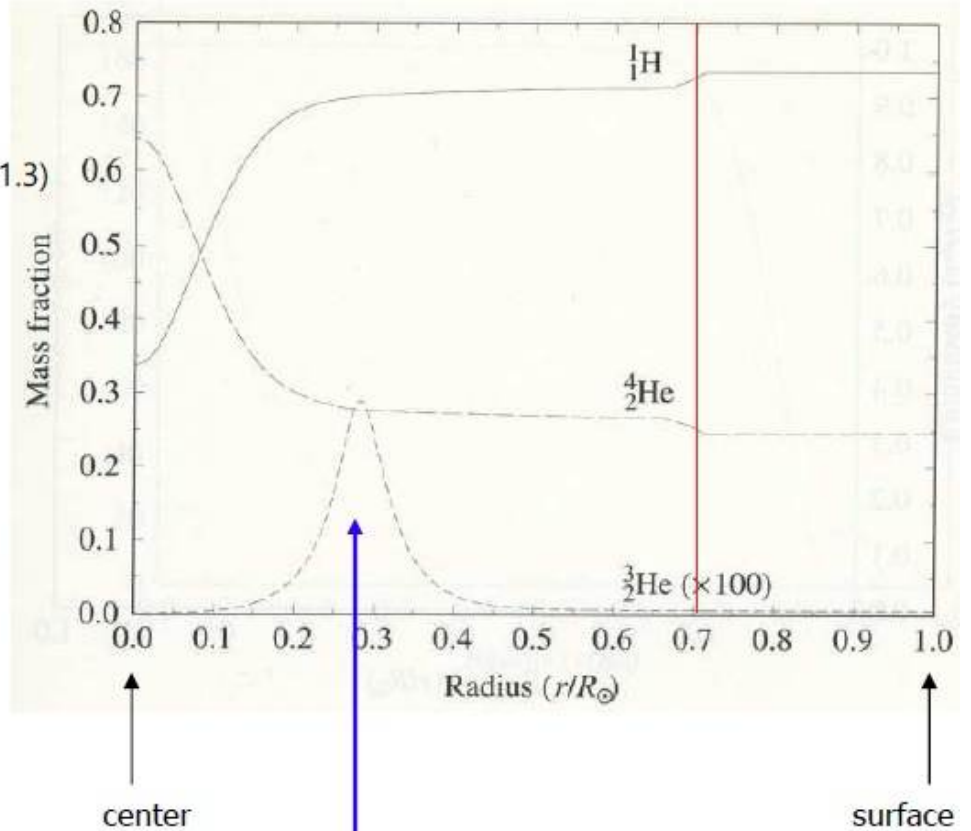


Solar composition structure

Solar Temp structure



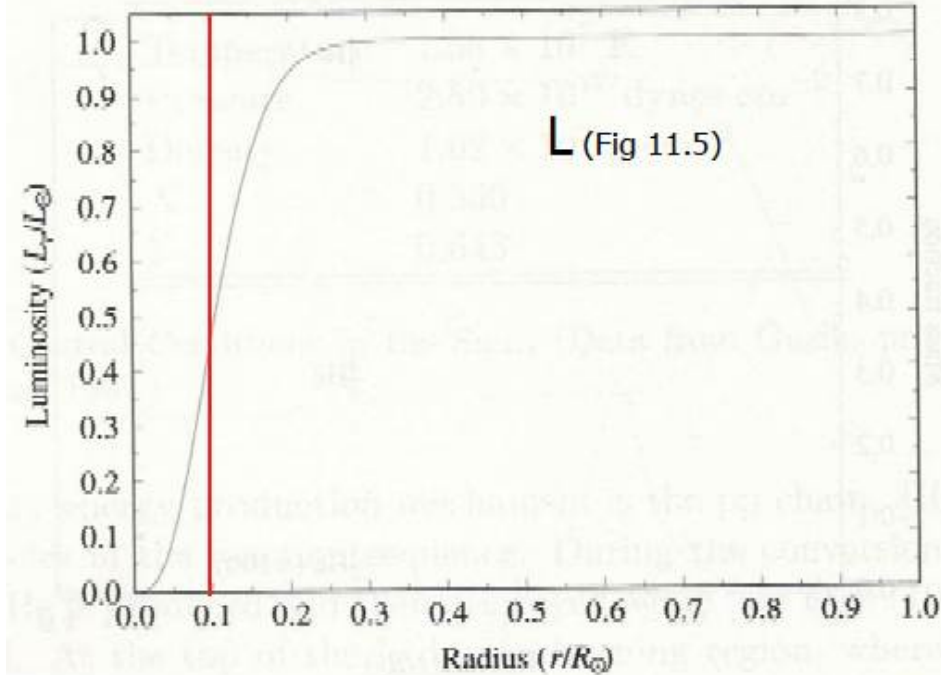
(Fig 11.3)



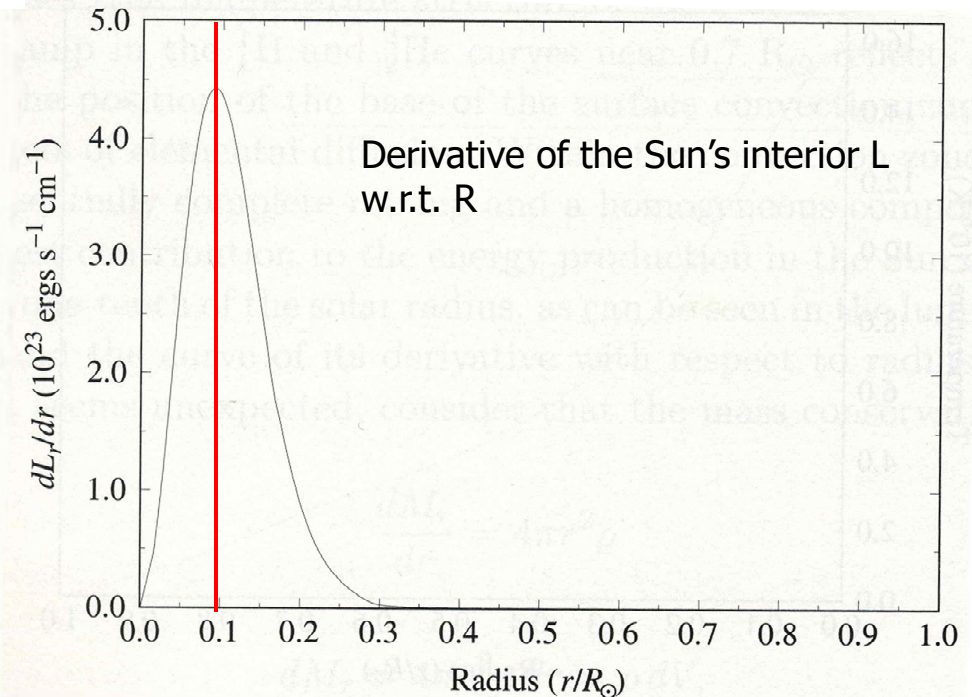
Produced more easily
than destroyed

※ ^3_2He : intermediate species in the pp chain
reaction sequence

Interior Lum of the Sun



Location of the greatest contribution to the E output



Though amount of E liberated per gram of material (ϵ) decreases steadily from $R=0$ outward
 → Largest contribution to the total L – in a shell that contains a significant amount of mass

