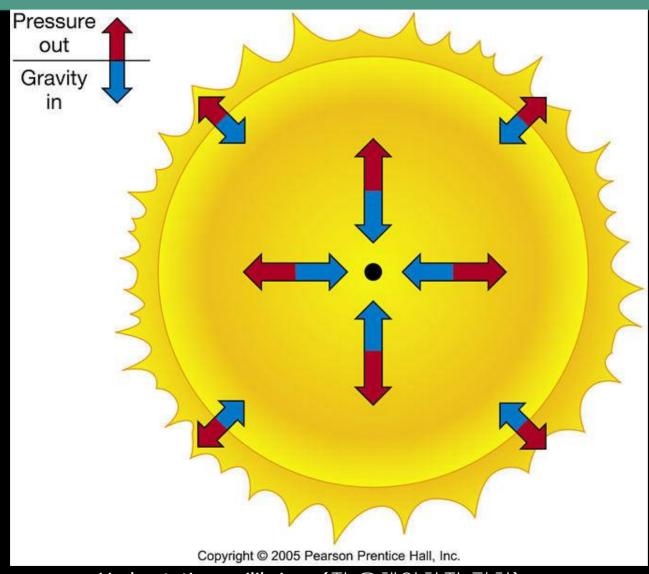
2. The Evolution of Stars (별의 진화) 2-1 Energy Generation (에너지 생성)



Hydrostatic equilibrium (정 유체역학적 평형)

https://pages.uoregon.edu/jimbrau/BraulmNew/Chap16/FG16_06.jpg

김상철 (Sang Chul KIM)

Main Sequence (MS, 주계열성)

- Nuclear fusion (proton-proton chain, 양성자-양성자 연쇄반응) → energy generation and radiation
- Mass decreases slowly → almost constant luminosity (equilibrium between pressure and gravity)
- core: N(H) decreases, N(He) increases
- M > 1.5 M $_{\odot}$, T_{center. \odot} > 1.5 × 10⁷ K \rightarrow H burning by CNO cycle (탄소 순환반응)

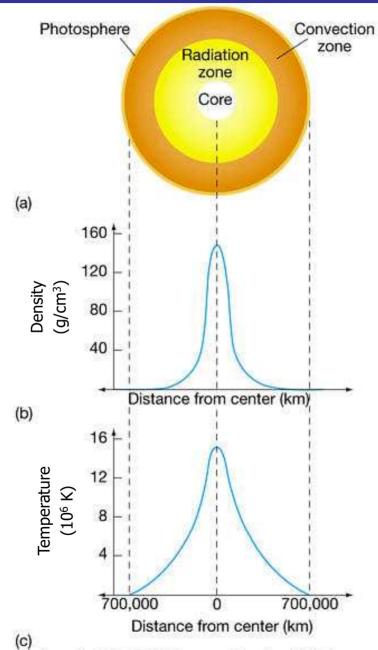
Hydrostatic equilibrium (정 유체역학적 평형)

• If somehow core H-burning accelerates --> Core T \uparrow , P \uparrow \rightarrow star expands

Expansion makes T ↓ → H-burning decelerates

Hydrostatic equilibrium makes H-burning speed keep ~constant

Interior structure of the Sun (태양의 내부 구조)



Why H-burning occurs at the core - 1

Low temperature: small speeds





Low Temp, small speeds

→ Electrical repulsion > proton-proton fusion

Why H-burning occurs at the core - 2

High temperature: large speeds



 \oplus

High Temp, large speeds

- → Strong nuclear force (강한 핵력)
- → Nuclei fuse, energy released

symbol

$${}_{Z}^{A}X$$

X: the chemical symbol of the element (e.g.: H, He, ...)

Z: the number of protons (the total positive charge, in units of e)

A: the mass number (the total number of nucleons, protons plus neutrons)

A = Z+N
 (mass number = Z protons + N neutrons)

$$^{(e.g.)}_{1}H$$
 $^{4}_{2}He$

```
H atomic weight: 1.0078
                                                                         E = mc^2 (Einstein's equation for the
                                                                         equivalence of mass and energy)
          4 H \rightarrow 4.0312
          1 He \rightarrow 4.0026
          \trianglem = 0.0286 (mass deficit/defect, 질량 결손)
\triangle m = 4 \times m(p) - m(He)
       = (0.0286 \times 1.67 \times 10^{-24} \text{g}) \times (3 \times 10^{10} \text{ cm/s})^2
       = 4.3 \times 10^{-5} \text{ erg}
       = 4.3 \times 10^{-12} J
                                          1 Joule = 1 \text{ kg} \cdot \text{m}^2/\text{s}^2
                                          = 1 N·m
                                          = 10^7 \text{ erg}
                                          = 6.24 \times 10^{18} \text{ eV}
                                                                                                                             Released
                                          = 0.2390 cal
                                                                                                                               energy
                                          = 2.78 \times 10^{-7} \text{ kW} \cdot \text{h}
```

4 protons

1 He nucleus (2 protons +

2 neutrons)

- Energy from coal 1 kg \sim 5000 kcal = 2.1 \times 10⁷ J
- Use H 1 kg to produce He
 - → 0.993 kg He produces, 0.007 kg changes into E

$$\rightarrow$$
 E = mc² = 7 g × (3 × 10¹⁰ cm/s)² = 7 × 9 × 10²⁰ g cm²/s²
= 6.3 × 10²¹ erg = 6.3 × 10¹⁴ J

 \rightarrow same as E from 3 \times 10⁷ kg = 30,000 tons of coal

Sun : 4×10^{38} protons/sec = 6.68×10^{14} g/sec are consumed. 2×10^{38} neutrinos/sec are generated.

Sun : $1 L_{\odot} = 3.9 \times 10^{33} \text{ erg/s} = 3.9 \times 10^{26} \text{ J/s}$

$$1 L_{\odot} = 3.9 \times 10^{33} \, \text{erg/s} = 3.9 \times 10^{26} \, \text{J/s}$$

= amount of electricity for all human beings can use for 10^7 years

Assuming:

Mankind populations = $5 \times 10^9 \rightarrow 10^9$ families (assume 1 family = 5 members)

Monthly family electricity uses, home use: 200~250 kW·h

Let's assume ~1000 kW·h/month including commercial use, etc

 $= 10^6 \text{ W} \times 3600 \text{ s/month} = 10^6 \text{ J/s} \times 3600 \text{ s/month} = 3.6 \times 10^9 \text{ J/month}$

$$1 W = 1 J/s$$

Monthly mankind electricity uses $\sim 3.6 \times 10^9 \text{ J} \times 10^9 \text{ families} = 3.6 \times 10^{18} \text{ J}$

$$\rightarrow \frac{3.9 \times 10^{26} \text{J}}{3.6 \times 10^{18} \text{J}} = 1.1 \times 10^8 \text{ months} = 9.2 \times 10^6 \text{ years} \sim 10^7 \text{ years}$$

Atomic weight (원자량, 原子量) or relative atomic mass (상대 원자 질량):

$$H \rightarrow 1$$

12
C →12 (1.998467052×10⁻²³ g) (since 1962),

then H
$$\rightarrow$$
 1.0078
He \rightarrow 4.0026

 α -ray, α -particle : He nucleus

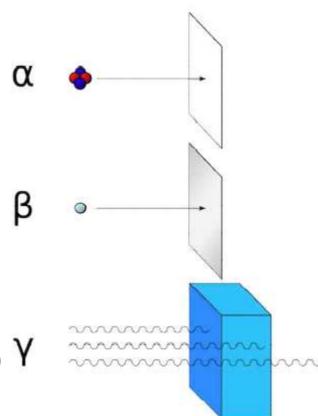
→ cannot penetrate a paper

 β -ray : electron

→ cannot penetrate aluminum

 γ -ray : high-energy photon

→ absorbed by dense materials (water, lead) Y



β(beta)-decay

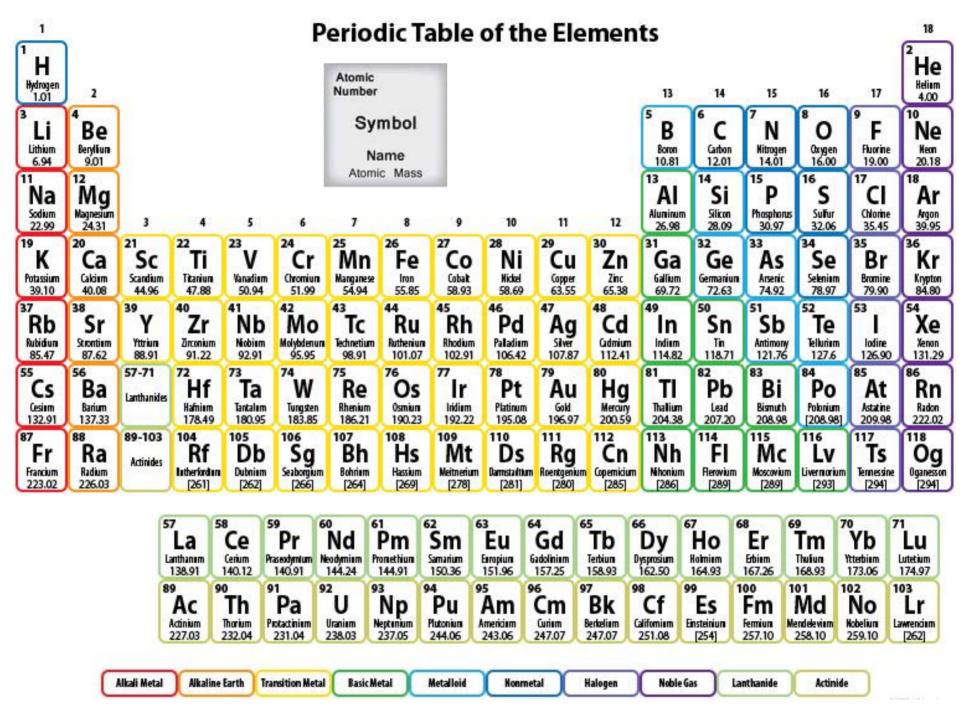
$$\beta$$
 decay : $n \rightarrow p + \beta + \overline{\nu_e}$

