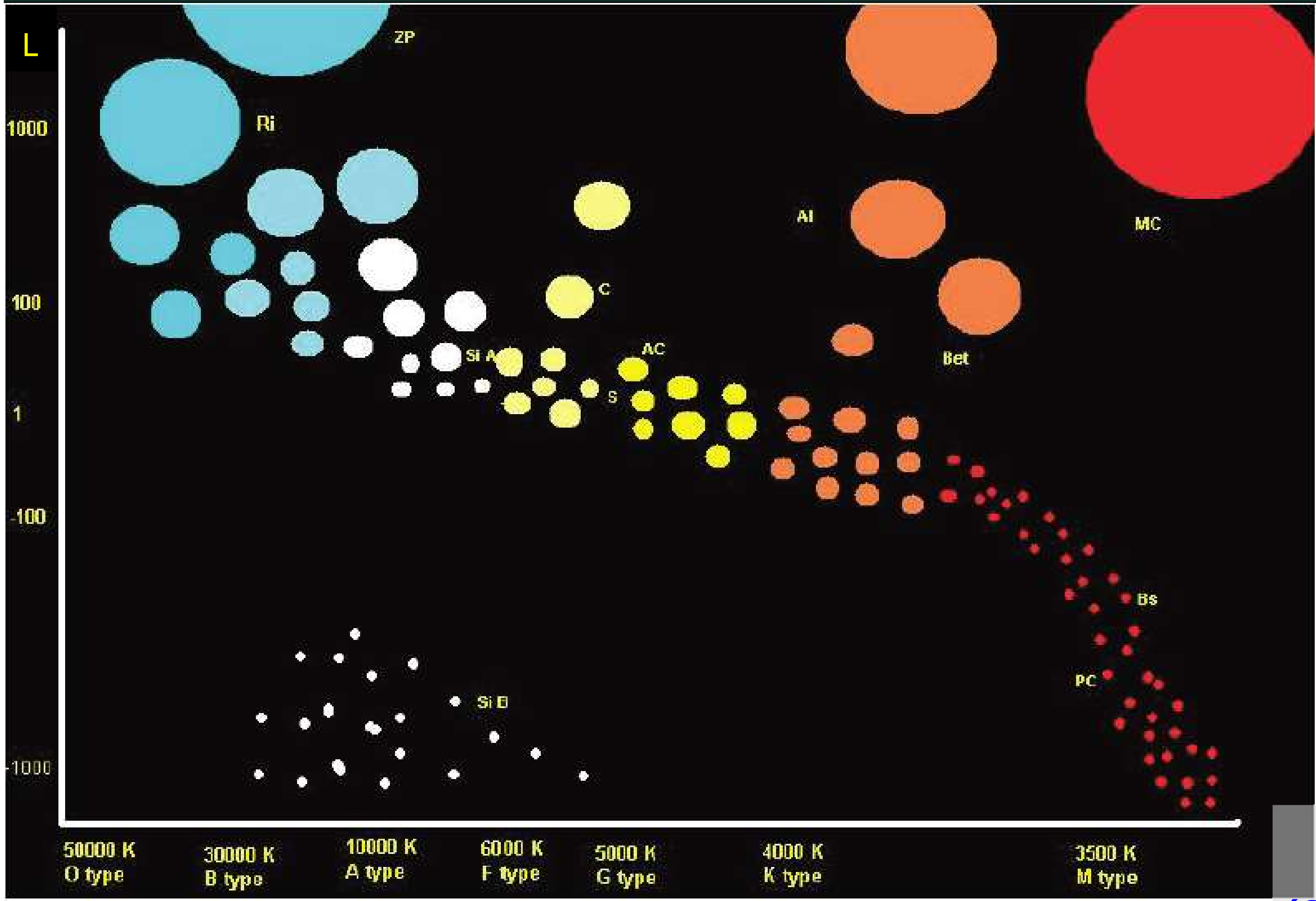
Part II. Stellar Evolution and the Milky Way Galaxy

Chapter 1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)

1-1 Two-dimensional distribution of stellar parameters
(별들의 2차원 분포 그림)



http://solarandspace.tripod.com/id11.html

ZP= Zeta Puppis
Ri= Rigel
SiA= Sirius A
SiB= Sirius B
C= Capella
S= Sun
AC= Alpha Centuri A
Al= Aldebaren
Bet= Betelgeuse
MC= Mu Cephi
PC= Proxima Centuri
Bs= Barnards star

김상철
(Sang Chul KIM)

Modern Astronomy

Part II. Stellar Evolution and the Milky Way Galaxy (항성진화와 우리은하)

- Instructor : 김상철(Sang Chul KIM, Center for Large Telescopes, JangYoungSil-Hall Room 315, 042-865-3246, 010-8622-5618, sckim@kasi.re.kr)
- References (참고문헌) :
  - Introductory Astronomy and Astrophysics (4th edition), Michael Zeilik & Stephen A. Gregory (1998)
  - An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996)
  - Galactic Astronomy (J. Binney & M. Merrifield, 1998)
  - An Introduction to Stellar Astrophysics (Francis LeBlanc, 2010)
  - Evolution of Stars and Stellar Populations (Maurizio Salaris & Santi Cassisi, 2005)
  - 항성내부구조 및 진화, Dina Prialnik 지음, 김용기 옮김, 2007 (An Introduction to the Theory of Stellar Structure and Evolution, 2000)

- Evaluation : Attendance 10%, Written final exam 90%
- Final exam : 2024 October
- Lecture note will be uploaded to sckim86.github.io by 1 hour before

Modern Astronomy

Part II. Stellar Evolution + MWG

Oct 7	Chapter 1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)
Oct 8	Chapter 2. The Evolution of Stars (별의 진화)
Oct 14	Chapter 3. Star Deaths (별의 죽음)
Oct 21	Chapter 4. The Milky Way Galaxy (우리은하)

Modern Astronomy

Part II. Stellar Evolution + MWG

Oct 7 Chapter 1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)

- 1.1 HRD (Hertzsprung-Russell Diagram, H-R도)
- 1.2 Distances (거리)
- 1.3 Magnitudes (등급)
- 1.4 The Classification of Stellar Spectra (별의 스펙트럼 분류)

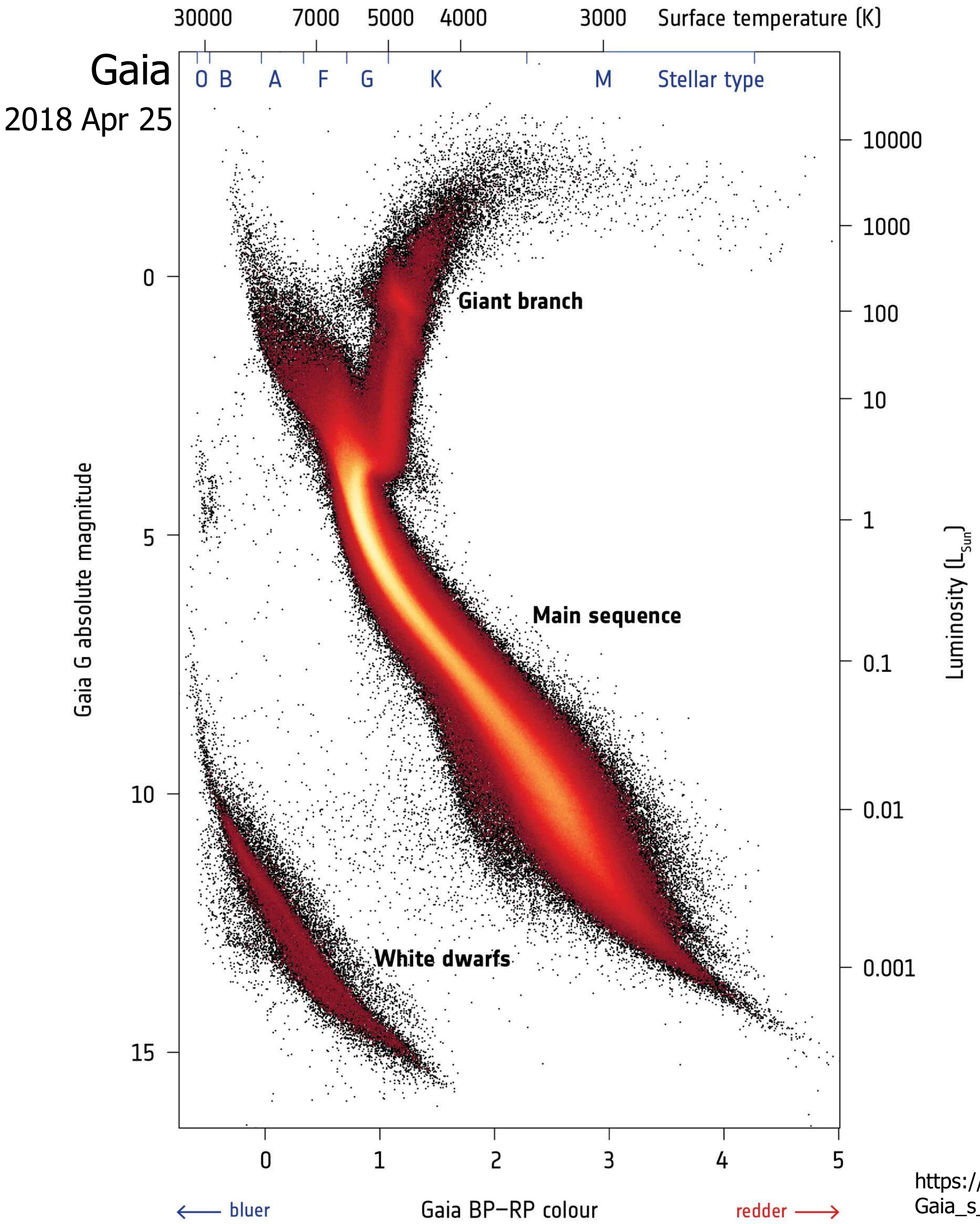
Oct 8 Chapter 2. The Evolution of Stars (별의 진화)

Oct 14 Chapter 3. Star Deaths (별의 죽음)

Oct 21 Chapter 4. The Milky Way Galaxy (우리은하)

1. Stars: The Hertzsprung-Russell Diagram

1.1 Two-dimensional distribution of stellar parameters (별들의 2차원 분포 그림)



https://www.esa.int/ESA_Multimedia/Images/2018/04/Gaia_s_Hertzsprung-Russell_diagram

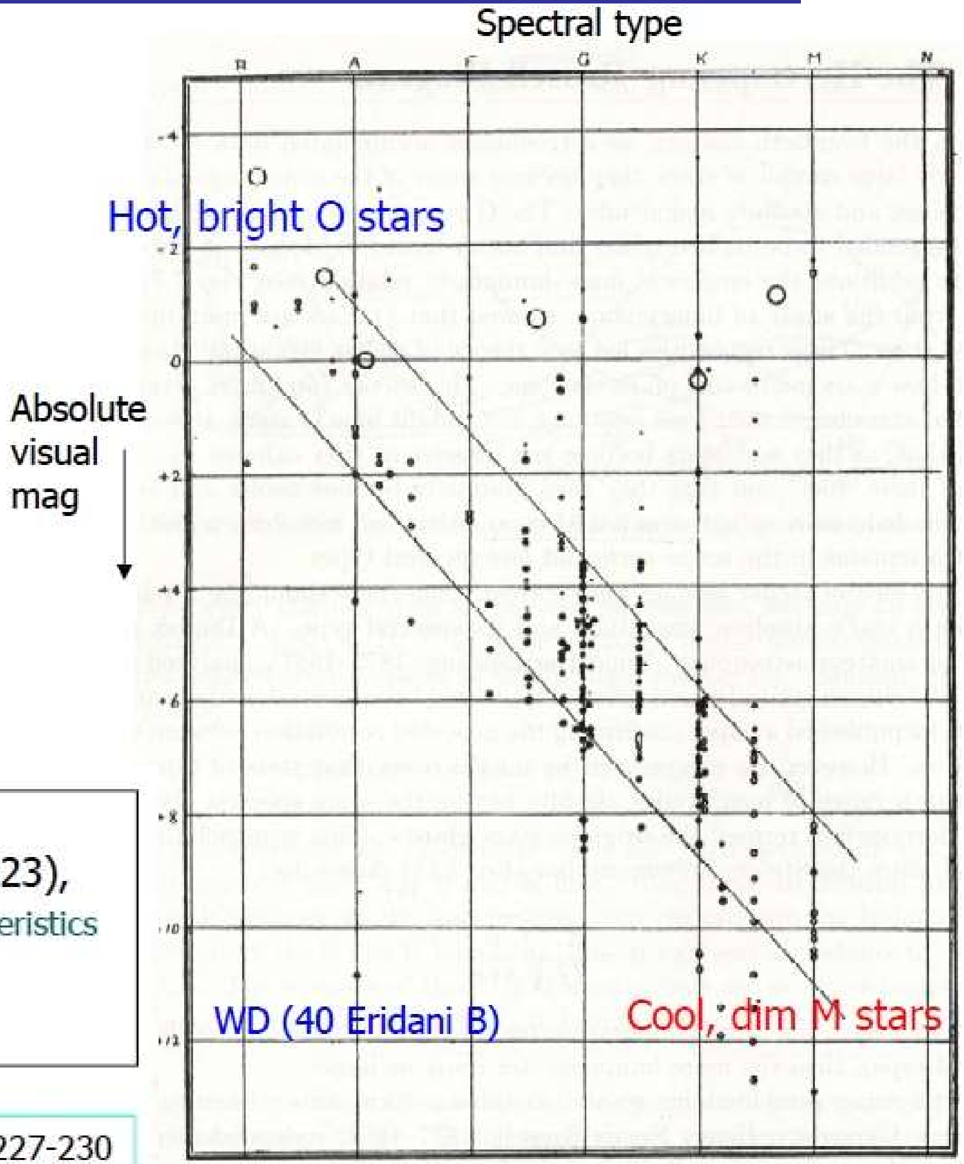
Hertzsprung-Russell Diagram

1911 Ejnar Hertzsprung
Danish engineer and
amateur astronomer

1913 Henry Norris Russell
US, Princeton University
1913 – published the "diagram"

80-90% of all stars – main sequence (MS) stars

※ Bengt Strömgren (1908-1987, Danish)
: suggested the name "H-R" diagram



An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 242

Fig 8.10 Henry Norris Russell's first diagram (Russell, H. N. 1914 May 07, Nature, 93 (Number 2323), 252-258 `Relations Between the Spectra and other Characteristics of the Stars. II. Brightness and Spectral Class')
Fig. 1. > 200 stars

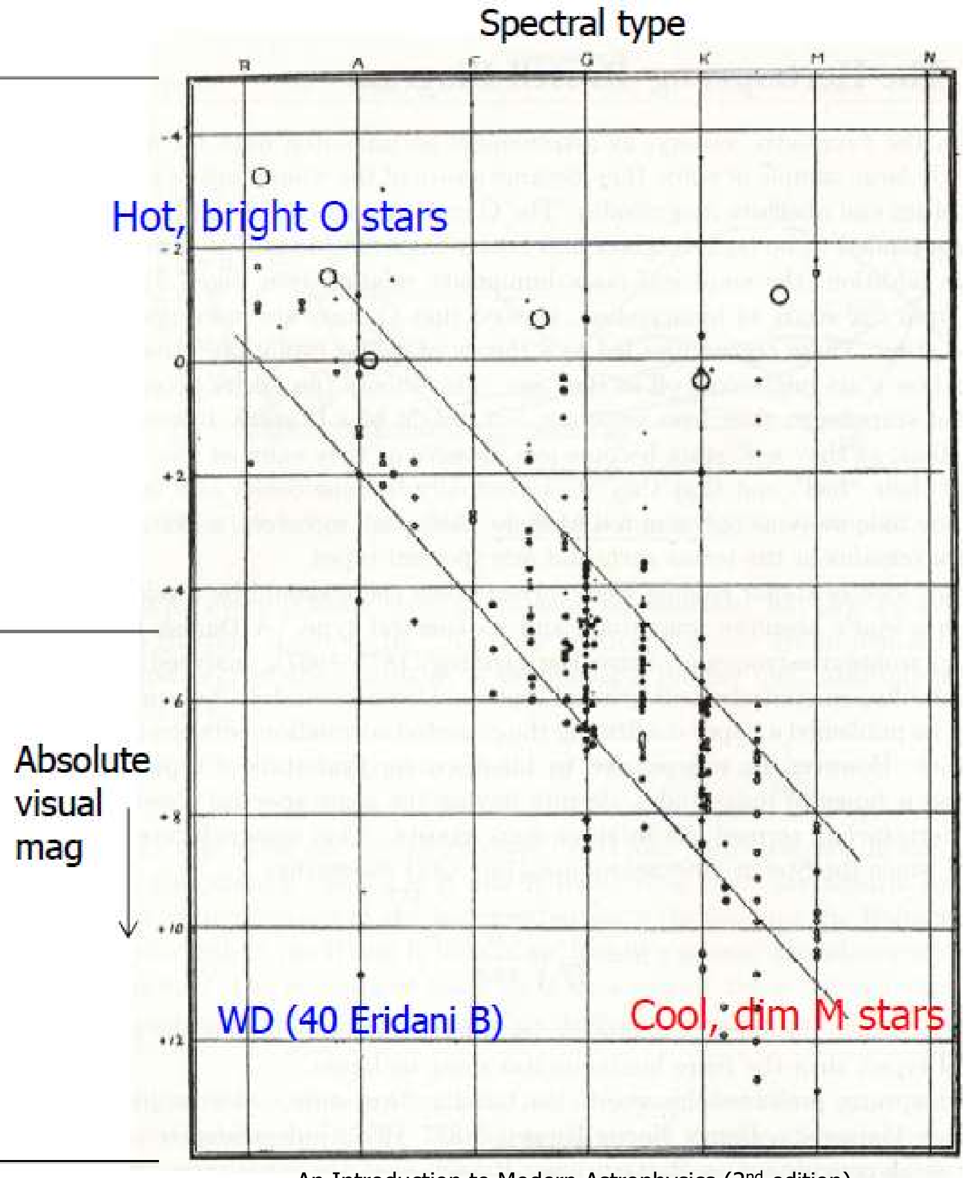
※ (Russell, H. N. 1914 April 30, Nature, 93 (Number 2322), 227-230 `Relations Between the Spectra and other Characteristics of the Stars. I. Historical')

Hertzsprung-Russell Diagram

$M_V = -5 \rightarrow L = 7500\ L_\odot$

$M_{V,\odot} = +4.7$

$M_V = +14 \rightarrow L = 1/5000\ L_\odot$



An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 242

Main Sequence (MS, 주계열성)

'Sequence'

NAVER 영영사전

sequence 미국식 [ˈsiːkwəns] 영국식

1. 명사 the order in which things happen or should happen
2. 명사 a group of things that come one after the other, series
3. 명사 a part of a movie, television show, etc., that deals with one subject, action, or idea

sequence | 유의어

n. chain, cycle, series, arrangement, order, progression succession

계열 系列 [발음 : 계 : 열/게 : 열]   파생어 : 계열적

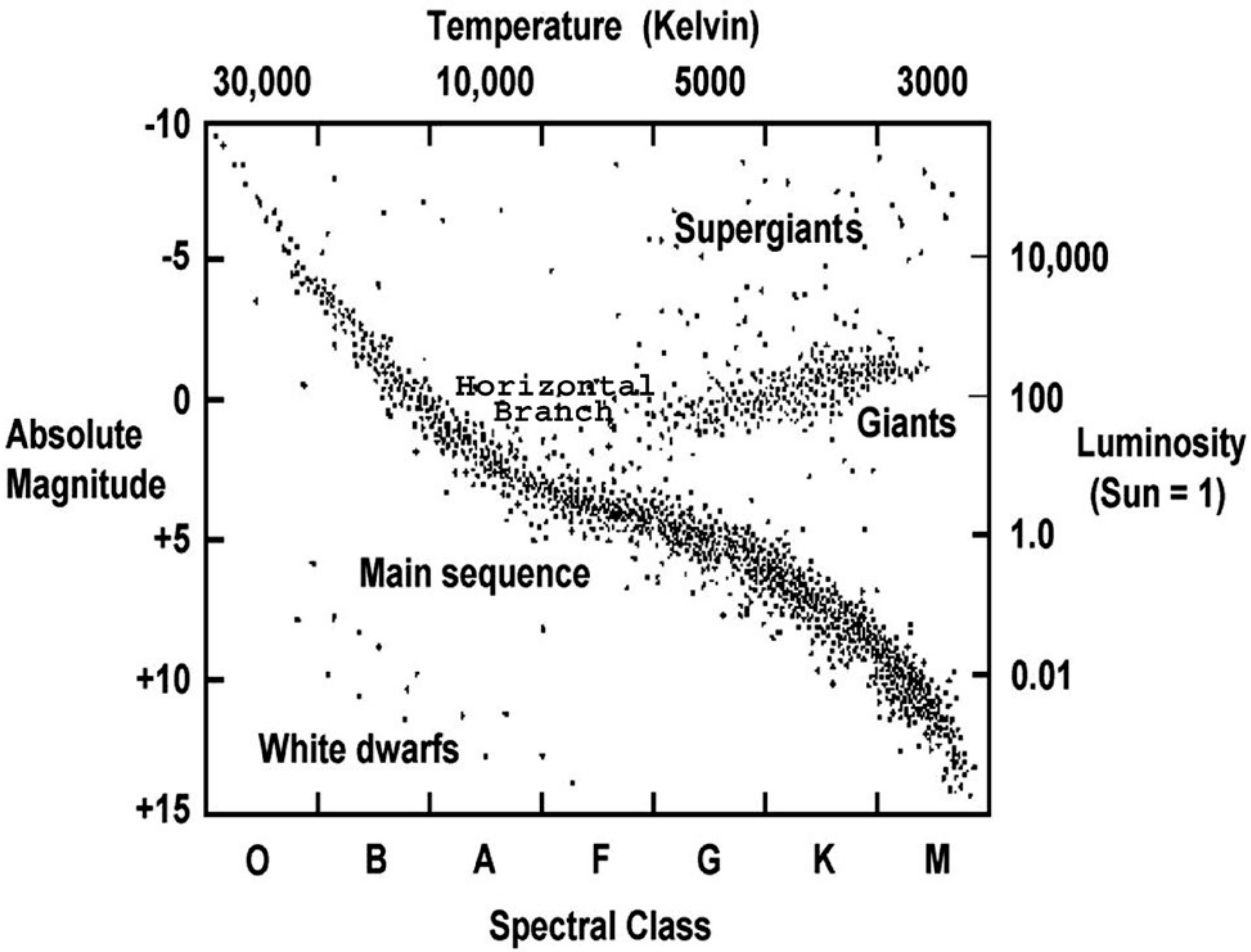
명사

1. **서로 관련이 있거나 유사한 점이 있어서 한 갈래로 이어지는 계통이나 조직.**
   - 인문 **계열**
   - 염상섭의 소설은 사실주의 **계열의** 작품이다.
   - 교내 **계열** 평균에서 13반이 꼴등입니다. 출처 : 전상국, 퇴장

2. 〈경제〉 **기업의 결합 형태의 하나. 생산, 판매, 자본, 기술, 중역 파견 따위에 따라 대기업 상호 간 또는 대기업과 중소기업 간에 볼 수 있는 기업 결합이다.**
   - **계열** 산업.

Main Sequence (MS, 주계열성)

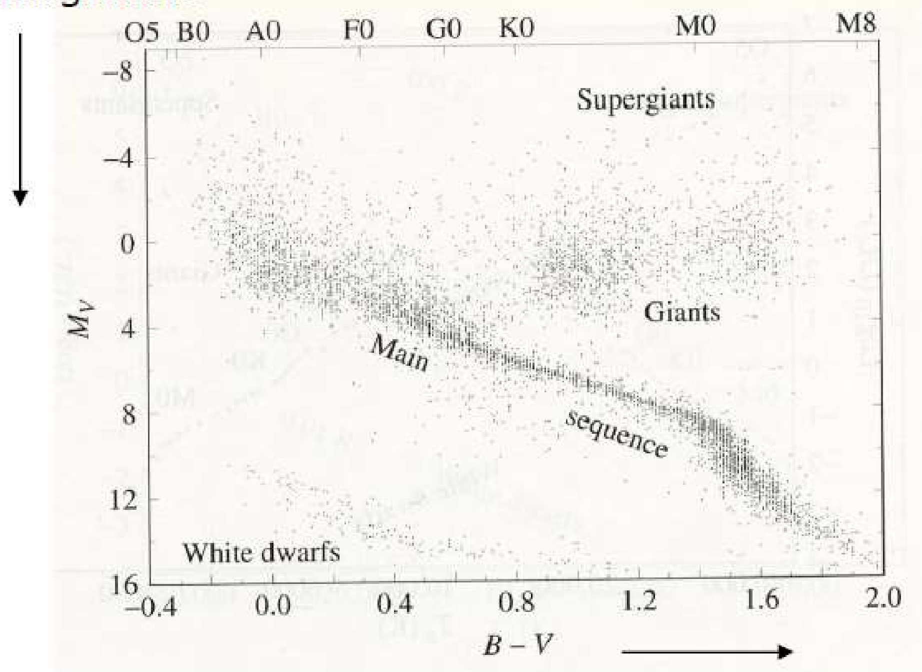
Sequences!



https://chandra.harvard.edu/edu/formal/variable_stars/HR_student.html

Observer's vs Theoriest's H-R diagrams

magnitude



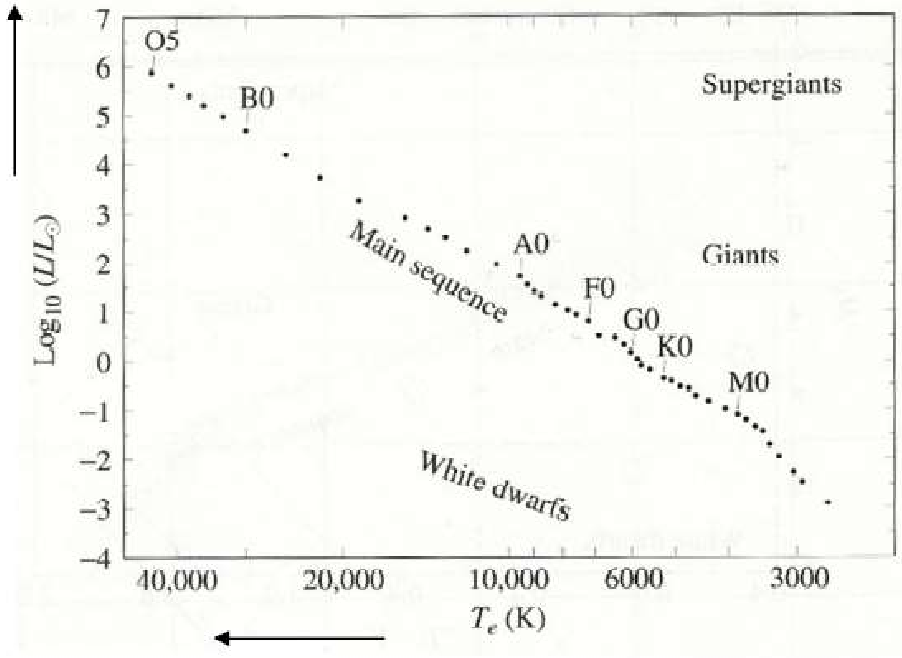
Color index
(Spectral type)

Fig 8.11 An observer's H-R diagram
※ MS → Sun : G2 V
Vega : A0 V

Color-Magnitude Diagram (CMD)

