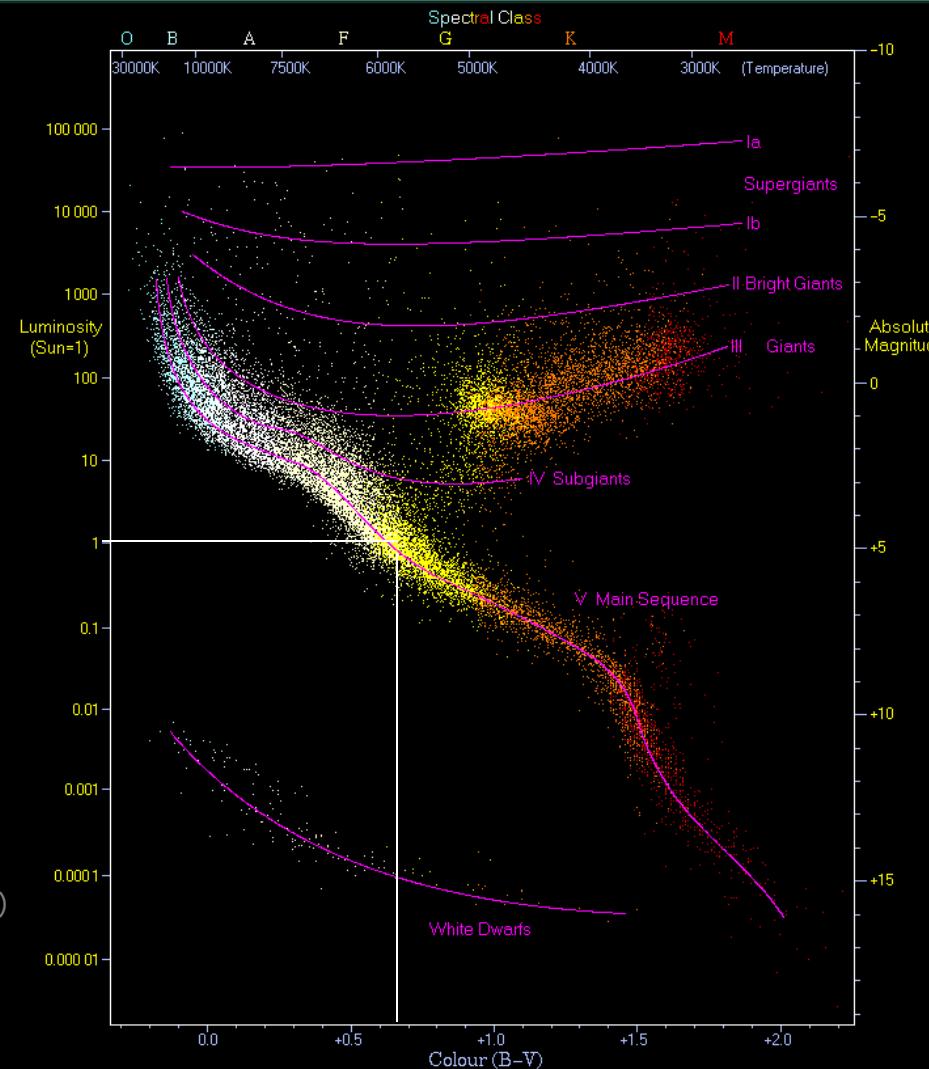


Part II. Stellar Evolution and the Milky Way Galaxy

Chapter 1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)

1-1 Two-dimensional distribution of stellar parameters (별들의 2차원 분포 그림)



https://en.wikipedia.org/wiki/Hertzsprung%20-%20Russell_diagram

김상철
(Sang Chul KIM)

Modern Astronomy

Part II. Stellar Evolution and the Milky Way Galaxy

(항성진화와 우리은하)

- **Instructor** : 김상철(Sang Chul KIM, Center for Large Telescopes, JangYoungSil-Hall
Room 315, 042-865-3246, 010-8622-5618, sckim@kasi.re.kr)
- **References (참고문헌)** :
 - Introductory Astronomy and Astrophysics (4th edition), Michael Zeilik & Stephen A. Gregory (1998)
 - An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996)
 - Galactic Astronomy (J. Binney & M. Merrifield, 1998)
 - An Introduction to Stellar Astrophysics (Francis LeBlanc, 2010)
 - Evolution of Stars and Stellar Populations (Maurizio Salaris & Santi Cassisi, 2005)
 - 항성내부구조 및 진화, Dina Privalnik 지음, 김용기 옮김, 2007 (An Introduction to the Theory of Stellar Structure and Evolution, 2000)
- **Evaluation** : Attendance 10%, Written final exam 90%
- **Final exam** : 2025 October
- **Lecture note** will be uploaded to sckim86.github.io by 1 hour before

Modern Astronomy

Part II. Stellar Evolution + MWG

Sep 29 Chapter 1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)

- 1.1 HRD (Hertzsprung-Russell Diagram, H-R도)
- 1.2 Distances (거리)
- 1.3 Magnitudes (등급)
- 1.4 The Classification of Stellar Spectra (별의 스펙트럼 분류)

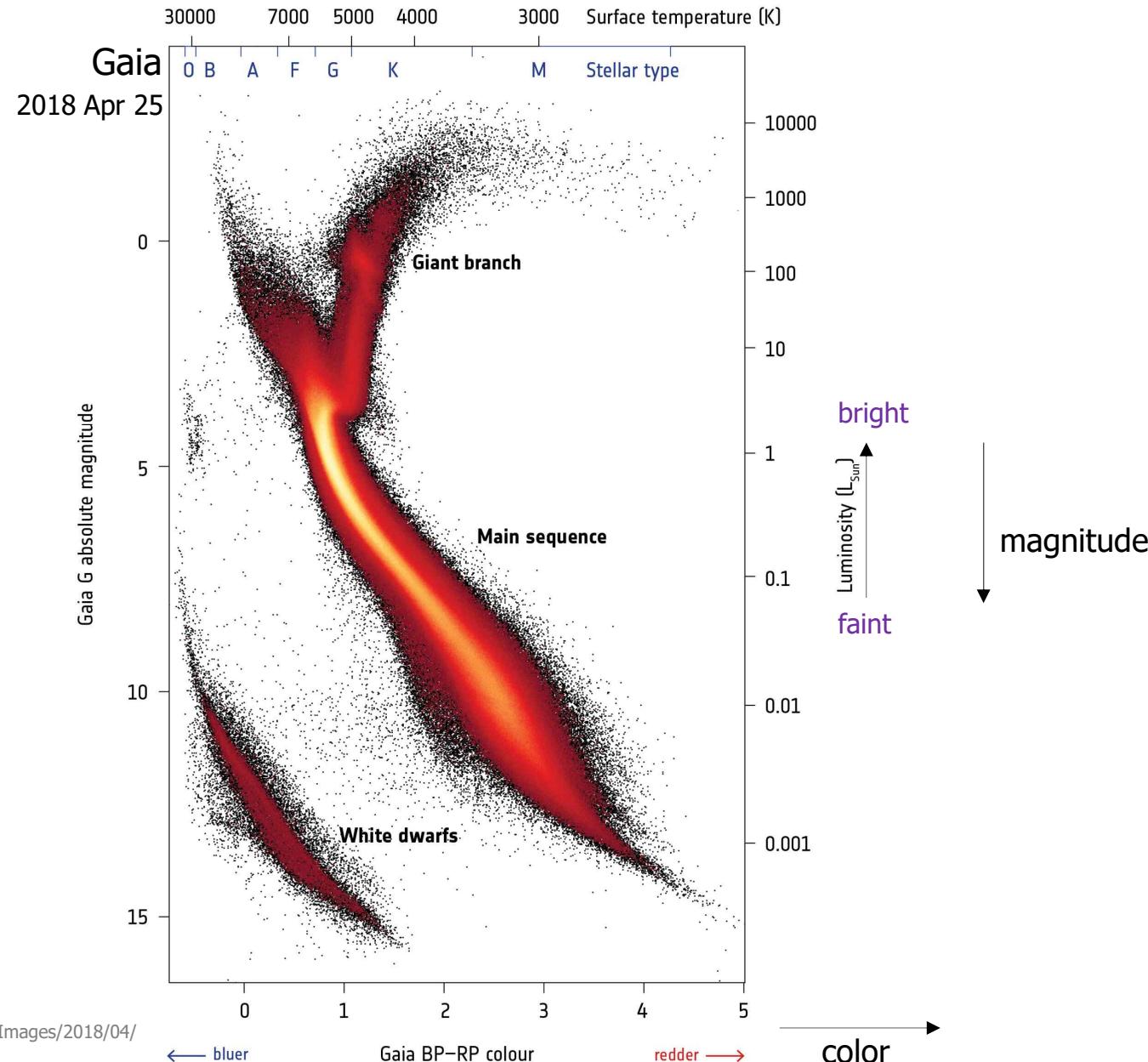
Oct Chapter 2. The Evolution of Stars (별의 진화)

Oct 13 Chapter 3. Star Deaths (별의 죽음)

Oct 20 Chapter 4. The Milky Way Galaxy (우리은하)

1. Stars: The Hertzsprung-Russell Diagram

1.1 Two-dimensional distribution of stellar parameters (별들의 2차원 분포 그림)



Hertzsprung-Russell Diagram

1911 Ejnar Hertzsprung (1873-1967)

Danish engineer and amateur astronomer

1913 Henry Norris Russell (1877-1957)

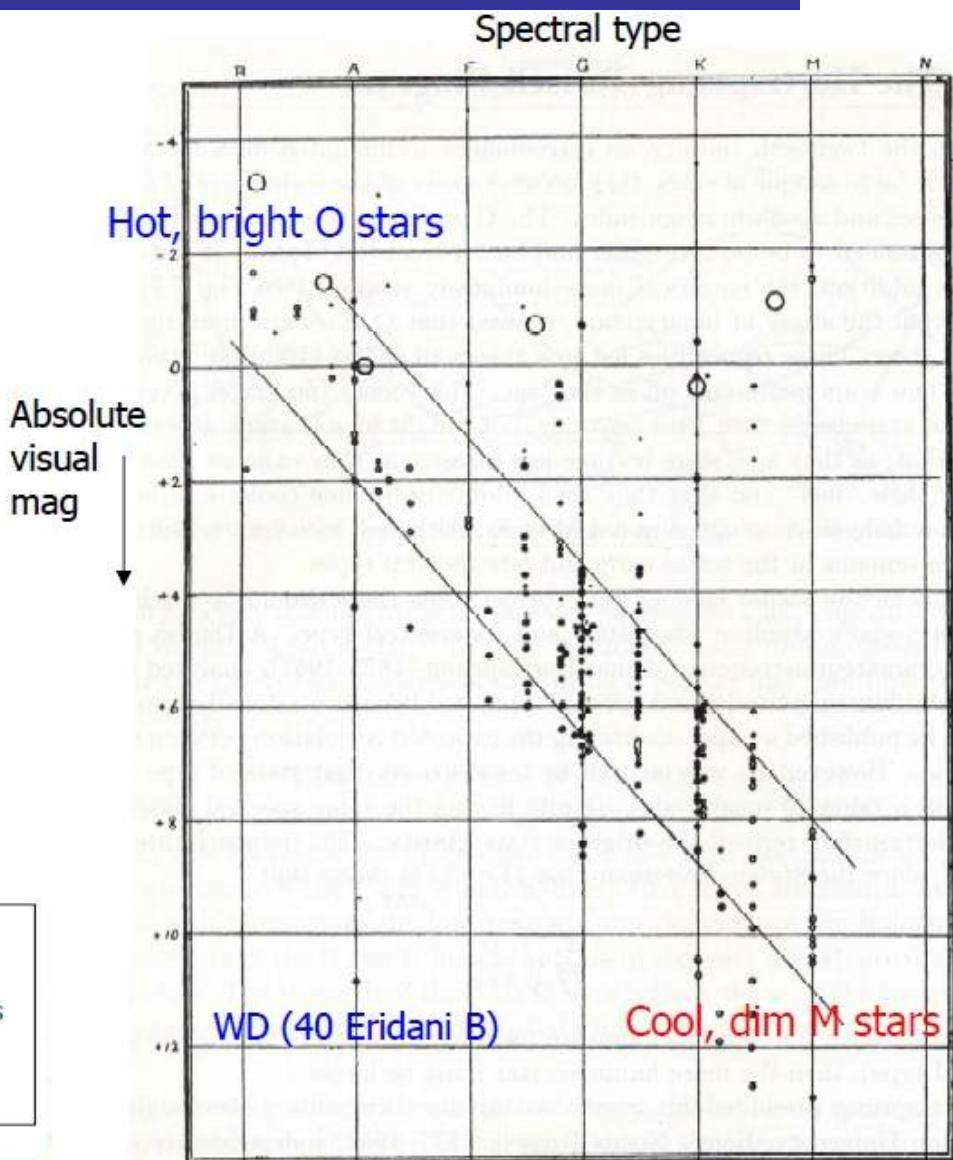
Princeton University, USA

1913 – published the “diagram”

- 80-90% of all stars – main sequence (MS) stars
- Bengt Strömgren (1908-1987, Danish) : suggested the name “H-R” diagram

Fig 8.10 Henry Norris Russell's first diagram
(Russell, H. N. 1914 May 07, Nature, 93 (Number 2323), 252-258 'Relations Between the Spectra and other Characteristics of the Stars. II. Brightness and Spectral Class')
Fig. 1. > 200 stars

* (Russell, H. N. 1914 April 30, Nature, 93 (Number 2322), 227-230 'Relations Between the Spectra and other Characteristics of the Stars. I. Historical')



An Introduction to Modern Astrophysics (2nd edition),
Bradley W. Carroll & Dale A. Ostlie (1996), p. 242

Henry Norris Russell prize



American Astronomical Society (AAS)

Henry Norris Russell Lectureship

The Russell Lecturer is normally chosen annually on the basis of a lifetime of eminence in astronomical research. The award includes a suitably engraved certificate, an invitation to deliver a lecture dealing with a broad astronomical field at a meeting designated by the Board of Trustees, travel expenses to the meeting at which the Russell Lecture is given, and publication of the lecture (or research related to the subject of the prize, though publication of the lecture is strongly preferred) in a Society journal.

Main Sequence (MS, 주계열성)

'Sequence'

NAVER 영영사전

sequence 미국식 ['si:kwəns] ⏪ 영국식 ⏪ +

1. 명사 the order in which things happen or should happen
2. 명사 a group of things that come one after the other, series
3. 명사 a part of a movie, television show, etc., that deals with one subject, action, or idea

sequence 유의어

n. chain, cycle, series, arrangement, order, progression succession

계열 系列 [발음 : 계 : 열/게 : 열]

파생어 : 계열적

명사

1. 서로 관련이 있거나 유사한 점이 있어서 한 갈래로 이어지는 계통이나 조직.

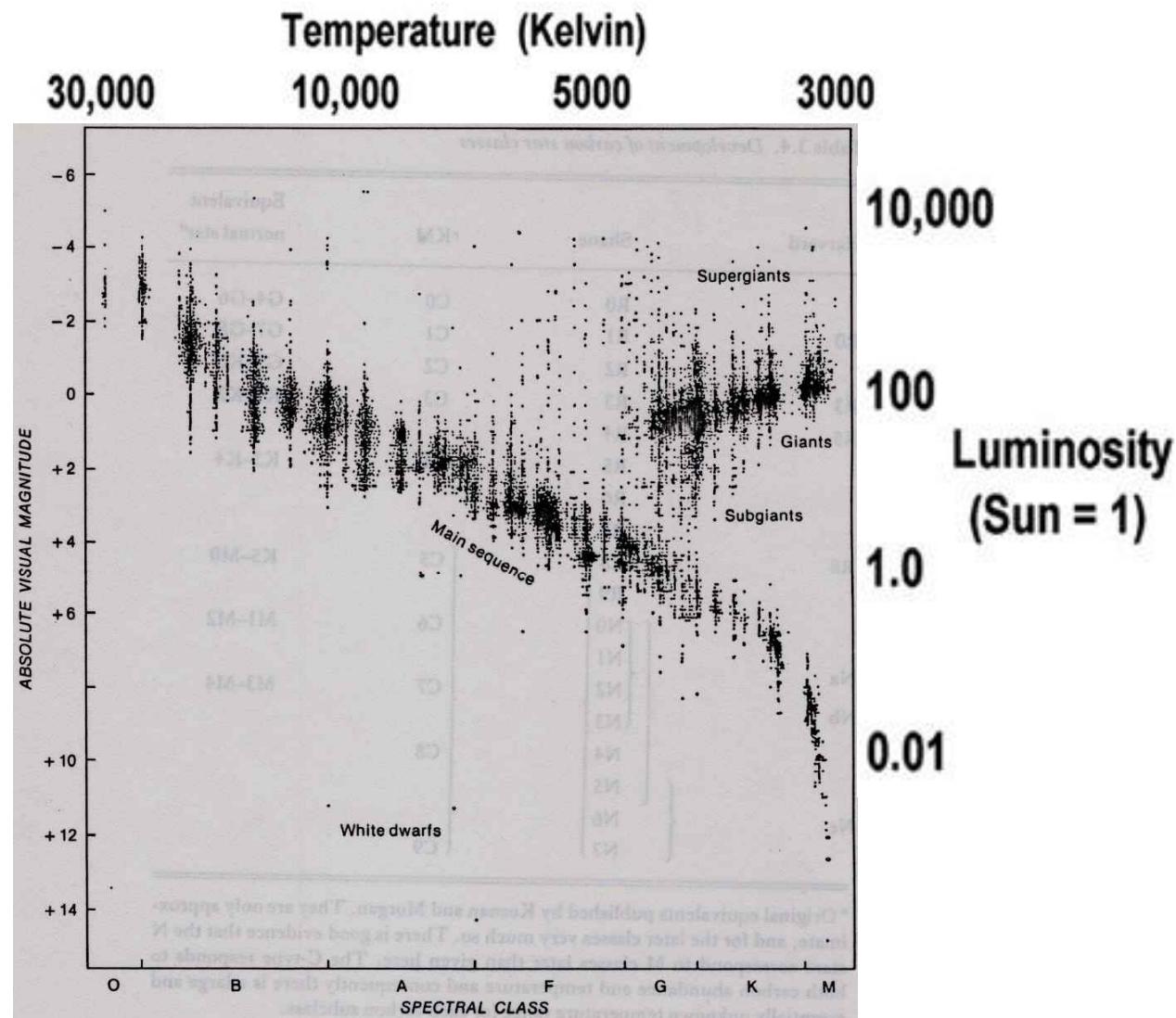
- 인문 계열
- 영상섭의 소설은 사실주의 계열의 작품이다.
- 교내 계열 평균에서 13반이 끌등입니다. 출처 : 전상국, 퇴장

2. <경제> 기업의 결합 형태의 하나. 생산, 판매, 자본, 기술, 중역 파견 따위에 따라 대기업 상호 간 또는 대기업과 중소기업 간에 볼 수 있는 기업 결합이다.

- 계열 산업.

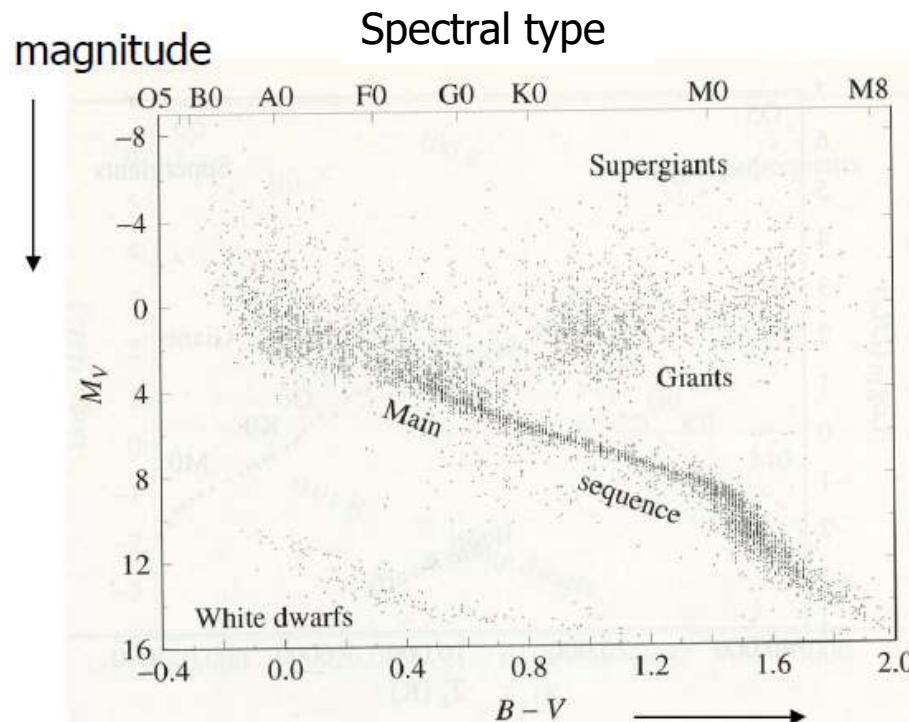
Main Sequence (MS, 주계열성)

Sequences!

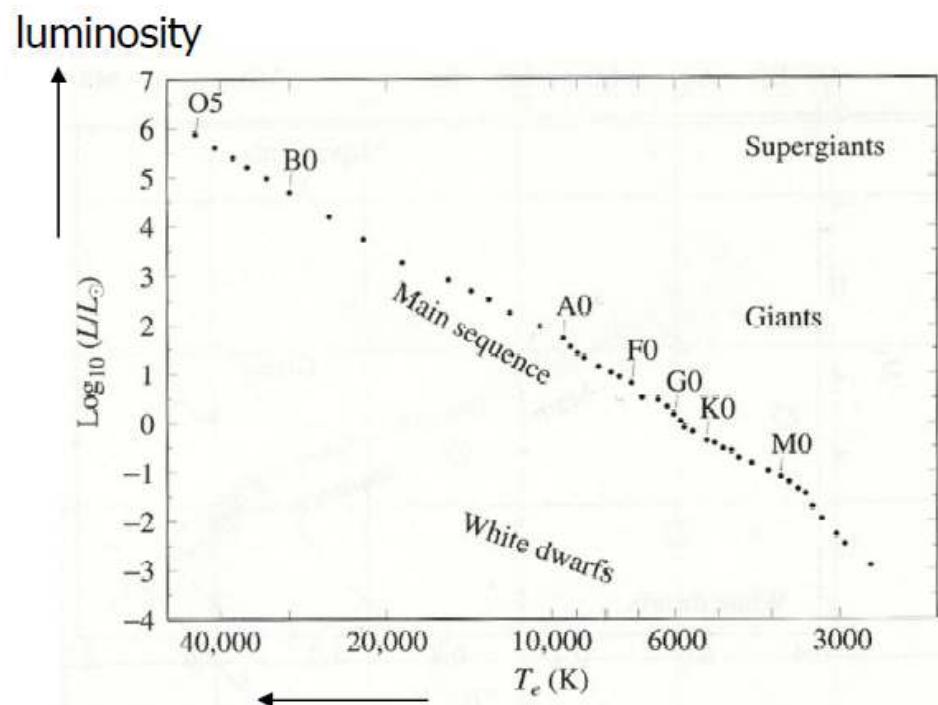


Compiled by W. Gyllenberg (Lund Observatory, Sweden)

Observers' vs Theorists' H-R Diagrams



Color index

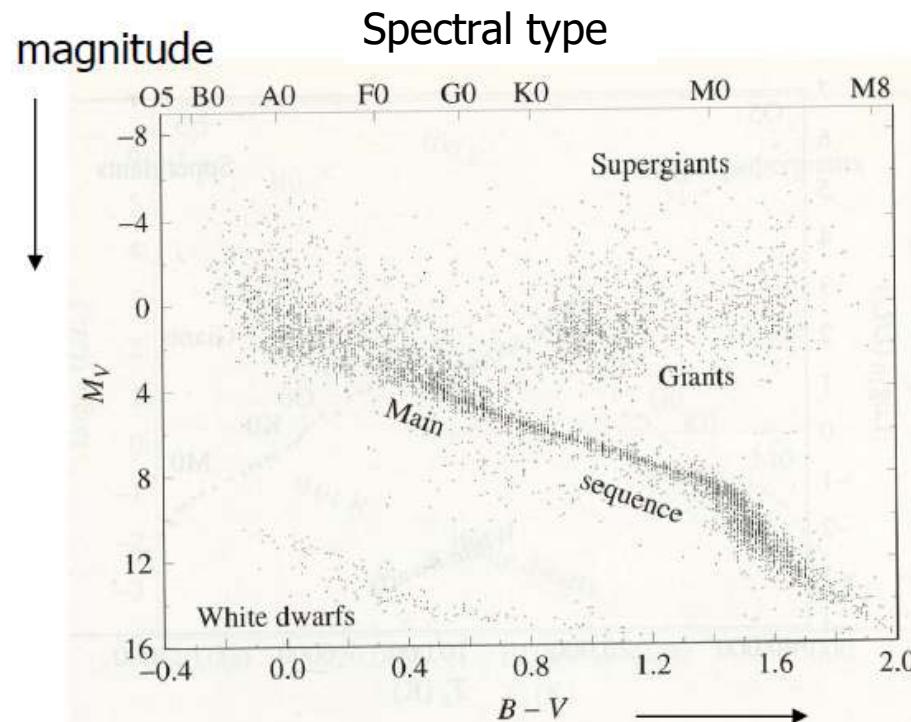


Effective temperature

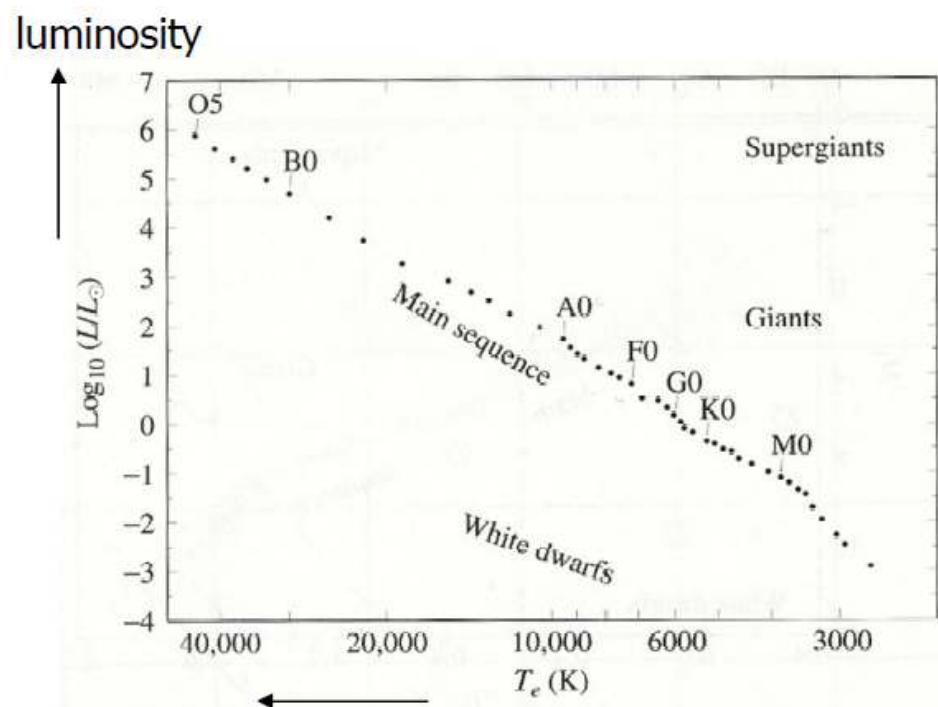
Color-Magnitude Diagram (CMD,
색등급도)
: observers' diagram

HR Diagram (HRD, HR도)
: theorists' diagram

Observers' vs Theorists' H-R Diagrams



Color index



Effective temperature

MS width \leftarrow (1) changes in T, L in the MS
 (2) Slight differences in the components of stars

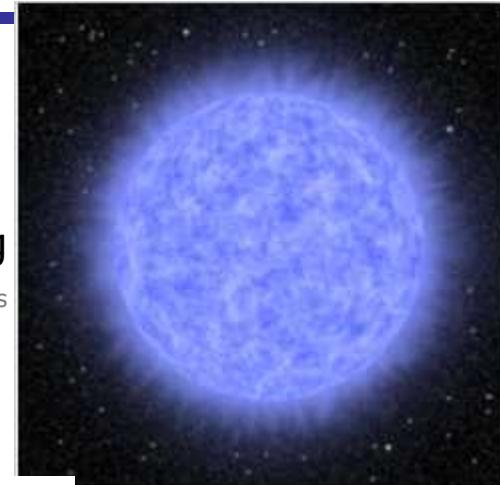
MS luminosities : $5 \times 10^{-4} L_\odot$ to $1 \times 10^6 L_\odot$
 \rightarrow over **10 orders** of mag

Spectral Types

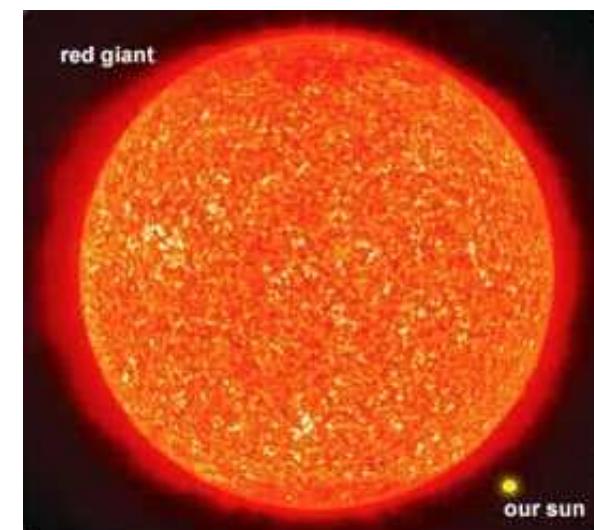
- O type : blue stars. Usually supergiants.
Very luminous and hot. Rare.
Strong helium absorption lines.

