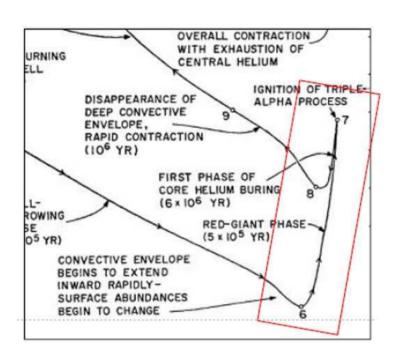


5 M $_{\odot}$ star evolution after ignition of the triple- α process

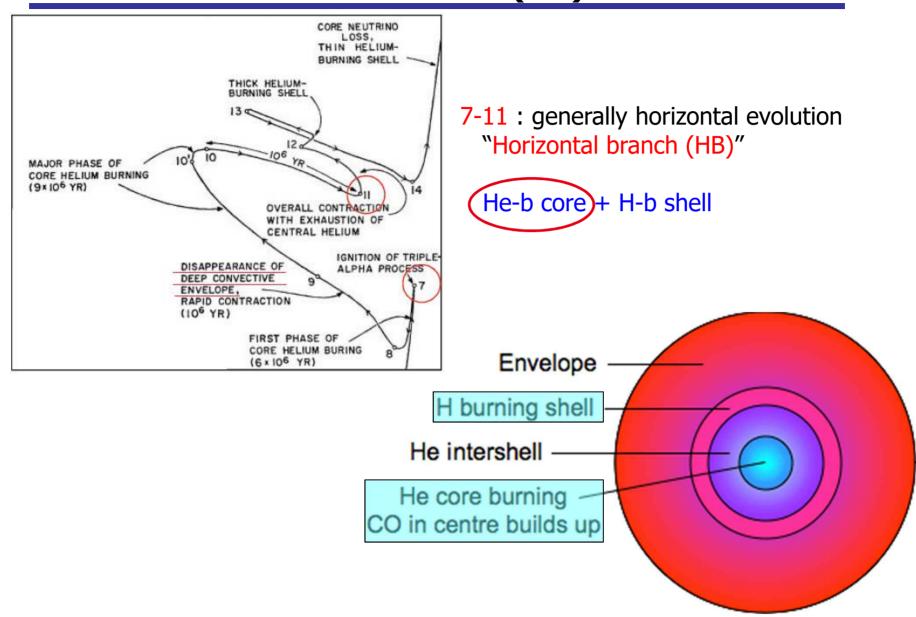


- At point 7 :
- $T_c = 1.3 \times 10^8 \text{ K}, \rho_c = 7700 \text{ g/cm}^3$
- High central T and ρ
 → triple-α process begins
- Strong T-dependence

$$\epsilon_{3\alpha} \simeq \epsilon'_{\circ,3\alpha} \rho^2 Y^3 f_{3\alpha} T_8^{41.0}$$

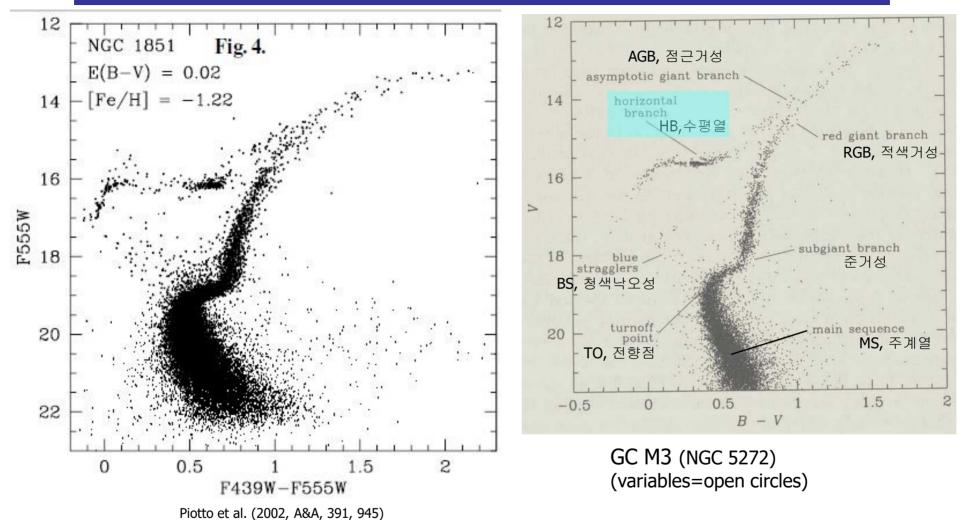
- (7→8)
- New E source in core \rightarrow core expands, cools \rightarrow shell E-output $\downarrow \rightarrow \downarrow \downarrow$
- Envelope contracts $\stackrel{\cdot}{\rightarrow}$ T_{eff} \uparrow
- (8→10)
- Since envelope contraction → H-b shell compresses → shell E-output↑ → L↑

Horizontal Branch (HB) Stars



https://astronomy.swin.edu.au/cosmos/H/Horizontal+Branch+stars

Color-Magnitude Diagrams for globular clusters (GCs)



Pulsating Variable Stars

HB stars in the instability strip (IS) = RR Lyrae stars

- →Instabilities in outer envelope
- → Periodic pulsations
- → Variations in L, T, R, surface radial vel.

Instability strip

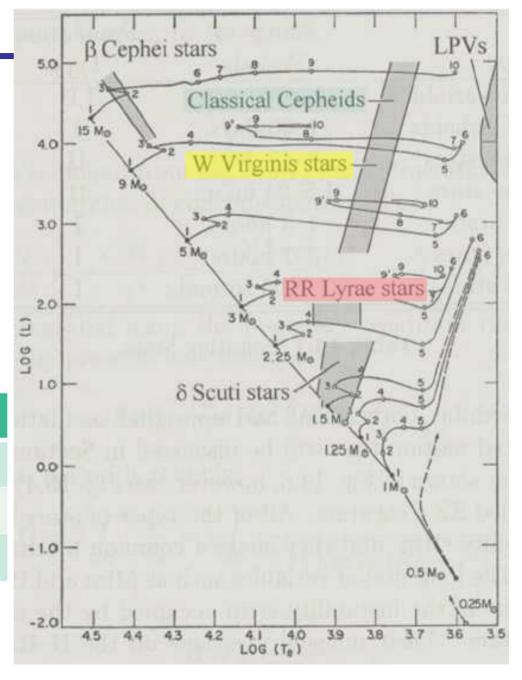
: narrow (~600 - 1000K wide)

Stars evolve horizontally along the IS

→Enters : starts pulsating →Leaves : cease pulsating

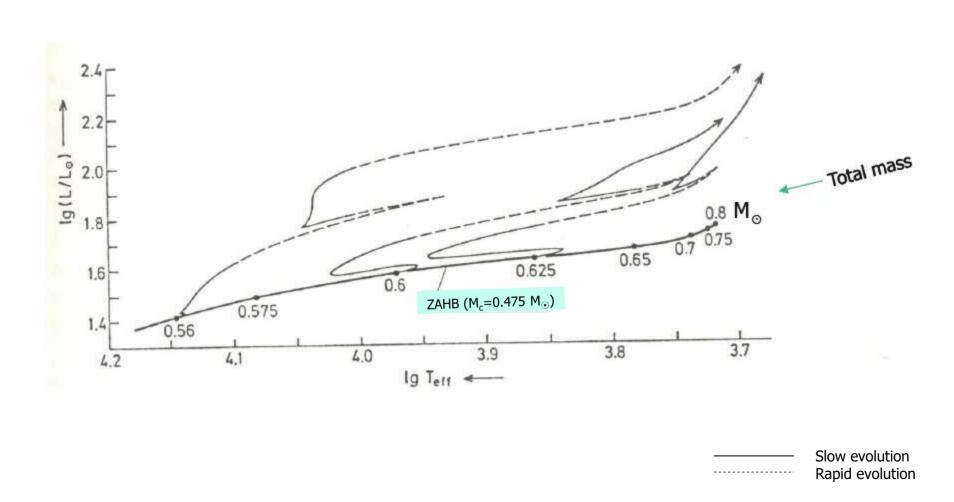
Туре	Periods	Population	Comments
Classical Cepheids	1-50 days	Ι	Radial Pulsation
W Virginis stars (Pop II Cep)	2-45 days	II	Radial Pulsation
RR Lyrae stars	1.5 – 24 hours	II	Radial Pulsation

These stars are distance indicators!