(색등급도)

luminosity



Effective temperature

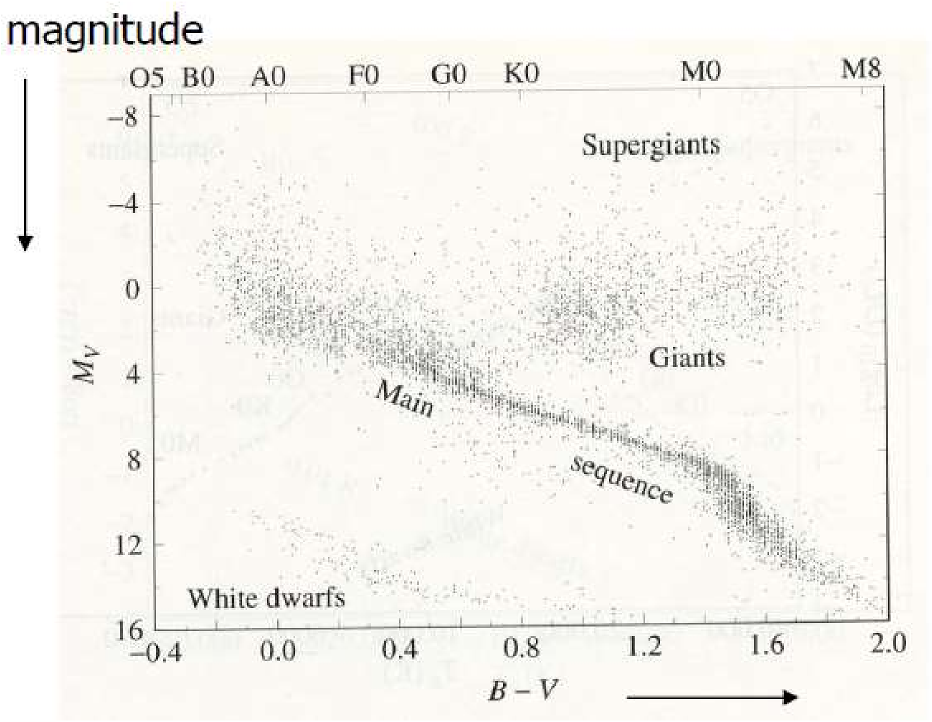
Fig 8.12 A theorist's H-R diagram
(log-log plot)

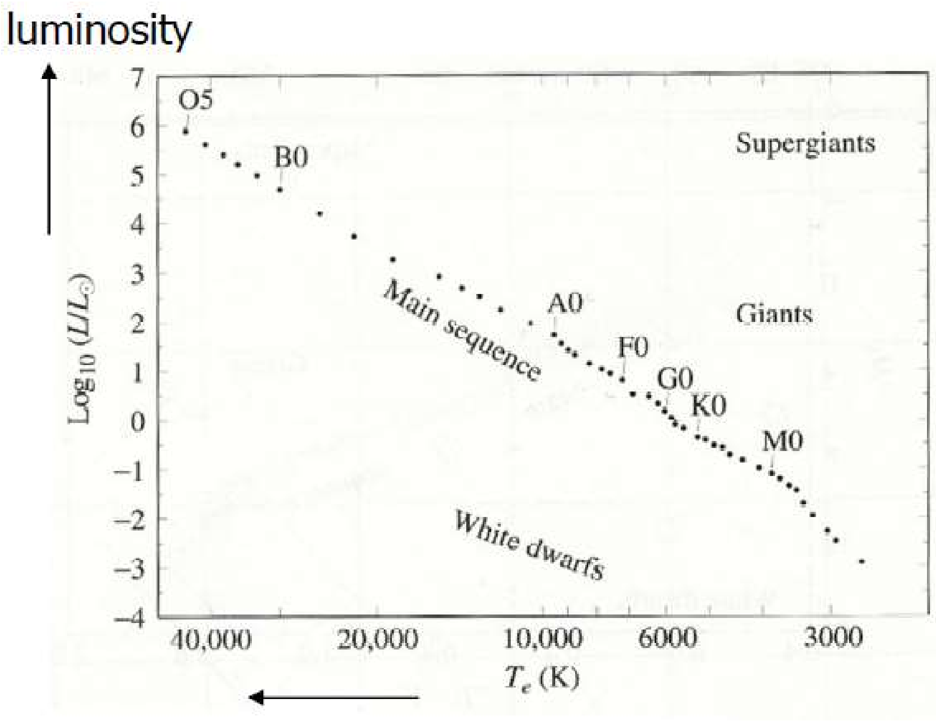
HR Diagram (HRD)

(HR도)

An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 243

Observer's vs Theoriest's H-R diagrams





Color index
(Spectral type)

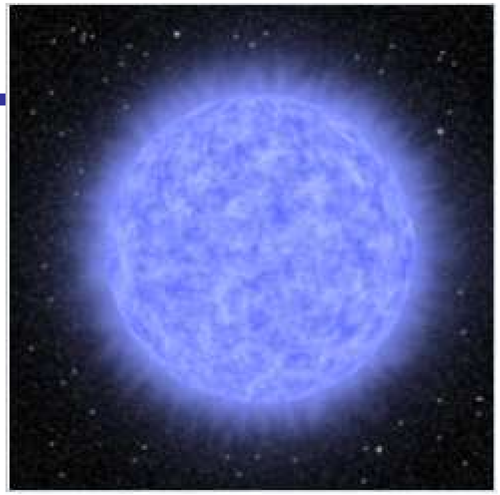
Effective temperature

MS width ← (1) changes in T, L in the MS
(2) Slight differences in the components of stars

MS luminosities : $5\times10^{-4}\,L_\odot$ to $1\times10^{6}\,L_\odot$
→ over 10 orders of mag

An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 243

Spectral types

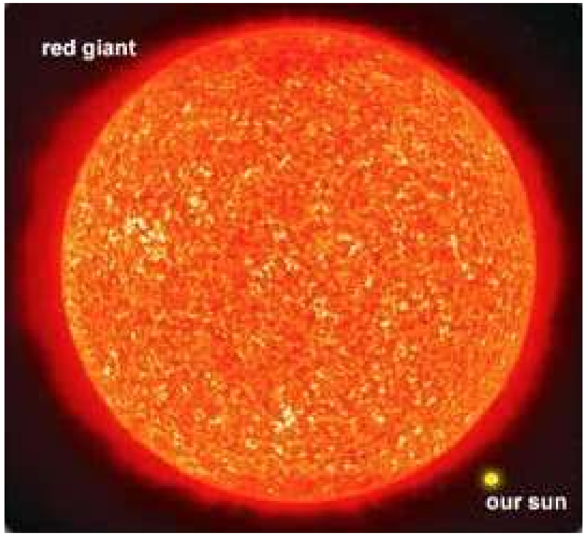


- O type : blue stars. Usually supergiants.
  Very luminous and hot. Rare.
  Strong helium absorption lines.

ζ Puppis (O4 I) – artist's rendering

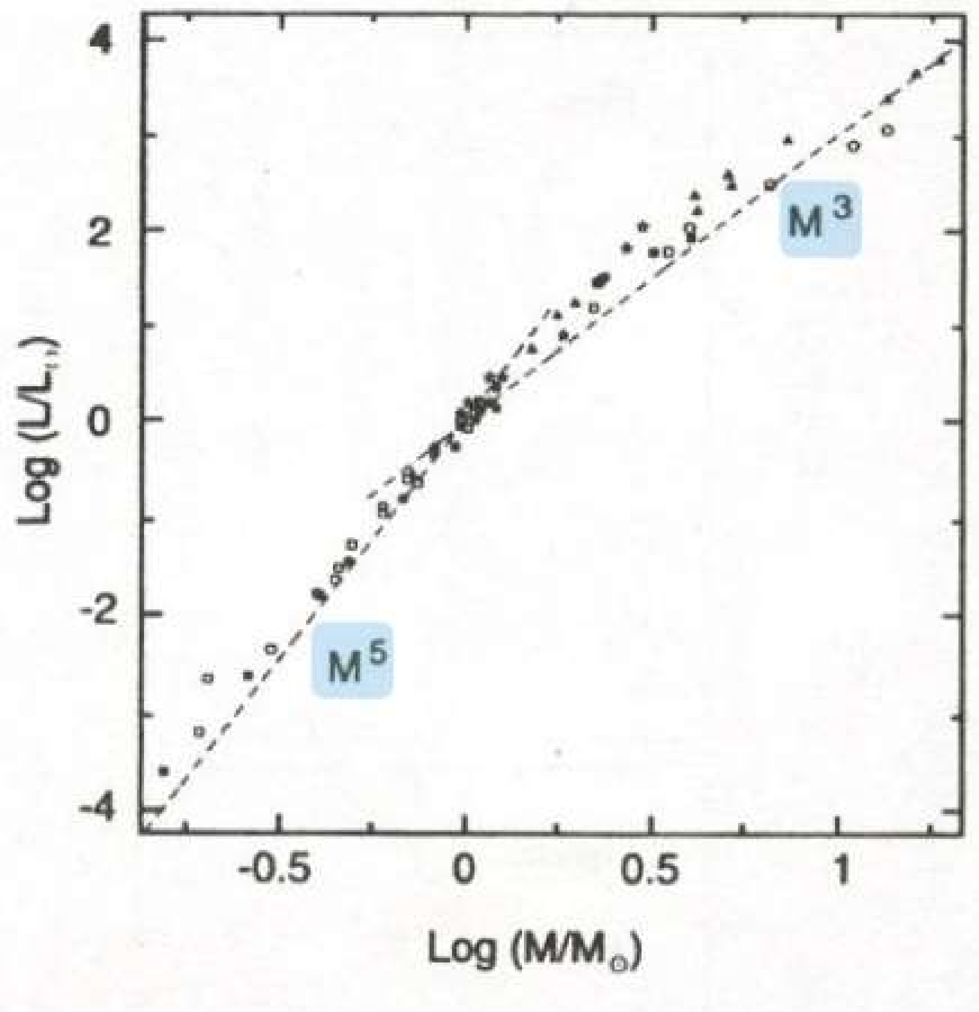
https://en.wikipedia.org/wiki/Zeta_Puppis

- B type : blue white stars. Mainly giants. Neutral He and H absorption lines.
- A type : white stars. Strong **H absorption lines**.
- F type : yellow white stars. Weak H and ionized Ca absorption lines.
- G type : yellow stars. Strong Ca absorption lines.
- K type : orange stars. Metallic absorption lines.
- M type : red stars. Strong metallic absorption lines.



https://archive.sssmediacentre.org/journals/Vol_05/01MAR07/04-SFI.htm

Stars → mass-luminosity relation



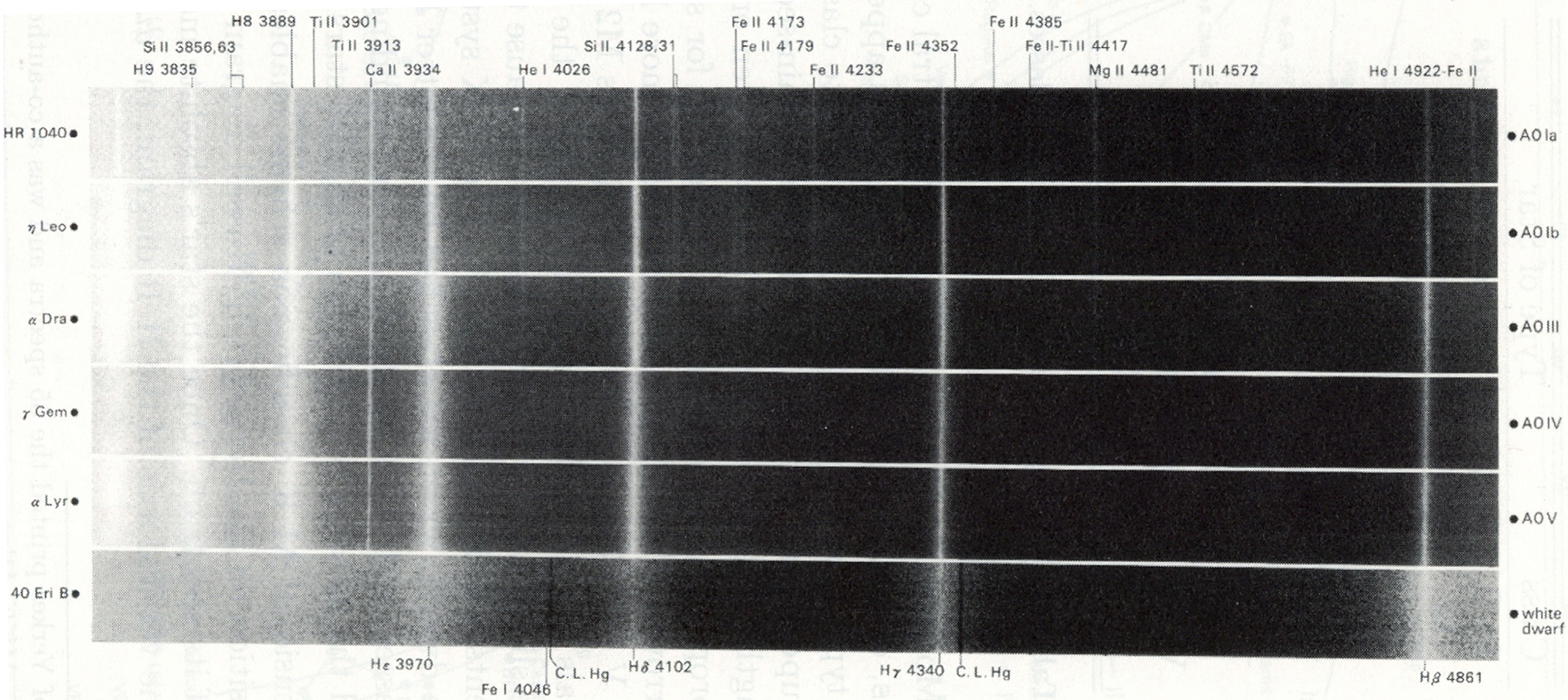
Power-law : $L \propto M^{\nu}$

$\nu = 3 - 5$

O stars : more luminous than M stars

→ O stars are more massive than M stars

‘A’ type stellar spectra – hydrogen Balmer lines



More luminous stars → narrower lines

Stefan-Boltzmann equation $L = 4\pi R^2 \sigma T^4$

σ : Stefan-Boltzmann constant

$\sigma = 5.67 \times 10^{-5} \mathrm{erg\ cm^{-2}\ sec^{-1}}\ K^{-4}$

$\sigma = 5.67 \times 10^{-8}\ \mathrm{W\ m^{-2}\ K^{-4}}$

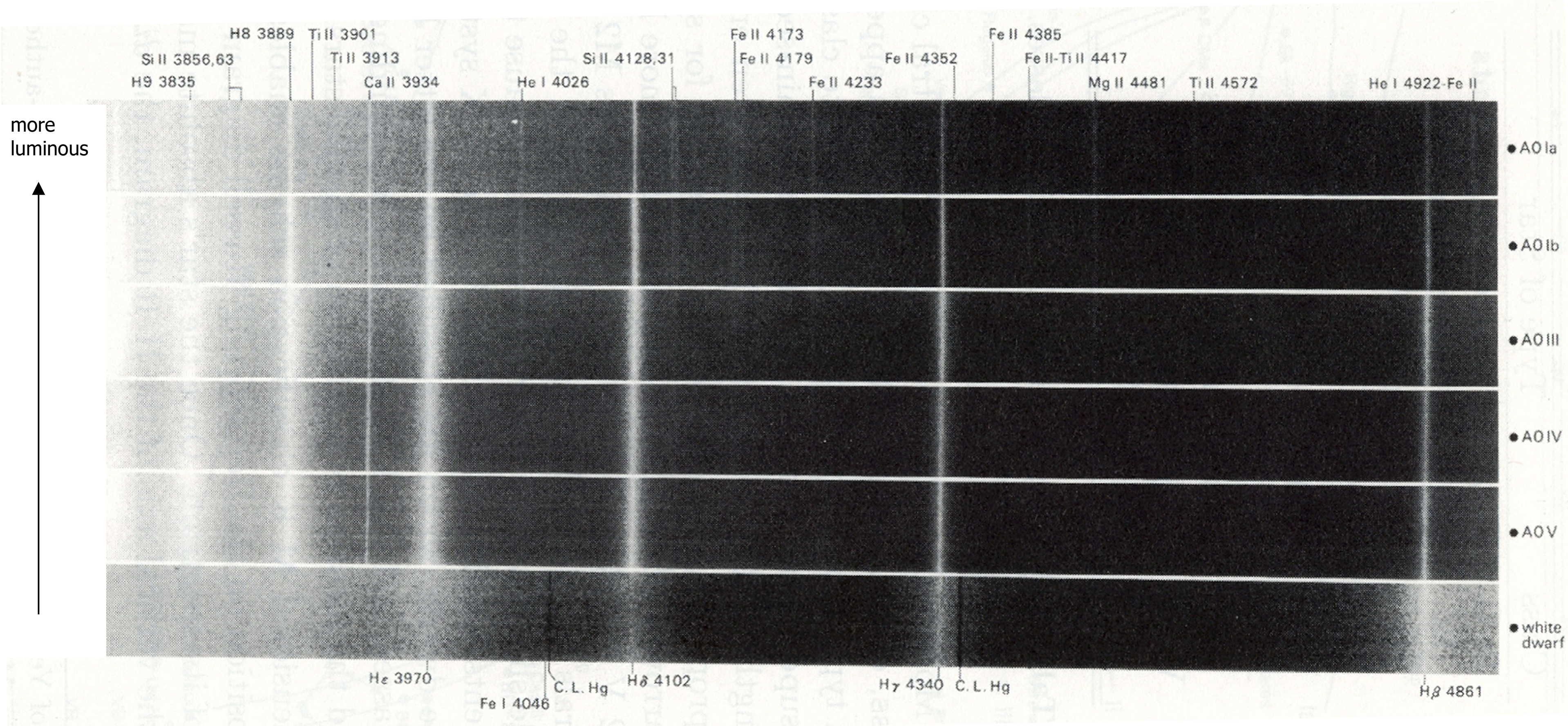
T : same

L ∝ R^2 → less dense → fewer collisions between atoms → less broadening

An Introduction to Modern Astrophysics (2nd edition),
Bradley W. Carroll & Dale A. Ostlie (1996), p. 247

'A' type stellar spectra – hydrogen Balmer lines

more luminous



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An Introduction to Modern Astrophysics (2nd edition),
Bradley W. Carroll & Dale A. Ostlie (1996), p. 247

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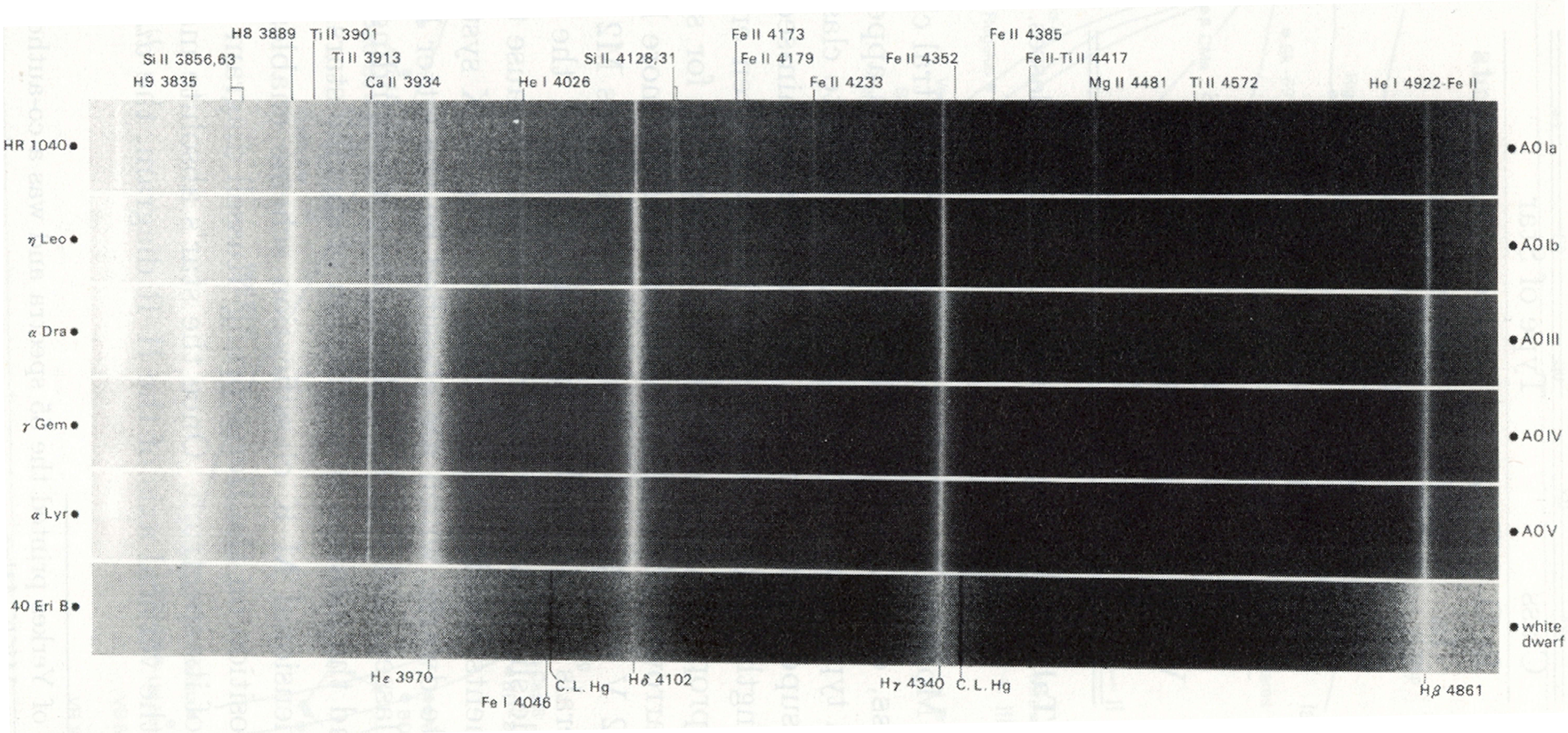


1943 Yerkes Observatory
William W. Morgan – Phillip C. Keenan - Edith Kellman
「An Atlas of Stellar Spectra」 (Chicago: Chicago University Press)

→ M-K (MKK) spectral classification system : two-dimensional spectral classification

An Introduction to Modern Astrophysics (2nd edition),
Bradley W. Carroll & Dale A. Ostlie (1996), p. 247

Morgan-Keenan Luminosity Classes

Class	Type of Star
Ia-O	Extreme, luminous supergiants (SGs)
Ia	Luminous SGs
Ib	Less luminous SGs
II	Bright giants
III	Normal giants
IV	Subgiants
V	Main-sequence (dwarf) stars
VI, sd	Subdwarfs
D	White dwarfs

- Same spectral type
- Same effective temperature
- Only luminosity differences ← subtle differences in the relative strengths of spectral lines

Morgan & Keenan (1973, ARA&A, 11, 29 – Spectral Classification)

An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 248

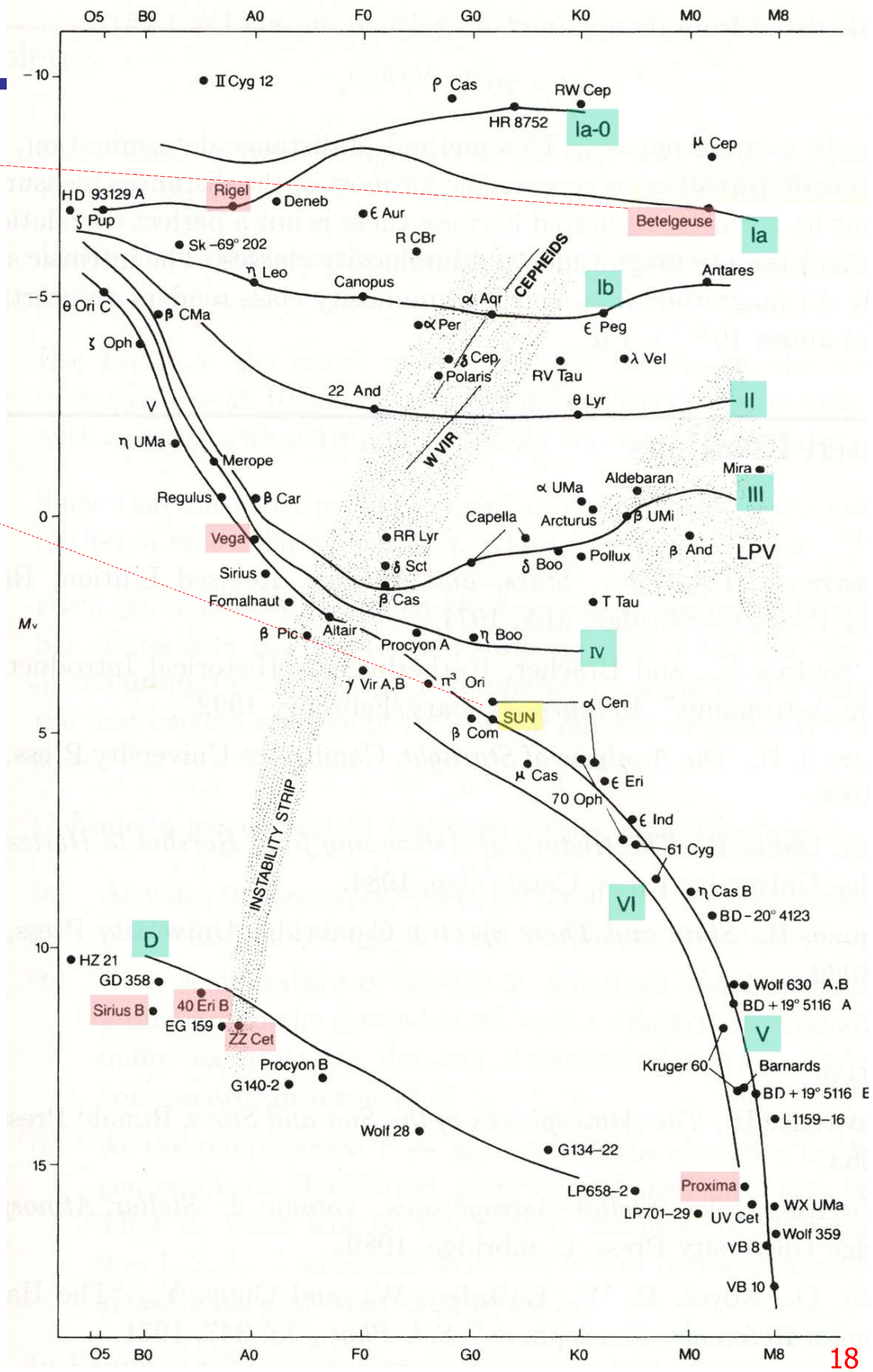
H-R diagram – luminosity classes

Betelgeuse (=α Orionis)
: M2 Ia (or M2 Iab) – pulsating variable

Sun : G2 V

- A star's position is fixed in H-R diagram

→ Vertical reading = absolute magnitude (M_V)
→ Distance can be calculated by
$(m-M)_0 = V - M_V - A_V = 5 \log d - 5$
"spectroscopic parallax"



An Introduction to Modern Astrophysics (2nd edition),
Bradley W. Carroll & Dale A. Ostlie (1996), p. 249

Line of constant radius

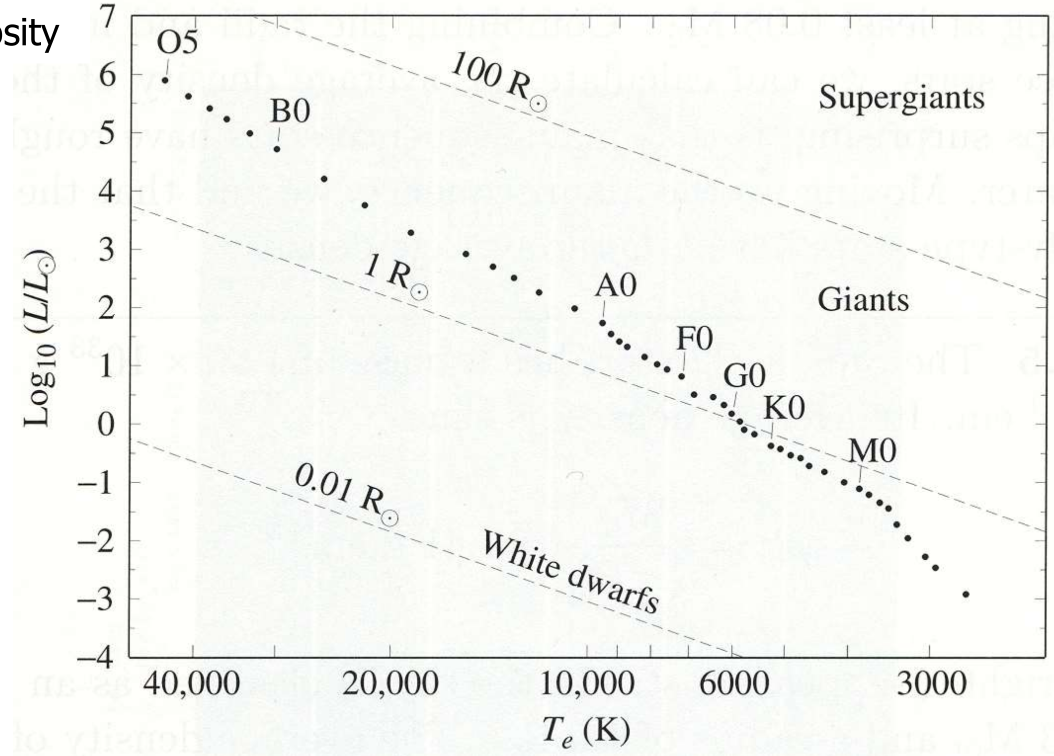
$$L = 4\pi R^2 \sigma T^4$$

100 × L
→ 10 × R larger

Giant stars : 10 – 800 $R_\odot$
(e.g. Aldebaran, α Tauri : 45 $R_\odot$)