ζ Puppis (O4 I) – artist's rendering

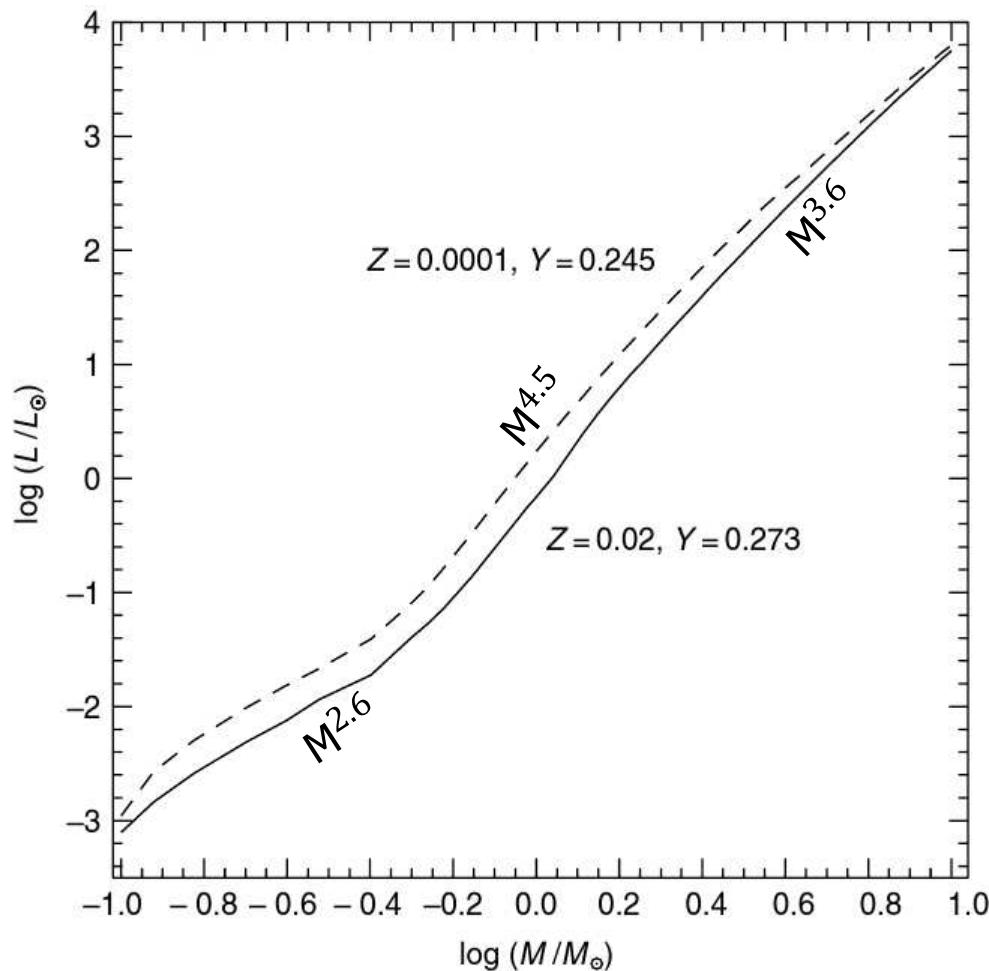
https://en.wikipedia.org/wiki/Zeta_Puppis



- B type : blue white stars. Mainly giants. Neutral He and H absorption lines.
- A type : white stars. Strong **H absorption lines**.
- F type : yellow white stars. Weak H and ionized Ca absorption lines.
- G type : yellow stars. Strong Ca absorption lines.
- K type : orange stars. Metallic absorption lines.
- M type : red stars. Strong metallic absorption lines.



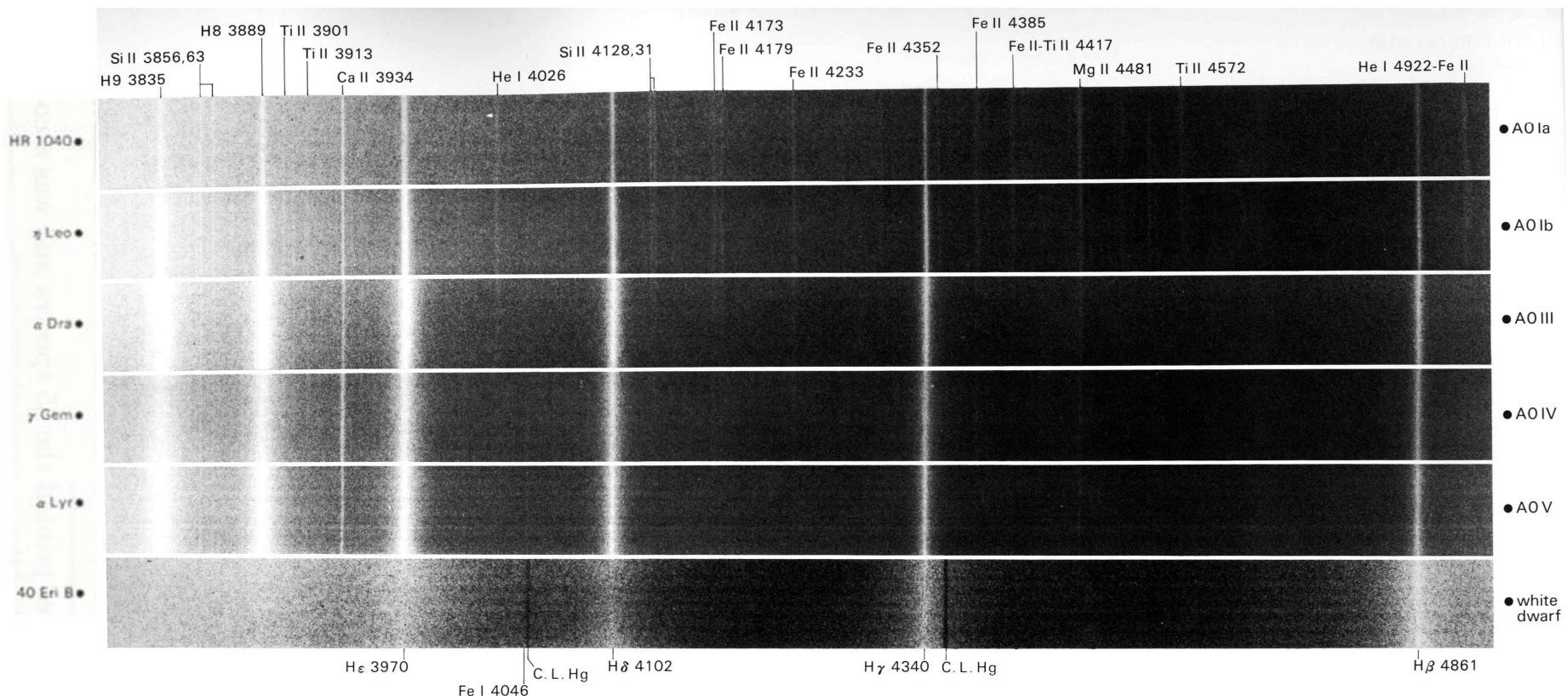
Stars → mass-luminosity relation



O stars : more luminous than M stars
→ O stars are more massive than M stars

$$\text{Power law : } L \propto M^{\nu}$$

'A' type stellar spectra – hydrogen Balmer lines



More **luminous stars** → narrower **lines**

$$\text{Stefan-Boltzmann equation } L = 4\pi R^2 \sigma T^4$$

T : same

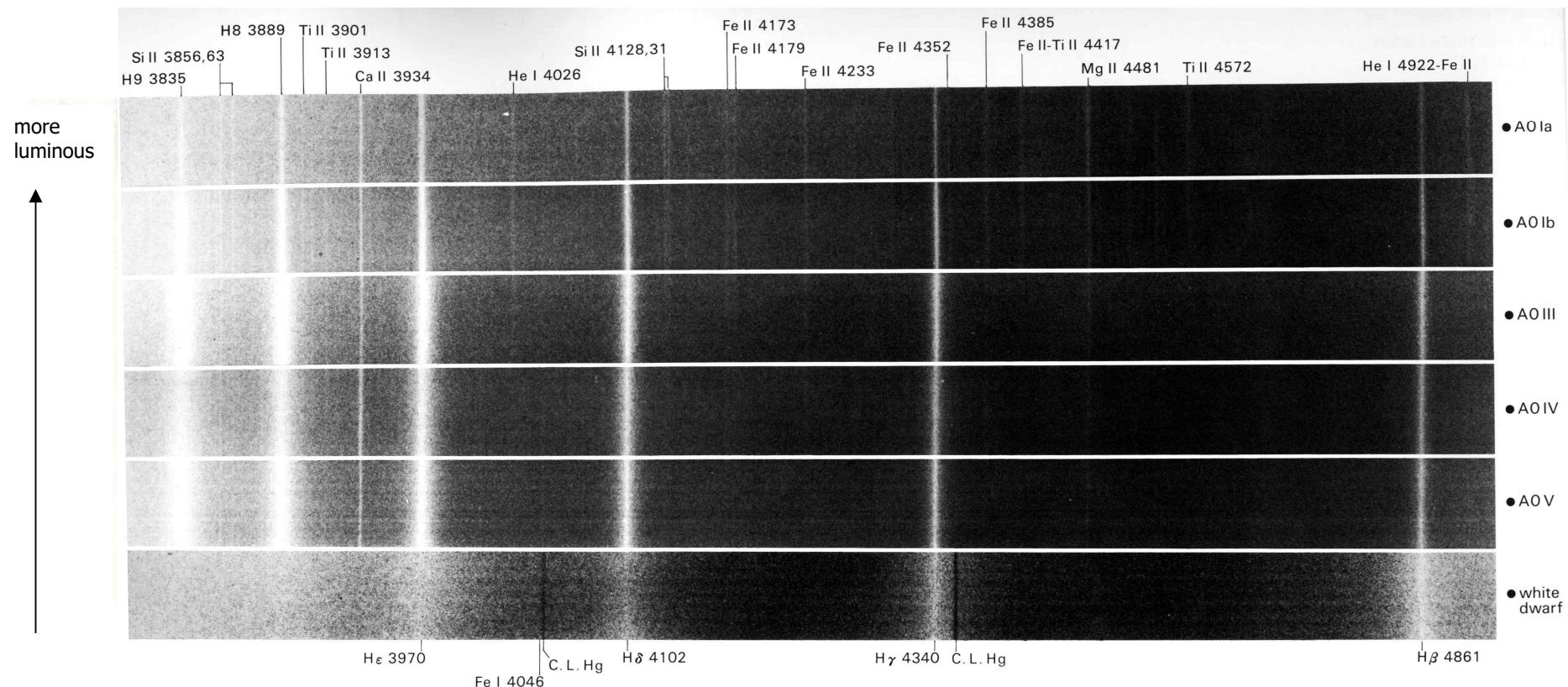
$L \propto R^2$ → less **dense** → fewer **collisions** between atoms → **less broadening**

σ = Stefan-Boltzmann constant

$$\sigma = 5.67 \times 10^{-5} \text{ erg cm}^{-2} \text{ sec}^{-1} \text{ K}^{-4}$$

$$\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$$

'A' type stellar spectra – hydrogen Balmer lines



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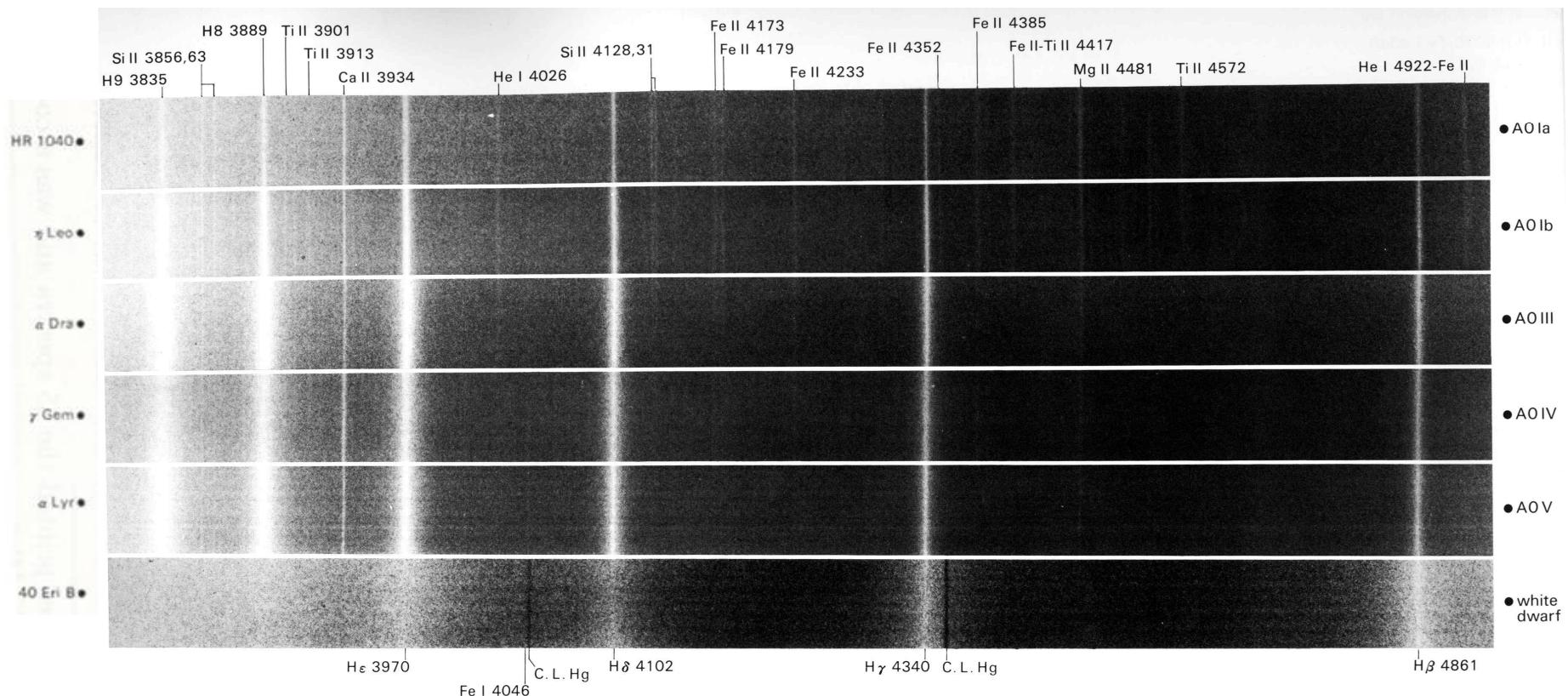
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'A' type stellar spectra – hydrogen Balmer lines



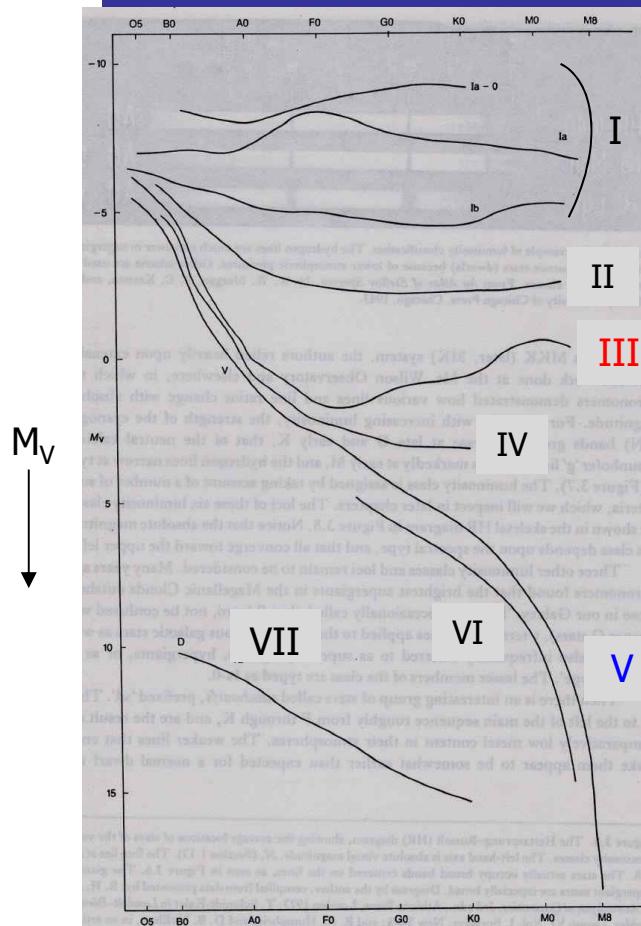
1943 Yerkes Observatory

William W. Morgan – Phillip C. Keenan – Edith Kellman

『An Atlas of Stellar Spectra』 (Chicago: Chicago University Press)

→ M-K (MKK) spectral **classification system** : two-dimensional spectral classification

Morgan-Keenan Luminosity Classes



class	Type of Star
I	Supergiants (SGs)
II	Bright giants
III	Giants
IV	Subgiants
V	Main-sequence (dwarf) stars
VI	Subdwarfs (sd)
VII, D	White dwarfs (WDs)

- Same **spectral type**
- Same **effective temperature**
- Only luminosity differences ← subtle differences in the relative **strengths** of **spectral lines**

Morgan & Keenan (1973, ARA&A, 11, 29 – Spectral Classification)

Stars and Their Spectra-An Introduction to the Spectral Sequence, James B. Kaler, 1989, p77

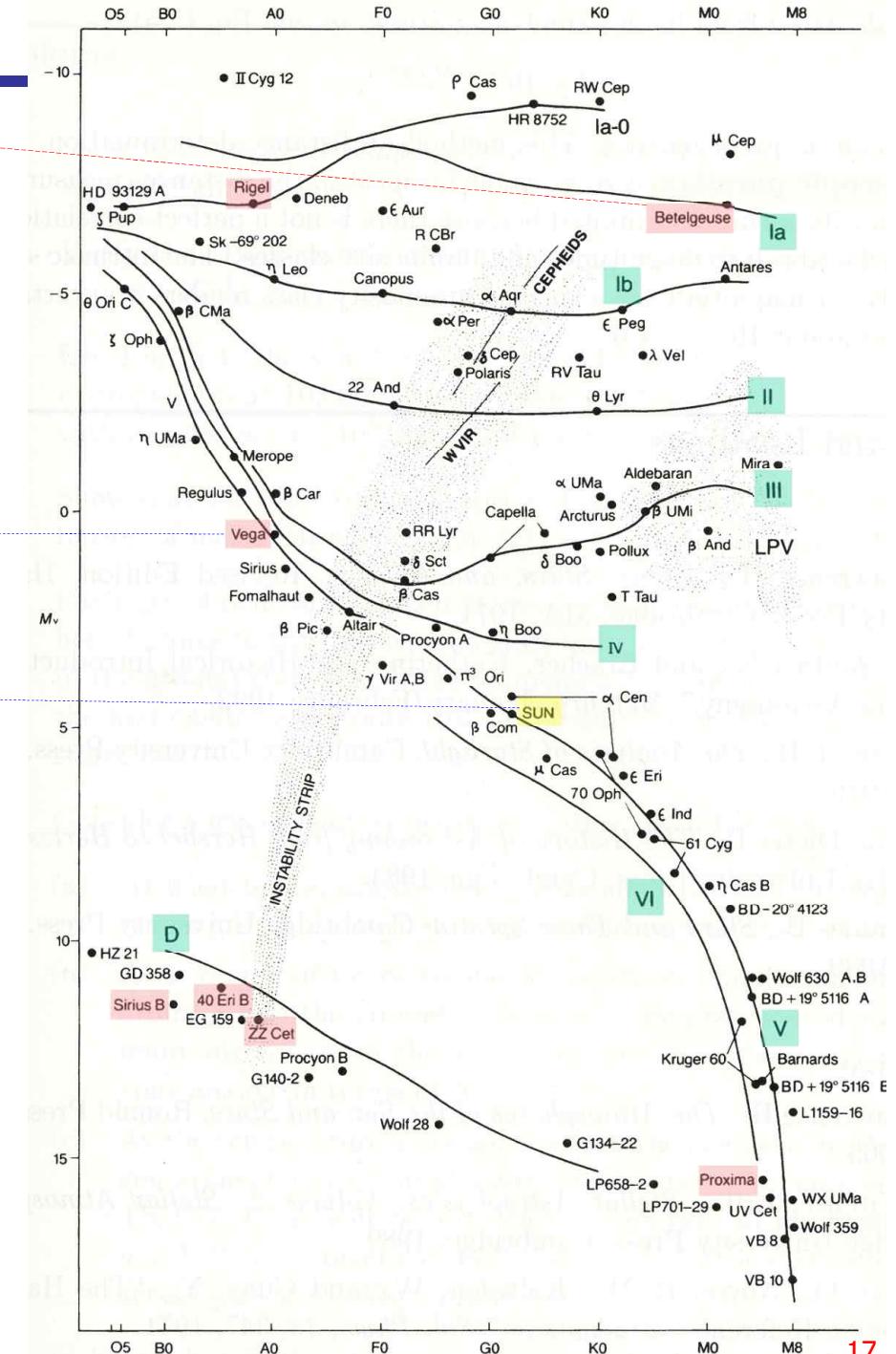
An Introduction to Modern Astrophysics (2nd edition),
Bradley W. Carroll & Dale A. Ostlie (1996), p. 248

H-R diagram – luminosity classes

Betelgeuse ($=\alpha$ Orionis) ←
: M2 Ia (or M2 Iab) – pulsating variable

Vega : A0 V
($T_{\text{eff}} = 10,000$ K)

Sun : G2 V



Size ~ Luminosity

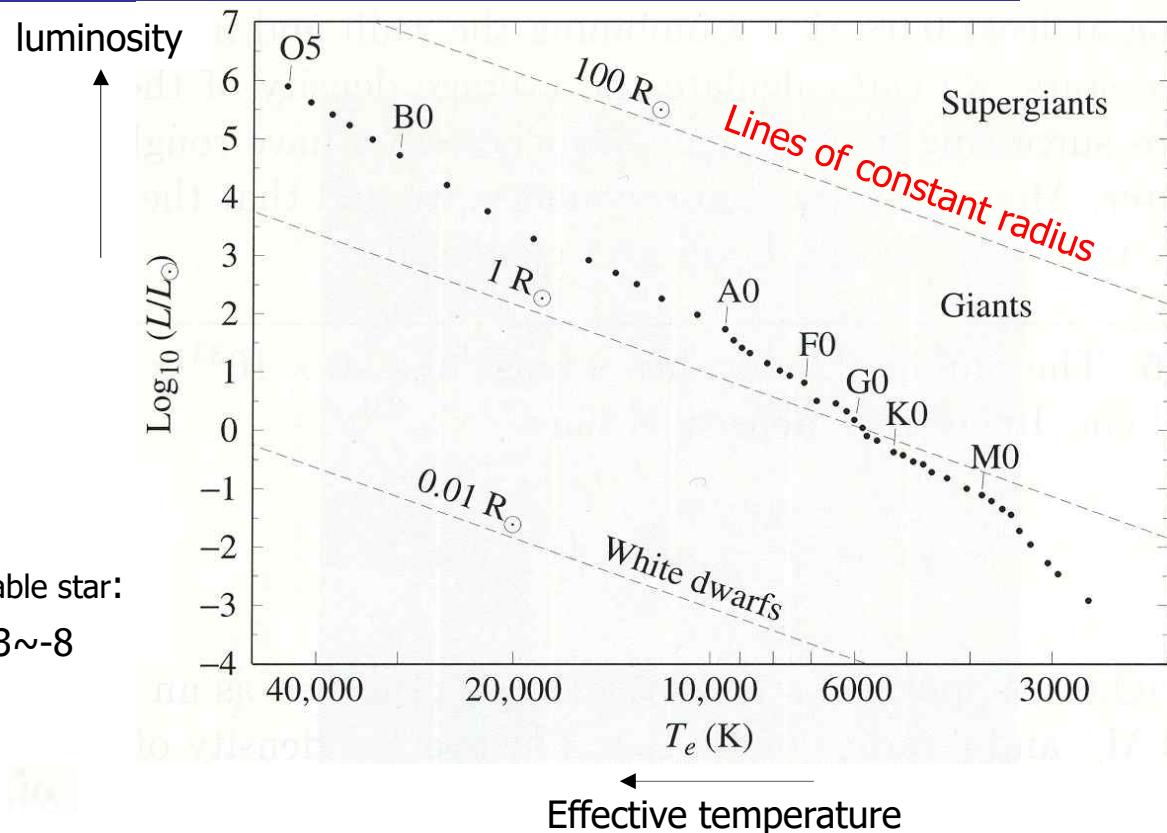
$$L = 4\pi R^2 \sigma T^4$$

$$100 \times L$$

$\rightarrow 10 \times R$ larger

Giant stars : 10s-100s R_\odot
 (e.g. Aldebaran, α Tauri : $45 R_\odot$)