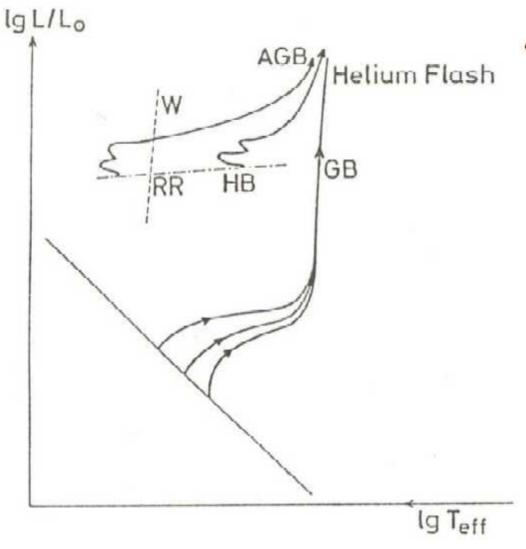


Post-HB Evolution – in HR diagram

Zero-age HB (ZAHB) and evolution afterwards (He-core $M_c = 0.475 M_{\odot}$, H-rich envelope with X=0.699, Y=0.3)



Post-HB Evolution – in HR diagram



 Evolution of low-mass stars, with three different masses

(RR = RR Lyrae stars)

(W = W Virginis stars)

RR Lyrae stars

- Periodic variable stars
- P = 1.5 to 24 h (\sim 12 h), Peak M_V \sim 0-1 mag, spectra A2 to F6
- Current mass ~ 0.8 M_☉ (original MS mass ~ 1 M_☉), old, relatively metal-poor
- In GCs and in low-metallicity systems (population II) But, some have high metallicity

$$M_V(RR) = +0.71 \pm 0.12$$
 at $\langle [Fe/H] \rangle = -1.61$ for the halo (162 stars)
 $M_V(RR) = +0.79 \pm 0.30$ at $\langle [Fe/H] \rangle = -0.76$ for the thick disk (51 stars)
Layden et al. (1996, AJ, 112, 2110)

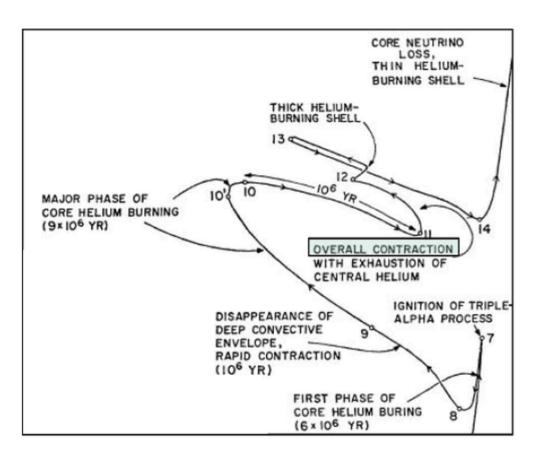
$$\langle M_V \rangle = (0.16 \pm 0.03)[\text{Fe/H}] + 1.02 \pm 0.03.$$
 (5.24)

$$\langle M_K \rangle = -(2.3 \pm 0.2) \log(P/1 \,\mathrm{d}) - 0.88 \pm 0.06$$
 (5.25)

$$\langle M_K \rangle = -(2.0 \pm 0.3) \log(P/1 \,\mathrm{d}) + (0.06 \pm 0.04) [\mathrm{Fe/H}] - 0.7 \pm 0.1$$
 (5.26)

Galactic Astronomy (James Binney and Michael Merrifield, 1998) p. 296

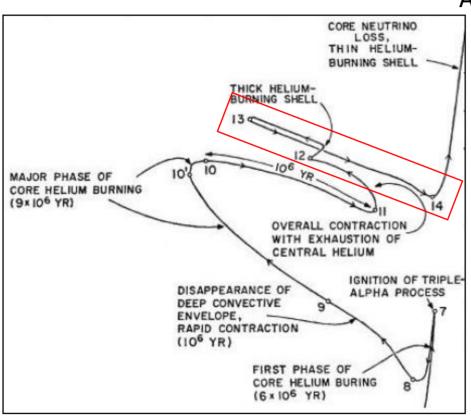
Post-HB, early-AGB (E-AGB)



- At point 11 : core He exhausted
 - → entire star contracts
 - → core T ↑
- During $11 \rightarrow 12$
 - : thick He-b shell develops

Asymptotic Giant Branch (AGB) stars

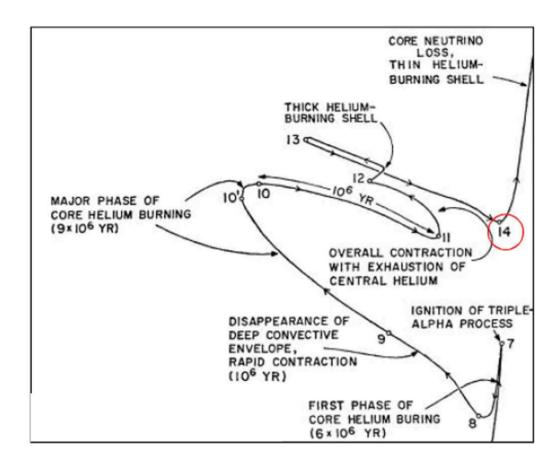
Early-AGB (E-AGB)



After point 12

- He-b shell produces more E
- Envelope expands + cools
- T_{eff} ↓ → convective envelope deepens again (extending downward to the chemical discontinuity between the H-rich outer layers and the He-rich region above the He-b shell)
- → Mixing = second dredge-up
- → Increases He-, N-content of the envelope

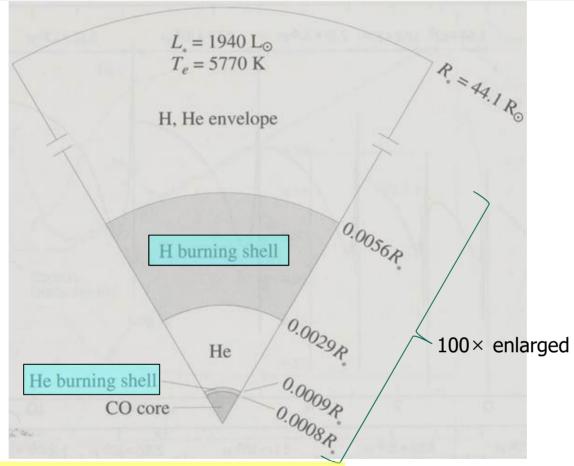
Early-AGB (E-AGB)



At point 14 : $T_c \sim 2 \times 10^8 \text{ K}$, $\rho_c \sim 10^6 \text{ g/cm}^3$ Interior structure \rightarrow

5 M_☉ star - AGB (asymptotic giant branch)

Inert CO core + Two shell sources (not to scale)



H shell burning: begins to turn-on and -off periodically

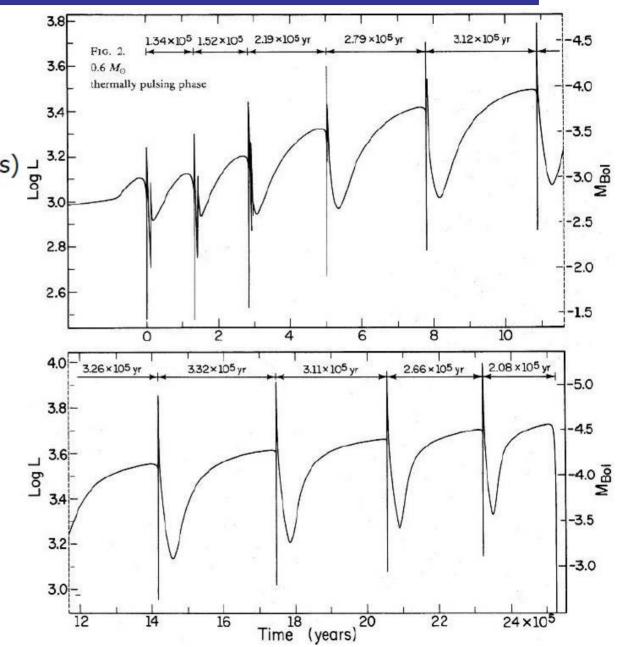
H-b shell dumps He onto the He-layer → He-layer mass↑, becomes slightly degenerate

- \rightarrow He-layer T \uparrow \rightarrow He-shell flash (~core He flash of low-mass stars, but much less energetic)
- \rightarrow Drives H-b shell outward \rightarrow cool, turn-off for a time

He-shell burning diminishes \rightarrow contract, $T \uparrow \rightarrow$ H-shell burning recovers \rightarrow repeats \rightarrow pulsing AGB

Thermally pulsing AGB (TPAGB)

- 0.6 M_o
- Pulse period = f(stellar mass) = from 10³ years (~5 M_o)
 to 10⁵ years (~0.6 M_o)
- Pulse amplitude grows w/successive event



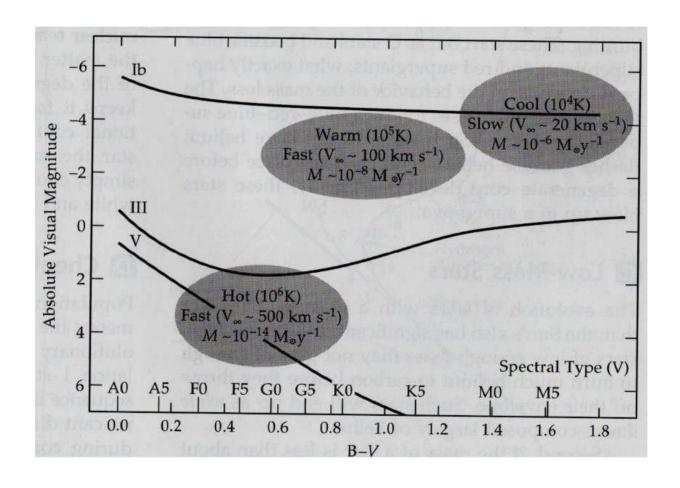
Iben 1982 (ApJ, 260, 821 – Low mass AGB evolution. I.) – Fig. 2

AGB stars

- AGB stars strong wind + rapid mass-loss $\dot{M}\sim 10^{-4}M_{\odot}~yr^{-1}$ "superwind" Cool (effective T \sim 3,000 K)
 - → dust grains exist in the matter expelled
 - O-rich environment → Silicate grains form
 - C-rich environment → Graphite grains form
- Stellar initial masses evolving to AGB : $0.89 \le \text{M/M}_{\odot} \le 5.0$ (Vassiliadis & Wood 1993, ApJ, 413, 641 : Evolution of low- and intermediate-mass stars to the end of the AGB with mass loss)
- Evolution afterwards
- depends on initial mass and mass-loss
- massive stars burnings up to form Fe → neutron stars (NSs), black holes (BHs)
- low-mass stars white dwarfs (WDs) + planetary nebulae (PNe)
- dividing mass ~ 8 M_☉

Mass Loss Rates

- Solar mass loss rate (via wind) : 10^{-14} M_{\odot}/yr
- RGB and supergiants, massive O-type stars : $10^{-7} \sim 10^{-6} \,\mathrm{M}_{\odot}/\mathrm{yr}$



Thermonuclear Energy Generation Stages

Process	Fuel	Major products	Temperat ure (K)	Minimum mass (M _☉)
H-burning	Н	He	$1-3\times10^{7}$	0.1
He-burning	He	¹² ₆ C, ¹⁶ ₈ O	2×10^8	1
C-burning	С	¹⁶ O, ²⁰ Ne, ²³ Na, ²³ Mg, ²⁴ Mg	8×10 ⁸	1.4
Ne-burning	Ne	¹⁶ ₈ O, Mg	1.5×10^{9}	5
O-burning	0	²⁴ ₁₂ Mg, ²⁷ ₁₃ AI, ²⁸ ₁₄ Si, ³¹ ₁₅ P, ³² ₁₆ S	2×10 ⁹	10
Si-burning	Mg to S	near Fe	3×10 ⁹	20

Thermonuclear Energy Generation Stages

Table 1 Evolution of a 15-solar-mass star.