Supergiant stars
(e.g. Betelgeuse, α Orionis – pulsating variable star : 700 – 1000 $R_\odot$, P = 2070 d)

luminosity



Effective temperature

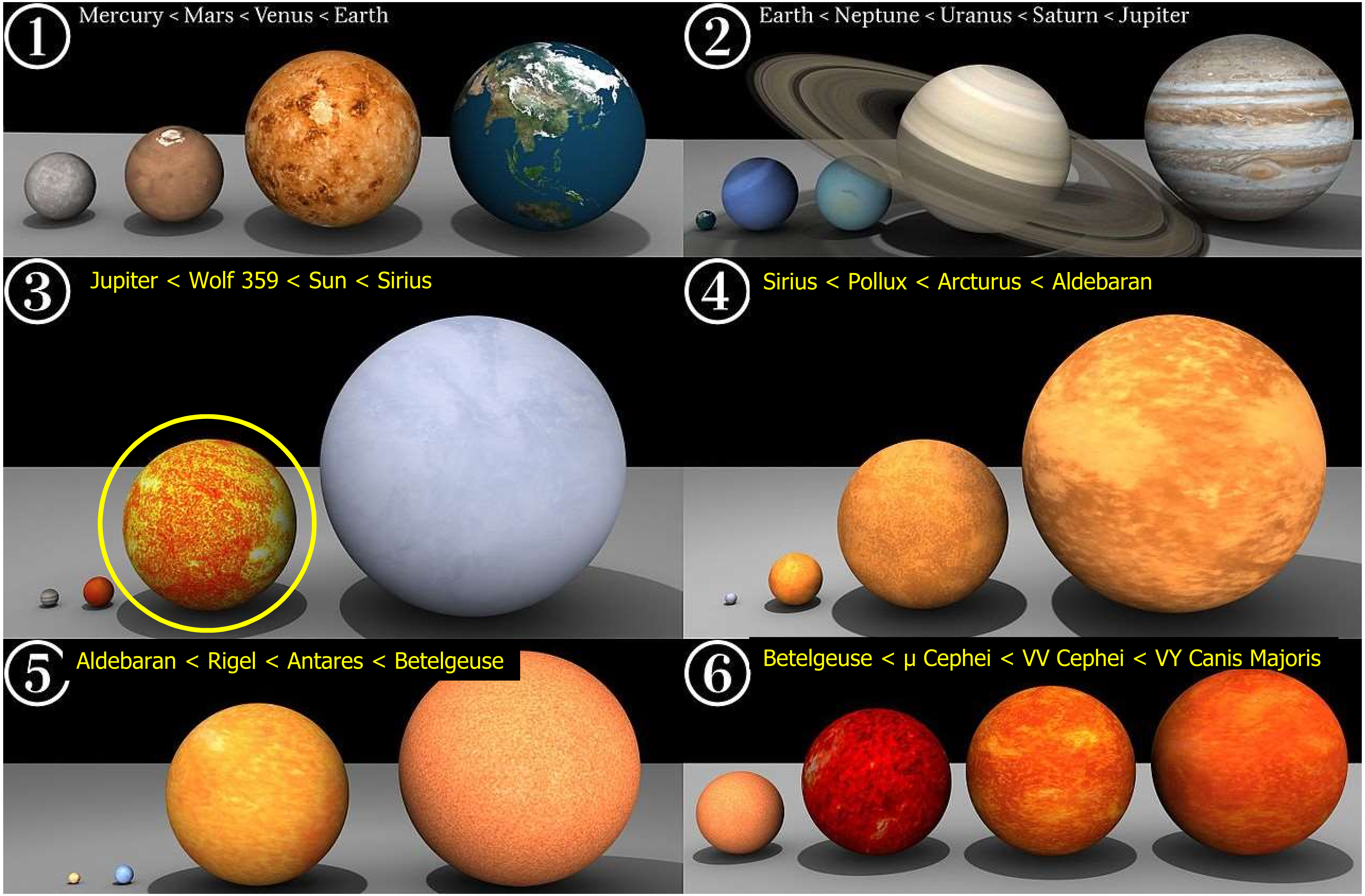
※ μ Cephei : 1260 $R_\odot$ = 5.9 AU
※ VY Canis Majoris : 1420 or 2069 $R_\odot$ = 6.6 or 9.7 AU

An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 245

※ 1000 $R_\odot$ = 4.7 AU
※ Jupiter, semi-major axis a = 5.2 AU
※ Saturn, semi-major axis a = 9.5 AU

https://www.space.com/22471-red-giant-stars.html

Sizes of stars



https://en.wikipedia.org/wiki/Betelgeuse#/media/File:Star-sizes.jpg

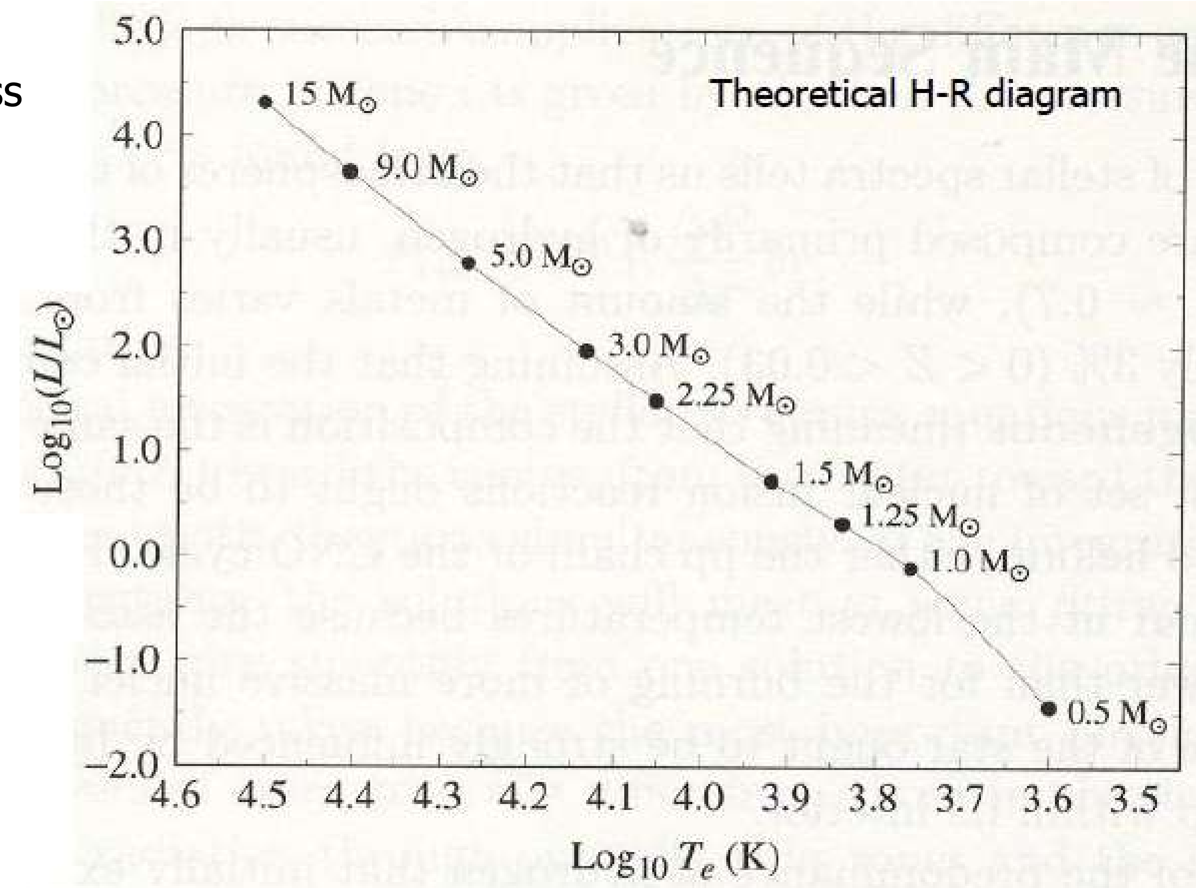
Vogt-Russell theorem

The **mass** and composition of a star
uniquely determine its radius, luminosity, and internal structure, as well as its subsequent evolution.

An Introduction to Modern Astrophysics (2nd edition),
Bradley W. Carroll & Dale A. Ostlie (1996), p. 368

Stellar masses from models

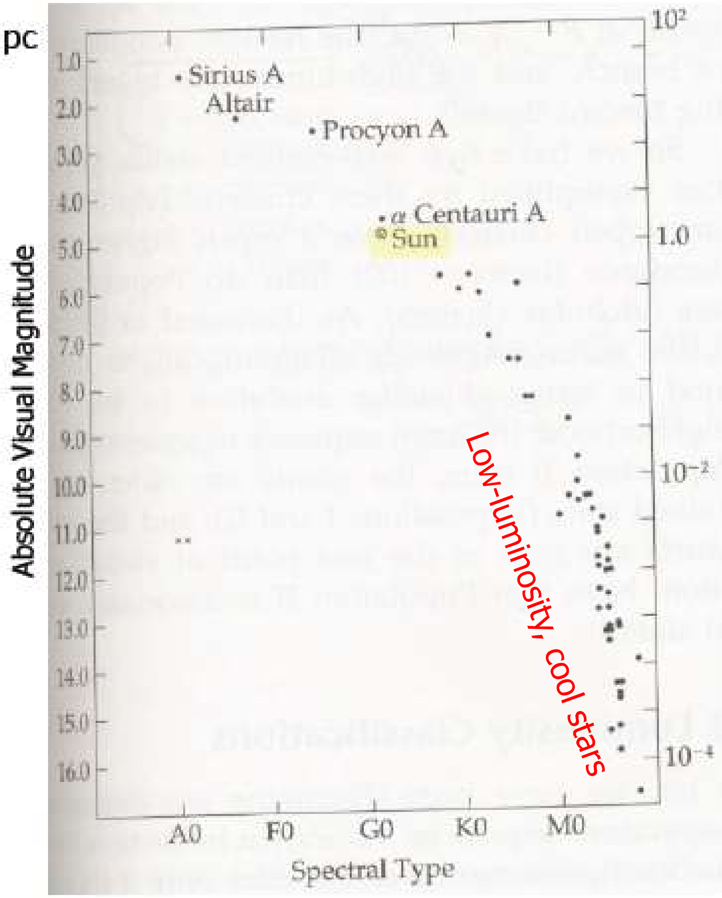
- Theoretical models for the mass range of core H-b
  → lie along the observational MS
- 100 – 0.08 $M_\odot$
  → Only 3 orders of mag
- At < 0.08 $M_\odot$
  → brown dwarfs (BDs)



An Introduction to Modern Astrophysics (2nd edition),
Bradley W. Carroll & Dale A. Ostlie (1996), p. 372

HR diagrams

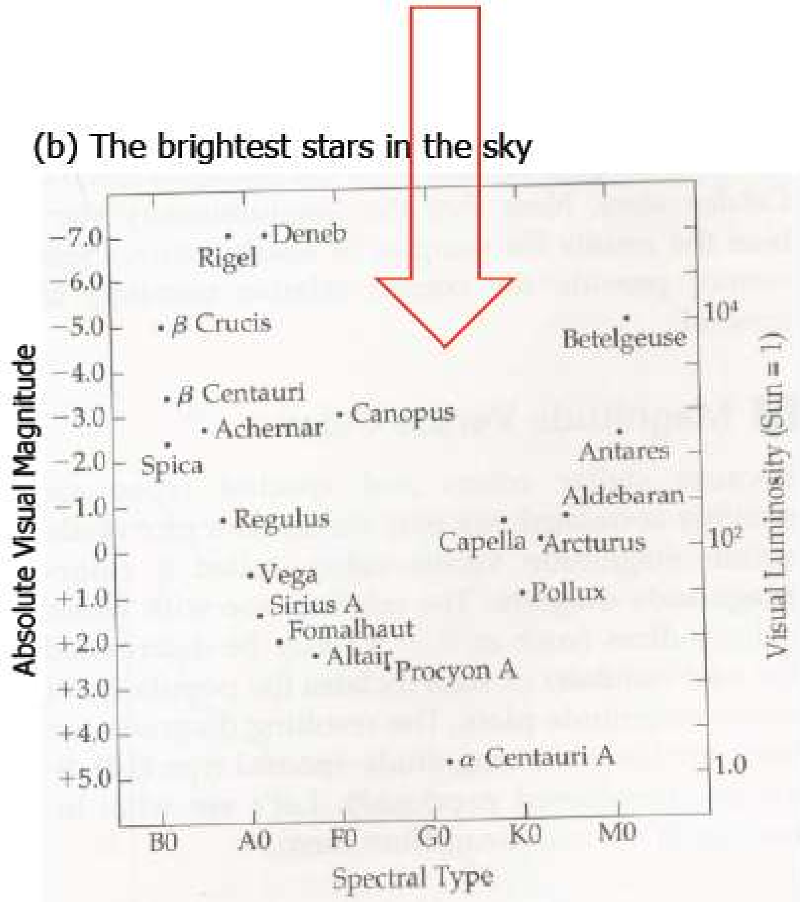
(a) Stars within 5 pc



- Well-defined MS + increasing number of stars toward later spectral types
- No stars earlier than A1

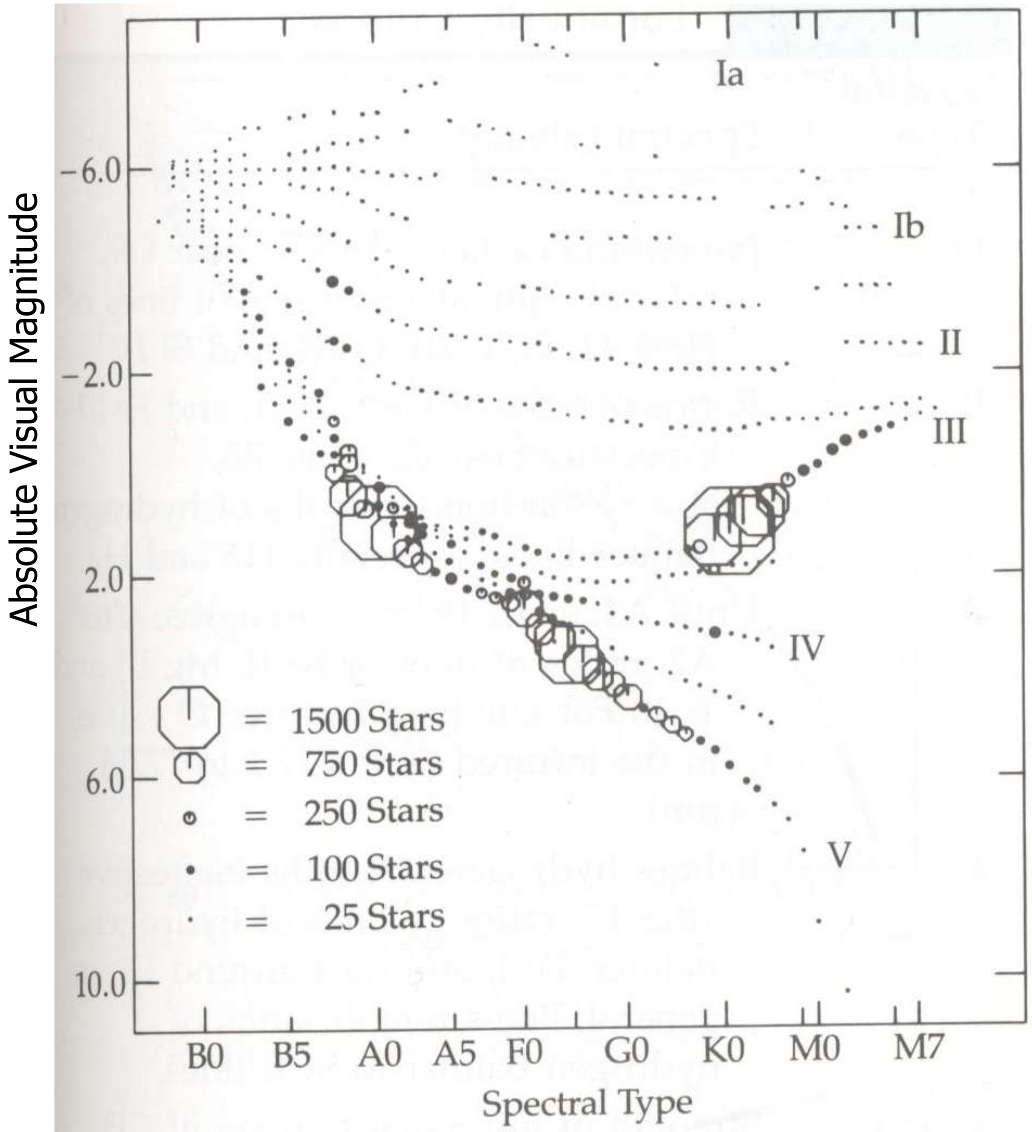
Hertzsprung Gap

(b) The brightest stars in the sky



- A significant number of giants and SGs
- Several early-type MS stars

HR diagrams



A sample of 36,000 stars

Size ~ number of stars of that spectral type

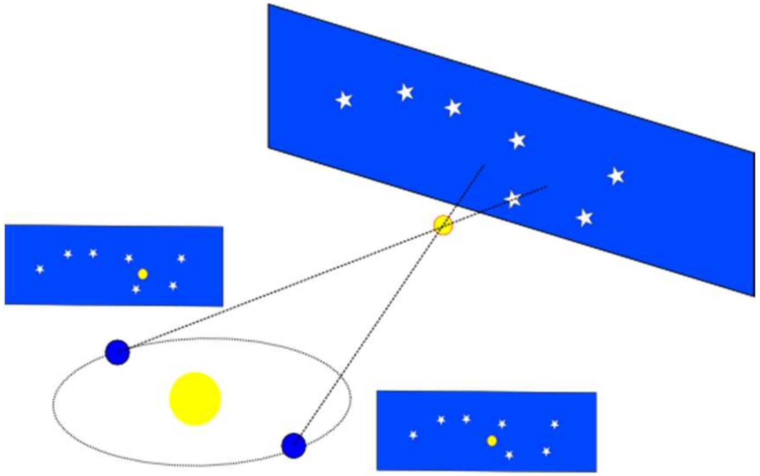
Introductory Astronomy and Astrophysics (4th edition)
Michael Zeilik & Stephen A. Gregory (1998), p. 261

1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)
1.2 Distances (거리)

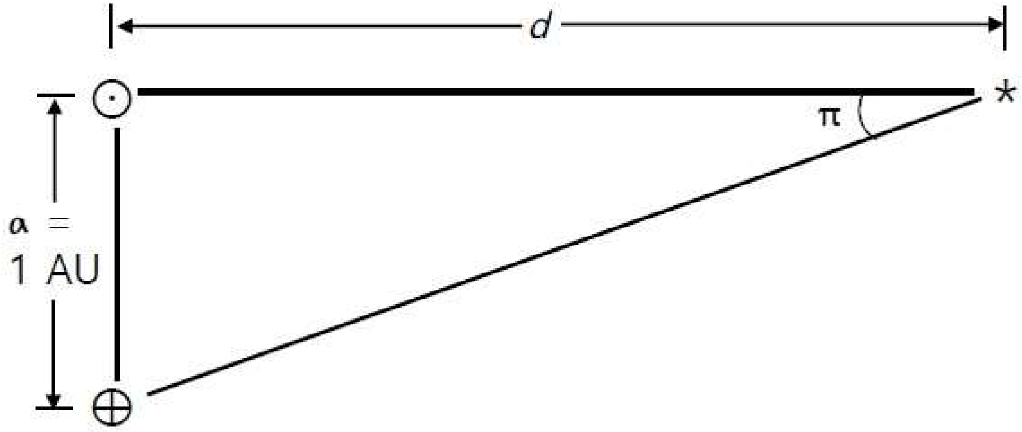
http://www.centauri-dreams.org/?p=11322
http://www.centauri-dreams.org/wp-content/uploads/2010/02/light-candles.jpg

1. Trigonometric parallax (삼각시차)

- First detection (1838) : Friedrich W. Bessel → 61 Cygni, d=10.4 ly
- In 1838, Friedrich G. W. von Struve → Vega (= α Lyr), d=25.0 ly



https://en.wikipedia.org/wiki/Parallax



$$\pi(\mathrm{rad}) = a/d$$

- 2π (rad) = 360° → 1 rad = 57° 17′ 44.81″ = 206265″

$$\boxed{\pi'' = \frac{1}{d}}$$ (π in arcsec, d in parsec [파섹])

1 pc = 3.086×10^{18} cm = 3.26 lightyears (광년)

- Largest parallax : Alpha Centauri (d=1.3 pc) → π =0.76″
- Ground-based observations → error ~ $\pm$0.004″

  → accurate only to π =0.001″ (d ~ 100 pc)

→ Satellites : Hipparcos (1989-1993), Gaia (2013 Dec 19-)

Spectroscopic parallax – using spectral type

- A star's spectrum → determine spectral type and luminosity class

- A star's position is fixed in H-R diagram

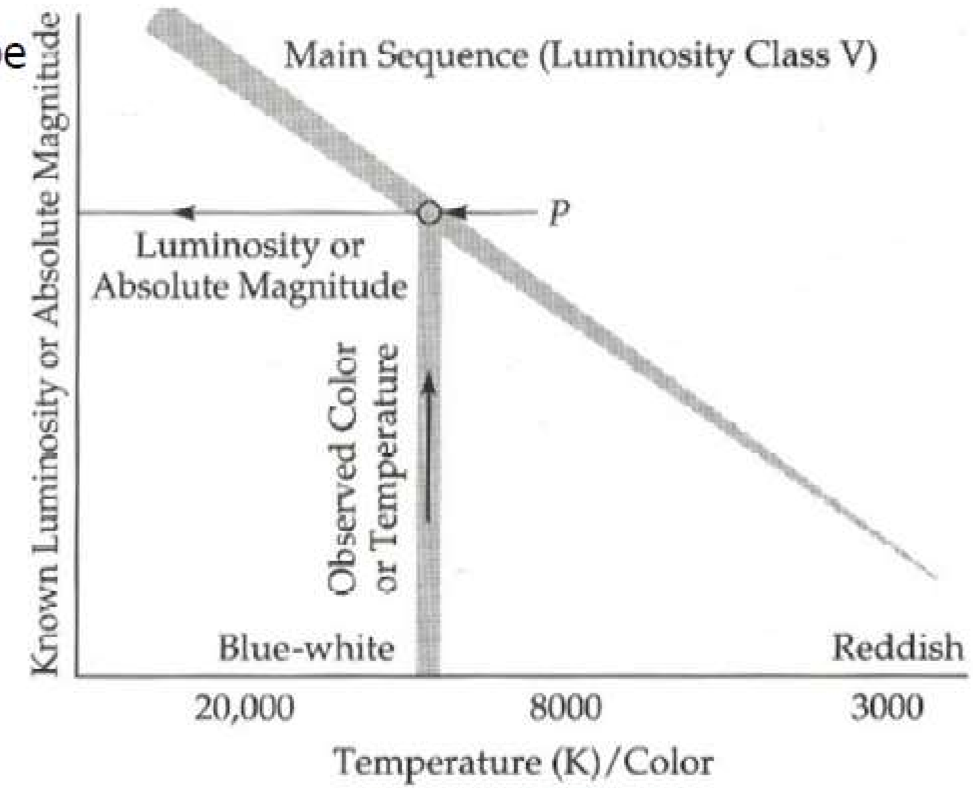
→(Vertical) reading of absolute mag (M_V)

→Distance can be calculated by

$(m-M)_0 = V - M_V - A_V = 5 \log d - 5$

"spectroscopic parallax"

- Observational errors, scatter in the HR diagram → mag uncertainty : ±1.0 mag (distance error : 50%)



A calibrated H-R diagram

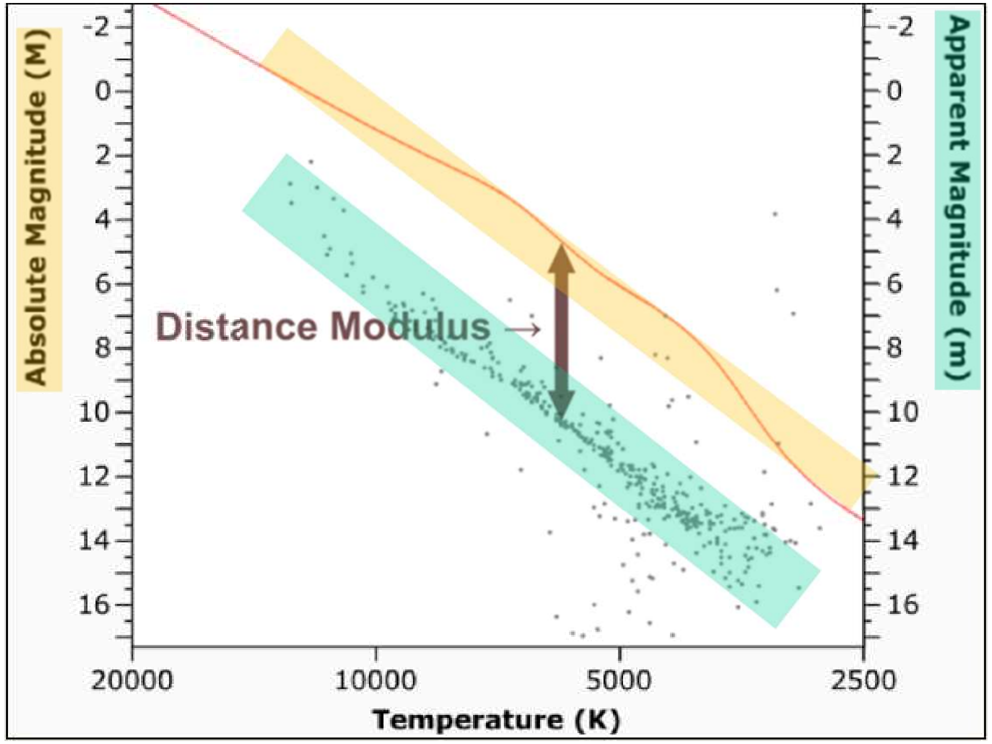
Introductory Astronomy and Astrophysics (4th edition)
Michael Zeilik & Stephen A. Gregory (1998), p. 266

Spectroscopic parallax – using spectral type

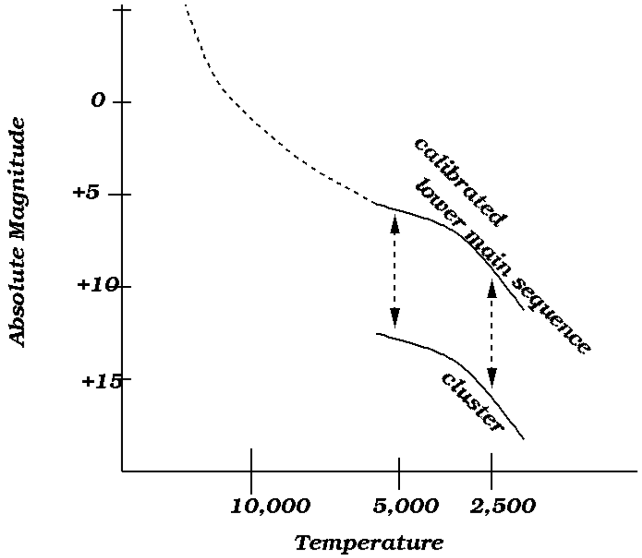
- For observational data of an entire star cluster : color – apparent magnitude
  → shift up and down (in magnitude)