Supergiant stars (blue, yellow, red)
 : 100s – 1000+ R_\odot
 (e.g. Betelgeuse, α Orionis – pulsating variable star:
 $700 - 1000 R_\odot$, $P = 2070$ d) $M_V = -3 \sim -8$

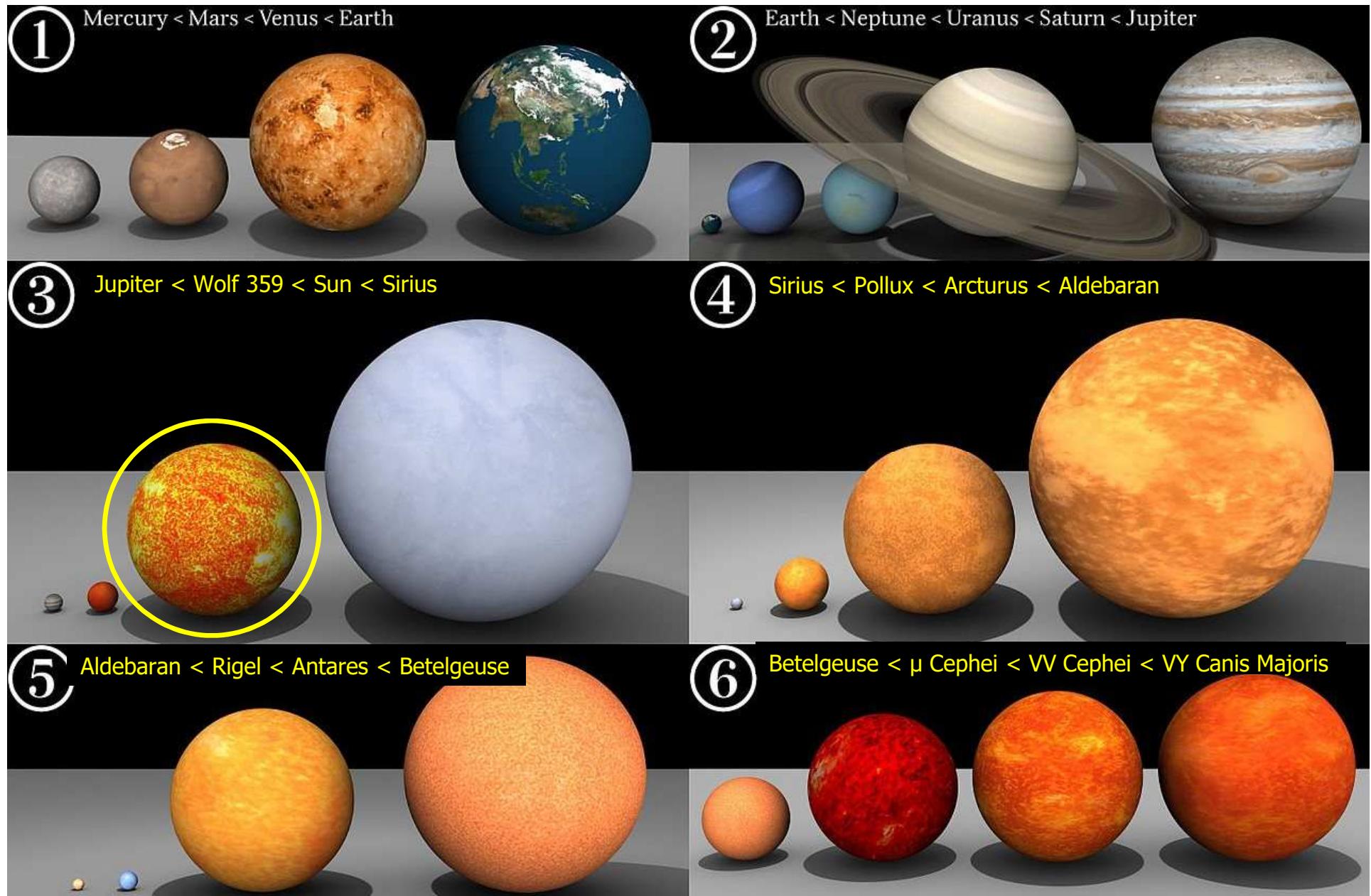


- * μ Cephei : $1260 R_\odot = 5.9$ AU
- * VY Canis Majoris : 1420 or $2069 R_\odot = 6.6$ or 9.7 AU

- * $1000 R_\odot = 4.7$ AU
- * Jupiter, semi-major axis $a = 5.2$ AU
- * Saturn, semi-major axis $a = 9.5$ AU

An Introduction to Modern Astrophysics (2nd edition),
 Bradley W. Carroll & Dale A. Ostlie (1996), p. 245

Stellar Size Comparison

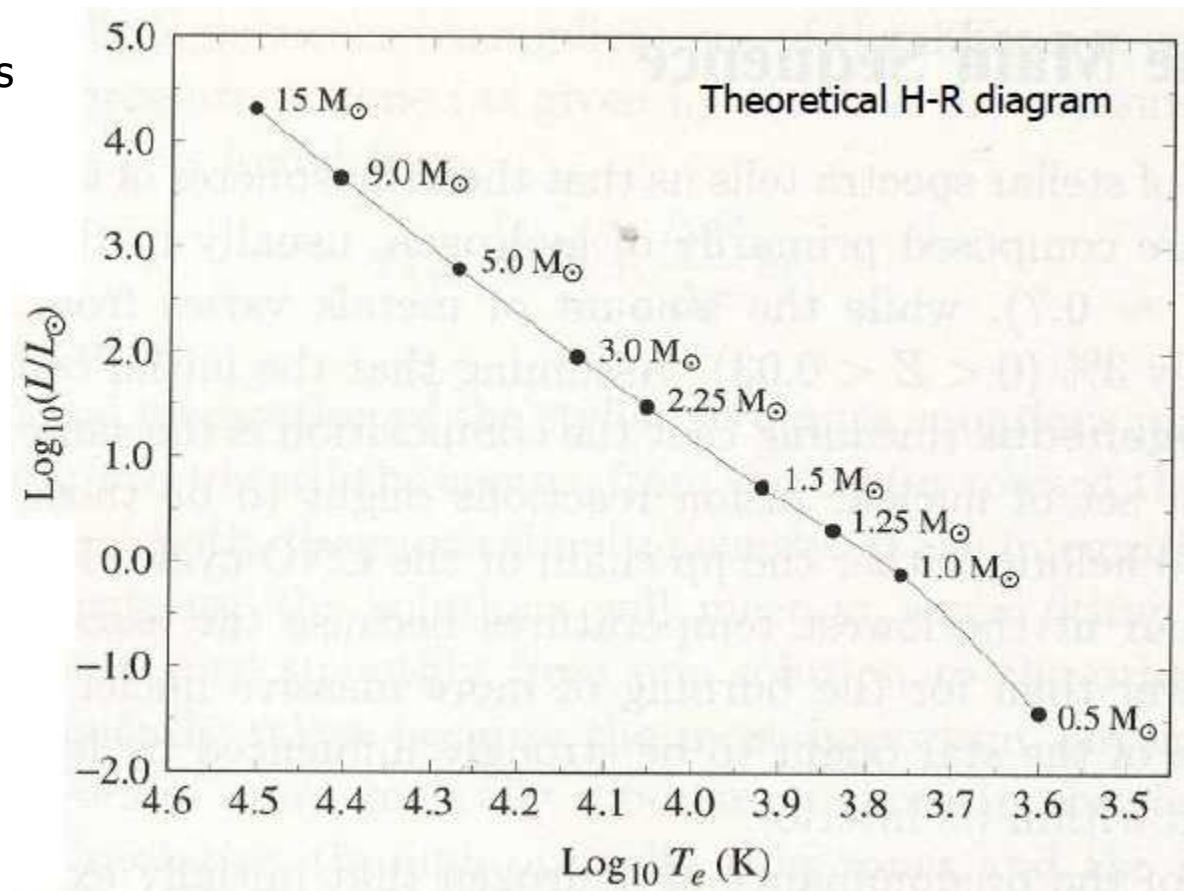


Vogt-Russell theorem

The **mass** and **composition** of a star uniquely determine its **radius**, **luminosity**, and **internal structure**, as well as its subsequent **evolution**.

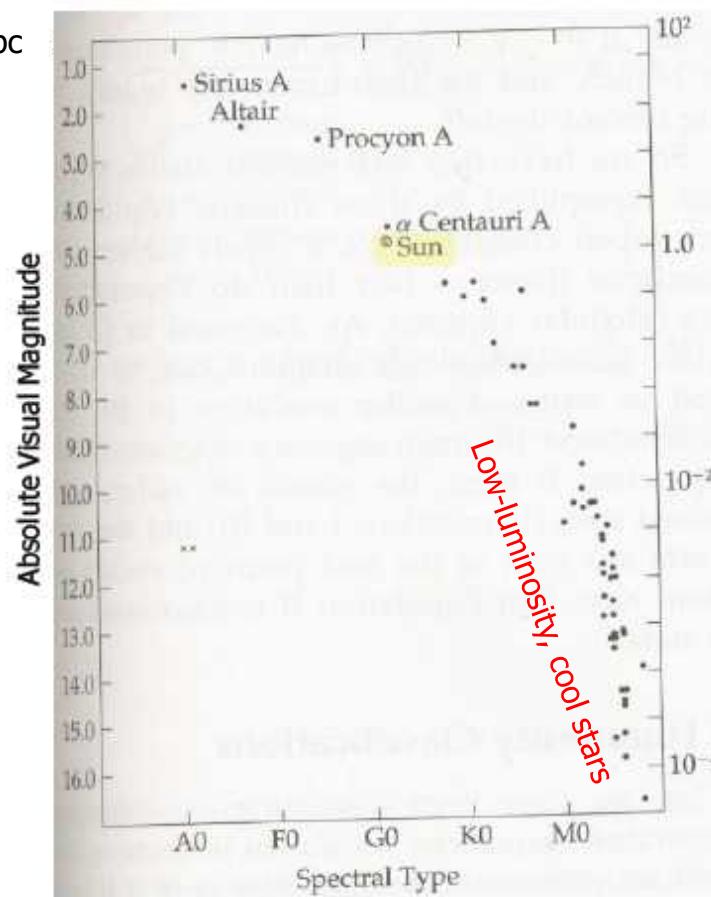
Stellar masses from models

- Theoretical models for the mass range of core hydrogen burning (H-b)
→ lie along the observational MS
- $100 - 0.08 M_{\odot}$
→ Only 3 orders of mag
- At $< 0.08 M_{\odot}$
→ brown dwarfs (BDs)



Example HR Diagrams

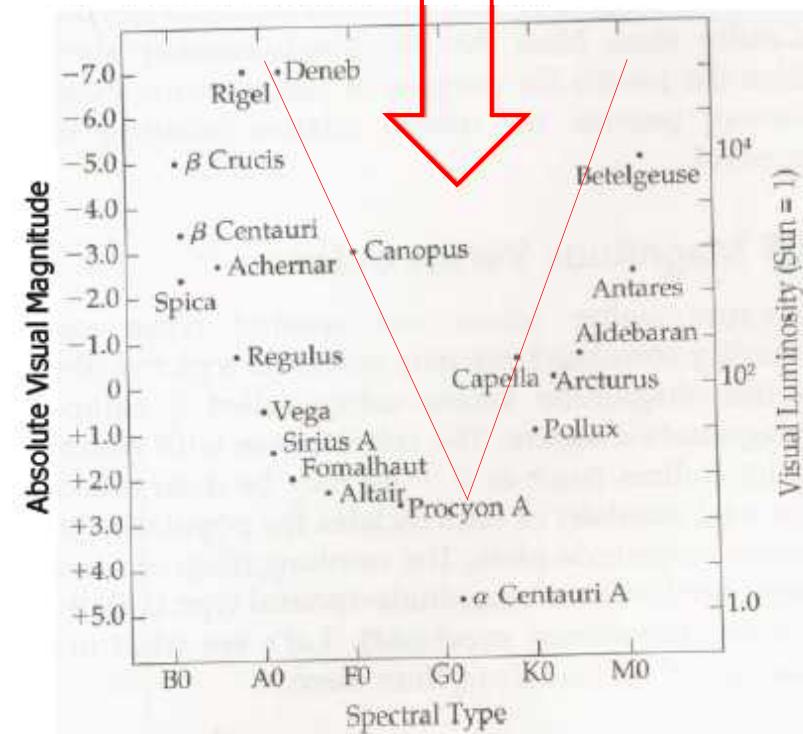
(a) Stars within 5 pc



- Well-defined MS + increasing number of stars toward later spectral types
- No stars earlier than A1

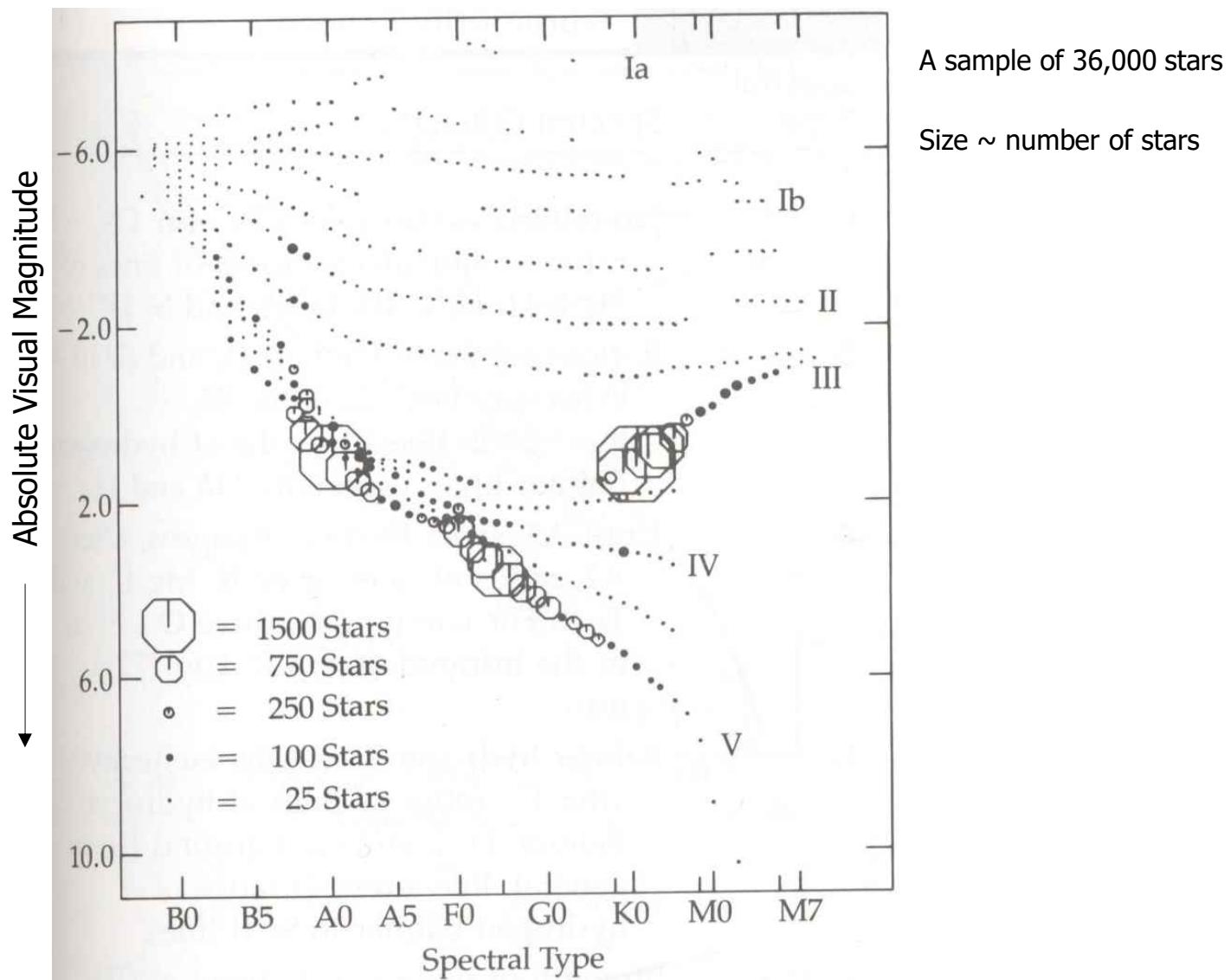
Hertzsprung Gap

(b) The brightest stars in the sky



- A significant number of giants and SGs
- Several early-type MS stars

HR diagrams



1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)

1.2 Distances (거리)

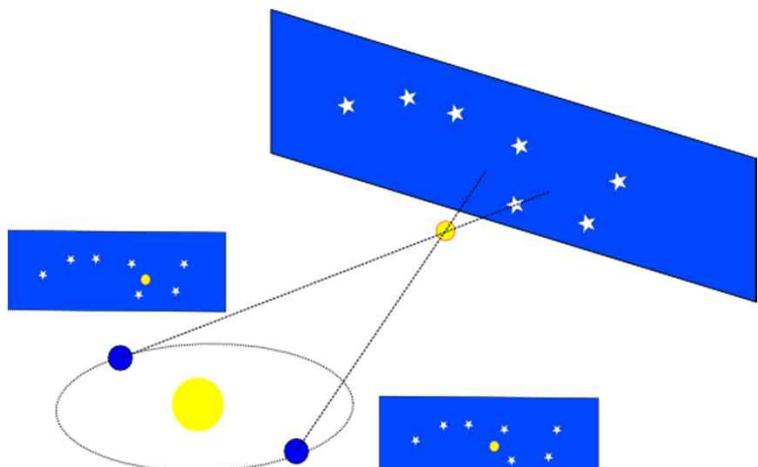


<http://www.centauri-dreams.org/?p=11322>

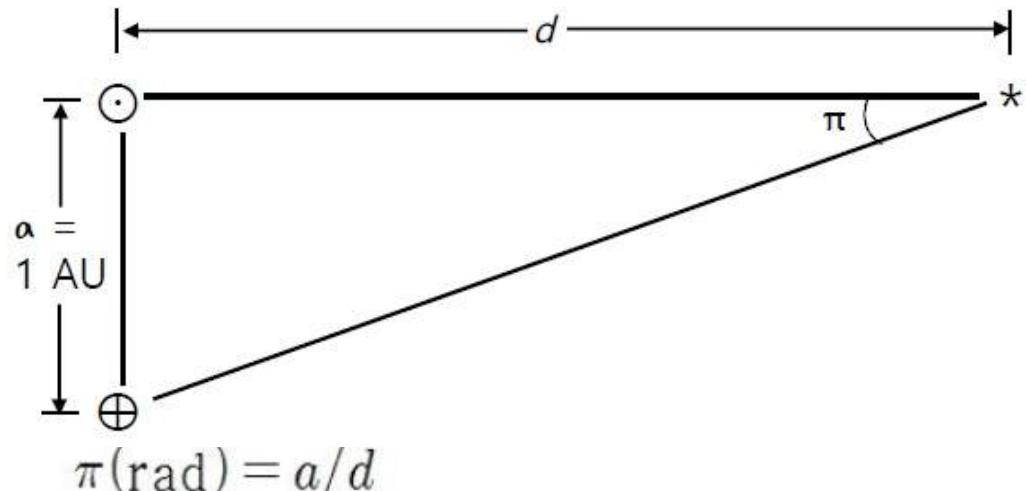
<http://www.centauri-dreams.org/wp-content/uploads/2010/02/light-candles.jpg>

1. Trigonometric parallax (삼각시차)

- First detection (1838) : Friedrich W. Bessel → 61 Cygni, $d=10.4$ ly
- In 1838, Friedrich G. W. von Struve → Vega (= α Lyr), $d=25.0$ ly



<https://en.wikipedia.org/wiki/Parallax>



- $2\pi \text{ (rad)} = 360^\circ \rightarrow 1 \text{ rad} = 57^\circ 17' 44.81'' = 206265''$

$$\boxed{\pi'' = \frac{1}{d}} \quad (\pi \text{ in arcsec, } d \text{ in parsec [파섹]})$$

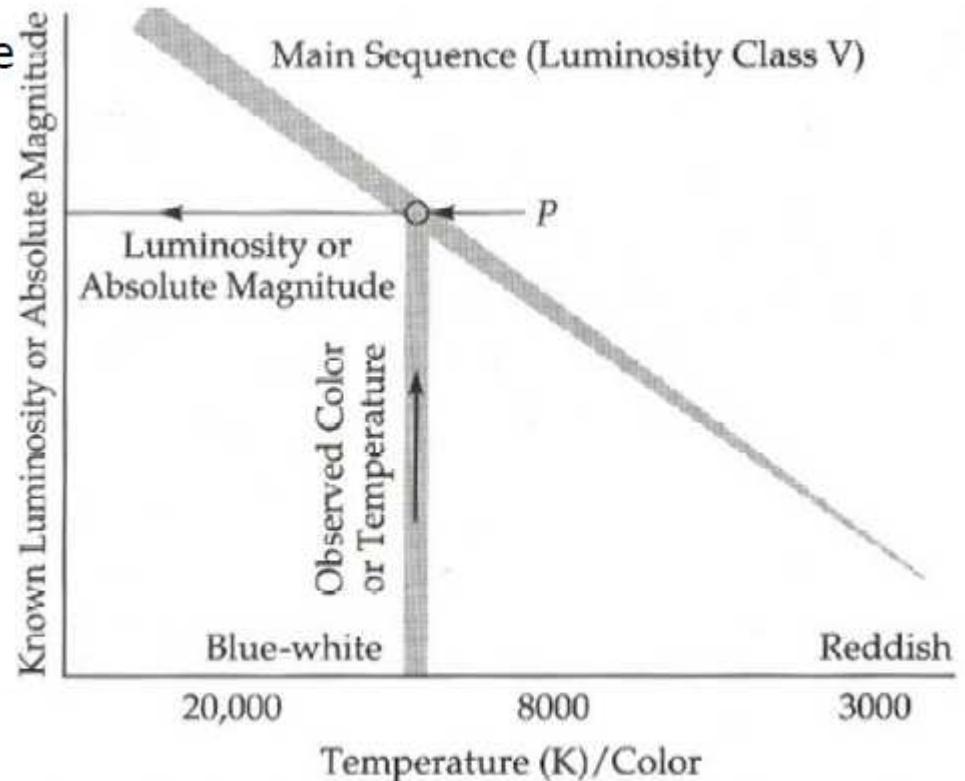
$$1 \text{ pc} = 3.086 \times 10^{18} \text{ cm} = 3.26 \text{ lightyears (광년)}$$

- Largest parallax : Alpha Centauri ($d=1.3$ pc) $\rightarrow \pi=0.76''$
- Ground-based observations \rightarrow error $\sim \pm 0.004''$
 \rightarrow accurate only to $\pi=0.001''$ ($d \sim 100$ pc)

→ Satellites : Hipparcos (1989-1993), Gaia (2013 Dec 19-)

Spectroscopic parallax – using **spectral type**

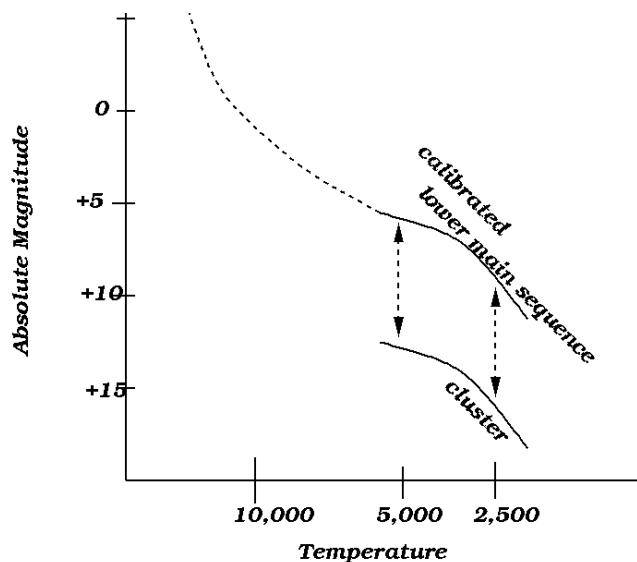
- A star's spectrum → determine spectral type and luminosity class
- A star's position is fixed in H-R diagram
→ Vertical reading = absolute magnitude (M_V)
→ Distance can be calculated by
 $(m-M)_0 = V - M_V - A_V = 5 \log d - 5$
“spectroscopic parallax”
- Observational errors, scatter in the HR diagram → mag uncertainty : **±1.0 mag**
(distance error : **50%**)