Stage	Timescale	Fuel or product	Ash or product	Temperature (10 ⁹ K)	Density (gm cm ⁻³)	Luminosity (solar units)	Neutrino losses (solar units)
Hydrogen	11 Myr	Н	He	0.035	5.8	28,000	1,800
Helium	2.0 Myr	He	C, 0	0.18	1,390	44,000	1,900
Carbon	2000 yr	С	Ne, Mg	0.81	2.8×10^{5}	72,000	3.7×10^{5}
Neon	0.7 yr	Ne	O, Mg	1.6	1.2×10^{7}	75,000	1.4×10^{8}
Oxygen	2.6 yr	O, Mg	Si, S, Ar, Ca	1.9	8.8×10^{6}	75,000	9.1×10^{8}
Silicon	18 d	Si, S, Ar, Ca	Fe, Ni, Cr, Ti,	3.3	4.8×10^{7}	75,000	1.3×10^{11}
Iron core collapse*	~1 s	Fe, Ni, Cr, Ti,	Neutron star	>7.1	$> 7.3 \times 10^9$	75,000	$> 3.6 \times 10^{15}$

^{*} The pre-supernova star is defined by the time at which the contraction speed anywhere in the iron core reaches 1,000 km s⁻¹.

Stellar lifetimes

Table 1 Stellar lifetimes^a for a selection of solar-metallicity (Z=0.014) models (using models from Karakas 2014)

Mass/M _☉	Main sequence	RGB	Core He burning	AGB	Total ^b
1.0	9685	2360	118.3	21.35	12,186
2.0	874.5	162.3	130.9	18.21	1185.9
5.0	80.03	3.053	23.07	1.997	108.15
8.0	29.12	0.484	6.475	0.435	36.519

^aLifetimes are in Myr (10⁶ years)

^bThe total stellar lifetimes includes all nuclear burning phases but does not include the post-AGB or white dwarf cooling phases

Evolving up the AGB (asymptotic giant branch)

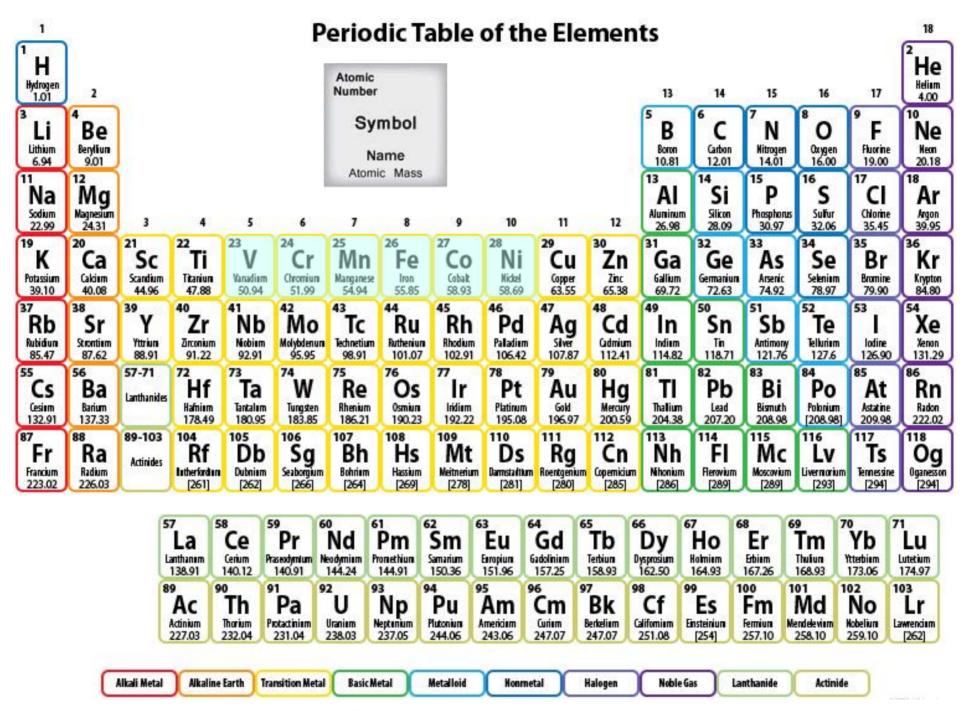
- Early-AGB (E-AGB): He shell burning Radius increases (up to 1 AU ~215 R_o)
- Thermally pulsing AGB (TP-AGB): when He shell runs out of fuel
 H shell burning
 When He builds up → He-shell ignites explosively (He-shell flash)
- He-b shell converts more and more of the He into C and then into O
 - \rightarrow CO core mass \uparrow / core contracts slowly, $\rho_c \uparrow$
 - → electron degeneracy pressure begins to dominate
- Similar to the development of an electron-degenerate He-core in a low-mass star during its rise up the RGB

Massive ($M \ge 8 M_{\odot}$) star evolution

- He-b shell → add ash to the CO core
- CO core continues to contract
- ¹²₆C-burning starts
- By-products: ¹⁶₈O, ²⁰₁₀Ne, ²³₁₁Na, ²³₁₂Mg, ²⁴₁₂Mg
- NeO core
- ¹⁶₈O-burning starts
- → Making ²⁸₁₄Si-dominated (and ³²₁₆S) core

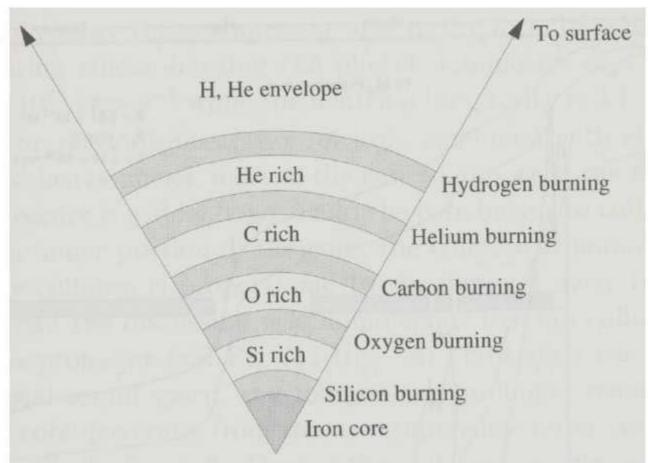
At T \sim 3×10⁹ K \rightarrow Si-burning starts

Making iron(
$${}^{56}_{26}$$
Fe)-peak elements, like ${}^{54}_{26}$ Fe, ${}^{56}_{26}$ Fe, ${}^{56}_{28}$ Fe, and finally iron-core
$$50 \le A \le 62$$
(Atomic mass)

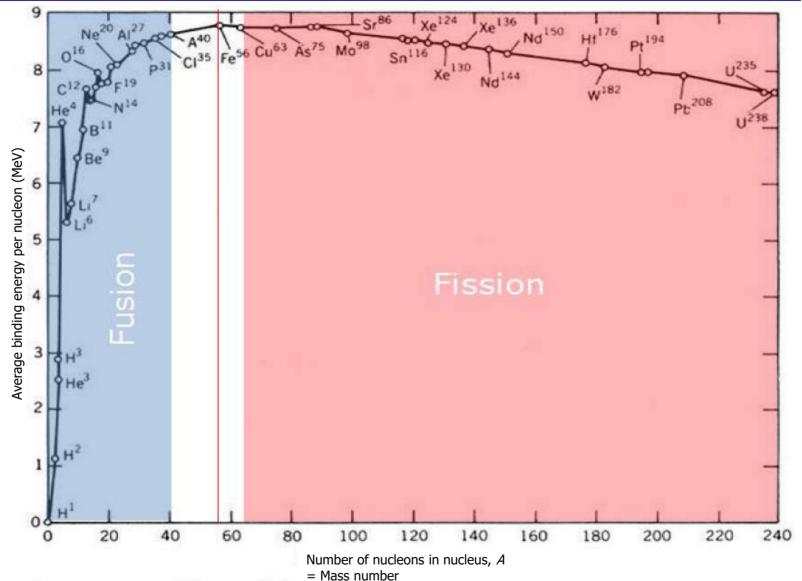


Massive (M ≥ 8 M_{\odot}) star evolution

Onion-like interior → (not to scale)