$$\beta^+$$
 decay : p \rightarrow n + β^+ + ν_e

$$\times \beta^- = e^-$$
 (electron)

$$\times \beta^+ = e^+$$
 (positron)

inverse-
$$\beta$$
 decay : $p^+ + e^- \rightarrow n + \nu$ (IBD)



Energy generation rate

H atomic weight: 1.0078
 4 H → 4.0312
 1 He → 4.0026
 △m = 0.0286

- $0.0286/4.0312 = 0.0071 \rightarrow 0.71\%$
- Only H in the core → T, P high enough to permit nuclear reactions → ~10 %
 of the mass of the Sun is available for energy conversion
- Thermonuclear energy available in the Sun :

$$L_{\odot} = 3.90 \times 10^{33} \text{ erg/s} = 3.90 \times 10^{26} \text{ J/s}$$

 $\rightarrow E/L_{\odot} = \text{Solar lifetime} = 8.11 \times 10^{9} \text{ yr} \sim 10 \text{ Gyr}$

Energy generation rate

** AGN → efficiency of conversion from mass to energy ~10% (η=0.1)
 (see, e.g., Fabian & Rees 1995, MNRAS, 277, L55,
 http://phys.huji.ac.il/~joaw/winterschool/heckman_1.pdf)

 \otimes Gravitational wave (e.g, by merging of two identical black holes) → conversion efficiency ~30% (η~0.3)

(FBlack Hole Physics 1991, Edited by Venzo de Sabbata, Zhenjiu Zhang, NATO ASI Series, Vol. 364, p. 139)

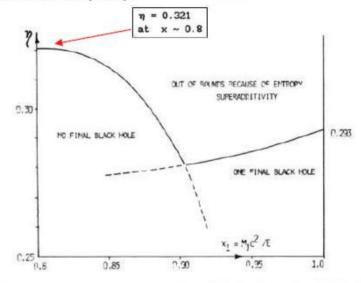
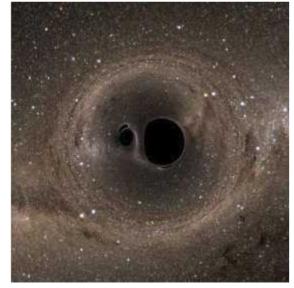


Figure 8. The maximum possible efficiency of gravitational wave energy production by the merging of two identical Schwarzschild black holes. The curves intersect at $x_1 \sim 0.903$, $\eta \sim 0.281$.



http://news.nationalgeographic.com/2016 /02/160211-gravitational-waves-foundspacetime-science/



Energy generation rate

```
MS Lifetime : \tau=10<sup>10</sup>(M/L) yr (M=stellar mass, L=stellar luminosity) 

** Mass-Luminosity Relation : L/L_{\odot} = (M/M_{\odot})^{4} \quad \text{for M} > 0.4M_{\odot}
L/L_{\odot} = (M/M_{\odot})^{2.3} \quad \text{for M} < 0.4M_{\odot}
\to \tau = 10^{10} (M/M^{4}) \text{ yr } = 10^{10} / \text{ [M(M_{\odot})]}^{3} \text{ yr}
1 \text{ M}_{\odot} \to 10^{10} \text{ yr}
10 \text{ M}_{\odot} \to 10^{7} \text{ yr}
```

O stars (the most massive stars) → a million years
"we are seeing some O stars!" = SF is still occurring in the MW

Main-sequence Lifetimes

http://www.ifa.Hawaii.edu/~szapudi/astro110/2007/ch21.pdf

Mass (M _☉)	Effective Temperature (K)	Spectral Class	Luminosity (L _o)	MS Lifetime (10 ⁶ yr)
25	35,000	0	80,000	3
15	30,000	В	10,000	15
3	11,000	Α	60	500
1.5	7000	F	5	3000
1.0	6000	G	1	10,000
0.75	5000	K	0.5	15,000
0.50	4000	M	0.03	200,000

Proton-proton (PP) fusion chain process

```
1st step: {}^{1}H + {}^{1}H \rightarrow {}^{2}H + e^{+} + \nu_{e} (\rightarrow1.44 MeV)
               ^{1}H + ^{1}H \rightarrow ^{2}H + e^{+} + \nu_{e} \leftarrow \text{weak nuclear force}
                (It takes 5 \times 10^9 years for a given proton to undergo this reaction.)
2^{\text{nd}} step: {}^{2}\text{H} + {}^{1}\text{H} \rightarrow {}^{3}\text{He} + \gamma
                                                      (\rightarrow 5.49 \text{ MeV})
                                                               (occurs in \sim 1 s)
                ^{2}H + ^{1}H \rightarrow ^{3}He + \gamma
3^{rd} step: {}^{3}He + {}^{3}He \rightarrow {}^{4}He + {}^{1}H + {}^{1}H \quad (\rightarrow 12.9 \text{ MeV})
                                                               ← strong nuclear force
                                                              (It takes \sim 3 \times 10^5 years.)
 {}^{1}H = p : proton
 <sup>2</sup>H: deuterium (중수소) = p + n
 e+: positron (e-의 반물질 antimatter, same mass,
                                         positive charge)
 v: neutrino (energy, spin, very small mass)
   ν<sub>e</sub>: electron neutrino
 ^{3}He: helium-3 nucleus = 2p + 1n
 y: photon
 ^{4}He: helium-4 nucleus = ^{2}p + ^{2}n
 \rightarrow 91% of the time in the Sun
```

Proton-proton (PP) fusion chain process

$${}^{1}_{1}H + {}^{1}_{1}H \longrightarrow {}^{2}_{1}H + e^{+} + v_{e}$$

$${}^{2}_{1}H + {}^{1}_{1}H \longrightarrow {}^{3}_{2}He + \gamma$$

$${}^{69}_{69}$$

$${}^{31}_{60}$$

$${}^{3}_{2}He + {}^{3}_{2}He \longrightarrow {}^{4}_{2}He + 2{}^{1}_{1}H$$

$${}^{3}_{2}He + {}^{4}_{2}He \longrightarrow {}^{7}_{4}Be + \gamma$$

$${}^{(PP I)}$$

$${}^{99.7}_{60}$$

$${}^{7}_{4}Be + e^{-} \longrightarrow {}^{7}_{3}Li + v_{e}$$

$${}^{7}_{4}Be + {}^{1}_{1}H \longrightarrow {}^{8}_{5}B + \gamma$$

$${}^{7}_{3}Li + {}^{1}_{1}H \longrightarrow {}^{2}_{2}He$$

$${}^{8}_{4}Be \longrightarrow {}^{8}_{4}Be + e^{+} + v_{e}$$

$${}^{8}_{4}Be \longrightarrow {}^{2}_{2}He$$

$${}^{8}_{4}Be \longrightarrow {}^{2}_{2}He$$

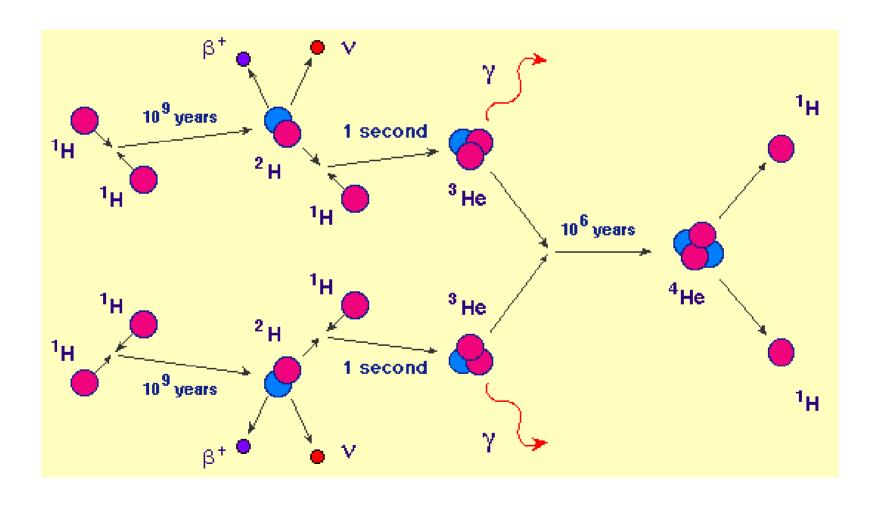
$${}^{99.11}_{(Lithium burning)}$$

$${}^{(PP III)}_{(Lithium burning)}$$

$${}^{(PP III)}_{(PP III)}$$

Why this complicated process?