- (test cluster apparent mag) – (calibrated absolute mag) = (m-M)
  → distance modulus
  → same for every star in the cluster

- Better accuracy than the spectroscopic parallaxes → mag uncertainty : ±0.2 mag



https://astro.unl.edu/naap/distance/cluster_fitting.html



https://ned.ipac.caltech.edu/level5/Bothun2/Bothun2_3_2.html

Main-sequence fitting

Spectroscopic parallax – using spectral type

- For observational data of an entire star cluster : color – apparent magnitude
  → shift up and down (in magnitude)
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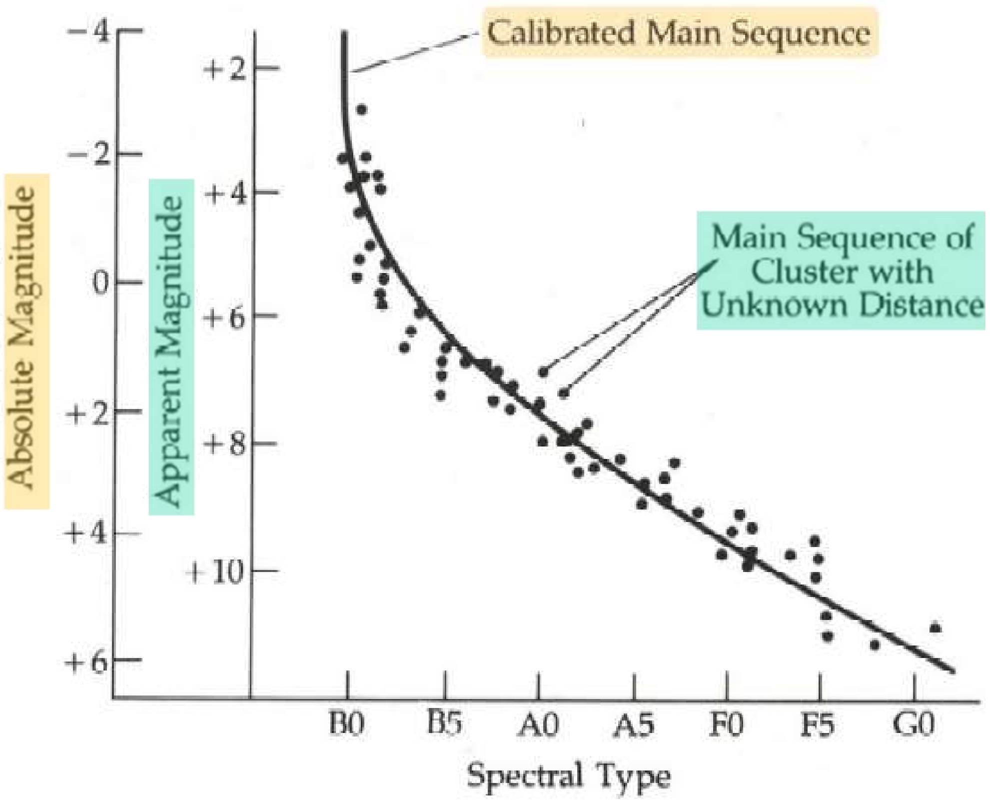
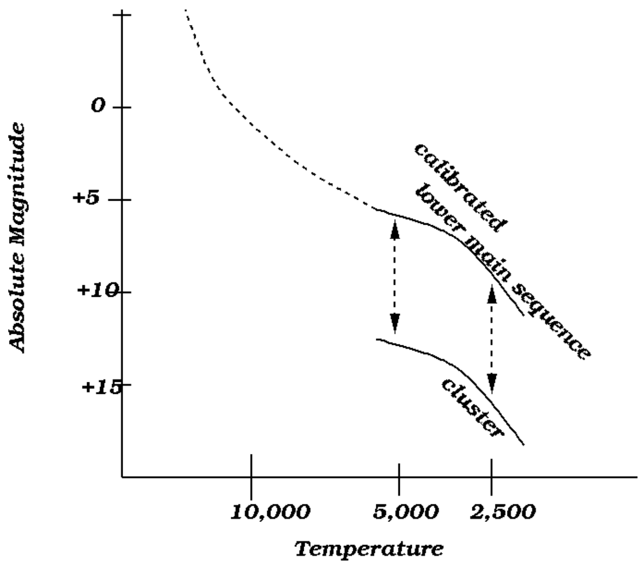


A calibrated H-R diagram

Introductory Astronomy and Astrophysics (4th edition)
Michael Zeilik & Stephen A. Gregory (1998), p. 266

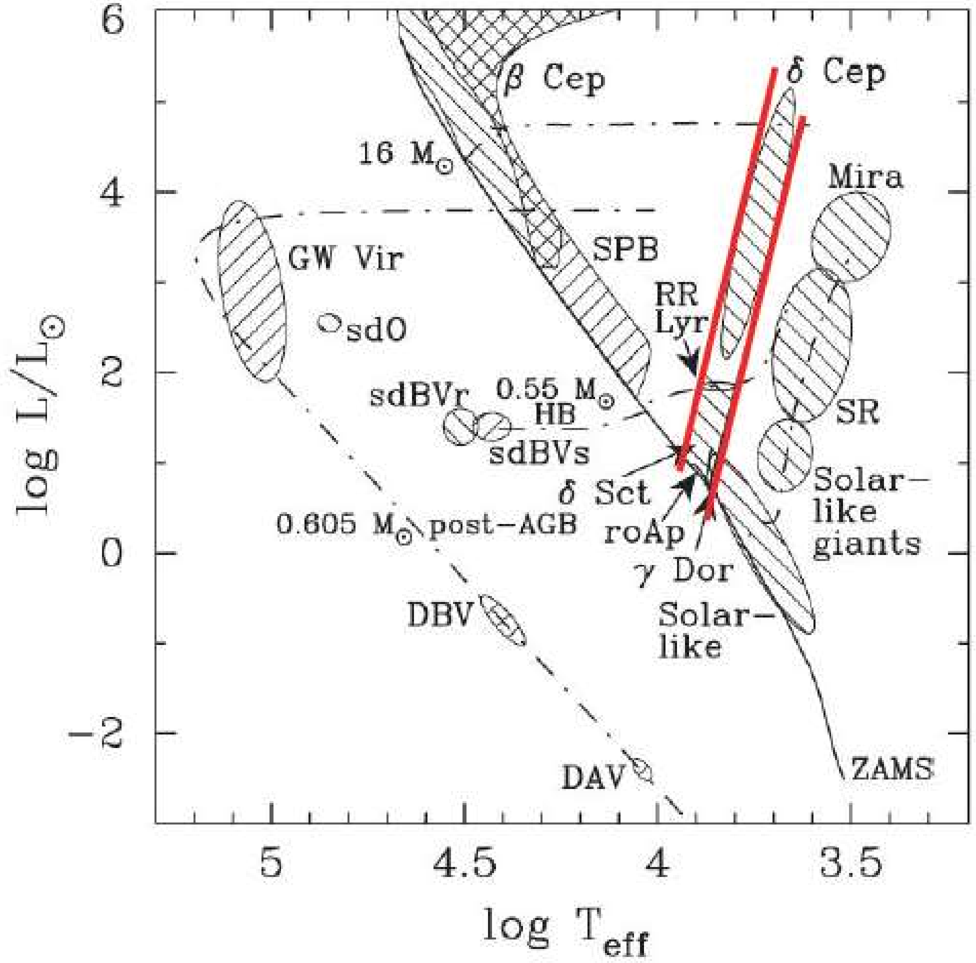


Main-sequence fitting

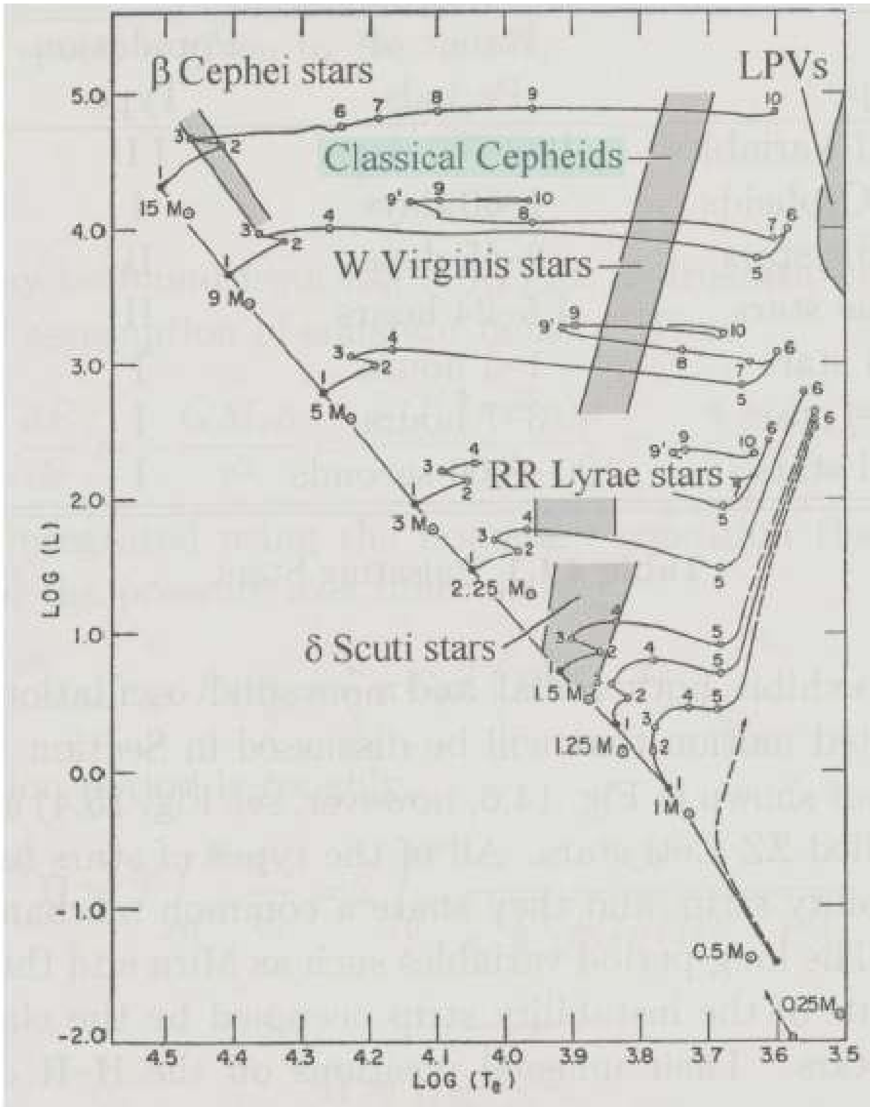
https://ned.ipac.caltech.edu/level5/Bothun2/Bothun2_3_2.html

2. Pulsating Variable Stars – Cepheids, RR Lyrae

Instability strip



Handler (2009, MNRAS, 398, 1339) Fig 1



An Introduction to Modern Astrophysics (2nd edition),
Bradley W. Carroll & Dale A. Ostlie (1996), p. 547

2. Pulsating Variable Stars – Cepheids, RR Lyrae

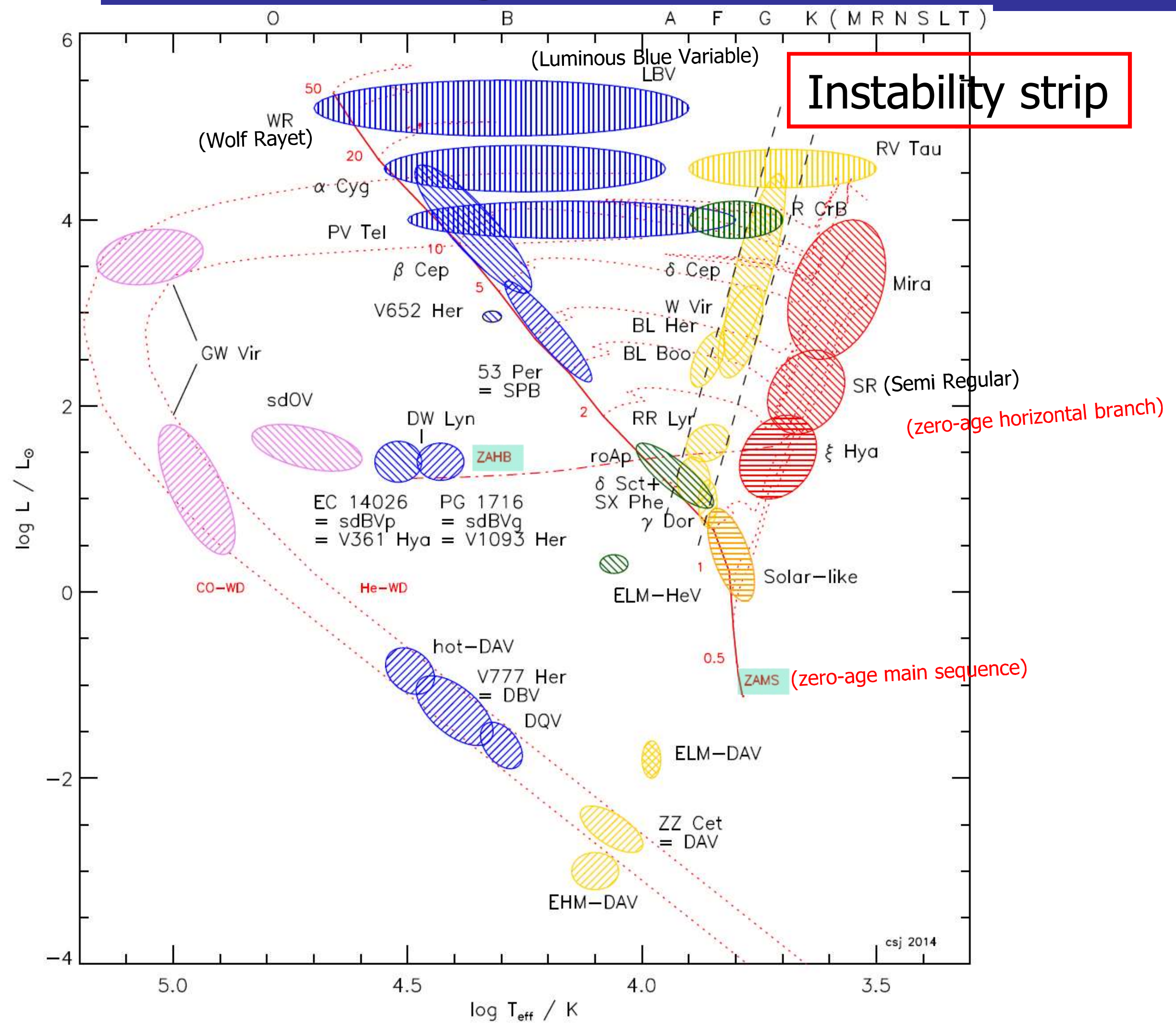
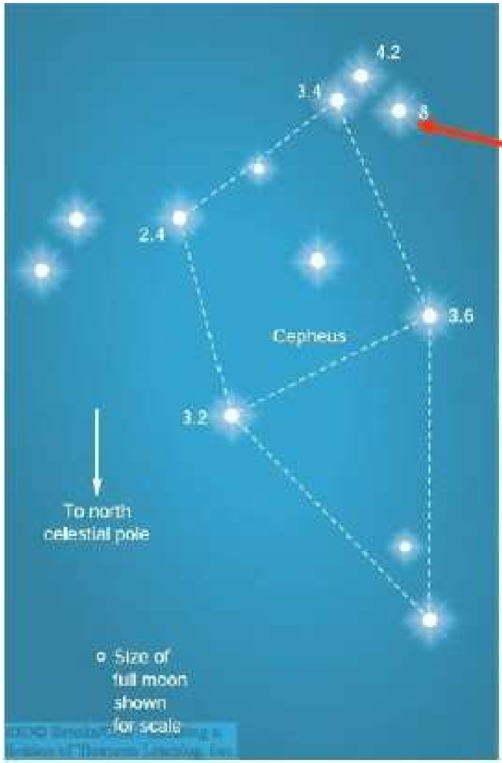
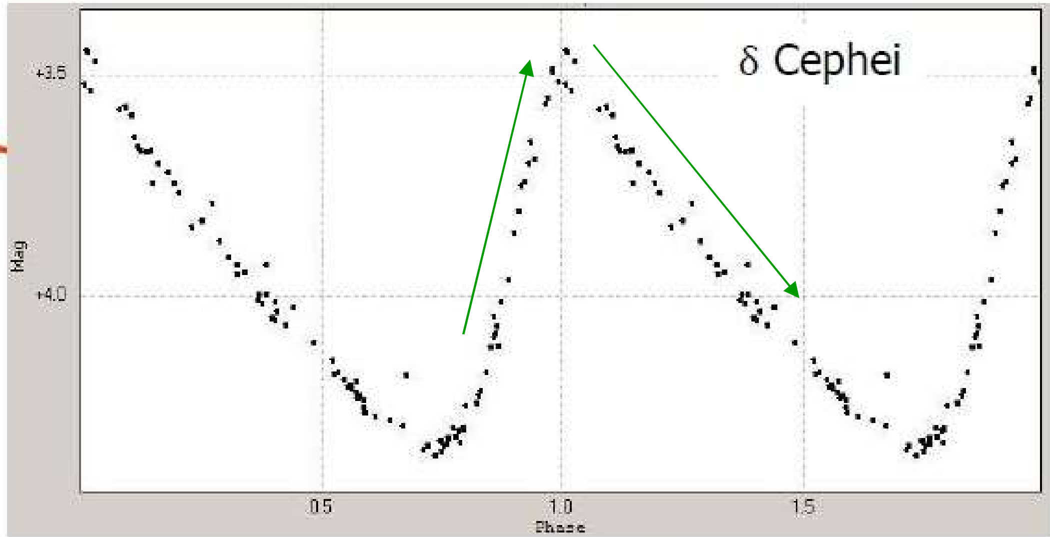


Figure 1. Luminosity-effective temperature (or H–R) diagram showing the approximate locations of major pulsating variables coloured roughly by spectral type, the zero-age main sequence and horizontal branch, the Cepheid instability strip, and evolution tracks for model stars of various masses, indicated by small numbers ($M_\odot$). Shadings represent opacity-driven p modes (\\\), g modes (///) and strange modes (|||) and acoustically driven modes (≡). Approximate spectral types are indicated on the top axis. Based on figures by Christensen-Dalsgaard and subsequently by Jeffery (2008a).

Jeffery & Saio 2016 (MN 458 1352)

Cepheid Variables – Light Curves (LCs)





3.48 mag

4.37 mag

P= 5.366341 d (http://earthsky.org/brightest-stars/delta-cephei-the-kings-famous-variable-star)

= δ Cepheids
= Classical Cepheids

$M_i \geq 5\ M_\odot$
(young stars)
(in spiral arms)
Age ≤ 0.1 Gyr

Galactic Astronomy (J. Binney & M. Merrifield, 1998) p. 291

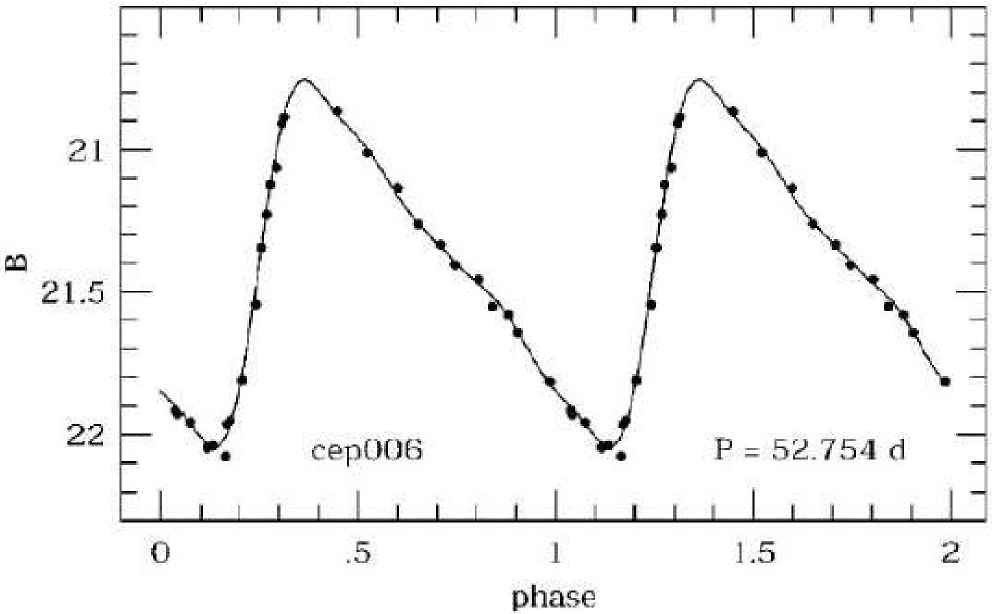
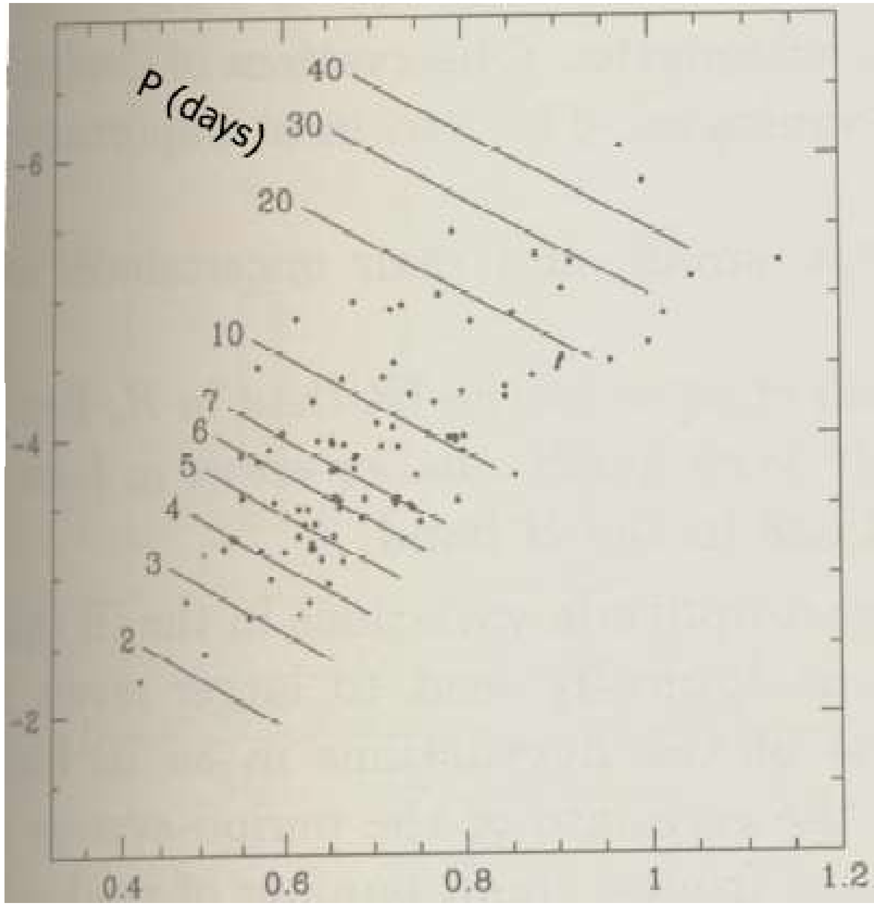


Figure 1: B light-curve of a typical Cepheid in NGC 300. The data were obtained with the ESO-MPA 2.2-m telescope and Wide Field Imager.

Gieren+01 (Messenger, 106, 15)

Cepheid Variables

Instability strip (불안정띠)



M_V

$(B\text{-}V)_0$

- Data : 98 Galactic Cepheids with well determined reddening (Fernie 1990 ApJ 354 295)
- Instability strip lines ← stellar evolution models (Chiosi+93 ApJS 86 541)

Galactic Astronomy (J. Binney & M. Merrifield, 1998) p. 291

Cepheid Variables

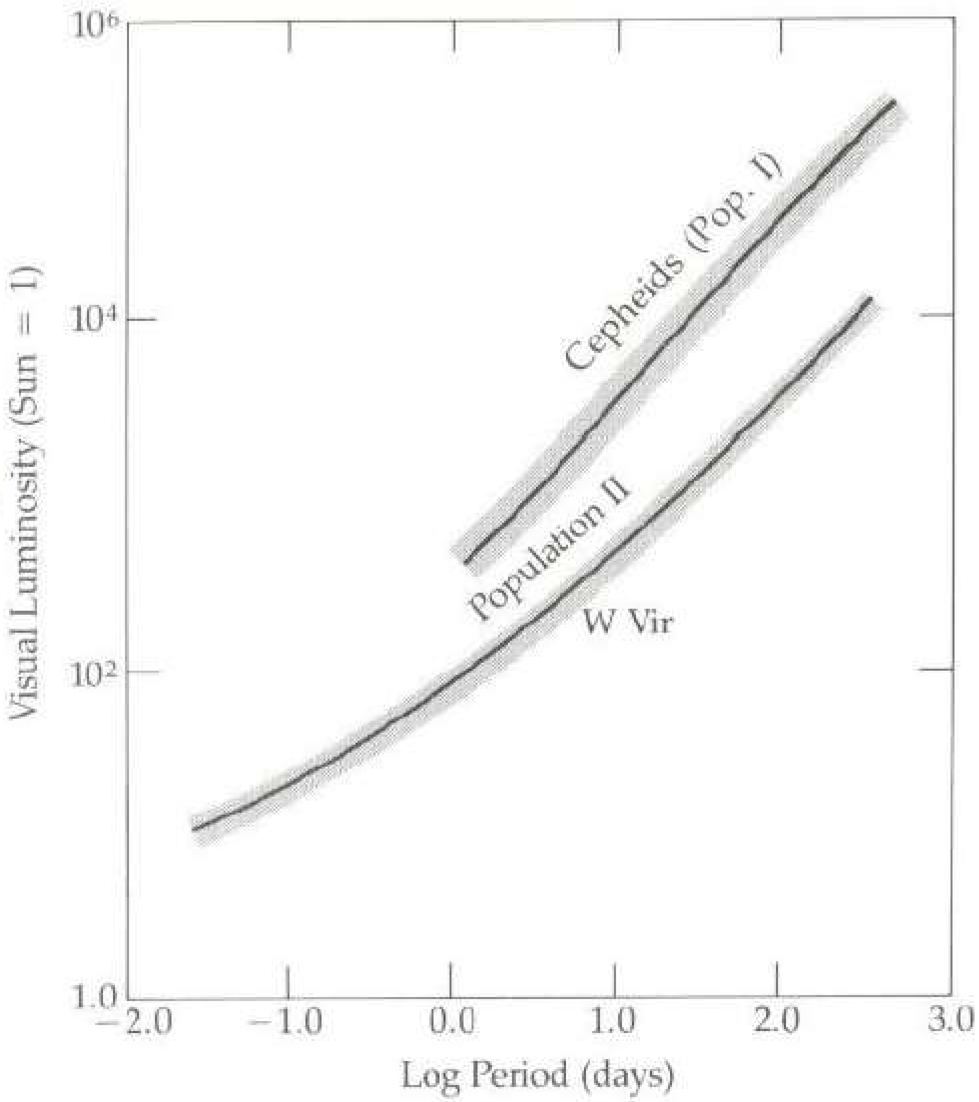
- Periodic (regular) variables
- Pulsation period ∝ median luminosity
- Period-Luminosity relation **(P-L relation)** : Leavitt's law
- Populations I, II - separate relations

- Classical Cepheids (pop I Cepheids) : more luminous, in spiral arms, P = 1 – 50 d (5-10 d), F6 to K2

$$\langle M_V \rangle = -(2.76 \pm 0.11)\log(P/10\,\mathrm{d}) - 4.16 \pm 0.05$$
$$(\text{scatter} \sim 0.27\ \text{mag})$$

Galactic Astronomy (J. Binney & M. Merrifield, 1998, p. 292)

- W Virginis Stars (pop II Cepheids) : 4-times less luminous than classical Cepheids, in globular clusters and other population II systems, P = 2 – 45 d (12-20 d), F2 to G6



Henrietta S. Leavitt (1912, Harvard College Obs. Circ., 173, 1 'Discovery of the Cepheid PL relation')

Introductory Astronomy and Astrophysics (4th edition)
Michael Zeilik & Stephen A. Gregory (1998), p. 356