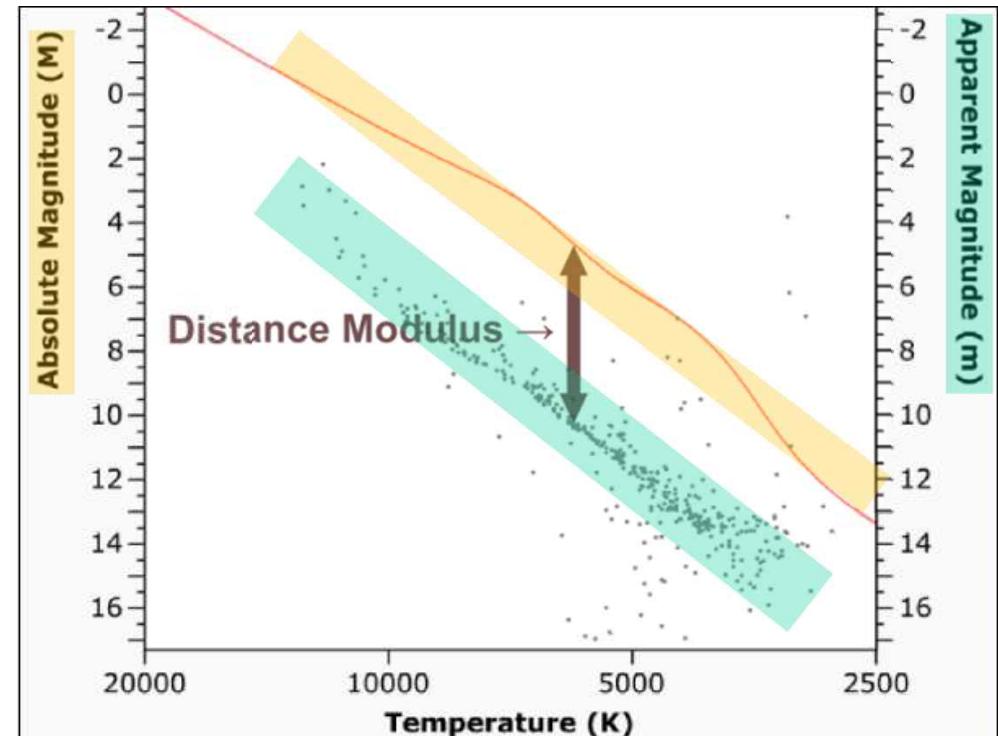
A calibrated **H-R diagram**

Spectroscopic parallax – using **spectral type**

- For observational data of an entire star cluster : color – apparent magnitude
→ shift up and down (in magnitude)
- $(\text{test cluster apparent mag}) - (\text{calibrated absolute mag}) = (m-M)$
→ distance modulus
→ same for every star in the cluster
- Better accuracy than the spectroscopic parallaxes → mag uncertainty : ± 0.2 mag



https://ned.ipac.caltech.edu/level5/Bothun2/Bothun2_3_2.html

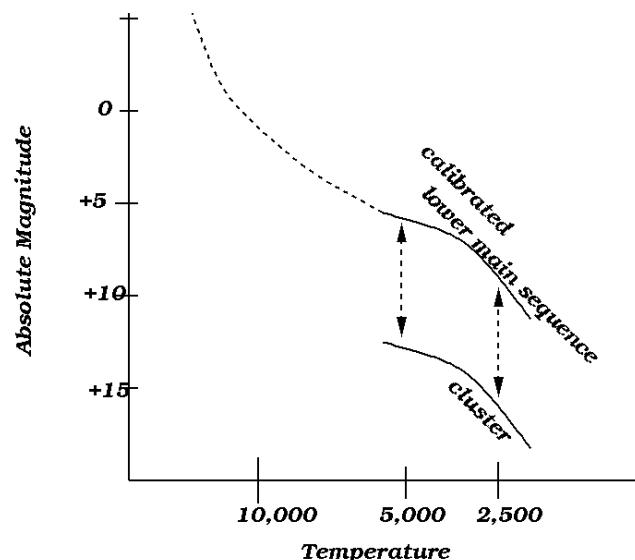


https://astro.unl.edu/naap/distance/cluster_fitting.html

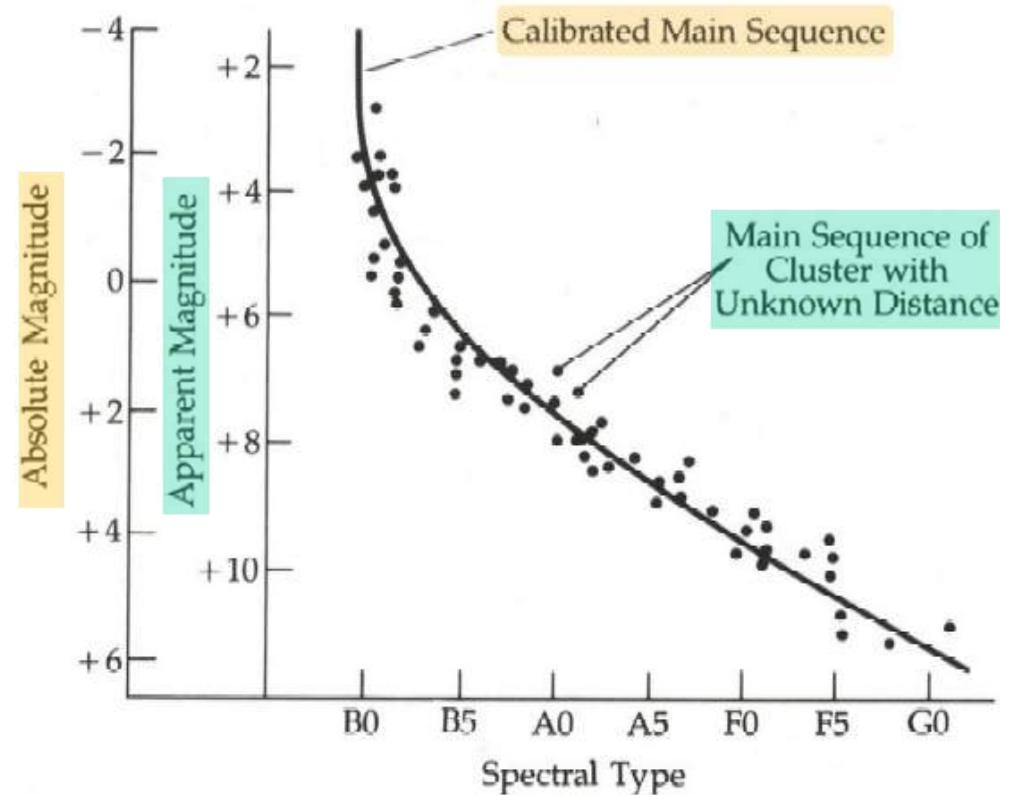
Main-sequence fitting

Spectroscopic parallax – using spectral type

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→ shift up and down (in magnitude)
- $(\text{test cluster apparent mag}) - (\text{calibrated absolute mag}) = (m-M)$
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https://ned.ipac.caltech.edu/level5/Bothun2/Bothun2_3_2.html



A calibrated H-R diagram

Introductory Astronomy and Astrophysics (4th edition)
Michael Zeilik & Stephen A. Gregory (1998), p. 266

Main-sequence fitting

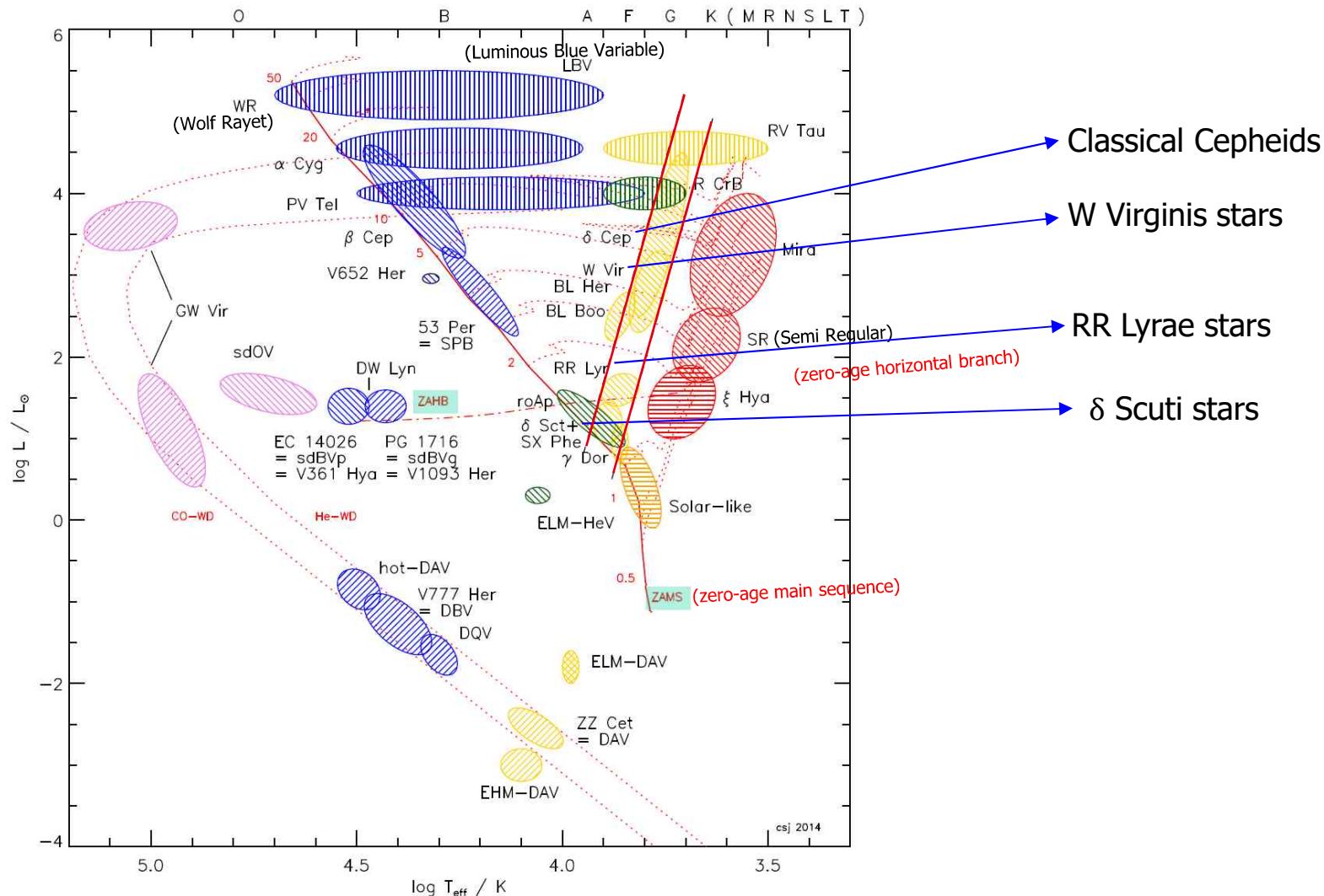
2. Pulsating Variable Stars – Cepheids, RR Lyrae

Instability strip

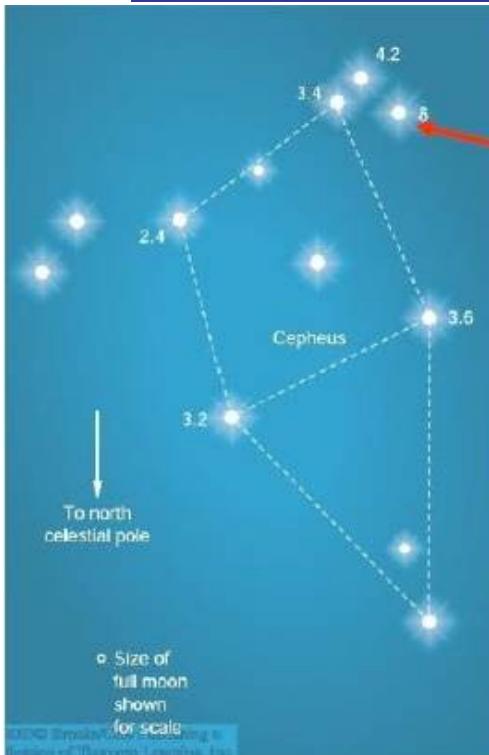
(불안정띠)

: stars are unstable to pulsations

: expand – contract → luminosity changes

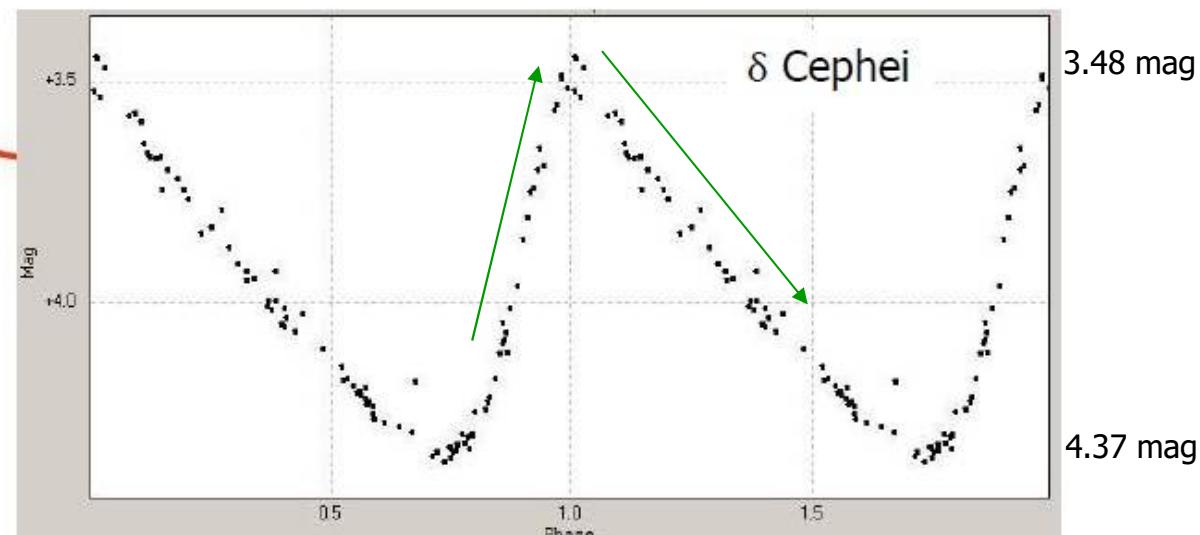


Cepheid Variables – Light Curves (LCs)



= δ Cepheids
 = Classical Cepheids
 $M_i \geq 5 M_{\odot}$
 (young stars)
 (in spiral arms)
 Age ≤ 0.1 Gyr

Galactic Astronomy (J. Binney & M. Merrifield, 1998) p. 291



P = 5.366341 d (<http://earthsky.org/brightest-stars/delta-cephei-the-kings-famous-variable-star>)

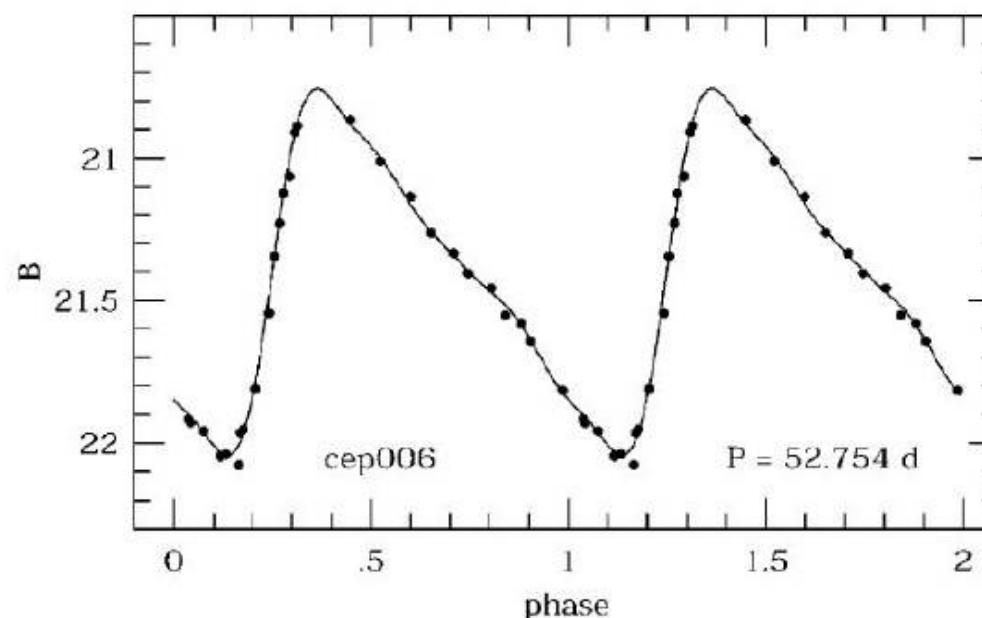
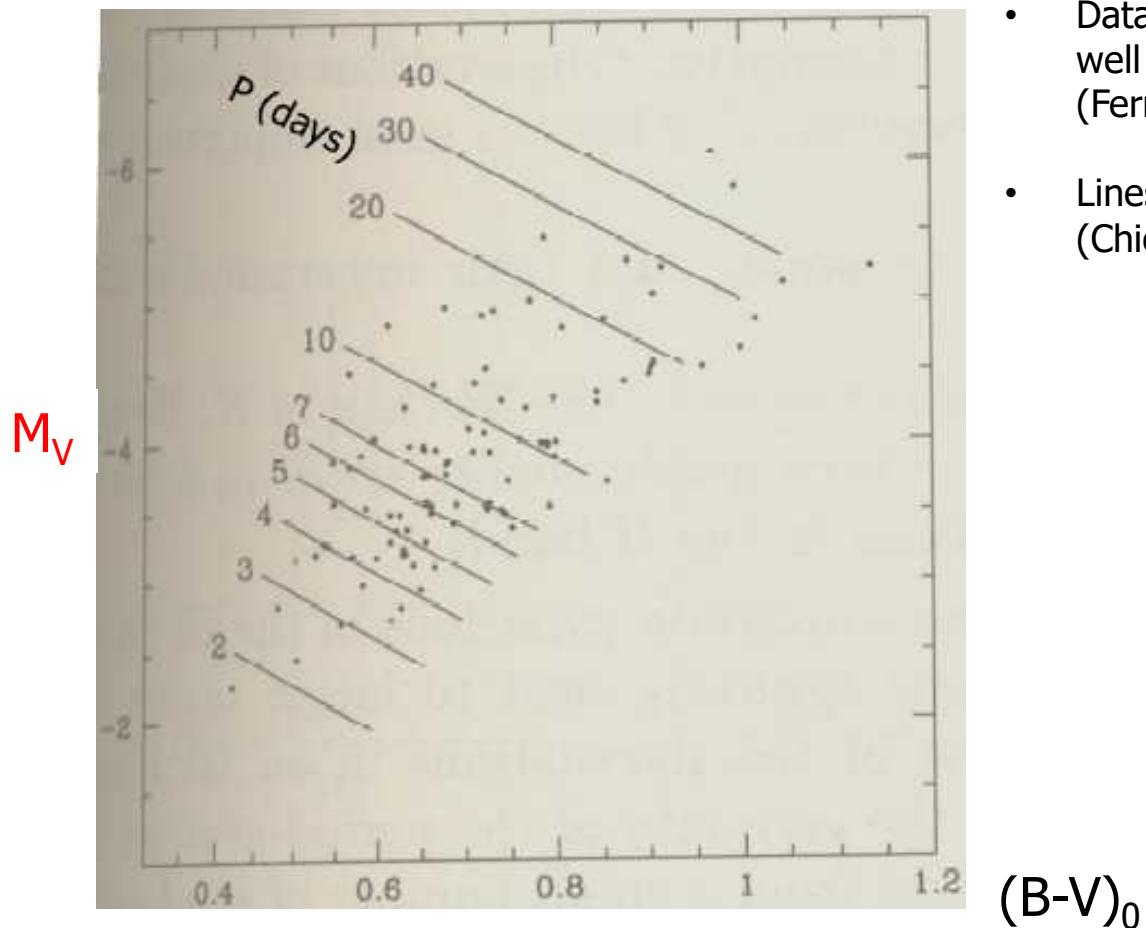


Figure 1: B light-curve of a typical Cepheid in NGC 300. The data were obtained with the ESO-MPA 2.2-m telescope and Wide Field Imager.

Cepheid Variables

Instability strip



- Data : 98 Galactic Cepheids with well determined reddening (Fernie 1990 ApJ 354 295)
- Lines \leftarrow stellar evolution models (Chiosi+93 ApJS 86 541)

Cepheid Variables

- Periodic (regular) variables
- Pulsation period \propto median luminosity
- Period-Luminosity relation (**P-L relation**) :
Leavitt's law
- Populations I, II - separate relations
- **Classical Cepheids** (pop I Cepheids) : more luminous, in spiral arms, $P = 1 - 50$ d (5-10 d), F6 to K2

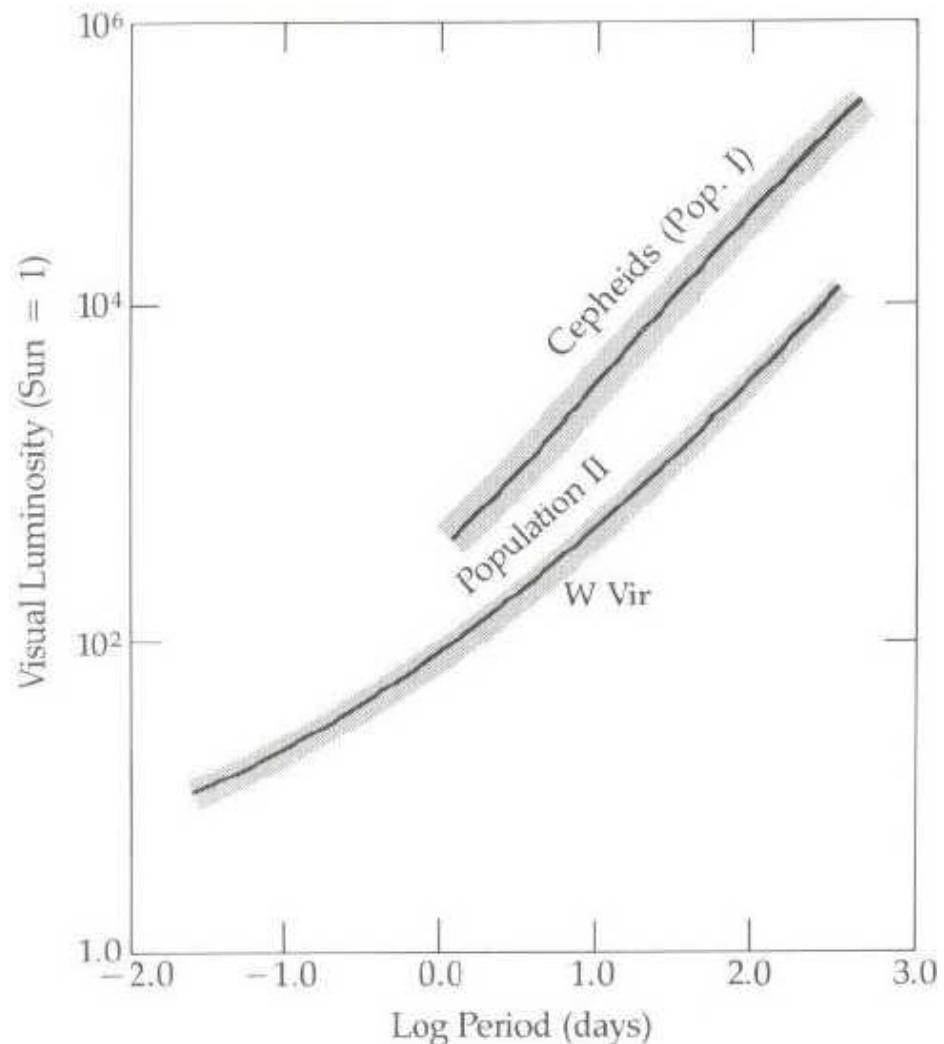
$$\langle M_V \rangle = -2.76 \log(P/10\text{ d}) - 4.16$$

(scatter ~ 0.27 mag)

Galactic Astronomy (J. Binney & M. Merrifield, 1998, p. 292)

- **W Virginis Stars** (pop II Cepheids) : 4-times less luminous than classical Cepheids, in globular clusters and other population II systems, $P = 2 - 45$ d (12-20 d), F2 to G6

* population (pop) I : young
* population (pop) II : old



Henrietta S. Leavitt (1912, Harvard College Obs. Circ., 173, 1 'Discovery of the Cepheid PL relation')

Introductory Astronomy and Astrophysics (4th edition)
Michael Zeilik & Stephen A. Gregory (1998), p. 356

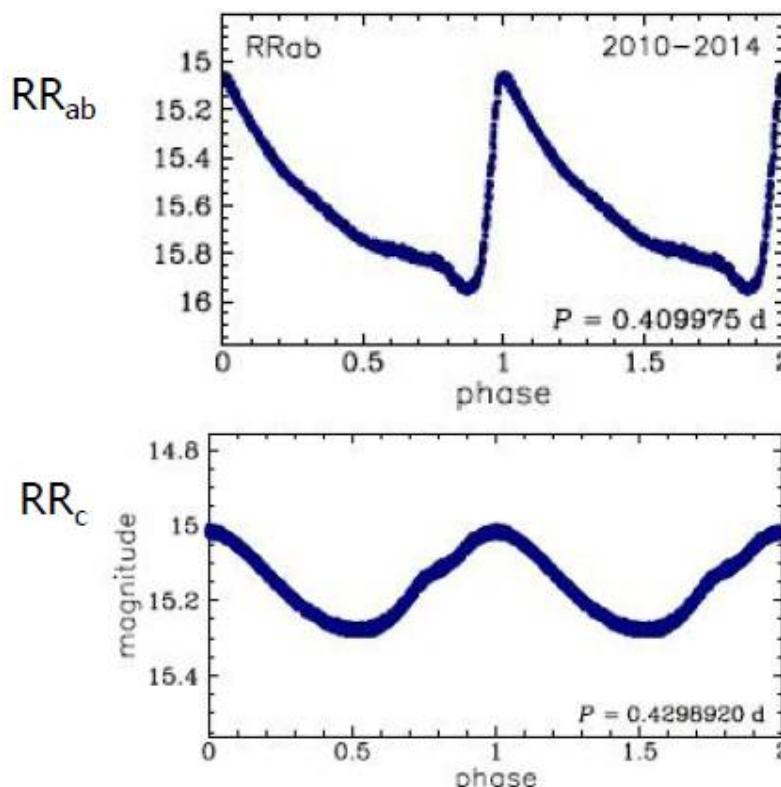
3. RR Lyrae stars

- Periodic variable stars
- $P = 1.5$ to 24 h (~ 12 h), Peak $M_V \sim 0.7$ - 0.8 mag, spectra A2 to F6
- Current mass $\sim 0.8 M_\odot$ (original MS mass $\sim 1 M_\odot$), old, relatively metal-poor
- In GCs and in low-metallicity systems (population II) – But, some have high metallicity