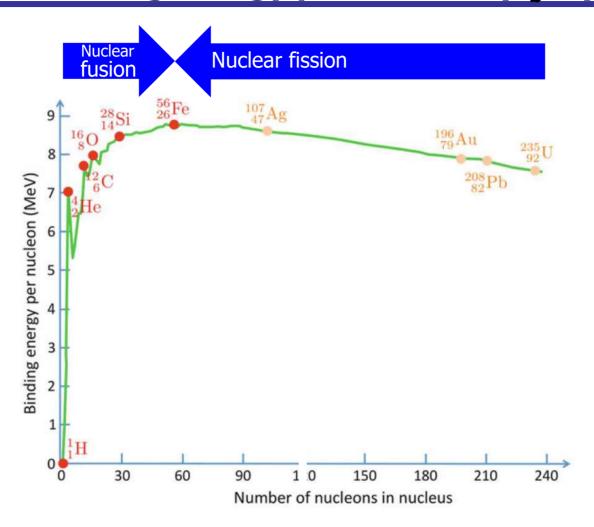


Binding energy per nuclear particle



⁵⁶₂₆Fe: the most stable nuclei

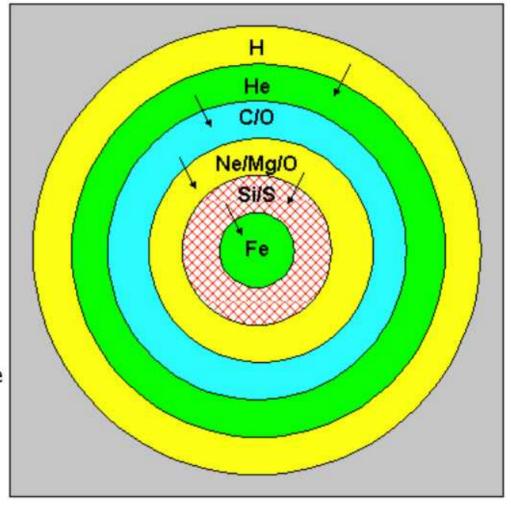
Binding energy per nucleon (E_b/A)



Fe: The largest binding energy
The most stable element
The final product of both nuclear fusion and nuclear fission

End of Massive stars → Core-Collapse Supernovae (CCSNe)

- Iron core collapse
- → shock wave propagates outward
- → outer layers (envelope) follows collapse
- → explosion!
- (expansion velocity ~a few 10⁴ km/s)



https://www.astro.umd.edu/~richard/ASTR680/A680_SNR_2019_lec1.pdf

- Final stage of the evolution of massive stars
- Outer part → SN explosion → interstellar media
- Inner part → neutron stars (pulsars) or black holes

Supernova SN 1987A (in Large Magellanic Cloud, LMC)

SN 1987A (II peculiar, LMC)

Tarantula Nebula

d~49.97 kpc (Pietrzynski+ 13 Nature 495 76)

1987 Feb 23.316 (UT)

B3 I (supergiant)

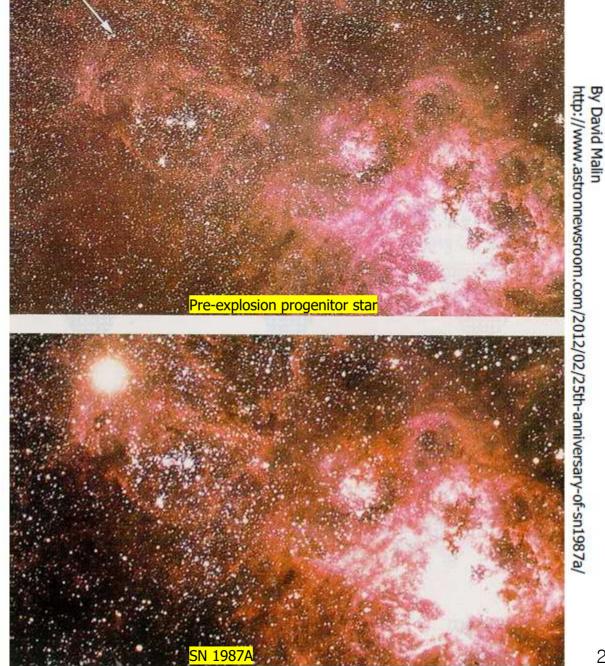
Peak: +2.9 mag

(B-V) = +0.085

 $T_{\rm eff} = 16,000 \text{ K}$

L ≥ 105 L_☉

 \rightarrow $M_{initial}\sim 20~M_{\odot}$ (N. Smith 2007 AJ 133 1034)



Yearly numbers of reported SN discoveries

Table 1 Yearly numbers of reported SN discoveries. Numbers in parentheses are that of confirmed and announced SNe on IAUCs/CBETs

Year	Discovery	1989	32	1998	163(162)	2007	607(572)
1981	11	1990	38	1999	206(201)	2008	520(261)
1982	27	1991	64	2000	185(184)	2009	475(390)
1983	28	1992	73	2001	307(305)	2010	586(337)
1984	22	1993	38	2002	338(334)	2011	902(298)
1985	21	1994	41	2003	426(335)	2012	1045(322)
1986	16	1995	58	2004	373(251)	2013	1457(228)
1987	20	1996	96	2005	377(367)	2014	1632(136)
1988	35	1997	163	2006	554(551)	2015	3412(61)

3. Star Deaths (별의 죽음) 3-2 Supernova Explosion (초신성 폭발)



Supernova (SN) types

- Brightest objects in galaxies $(M_V = -14 \sim -22)$
- Typical types

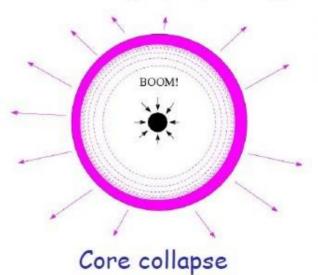
No H lines (pop II) → Type Ia Ib Ic

H lines (pop I) → Type II



WD + Giant/MS/He *
(Single Degenerate, SD)

WD + WD (Double Degenerate, DD)



.

SNe Ia (thermonuclear stellar explosion)
(WD originated SNe)
백색왜성 기원 초신성

CC SNe

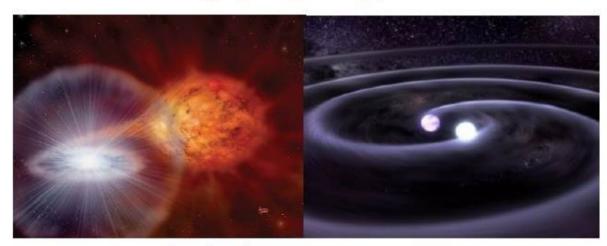
핵붕괴 초신성

http://dujs.dartmouth.edu/2008/05/type-ia-supernovae-properties-models-and-theories-of-their-progenitor-systems http://wwwmpa.mpa-garching.mpg.de/mpa/research/current_research/hl2013-8/hl2013-8-en.html http://spiff.rit.edu/richmond/sdss/sn_survey/sn_survey.html

Supernova (SN) types

- Brightest objects in galaxies ($M_V = -14 \sim -22$)
- Typical types

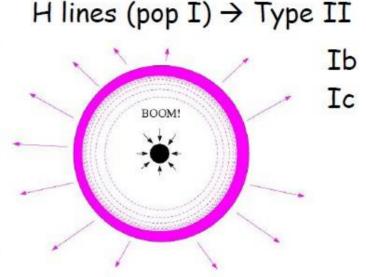
No H lines (pop II) → Type Ia



WD + Giant/MS/He *
(Single Degenerate, SD)

WD + WD (Double Degenerate, DD)

SNe Ia (thermonuclear stellar explosion)
(WD originated SNe)
백색왜성 기원 초신성



CC SNe

Core collapse

핵붕괴 초신성

http://dujs.dartmouth.edu/2008/05/type-ia-supernovae-properties-models-and-theories-of-their-progenitor-systems http://wwwmpa.mpa-garching.mpg.de/mpa/research/current_research/hl2013-8/hl2013-8-en.html http://spiff.rit.edu/richmond/sdss/sn_survey/sn_survey.html

Supernovae taxonomy

Туре	Sub-types						
I No H	Ta Si II (6150Å) absorption near peak light						
	Ib/c Weak/no Si absorption	Ib He I (5876Å) emi					
		Ic Weak/no He					
II	II-P/L/n	II-P/L No narrow lines	II-P Plateau in light curve(LC: mag vs time)	SNII-P			
			II-L Linear decrease in LC	SNII-L			
	Some narrow lines	IIn: Hines					
			Ibn: He lines				
5Ne	IIb : Spectrum chang	ges to become like t	type Ib				

Ic-BL: sometimes associated with GRBs and/or hypernova (broad lines: (2-3)×10⁴ km/s)

ultra-bright type II: ~10⁵¹ erg radiation energy

.Ia: changing rapidly

Superluminous SNe, pair-instability SNe, Superluminous Ia

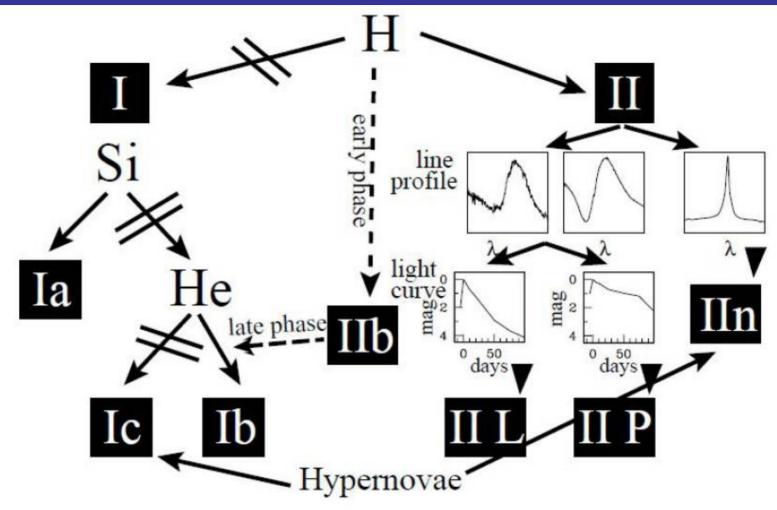
Subluminous SNe, Subluminous Ia

Super-Chandrasekhar Ia: mass > Chandrasekhar limit

Ia-IIn: CSM

Iax : Ia w/lower L, less E, less ejecta mass Kilonova/macronova, SN imposters, magnetar

