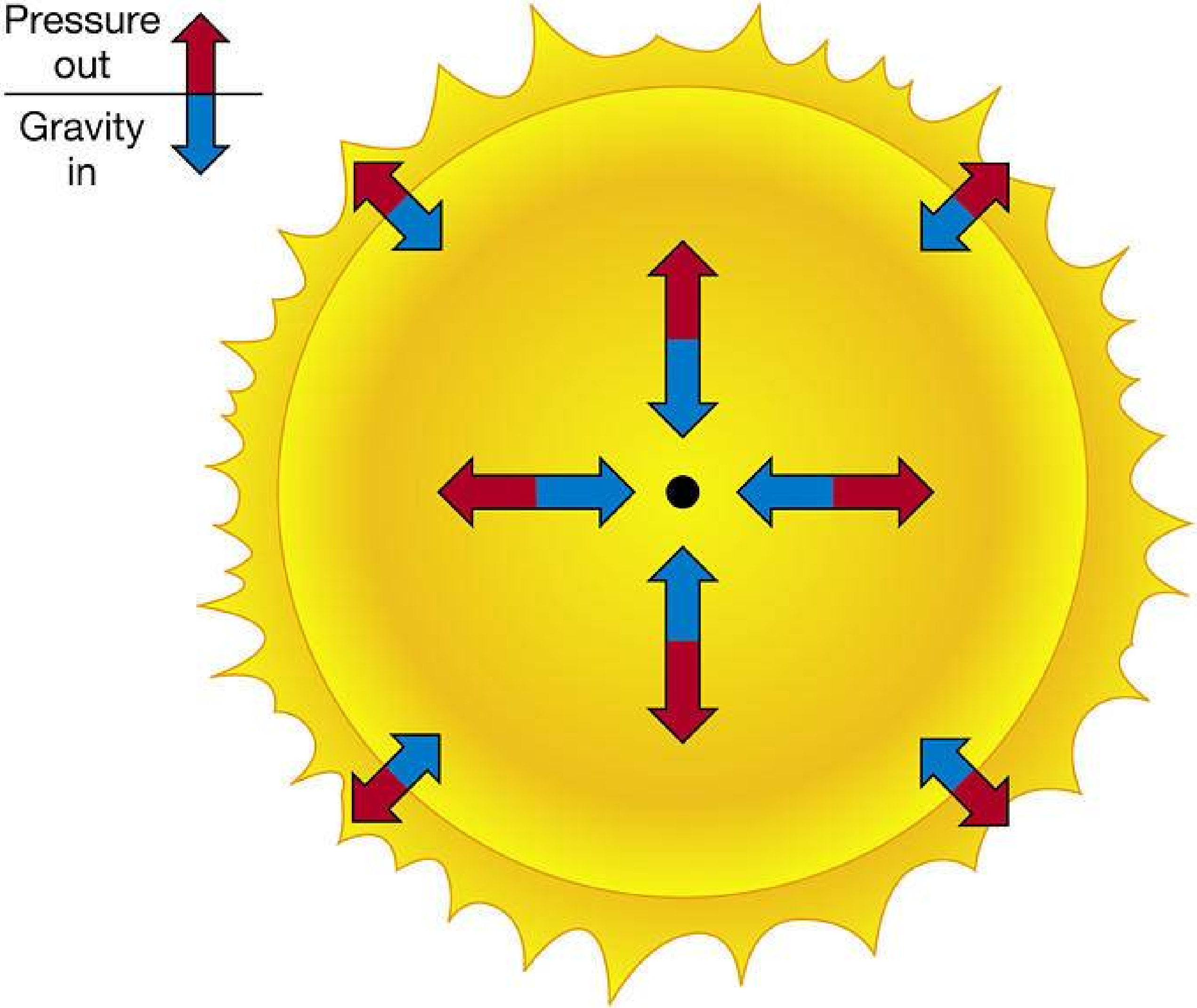
2. The Evolution of Stars (별의 진화)
2-1 Energy Generation (에너지 생성)



Hydrostatic equilibrium (정 유체역학적 평형)

https://pages.uoregon.edu/jimbrau/BraulmNew/Chap16/FG16_06.jpg

김상철
(Sang Chul KIM)

Main Sequence (MS, 주계열성)

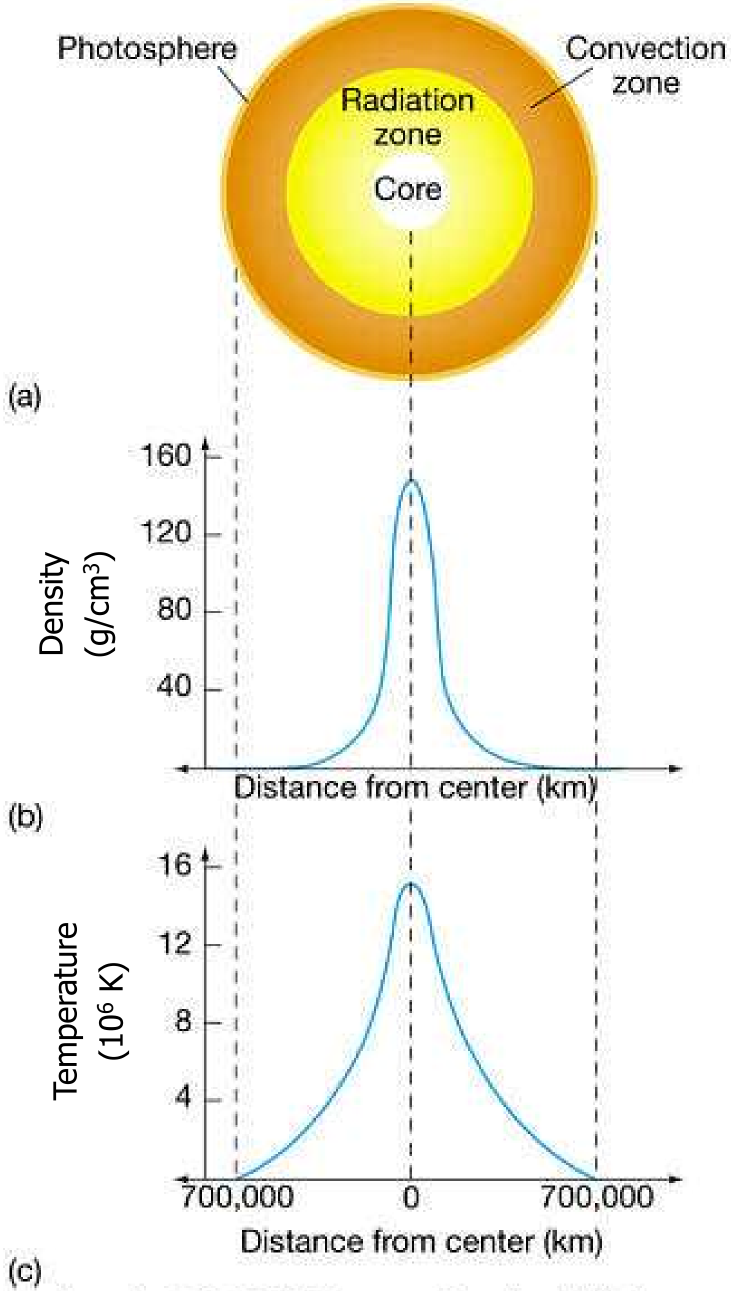
- Nuclear fusion (proton-proton chain, 양성자-양성자 연쇄반응) → energy generation and radiation
- Mass decreases slowly → almost constant luminosity (equilibrium between pressure and gravity)
- core : N(H) decreases, N(He) increases