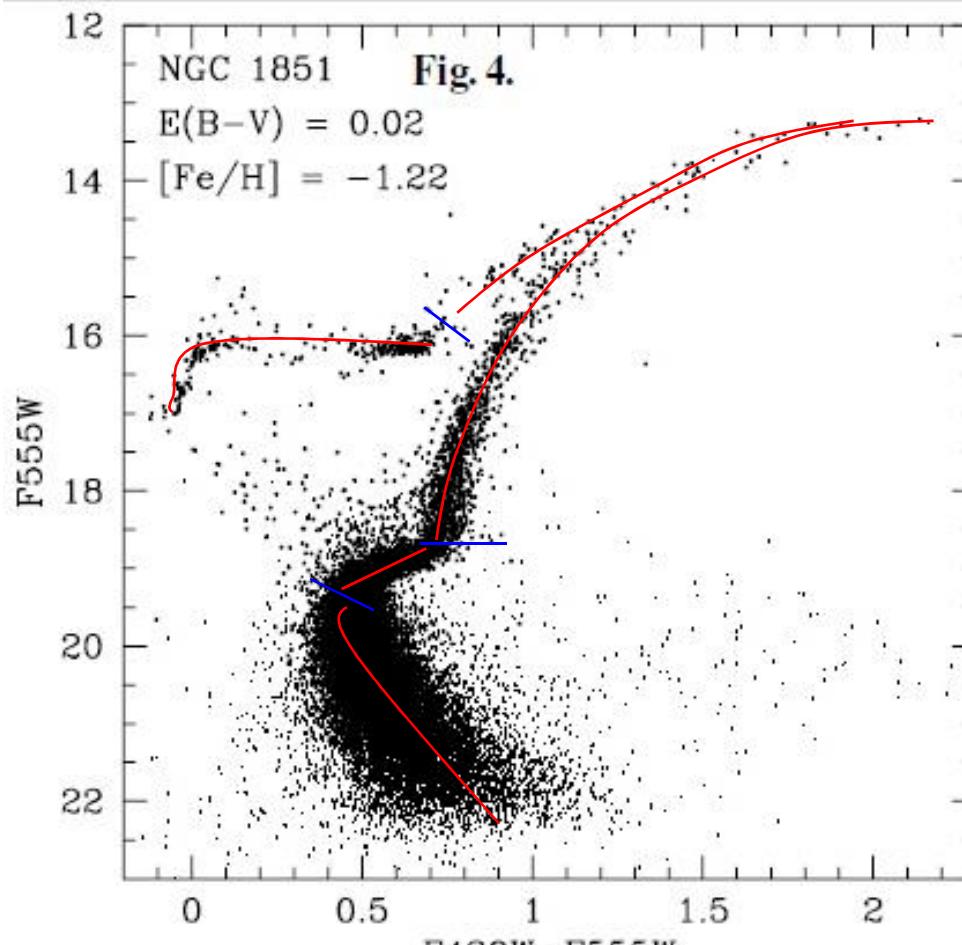
$M_V(RR) = +0.71 \pm 0.12$ at $\langle [\text{Fe}/\text{H}] \rangle = -1.61$ for the halo (162 stars)

$M_V(RR) = +0.79 \pm 0.30$ at $\langle [\text{Fe}/\text{H}] \rangle = -0.76$ for the thick disk (51 stars)

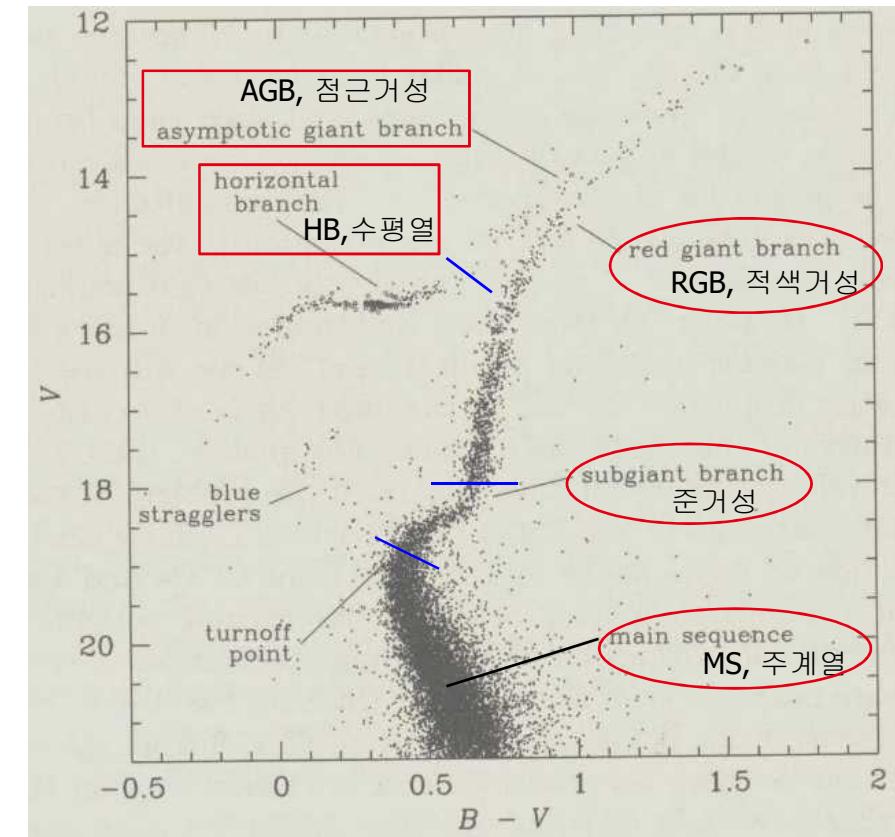
Layden+ 96 AJ 112 2110



Color-Magnitude Diagrams for globular clusters (GCs)

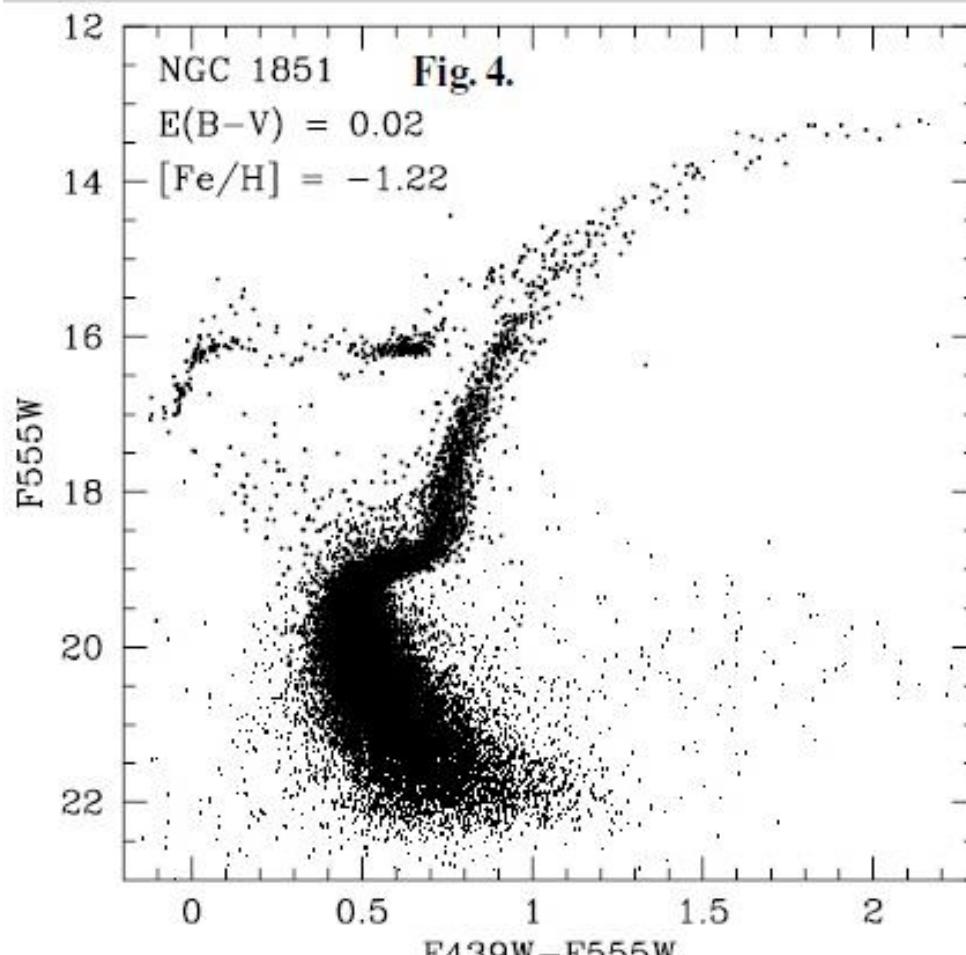


Piotto et al. (2002, A&A, 391, 945)

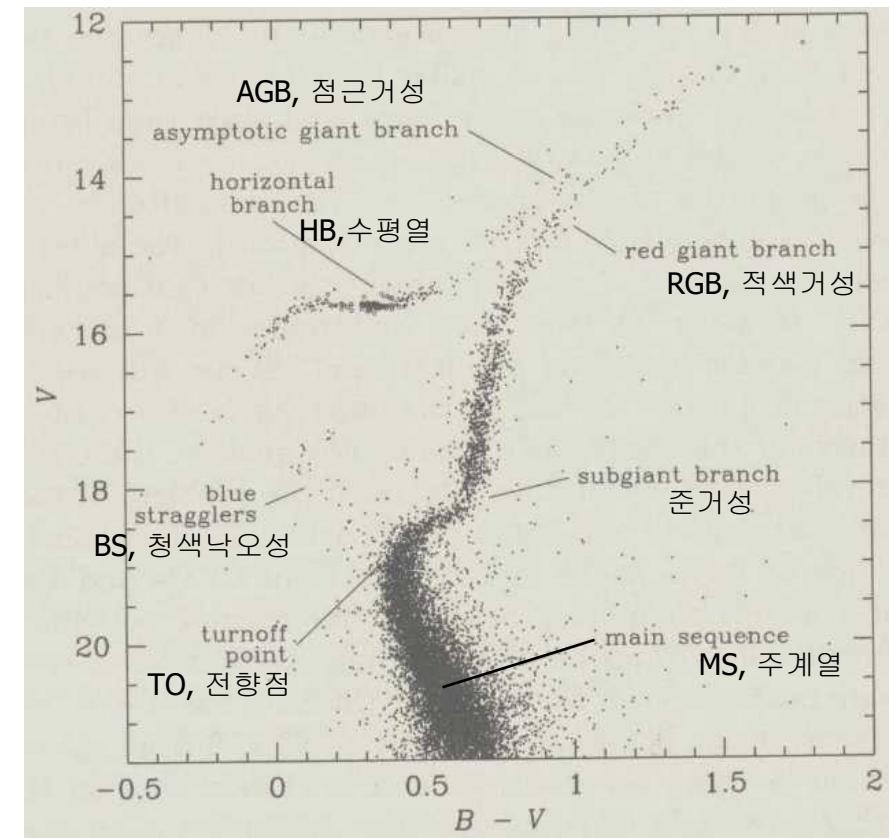


GC M3 (NGC 5272)
 (variables=open circles)

Color-Magnitude Diagrams for globular clusters (GCs)



Piotto et al. (2002, A&A, 391, 945)



GC M3 (NGC 5272)
(variables=open circles)

4. Tip of the red giant branch (TRGB)

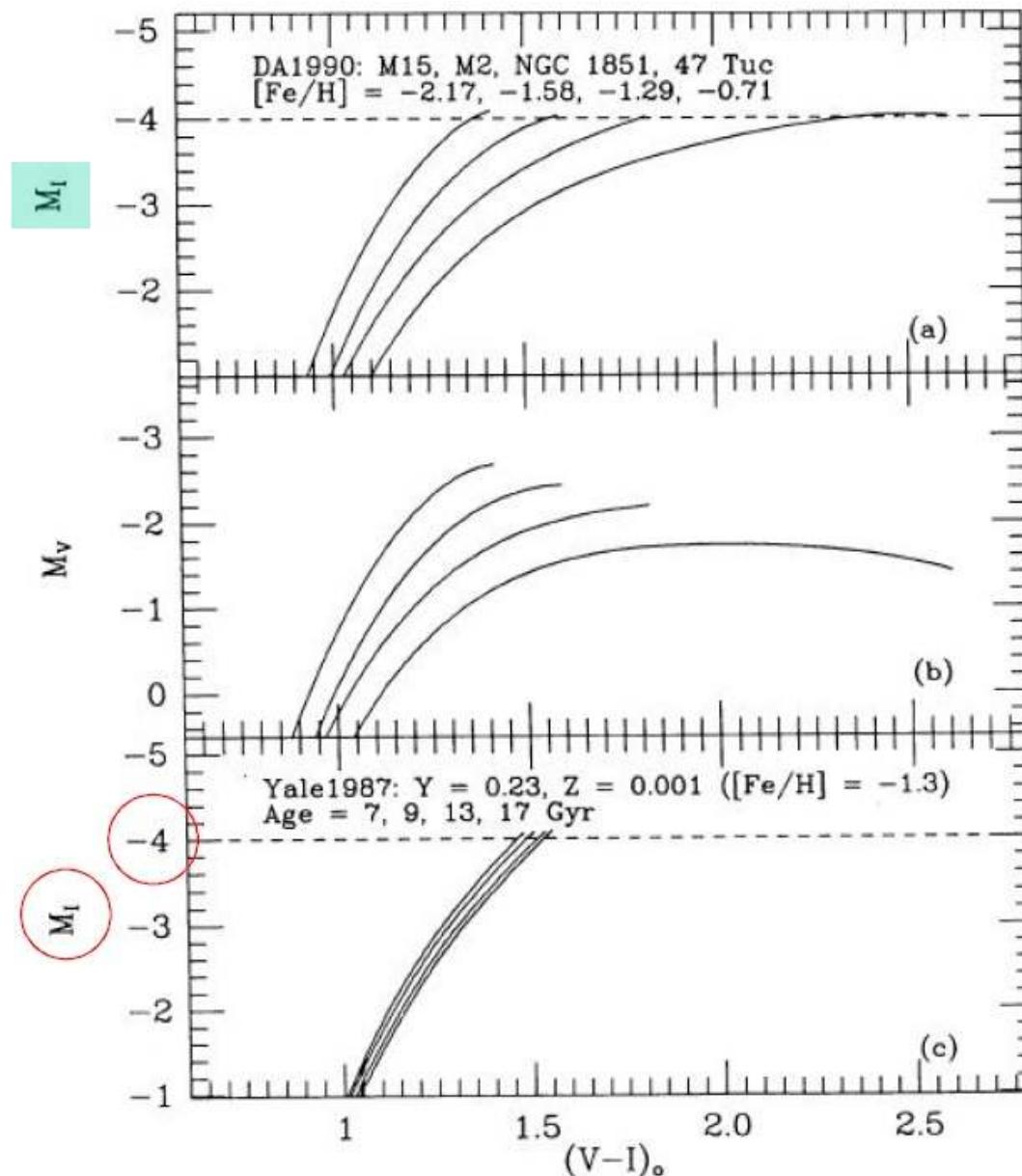


Fig. 1

Lee et al. 1993, ApJ, 417, 553
이명근

Citations 686

Tip of the red giant branch (TRGB)

TABLE 1
DISTANCE ESTIMATES FOR RESOLVED GALAXIES BASED ON PRIMARY DISTANCE INDICATORS

GALAXY (1)	TYPE ^a (2)	$E(B-V)$ (3)	$(m - M)_0$			I_{TRGB} (7)	REFERENCE ^b (8)	$[\text{Fe}/\text{H}]^c$ (9)	M_B (10)	M_V (11)
			Cepheid (4)	RR Lyrae (5)	I_{TRGB} (6)					
LMC	SBmII	0.10	18.50	18.28	18.42	14.6	1, 2, 3	-1.2	-17.93	-18.36
NGC 6822	ImIV-V	0.28	23.62	...	23.46	20.05	4, 4	-1.8:	-15.13	-16.42
NGC 185	dE3pec	0.19	...	24.01	23.94	20.30	5, 6	-1.2	-14.63	-15.52
NGC 147	dE5	0.17	...	24.06	24.13	20.4	7, 8	-0.9	-14.39	-15.17
IC 1613	IMV	0.02	24.42	24.27	24.27	20.25	1, 9, 10	-1.3	-14.51	-15.16
M31	Sbl-II	0.08	24.44	24.36	24.44	20.55	1, 11, 12	-0.8	-20.98	-21.74
M33	Sc(s)II-III	0.10	24.63	24.71	24.70	20.95	1, 13, 12	-2.0	-18.94	-19.40
WLM	ImIV-V	0.02	24.92	...	24.81	20.85	14, 14	-1.6:	-14.28	-14.62
NGC 205	S0/dE5pec	0.035	...	24.76	24.42	20.45	15, 16	-0.8	-15.80	-16.62
NGC 3109	SmlV	0.04	25.5	...	25.45	21.55	17, 18	-1.6	-15.95	-16.25

^a From Sandage & Tammann 1987.

^b References: (1) Madore & Freedman 1991, (2) Walker 1988, (3) Reid & Mould 1987, (4) Lee, Freedman, & Madore 1993, (5) Saha & Hoessel 1990, (6) Lee, Freedman, & Madore 1992, 1993c; (7) Saha, Hoessel, & Mossman 1990; (8) Mould, Kristian, & Da Costa 1983; (9) Saha et al. 1992; (10) Freedman 1988; (11) Pritchett & van den Bergh 1987, 1988; (12) Mould & Kristian 1986; (13) Pritchett 1988; (14) Lee, Freedman, & Madore 1993a; (15) Mould, Kristian, & Da Costa 1984; (16) Saha, Hoessel, & Krist 1991; (17) Capaccioli, Piotto, & Bresolin 1992; (18) Lee 1993.

^c The metallicity $[\text{Fe}/\text{H}]$ has been determined using the color $(V-I)_{-3.5}$.

$$-2.2 < [\text{Fe}/\text{H}] < -0.7 \text{ dex}$$

Tip of the red giant branch (TRGB)

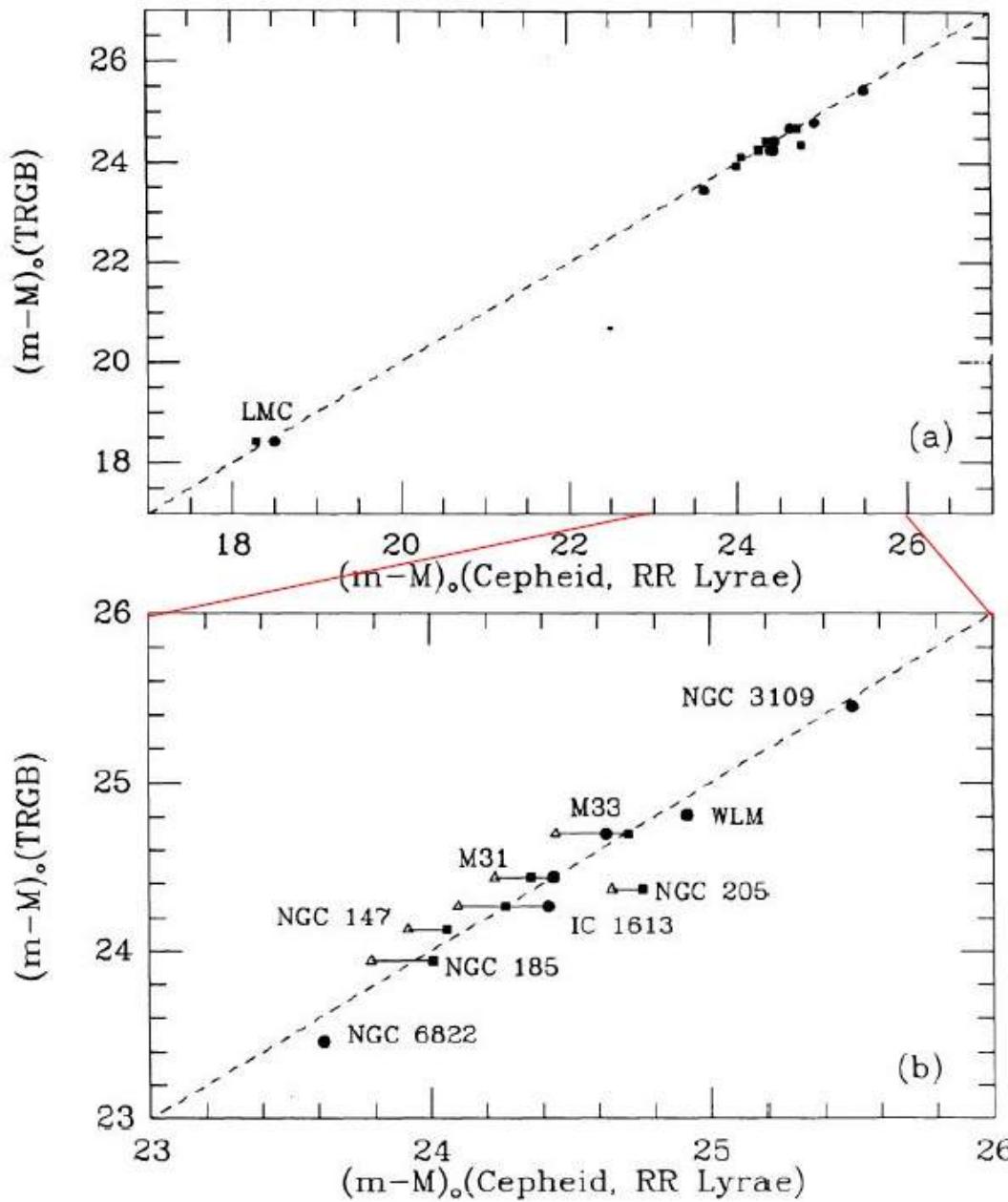


Fig. 4

Lee et al. 1993, ApJ, 417, 553

- No repeated observations
- Less extinction
- Large luminosity

⌘ Mass fractions

Mass ratios (rather than numbers of particles)

$$\text{Mass fractions of hydrogen : } X \equiv \frac{\text{total mass of hydrogen}}{\text{total mass of gas}}$$

$$\text{Mass fractions of helium : } Y \equiv \frac{\text{total mass of helium}}{\text{total mass of gas}}$$

$$\text{Mass fractions of metals : } Z \equiv \frac{\text{total mass of metals}}{\text{total mass of gas}}$$

$$X + Y + Z = 1$$

For stars, usually, $X \sim 0.7$, $0 < Z < 0.03$

$$[\text{Fe}/\text{H}] = \log \frac{(\text{Fe}/\text{H})_*}{(\text{Fe}/\text{H})_\odot} = \log (\text{Fe}/\text{H})_* - \log (\text{Fe}/\text{H})_\odot \quad \text{dex}$$

$$\log Z = 0.977[\text{Fe}/\text{H}] - 1.699$$

$$[\text{Fe}/\text{H}] = 1.024 \log Z + 1.739$$

An Introduction to Modern Astrophysics (2nd edition) Bradley W. Carroll & Dale A. Ostlie (1996) p. 325

<https://en.wikipedia.org/wiki/Metallicity>

<http://burro.case.edu/Academics/Astr222/Galaxy/Structure/metals.html>

Bertelli et al. (1994 A&AS 106 275 – Theoretical isochrones from models with new radiative opacities)

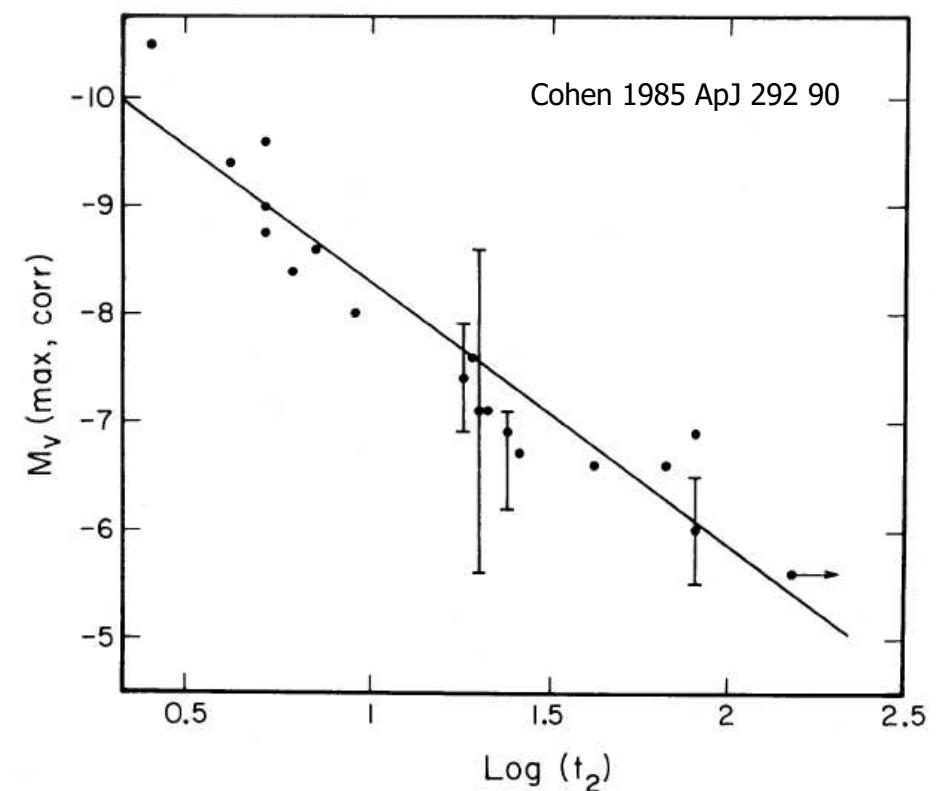
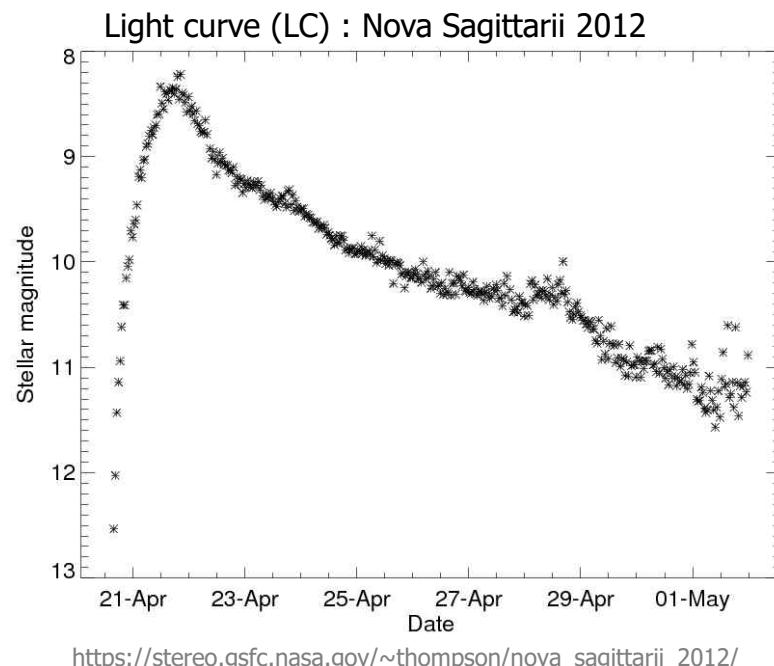
5. Novae (신성) – Rate of Decline