- Direct collision of 4 H atoms to produce He → probability is very low
- Relatively, 2-body collision is more often!



proton-proton (PP) fusion chain process

Proton-proton fusion chain process



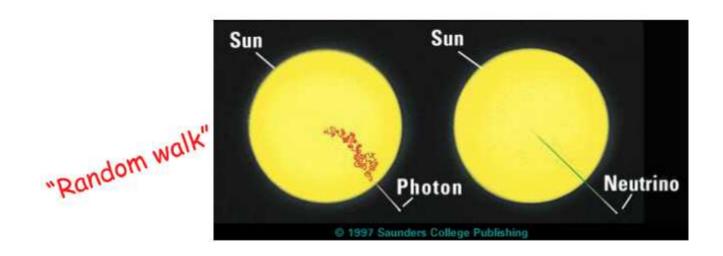


1st step: In two separate reactions, 2 protons in each reaction fuse

- 1st step : $p + p -> \beta^+ + \nu + {}^2H$
- 2^{nd} step : ${}^{2}H + p --> {}^{3}He + \gamma$
- 3^{rd} step : 3 He + 3 He --> 4 He + p + p

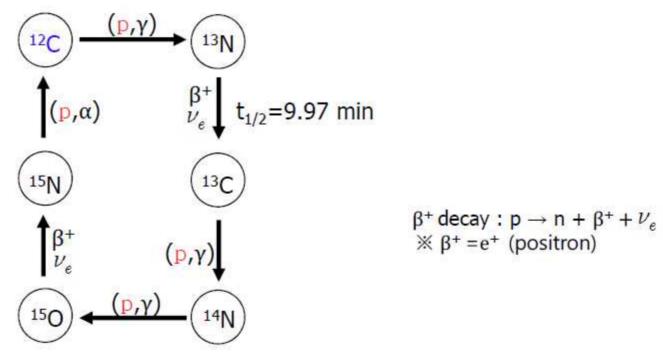
Photon, neutrino – escape from the Sun

Photon and neutrino – travel times out of the center of the Sun 10^4 - 10^5 yr 2 sec



CNO Cycle

- Carbon = catalyst : a substance that causes a chemical reaction to happen more quickly, while the substance not consumed and remain unchanged
- 촉매(觸媒): 반응과정에서 소모되거나 변화되지 않으면서 반응속도를
 빠르거나 느리게 변화시키는 물질



- Start : C + p
- At high-temp stars : T > 1.6 \times 10⁷ K, M > 1.1 M $_{\odot}$

CNO cycle process

$$^{12}\text{C} + ^{1}\text{H} \rightarrow ^{13}\text{N} + \gamma$$

$$^{13}N \rightarrow ^{13}C + e^+ + \nu_e$$
 ^{13}N : unstable isotope

$$^{13}\text{C} + ^{1}\text{H} \rightarrow ^{14}\text{N} + \gamma$$

$$^{14}N + ^{1}H \rightarrow ^{15}O + \gamma$$

$$^{15}O \rightarrow ^{15}N + e^{+} + \nu_{e}$$

 $^{15}O \rightarrow ^{15}N + e^+ + \nu_e$ ^{15}O : unstable isotope

$$^{15}N + ^{1}H \rightarrow ^{12}C + ^{4}He$$

CNO cycle process

$$^{12}\text{C} + ^{1}\text{H} \rightarrow ^{13}\text{N} + \gamma$$
 (1.95 MeV)

$$^{13}N \rightarrow ^{13}C + e^{+} + \nu_{e}$$
 (1.20 MeV, ^{13}N half-life=9.965^m)

$$^{13}\text{C} + ^{1}\text{H} \rightarrow ^{14}\text{N} + \gamma$$
 (7.54 MeV)

$$^{14}N + ^{1}H \rightarrow ^{15}O + \gamma$$
 (7.35 MeV)

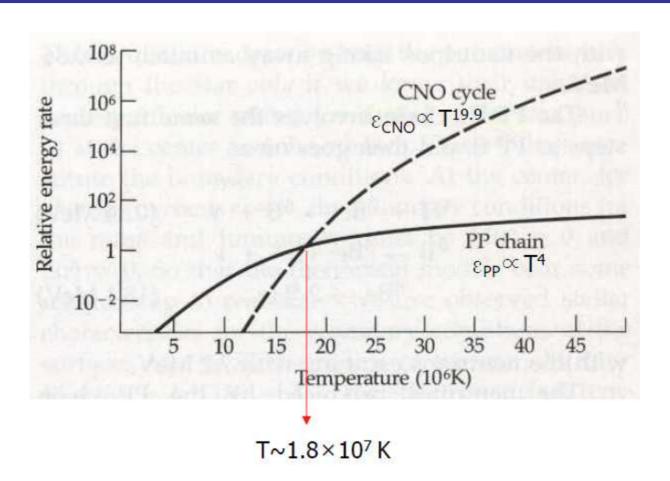
$$^{15}\text{O} \rightarrow ^{15}\text{N} + \text{e}^+ + \nu_{\text{e}}$$
 (1.73 MeV, ^{15}O half-life=122.24s)

$$^{15}N + ^{1}H \rightarrow ^{12}C + ^{4}He$$
 (4.96 MeV)

※ 2 positrons annihilate with 2 ambient electrons → produce 2.04 MeV

Total 24.73 + 2.04 = 26.73 MeV

Energy-generation rates



Triple-alpha (3 α) process

Nucleosynthesis using He:

T \geq 10⁸ K, $\rho \geq$ 10⁵ g cm⁻³ : He \rightarrow heavier elements

$$^{4}\text{He} + ^{4}\text{He} \Leftrightarrow ^{8}\text{Be} + \gamma$$

* 8Be lifetime $\sim 2.6 \times 10^{-16}$ s

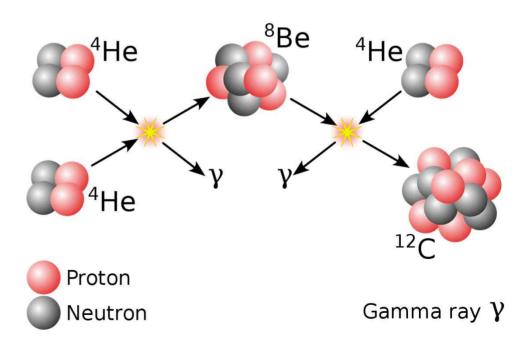
> mean collision (scattering) time of α -particle ($T_{scattering}$)

Huge amount of He, $n(^{8}Be) : n(^{4}He) = 1 : 10^{9}$

⁸Be + ⁴He → ¹²C +
$$\gamma$$

[†]

"Triple- α process"



C, O-burning

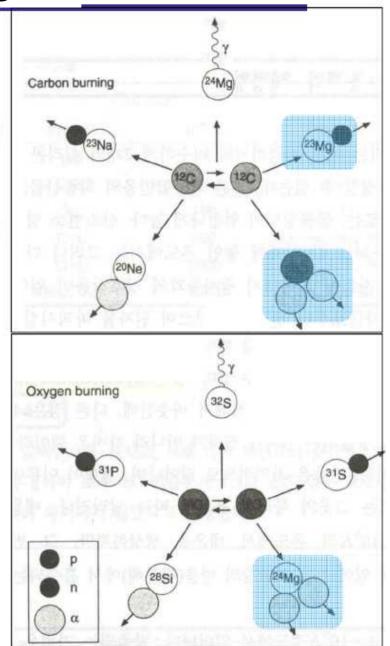
T
$$\geq$$
 5×10⁸ K \rightarrow C-burning

 $^{12}\text{C} + ^{12}\text{C} \rightarrow ^{24}\text{Mg} + \gamma$ (13.933 MeV)
 $\rightarrow ^{23}\text{Mg} + n$ (-2.599 MeV) (endothermic)
 $\rightarrow ^{23}\text{Na} + p$ (2.241 MeV)
 $\rightarrow ^{20}\text{Ne} + \alpha$ (4.617 MeV)
(E) $\rightarrow ^{16}\text{O} + 2\alpha$ (-0.113 MeV) (endothermic)
평균 방출에너지 \approx 13 MeV
 \sim 5.2 x 10¹³ J/kg = 5.2 x 10¹⁷ erg/g

T
$$\geq$$
 1×10⁹ K \rightarrow O-burning

 $^{16}O + ^{16}O \rightarrow ^{28}Si + \alpha \quad (9.954 \text{ MeV}) \ (\sim 60\%)$
 $\rightarrow ^{31}P + p \quad (7.678 \text{ MeV}) \ (\sim 40\%)$
 $\rightarrow ^{31}S + n \quad (1.500 \text{ MeV})$
 $\rightarrow ^{32}S + \gamma$
 $\rightarrow ^{24}Mg + 2\alpha \quad \text{(endothermic)}$