Post-MS Stellar Evolution

TABLE III STELLAR LIFETIMES (yr)^a

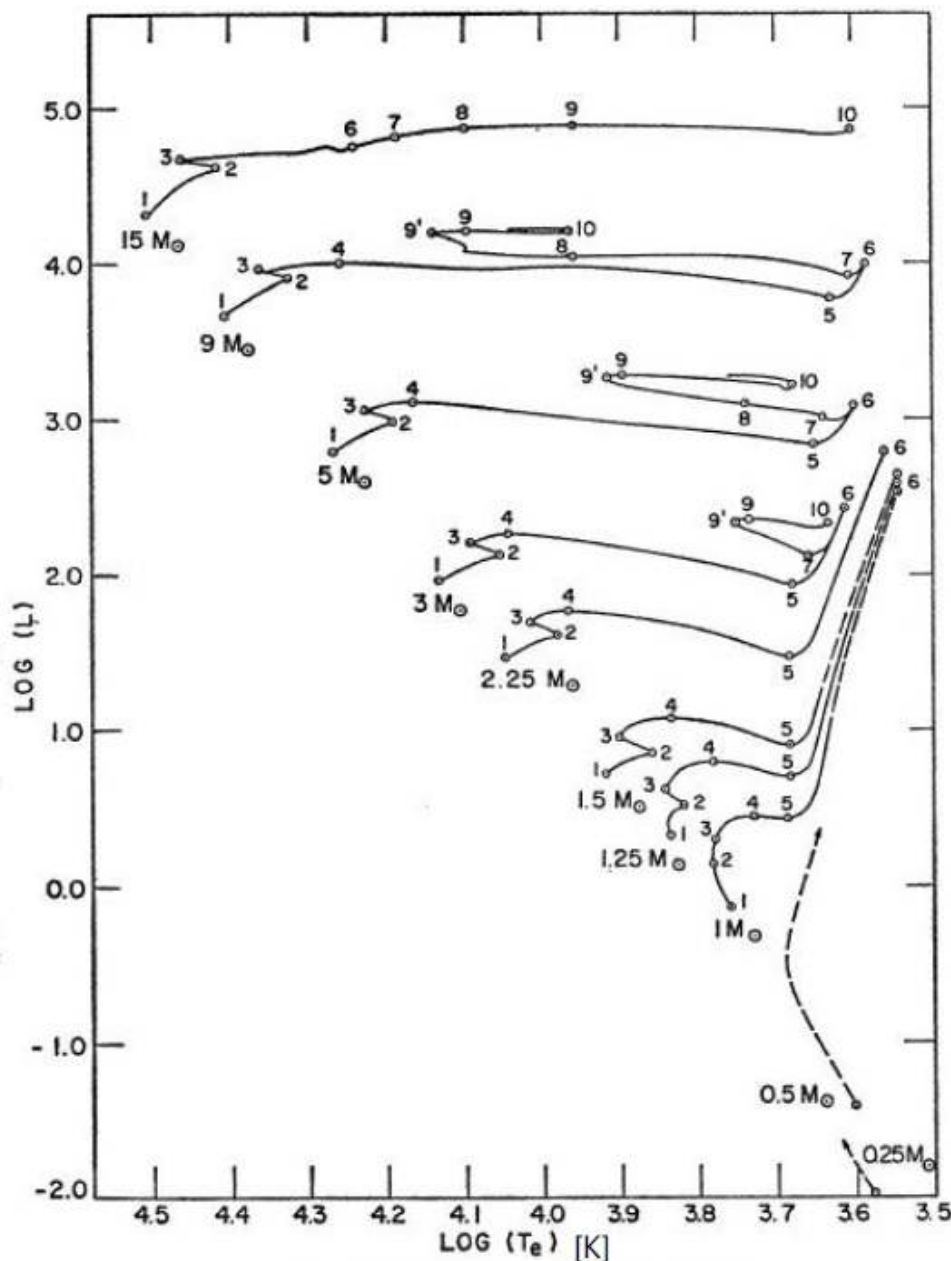
Interval (i-j)	(1-2)	(2-3)	(3-4)	(4-5)	(5-6)
Mass (M_{\odot})					
15	1.010 (7)	2.270 (5)	7.55 (4)		
9	2.144 (7)	6.053 (5)	9.113 (4)	1.477 (5)	6.552 (4)
5	6.547 (7)	2.173 (6)	1.372 (6)	7.532 (5)	4.857 (5)
3	2.212 (8)	1.042 (7)	1.033 (7)	4.505 (6)	4.238 (6)
2.25	4.802 (8)	1.647 (7)	3.696 (7)	1.310 (7)	3.829 (7)
1.5	1.553 (9)	8.10 (7)	3.490 (8)	1.049 (8)	≥2 (8)
1.25	2.803 (9)	1.824 (8)	1.045 (9)	1.463 (8)	≥4 (8)
1.0	7 (9)	2 (9)	1.20 (9)	1.57 (8)	≥1 (9)

^a Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.

TABLE IV STELLAR LIFETIMES (yr)^a

Interval (i-j)	(6-7)	(7-8)	(8-9)	(9-10)
Mass (M_{\odot})				
15	7.17 (5)	6.20 (5)	1.9 (5)	3.5 (4)
9	4.90 (5)	9.50 (4)	3.28 (6)	1.55 (5)
5	6.05 (6)	1.02 (6)	9.00 (6)	9.30 (5)
3	2.51 (7)	4.08 (7)	6.00 (6)	

^a Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.