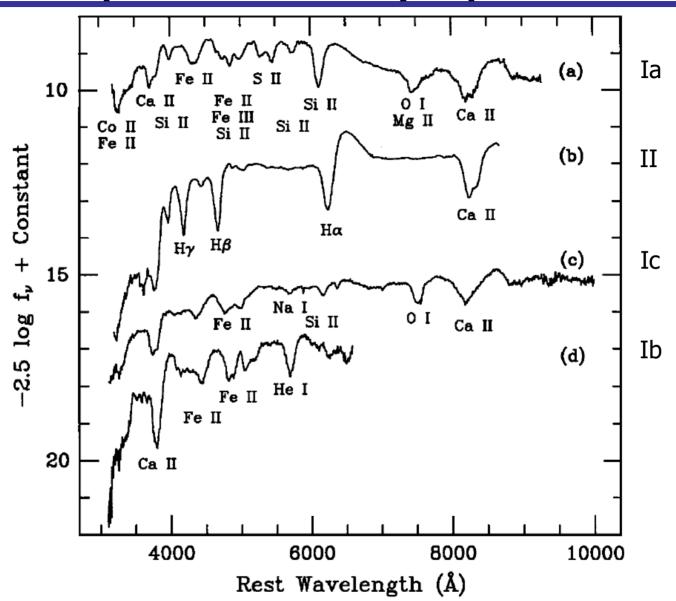
Supernova taxonomy



Cappellaro & Turatto (2000) Figure 2

https://arxiv.org/abs/astro-ph/0012455

Supernova taxonomy - spectra



Supernova imposters

im-pos-tor, -post-er [impáster/-pós-] n.

남의 이름을 사칭하는 자; 사기꾼, 협잡꾼.

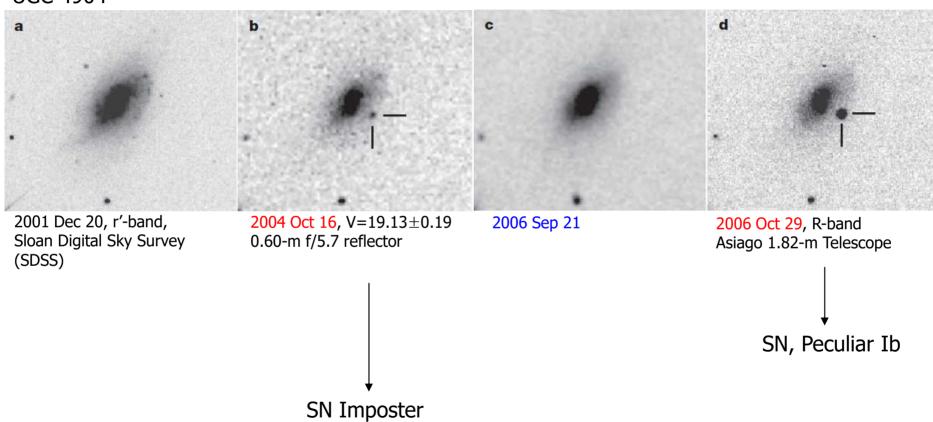
impostor



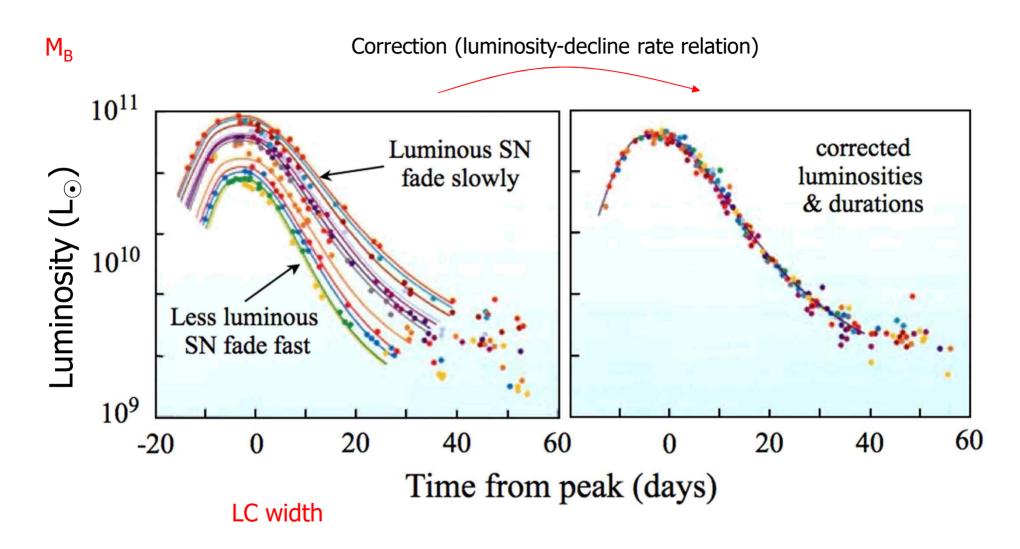
a person who pretends to be someone else in order to deceive others:

 He felt like an impostor among all those intelligent people, as if he had no right to be there.

UGC 4904



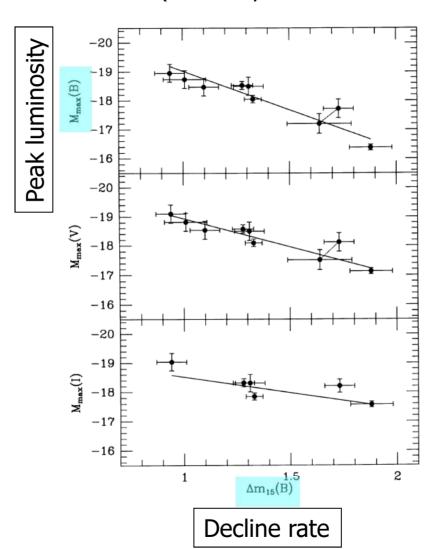
Supernova(SN) Ia light curve (LC)



Supernova(SN) Ia light curve (LC)

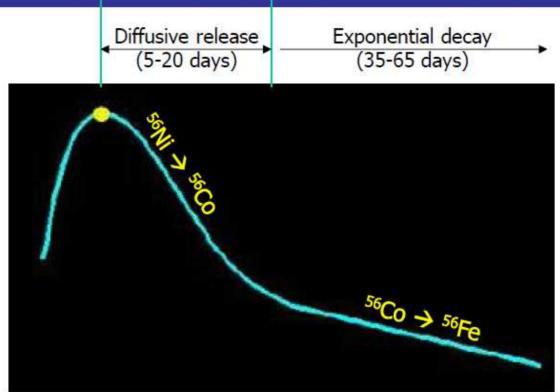
Correction (luminosity-decline rate relation)

Philips Relation (Philips 1993 ApJL 413, L105)



: Mag decrease from the peak mag for 15 days

Supernova(SN) Ia light curve (LC)

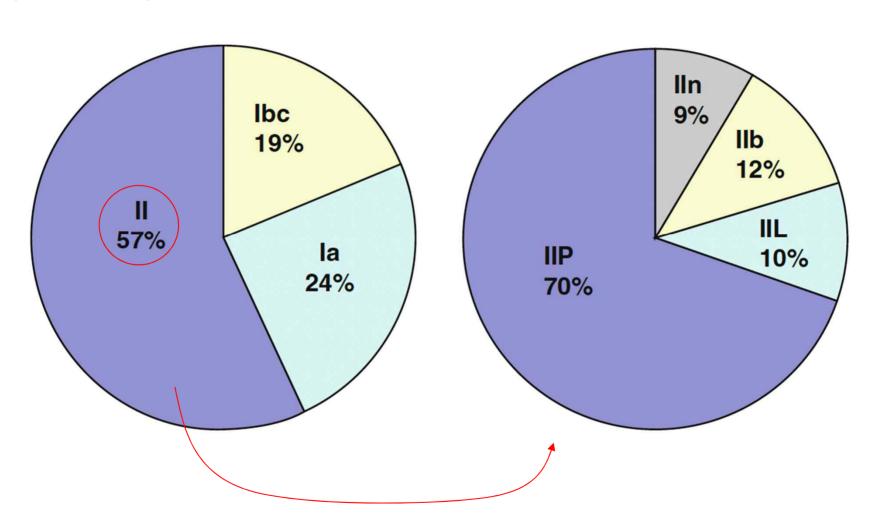


Radioactive decay of $^{56}Ni \rightarrow ^{56}Co \rightarrow ^{56}Fe$ (Colgate & McKee 69 ApJ 157 623; Arnett 82 ApJ 253 785)