- $M > 1.5\ M_{\odot}$, $T_{center,\odot} > 1.5 \times 10^7$ K → H burning by CNO cycle (탄소 순환반응)

Hydrostatic equilibrium (정 유체역학적 평형)

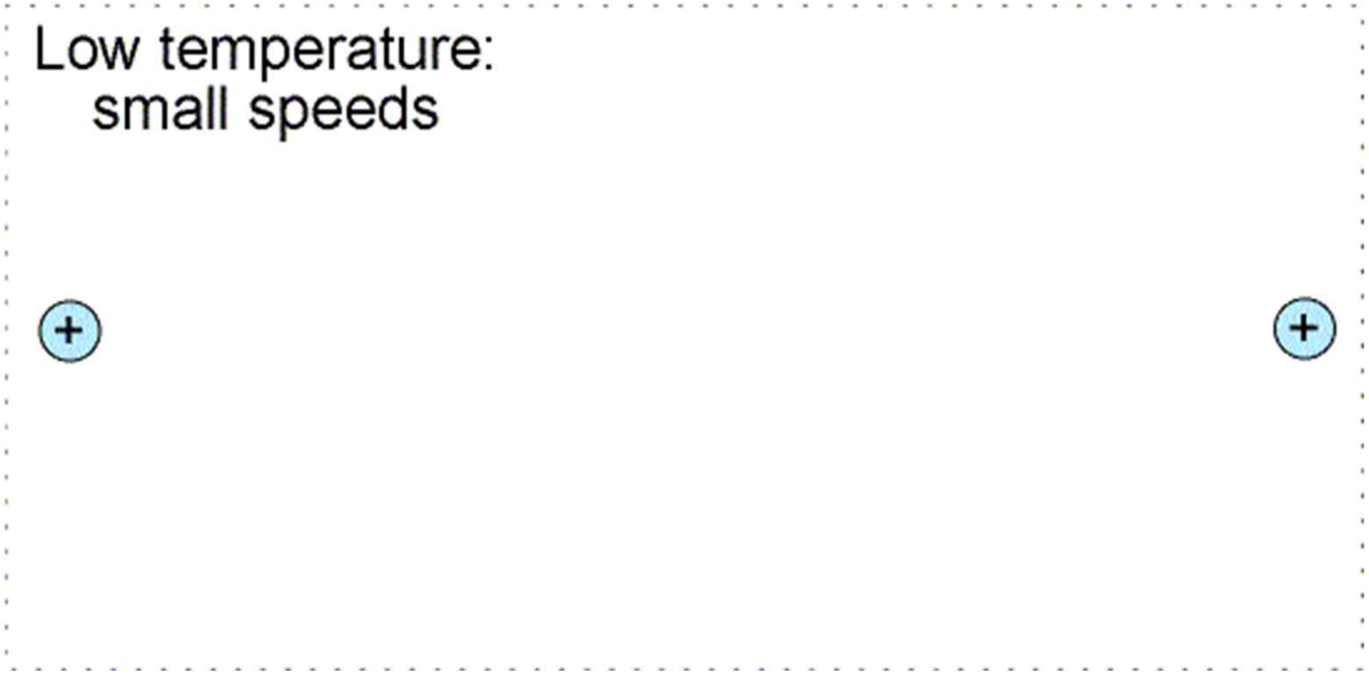
- If somehow core H-burning accelerates → Core T ↑, P ↑ → star expands
- Expansion makes T ↓ → H-burning decelerates
- Hydrostatic equilibrium makes H-burning speed keep ~constant

Interior structure of the Sun (태양의 내부 구조)



http://pages.uoregon.edu/jimbrau/BrauImNew/Chap16/FG16_08.jpg

Why H-burning occurs at the core - 1

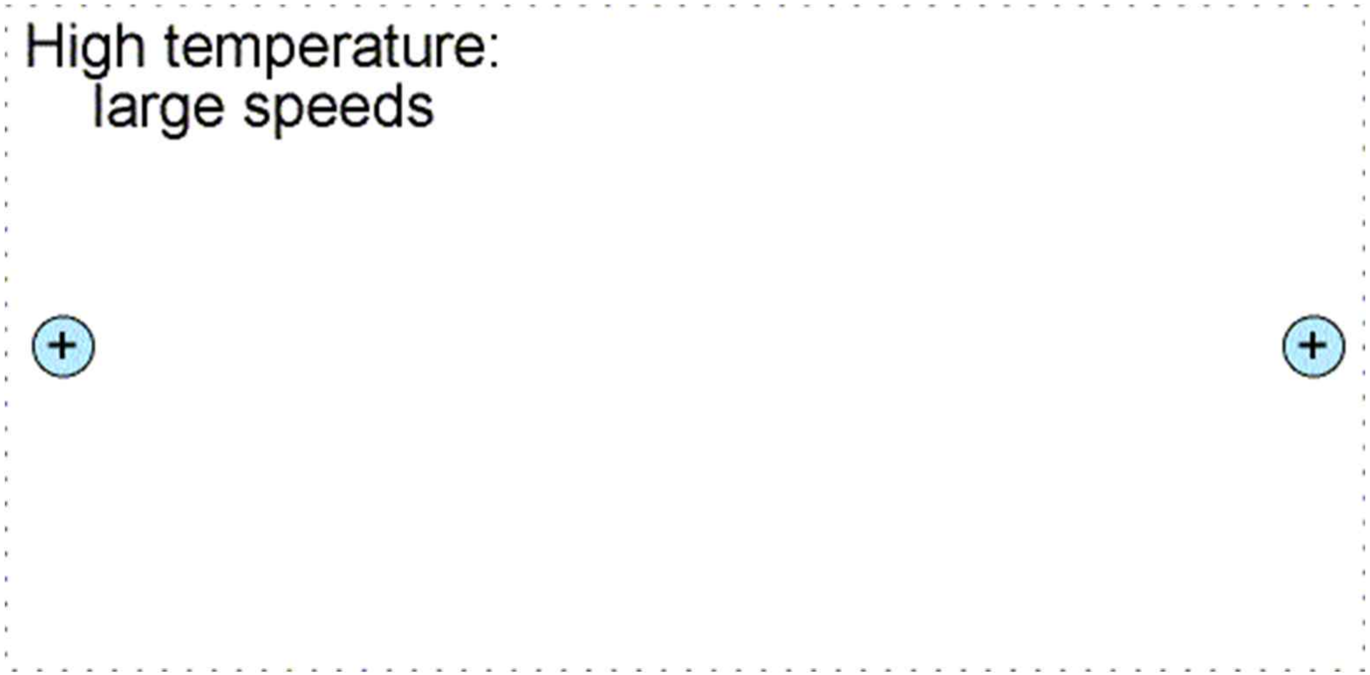


Low Temp : small speeds

→ mutual Electrical repulsion > proton-proton fusion

http://www.astronomynotes.com/starsun/s3.htm

Why H-burning occurs at the core - 2



High Temp : large speeds

→ Nuclei able to get close enough for strong nuclear force (강한 핵력) to act

→ Nuclei fuse & energy released

http://www.astronomynotes.com/starsun/s3.htm

symbol

$$^{A}_{Z}X$$

X : the chemical symbol of the element (e.g. : H, He, ...)
Z : the number of protons (the total positive charge, in units of e)
A : the mass number (the total number of nucleons, protons plus neutrons)

- $A = Z+N$
  (mass number = Z protons + N neutrons)