평균 방출에너지 $\approx 16 \text{ MeV}$
 $\sim 4.8 \times 10^{13} \text{ J/kg} = 4.8 \times 10^{17} \text{ erg/g}$

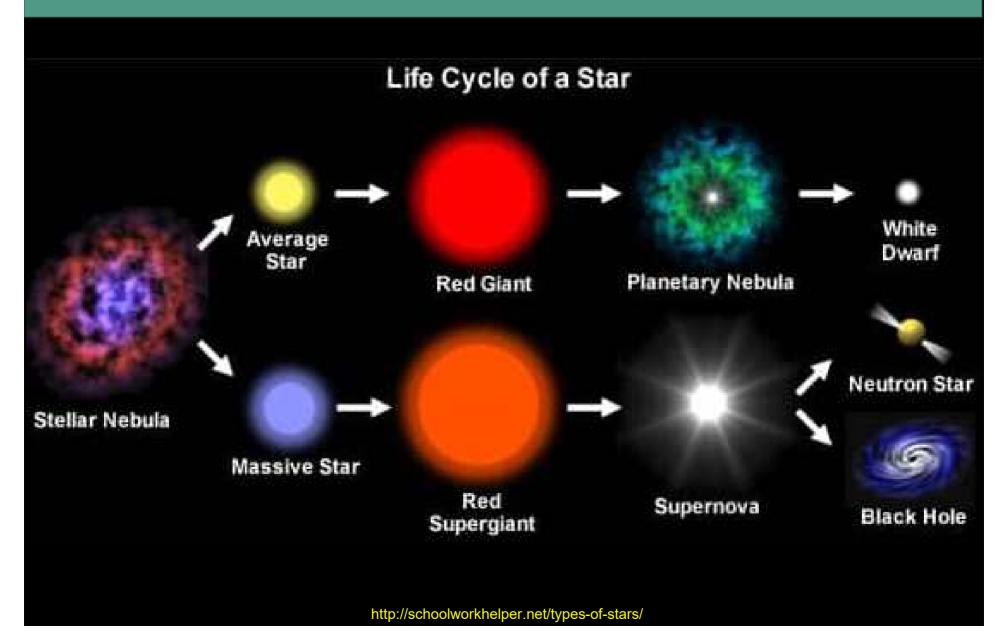


Si-burning

- After O-burning, core = Si + S
- T ~ $(2.7-3.5) \times 10^9$ K (depends on mass)
- Duration ~ 2 weeks
- No further fusion is possible.

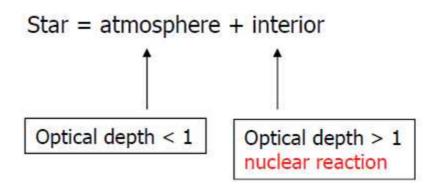
$$^{28}_{14}\text{Si}$$
 + $^{4}_{2}\text{He}$ \rightarrow $^{32}_{16}\text{S}$
 $^{32}_{16}\text{S}$ + $^{4}_{2}\text{He}$ \rightarrow $^{36}_{18}\text{Ar}$
 $^{36}_{18}\text{Ar}$ + $^{4}_{2}\text{He}$ \rightarrow $^{40}_{20}\text{Ca}$
 $^{40}_{20}\text{Ca}$ + $^{4}_{2}\text{He}$ \rightarrow $^{44}_{22}\text{Ti}$
 $^{44}_{22}\text{Ti}$ + $^{4}_{2}\text{He}$ \rightarrow $^{48}_{24}\text{Cr}$
 $^{48}_{24}\text{Cr}$ + $^{4}_{2}\text{He}$ \rightarrow $^{52}_{26}\text{Fe}$
 $^{52}_{26}\text{Fe}$ + $^{4}_{2}\text{He}$ \rightarrow $^{56}_{28}\text{Nii}$

2. The Evolution of Stars (별의 진화) 2-2 Stellar Evolution (항성 진화)



Sun + Star

Solar surface composition: X=0.73, Y=0.25, Z=0.02



imes Optical depth, $au_{\lambda} : d au_{\lambda} = -\kappa_{\lambda} \,
ho \, ds$

 $au_{\lambda}\gg 1$: optically thick

 $au_{\lambda} \ll 1$: optically thin

1.0 Ro Thermonuclear core

Sun's interior

 $\times \kappa_{\lambda}$: absorption coefficient (opacity)

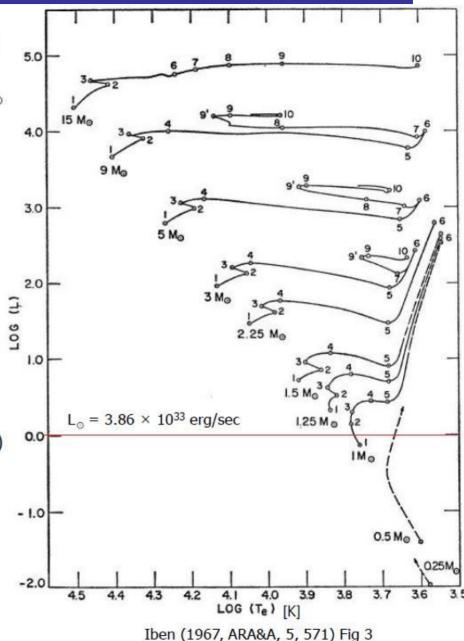
Post-MS Stellar Evolution

Hertzsprung-Russell Diagram of Metal-rich stars (X=0.708, Y=0.272, Z=0.020)

 $M = 15, 9, 5, 3, 2.25, 1.5, 1.25, 1, 0.5, 0.25 M_{\odot}$

Dashed lines: estimates

• Sun's L, R, T: increased steadily since it reached the zero-age main sequence (ZAMS) ~4.5 Gyr ago



Solar Evolution

Sun's center, during its lifetime :

 $X: 0.71 \rightarrow 0.34$ $Y: 0.27 \rightarrow 0.64$

changing the composition and structure

The change in the Sun's central composition

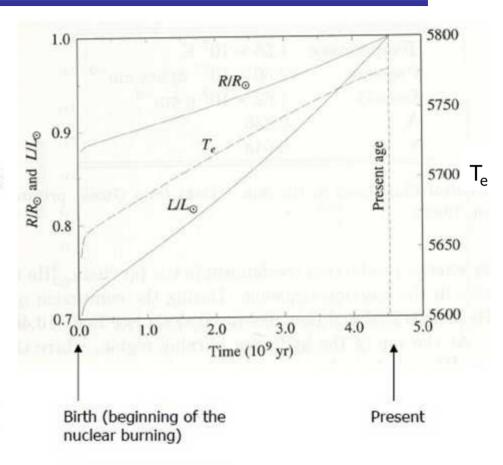
→direct influence on observable L, T_{eff}, and R

L increased by 40% R increased by >10%

※ Physical parameters of the Solar center (standard solar model of Joyce Guzik)

Central conditions in the Sun

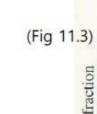
Tc	(1.56~) 1.58 ×10 ⁷ K
P _C	2.50×10 ¹⁷ dyne/cm ²
ρ_{C}	162 (150-160) g/cm ³
X_{C}	0.336
Yc	0.643



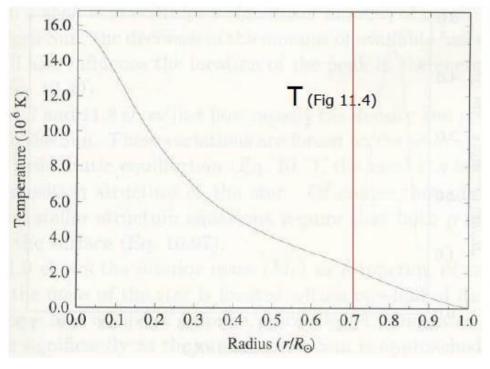
L: 1.43 times increase

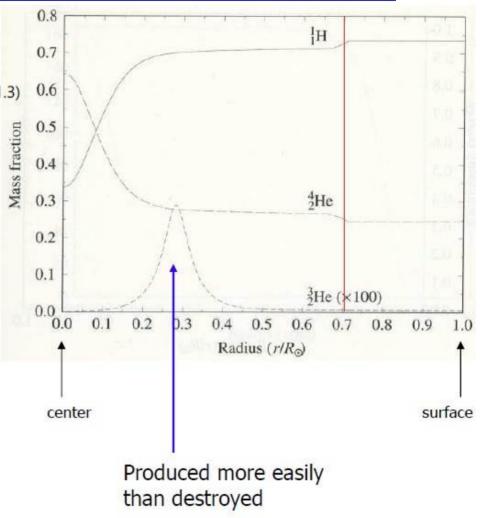
Solar composition structure

³He: intermediate species in the pp chain reaction sequence



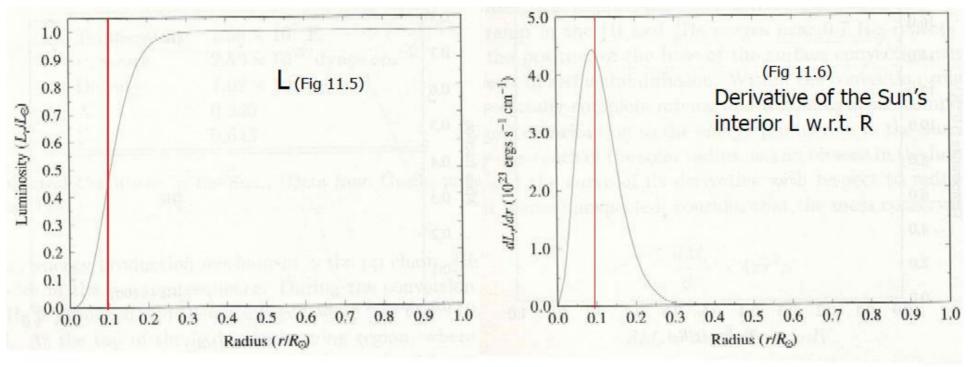
Solar Temp structure





Interior Lum of the Sun

Location of the greatest contribution to the E output



Though amount of E liberated per gram of material (ε) decreases steadily from R=0 outward