Iben (1967, ARA&A, 5, 571) Fig 3

Post-MS Stellar Evolution

TABLE III STELLAR LIFETIMES (yr)^a

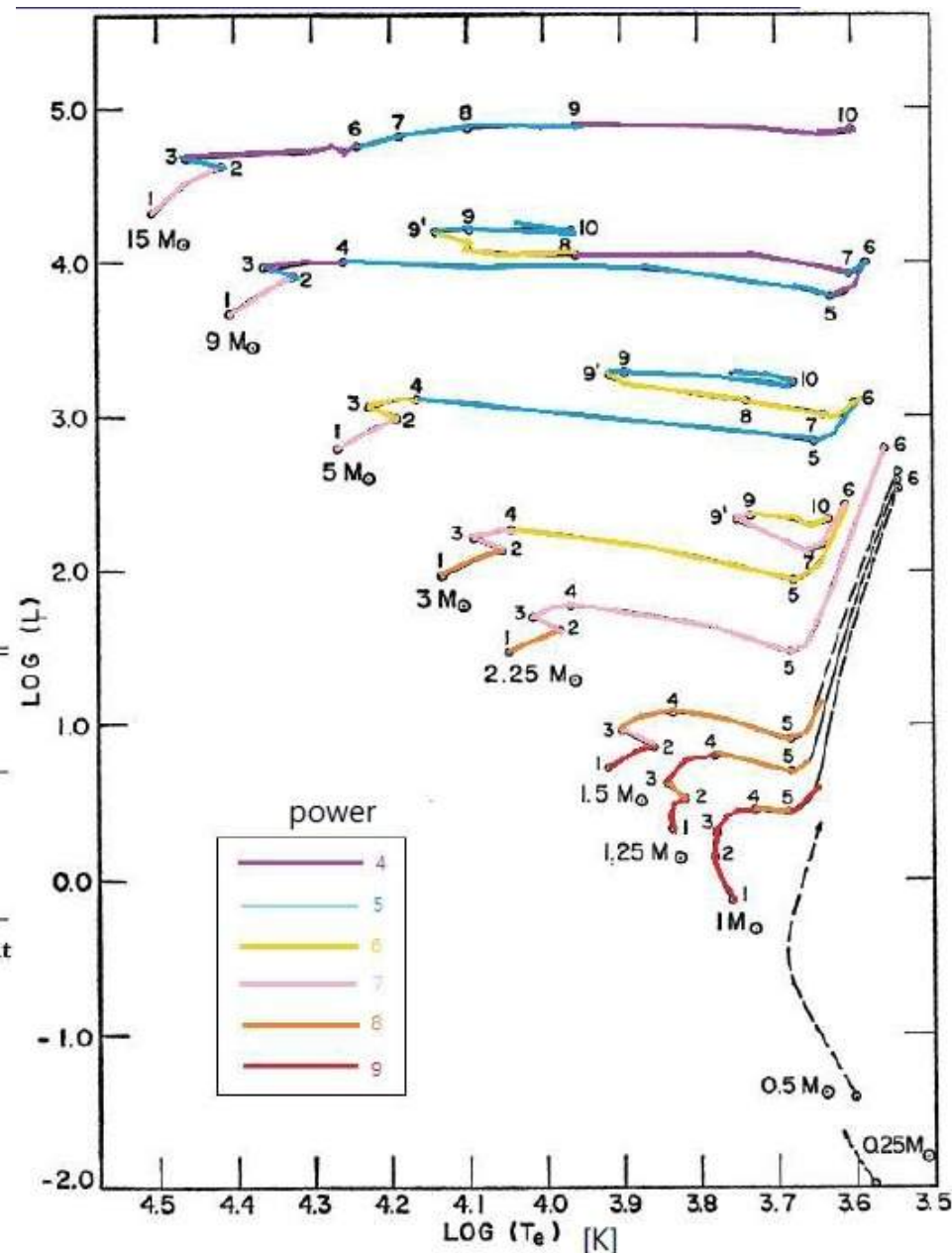
Interval (i-j)	(1-2)	(2-3)	(3-4)	(4-5)	(5-6)
Mass (M_{\odot})					
15	1.010 (7)	2.270 (5)		7.55 (4)	
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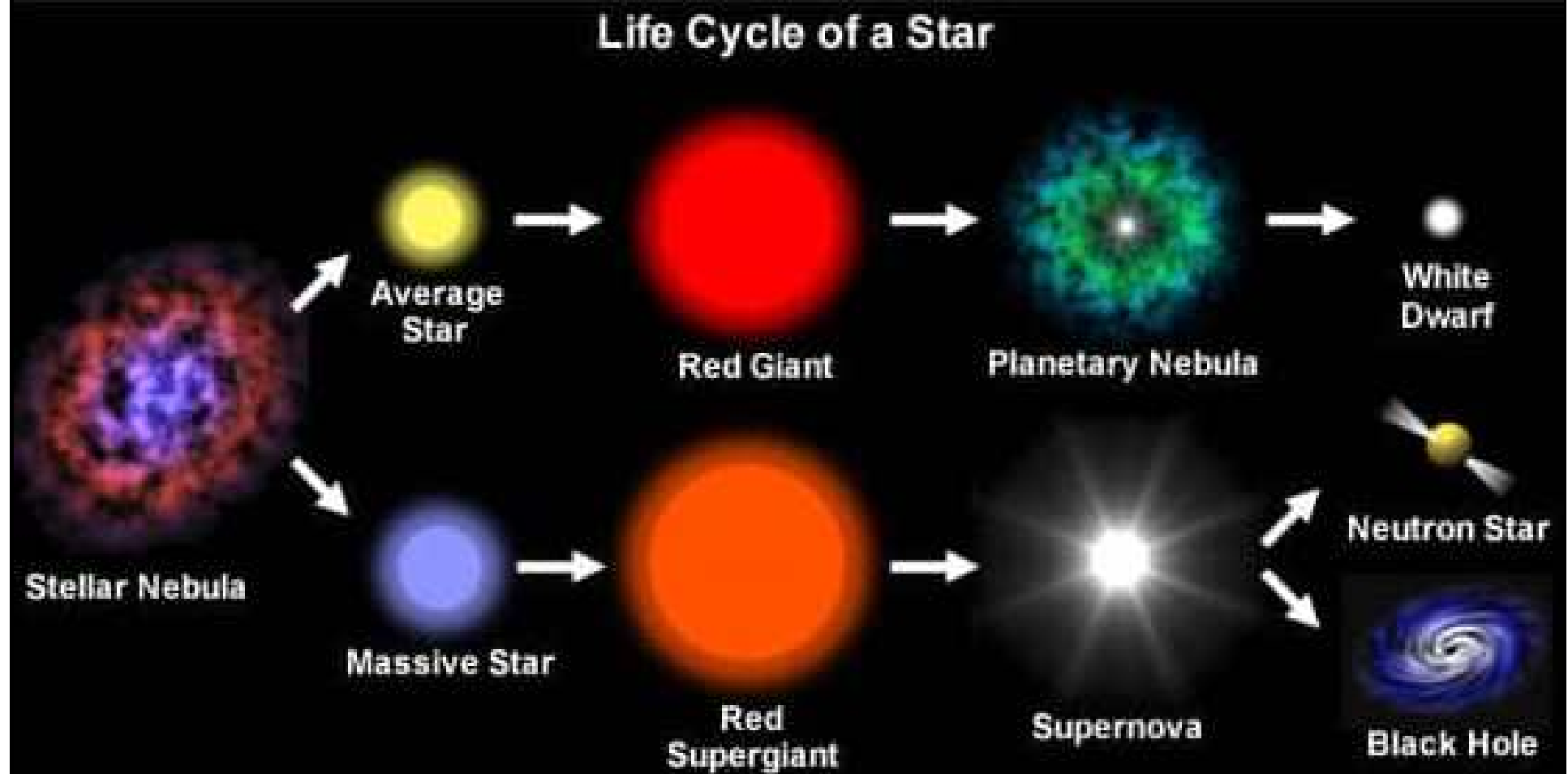
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^a Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.



2. The Evolution of Stars (별의 진화)

2-3 Post-Main-Sequence Evolution (주계열 이후 진화)

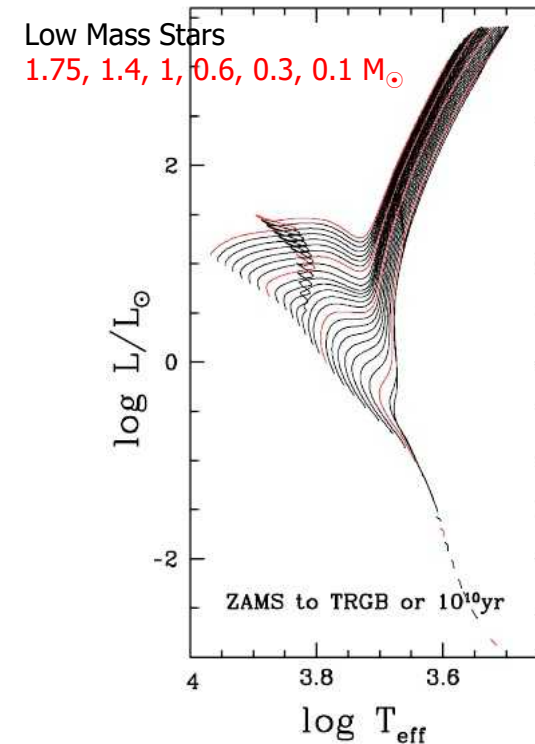
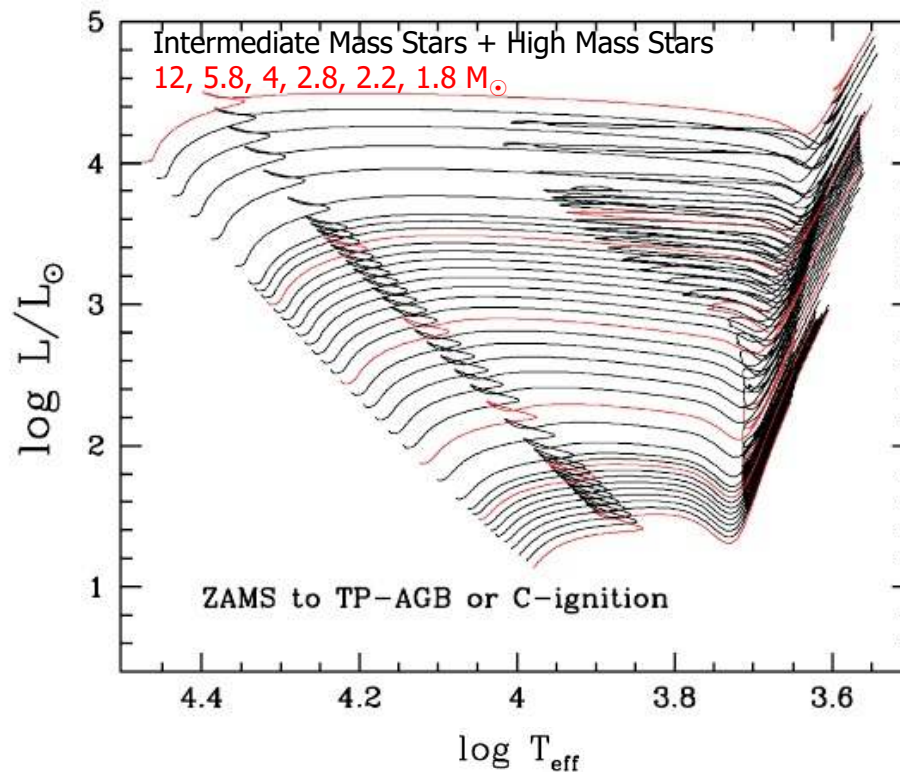