(e.g.) $^{1}_{1}H$ $\quad$ $^{4}_{2}He$

Energy from proton-proton chain

H atomic weight : 1.0078

4 H → 4.0312

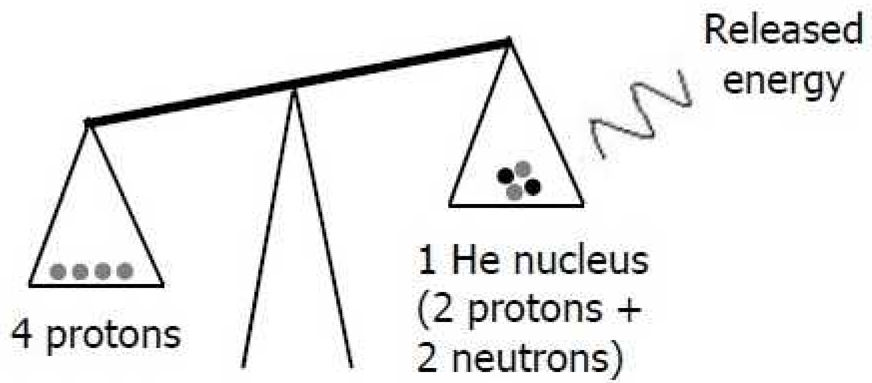
1 He → 4.0026

$\triangle m = 0.0286$ (mass deficit/defect, 질량 결손)

E = mc² (Einstein's equation for the equivalence of mass and energy)

$$\triangle m = 4 \times m(p) - m(He)$$
$$= (0.0286 \times 1.67 \times 10^{-24} g) \times (3 \times 10^{10}\ cm/s)^2$$
$$= 4.3 \times 10^{-5}\ erg$$
$$= 4.3 \times 10^{-12}\ J$$

1 Joule = 1 kg·m²/s²
= 1 N·m
= **10⁷ erg**
= 6.24×10¹⁸ eV
= 0.2390 cal
= 2.78×10⁻⁷ kW·h



Energy from proton-proton chain

- Energy from coal 1 kg ~ 5000 kcal = 2.1×10^7 J

- Use H 1 kg to produce He

→ 0.993 kg He produces, 0.007 kg changes into E

→ $E = mc^2 = 7\ \mathrm{g} \times (3 \times 10^{10}\ \mathrm{cm/s})^2 = 7 \times 9 \times 10^{20}\ \mathrm{g\ cm^2/s^2}$

$= 6.3 \times 10^{21}\ \mathrm{erg} = 6.3 \times 10^{14}\ \mathrm{J}$

→ same as E from 3×10^7 kg = 30,000 tons of coal

Sun : 4×10^{38} protons/sec = 6.68×10^{14} g/sec are consumed.

2×10^{38} neutrinos/sec are generated.

Sun : $1\ L_\odot = 3.9 \times 10^{33}$ erg/s = 3.9×10^{26} J/s

Energy from proton-proton chain

$1\ L_\odot = 3.9 \times 10^{33}$ erg/s $= 3.9 \times 10^{26}$ J/s

= amount of electricity for all human beings can use for 10^7 years

Assuming :

Mankind populations = $5 \times 10^9 \rightarrow 10^9$ families (assume 1 family = 5 members)

Monthly family electricity uses, home use : 200~250 kW·h

Let's assume ~1000 kW·h/month including commercial use, etc

$= 10^6\ \mathrm{W} \times 3600$ s/month $= 10^6\ \mathrm{J/s} \times 3600$ s/month $= 3.6 \times 10^9$ J/month

1 W = 1 J/s

Monthly mankind electricity uses $\sim 3.6 \times 10^9\ \mathrm{J} \times 10^9$ families/month $= 3.6 \times 10^{18}$ J/month

$$\rightarrow \quad \frac{3.9 \times 10^{26}\,\mathrm{J}}{3.6 \times 10^{18}\,\mathrm{J}} = 1.1 \times 10^8 \text{ months} = 9.2 \times 10^6 \text{ years} \sim 10^7 \text{ years}$$

Energy from proton-proton chain

Atomic weight (원자량, 原子量) or relative atomic mass (상대 원자 질량) :

H → 1

^{12}C →12 (1.998467052×10^{-23} g) (since 1962),

then H → 1.0078

He → 4.0026

α-ray, α-particle : He nucleus

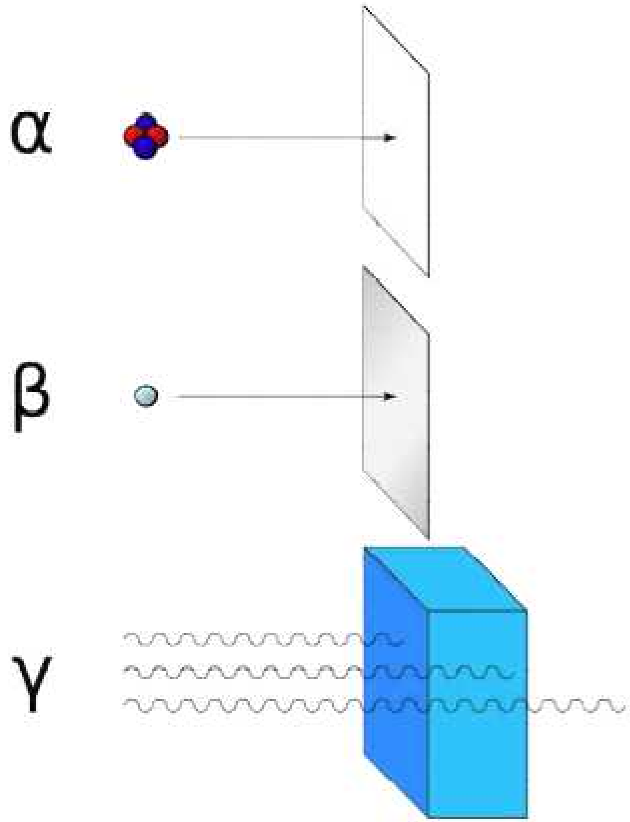
→ cannot penetrate a paper

β-ray : electron

→ cannot penetrate aluminum

γ-ray : high-energy photon

→ absorbed by dense materials (water, lead)



https://ko.wikipedia.org/wiki/알파_입자

β(beta)-decay

$\boxed{\beta^- \text{ decay} : n \rightarrow p + \beta^- + \overline{\nu_e}}$

β^+ decay : $p \rightarrow n + \beta^+ + \nu_e$

※ $\beta^- = e^-$ (electron)

※ $\beta^+ = e^+$ (positron)

$\boxed{\text{inverse-}\beta \text{ decay} : \; p^+ + e^- \rightarrow n + \nu}$

(IBD)