- Peak brightness : $M_V = -5 \sim -10$
- MMRD (Maximum Magnitude – Rate of Decline) relation
light from faint novae decays more slowly

$$M_V(\text{max, corr}) = -10.70(\pm 0.30) + 2.41(\pm 0.23) \log t_2$$

t_2 : time that nova takes to decline in brightness by 2 mag from the maximum

Cohen 1985 ApJ 292 90 (eqn. 3)

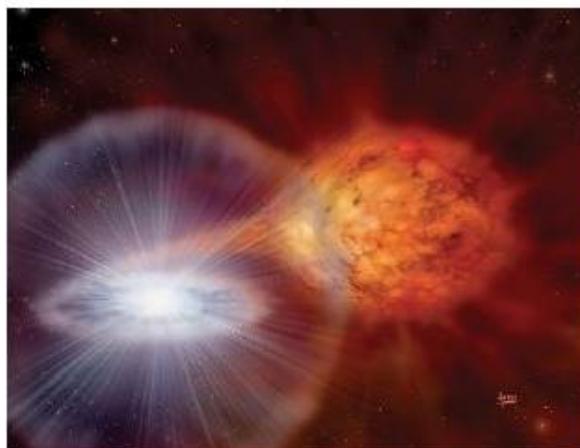


6. Supernovae (초신성)

- Brightest objects in galaxies ($M_V = -14 \sim -22$)

- Typical types

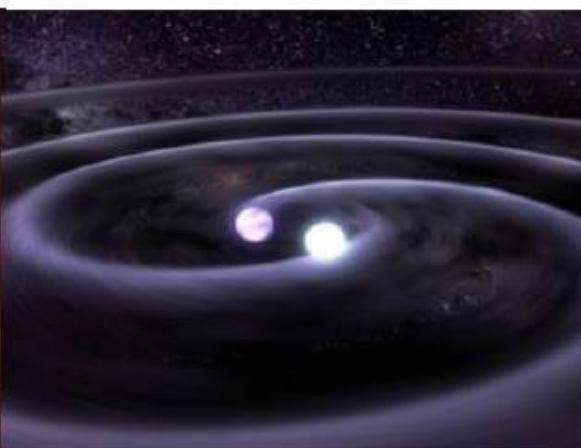
No H lines (pop II) → Type Ia



WD + Giant/MS/He *
(Single Degenerate, SD)

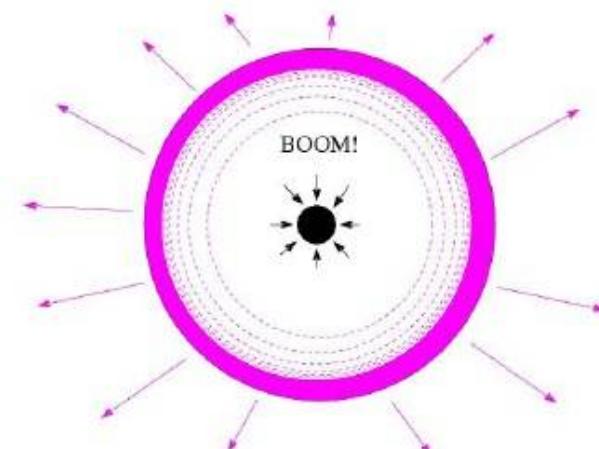
SNe Ia (thermonuclear stellar explosion)
(WD originated SNe)

백색왜성 기원 초신성



WD + WD
(Double Degenerate, DD)

H lines (pop I) → Type II



Core collapse

Ib
Ic

CC SNe

핵붕괴 초신성

<http://dujs.dartmouth.edu/2008/05/type-ia-supernovae-properties-models-and-theories-of-their-progenitor-systems>

http://wwwmpa.mpa-garching.mpg.de/mpa/research/current_research/hl2013-8/hl2013-8-en.html

http://spiff.rit.edu/richmond/sdss/sn_survey/sn_survey.html

SN Ia absolute magnitude

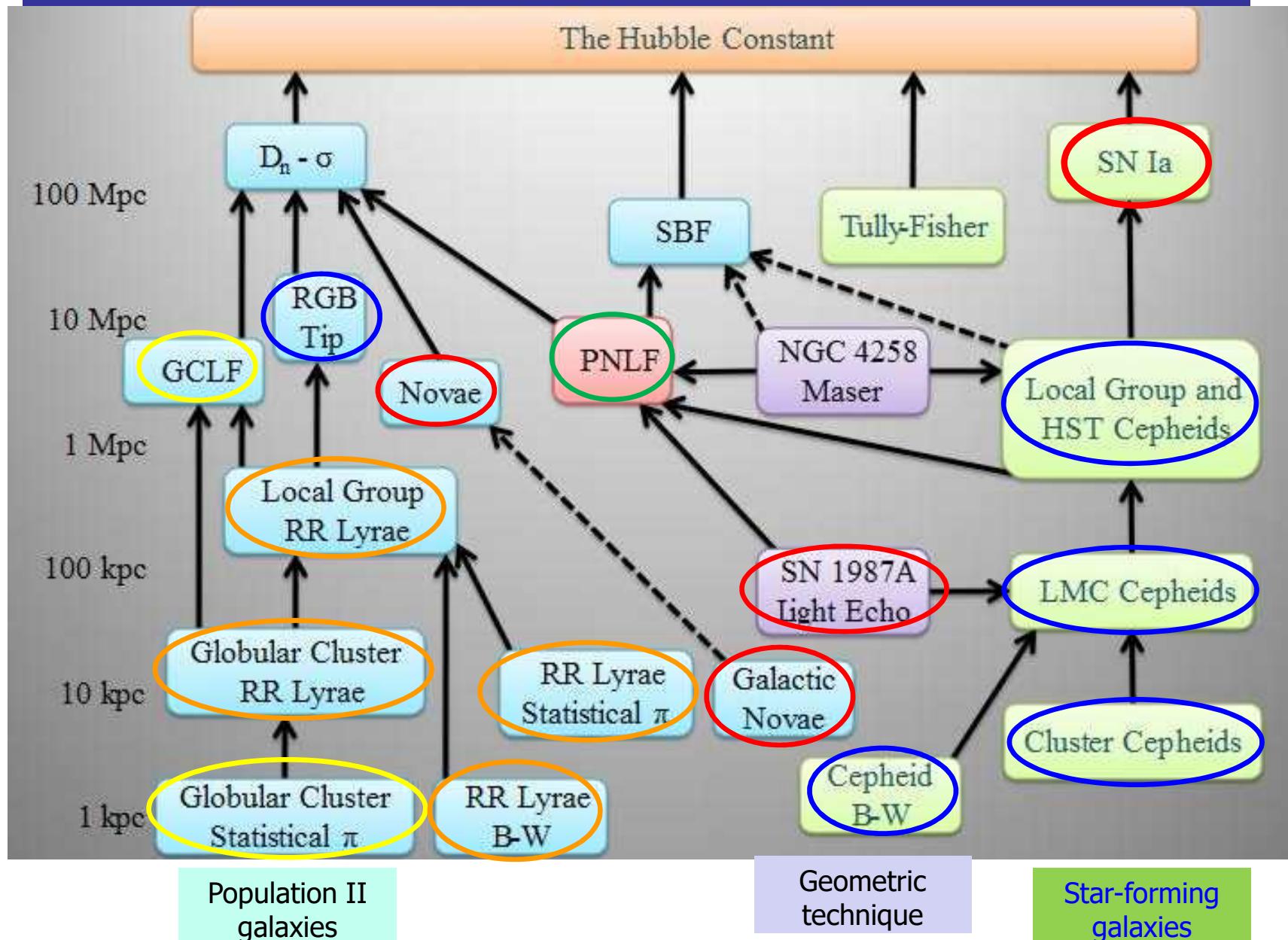
Photometrically, SN Ia rise to maximum light in a period of approximately 20 days (Riess et al 1999b) reaching

$$M_B \approx M_V \approx -19.30 \pm 0.03 + 5 \log(H_0/60) \quad (1)$$

with a dispersion of $\sigma_M \leq 0.3$ (Hamuy et al 1996b).

W. Hillebrandt & J. C.Niemeyer (2000, ARA&A, 38, 191 – Type Ia SN
explosion models)

Extragalactic Distance Ladder



1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)

1.3 Magnitudes (등급)



<http://www.centauri-dreams.org/?p=11322>

<http://www.centauri-dreams.org/wp-content/uploads/2010/02/light-candles.jpg>

1. Magnitude scale

$$m - n = 2.5 \log\left(\frac{l_n}{l_m}\right)$$

→ apparent magnitude (겉보기등급, 실시등급)

- $m > n \leftarrow l_n > l_m$
- Brighter objects : numerically smaller magnitudes

Absolute magnitude, Distance modulus

- A very luminous star appears dim – if far away
- A low-luminosity star look bright – if very close
→ distance links fluxes and luminosities
- **absolute magnitude (절대등급)** = the magnitude to be observed if the star is placed at a distance of **10 pc** from the Sun → capital M

$$\frac{L}{l} = \left(\frac{d}{D}\right)^2 = \left(\frac{d}{10}\right)^2$$

- $M - L, m - l$

$$m - M = 2.5 \log\left(\frac{L}{l}\right) = 2.5 \log\left[\left(\frac{d}{10}\right)^2\right] = 5 \log\left(\frac{d}{10}\right)$$

- Apply extinction correction :

"distance modulus"

$$m - M = 5 \log d - 5 + A$$

(e.g.) $V - M_V = 5 \log d - 5 + A_V$

$$(m - M)_0 = 5 \log d - 5$$

Subscript 0 :
"extinction corrected"

2. Photometric Filter Systems (측광계)

Bandwidth :

Broadband : $\Delta\lambda < 1000 \text{ \AA}$ (광대역)

Intermediate band : $70 \text{ \AA} < \Delta\lambda < 400 \text{ \AA}$ (중대역)

Narrowband : $\Delta\lambda < 70 \text{ \AA}$ (협대역)

2. Photometric Filter Systems (측광계)

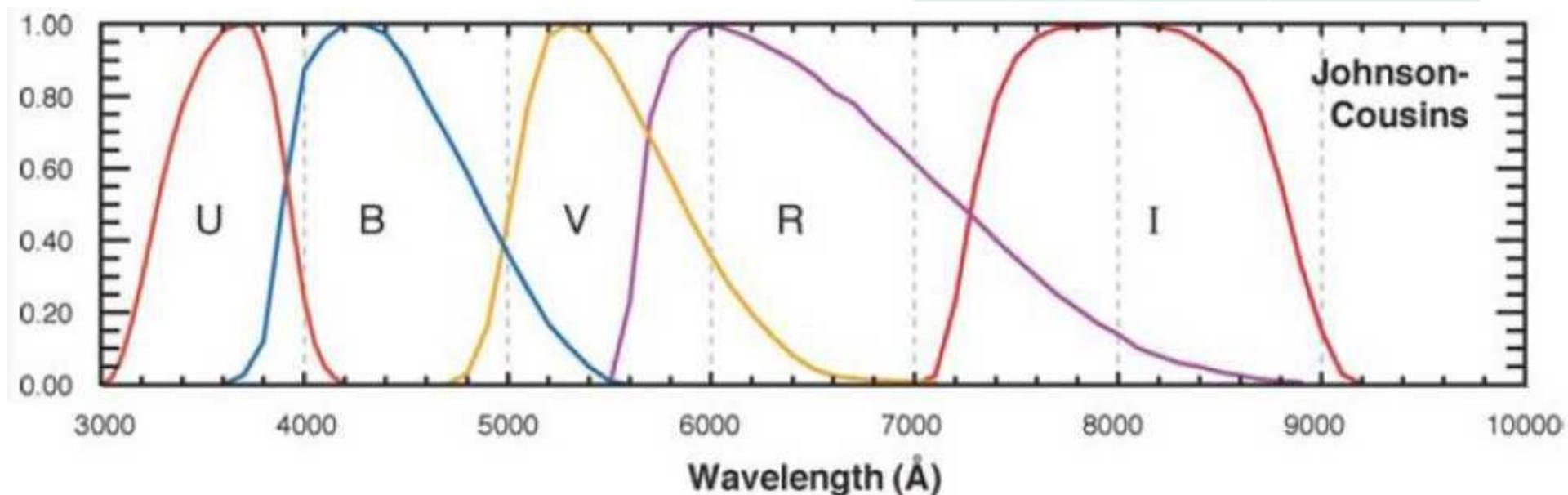
➤ Johnson-Cousins UBVRI System

- Originally defined by Johnson & Morgan (1953) : UBV
- Extended by Cousins (1974) : UBVRI
- Re-analyzed by Bessell (1990)

	Effective Wavelength (λ_{eff})	Bandpass ($\Delta\lambda$)
U	3663 Å	650 Å
B	4361 Å	890 Å
V	5448 Å	840 Å
R	6407 Å	1580 Å
I	7980 Å	1540 Å

$$\begin{aligned}1 \text{ nm} &= 10^{-9} \text{ m} \\1 \text{ Å} &= 10^{-10} \text{ m} \\1 \text{ nm} &= 10 \text{ Å}\end{aligned}$$

$$366 \text{ nm} =$$



2. Photometric Filter Systems (측광계)

➤ Sloan Digital Sky Survey (SDSS) System

- ugriz

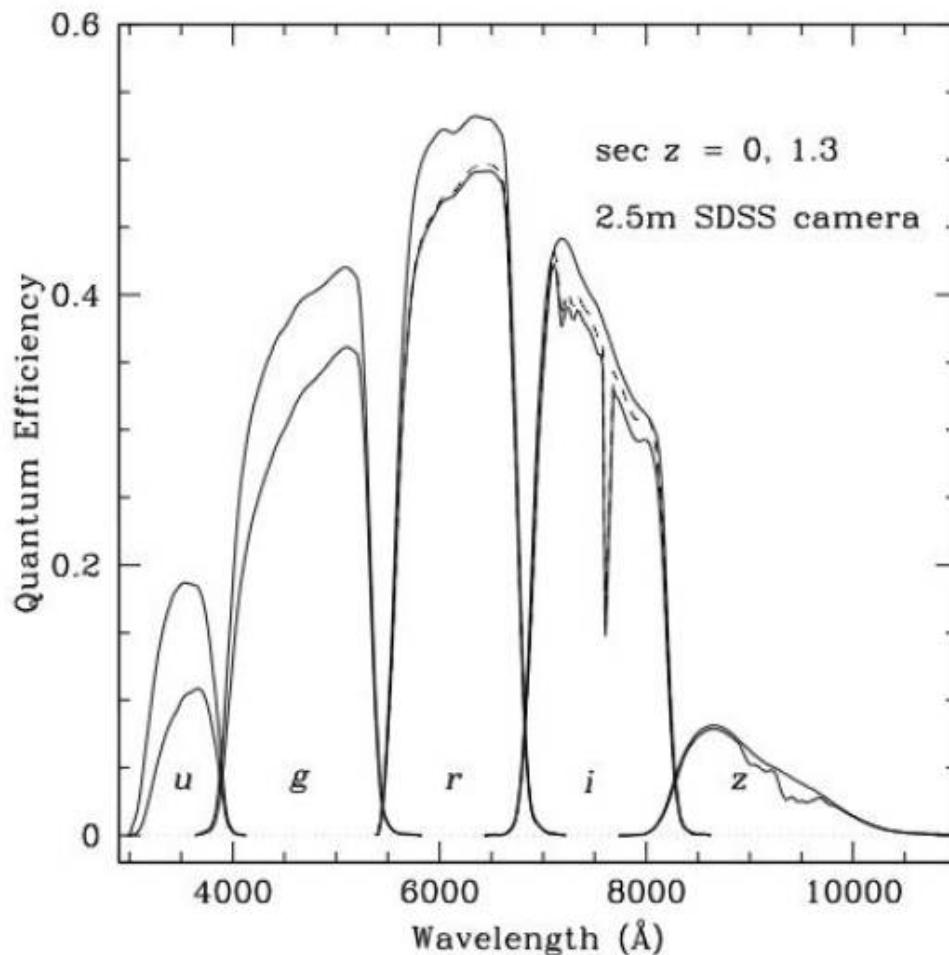


TABLE 19
SDSS FILTER PARAMETERS

Name	λ_{eff} (Å)	σ^2	FWHM (Å)	Q
u.....	3551	3.00×10^{-3}	581	0.0171
g.....	4686	7.13×10^{-3}	1262	0.0893
r.....	6166	3.13×10^{-3}	1149	0.0886
i.....	7480	2.58×10^{-3}	1237	0.0591
z.....	8932	3.18×10^{-3}	994	0.0099

3. Color Index (CI, 색지수, 색)

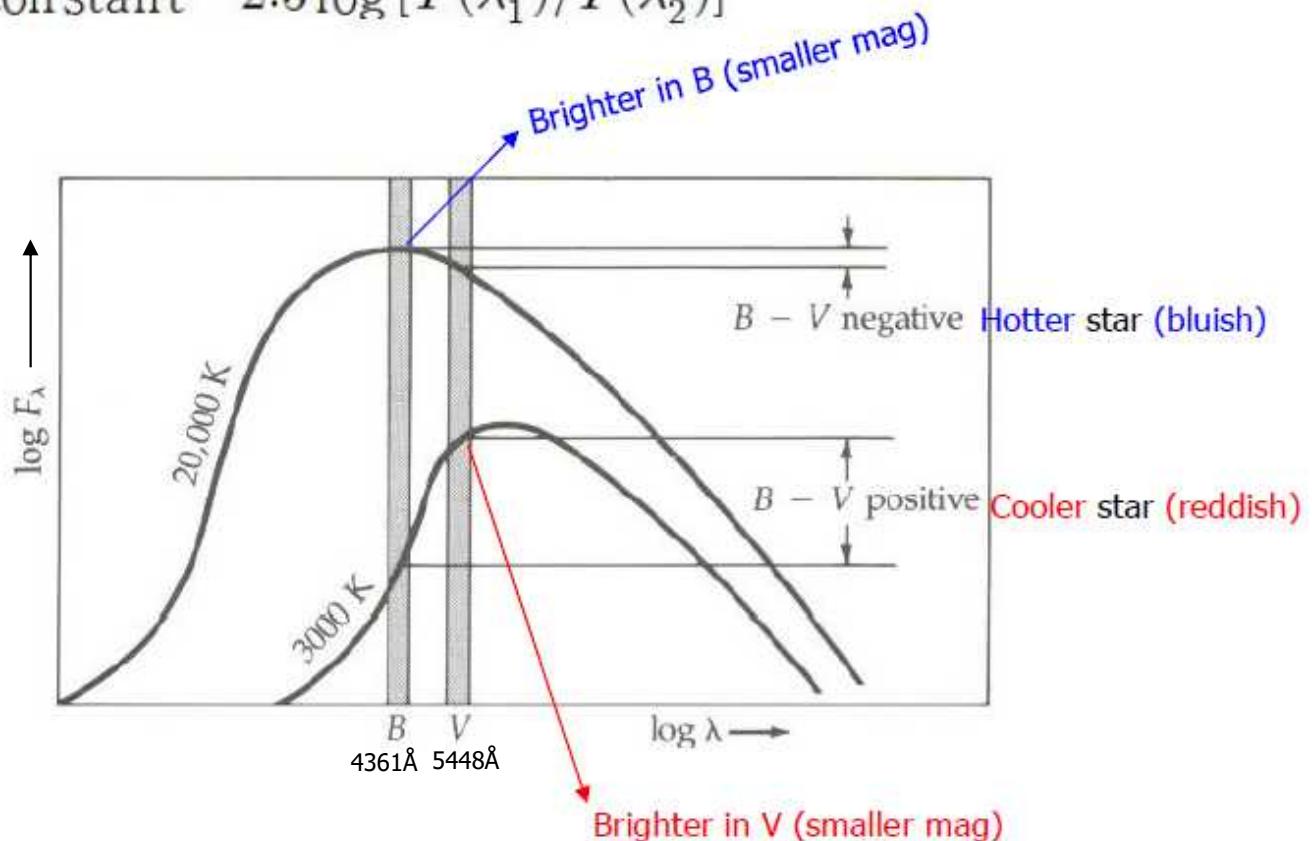
- Color index = difference between magnitudes at two different effective wavelengths

$$CI = m(\lambda_1) - m(\lambda_2)$$

- Mag difference \rightarrow flux ratio at the specific wavelengths involved

$$CI = \text{constant} - 2.5 \log [F(\lambda_1)/F(\lambda_2)]$$

- Hotter stars (bluish) : negative CI
- Cooler stars (reddish) : positive CI



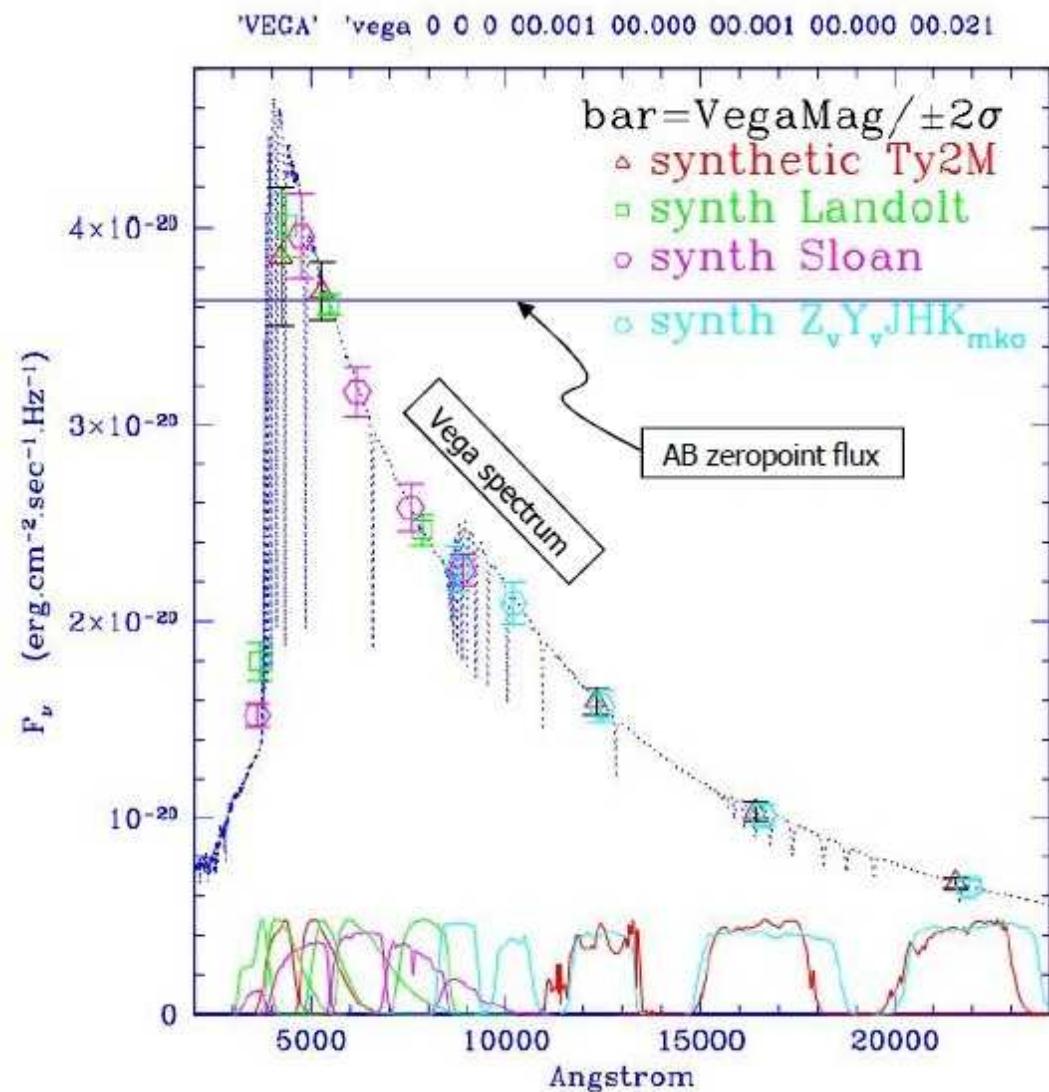
Magnitude systems

➤ Vega magnitude system

- Vega ($=\alpha$ Lyr) : the primary calibrating star
- Surface temperature = 10,000 K
- CI = 0
- Zero-point was defined in terms of unreddened main-sequence (MS) stars of class A0 ... with an accuracy sufficient to permit the placement of the zero-point to about 0.01 mag

➤ AB magnitude system

- Magnitude zero point corresponds to a flux density of 3631 Jy (1 Jy = 1 Jansky = 10^{-26} W Hz $^{-1}$ m $^{-2}$ = 10^{-23} erg s $^{-1}$ Hz $^{-1}$ cm $^{-2}$)



Pickles & Depagne (2010 PASP 122 1437)

- Bessell (2005, ARA&A, 43, 293 – Standard photometric systems)
- Casagrande & Vandenberg (2014, MNRAS, 444, 392 – Synthetic stellar photometry. I. General considerations and new transformations for broad-band systems)

4. Color Excess, Bolometric Magnitude

- Interstellar dust grains absorb and scatter starlight
- Observed light gets faint (**extinction**) and appears redder (**interstellar reddening**)
(소광) (성간적색화: λ -dependent)

- **Color Excess** (색초과) = observed color – intrinsic color

$$E(B-V) = (B-V) - (B-V)_0$$

- **Interstellar extinction** :