Cepheid Variables

Henrietta S. Leavitt (1868 – 1921)

Radcliffe College

https://en.wikipedia.org/wiki/Henrietta_Swan_Leavitt

Computer(s)

Harvard College Observatory

https://en.wikipedia.org/wiki/Henrietta_Swan_Leavitt

3. RR Lyrae stars

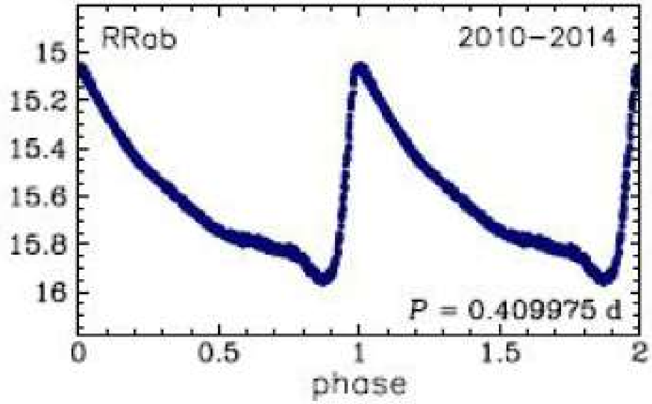
- Periodic variable stars
- P = 1.5 to 24 h (~12 h), Peak M_V ~ 0-1 mag, spectra A2 to F6
- Current mass ~ 0.8 $M_\odot$ (original MS mass ~ 1 $M_\odot$), old, relatively metal-poor
- In GCs and in low-metallicity systems (population II) – But, some have high metallicity

$$M_V(RR) = +0.71 \pm 0.12 \text{ at } \langle[\text{Fe/H}]\rangle = -1.61 \text{ for the halo (162 stars)}$$

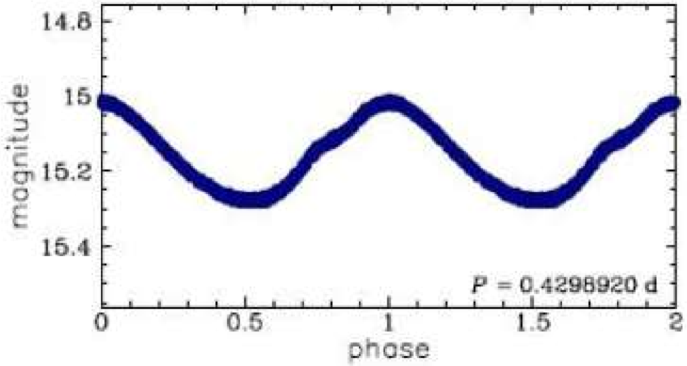
$$M_V(RR) = +0.79 \pm 0.30 \text{ at } \langle[\text{Fe/H}]\rangle = -0.76 \text{ for the thick disk (51 stars)}$$

Layden et al. (1996, AJ, 112, 2110)

RR_{ab}

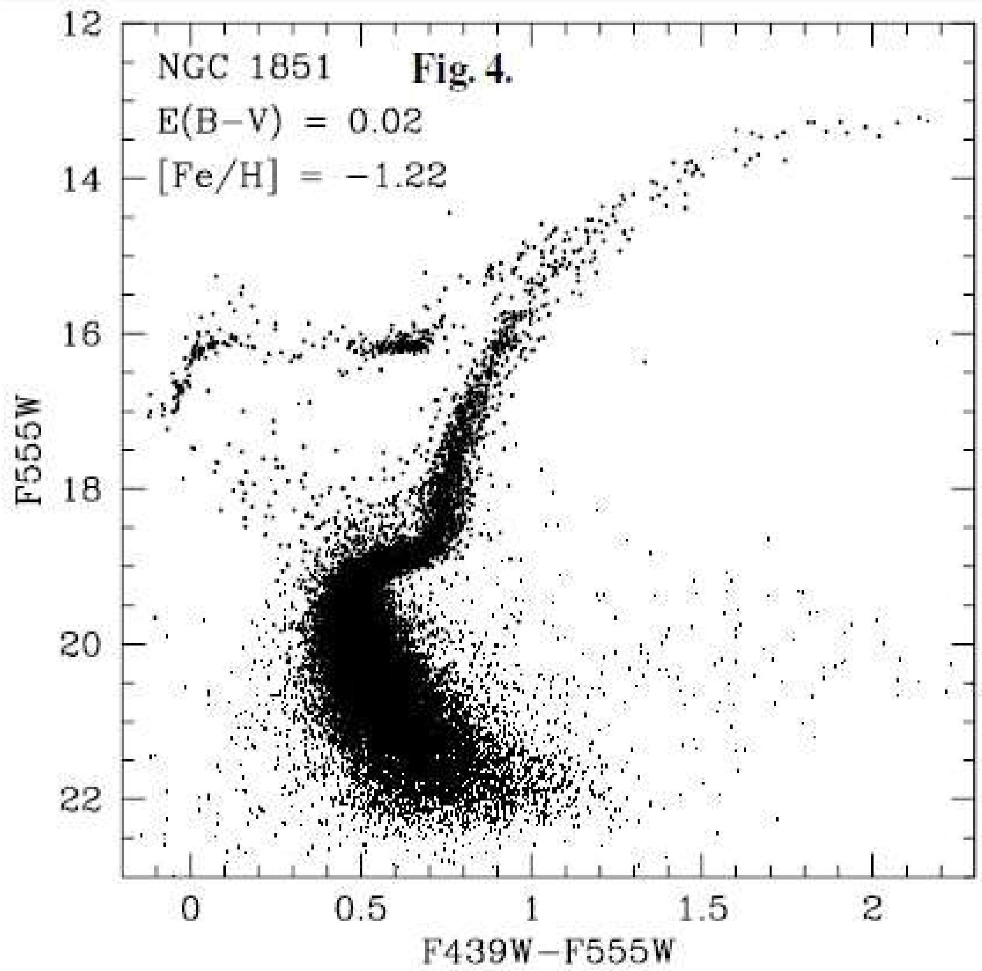


RR_c

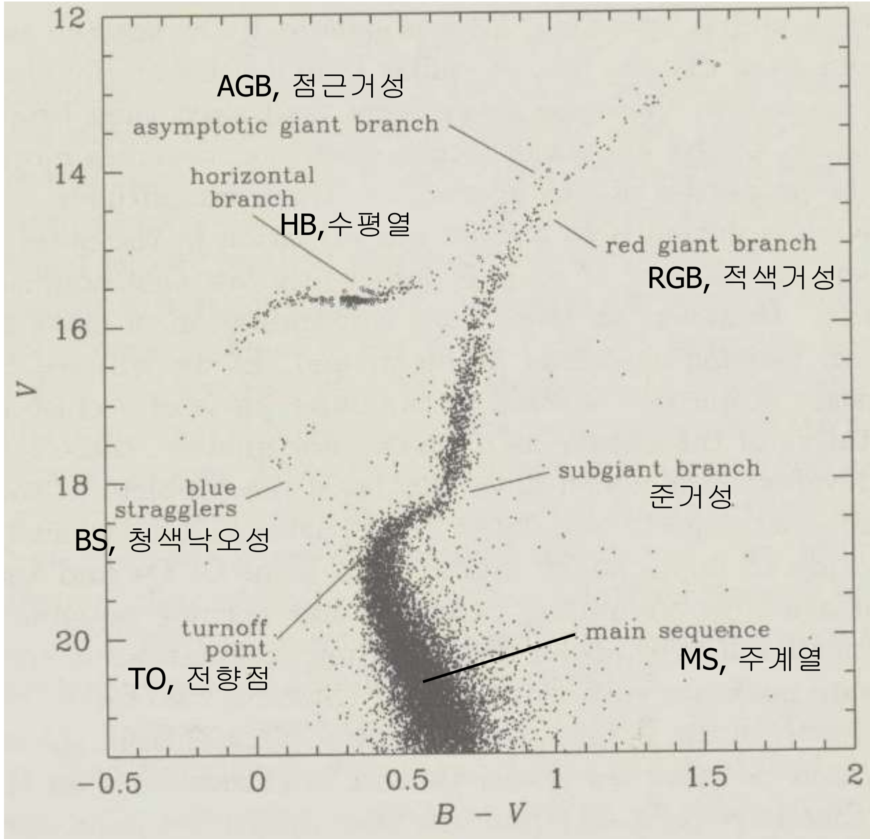


http://ogle.astrouw.edu.pl/atlas/RR_Lyr.html

Color-Magnitude Diagrams for globular clusters (GCs)



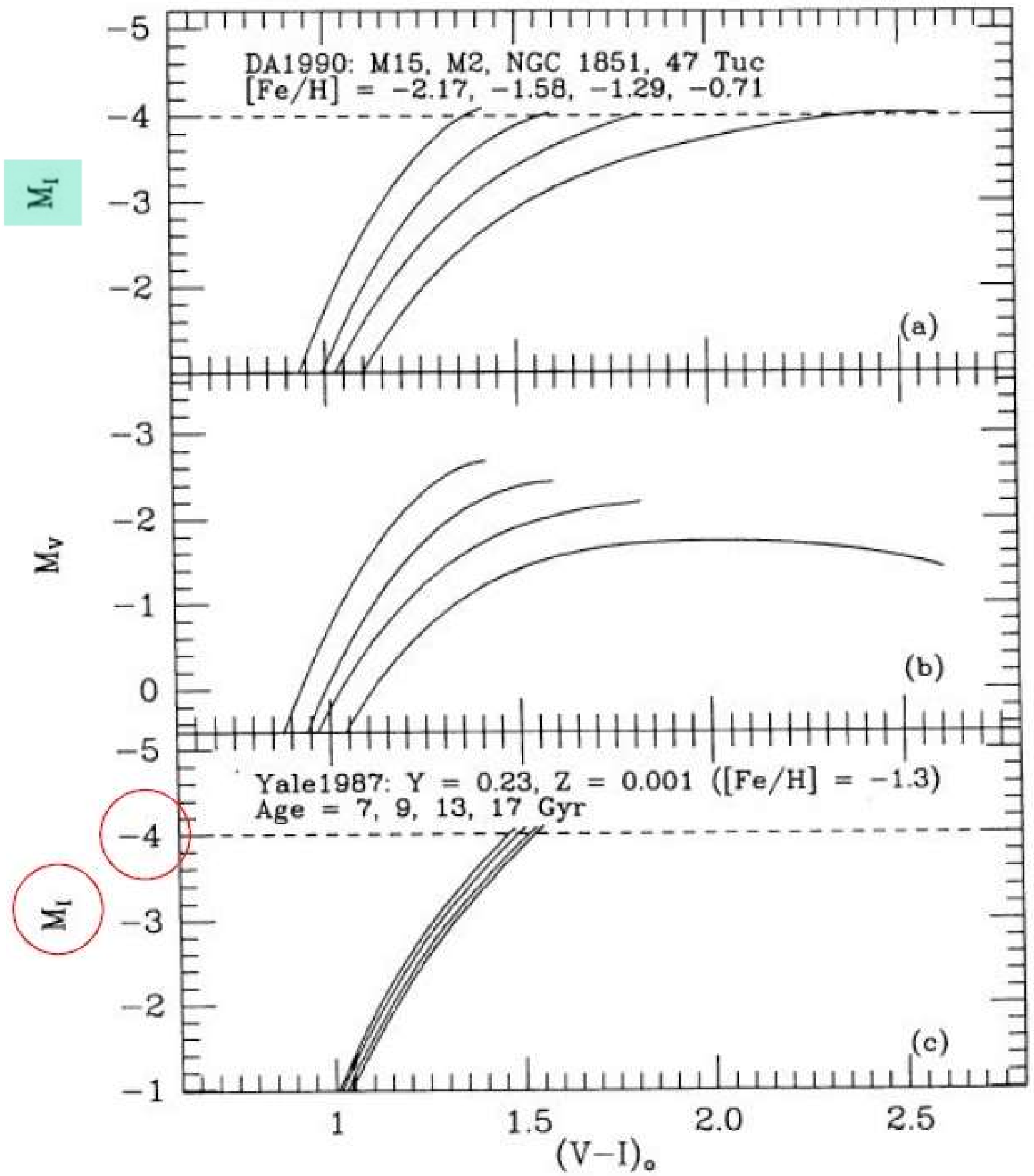
Piotto et al. (2002, A&A, 391, 945)



GC M3 (NGC 5272)
(variables=open circles)

Galactic Astronomy (J. Binney & M. Merrifield, 1998) p. 334

4. Tip of the red giant branch (TRGB)



Citations 660

Fig. 1

Lee et al. (1993, ApJ, 417, 553)
이명균

Tip of the red giant branch (TRGB)

TABLE 1

DISTANCE ESTIMATES FOR RESOLVED GALAXIES BASED ON PRIMARY DISTANCE INDICATORS

GALAXY (1)	TYPE[a] (2)	$E(B-V)$ (3)	$(m-M)_0$ Cepheid (4)	RR Lyrae (5)	I_{TRGB} (6)	I_{TRGB} (7)	REFERENCE[b] (8)	[Fe/H][c] (9)	M_B (10)	M_V (11)
LMC	SBmII	0.10	18.50	18.28	18.42	14.6	1, 2, 3	−1.2	−17.93	−18.36
NGC 6822	ImIV–V	0.28	23.62	...	23.46	20.05	4, 4	−1.8:	−15.13	−16.42
NGC 185	dE3pec	0.19	...	24.01	23.94	20.30	5, 6	−1.2	−14.63	−15.52
NGC 147	dE5	0.17	...	24.06	24.13	20.4	7, 8	−0.9	−14.39	−15.17
IC 1613	IMV	0.02	24.42	24.27	24.27	20.25	1, 9, 10	−1.3	−14.51	−15.16
M31	SbI–II	0.08	24.44	24.36	24.44	20.55	1, 11, 12	−0.8	−20.98	−21.74
M33	Sc(s)II–III	0.10	24.63	24.71	24.70	20.95	1, 13, 12	−2.0	−18.94	−19.40
WLM	ImIV–V	0.02	24.92	...	24.81	20.85	14, 14	−1.6:	−14.28	−14.62
NGC 205	S0/dE5pec	0.035	...	24.76	24.42	20.45	15, 16	−0.8	−15.80	−16.62
NGC 3109	SmIV	0.04	25.5	...	25.45	21.55	17, 18	−1.6	−15.95	−16.25

[a] From Sandage & Tammann 1987.

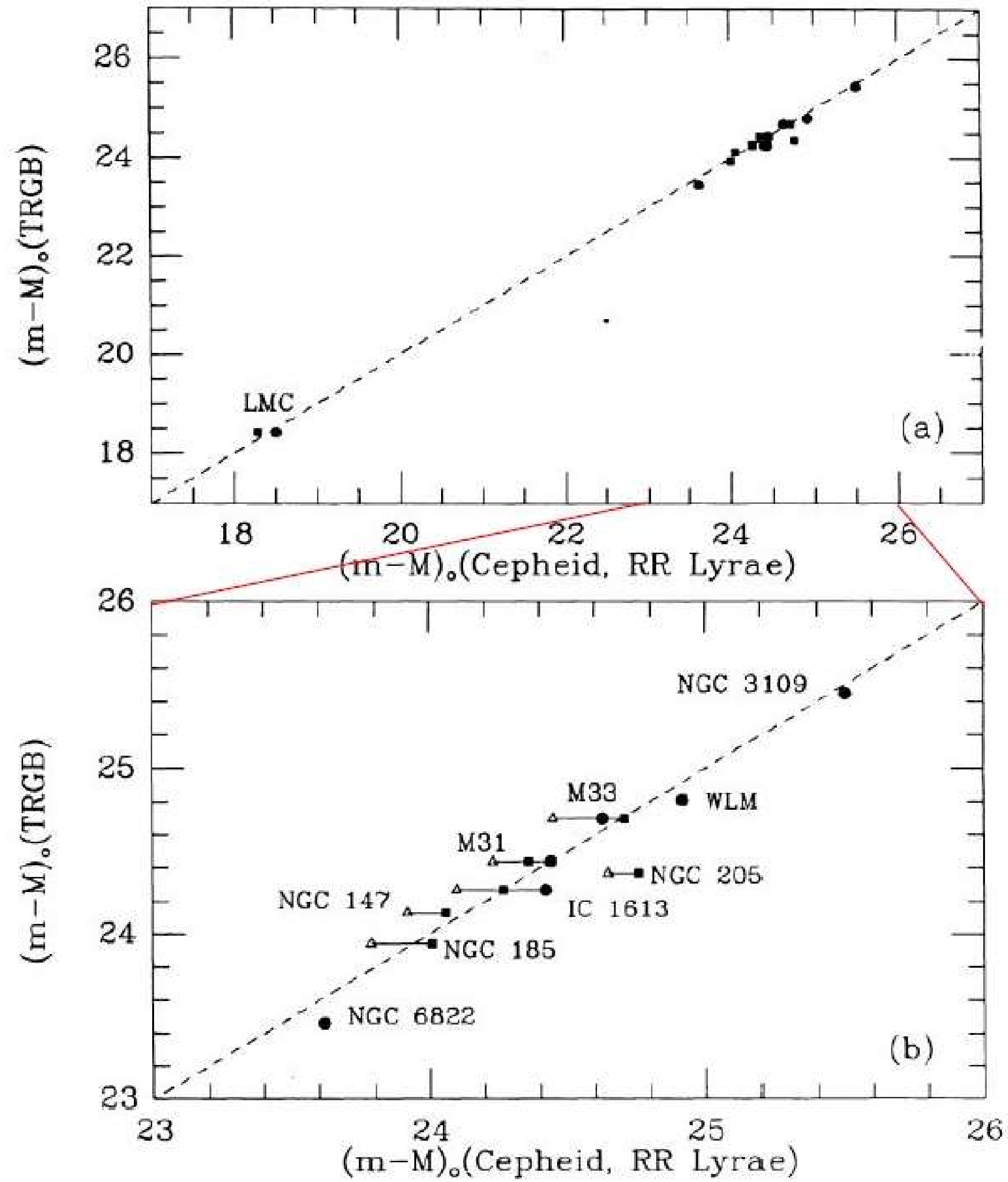
[b] References: (1) Madore & Freedman 1991, (2) Walker 1988, (3) Reid & Mould 1987, (4) Lee, Freedman, & Madore 1993, (5) Saha & Hoessel 1990, (6) Lee, Freedman, & Madore 1992, 1993c; (7) Saha, Hoessel, & Mossman 1990; (8) Mould, Kristian, & Da Costa 1983; (9) Saha et al. 1992; (10) Freedman 1988; (11) Pritchet & van den Bergh 1987, 1988; (12) Mould & Kristian 1986; (13) Pritchet 1988; (14) Lee, Freedman, & Madore 1993a; (15) Mould, Kristian, & Da Costa 1984; (16) Saha, Hoessel, & Krist 1991; (17) Capaccioli, Piotto, & Bresolin 1992; (18) Lee 1993.

[c] The metallicity [Fe/H] has been determined using the color $(V-I)_{-3.5}$.

$$-2.2 < [\mathrm{Fe/H}] < -0.7 \text{ dex}$$

Lee et al. (1993, ApJ, 417, 553)

Tip of the red giant branch (TRGB)



- Observations – repeat?
- Extinction
- Luminosity

Fig. 4 Lee et al. (1993, ApJ, 417, 553)

※ Mass fractions

Mass ratios (rather than numbers of particles)

Mass fractions of hydrogen : $X \equiv \frac{total\ mass\ of\ hydrogen}{total\ mass\ of\ gas}$

Mass fractions of helium : $Y \equiv \frac{total\ mass\ of\ helium}{total\ mass\ of\ gas}$

Mass fractions of metals : $Z \equiv \frac{total\ mass\ of\ metals}{total\ mass\ of\ gas}$

X + Y + Z = 1

For stars, usually, X ~ 0.7, 0 < Z < 0.03

$$[\mathrm{Fe/H}] = \log \frac{(\mathrm{Fe/H})_*}{(\mathrm{Fe/H})_\odot} = \log(\mathrm{Fe/H})_* - \log(\mathrm{Fe/H})_\odot$$

$$\log Z = 0.977[\mathrm{Fe/H}] - 1.699 \qquad [\mathrm{Fe/H}] = 1.024 \log Z + 1.739$$

An Introduction to Modern Astrophysics (2nd edition) Bradley W. Carroll & Dale A. Ostlie (1996) p. 325

https://en.wikipedia.org/wiki/Metallicity

http://burro.case.edu/Academics/Astr222/Galaxy/Structure/metals.html

Bertelli et al. (1994 A&AS 106 275 – Theoretical isochrones from models with new radiative opacities)

5. Novae (신성) – Rate of Decline

- **Peak brightness (M_V = -4.8 ~ -8.9)**
- **$\boxed{\text{MMRD}}$ (Maximum Magnitude – Rate of Decline) relation**

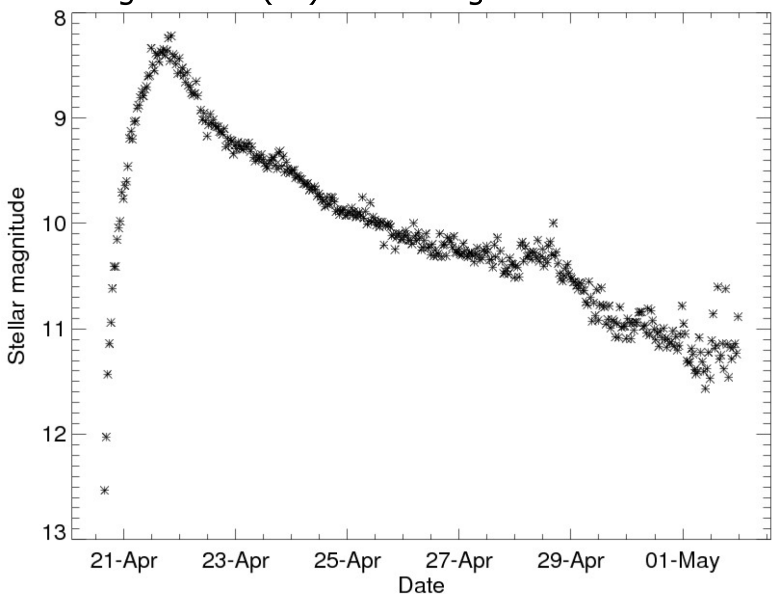
  light from faint novae decays more slowly

$$M_V(\text{max, corr}) = -10.70(\pm 0.30) + 2.41(\pm 0.23) \log t_2$$

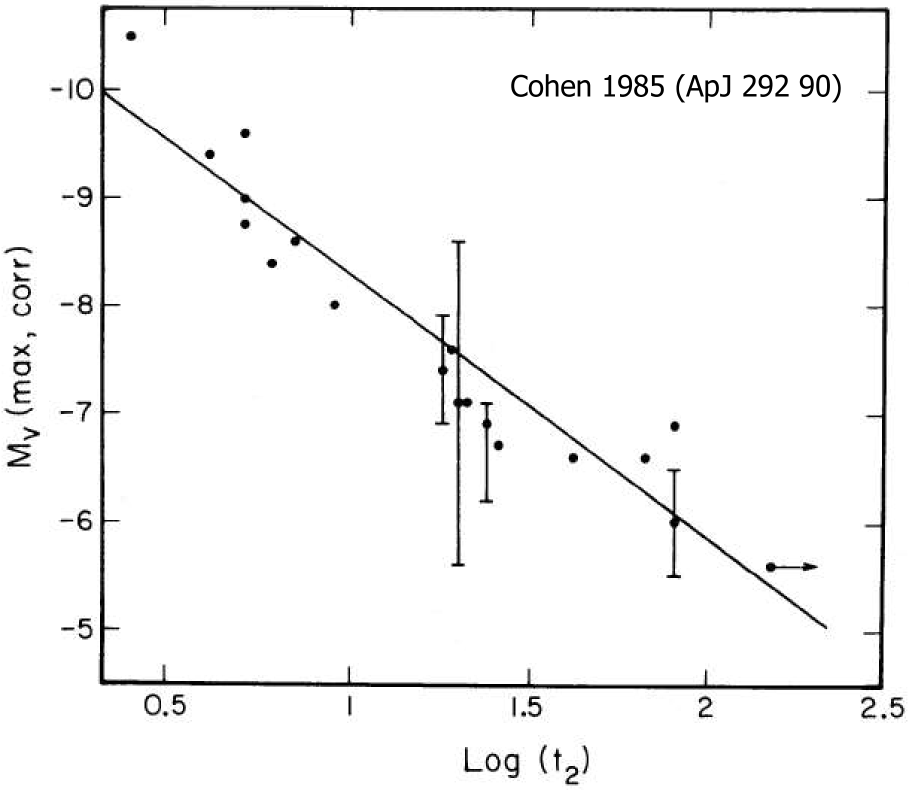
t_2 : time that nova takes to decline in brightness by 2 mag from the maximum

Cohen 1985 (ApJ 292 90)

Light curve (LC) : Nova Sagittarii 2012



https://stereo.gsfc.nasa.gov/~thompson/nova_sagittarii_2012/



Galactic Astronomy (J. Binney & M. Merrifield, 1998) p. 419

6. Supernovae (초신성)

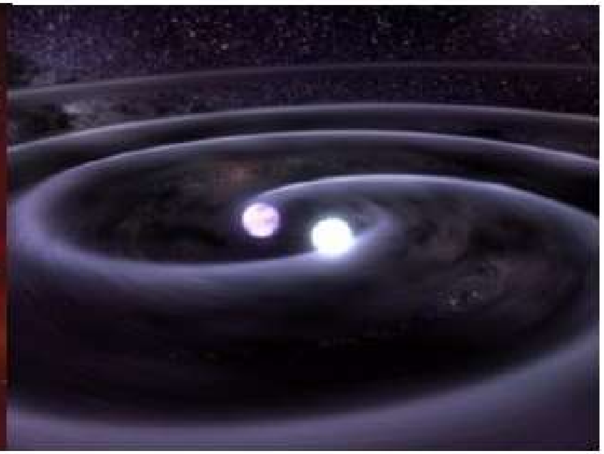
- Brightest objects in galaxies (M_V = -14 ~ -22)

- Typical types

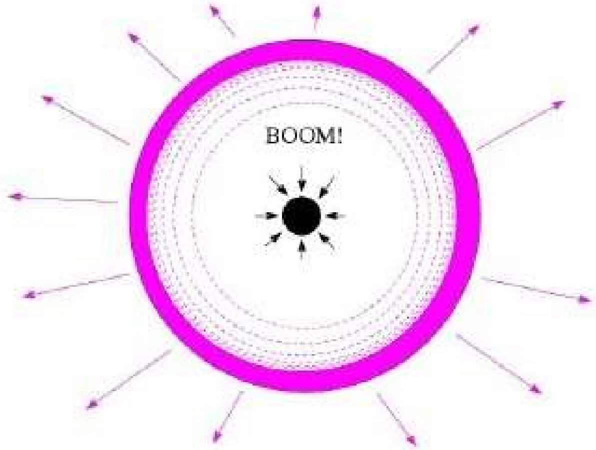
No H lines (pop II) → Type Ia Ib Ic

H lines (pop I) → Type II

WD + Giant/MS/He *
(Single Degenerate, SD)



WD + WD
(Double Degenerate, DD)



Core collapse

SNe Ia (thermonuclear stellar explosion)
(WD originated SNe)
백색왜성 기원 초신성

CC SNe

핵붕괴 초신성

http://dujs.dartmouth.edu/2008/05/type-ia-supernovae-properties-models-and-theories-of-their-progenitor-systems
http://wwwmpa.mpa-garching.mpg.de/mpa/research/current_research/hl2013-8/hl2013-8-en.html
http://spiff.rit.edu/richmond/sdss/sn_survey/sn_survey.html

6. Supernovae (초신성)

- Brightest objects in galaxies (M_V = -14 ~ -22)