Periodic Table of the Elements

Atomic Number
Symbol
Name
Atomic Mass

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
1 **H** Hydrogen 1.01																	2 **He** Helium 4.00
3 **Li** Lithium 6.94	4 **Be** Beryllium 9.01											5 **B** Boron 10.81	6 **C** Carbon 12.01	7 **N** Nitrogen 14.01	8 **O** Oxygen 16.00	9 **F** Fluorine 19.00	10 **Ne** Neon 20.18
11 **Na** Sodium 22.99	12 **Mg** Magnesium 24.31											13 **Al** Aluminum 26.98	14 **Si** Silicon 28.09	15 **P** Phosphorus 30.97	16 **S** Sulfur 32.06	17 **Cl** Chlorine 35.45	18 **Ar** Argon 39.95
19 **K** Potassium 39.10	20 **Ca** Calcium 40.08	21 **Sc** Scandium 44.96	22 **Ti** Titanium 47.88	23 **V** Vanadium 50.94	24 **Cr** Chromium 51.99	25 **Mn** Manganese 54.94	26 **Fe** Iron 55.85	27 **Co** Cobalt 58.93	28 **Ni** Nickel 58.69	29 **Cu** Copper 63.55	30 **Zn** Zinc 65.38	31 **Ga** Gallium 69.72	32 **Ge** Germanium 72.63	33 **As** Arsenic 74.92	34 **Se** Selenium 78.97	35 **Br** Bromine 79.90	36 **Kr** Krypton 84.80
37 **Rb** Rubidium 85.47	38 **Sr** Strontium 87.62	39 **Y** Yttrium 88.91	40 **Zr** Zirconium 91.22	41 **Nb** Niobium 92.91	42 **Mo** Molybdenum 95.95	43 **Tc** Technetium 98.91	44 **Ru** Ruthenium 101.07	45 **Rh** Rhodium 102.91	46 **Pd** Palladium 106.42	47 **Ag** Silver 107.87	48 **Cd** Cadmium 112.41	49 **In** Indium 114.82	50 **Sn** Tin 118.71	51 **Sb** Antimony 121.76	52 **Te** Tellurium 127.6	53 **I** Iodine 126.90	54 **Xe** Xenon 131.29
55 **Cs** Cesium 132.91	56 **Ba** Barium 137.33	57-71 Lanthanides	72 **Hf** Hafnium 178.49	73 **Ta** Tantalum 180.95	74 **W** Tungsten 183.85	75 **Re** Rhenium 186.21	76 **Os** Osmium 190.23	77 **Ir** Iridium 192.22	78 **Pt** Platinum 195.08	79 **Au** Gold 196.97	80 **Hg** Mercury 200.59	81 **Tl** Thallium 204.38	82 **Pb** Lead 207.20	83 **Bi** Bismuth 208.98	84 **Po** Polonium [208.98]	85 **At** Astatine 209.98	86 **Rn** Radon 222.02
87 **Fr** Francium 223.02	88 **Ra** Radium 226.03	89-103 Actinides	104 **Rf** Rutherfordium [261]	105 **Db** Dubnium [262]	106 **Sg** Seaborgium [266]	107 **Bh** Bohrium [264]	108 **Hs** Hassium [269]	109 **Mt** Meitnerium [278]	110 **Ds** Darmstadtium [281]	111 **Rg** Roentgenium [280]	112 **Cn** Copernicium [285]	113 **Nh** Nihonium [286]	114 **Fl** Flerovium [289]	115 **Mc** Moscovium [289]	116 **Lv** Livermorium [293]	117 **Ts** Tennessine [294]	118 **Og** Oganesson [294]

57 **La** Lanthanum 138.91	58 **Ce** Cerium 140.12	59 **Pr** Praseodymium 140.91	60 **Nd** Neodymium 144.24	61 **Pm** Promethium 144.91	62 **Sm** Samarium 150.36	63 **Eu** Europium 151.96	64 **Gd** Gadolinium 157.25	65 **Tb** Terbium 158.93	66 **Dy** Dysprosium 162.50	67 **Ho** Holmium 164.93	68 **Er** Erbium 167.26	69 **Tm** Thulium 168.93	70 **Yb** Ytterbium 173.06	71 **Lu** Lutetium 174.97
89 **Ac** Actinium 227.03	90 **Th** Thorium 232.04	91 **Pa** Protactinium 231.04	92 **U** Uranium 238.03	93 **Np** Neptunium 237.05	94 **Pu** Plutonium 244.06	95 **Am** Americium 243.06	96 **Cm** Curium 247.07	97 **Bk** Berkelium 247.07	98 **Cf** Californium 251.08	99 **Es** Einsteinium [254]	100 **Fm** Fermium 257.10	101 **Md** Mendelevium 258.10	102 **No** Nobelium 259.10	103 **Lr** Lawrencium [262]

Alkali Metal	Alkaline Earth	Transition Metal	Basic Metal	Metalloid	Nonmetal	Halogen	Noble Gas	Lanthanide	Actinide

http://sciencenotes.org/printable-periodic-table/

Energy generation rate

- H atomic weight : 1.0078

4 H → 4.0312

1 He → 4.0026

$\triangle m = 0.0286$

- 0.0286/4.0312 = 0.0071 → 0.71%

- Only H in the core → T, P high enough to permit nuclear reactions → ~10 % of the mass of the Sun is available for energy conversion
- Thermonuclear energy available in the Sun :

$$E_{Total} = mc^2 = \left(\frac{4\,{}^1H - {}^4He}{4\,{}^1H} \times 0.1 M_\odot\right) \times (c^2)$$

$$= 0.0071 \times (1.99 \times 10^{32}\ \mathrm{g}) \times (3 \times 10^{10}\ \mathrm{cm/s})^2$$

$$\approx 10^{51}\ \mathrm{g \cdot cm^2/s^2}$$

$$\approx 10^{51}\ \mathrm{erg}$$

$$\approx 10^{44}\ \mathrm{J}$$

1 Joule = 1 $\mathrm{kg \cdot m^2/s^2}$
= 1 N·m
= 10^7 erg
= 6.24×10^{18} eV
= 0.2390 cal
= 2.78×10^{-7} kW·h

$L_\odot = 3.90 \times 10^{33}\ \mathrm{erg/s} = 3.90 \times 10^{26}\ \mathrm{J/s}$

→ $E/L_\odot$ = Solar lifetime = 8.11×10^9 yr ~10 Gyr

Energy generation rate

※ AGN → efficiency of conversion from mass to energy ~10% (η=0.1)
(see, e.g., Fabian & Rees 1995, MNRAS, 277, L55,
http://phys.huji.ac.il/~joaw/winterschool/heckman_1.pdf)

※ Gravitational wave (e.g, by merging of two identical black holes) → conversion efficiency ~30% (η~0.3)
(『Black Hole Physics』 1991, Edited by Venzo de Sabbata, Zhenjiu Zhang, NATO ASI Series, Vol. 364, p. 139)