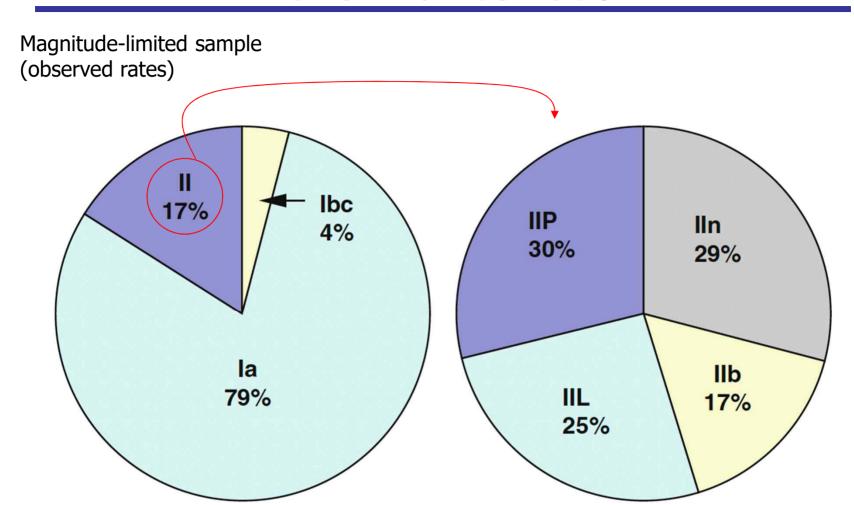
$$\begin{array}{c} {\rm half\; life} \\ {\rm ^{56}Ni} \ \to \ {\rm ^{56}Co} + e^+ + \nu_e + \gamma \\ {\rm ^{56}Co} \ \to \ {\rm ^{56}Fe} + e^+ + \nu_e + \gamma \\ \end{array} \begin{array}{c} {\rm half\; life} \\ {\rm ^{6.10\; d,\; E=1.72\; MeV} } \end{array}$$

SNe – number ratio

Volume-limited sample (Intrinsic rates)



SNe – number ratio



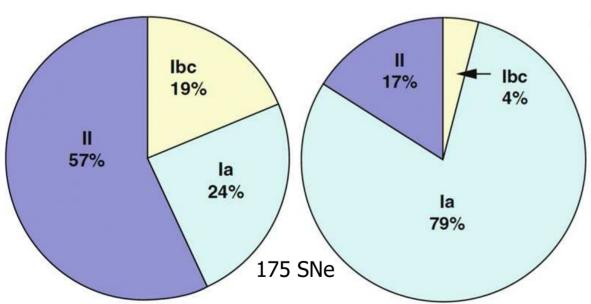
SNe Ia – distance indicator

- SN Ia : maximum brightness (peak luminosity) $M_V \sim -19.30 \pm 0.03 + 5 \log (H_0/60)$
- Rising time ~ 20 days

Number ratio

Ia : CC = 24 : 76

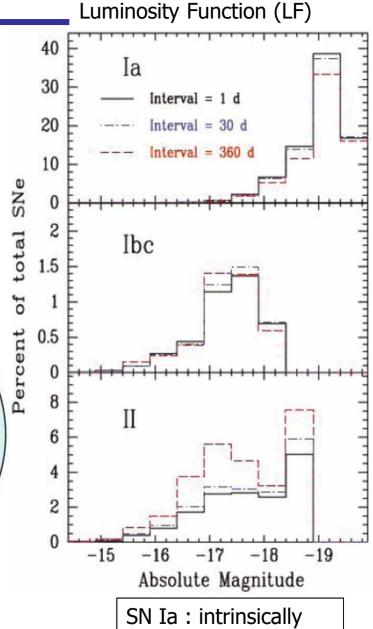
Ia : CC = 79 : 21



Volume-limited sample $D \le 60 \text{ Mpc}$ (CC SNe)

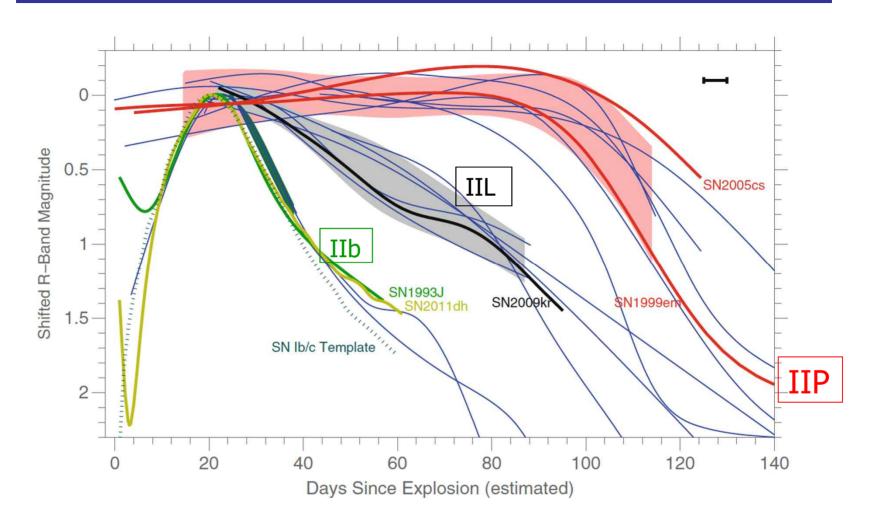
 $D \le 80 \text{ Mpc} (SNe Ia)$

Magnitude-limited sample

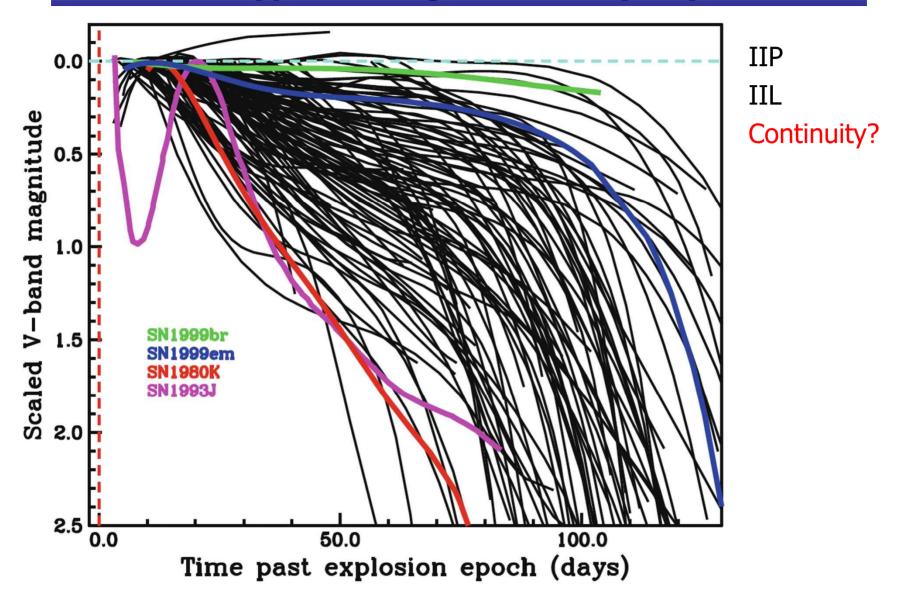


SN Ia: intrinsically brighter than CC SNe

Type II – Light Curves (LCs)



Type II – Light Curves (LCs)



CC SNe vs. SNe Ia

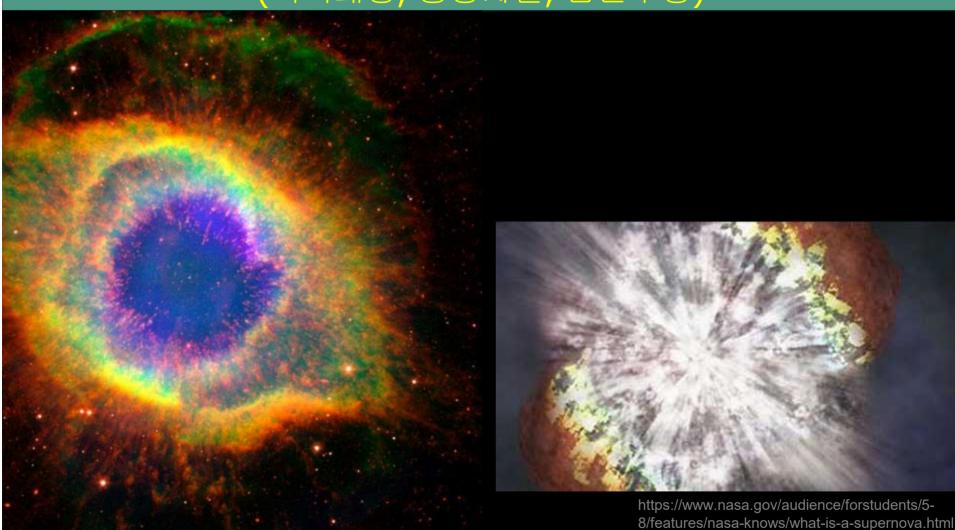
- CC SNe: not in early-type galaxies, Spiral galaxies spiral arms
- SN Ia: all types of galaxies (Spiral galaxies no spatial preference)
- spiral arms = short-lived massive stars
- → CC SNe = massive stars
 SN Ia = not that massive stars
- Total energy emitted in neutrinos 3×10⁵³ erg
- Total kinetic energy ~10⁵¹ erg = f.o.e. = foe
- ~1% of total kinetic energy comes in photons ~ 10^{49} erg (peak luminosity ~ 10^{43} erg/s, ~ 10^9 L_{$_{\odot}$}, ~brightness of an entire galaxy)

CC SNe vs. SNe Ia

- Total energy emitted in neutrinos 3×10⁵³ erg
- Total kinetic energy ~10⁵¹ erg = f.o.e. = foe
- ~1% of total kinetic energy comes in photons ~ 10^{49} erg (peak luminosity ~ 10^{43} erg/s, ~ 10^9 L_o, ~brightness of an entire galaxy)