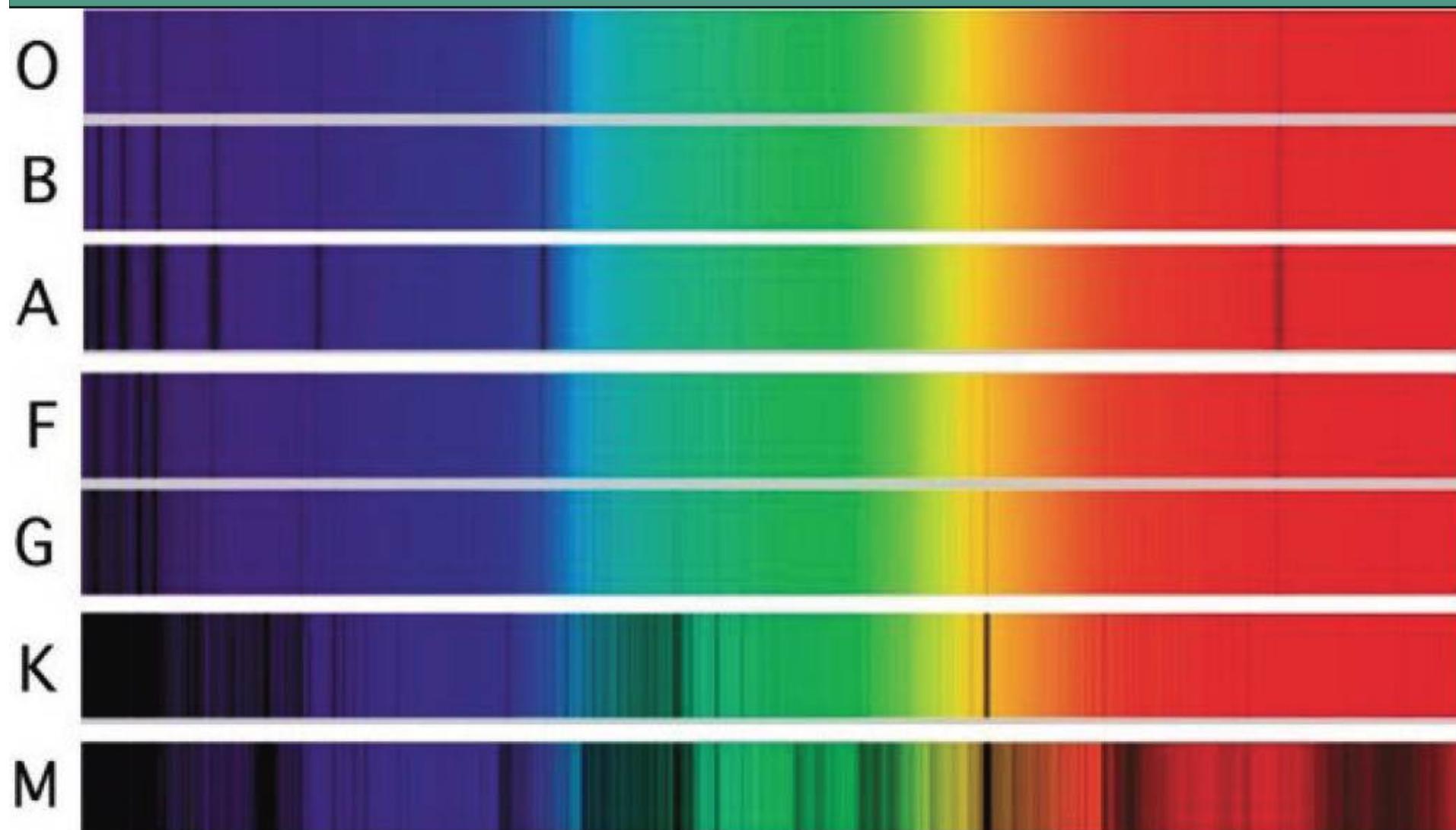
$$A_V \sim R \times E(B-V), \quad R = 3.0, 3.1, 3.2, 3.3$$

R : total-to-selective extinction ratio

- ← • Amount of interstellar medium (ISM)
• ISM composition
• Galactic longitude

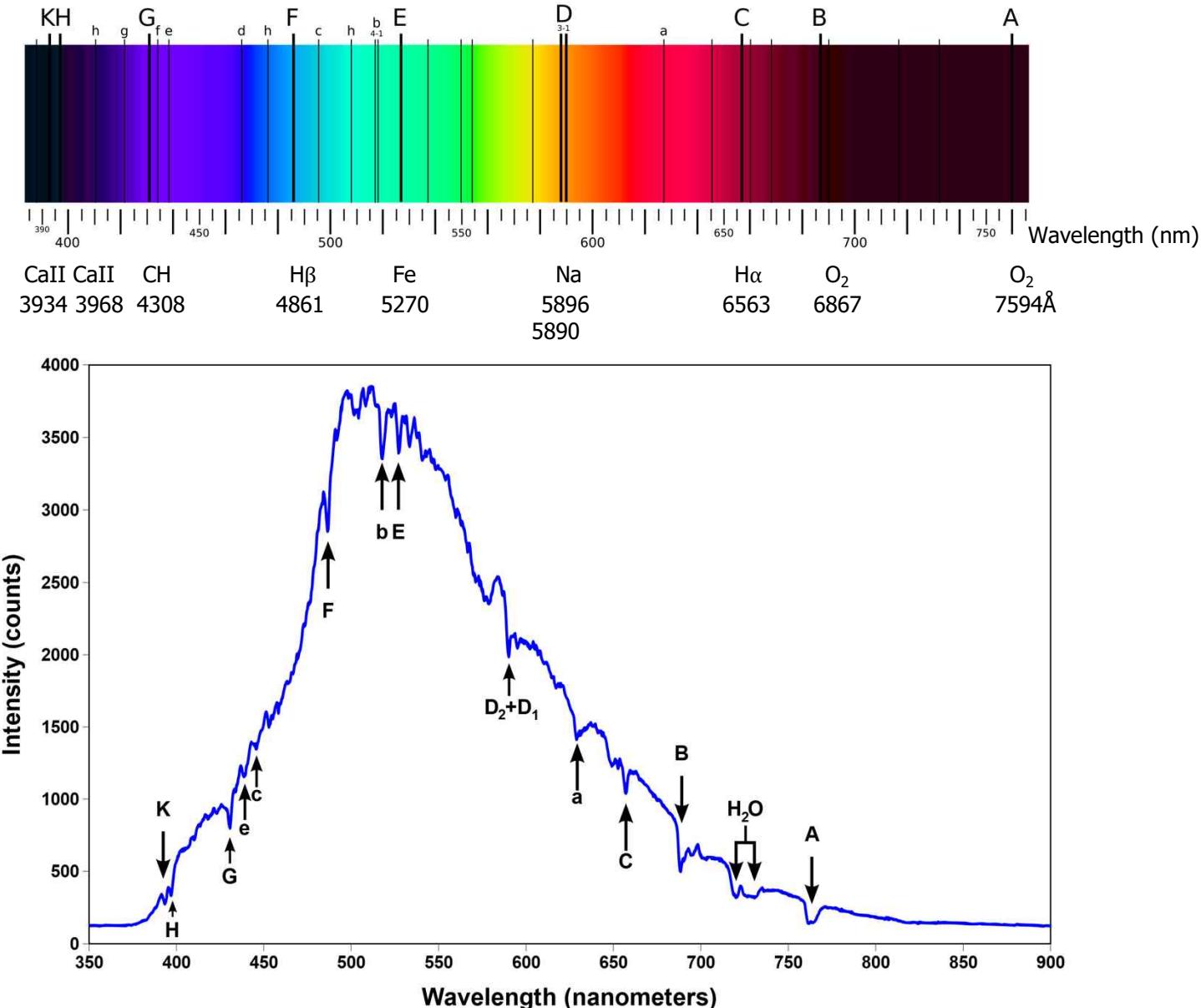
1. Stars: The Hertzsprung-Russell Diagram (항성: HR도)

1.4 The Classification of Stellar Spectra (별의 스펙트럼 분류)



Fraunhofer lines

Joseph von Fraunhofer observed **dark absorption lines** in the Solar optical spectrum (1814)



Spectral types

How to memorize spectral types?

OBAFGKM



Oh Beautiful And Fine
Girl(Guy),
Kiss Me!

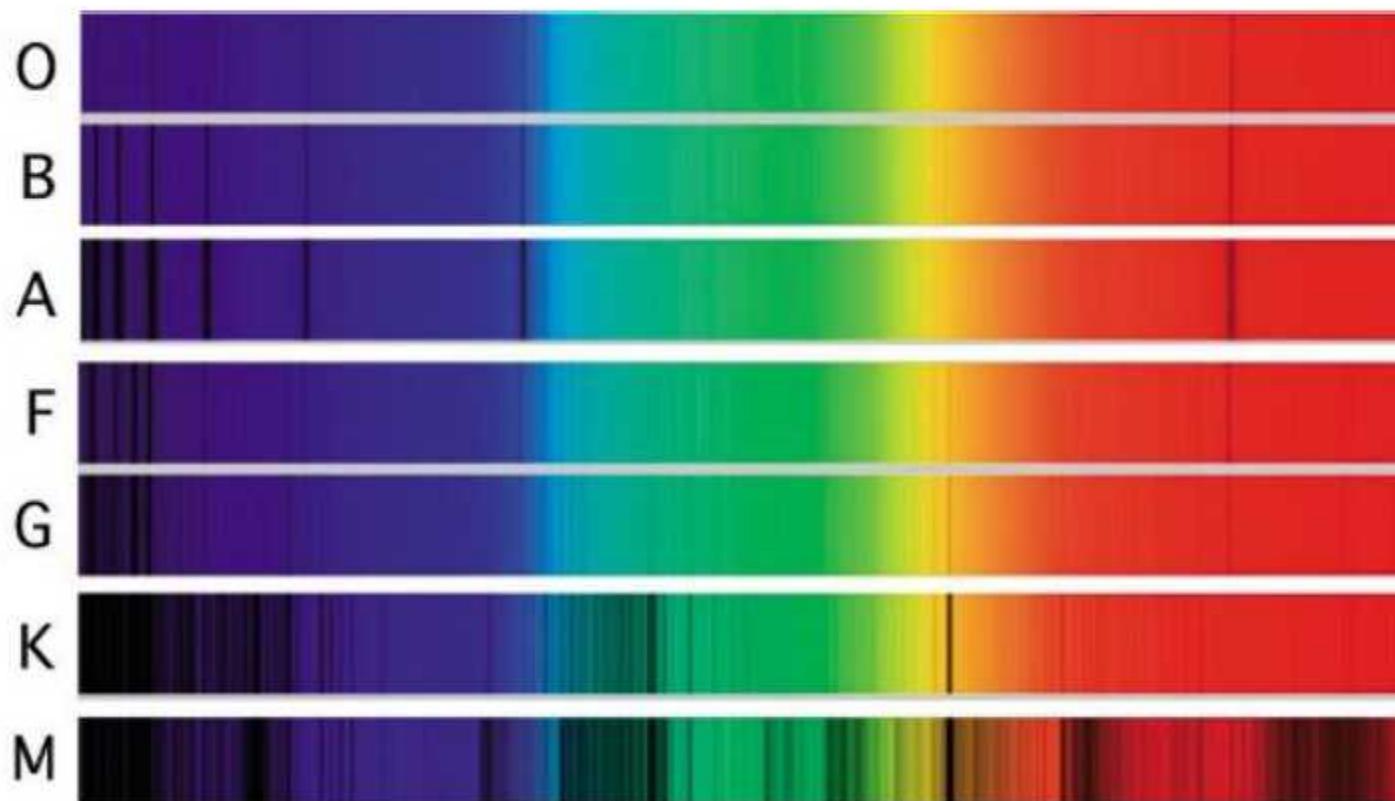
O0, O1, O2, ...O9, B0, B1, B2, ...B9, ...

Stellar spectra

Stars' spectra : differ depending on **T** and **composition**

Early-types (O and B) stars – few spectral lines

Late-types (K and M) stars – many spectral lines



Spectral types

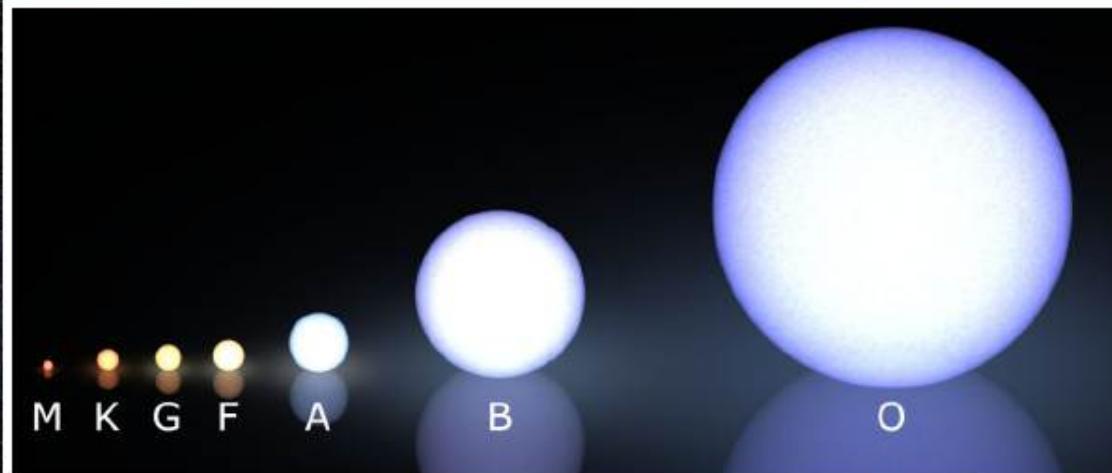
Spectral type	Stars	Spectral features	(e.g.)
O	blue stars, usually SGs, very luminous and hot, rare	He II absorption lines (sometimes emission: 4541, 4200Å); He I lines (4471, 4026Å) weak but increasing in strength from O5 to O9; lines from highly ionized species (e.g., C III, N III, O III, Si IV); H lines prominent but relatively weak; strong UV continuum	ζ (Zeta) Puppis (O4 I)
B	blue white stars, mainly giants	Strong He I lines, maximum at B2 ; no He II lines; H absorption lines strengthening from B0 to B9 ; lower-excitation ions (e.g., C II, O II, Mg II, Si II, Si III)	Rigel (= β Orionis, B8 Ia), ϵ Ori (B0 Ia)
A	White stars, dwarfs to giants	H absorption lines maximum strength at A0 and decrease towards later types; ionized metal lines (Fe II, Mg II, Si II) at max strength near A5 ; Ca II weak and increase in strength; lines of neutral metals appear weakly	Sirius (A1 V), α Lyr (=Vega, A0 V)
F	yellow white stars, mainly dwarfs	H absorption lines weakening rapidly, Ca II H&K absorption lines strengthen ; lines of neutral metals (Fe I, Cr I) and first ionization states of metals appear prominently	Procyon (= α CMi, F5 IV-V)
G	yellow stars, mainly dwarfs	Solar-type spectra; Ca II absorption lines dominate (max near G2) ; neutral metal lines (Fe I, Mn I, Ca I) strengthening; ionized metal lines diminish; G band (CH) strong ; H lines very weak	Sun (G2 V)
K	orange stars, can exist as giants and dwarfs	Neutral metallic absorption lines dominate ; Ca lines strong ; H lines almost gone; molecular bands (CH, CN, TiO) developing; continuum weak in blue	Arcturus (= α Boötis, K0 III), Aldebaran (= α Tau, K5 III)
M	red stars, exist at extremes either giants or red dwarfs	Strong molecular bands, particularly TiO by M5 ; neutral metallic absorption lines (e.g., quite strong Ca I); red continuum	Betelgeuse (= α Orionis, M2 I), Proxima Centauri (M5.5 V)

Spectral types

Spectral type	Stars	Spectral features	(e.g.)
O	blue stars, usually SGs, very luminous and hot, rare	He II absorption lines (sometimes emission: 4541, 4200Å); He I lines (4471, 4026Å) weak but increasing in strength from O5 to O9; lines from highly ionized species (e.g., C III, N III, O III, Si IV); H lines prominent but relatively weak; strong UV continuum	ζ (Zeta) Puppis



ζ Puppis (O4 I) – artist's rendering
https://en.wikipedia.org/wiki/Stellar_classification

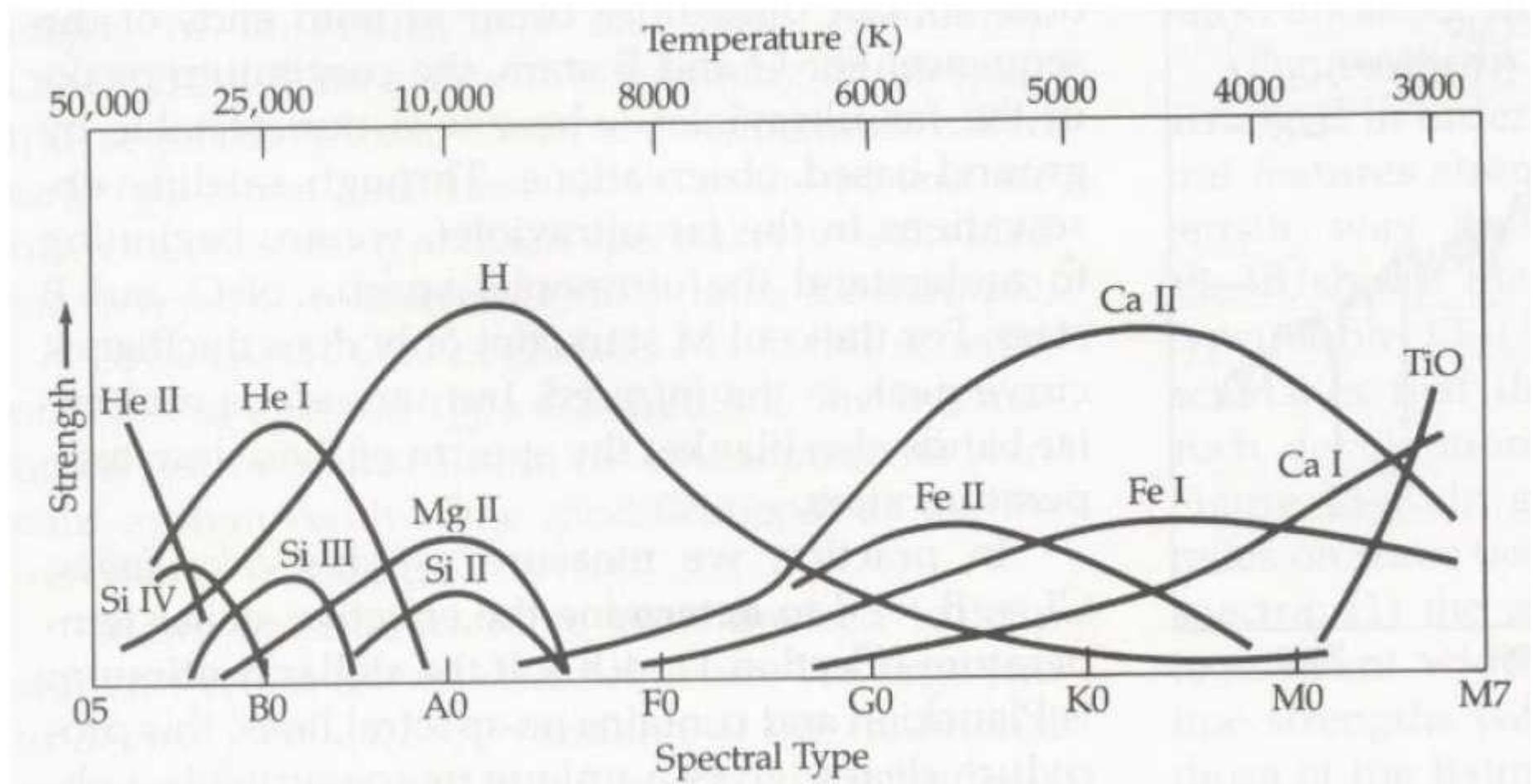


Relative size of O-type stars with other MS stars

https://en.wikipedia.org/wiki/Stellar_classification

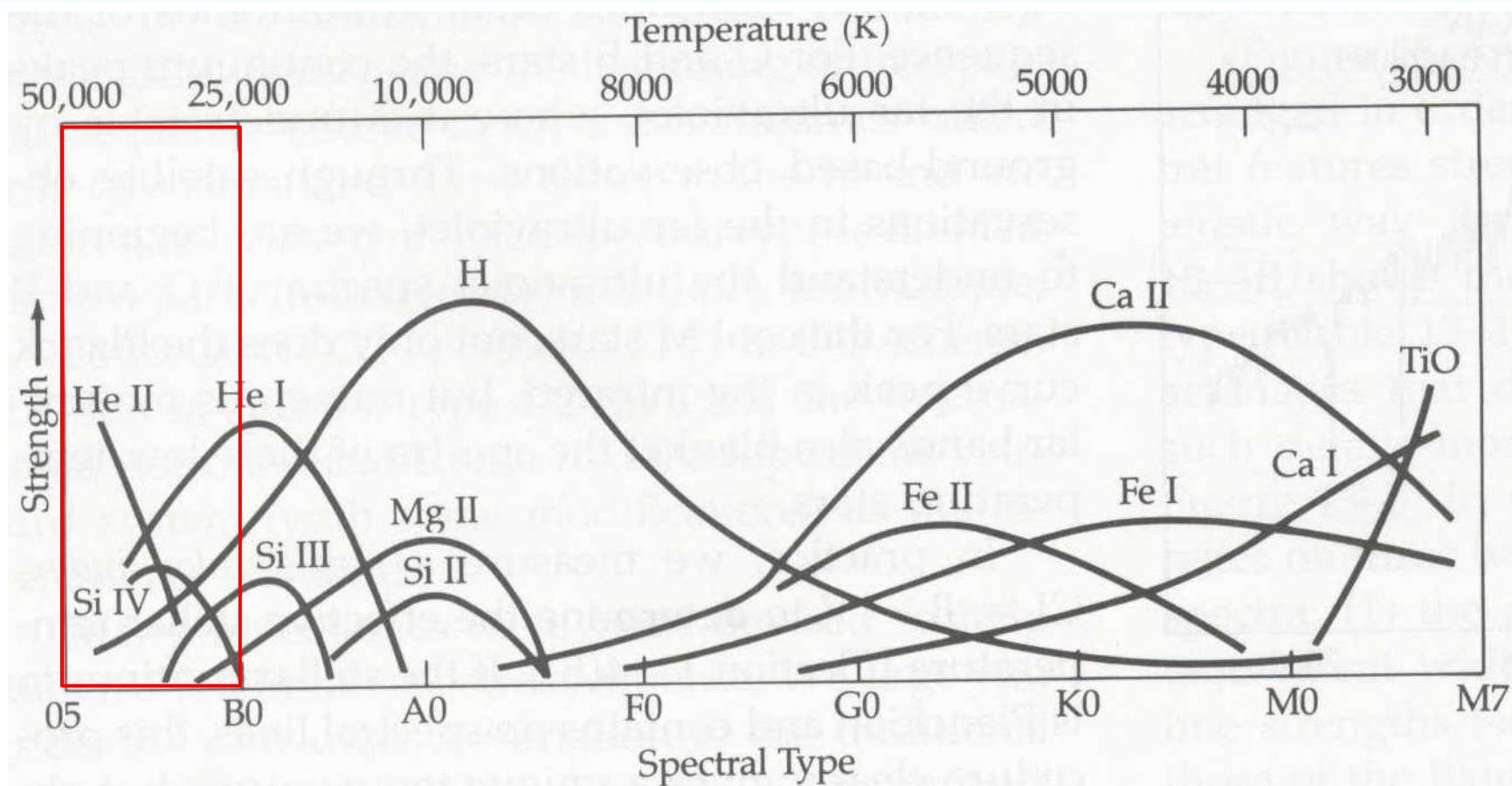
Spectral types

absorption lines



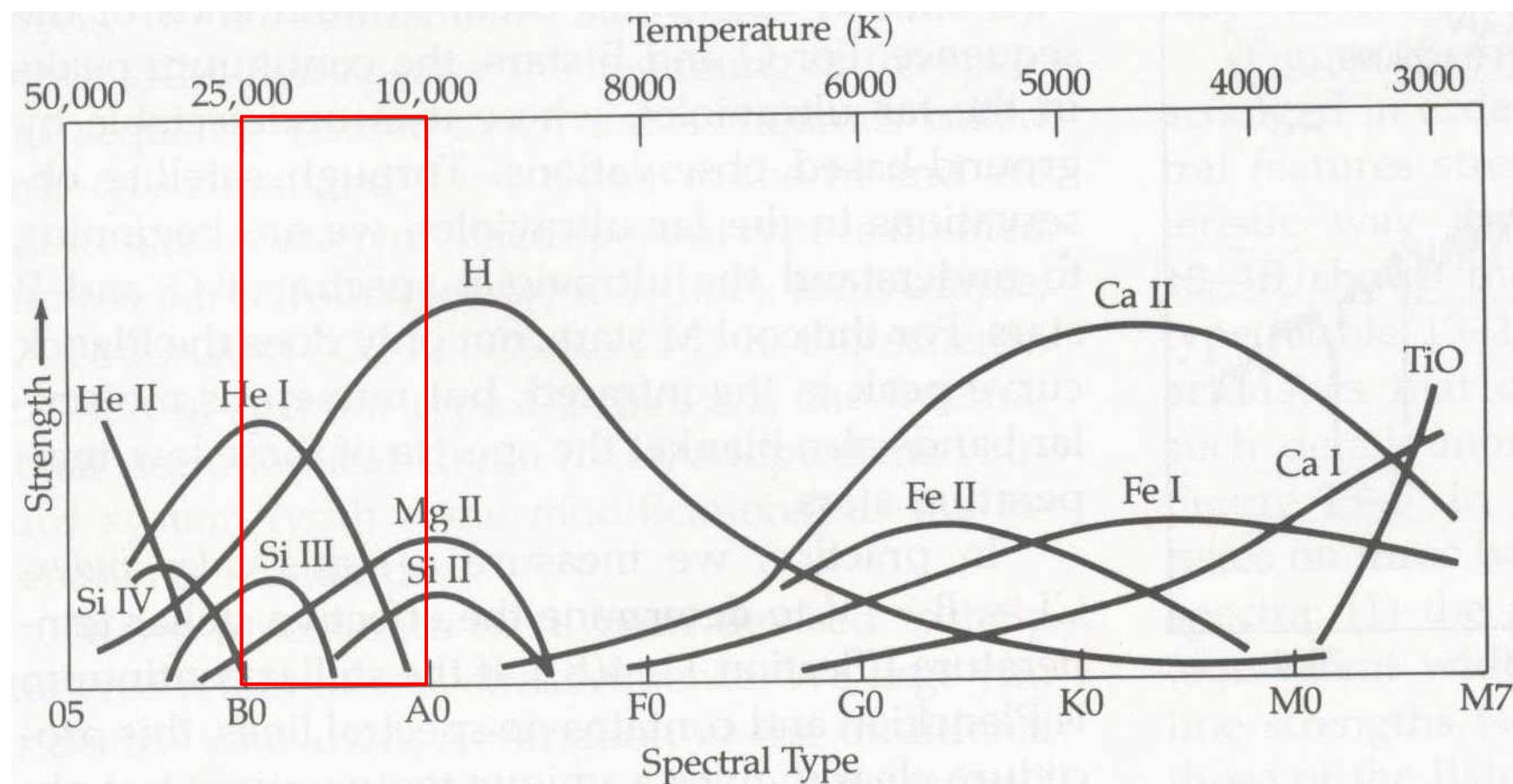
Spectral types

Spectral type	Stars	Spectral features	(e.g.)
O	blue stars, usually SGs, very luminous and hot, rare	He II absorption lines (sometimes emission: 4541, 4200Å); He I lines (4471, 4026Å) weak but increasing in strength from O5 to O9; lines from highly ionized species (e.g., C III, N III, O III, Si IV); H lines prominent but relatively weak; strong UV continuum	ζ (Zeta) Puppis