Post-MS Stellar Evolution

Stellar evolution isochrones

- Padova (Bressan+12 MN 427 127)
- Geneva
- VandenBerg (83 ApJS 51 29)
- Yonsei-Yale (Y^2) (Demarque+04 ApJS 155 667)
- Dartmouth (Dotter+07 ApJ 666 403)
- Modules for Experiments in Stellar Astrophysics (MESA) (Paxton+11 ApJS 192 3)
- MESA Isochrones and Stellar Tracks (MIST) (Dotter 16 ApJS 222 8)
- Yunnan-III (Zhang+13 MN 428 3390)

Bressan et al. 2012 MNRAS 427 127 (PARSEC: stellar tracks and isochrones with the PADova and TRIeste Stellar Evolution Code)



Post-MS Stellar Evolution

D. Schaerer, C. Charbonnel, G. Meynet, A. Maeder and G. Schaller
Geneva Observatory, CH-1290 Sauverny, Switzerland
1993 *Astron. Astrophys. Suppl. Ser.* **102**, 339

Grids of stellar models.

IV. From 0.8 to 120 M_{\odot} at $Z = 0.040$

HRD of massive stars (15 – 120 M_{\odot}) with $Z=0.040$

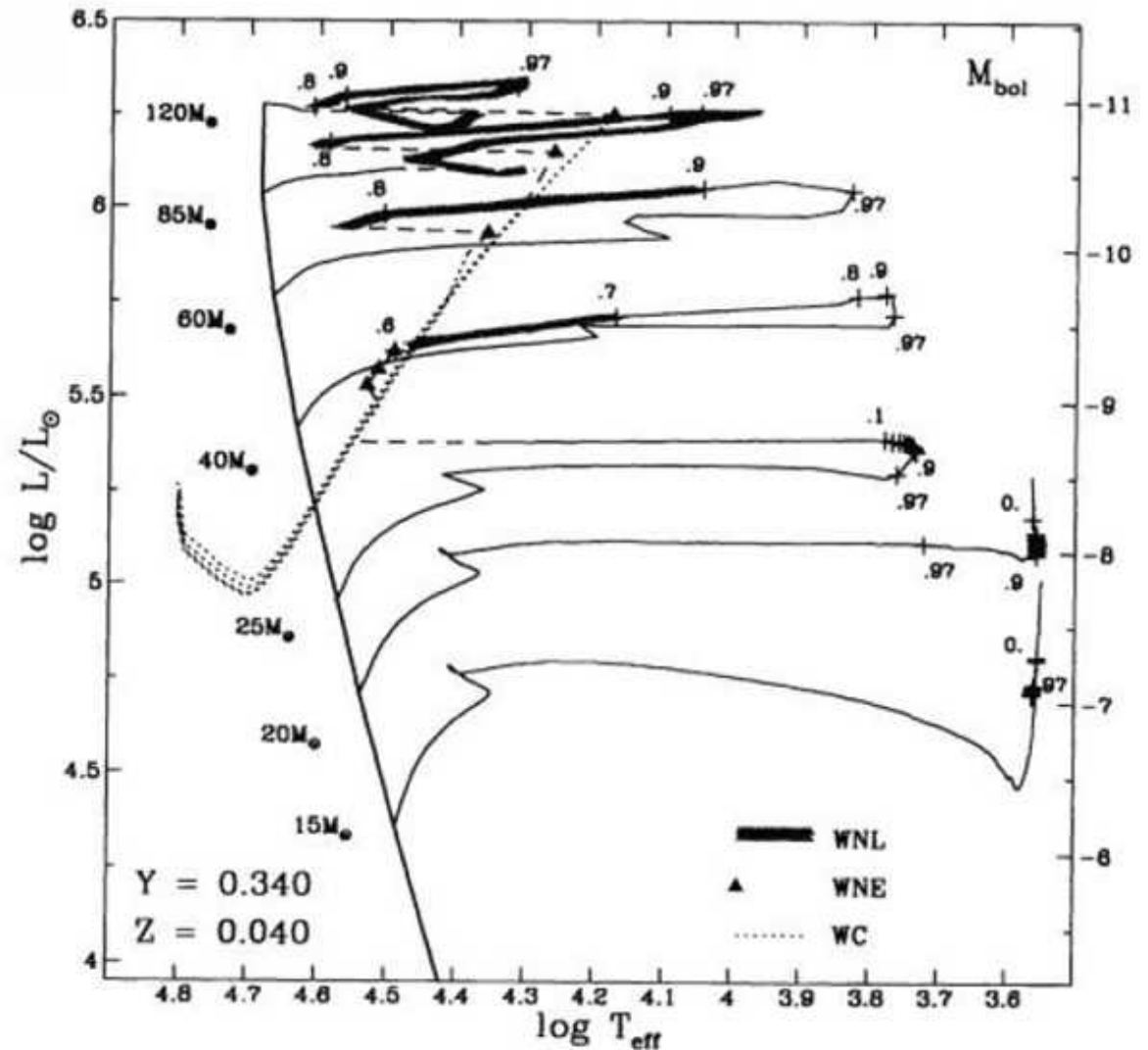
Y_c (central He content) : 0.97, 0.90, 0.80, 0.70, 0.60, ---, 0.10, 0

Wolf-Rayet stars

- Hot : $T_{\text{eff}} = 30,000 - 200,000$ K
- Broad emission lines of He I, He II, C III, C IV, N III, N V
- Very high surface enhancement of heavy elements (He etc.), depletion of hydrogen
- Strong stellar winds

N rich : WN

C rich : WC



Schaerer et al (1993, A&AS, 102, 339) – Fig 3

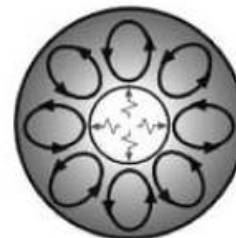
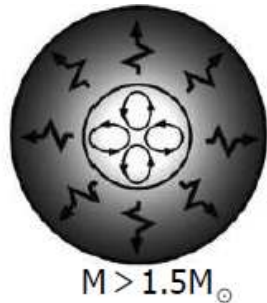
Characteristics of MS Stars

$M > 1.5 M_{\odot}$	$M < 1.5 M_{\odot}$
$T_c > 2 \times 10^7 \text{ K}$	$T_c < 2 \times 10^7 \text{ K}$
CNO cycle	PP chain
Energy production rate : $\epsilon_{\text{CNO}} \propto T^{19.9} \rightarrow$ Production of most E near the center	$\epsilon_{\text{CNO}} \propto T^4 \rightarrow$ E source is not concentrated to the center
core : convective	core : radiative
envelope : radiation	envelope : H-convection

The more massive,
the larger convective core.