3. Star Deaths (별의 죽음) 3-3 White Dwarfs, Neutron Stars, and Black Holes (백색왜성, 중성자별, 검은구멍)

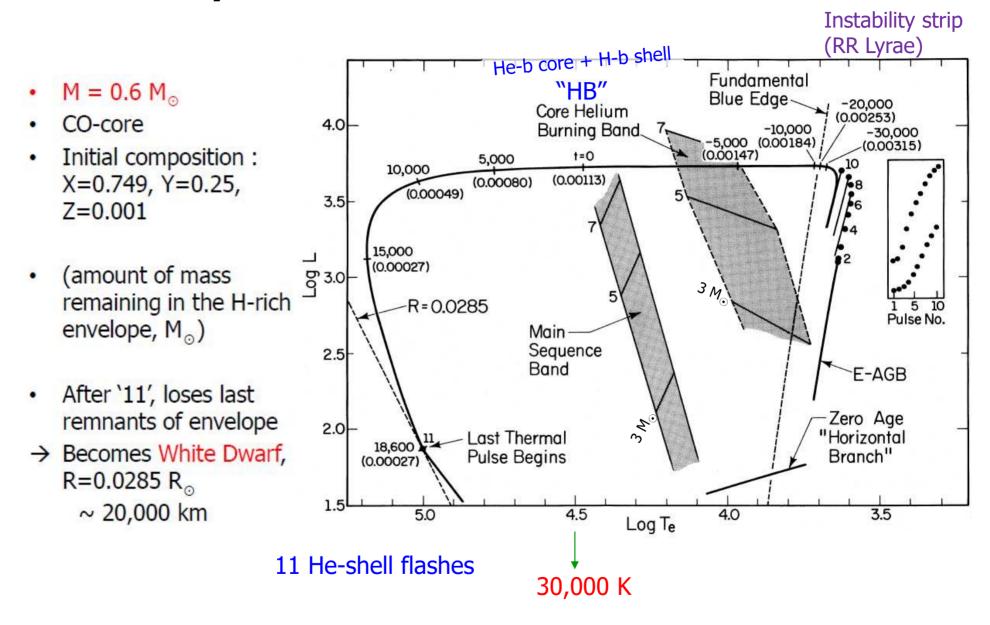


Helix Nebula in the Aquarius

© © NASA/JPL-Caltech/Corbis

https://www.dailymail.co.uk/sciencetech/article-3517714/The-dying-star-rewrite-know-stellar-evolution-White-dwarf-bizarre-atmosphere-oxygen.html

1. Planetary nebula evolution in the CMD



WDs - general

RG

```
Extremely low-mass (M_i \le 0.2 M_{\odot}) \rightarrow \text{no He-b} \rightarrow \text{He WD}

M_i \le 8 M_{\odot}, T_c < 10^9 \text{ K, No C-burning} \rightarrow \text{CO-core} + \text{PN}

\rightarrow \text{CO WD}

8 < M_i < 10.5 M_{\odot} \rightarrow \text{C-b, but no Ne-b}

\rightarrow \text{ONeMg WD}
```

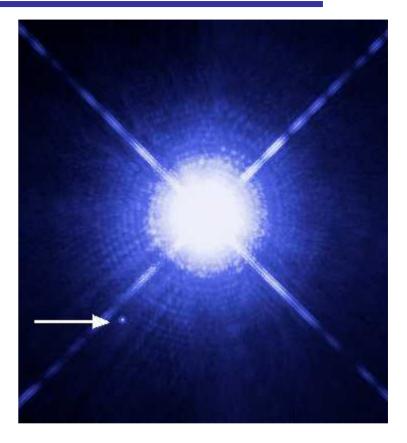
No fusion reactions, supported by electron degenerate pressure

```
(Current) Mass: 0.55-0.6~{\rm M}_{\odot}
- min mass \sim 0.4~{\rm M}_{\odot}
- max mass for a non-rotating WD = Chandrasekhar mass \sim 1.4~{\rm M}_{\odot}
Typical density \sim 10^6~{\rm g/cm}^3
Typical B \sim 10^6~{\rm Gauss}~(2\times 10^3 - 10^9~{\rm Gauss})
```

Binary – mass transfer from a companion → CO WD mass approaches the Chandrasekhar mass → C-detonation → SN Ia

Evolution: hot WD → E decreases, color reddens → black dwarf (timescale > 13.8 Gyr)

→ no black dwarf yet formed



Sirius A, Sirius B (WD) - HST

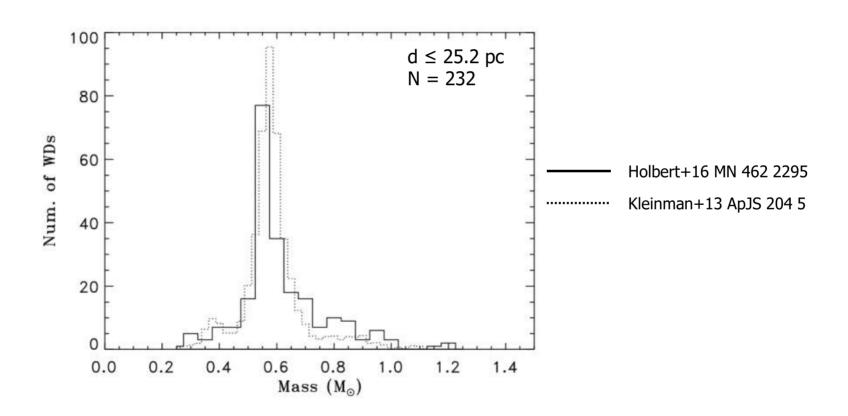
https://en.wikipedia.org/wiki/White_dwarf

WD catalog

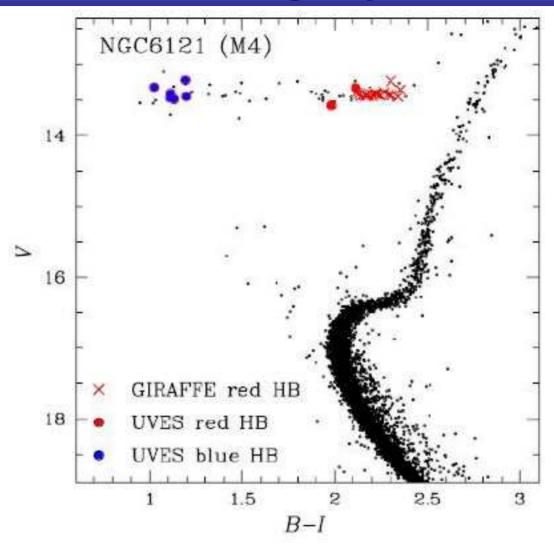
 Villanova Catalogue of Spectroscopically identified WDs (McCook & Sion 99 ApJS 121, 1-130, N=2249)

http://www.astronomy.villanova.edu/WDCatalog/index.html

• Volume-limited WD sample within 25 pc : Holbert+16 MN 462 2295



WD – cooling sequence



Marino+11 (ApJ 730 L16 - Sodium-Oxygen Anticorrelation Among HB Stars in the GC M4)

VLT 8.2m

WD - cooling sequence

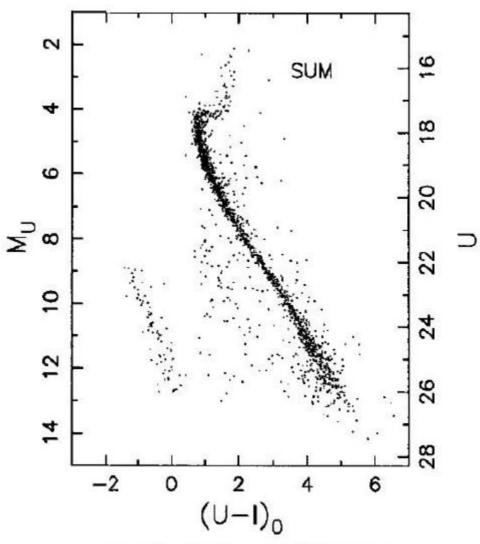
WD cooling line of the GC M4

: bluest stars

: U = 22 - 26 mag

$$L \propto T_{eff}^4$$
 or
$$M_{bol} = - \, 10 \, \log T_{eff} + const.$$

- Constant radius line
- Roughly parallel to the MS
- Stretched not by mass, but by age (young → old)



U-(U-I) CMD of GC M4 (NGC 6121)
HST

Richer et al. 1995 (ApJ 451 L17 - HST Observations of WDs in the GC M4)

WD – cooling sequence

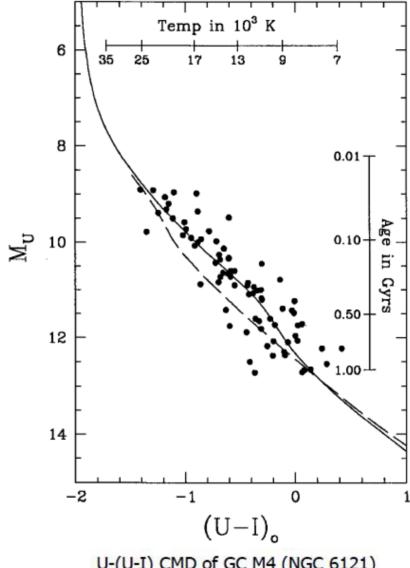
WD cooling line of the GC M4

: bluest stars

: U = 22 - 26 mag

$$L \propto T_{eff}^4$$
 or $M_{bol} = -10 \log T_{eff} + const.$

- Constant radius line
- Roughly parallel to the MS
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U-(U-I) CMD of GC M4 (NGC 6121) HST