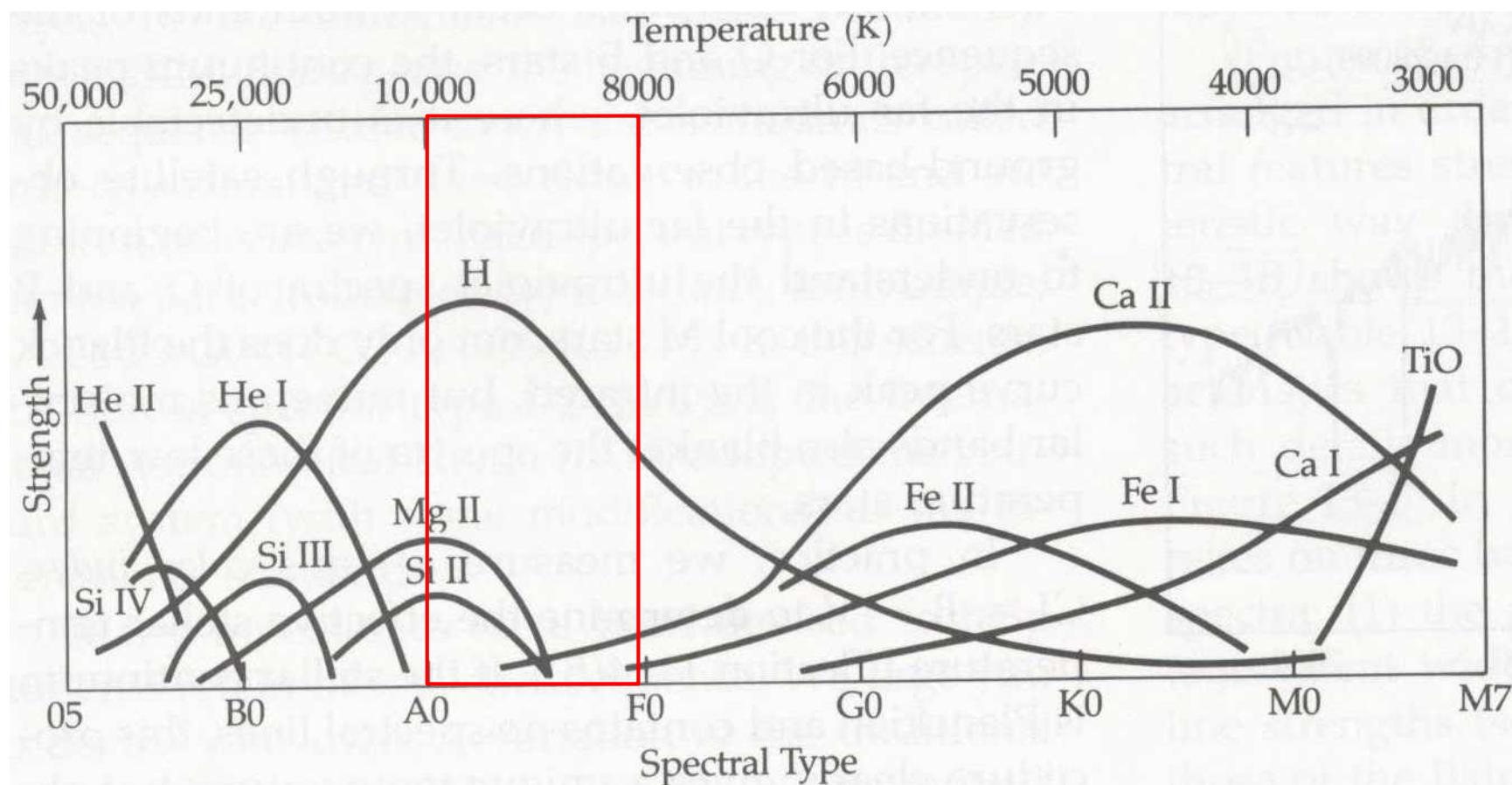
Spectral types

Spectral type	Stars	Spectral features	(e.g.)
B	blue white stars, mainly giants	Strong He I lines, maximum at B2; no He II lines; H absorption lines strengthening from B0 to B9; lower-excitation ions (e.g., C II, O II, Mg II, Si II, Si III)	Rigel (= β Orionis, B8 Ia), ϵ Ori (B0 Ia)



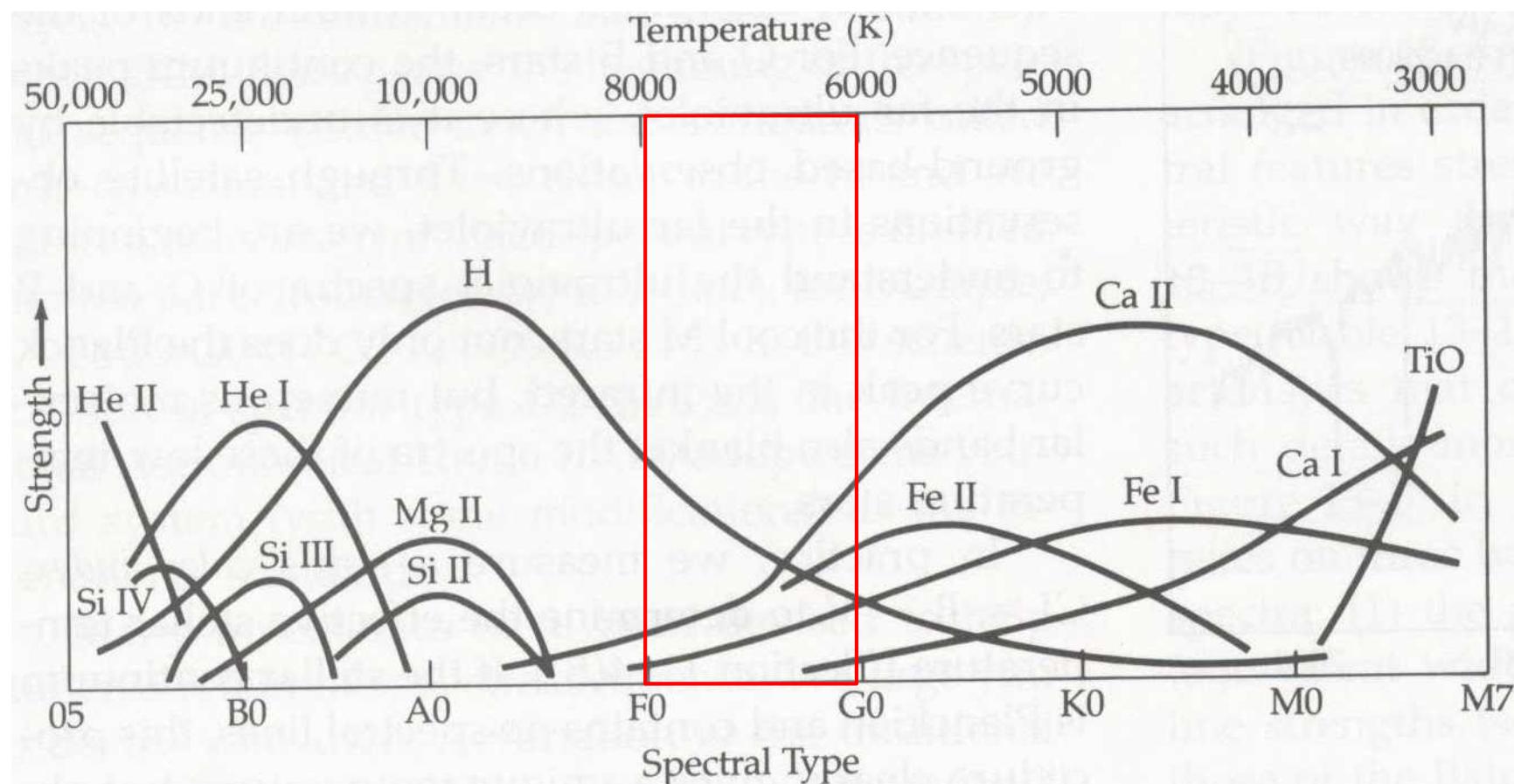
Spectral types

Spectral type	Stars	Spectral features	(e.g.)
A	White stars, dwarfs to giants	H absorption lines maximum strength at A0 and decrease towards later types; ionized metal lines (Fe II, Mg II, Si II) at max strength near A5 ; Ca II weak and increase in strength; lines of neutral metals appear weakly	Sirius (A1 V), α Lyr (=Vega, A0 V)



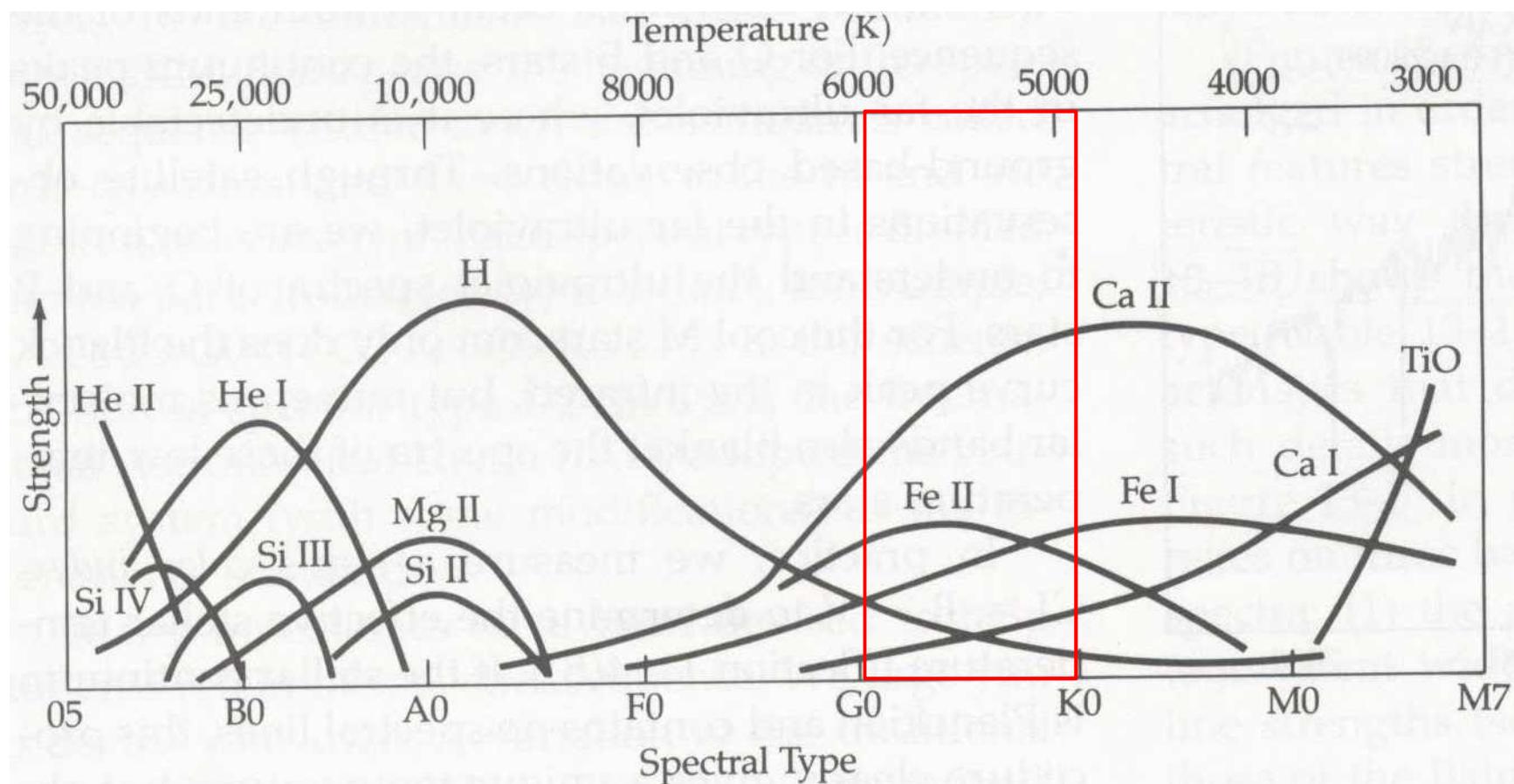
Spectral types

Spectral type	Stars	Spectral features	(e.g.)
F	yellow white stars, mainly dwarfs	H absorption lines weakening rapidly, Ca II H&K absorption lines strengthen ; lines of neutral metals (Fe I, Cr I) and first ionization states of metals appear prominently	Procyon ($=\alpha$ CMi, F5 IV-V)



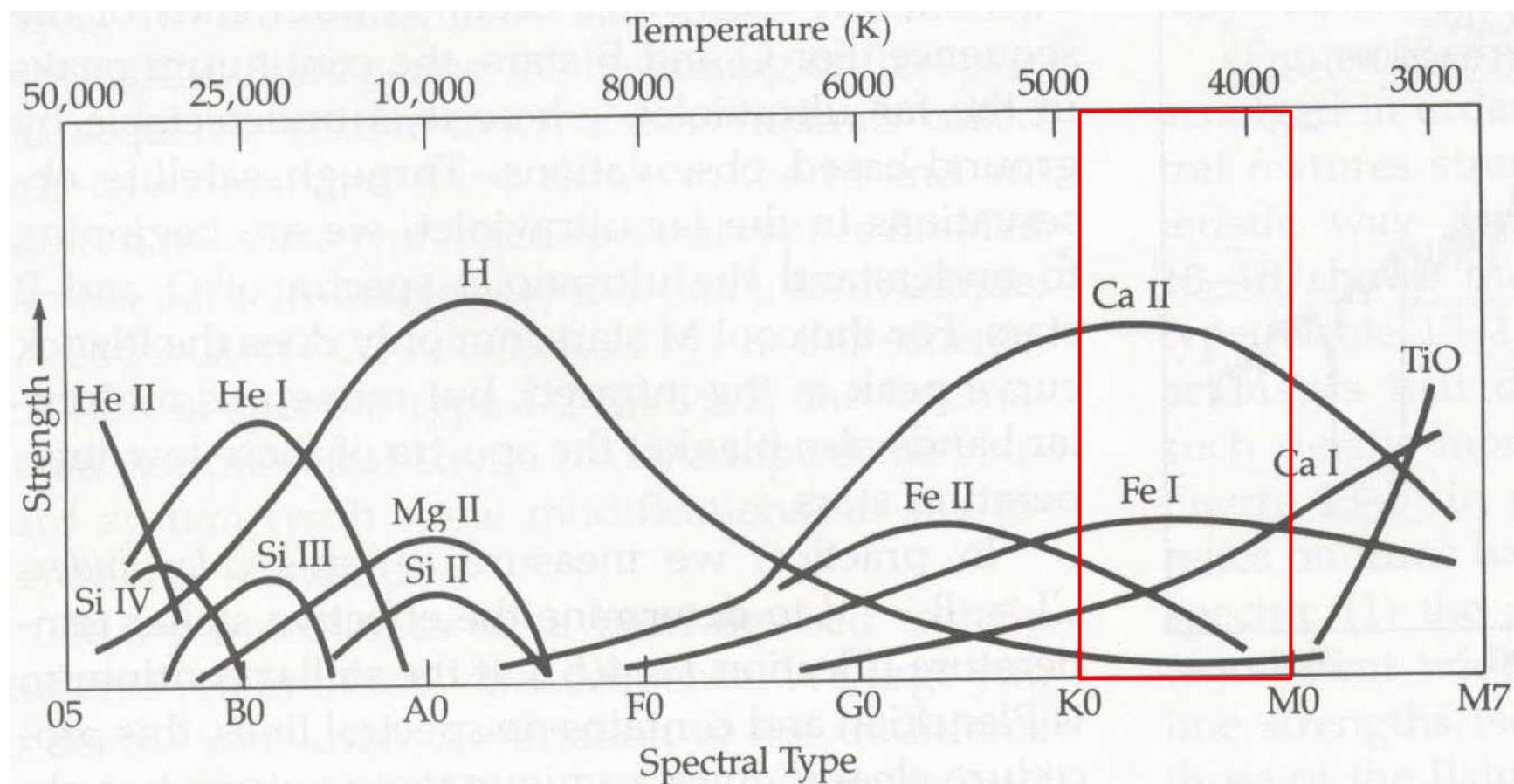
Spectral types

Spectral type	Stars	Spectral features	(e.g.)
G	yellow stars, mainly dwarfs	Solar-type spectra; Ca II absorption lines dominate (max near G2) ; neutral metal lines (Fe I, Mn I, Ca I) strengthening; ionized metal lines diminish; G band (CH) strong ; H lines very weak	Sun (G2 V)



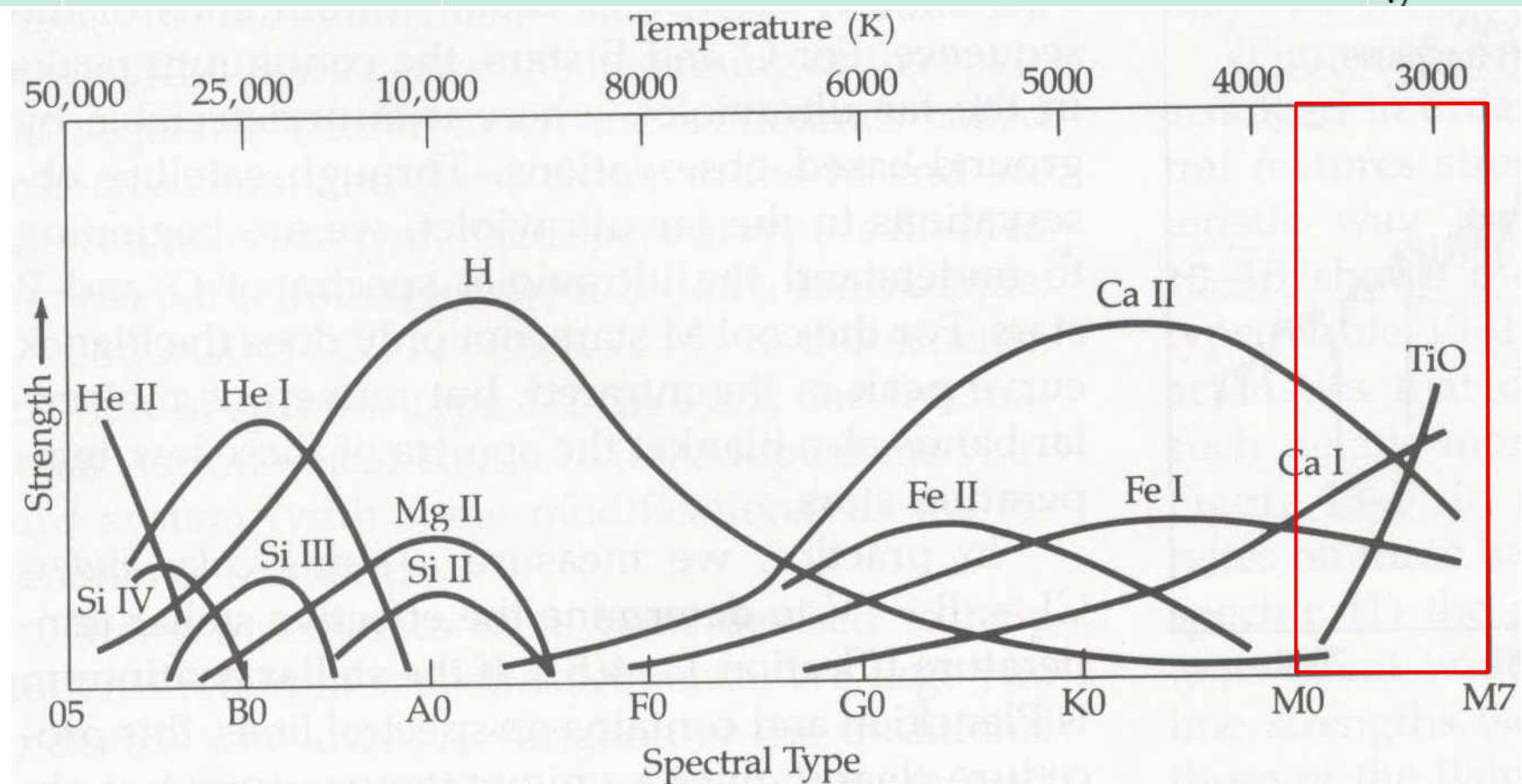
Spectral types

Spectral type	Stars	Spectral features	(e.g.)
K	orange stars, can exist as giants and dwarfs	Neutral metallic absorption lines dominate; Ca lines strong; H lines almost gone; molecular bands (CH, CN, TiO) developing; continuum weak in blue	Arcturus ($=\alpha$ Boötis, K0 III), Aldebaran ($=\alpha$ Tau, K5 III)



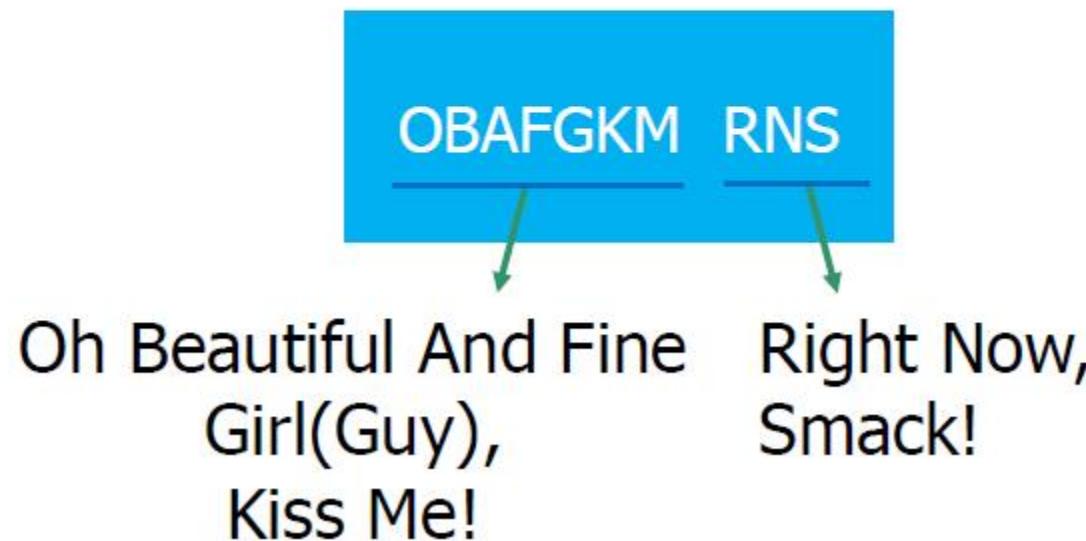
Spectral types

Spectral type	Stars	Spectral features	(e.g.)
M	red stars, exist at extremes either giants or red dwarfs	Strong molecular bands, particularly TiO by M5; neutral metallic absorption lines (e.g., quite strong Ca I); red continuum	Betelgeuse (α Orionis, M2 I), Proxima Centauri (M5.5 V)



Extended spectral types

How to memorize spectral types?



Extended spectral types – Carbon Stars

C (carbon) stars

- giant stars with similar temperatures of G, K, M stars ($T = 3100 - 4600$ K)
- different compositions : C is overabundant relative to O

hotter R stars (C_2 , CN bands)

cooler N stars (C_2 , CN, CH bands, little TiO)

S stars : molecular bands of the heavy-metal oxides ZrO, LaO, YO (instead of TiO)

: enhanced CN absorption bands

: neutral atoms strong as in K and M types

Galactic Astronomy (J. Binney & M. Merrifield, 1998) p. 92

Introductory Astronomy and Astrophysics (4th edition) Michael Zeilik & Stephen A. Gregory (1998), p. 266

$^{22}_{\text{Ti}}{}^{48}$: Titanium
$^{39}_{\text{Y}}{}^{89}$: Yttrium
$^{40}_{\text{Zr}}{}^{91}$: Zirconium
$^{57}_{\text{La}}{}^{139}$: Lanthanum

R Sculptoris : a sample C star
(Maercker+12 Nature 490 232)
https://en.wikipedia.org/wiki/Stellar_classification



Extended spectral types – Brown Dwarfs

- Cool red dwarfs and brown dwarfs (BDs) - Infrared spectra
- BD : objects whose central temperatures never reach the critical threshold for stable thermonuclear burning (Kirkpatrick + 11 ApJS 197, 19
‘The first hundred BDs discovered by the Wide-field Infrared Survey Explorer (WISE)’)
- BDs cool as they age : from M to L, T, Y type
The less massive, the faster cooling
- Class L : mostly BDs with substellar mass, some stars with H-fusion
(e.g.) V838 Mon
 - Temp $\sim 1,700$ K ($\sim 1,400$ °C)
 - M and L types = mixture of stars and BDs

J. D. Kirkpatrick (2005, ARA&A, 43, 195 ‘New spectral types L and T’)



L dwarf - artist's impression



V838 Monocerotis – HST
https://en.wikipedia.org/wiki/V838_Monocerotis

Extended spectral types – Brown Dwarfs

- Class T
cool brown dwarfs
surface $T \sim 1,200 \text{ K}$ (1,000 – 1,600 K)
 $(\sim 900 \text{ }^\circ\text{C})$ (700 – 1,300 °C)
prominent methane (CH_4) in the spectra
→ “methane dwarfs”

T dwarfs would appear reddish, or magenta, to the eye.



T dwarf - artist's impression

Extended spectral types – Brown Dwarfs

- **Class Y**

BDs cooler than class T

(coldest BDs, latest classification letter)

Cushing + 11 (ApJ, 743, 50 'The discovery of Y dwarfs using data from the Wide-field Infrared Survey Explorer (WISE)')

Temp $\sim 298 - 448$ K (25 – 175 °C)

Mass : $9 - 25 M_J$

N = 17 (2013 August)

mostly nearby : 9 – 40 ly

(WISE 1541-2250, d~9 ly : 7th closest star system)

not detected at visible wavelengths

Kirkpatrick+13 ApJ 776 128 ('Discovery of the Y1 dwarf J064723.23-623235.5')

https://en.wikipedia.org/wiki/Stellar_classification

http://www.nasa.gov/mission_pages/WISE/multimedia/pia14720.html

http://science.nasa.gov/science-news/science-at-nasa/2011/23aug_coldeststars/

Brown Dwarfs (BDs)

- WISE (Wide-field Infrared Survey Explorer) → found ~100 new BDs → 6 Y stars
- Coldest : **WISE 1828+2650, T~300 K (25°C)**



Y dwarf **WISE 1828+2650**
- artist's impression
- purple color choice : artistic reason

https://en.wikipedia.org/wiki/Stellar_classification

http://science.nasa.gov/science-news/science-at-nasa/2011/23aug_coldeststars/

Brown Dwarfs (BDs)