← mass

As mass decreases,
H-convection zone deepens.



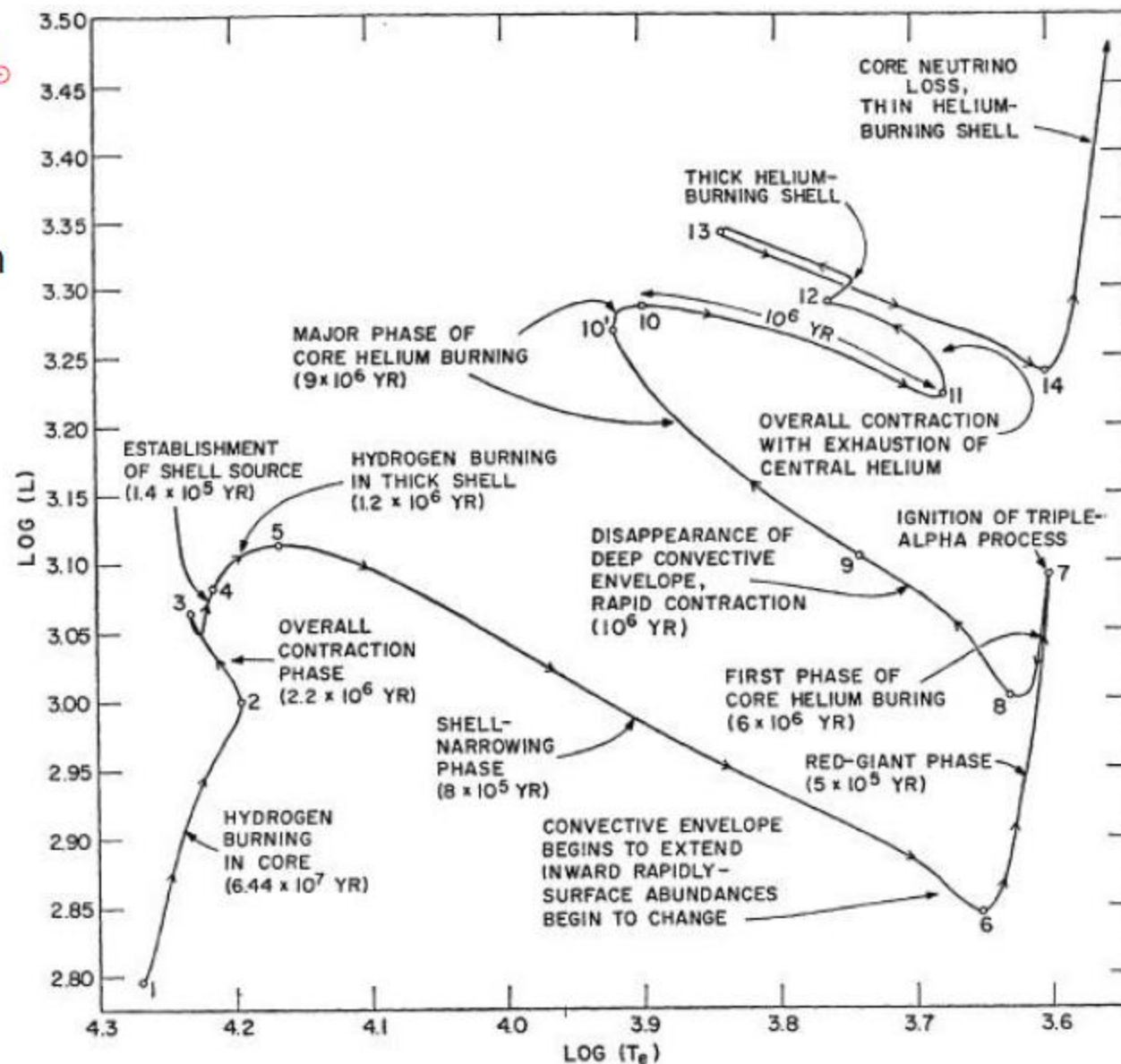
https://ase.tufts.edu/cosmos/view_picture.asp?id=1409

Dominant energy transport mode :

- Low temperature gradient, low opacity \rightarrow radiation
- Steep temperature gradient \rightarrow convection