- Typical types

No H lines (pop II) → Type Ia

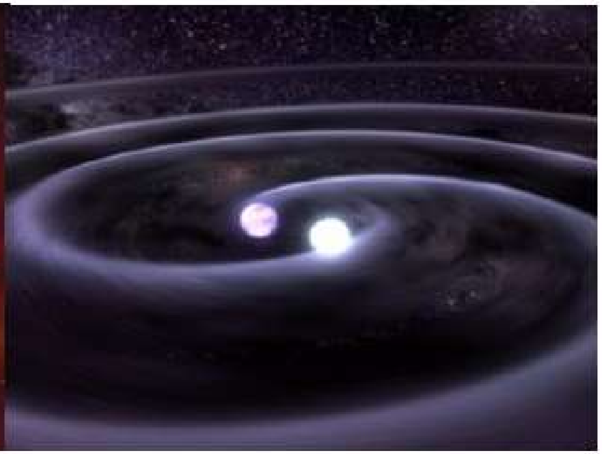
H lines (pop I) → Type II

Ib

Ic

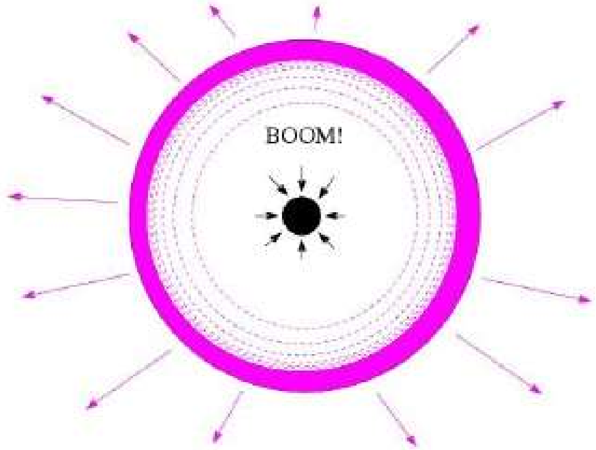
WD + Giant/MS/He *

(Single Degenerate, SD)



WD + WD

(Double Degenerate, DD)



Core collapse

SNe Ia (thermonuclear stellar explosion)

(WD originated SNe)

백색왜성 기원 초신성

CC SNe

핵붕괴 초신성

http://dujs.dartmouth.edu/2008/05/type-ia-supernovae-properties-models-and-theories-of-their-progenitor-systems
http://wwwmpa.mpa-garching.mpg.de/mpa/research/current_research/hl2013-8/hl2013-8-en.html
http://spiff.rit.edu/richmond/sdss/sn_survey/sn_survey.html

SN Ia absolute magnitude

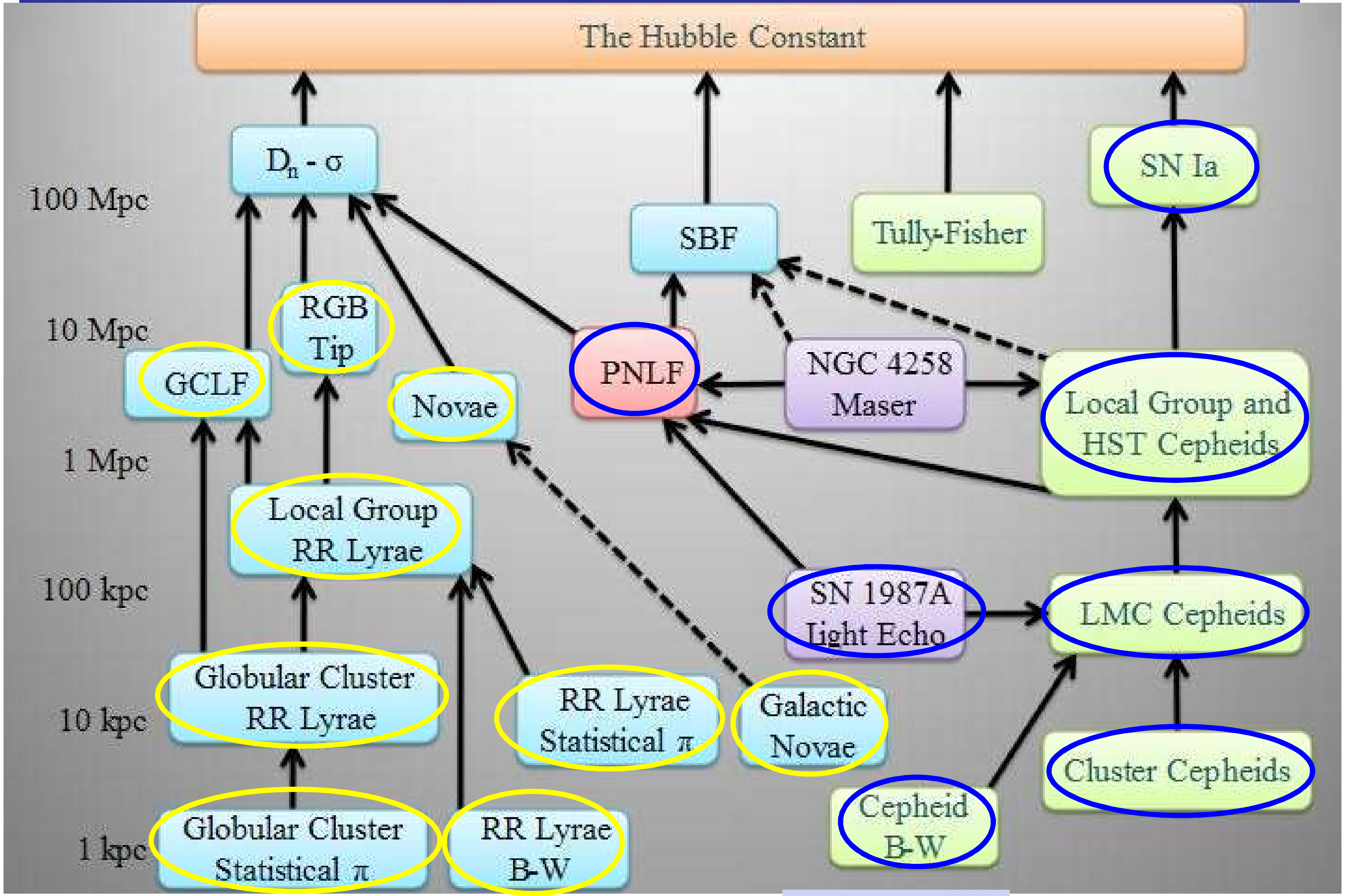
Photometrically, SN Ia rise to maximum light in a period of approximately 20 days (Riess et al 1999b) reaching

$$\boxed{M_{\rm B} \approx M_{\rm V} \approx -19.30 \pm 0.03 + 5\log(H_0/60)} \qquad (1)$$

with a dispersion of $\sigma_M \leq 0.3$ (Hamuy et al 1996b).

W. Hillebrandt & J. C.Niemeyer (2000, ARA&A, 38, 191 – Type Ia SN explosion models)

Extragalactic Distance Ladder



Population II galaxies

Geometric technique

Star-forming galaxies

https://en.wikipedia.org/wiki/Cosmic_distance_ladder

1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)
1.3 Magnitudes (등급)

http://www.centauri-dreams.org/?p=11322
http://www.centauri-dreams.org/wp-content/uploads/2010/02/light-candles.jpg

1. Magnitude scale

$$\boxed{m - n = 2.5 \log(\frac{l_n}{l_m})}$$

→ apparent magnitude (겉보기등급, 실시등급)

- $m > n \leftarrow l_n > l_m$
- Brighter objects : numerically smaller magnitudes

Absolute magnitude, Distance modulus

- A very luminous star appears dim – if far away
- A low-luminosity star look bright – if very close
  → distance links fluxes and luminosities
- absolute magnitude (절대등급) = the magnitude to be observed if the star is placed at a distance of 10 pc from the Sun → capital M

$$\frac{L}{l} = (\frac{d}{D})^2 = (\frac{d}{10})^2$$

- M – L, m – *l*

$$m - M = 2.5 \log(\frac{L}{l}) = 2.5\log[(\frac{d}{10})^2] = 5 \log(\frac{d}{10})$$

$$\boxed{(m - M)_0 = 5 \log d - 5}$$ distance modulus

Extinction corrected

$$\boxed{m - M = 5 \log d - 5 + A} \qquad V - M_V = 5 \log d - 5 + A_V$$

2. Photometric Filter Systems (측광계)

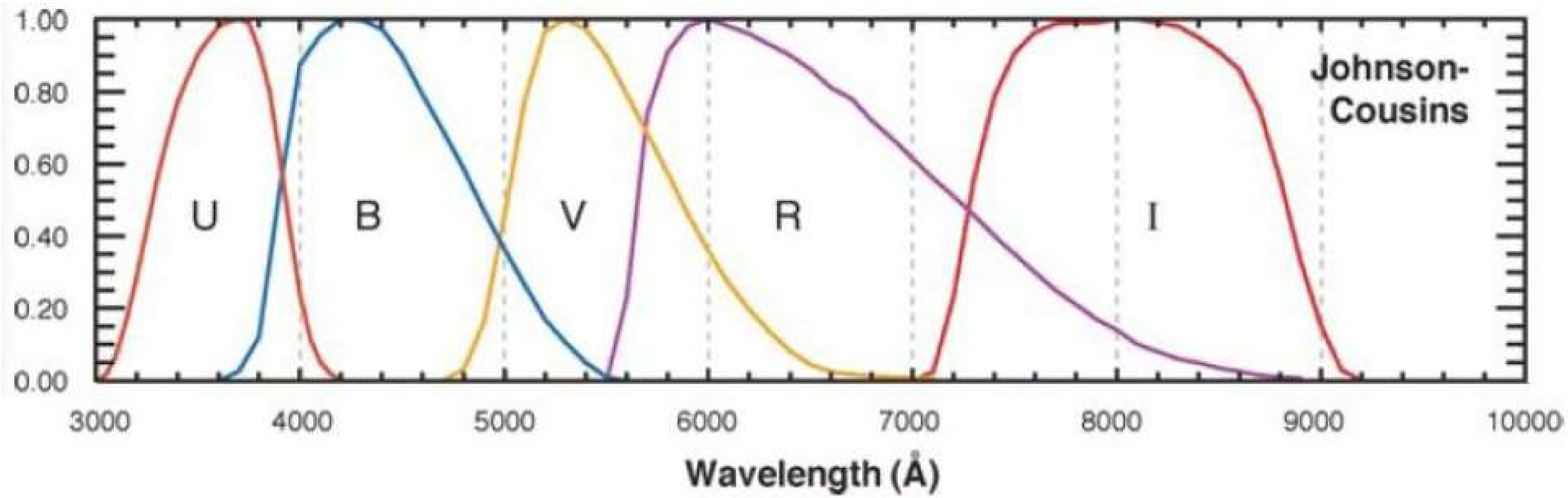
➢ Johnson-Cousins UBVRI System

- Originally defined by Johnson & Morgan (1953) : UBV
- Extended by Cousins (1974) : UBVRI
- Re-analyzed by Bessell (1990)

1 nm = 10^{-9} m
1 Å = 10^{-10} m
1 nm = 10Å

366 nm =

	Effective Wavelength (λ_{eff})	Bandpass ($\Delta\lambda$)
U	3663 Å	650 Å
B	4361 Å	890 Å
V	5448 Å	840 Å
R	6407 Å	1580 Å
I	7980 Å	1540 Å



Bessell (2005, ARA&A, 43, 293 – Standard photometric systems)

2. Photometric Filter Systems (측광계)

Bandwidth :

Broadband : Δλ < 1000 Å (광대역)
Intermediate band : 70 Å < Δλ < 400 Å (중대역)
Narrowband : Δλ < 70 Å (협대역)

Bessell (2005, ARA&A, 43, 293 – Standard photometric systems)

2. Photometric Filter Systems (측광계)

➢ Sloan Digital Sky Survey (SDSS) System

- ugriz

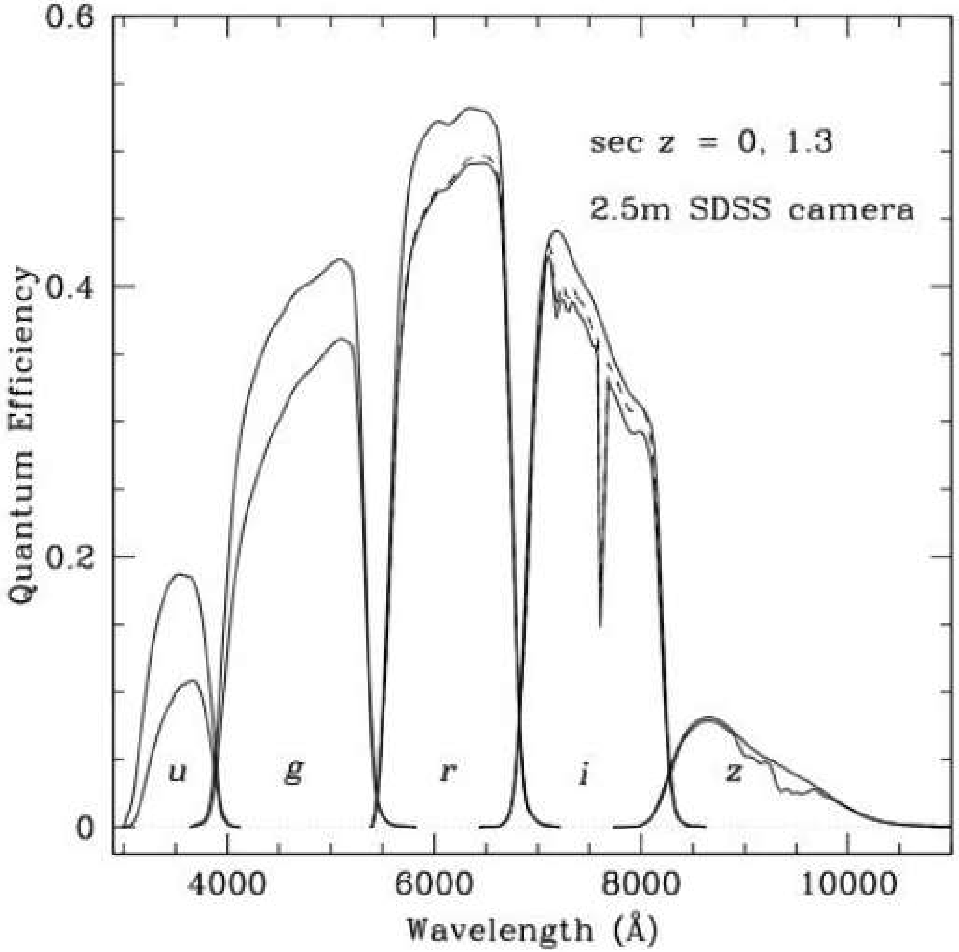


TABLE 19

SDSS Filter Parameters

Name	λ_{eff} (Å)	σ^2	FWHM (Å)	Q
u..........	3551	3.00×10^{-3}	581	0.0171
g..........	4686	7.13×10^{-3}	1262	0.0893
r..........	6166	3.13×10^{-3}	1149	0.0886
i..........	7480	2.58×10^{-3}	1237	0.0591
z..........	8932	3.18×10^{-3}	994	0.0099

C. Stoughton et al. 2002, AJ, 123, 485 (SDSS: Early Data Release)

3. Color Index (CI, 색지수, 색)

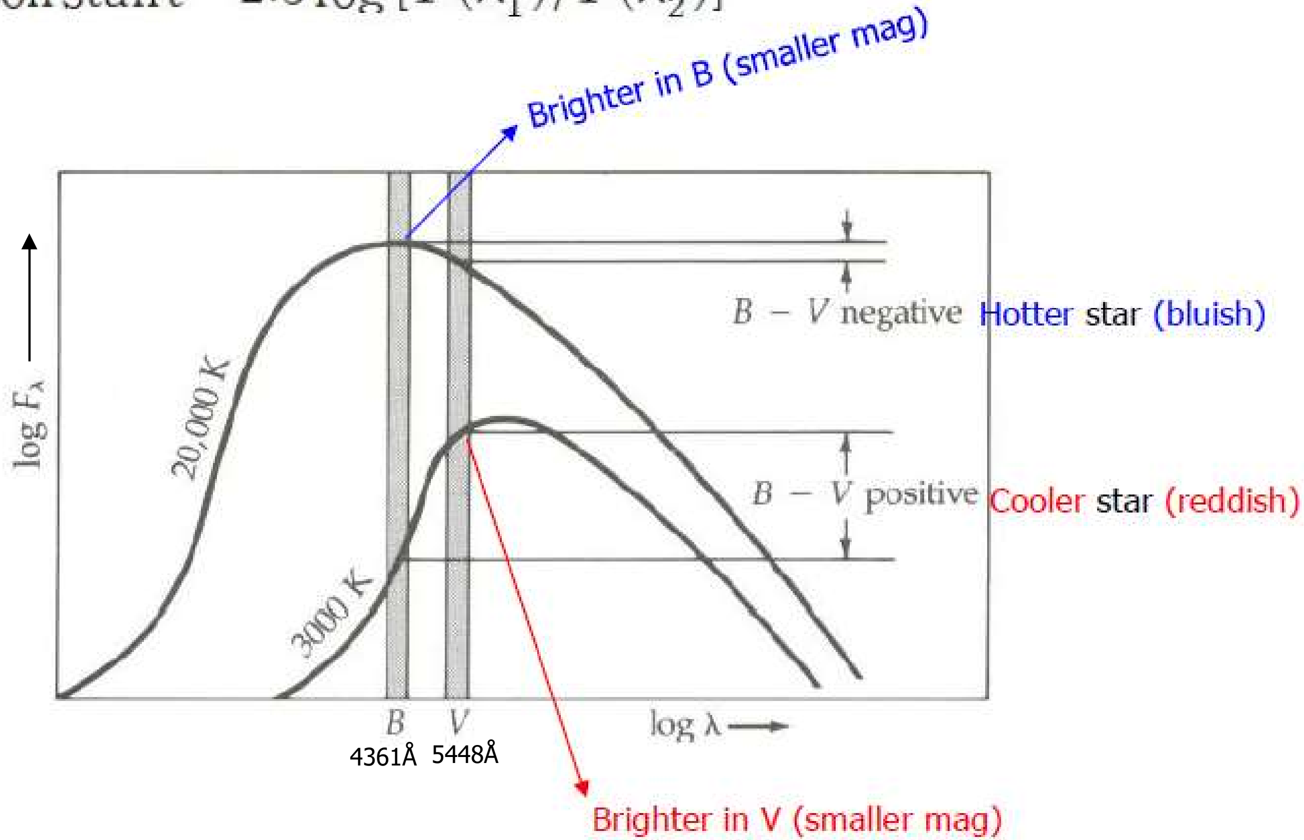
- Color index = difference between magnitudes at two different effective wavelengths

$$CI = m(\lambda_1) - m(\lambda_2)$$

- Mag difference → flux ratio at the specific wavelengths involved

$$CI = \text{constant} - 2.5\log[F(\lambda_1)/F(\lambda_2)]$$

- Hotter stars (bluish) : negative CI
- Cooler stars (reddish) : positive CI

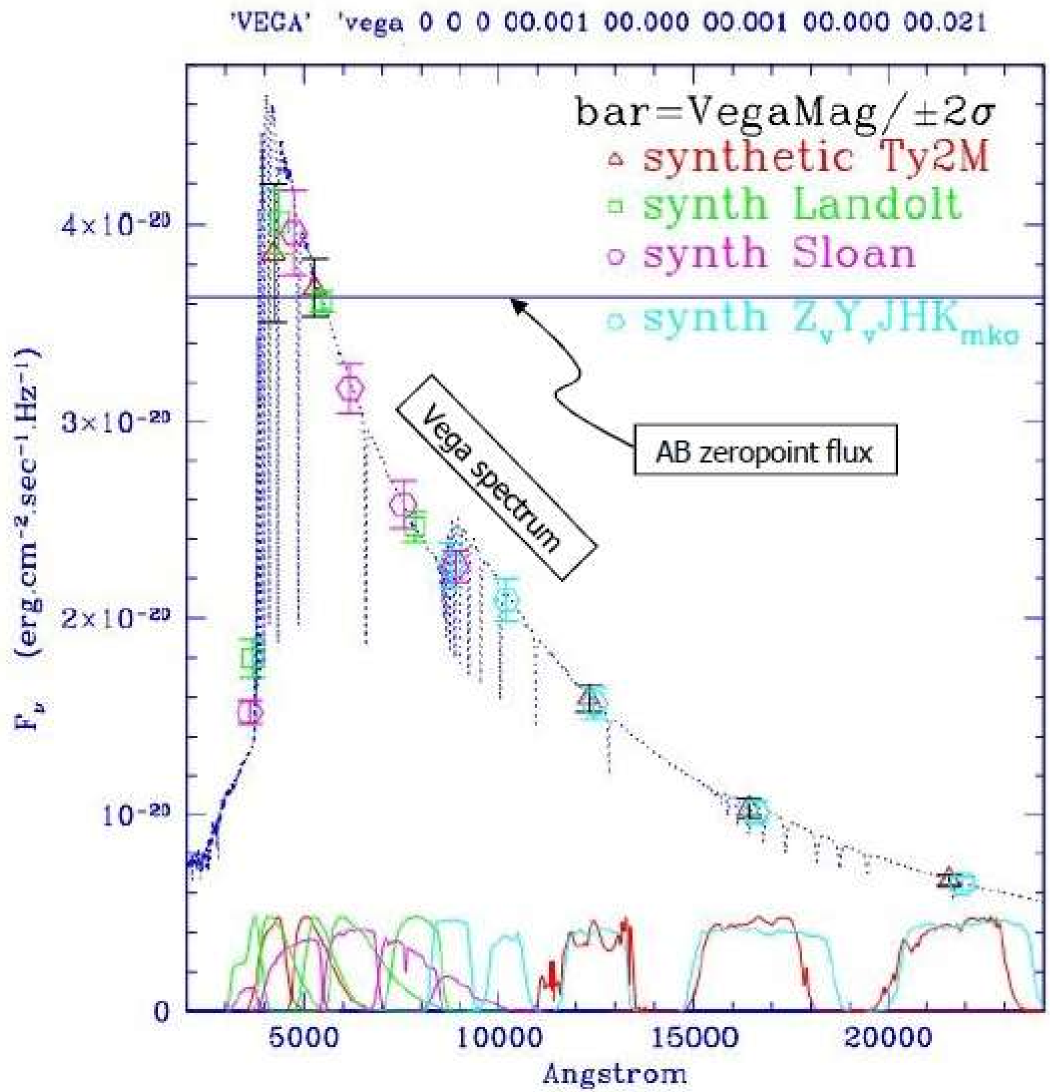


Introductory Astronomy and Astrophysics (4th edition)
Michael Zeilik & Stephen A. Gregory (1998), p. 229

Magnitude systems

➤ Vega magnitude system

- Vega (=α Lyr) : the primary calibrating star
- Surface temperature = 10,000 K
- CI = 0
- Zero-point was defined in terms of unreddened main-sequence (MS) stars of class A0 … with an accuracy sufficient to permit the placement of the zero-point to about 0.01 mag



Pickles & Depagne (2010 PASP 122 1437)

➤ AB magnitude system

- Magnitude zero point corresponds to a flux density of 3631 Jy (1 Jy = 1 Jansky = 10^{-26} W Hz^{-1} m^{-2} =10^{-23} erg s^{-1} Hz^{-1} cm^{-2})

- Bessell (2005, ARA&A, 43, 293 – Standard photometric systems)
- Casagrande & VandenBerg (2014, MNRAS, 444, 392 – Synthetic stellar photometry. I. General considerations and new transformations for broad-band systems)

4. Color Excess, Bolometric Magnitude

- Interstellar dust grains absorb and scatter starlight
- Observed light gets faint (extinction) and appears redder (interstellar reddening)

(소광) (성간적색화: λ-dependent)

- Color Excess (색초과) = observed color – intrinsic color

  $E(B\text{-}V) = (B\text{-}V) - (B\text{-}V)_0$

- Interstellar extinction :

  $A_V \sim R \times E(B\text{-}V)$, R = 3.0, $\boxed{3.1,}$ 3.2, 3.3

  R : total-to-selective extinction ratio

  - Amount of interstellar medium (ISM)
  - ISM composition
  - Galactic longitude

- Bolometric magnitude (복사등급) : total rate of energy output at all wavelength

$$l_{bol} = \int_0^\infty l_\lambda \, d\lambda$$

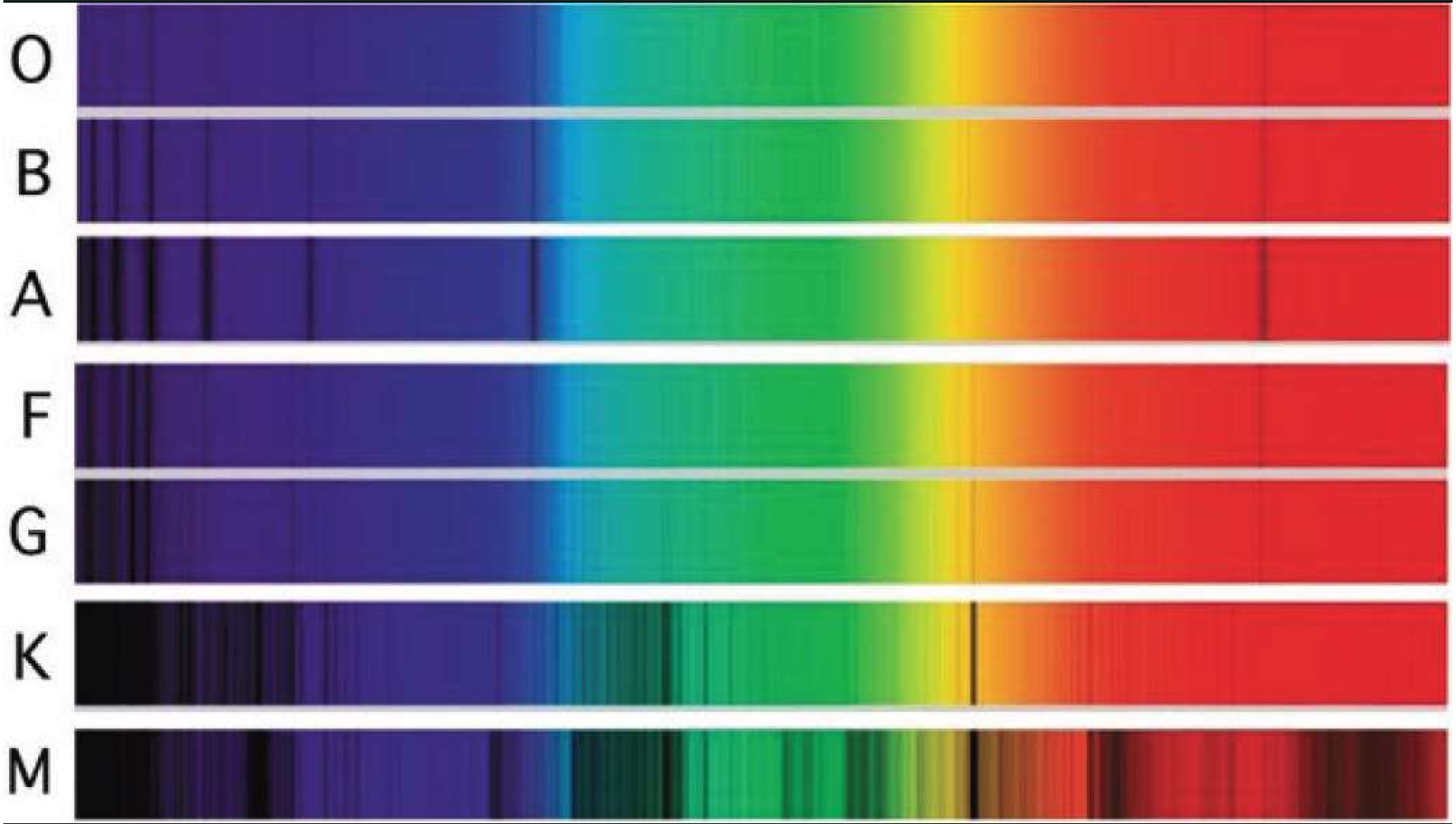
- Bolometric correction (BC, 복사보정) : difference between the bolometric and visual magnitudes

$$\mathrm{BC} = m_{\mathrm{bol}} - m_v = M_{\mathrm{bol}} - M_v = 2.5 \log\left(\frac{l_v}{l_{\mathrm{bol}}}\right)$$

for the Sun (G2) : BC = -0.07

Introductory Astronomy and Astrophysics (4th edition)
Michael Zeilik & Stephen A. Gregory (1998), p. 231