→ Largest contribution to the total L – in a shell that contains a significant amount of mass

Post-MS Stellar Evolution

TABLE III STELLAR LIFETIMES (yr)a

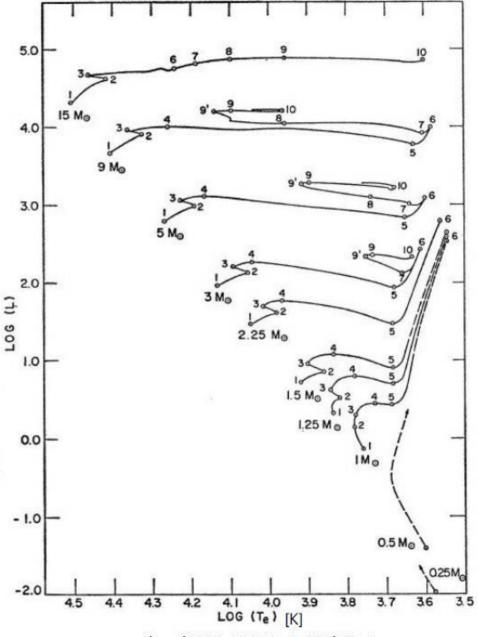
Interval $(i-j)$ Mass (M_{\odot})	(1-2	2)	(2-3	3)	(3-	1)	(4-5	5)	(5-6	5)
15	1.010	(7)	2.270	(5)			7.55	(4)		
9	2.144	(7)	6.053	(5)	9.113	(4)	1.477	(5)	6.552	(4)
5	6.547	(7)	2.173	(6)	1.372	(6)	7.532	(5)	4.857	(5)
3	2.212	(8)	1.042	(7)	1.033	(7)	4.505	(6)	4.238	(6)
2.25	4.802	(8)	1.647	(7)	3.696	(7)	1.310	(7)	3.829	(7)
1.5	1.553	(9)	8.10	(7)	3.490	(8)	1.049	(8)	≥2	(8)
1.25	2.803	(9)	1.824	10.541.501		1/5/081/		10.7000000	00000 - 00000000	(8)
1.0	7	(9)		100000	1.20	0.50020		1000 A		(9)

Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.

TABLE IV STELLAR LIFETIMES (yr)*

Interval (i-j) Mass (Mo)	(6–7)	(7–8)	(8-9)	(9–10)
15	7.17 (5)	6.20 (5)	1.9 (5)	3.5 (4)
9	4.90 (5)	9.50 (4)	3.28 (6)	1.55 (5)
5	6.05 (6)	1.02 (6)	9.00 (6)	9.30 (5)
3	2.51 (7)	4.0	8 (7)	6.00 (6)

^{*} Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.



Post-MS Stellar Evolution

TABLE III STELLAR LIFETIMES (yr)^a

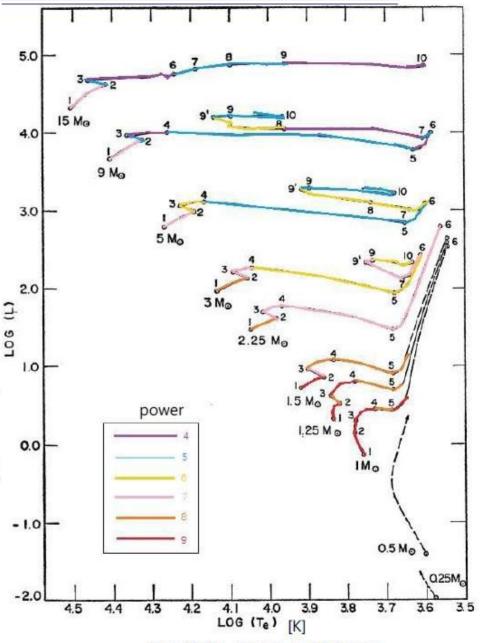
Interval $(i-j)$ Mass (M_{\odot})	(1-2	2)	(2-3	3)	(3-	1)	(4-	5)	(5-0	5)
15	1.010	(7)	2.270	(5)			7.55	(4)		
9	2.144	(7)	6.053	(5)	9.113	(4)	1.477	(5)	6.552	(4)
5	6.547	(7)	2.173	(6)	1.372	(6)	7.532	(5)	4.857	(5)
3	2.212	(8)	1.042	(7)	1.033	(7)	4.505	(6)	4.238	(6)
2.25	4.802	(8)	1.647	(7)	3.696	(7)	1.310	(7)	3.829	(7)
1.5	1.553	(9)	8.10	(7)	3.490	(8)	1.049	(8)	≥2	(8)
1.25	2.803	(9)	1.824	(8)	1.045	(9)	1.463	(8)	≥4	(8)
1.0	7	(9)		(9)	1.20	1000000	1.57	(8)	≥1	(9)

Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.

TABLE IV STELLAR LIFETIMES (yr)*

Interval (i-j) Mass (Mo)	(6–7)	(7–8)	(8-9)	(9–10)
15	7.17 (5)	6.20 (5)	1.9 (5)	3.5 (4)
9	4.90 (5)	9.50 (4)	3.28 (6)	1.55 (5)
5	6.05 (6)	1.02 (6)	9.00 (6)	9.30 (5)
3	2.51 (7)	4.08	3 (7)	6.00 (6)

Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.



Stellar Evolution – zoom in

- Evolutionary paths for pop I stars M = 1.5, 1.25, 1 ${\rm M}_{\odot}$
- Circled numbers: factors by which surface ⁷Li abundance has been depleted (relative to its MS value) 6708Å, 6104Å

(Times to reach circled points)
TABLE 1 EVOLUTIONARY LIFETIMES (109 yr)

Point	1 №⊙	1.25 M ⊙	1.50 M ⊙		
1 .	0 05060	0 02954	0 01821		
2	3 8209	1 4220	1 0277		
3	6 7100	2 8320	1 5710		
4	8 1719	3 0144	1 6520		
2 3 4 5	9 2012	3 5524	1 8261		
	9 9030	3 9213	1 9666		
7	10 195	4 0597	2 0010		
8	(G1000941060	4 1204	2 0397		
8	604 (e)	4 1593	2 0676		
10	10 352	4 2060	2 1059		
11	10 565	4 3427	2 1991		
12	10 750	4 4505	2 2628		
13	10 875	4 5349			

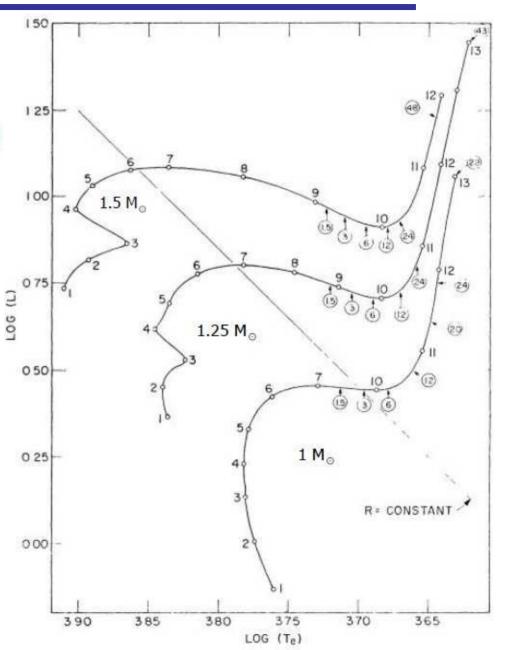


Fig 1

Stellar Evolution – zoom in

• Evolutionary paths for pop I stars $M = 1.5, 1.25, 1 M_{\odot}$

 Circled numbers: factors by which surface ⁷Li abundance has been depleted (relative to its MS value) 6708Å, 6104Å

(1) Solar surface lithium abundance : 140× less than the protosolar value

- (2) Temperature at the base of the surface convective zone : not hot enough to burn lithium
- → Li depletion process is needed (Israelian+09 Nature 462 189 - Enhanced lithium depletion in Sun-like stars with orbiting planets)