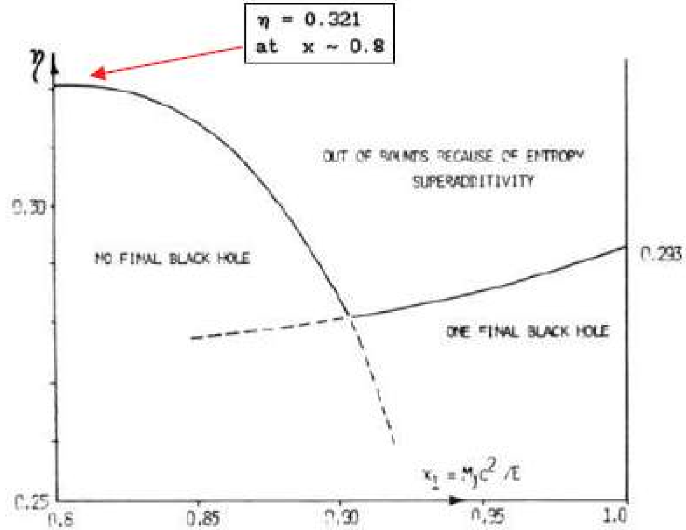
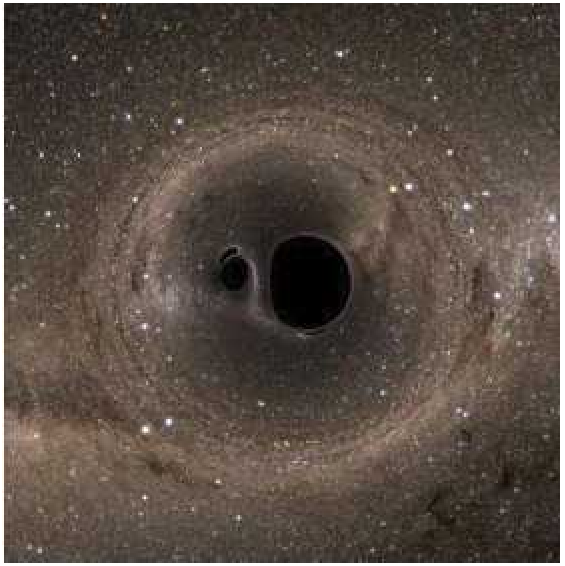
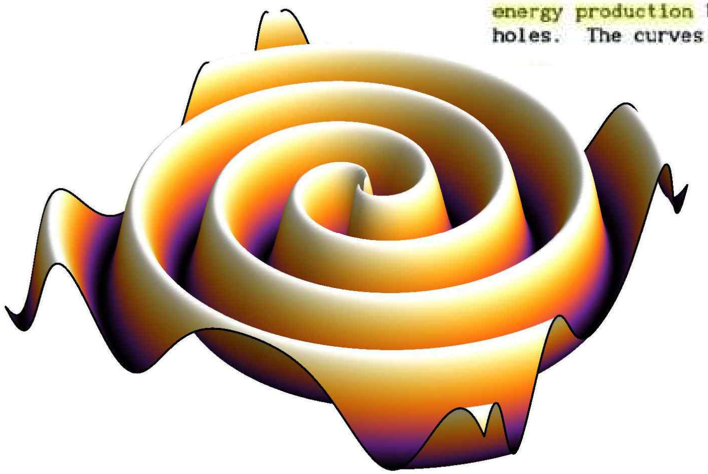


Figure 8. The maximum possible efficiency of gravitational wave energy production by the merging of two identical Schwarzschild black holes. The curves intersect at x_1 ~ 0.903, η ~ 0.281.



http://news.nationalgeographic.com/2016/02/160211-gravitational-waves-found-spacetime-science/



http://www.universetoday.com/127329/gravitational-wave-sources/

Energy generation rate

MS Lifetime : $\tau = 10^{10}(M/L)$ yr

(M=stellar mass, L=stellar luminosity)

※ Mass-Luminosity Relation :

$L/L_\odot = (M/M_\odot)^4$ for $M > 0.4M_\odot$

$L/L_\odot = (M/M_\odot)^{2.3}$ for $M < 0.4M_\odot$

→ $\tau = 10^{10}(M/M^4)$ yr $= 10^{10} / [M(M_\odot)]^3$ yr

1 $M_\odot$ → 10^{10} yr

10 $M_\odot$ → 10^7 yr

O stars (the most massive stars) → a million years

"we are seeing some O stars!" = SF is still occurring in the MW

Main-sequence Lifetimes

http://www.ifa.Hawaii.edu/~szapudi/astro110/2007/ch21.pdf

Mass ($M_\odot$)	Effective Temperature (K)	Spectral Class	Luminosity ($L_\odot$)	MS Lifetime (10^6 yr)
25	35,000	O	80,000	3
15	30,000	B	10,000	15
3	11,000	A	60	500
1.5	7000	F	5	3000
1.0	6000	G	1	10,000
0.75	5000	K	0.5	15,000
0.50	4000	M	0.03	200,000

http://ircamera.as.arizona.edu/astr_250/Lectures/Lecture_20.htm

Proton-proton (PP) fusion chain process

1^{st} step : $^1H + {^1H} \rightarrow {^2H} + e^+ + \nu_e$ $(\rightarrow 1.44\ \text{MeV})$

$^1H + {^1H} \rightarrow {^2H} + e^+ + \nu_e$ ← weak nuclear force

(It takes 5×10^9 years for a given proton to undergo this reaction.)

2^{nd} step : $^2H + {^1H} \rightarrow {^3He} + \gamma$ $(\rightarrow 5.49\ \text{MeV})$

$^2H + {^1H} \rightarrow {^3He} + \gamma$ (occurs in ~1 s)

3^{rd} step : $^3He + {^3He} \rightarrow {^4He} + {^1H} + {^1H}$ $(\rightarrow 12.9\ \text{MeV})$

← strong nuclear force

(It takes $\sim 3 \times 10^5$ years.)

^1H = p : proton
^2H : deuterium (중수소) = p + n
e^+ : positron (e^-의 반물질 antimatter, same mass, positive charge)
ν: neutrino (energy, spin, very small mass)
  ν_e : electron neutrino
^3He : helium-3 nucleus = 2p + 1n
γ : photon
^4He : helium-4 nucleus = 2p + 2n

→ 91% of the time in the Sun

Proton-proton (PP) fusion chain process

$$ {}^1_1\mathrm{H} + {}^1_1\mathrm{H} \longrightarrow {}^2_1\mathrm{H} + e^+ + \nu_e $$

$$ {}^2_1\mathrm{H} + {}^1_1\mathrm{H} \longrightarrow {}^3_2\mathrm{He} + \gamma $$

69%

31%

$$ {}^3_2\mathrm{He} + {}^3_2\mathrm{He} \longrightarrow {}^4_2\mathrm{He} + 2\,{}^1_1\mathrm{H} $$

(PP I)

$$ {}^3_2\mathrm{He} + {}^4_2\mathrm{He} \longrightarrow {}^7_4\mathrm{Be} + \gamma $$

99.7%

0.3%

$$ {}^7_4\mathrm{Be} + e^- \longrightarrow {}^7_3\mathrm{Li} + \nu_e $$

$$ {}^7_3\mathrm{Li} + {}^1_1\mathrm{H} \longrightarrow 2\,{}^4_2\mathrm{He} $$

(PP II)
(Lithium burning)

$$ {}^7_4\mathrm{Be} + {}^1_1\mathrm{H} \longrightarrow {}^8_5\mathrm{B} + \gamma $$