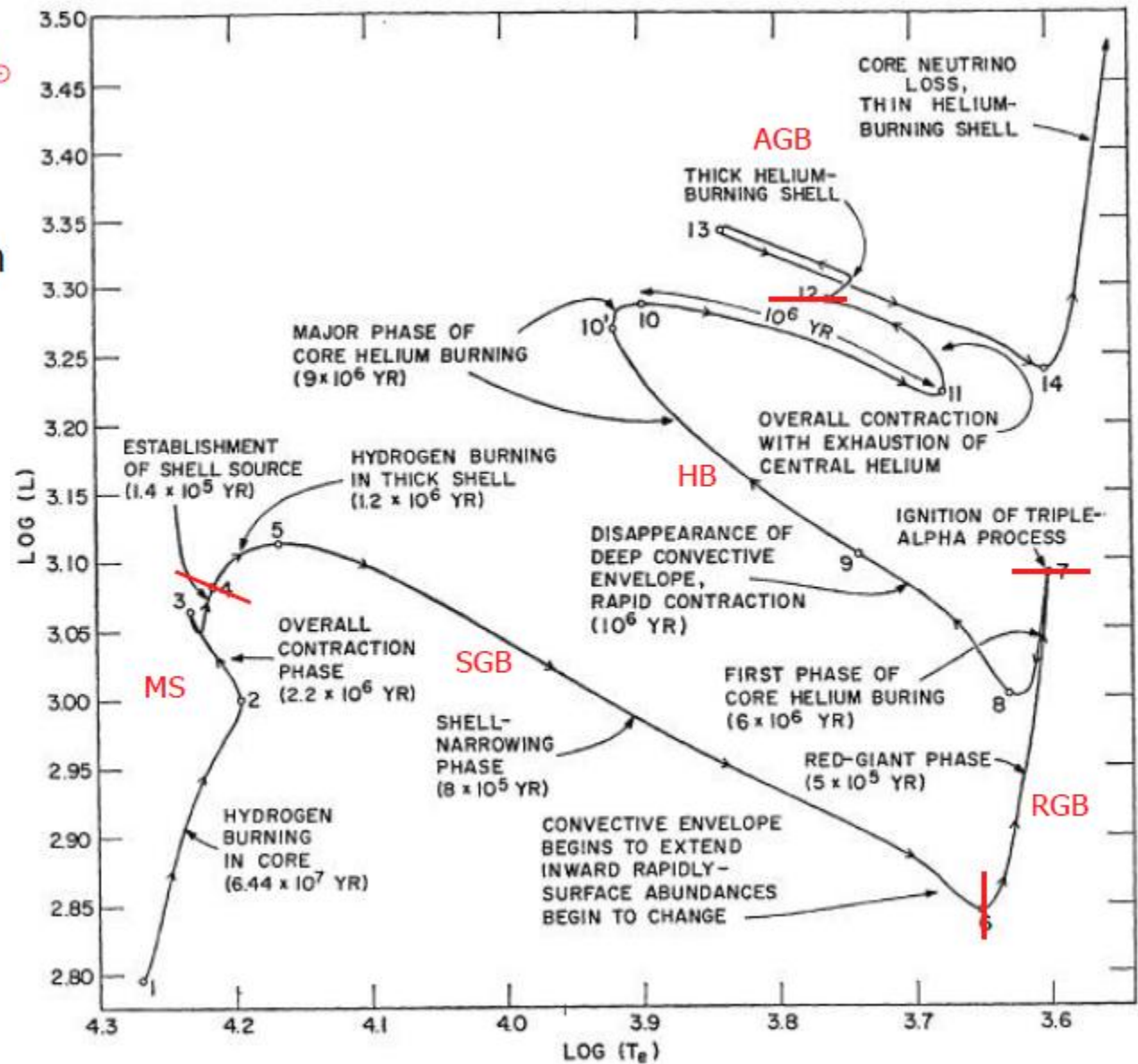
Post-MS Stellar Evolution

- Evolutionary path of a $5 M_{\odot}$ metal-rich star in the HRD
- From ZAMS to the asymptotic giant branch (AGB)

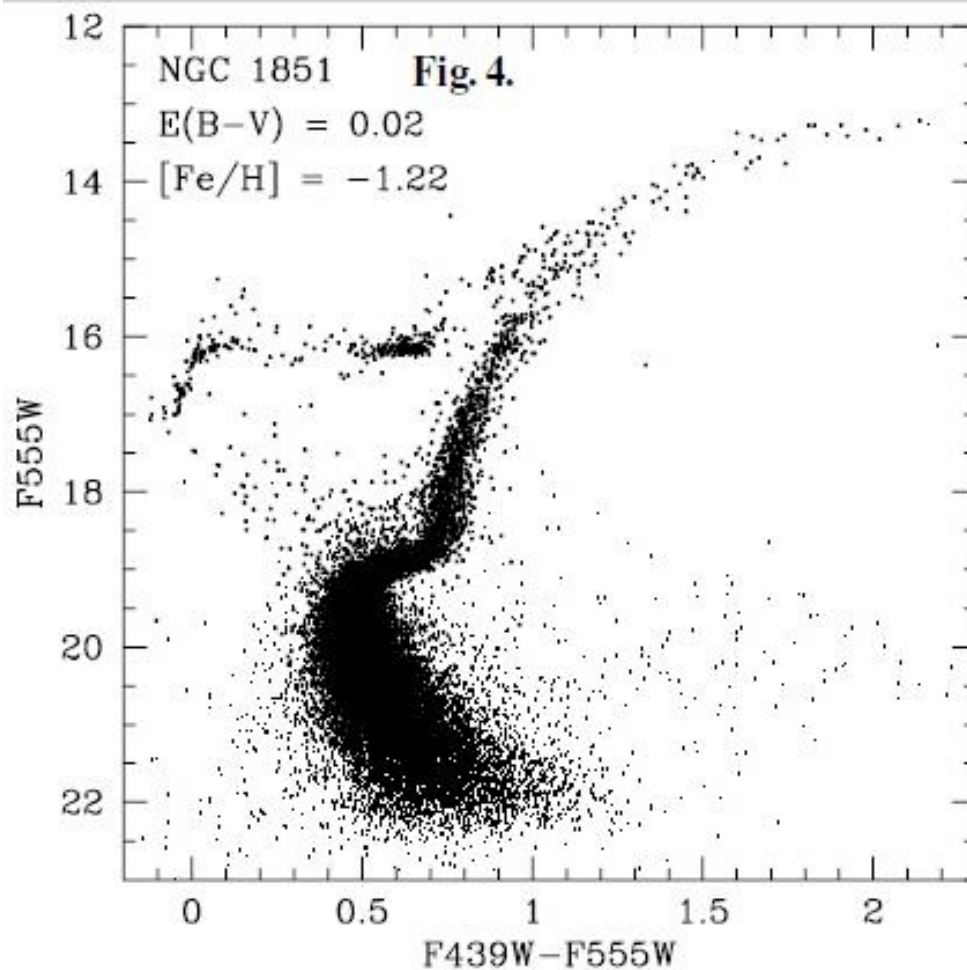


Post-MS Stellar Evolution

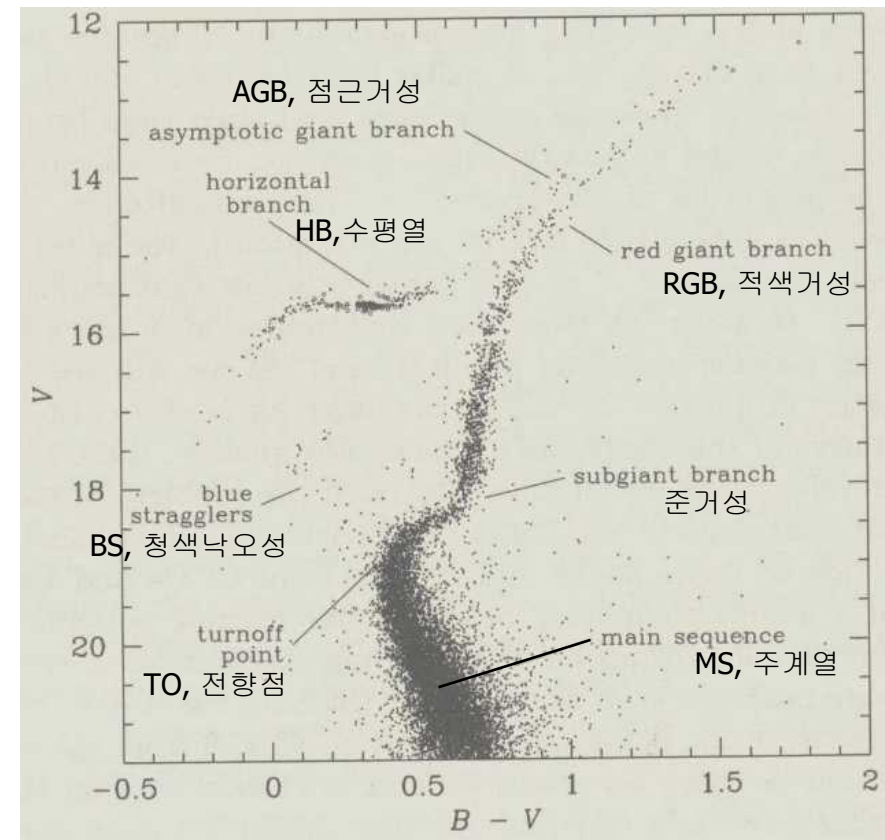
- Evolutionary path of a $5 M_{\odot}$ metal-rich star in the HRD
- From ZAMS to the asymptotic giant branch (AGB)



Color-Magnitude Diagrams for globular clusters (GCs)



Piotto et al. (2002, A&A, 391, 945)