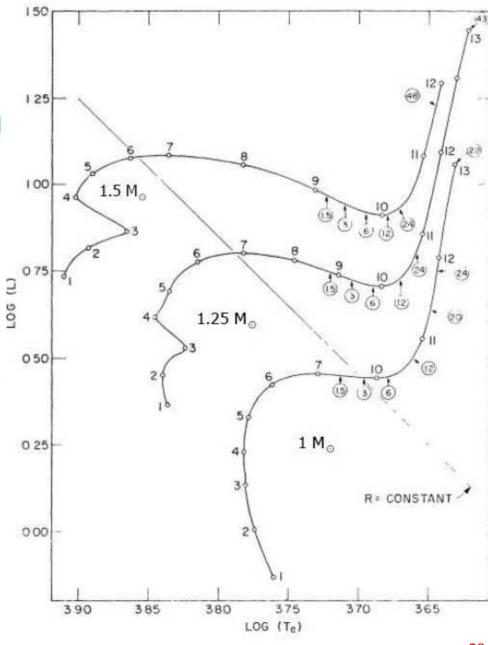


Fig 1

Stellar Evolution – zoom in

- As stellar mass \(\psi, \) the direction of evolution off the MS shifts from movement to the red to movement to the blue
- The phase of over-all contraction and increasing surface temperature (points 3 → 4): becomes less pronounced with M ↓, disappearing between 1.25 M_☉ and 1 M_☉ (core convection during the Hburning phase vanishes in this mass range)
- During the shell-narrowing phase (points 7 → 10), the drop in L decreases with M ↓

$$-\Delta(\log L) = 0.15, \quad 0.10, \quad 0.015$$

 $1.5 \ M_{\odot}, \ 1.25 \ M_{\odot}, \ 1 \ M_{\odot}$

 As mass ↓, the △L (increase) between points 1 and 7: increases

$$\Delta(\log L) = 0.35, \quad 0.44, \quad 0.69$$

 $1.5 M_{\odot}, \quad 1.25 M_{\odot}, \quad 1 M_{\odot}$

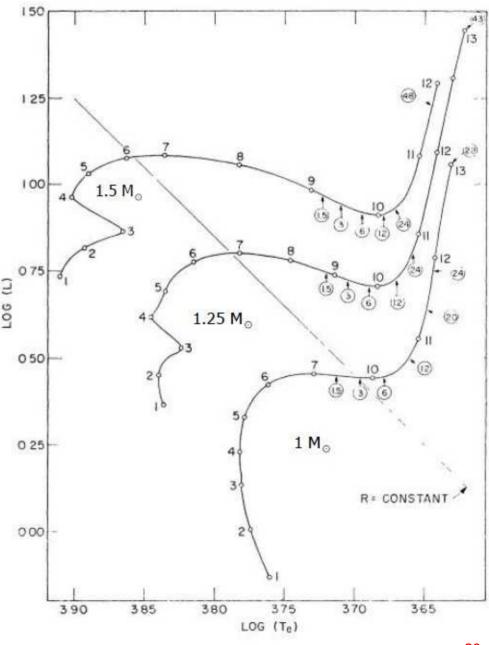
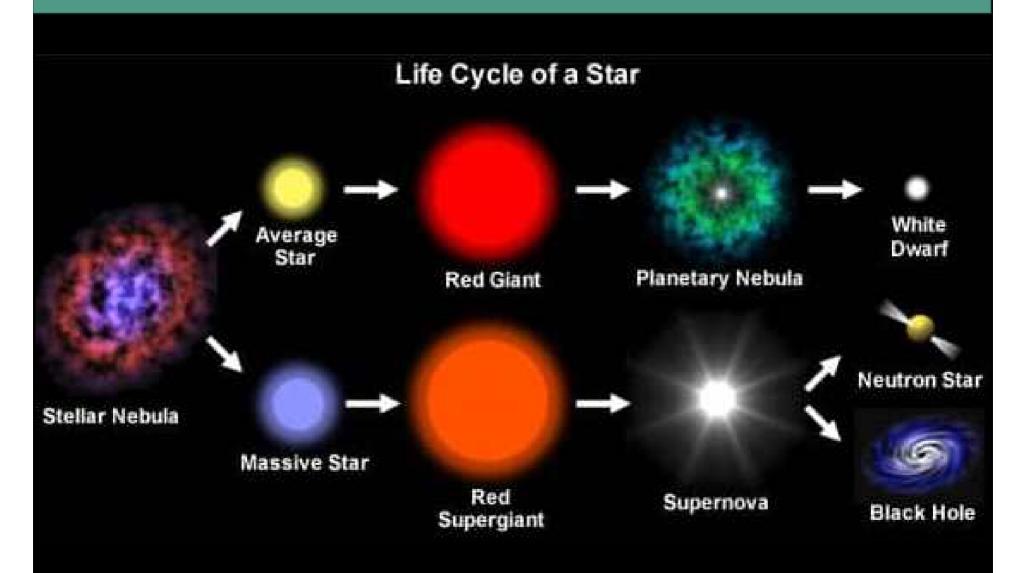


Fig 1

2. The Evolution of Stars (별의 진화) 2-3 Post-Main-Sequence Evolution (주계열 이후 진화)



Post-MS Stellar Evolution

D. Schaerer, C. Charbonnel, G. Meynet, A. Maeder and G. Schaller 1993 Astron. Astrophys. Suppl. Ser. 102, 339-342

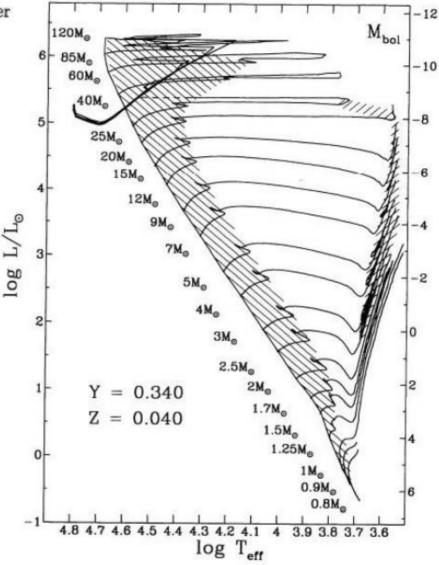
Grids of stellar models.

IV. From 0.8 to 120 M_{\odot} at Z = 0.040

Stellar evolution isochrones

- Padova
- Geneva
- VandenBerg
- Yonsei-Yale (Y²)
- Dartmouth
- MESA MIST Yunnan-III (Zhang+13 MN 428 3390)

Hatched areas: slow phases of nuclear burning



Schaerer et al (1993, A&AS, 102, 339) - Fig 1

Post-MS Stellar Evolution

D. Schaerer, C. Charbonnel, G. Meynet, A. Maeder and G. Schaller 1993 Astron. Astrophys. Suppl. Ser. 102, 339-342

Grids of stellar models.

IV. From 0.8 to 120 M_{\odot} at Z = 0.040

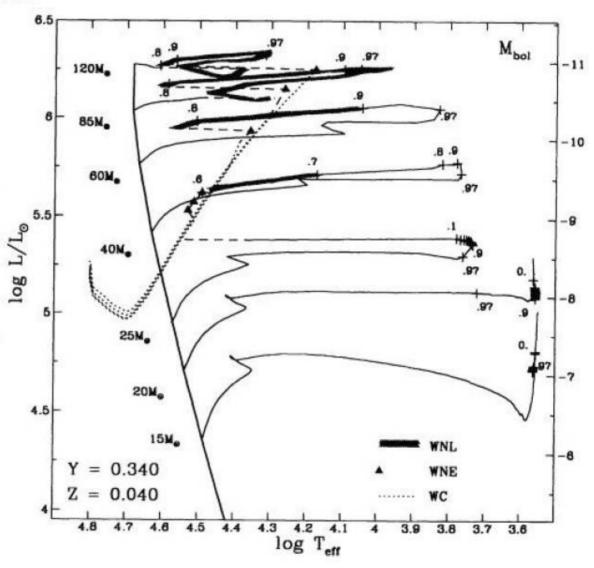
HRD of massive stars (15 – 120 M_{\odot}) with Z=0.040

Yc (central He content): 0.97, 0.90, 0.80, 0.70, 0.60, ---, 0.10, 0

Wolf-Rayet stars

- broad emission lines of highly ionized He and N or C
- very high surface enhancement of heavy elements, depletion of hydrogen
- strong stellar winds
- T_{eff} = 30,000 K 200,000 K

WN Early (WN2 – WN6) WN Late (WN6 – WN9) WC

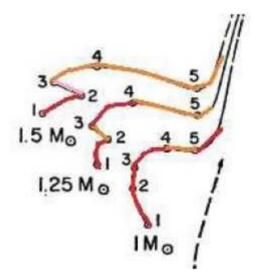


Schaerer et al (1993, A&AS, 102, 339) - Fig 3

Evolution beyond point 3

Maximum fraction of a star's mass
that can exist in an isothermal core + still support the overlying layers
= Schönberg-Chandrasekhar limit (1942)

$$\left(\frac{M_{ic}}{M}\right)_{\rm SC} \simeq 0.37 \left(\frac{\mu_e}{\mu_{ic}}\right)^2$$



where, $\mu = \langle m \rangle / m_H$: mean molecular weight (the average mass $\langle m \rangle$ in units of the mass of a hydrogen atom m_H)