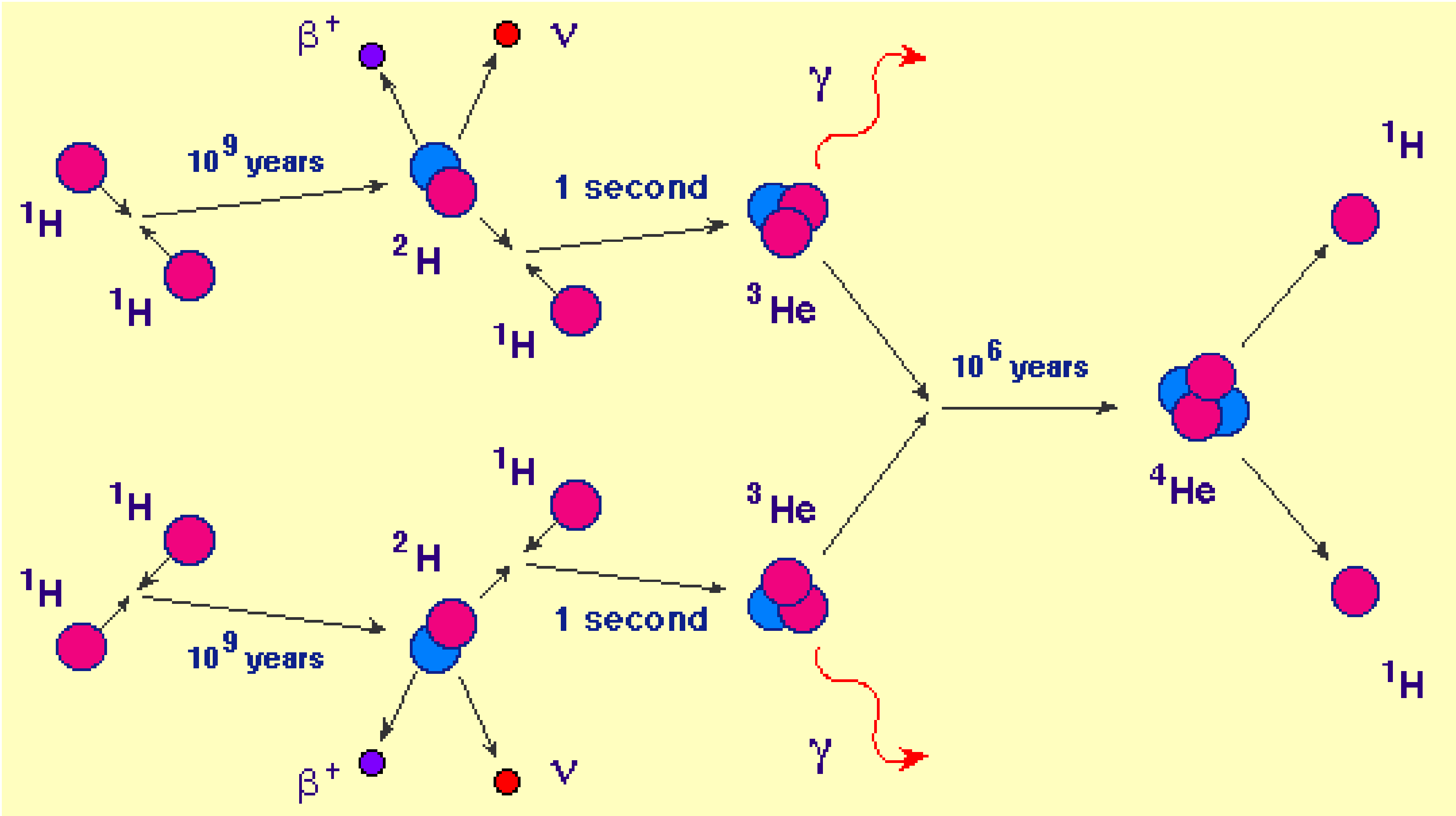
$$ {}^8_5\mathrm{B} \longrightarrow {}^8_4\mathrm{Be} + e^+ + \nu_e $$

$$ {}^8_4\mathrm{Be} \longrightarrow 2\,{}^4_2\mathrm{He} $$

(PP III)

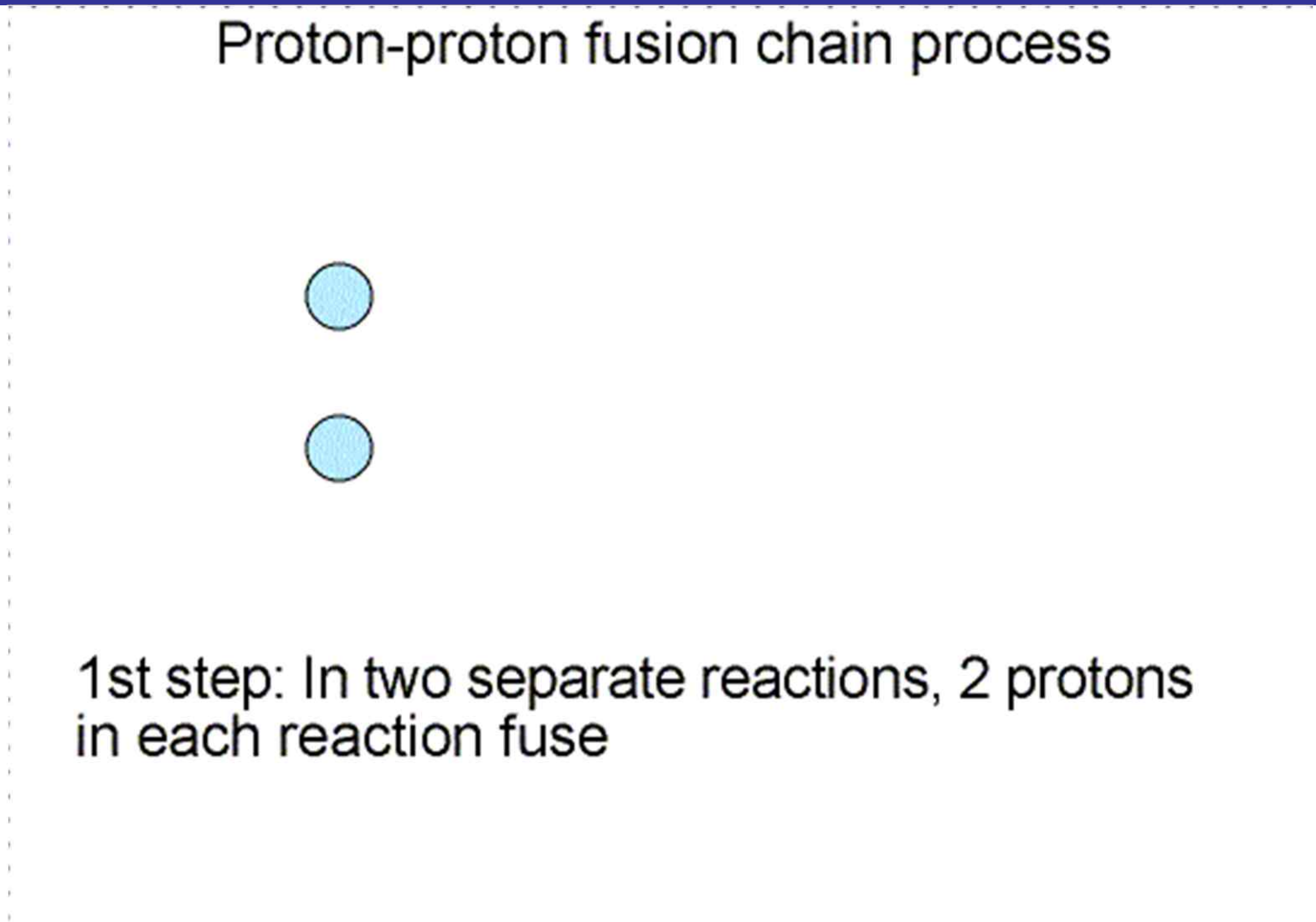
Why this complicated process?

- Direct collision of 4 H atoms to produce He → probability is very low
- Relatively, 2-body collision is more often !



http://atropos.as.arizona.edu/aiz/teaching/a250/pp.html

proton-proton (PP) fusion chain process



- 1^{st} step : p + p --> β^{+} + ν + ^{2}H
- 2^{nd} step : ^{2}H + p --> ^{3}He + γ
- 3^{rd} step : ^{3}He + ^{3}He --> ^{4}He + p + p

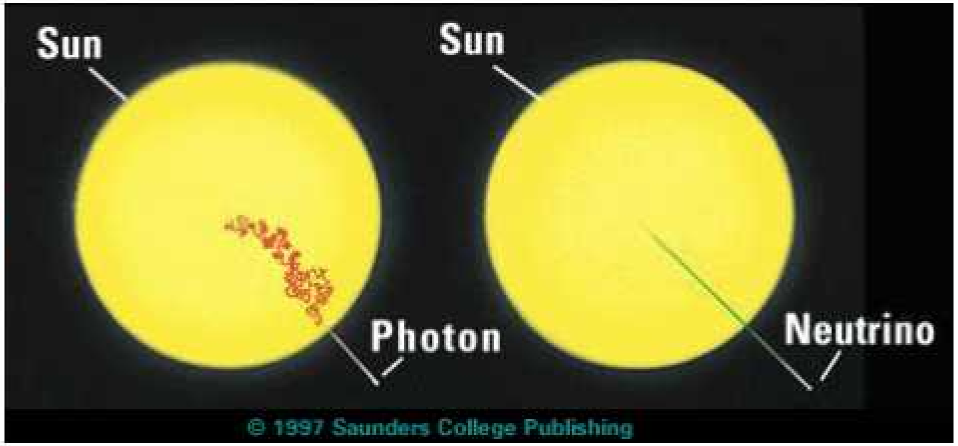
http://www.astronomynotes.com/starsun/s3.htm