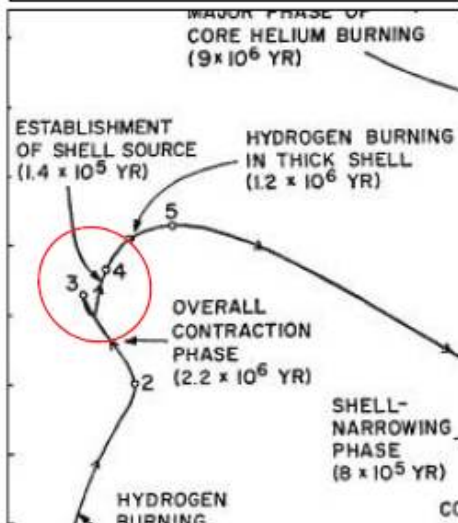
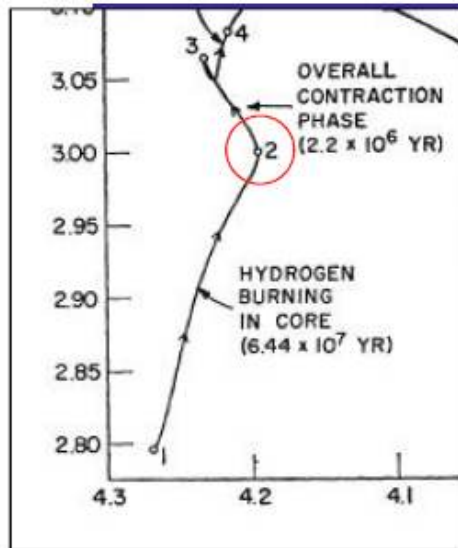


GC M3 (NGC 5272) $[Fe/H] = -1.34$
 (variables=open circles)

Galactic Astronomy (J. Binney & M. Merrifield, 1998) p. 334

Forbes & Bridges 10 MN 404 1203 (Accreted vs. in situ MW GCs)

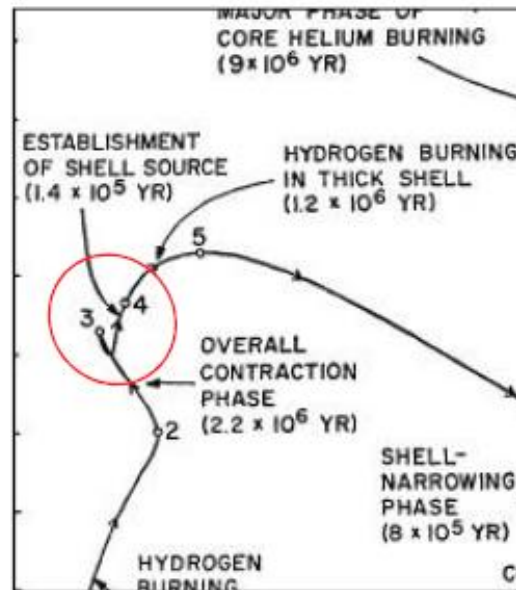
5 M_☉ star - structure



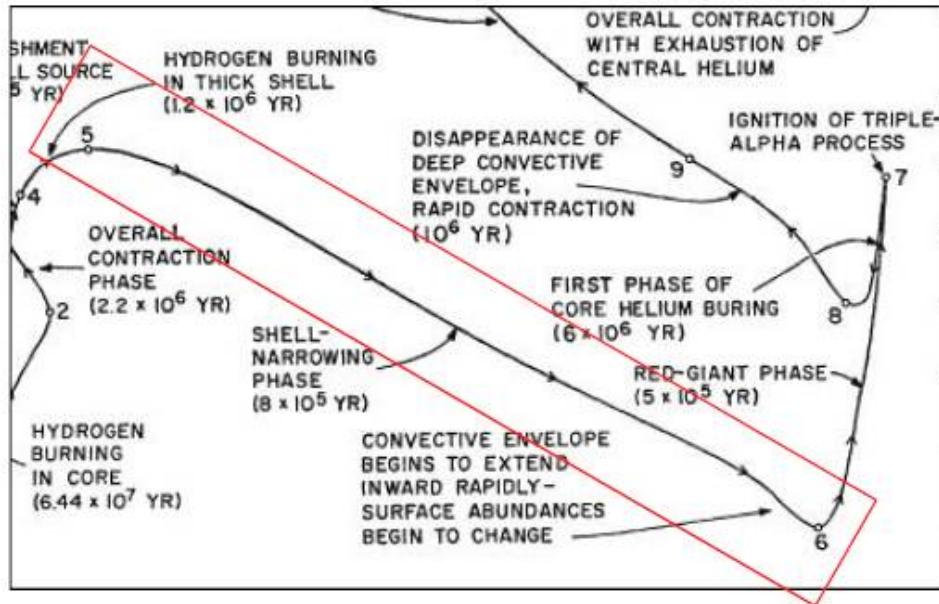
- At point 2 : near depletion of H fuel in the core
- During 2 → 3 : overall contraction (Core H mass fraction X : reduced to 0.01)
- During 3 → 4 : establishment of shell source - H burning begins in a thick shell
- Overlying envelope absorbs some or much of the E release by the shell → envelope slightly expands

Evolution beyond point 3

- Generated energy → goes into slow **expansion of the envelope**
- T_{eff} **decreases** slightly, evolutionary track bends to the **right**
- Redward locus = **subgiant branch**



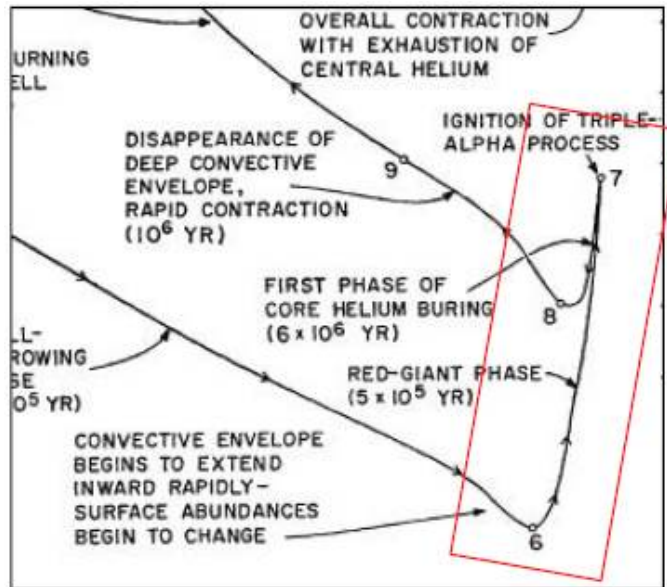
Sub Giant Branch (SGB) : $5 M_{\odot}$ star



- During point 5 \rightarrow 6 :
 - **Envelope expands** (absorbing much of the shell's E, before it reaches the surface)
 - \rightarrow L decreases, effective T decreases, photospheric opacity increases (H^- ion)
 - \rightarrow **convection zone** begins to develop near the surface

- Base of the **convection zone** \rightarrow **extends down** into regions where the **chemical composition has been modified** by nuclear processes
- Surface convection zone encounters these chemically modified regions
 - \rightarrow Processed material become **mixed**
 - \rightarrow **Photosphere composition** change ($Li \downarrow$, ${}^3He \uparrow$)
 - "First dredge-up"** begins at point 6

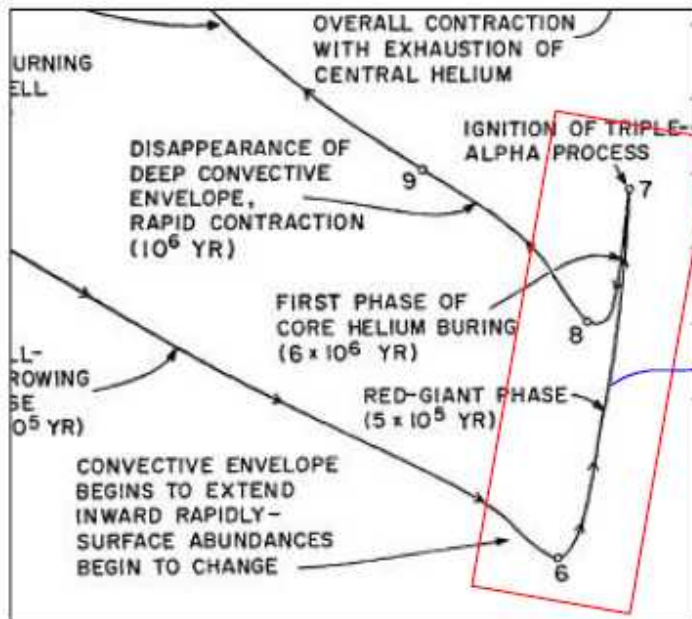
5 M_⊙ star at the RGB



- During 6 → 7
 - : core continues to contract – **degenerate He**
 - (narrowing) H-b **shell E-production rate** ↑
 - **L↑, R↑**
 - vertical evolution, “**red giant branch (RGB)**”