Characteristics of MS Stars

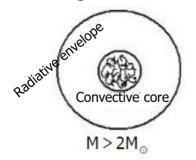
M > 1.5 M _☉	M <1.5 M _☉				
$T_c > 2 \times 10^7 \text{ K}$	$T_c < 2 \times 10^7 \text{ K}$				
CNO cycle	PP chain				
Energy production rate : $\epsilon_{CNO} \propto T^{19.9}$ > Production of most E near the center	$\epsilon_{CNO} \propto T^4> E$ source is not concentrated to the center				
core : convective	core : radiative				
envelope : radiation	envelope : H-convection				

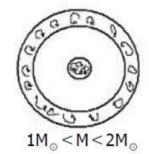
The more massive, the larger convective core.

mass

As mass decreases,

H-convection zone deepens.







http://www.maths.qmul.ac.uk/~svv/MTH725U/Lecture8.htm



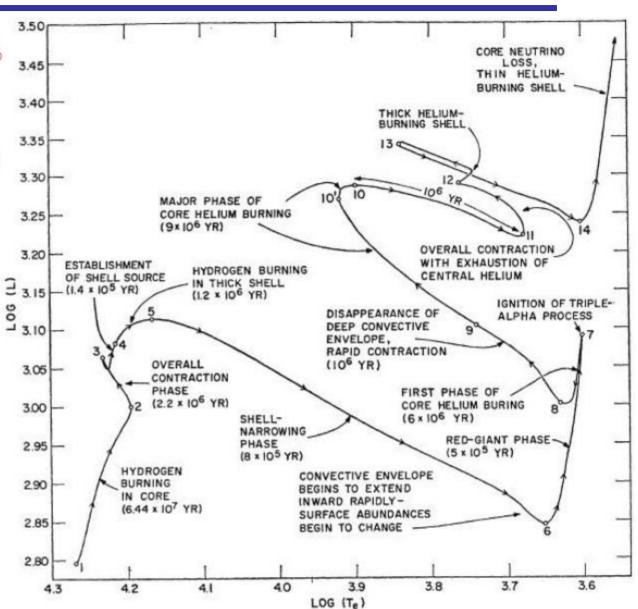




M<0.5M_o

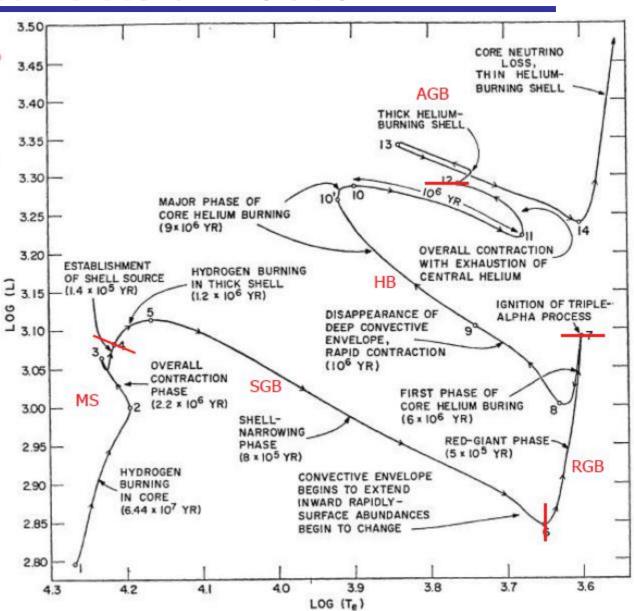
Post-MS Stellar Evolution

- Evolutionary path of a 5 M_o metal-rich star in the HRD
- From ZAMS
 to the asymptotic giant branch
 (AGB)

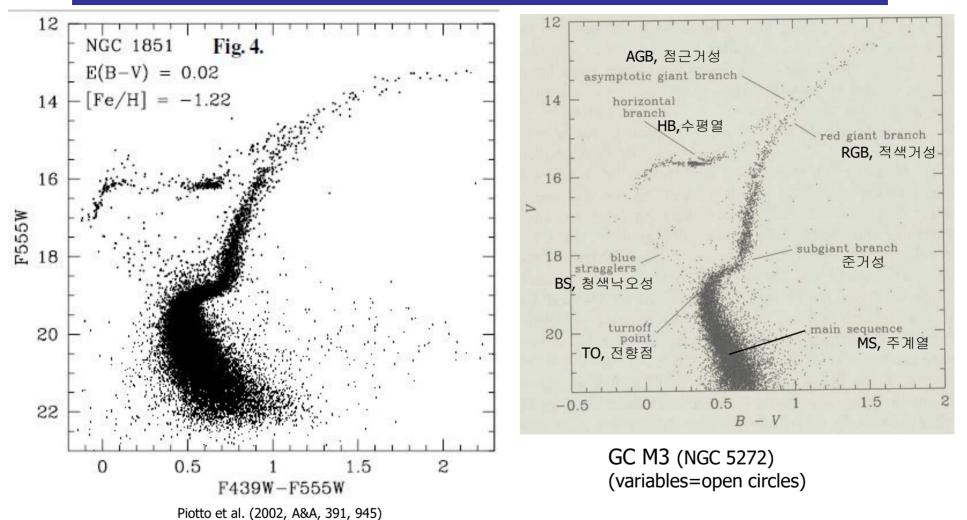


Post-MS Stellar Evolution

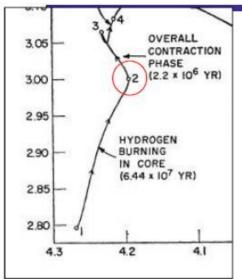
- Evolutionary path of a 5 M_o metal-rich star in the HRD
- From ZAMS
 to the asymptotic giant branch
 (AGB)



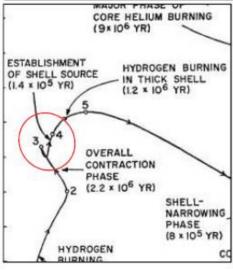
Color-Magnitude Diagrams for globular clusters (GCs)



5 M_o star - structure



- At point 2: near depletion of H fuel in the core
- During 2 → 3 : overall contraction (Core H mass fraction X : reduced to 0.01)

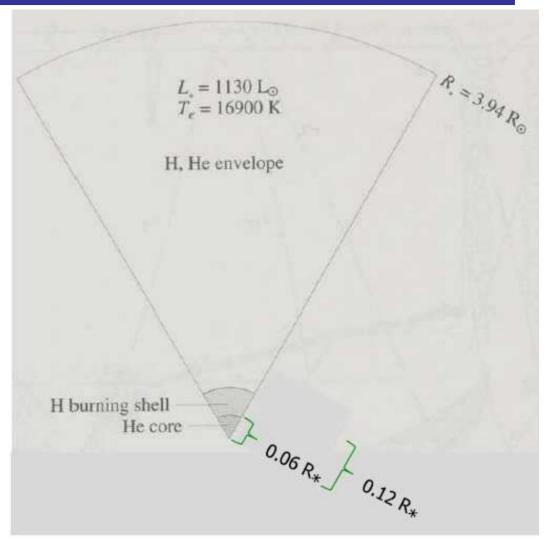


- During 3 → 4 : establishment of shell source H burning begins in a thick shell
- Rapid shell ignition → overlying envelope absorbs some or much of the E release by the shell → envelope slightly expands

5 M_☉ star approaching the RGB

Shortly after point 3

H shell burning



An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 498

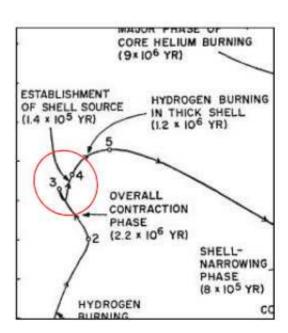
Evolution beyond point 3

- At this point,
- L (generated in the thick shell) > L (produced by the core during the core-H-b)
- → Evolutionary track continues to rise beyond point 3
- Some of the energy generated → goes into a slow expansion of the envelope
- T_{eff} decrease slightly, evolutionary track bends to the right

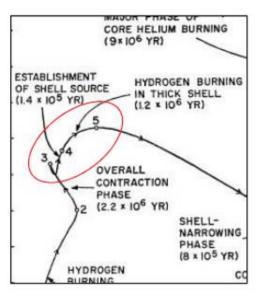
$$\frac{\text{(shell H-b time)}}{\text{(core H-b time)}} \propto \frac{1}{\text{mass}}$$

H-b shell continues to consume its nuclear fuel

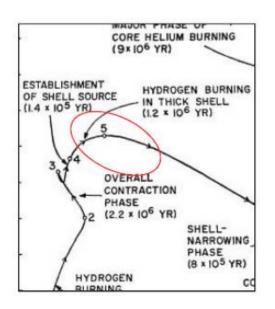
- → Isothermal He-core grows in mass Star moves farther to the red in the HRD
- → Redward locus = subgiant branch