Photon, neutrino – escape from the Sun

Photon and neutrino – travel times out of the center of the Sun

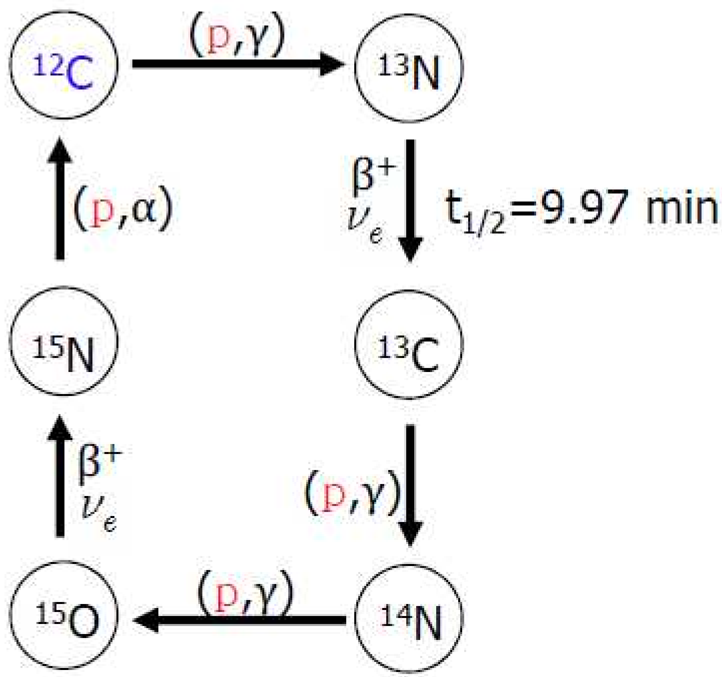
10^4 -10^5 yr 2 sec

"Random walk"



CNO Cycle

- Carbon = catalyst : a substance that causes a chemical reaction to happen more quickly, while the substance not consumed and remain unchanged
- 촉매(觸媒) : 반응과정에서 소모되거나 변화되지 않으면서 반응속도를 빠르거나 느리게 변화시키는 물질



β^+ decay : $p \rightarrow n + \beta^+ + \nu_e$
※ $\beta^+ = e^+$ (positron)

- Start : C + p
- At high-temp stars : $T > 1.6 \times 10^7$ K, $M > 1.1\ M_{\odot}$

CNO cycle process

$$^{12}C + {}^{1}H \rightarrow {}^{13}N + \gamma$$

$$^{13}N \rightarrow {}^{13}C + e^{+} + \nu_e$$

^{13}N : unstable isotope

$$^{13}C + {}^{1}H \rightarrow {}^{14}N + \gamma$$

$$^{14}N + {}^{1}H \rightarrow {}^{15}O + \gamma$$

$$^{15}O \rightarrow {}^{15}N + e^{+} + \nu_e$$

^{15}O : unstable isotope

$$^{15}N + {}^{1}H \rightarrow {}^{12}C + {}^{4}He$$

CNO cycle process

$$^{12}C + {}^{1}H \rightarrow {}^{13}N + \gamma \qquad (1.95\ \text{MeV})$$

$$^{13}N \rightarrow {}^{13}C + e^{+} + \nu_e \qquad (1.20\ \text{MeV},\ {}^{13}N\ \text{half-life}=9.965^{m})$$

$$^{13}C + {}^{1}H \rightarrow {}^{14}N + \gamma \qquad (7.54\ \text{MeV})$$

$$^{14}N + {}^{1}H \rightarrow {}^{15}O + \gamma \qquad (7.35\ \text{MeV})$$

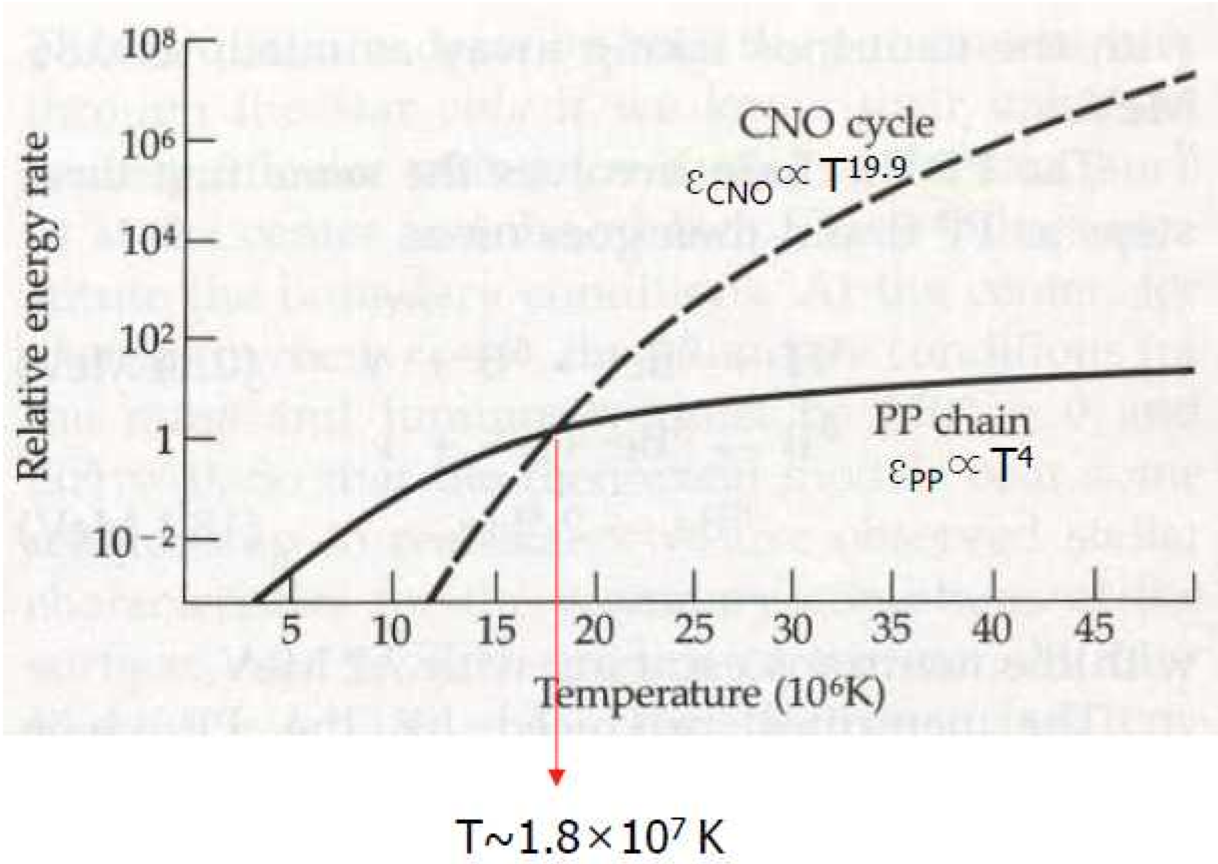
$$^{15}O \rightarrow {}^{15}N + e^{+} + \nu_e \qquad (1.73\ \text{MeV},\ {}^{15}O\ \text{half-life}=122.24^{s})$$

$$^{15}N + {}^{1}H \rightarrow {}^{12}C + {}^{4}He \qquad (4.96\ \text{MeV})$$

※ 2 positrons annihilate with 2 ambient electrons → produce 2.04 MeV

Total 24.73 + 2.04 = 26.73 MeV

Energy-generation rates



Introductory Astronomy and Astrophysics (4th edition)
Michael Zeilik & Stephen A. Gregory (1998), Fig 16-2