Richer et al. 1995 (ApJ 451 L17 - HST Observations of WDs in the GC M4)

2. Neutron Stars (NSs, 중성자별)

- M_i ≥8 M_☉
- M_f > 1.4 M_☉ → degenerate electron gas pressure cannot hold off gravity
 → matter is crushed to very high densities → inverse- β decay occurs :

$$p^+ + e^- \rightarrow n + \nu$$

(protons and electrons are squeezed into neutrons)

- Degenerate neutron gas → provides internal pressure
- Mass: 1.1 2 M_☉ (upper limit ~ 3 M_☉)

```
Typical mass \sim 1.4 \rm M_{\odot}
Typical radius \sim 10 km
Typical density \sim 4 \times 10<sup>14</sup> g/cm<sup>3</sup>
(400,000 ton/mm<sup>3</sup>)
B \sim 10<sup>12</sup> Gauss
Surface temp \sim6 \times 10<sup>5</sup> K
```

```
※ 1 Tesla = 10<sup>4</sup> Gauss

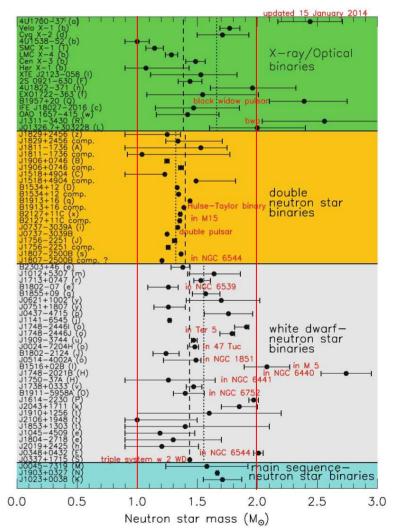
※ Sun: mean density ~ 1.408 g/cm<sup>3</sup>

B<sub>⊙</sub>~1-2 Gauss

※ Earth: B<sub>⊕</sub>~0.1 Gauss

※ Magnetic Resonance Imager (MRI, 자기공명영상):

B~10<sup>5</sup> B<sub>⊕</sub>~1 Tesla
```

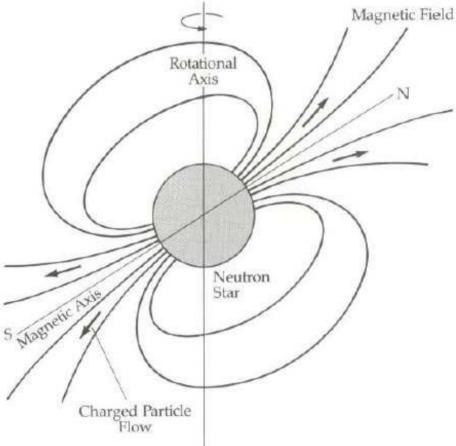


Horvath & Valentim 2017, Handbook of Supernovae, Volume 2, p. 1317

2-1. Pulsars (펄사)

- pulsating star = pulsar = rotating neutron stars
- 1967 discovered by Jocelyn Bell Burnell and Anthony Hewish (1974 Nobel prize)
 Radio pulses coming every 1.33730113s (at 81.5 MHz)+ 3 more objects
- Now, N~2300, P~1.6×10⁻³ to 4.0 s (average 0.65 s)
- · Strong magnetic field
- → Synchrotron radiation along the magnetic dipolar axis
- Lighthouse model: transforms the rotational energy into electromagnetic energy → emits through the magnetic axes → pulse period = rotation period
- If the Sun becomes a NS → R = 7 km

TABLE 17–1 Properties of Selected Pulsars					
Name (PSR)	Period (s)	$dP/dt (10^{-15} \text{ s/s})$	DM(pc/cm ³)		
1937 + 21	0.001557	1.07×10^{-4}	71.2		
1855 + 09	0.005362	46421	13.3		
0531 + 21 (Crab)	0.033326	421	56.8		
0833 - 45 (Vela)	0.089234	124	69.1		



magnetic axis is inclined with respect to the rotation axis

2-1. Pulsars (펄사)

- Dispersion: a given pulse arrives at the Earth later as we look at lower frequencies
 - Due to a slowing down of the photon velocity by electrons in the line-of-sight (los)
 - Longer λ are slowed down more
 - Observations can tell us the mean electron density in the los
- If pulses of ν₁ and ν₂ (ν₁ > ν₂) are emitted at time t₀ → they arrive at t₁ and t₂,

- respectively $\text{Then,} \quad t_1-t_0=\frac{d}{v_1} \quad \text{and} \quad t_2-t_0=\frac{d}{v_2}$ $\text{We can measure} \quad t_2-t_1 \ \Rightarrow \text{equal to} \quad (\frac{1}{v_2}-\frac{1}{v_1})d$
- Velocities depend on the electron density → if we know the electron density, we can get the distance
- Dispersion Measure (DM) = integrated electron density : $DM = \int_{-a}^{a} n_e dl$

TABLE 17-1	Properties of	Selected	Pulsars
TABLE /-	1 10 DCI CICS OI	Delected	1 61136113

Name (PSR)	Period (s)	$dP/dt \ (10^{-15} \text{ s/s})$	DM(pc/cm ³)
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Binary pulsars (쌍성 펄사)

- First binary pulsar, PSR B1913+16: 1974 at Arecibo by Joseph H. Taylor, Jr. (조세프 테일러, b. 1941), Russell Hulse (러셀 헐스, b. 1950)
- "Hulse-Taylor binary pulsar"
- Einstein's theory of general relativity → two NSs would emit gravitational waves as they orbit a common center of mass
- Gravitational waves carry away orbital energy → cause the two stars get closer → orbital P ↓

The Nobel Prize in Physics 1993

Russell A. Hulse and Joseph H. Taylor Jr. "for the discovery of a new type of pulsar, a discovery that has opened up new possibilities for the study of gravitation"

https://www.nobelprize.org/prizes/lists/all-nobel-prizes-in-physics/

3. Black Holes (BHs, 검은구멍)

- A region of spacetime in which gravity is so strong that nothing (incl. light) can escape it
- Minimum mass ~ 3 M_o
- Theoretically zero volume and infinite density → "singularity" (breakdown of the laws of physics)
- An object with escape speed $v_{\it esc}$ at the surface of the BH :

Total Energy = KE + PE =
$$\frac{mv_{\it esc}^2}{2} - \frac{\it GmM}{\it R} = 0$$

Assuming max escape velocity = c

$$R = \frac{2GM}{c^2} = 3M \text{ km}$$

- If the Sun becomes a BH → density ~10¹⁶ g/cm³ (~nucleus of an atom)
- If an object cross the Schwarzshild radius, it crashes into a singularity (zero volume)

Schwarzshild radius



black_hole_baird.jpg
http://sciencequestionswithsurprisinganswers.org/20
13/06/18/can-you-go-fast-enough-to-get-enoughmass-to-become-a-black-hole/
56

3. Black Holes (BHs, 검은구멍)

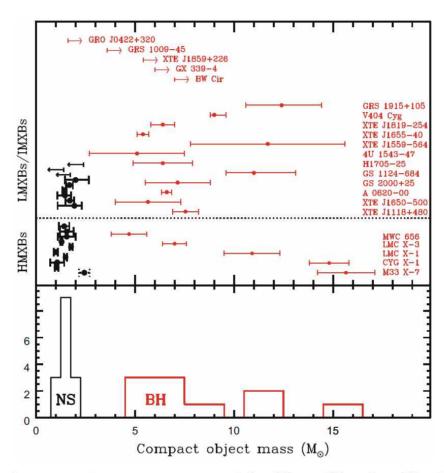
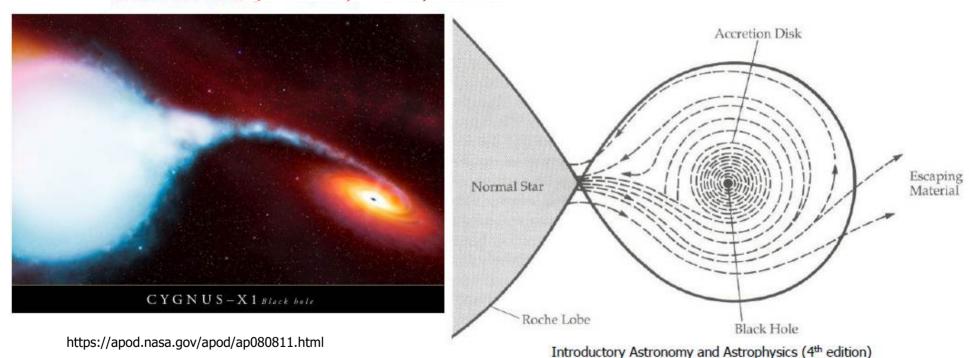


Fig. 2 *Top*: compact remnant masses measured in X-ray binaries. Neutron stars and black holes are indicated in *black* and *red colors*, respectively. 4U 1700-37 is plotted in *dotted-style line* because the nature of the compact star is uncertain. The *horizontal dotted line* divides LXMBs/IMXBs from HMXBs. *Bottom*: observed distribution of neutron stars and black hole masses

3. Black Holes (BHs, 검은구멍)

- How to observe/find a BH?
- not for an isolated BH → but for a BH in a binary system (interactions with other material)
- matter falling toward a BH gains kinetic energy → heats up, becomes ionized → emits electromagnetic radiation
- If T reaches a few×10⁶ K → emits X-rays
- accreted material + initial angular momentum → form a disk around the BH : accretion disk (강착원반) = X-ray source



X-ray sources: good candidates for BHs

Michael Zeilik & Stephen A. Gregory (1998), p. 348