Sub Giant Branch (SGB) : 5 M_☉ star

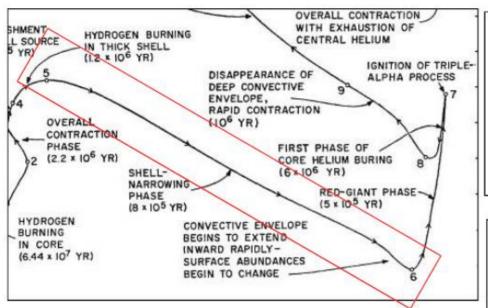


- During 3 → 5 : Shell continues to consume H
- → He-core : mass and size steadily increase
- → becomes nearly isothermal core
- At Point 5 → Schönberg-Chandrasekhar limit is reached
 - → Core begins to collapse
 - → Much faster evolution



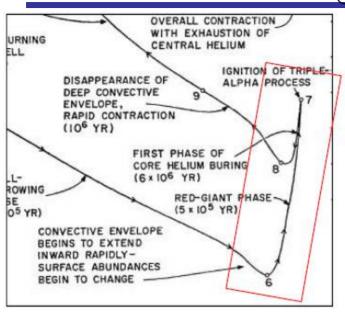
- At points from 5 :
 - Core begins to collapse → gravitational potential E releases
 - → T gradient re-appears
 - H-b shell : Τ, ρ increase
 - Though shell begins to narrow significantly / shell E-generation rate increases rapidly

Sub Giant Branch (SGB) : 5 M_☉ star



- During point 5 → 6 :
 - Envelope expands (absorbing much of the shell's E, before it reaches the surface)
- → L decreases, effective T decreases, photospheric optacity increases (H⁻ ion)
- convection zone begins to develop near the surface
- Base of the convection zone → extends down into regions where the chemical composition has been modified by nuclear processes
- Surface convection zone encounters these chemically modified regions
- → Processed material become mixed
- \rightarrow Photosphere composition change (Li \downarrow , ${}_{2}^{3}$ He \uparrow)
- "First dredge-up" begins at point 6

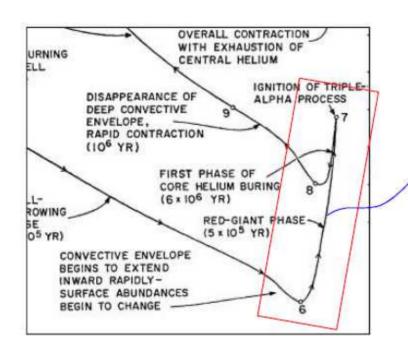
5 M_☉ star at the RGB



- Surface of the envelope continues to cool →
 recombination → N(free e⁻) ↓ → contribution of
 the H⁻ ion to the opacity ↓ → more E release
- During 6 → 7
 - : core continues to contract degenerate He
- → (narrowing) H-b shell E-production rate ↑
- \rightarrow L \uparrow , R \uparrow
- → vertical evolution, "red giant branch (RGB)"
- At point 7 :
- $-T_c = 1.3 \times 10^8 \text{ K}$
- $-\rho_c = 7700 \text{ g/cm}^3$
- High central T and density → quantum-mechanical tunneling through the Coulomb barrier (acting between ⁴₂He nuclei) becomes effective
 - \rightarrow triple- α process begins
- Slow ignition of He-burning phase!
- New source of E → core expands
- → Shell E-generation rate decreases
- $\rightarrow L \downarrow$

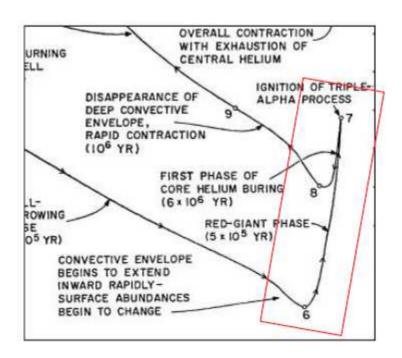
and envelope contracts, T_{eff} ↑

※ For low mass stars of M < 2 M_☉



- As He-core continues to collapse
- → Core becomes strongly electron-degenerate
- T, ρ become high enough to initiate the triple- α process (10⁸ K, 10⁴ g/cm³)
- → Explosive E release! (core) helium flash
- Luminosity ~10¹¹ L_o
- → For only a few seconds!
 (most of the E never reaches the surface)
- → E "lifts" the degeneracy and absorbed by the overlying layers of the envelope (possibly cause some mass loss)

※ For low mass stars of M < 2 M_☉



(core) helium flash

: Nearly constant mass – function of metallicity ~1.6 M_o for population I stars

~1 M_☉ for population II stars

 For pop II stars (ages 2-15 Gyr), if metallicity is same

→ bolometric luminosity is ~ constant (varies only by ~ 0.1 mag)

→ TRGB (tip of the red giant branch)
: distance indicator for old, resolved galaxies

TRGB (tip of the red giant branch)

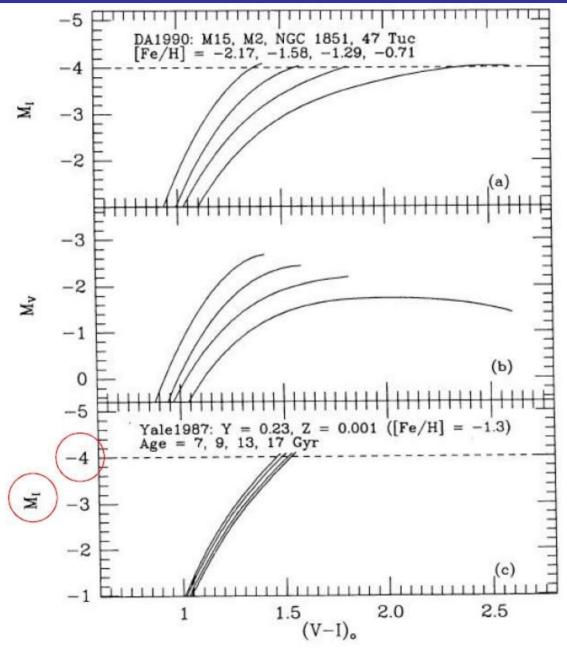


Fig. 1

TRGB (tip of the red giant branch)

TABLE 1

DISTANCE ESTIMATES FOR RESOLVED GALAXIES BASED ON PRIMARY DISTANCE INDICATORS

GALAXY (1)	Түре ^а <i>Е</i> (2)		$(m-M)_0$							
		$\frac{E(B-V)}{(3)}$	Cepheid (4)	RR Lyrae (5)	I _{TRGB} (6)	I _{TRGB} (7)	Reference ^b (8)	[Fe/H] ^c (9)	M_B (10)	M_V (11)
LMC	SBmII	0.10	18.50	18.28	18.42	14.6	1, 2, 3	-1.2	-17.93	-18.36
NGC 6822	ImIV-V	0.28	23.62		23.46	20.05	4, 4	-1.8:	-15.13	-16.42
NGC 185	dE3pec	0.19		24.01	23.94	20.30	5, 6	-1.2	-14.63	-15.52
NGC 147	dE5	0.17	***	24.06	24.13	20.4	7, 8	-0.9	-14.39	-15.17
IC 1613	IMV	0.02	24.42	24.27	24.27	20.25	1, 9, 10	-1.3	-14.51	-15.16
M31	SbI-II	0.08	24.44	24.36	24.44	20.55	1, 11, 12	-0.8	-20.98	-21.74
M33	Sc(s)II-III	0.10	24.63	24.71	24.70	20.95	1, 13, 12	-2.0	-18.94	-19.40
WLM	ImIV-V	0.02	24.92		24.81	20.85	14, 14	-1.6:	-14.28	-14.62
NGC 205	S0/dE5pec	0.035	***	24.76	24.42	20.45	15, 16	-0.8	-15.80	-16.62
NGC 3109	SmIV	0.04	25.5	***	25.45	21.55	17, 18	-1.6	-15.95	-16.25

^{*} From Sandage & Tammann 1987.

$$-2.2 < [Fe/H] < -0.7 \text{ dex}$$

b References: (1) Madore & Freedman 1991, (2) Walker 1988, (3) Reid & Mould 1987, (4) Lee, Freedman, & Madore 1993, (5) Saha & Hoessel 1990, (6) Lee, Freedman, & Madore 1992, 1993c; (7) Saha, Hoessel, & Mossman 1990; (8) Mould, Kristian, & Da Costa 1983; (9) Saha et al. 1992; (10) Freedman 1988; (11) Pritchet & van den Bergh 1987, 1988; (12) Mould & Kristian 1986; (13) Pritchet 1988; (14) Lee, Freedman, & Madore 1993a; (15) Mould, Kristian, & Da Costa 1984; (16) Saha, Hoessel, & Krist 1991; (17) Capaccioli, Piotto, & Bresolin 1992; (18) Lee 1993.

^o The metallicity [Fe/H] has been determined using the color $(V-I)_{-3.5}$.

TRGB (tip of the red giant branch)

- Y-axis (L scale): squeezed
- · Time scale : different
- Low-mass stars : less structure variation, less contraction → more simple and smooth tracks
- Thicker parts: major phases of fusion burning
- Dashed lines: uncertain phases