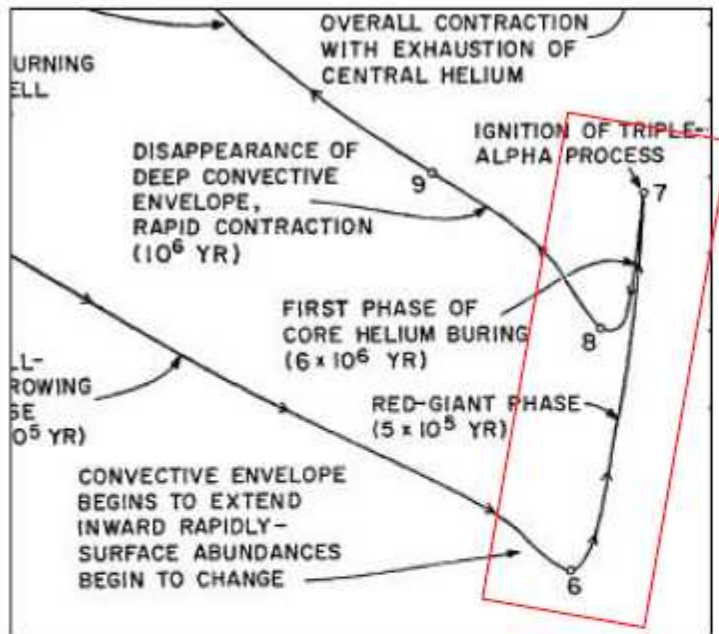
- At point 7 :
 - $T_c = 1.3 \times 10^8$ K
 - $\rho_c = 7700$ g/cm³
 - High central T and density → **quantum-mechanical tunneling** through the Coulomb barrier (acting between ${}^4_2\text{He}$ nuclei) becomes effective
 - **triple- α process** begins
- **Slow ignition** of He-burning phase!
- New source of E → core expands
 - Shell E-generation rate decreases
 - **L↓**
 - and envelope contracts, $T_{\text{eff}} \uparrow$

✧ For low mass stars of $M < 2 M_{\odot}$



- As He-core continues to collapse
→ Core becomes strongly electron-degenerate
- T, ρ become high enough
to initiate the triple- α process (10^8 K, 10^4 g/cm³)
→ Explosive E release!
(core) helium flash
- Luminosity $\sim 10^{11} L_{\odot}$
→ For only a few seconds!
(most of the E never reaches the surface)
→ E "lifts" the degeneracy and
absorbed by the overlying layers of the envelope (possibly
cause some mass loss)

✧ For low mass stars of $M < 2 M_{\odot}$



- **(core) helium flash**

: Nearly constant mass – function of metallicity

$\sim 1.6 M_{\odot}$ for population I stars

$\sim 1 M_{\odot}$ for population II stars

- For pop II stars (ages 2-15 Gyr), if metallicity is same

→ **bolometric luminosity** is \sim constant
(varies only by ~ 0.1 mag)

→ TRGB (tip of the red giant branch)
: distance indicator for old, resolved galaxies

TRGB (tip of the red giant branch)

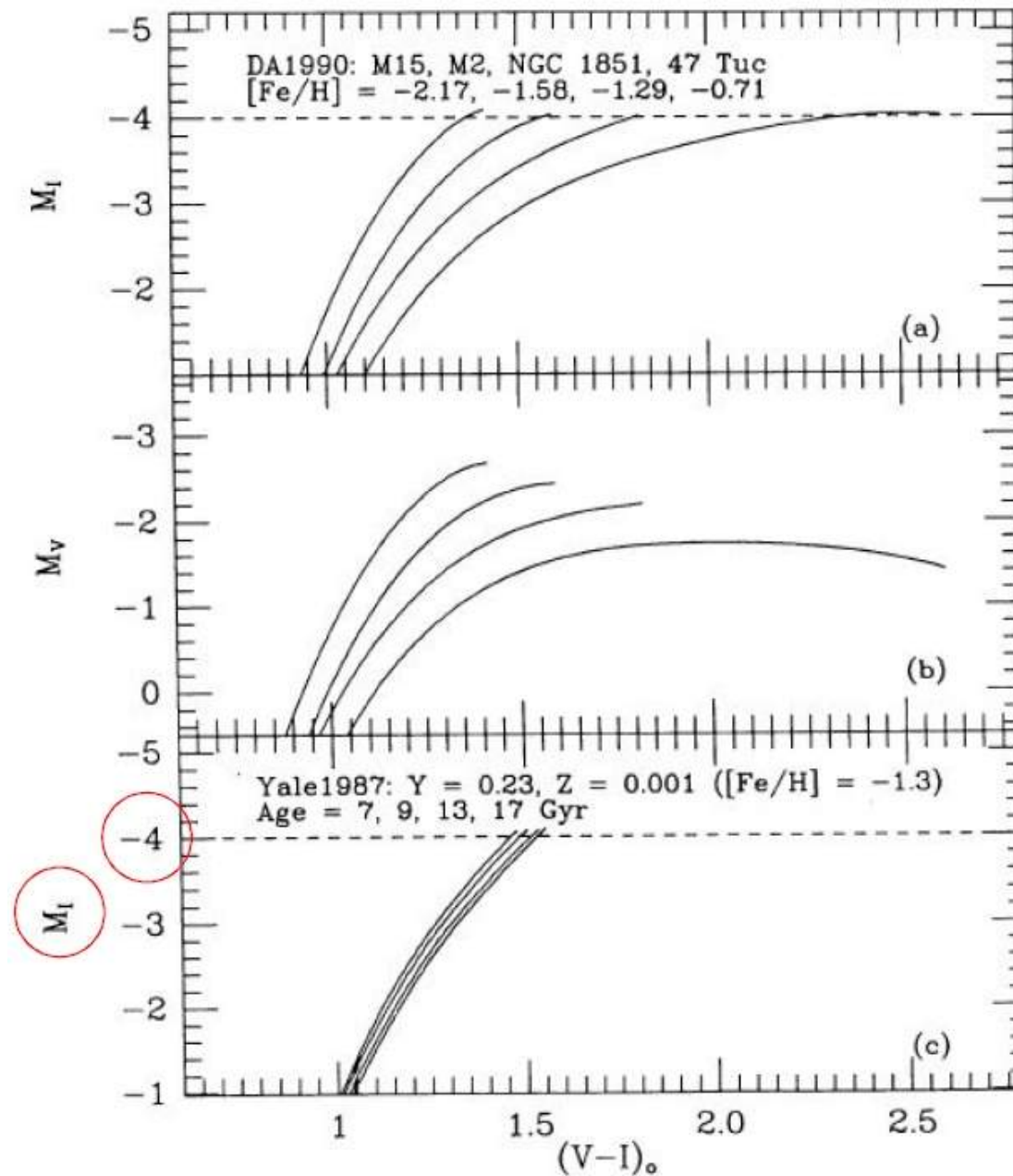


Fig. 1