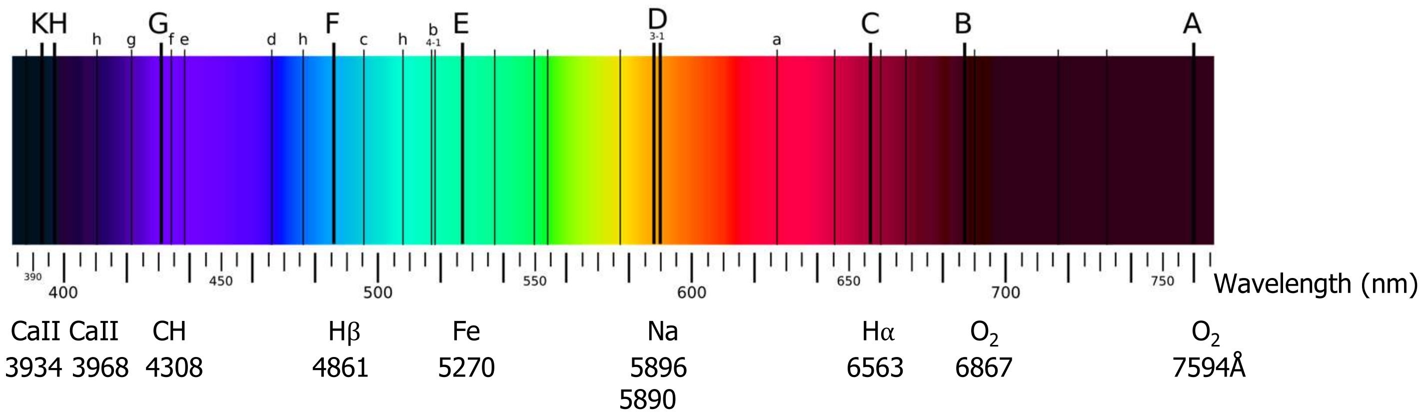
1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)
1.4 The Classification of Stellar Spectra (별의 스펙트럼 분류)

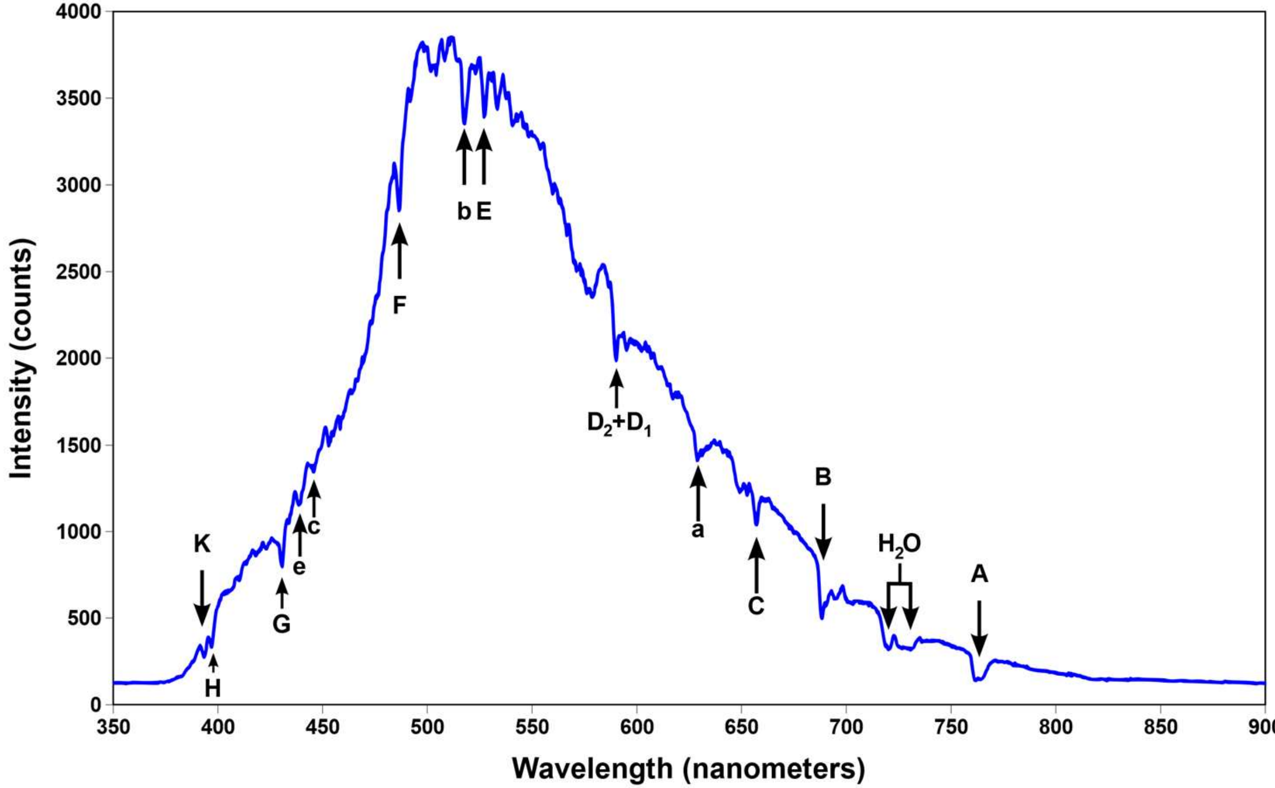


http://science.jburroughs.org/astromet/NAAP/ebs/spectraltype.html

Fraunhofer lines

Joseph von Fraunhofer observed dark absorption lines in the Solar optical spectrum (1814)





https://en.wikipedia.org/wiki/Fraunhofer_lines

Spectral types

How to memorize spectral types?

OBAFGKM

$\downarrow$

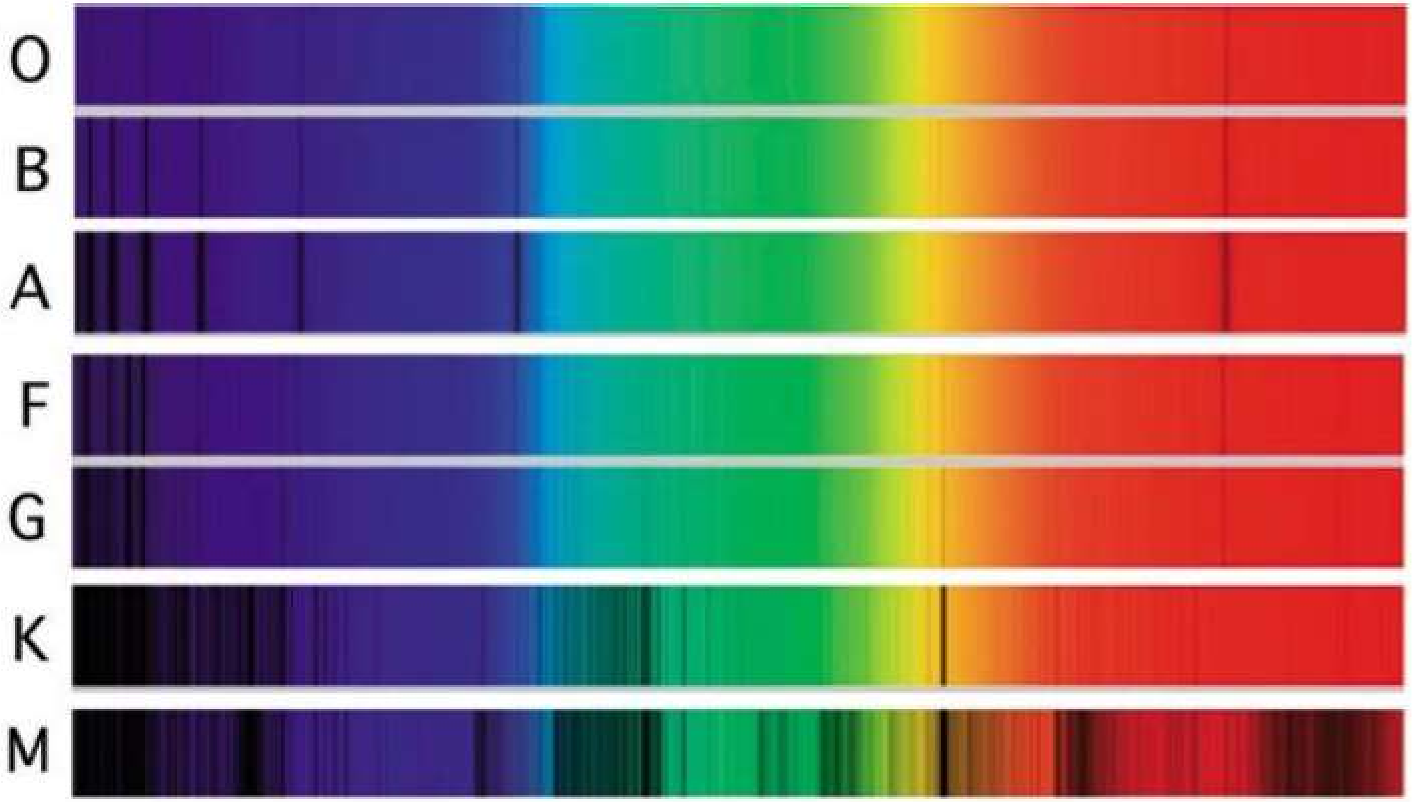
Oh Beautiful And Fine
Girl(Guy),
Kiss Me!

O0, O1, O2, …O9, B0, B1, B2, …B9, …

Stellar spectra

Stars' spectra : differ depending on T and composition

Early-types (O and B) stars – few spectral lines
Late-types (K and M) stars – many spectral lines



http://science.jburroughs.org/astromet/NAAP/ebs/spectraltype.html

Spectral types

Spectral type	Stars	Spectral features	(e.g.)
O	blue stars, usually SGs, very luminous and hot, rare	**He II absorption lines** (sometimes emission: 4541, 4200Å); He I lines (4471, 4026Å) weak but increasing in strength from O5 to O9; lines from highly ionized species (e.g., C III, N III, O III, Si IV); H lines prominent but relatively weak; strong UV continuum	ζ(Zeta) Puppis (O4 I)
B	blue white stars, mainly giants	**Strong He I lines, maximum at B2**; no He II lines; **H absorption lines strengthening from B0 to B9**; lower-excitation ions (e.g., C II, O II, Mg II, Si II, Si III)	Rigel (=β Orionis, B8 Ia), ε Ori (B0 Ia)
A	White stars, dwarfs to giants	**H absorption lines maximum strength at A0** and decrease towards later types; **ionized metal lines (Fe II, Mg II, Si II) at max strength near A5**; Ca II weak and increase in strength; lines of neutral metals appear weakly	Sirius (A1 V), α Lyr (=Vega, A0 V)
F	yellow white stars, mainly dwarfs	H absorption lines weakening rapidly, **Ca II H&K absorption lines strengthen**; lines of neutral metals (Fe I, Cr I) and first ionization states of metals appear prominently	Procyon (=α CMi, F5 IV-V)
G	yellow stars, mainly dwarfs	Solar-type spectra; **Ca II absorption lines dominate (max near G2)**; neutral metal lines (Fe I, Mn I, Ca I) strengthening; ionized metal lines diminish; **G band (CH) strong**; H lines very weak	Sun (G2 V)
K	orange stars, can exist as giants and dwarfs	**Neutral metallic absorption lines dominate**; **Ca lines strong**; H lines almost gone; molecular bands (CH, CN, TiO) developing; continuum weak in blue	Arcturus (=α Boötis, K0 III), Aldebaran (=α Tau, K5 III)
M	red stars, exist at extremes either giants or red dwarfs	Strong **molecular bands, particularly TiO by M5**; **neutral metallic absorption lines** (e.g., quite strong Ca I); red continuum	Betelgeuse (=α Orionis, M2 I), Proxima Centauri (M5.5 V)

Galactic Astronomy (J. Binney & M. Merrifield, p. 92)
Introductory Astronomy & Astrophysics (Zeilik & Gregory, p. 258)

http://solarandspace.tripod.com/id11.html

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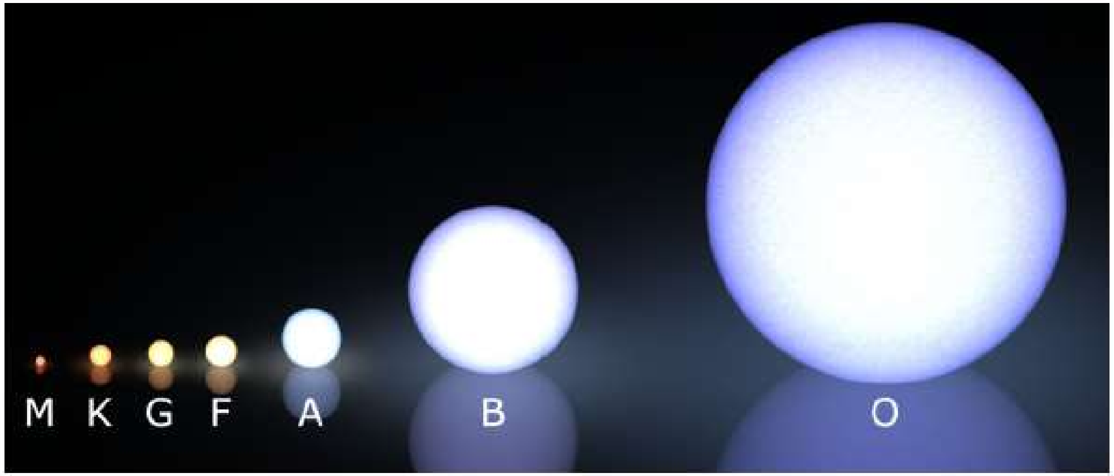
ζ Puppis (O4 I) – artist's rendering
https://en.wikipedia.org/wiki/Stellar_classification



Relative size of O-type stars with other MS stars

https://en.wikipedia.org/wiki/Stellar_classification

Galactic Astronomy (J. Binney & M. Merrifield, p. 92)
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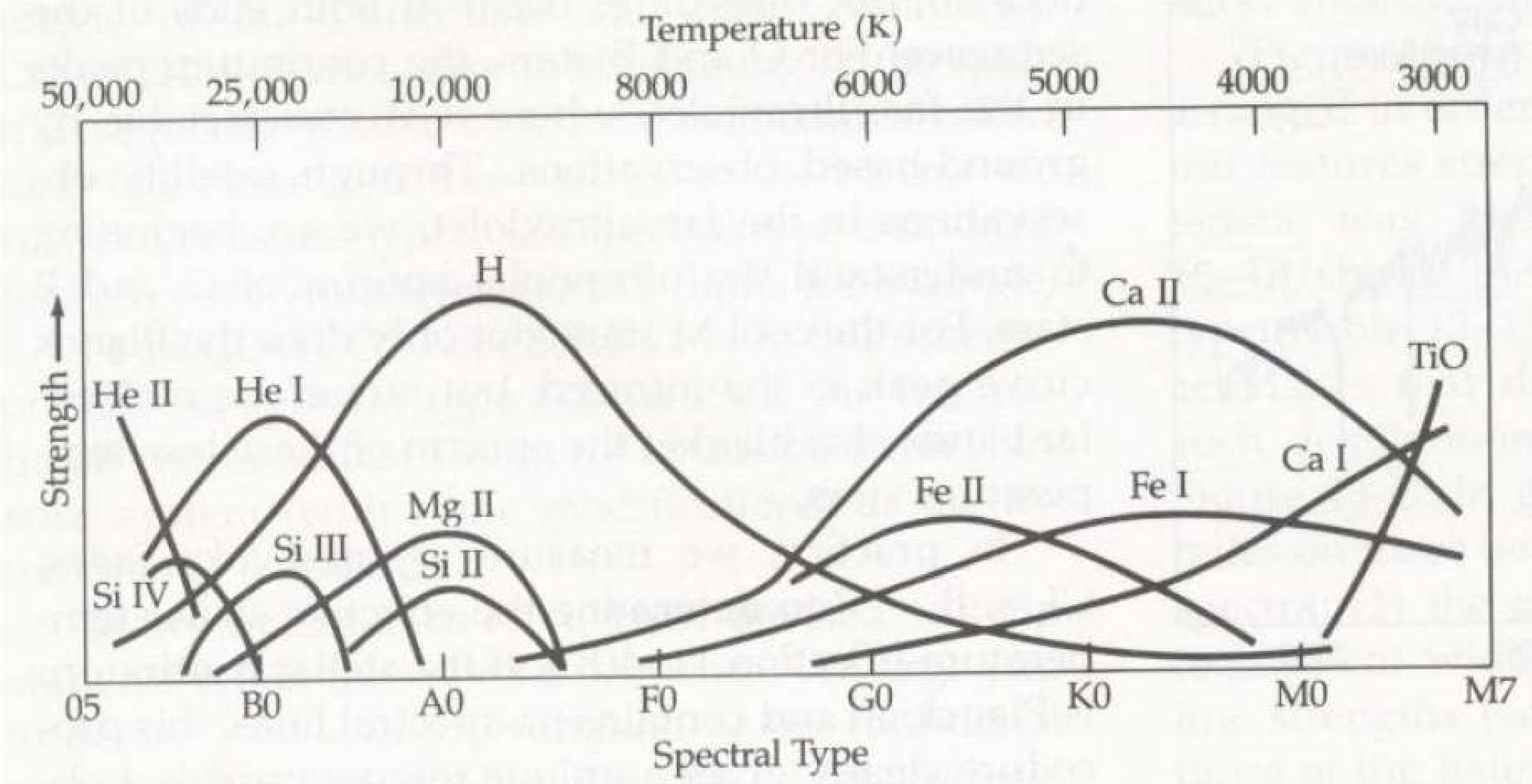
Spectral types

absorption lines



Introductory Astronomy and Astrophysics (4th edition) Michael Zeilik & Stephen A. Gregory (1998), p. 258
An Introduction to Modern Astrophysics (2nd edition) Bradley W. Carroll & Dale A. Ostlie (1996) p. 240

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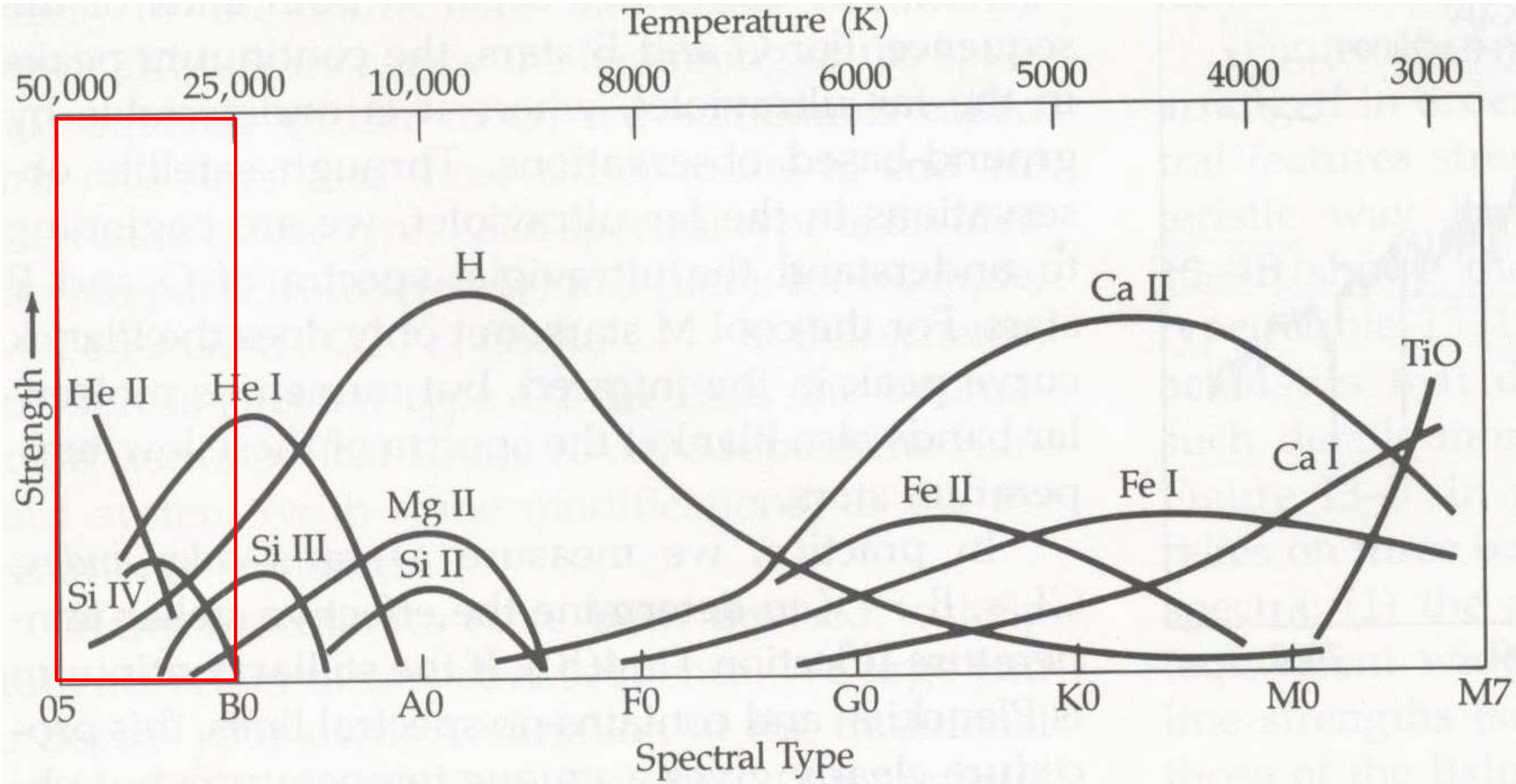

Galactic Astronomy (J. Binney & M. Merrifield, p. 92)

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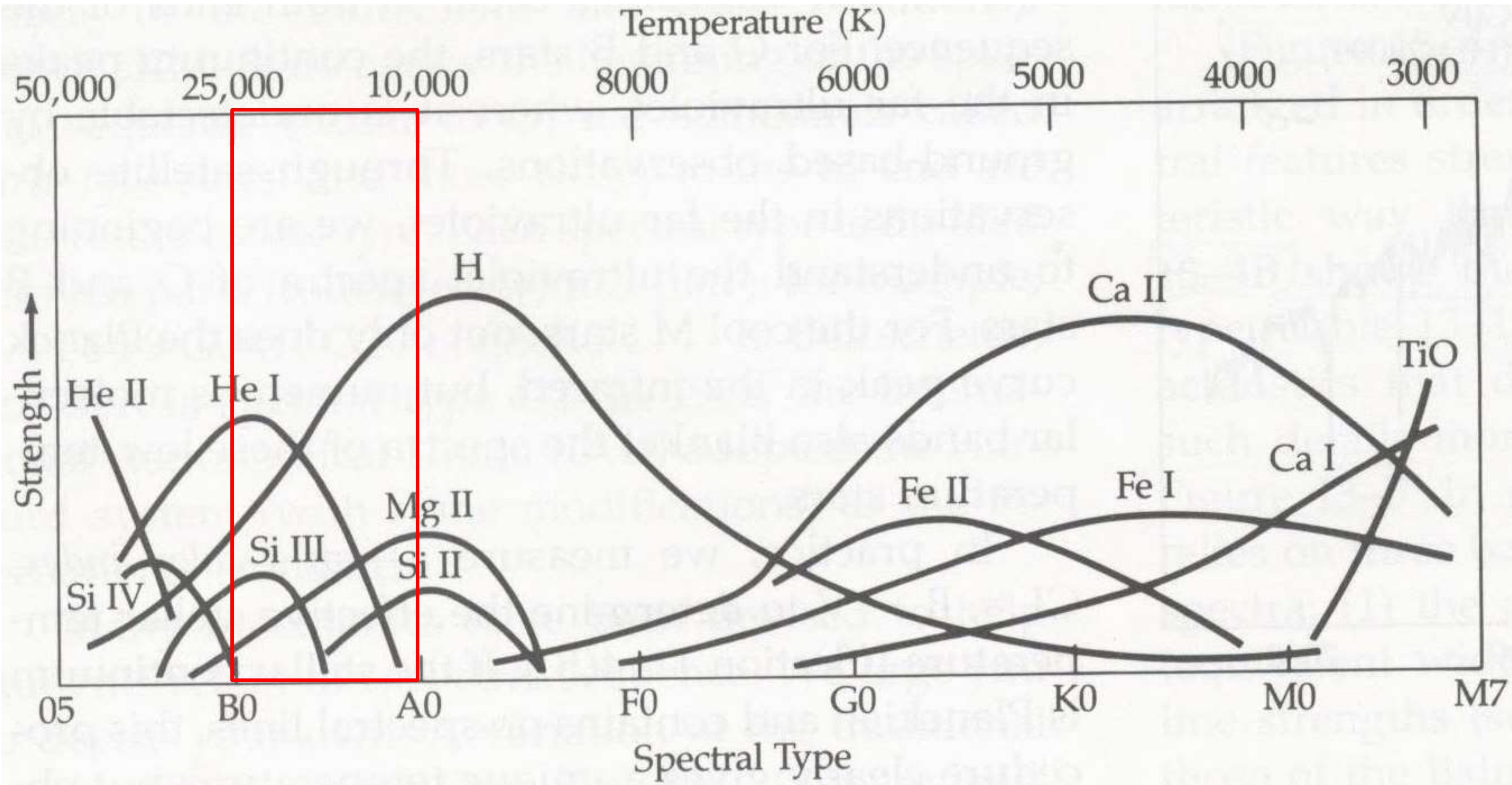

Galactic Astronomy (J. Binney & M. Merrifield, p. 92)
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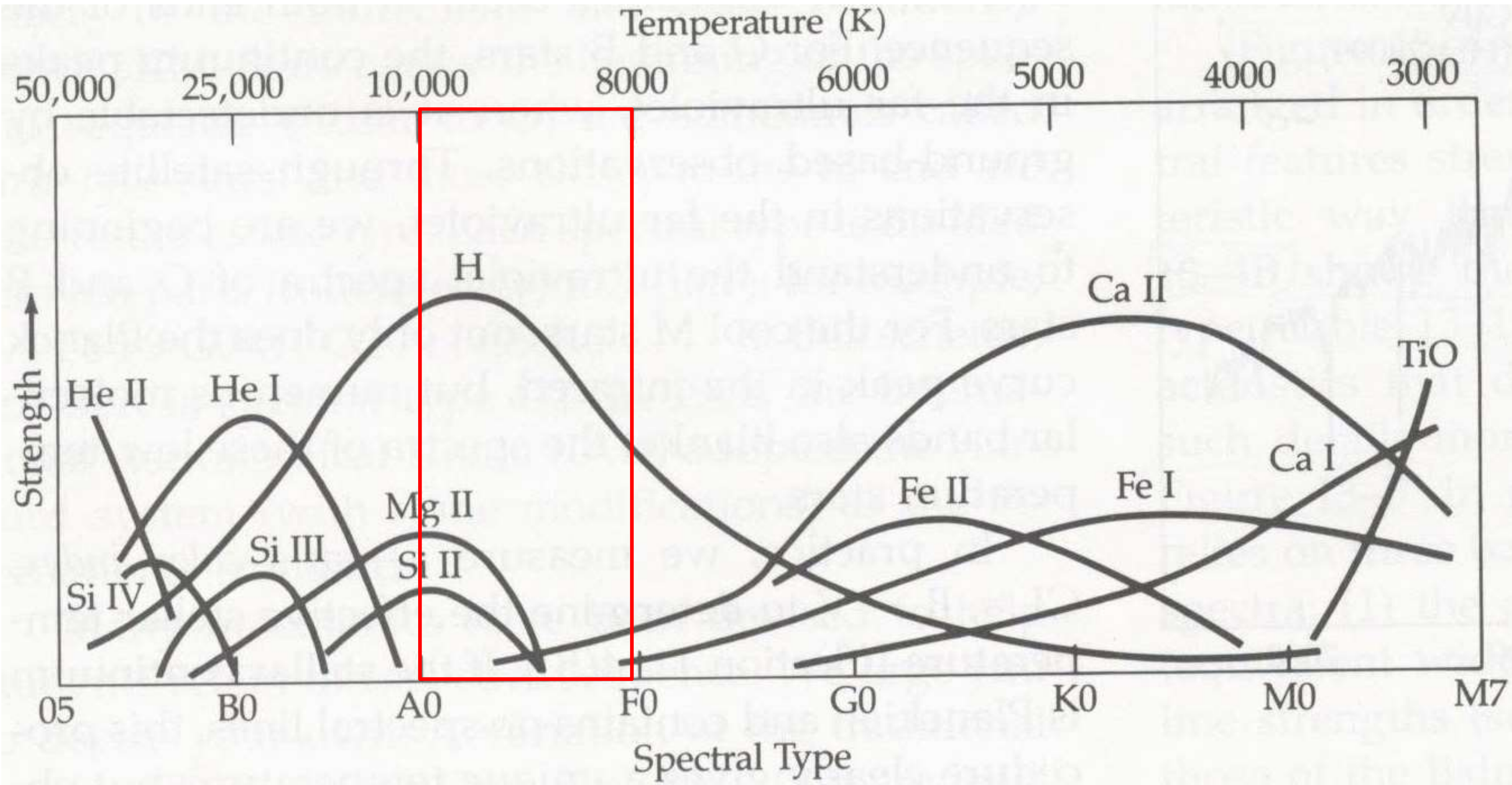

Galactic Astronomy (J. Binney & M. Merrifield, p. 92)
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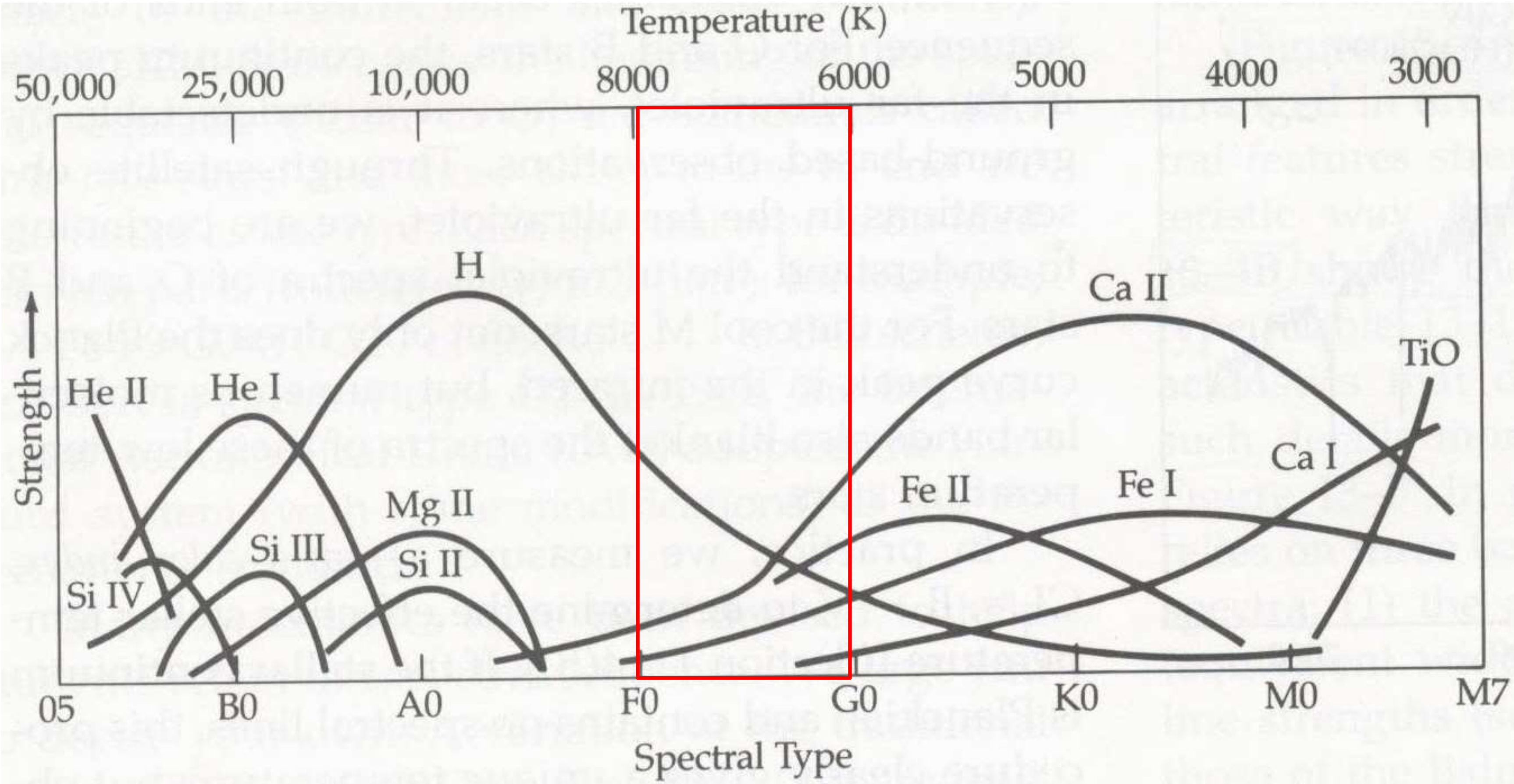

Galactic Astronomy (J. Binney & M. Merrifield, p. 92)
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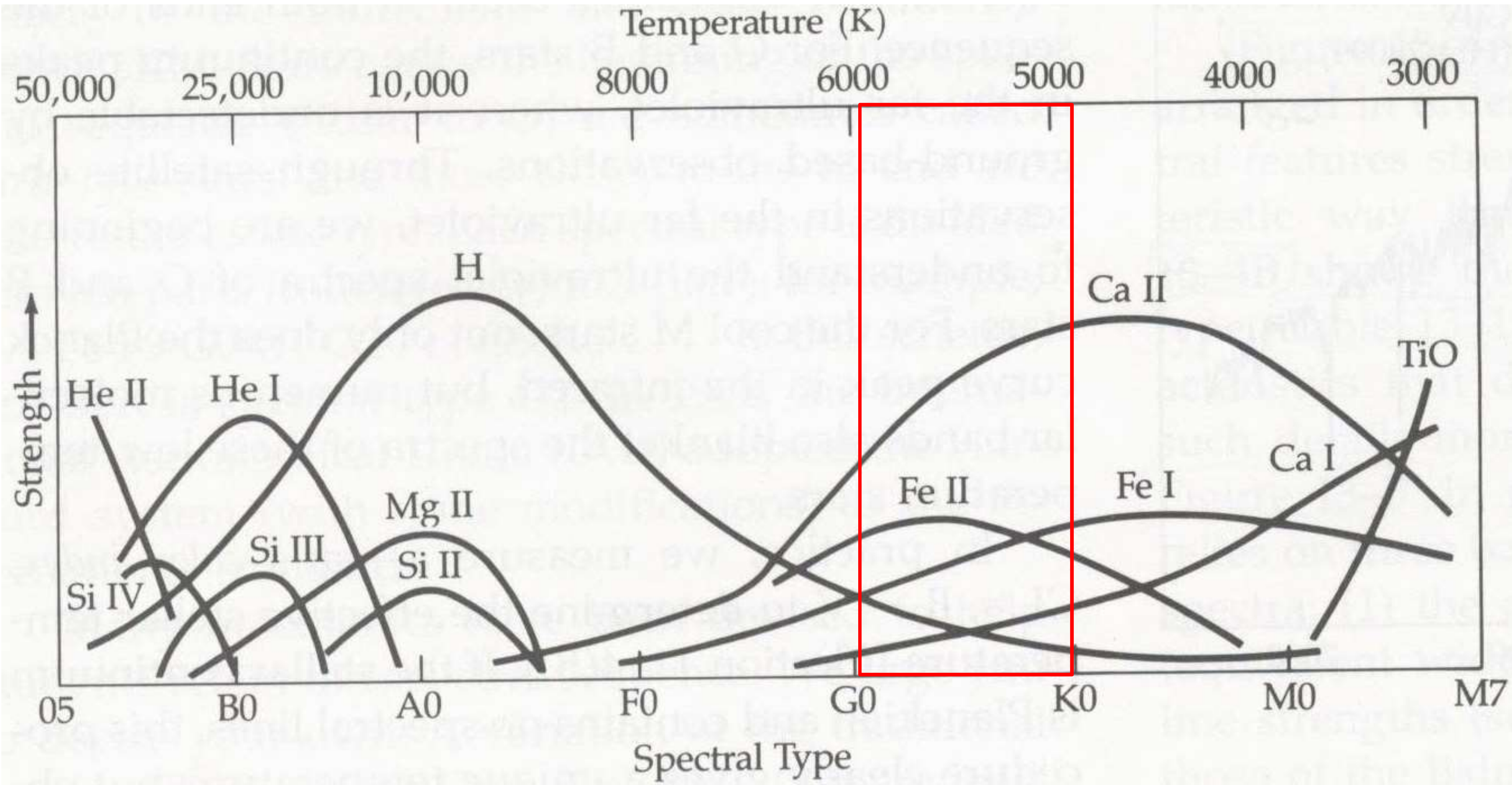

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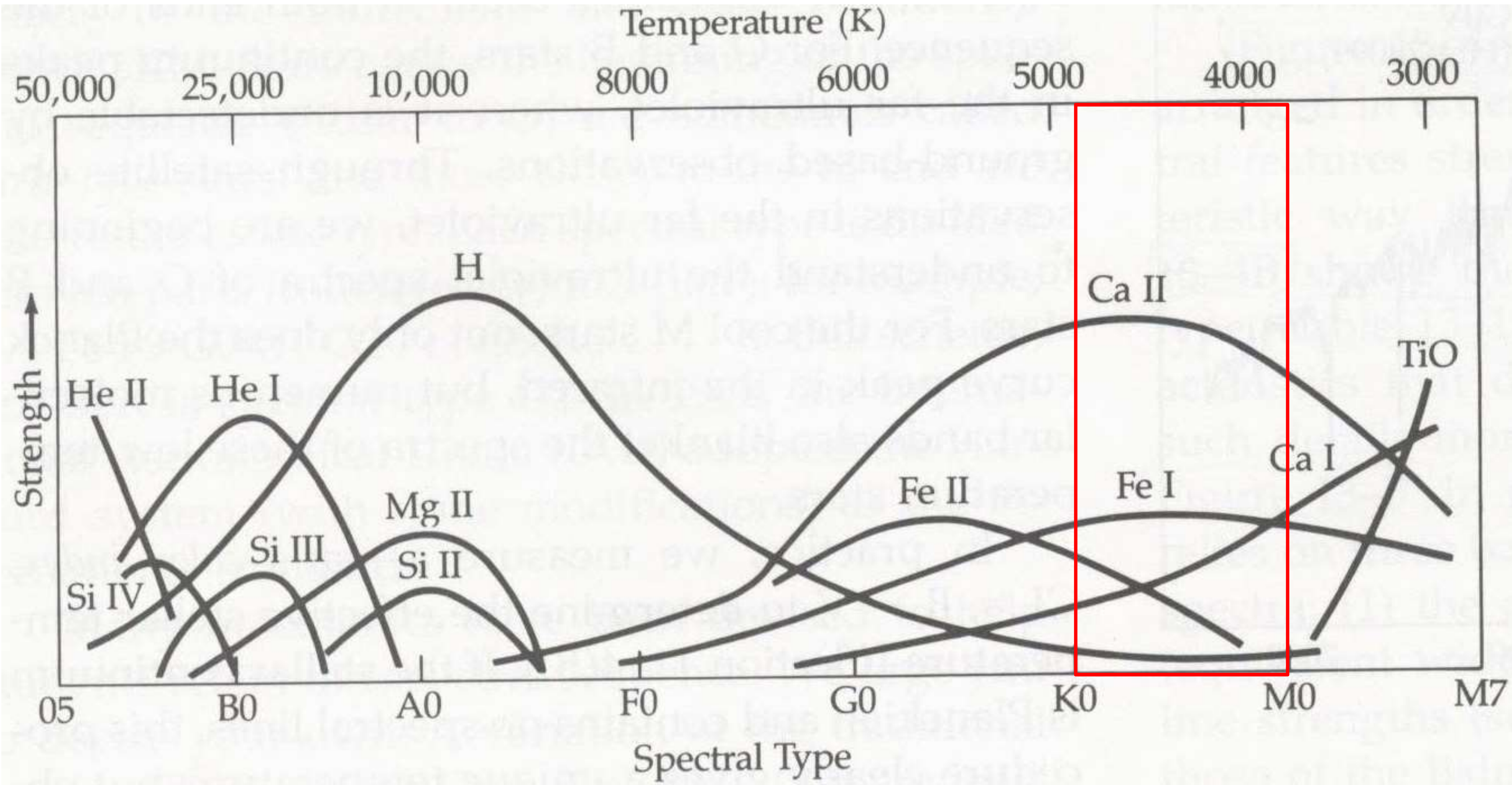

Galactic Astronomy (J. Binney & M. Merrifield, p. 92)
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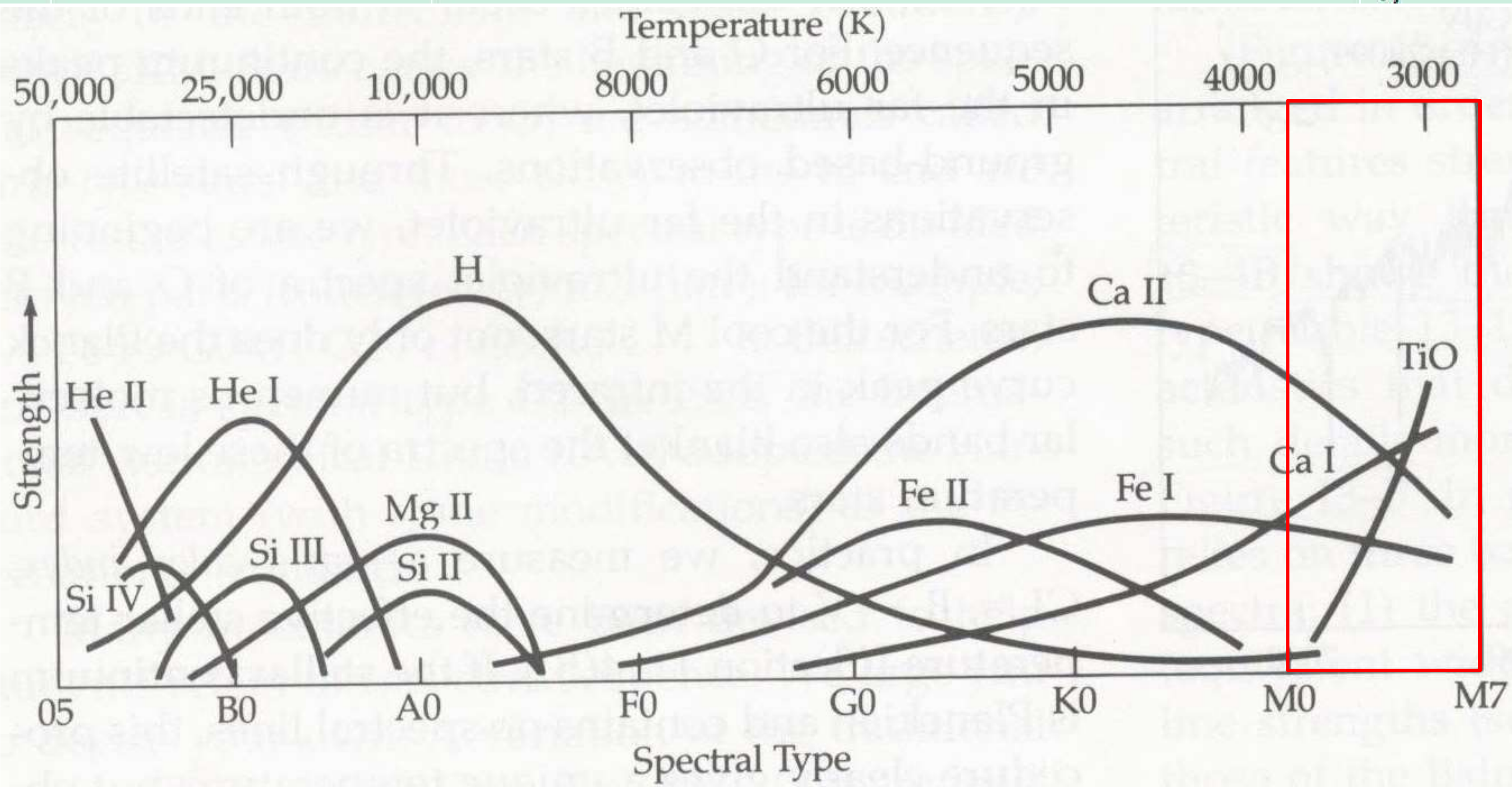

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Extended spectral types

How to memorize spectral types?

OBAFGKM RNS

Oh Beautiful And Fine Girl(Guy), Kiss Me!

Right Now, Smack!

Extended spectral types

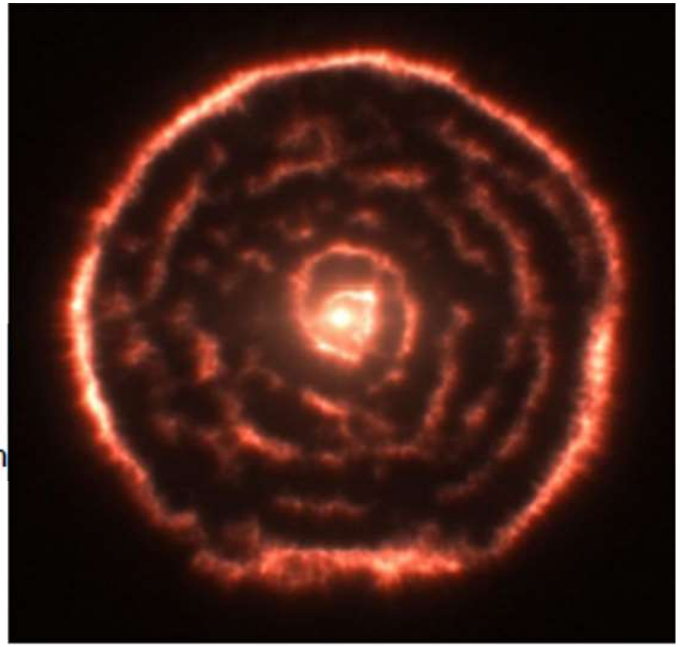
C (carbon) stars
- giant stars with similar temperatures of G, K, M stars (T = 3100 - 4600 K)
- different compositions : C is overabundant relative to O

hotter R stars (C_2, CN bands)
cooler N stars (C_2, CN, CH bands, little TiO)

S stars : molecular bands of the heavy-metal oxides ZrO, LaO, YO (instead of TiO)
: enhanced CN absorption bands
: neutral atoms strong as in K and M types

Galactic Astronomy (J. Binney & M. Merrifield, 1998) p. 92
Introductory Astronomy and Astrophysics (4th edition) Michael Zeilik & Stephen A. Gregory (1998), p. 266

R Sculptoris : a sample C star
(Maercker+12, Nature, 490, 232)
https://en.wikipedia.org/wiki/Stellar_classification



${}_{22}Ti^{48}$: Titanium
${}_{39}Y^{89}$: Yttrium
${}_{40}Zr^{91}$: Zirconium
${}_{57}La^{139}$: Lanthanum

Extended spectral types

- Cool red dwarfs and brown dwarfs (BDs) - Infrared spectra
- BD : objects whose central temperatures never reach the critical threshold for stable thermonuclear burning (Kirkpatrick + 11 ApJS 197, 19 'The first hundred BDs discovered by the Wide-field Infrared Survey Explorer (WISE)')

- BDs cool as they age : from M to L, T, Y type

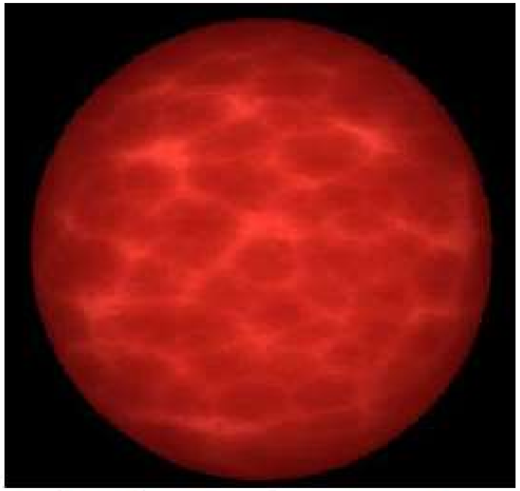
The less massive, the faster cooling

- Class L : mostly BDs with substellar mass, some stars with H-fusion

(e.g.) V838 Mon

- Temp ~1,700 K (~ 1,400 °C)
- M and L types = mixture of stars and BDs

J. D. Kirkpatrick (2005, ARA&A, 43, 195 'New spectral types L and T')



L dwarf - artist's impression

V838 Monocerotis – HST
https://en.wikipedia.org/wiki/V838_Monocerotis

https://en.wikipedia.org/wiki/Stellar_classification
http://www.nasa.gov/mission_pages/WISE/multimedia/pia14722.html

Extended spectral types

- Class T
  cool brown dwarfs
  surface T ~1,200 K (1,000 – 1,600 K)
  (~ 900 °C) (700 – 1,300 °C)
  prominent methane (CH_4) in the spectra
  ➔ "methane dwarfs"

  T dwarfs would appear reddish, or magenta, to the eye.

T dwarf - artist's impression

https://en.wikipedia.org/wiki/Stellar_classification
http://www.nasa.gov/mission_pages/WISE/multimedia/pia14720.html

Extended spectral types

- Class Y

  BDs cooler than class T

  (coldest BDs, latest classification letter)

  Cushing + 11 (ApJ, 743, 50 'The discovery of Y dwarfs using data from the Wide-field Infrared Survey Explorer (WISE)')

  Temp ~ 298 – 448 K (25 – 175 °C)

  Mass : 9 – 25 M_J

  N = 17 (2013 August)

  mostly nearby : 9 – 40 ly

  (WISE 1541-2250, d~9 ly : 7th closest star system)

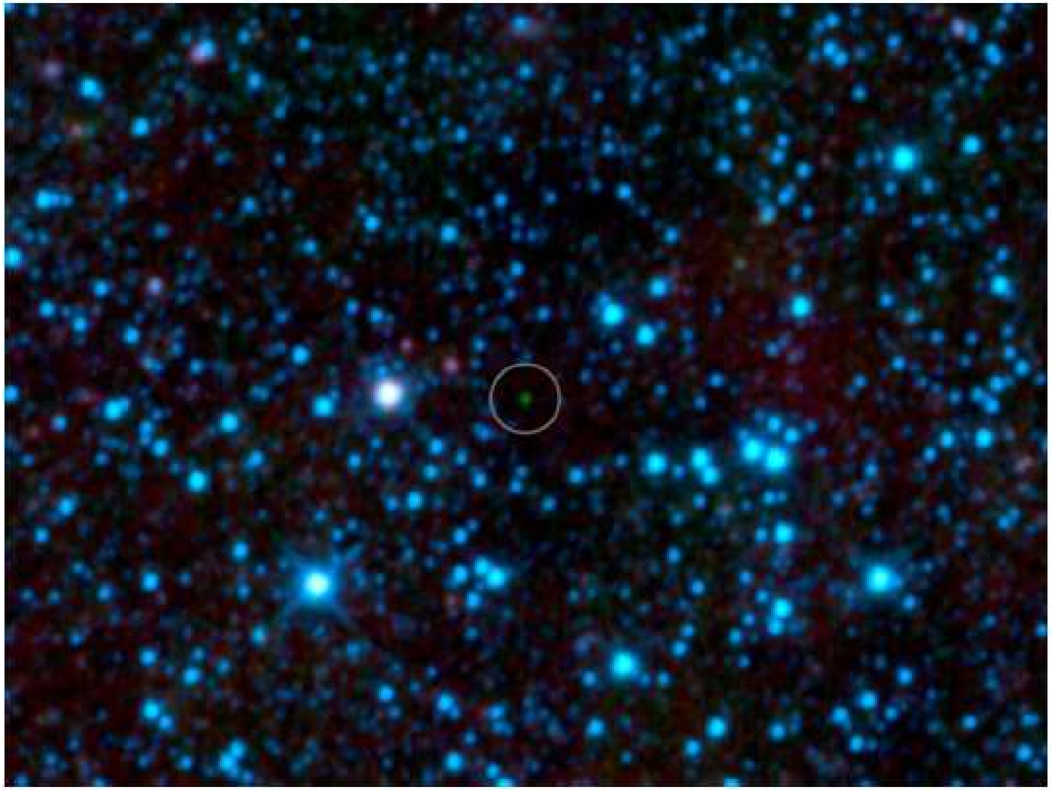
  not detected at visible wavelengths

Kirkpatrick + 13 (ApJ, 776, 128 'Discovery of the Y1 dwarf J064723.23-623235.5')

https://en.wikipedia.org/wiki/Stellar_classification
http://www.nasa.gov/mission_pages/WISE/multimedia/pia14720.html
http://science.nasa.gov/science-news/science-at-nasa/2011/23aug_coldeststars/

Extended spectral types

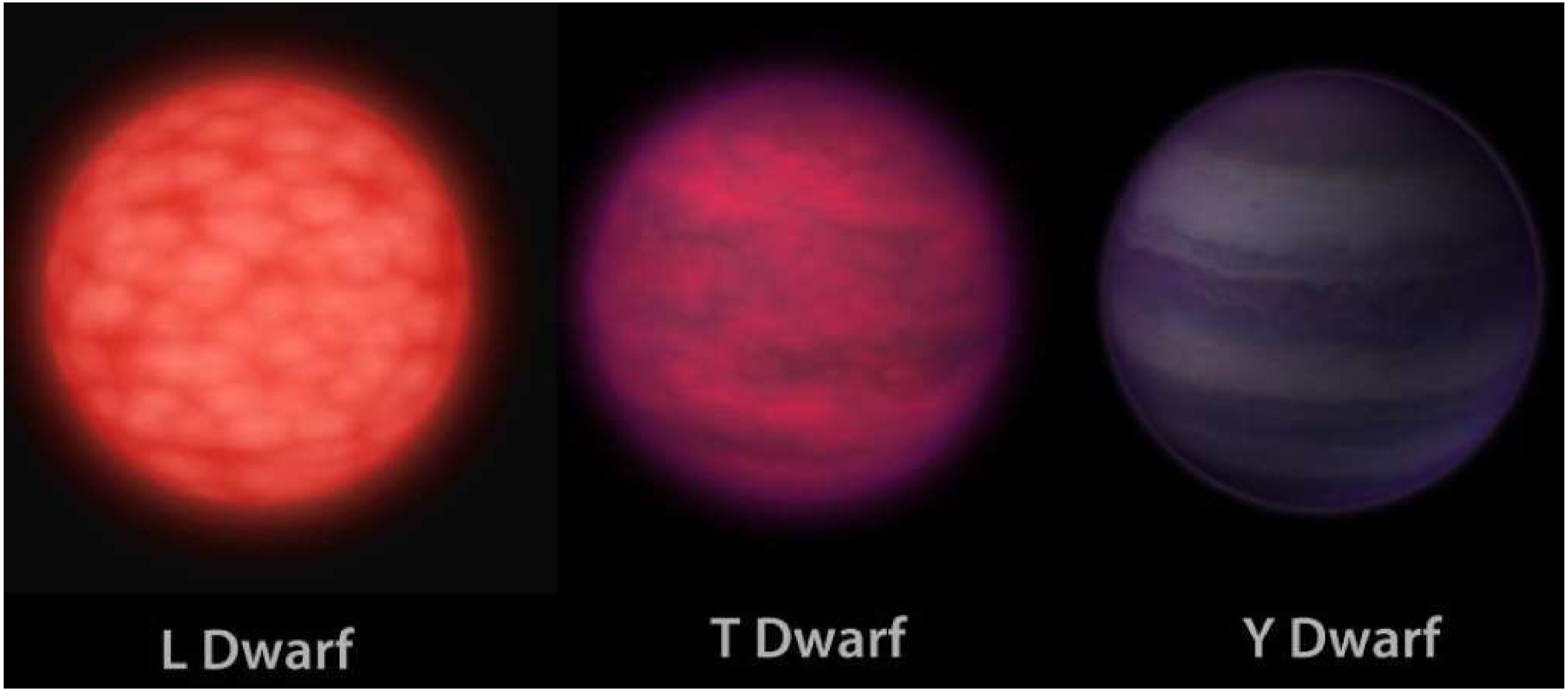
- WISE (Wide-field Infrared Survey Explorer) → found ~100 new BDs → 6 Y stars
- Coldest : WISE 1828+2650, T~300 K (25°C)



Y dwarf WISE 1828+2650
- artist's impression
- purple color choice : artistic reason

https://en.wikipedia.org/wiki/Stellar_classification
http://science.nasa.gov/science-news/science-at-nasa/2011/23aug_coldeststars/

Extended spectral types



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