Triple-alpha (3α) process

Nucleosynthesis using He :

$T \geq 10^8$ K, $\rho \geq 10^5$ g cm^{-3} : He → heavier elements

$^4He + {}^4He \Leftrightarrow {}^8Be + \gamma$ (-0.0918 MeV)

※ ^{8}Be lifetime ~ 2.6×10^{-16} s

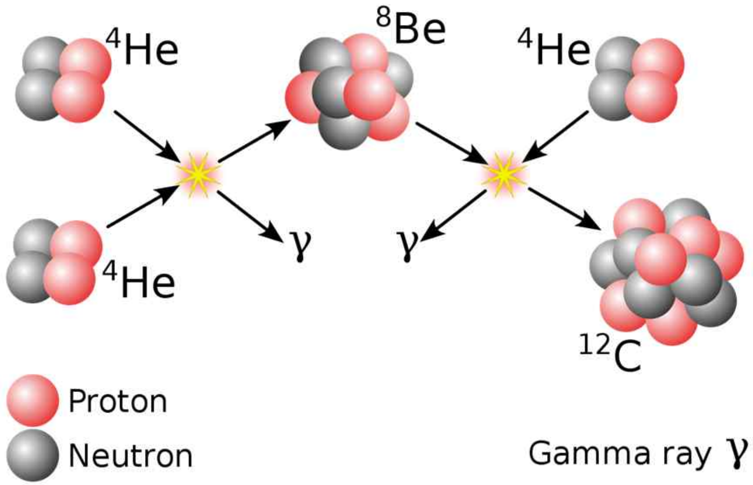
> mean collision (scattering) time of α-particle ($T_{scattering}$)

Huge amount of He, n(^{8}Be) : n(^{4}He) = 1 : 10^9

$^8Be + {}^4He \rightarrow {}^{12}C + \gamma$ (+7.367 MeV)

〈Emitted energy〉 = +7.275 MeV

"Triple- α process"



https://en.wikipedia.org/wiki/Triple-alpha_process

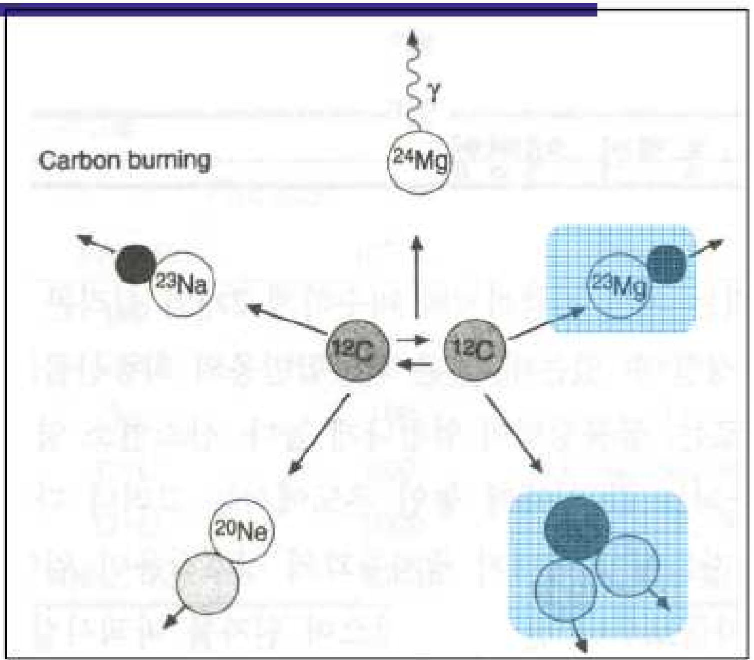
C, O-burning

$T \geq 5\times10^8$ K → C-burning

$$
\begin{aligned}
{}^{12}C + {}^{12}C &\rightarrow {}^{24}Mg + \gamma \quad (13.933\ \text{MeV})\\
&\rightarrow {}^{23}Mg + n \quad (-2.599\ \text{MeV})\ \text{(endothermic)}\\
&\rightarrow {}^{23}Na + p \quad (2.241\ \text{MeV})\\
&\rightarrow {}^{20}Ne + \alpha \quad (4.617\ \text{MeV})\\
&\rightarrow {}^{16}O + 2\alpha \quad (-0.113\ \text{MeV})\ \text{(endothermic)}
\end{aligned}
$$

〈Emitted energy〉 ≈ 13 MeV

~5.2 x 10^{13} J/kg = 5.2 x 10^{17} erg/g

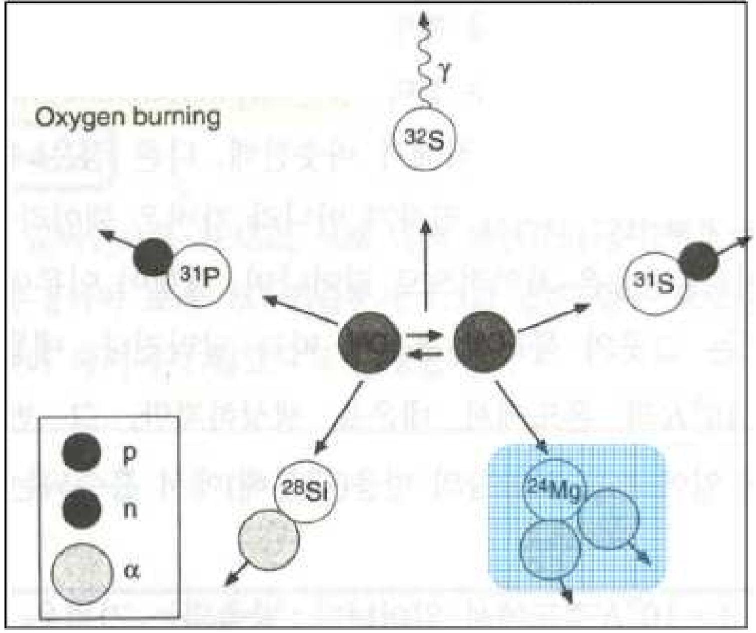


$T \geq 1\times10^9$ K → O-burning

$$
\begin{aligned}
{}^{16}O + {}^{16}O &\rightarrow {}^{28}Si + \alpha \quad (9.954\ \text{MeV})\ (\sim60\%)\\
&\rightarrow {}^{31}P + p \quad (7.678\ \text{MeV})\ (\sim40\%)\\
&\rightarrow {}^{31}S + n \quad (1.500\ \text{MeV})\\
&\rightarrow {}^{32}S + \gamma\\
&\rightarrow {}^{24}Mg + 2\alpha \quad \text{(endothermic)}
\end{aligned}
$$

〈Emitted energy〉 ≈ 16 MeV

~4.8 x 10^{13} J/kg = 4.8 x 10^{17} erg/g



항성내부구조 및 진화, Dina Prialnik 지음, 김용기 옮김, 2007 (An Introduction to the Theory of Stellar Structure and Evolution, 2000), p 85

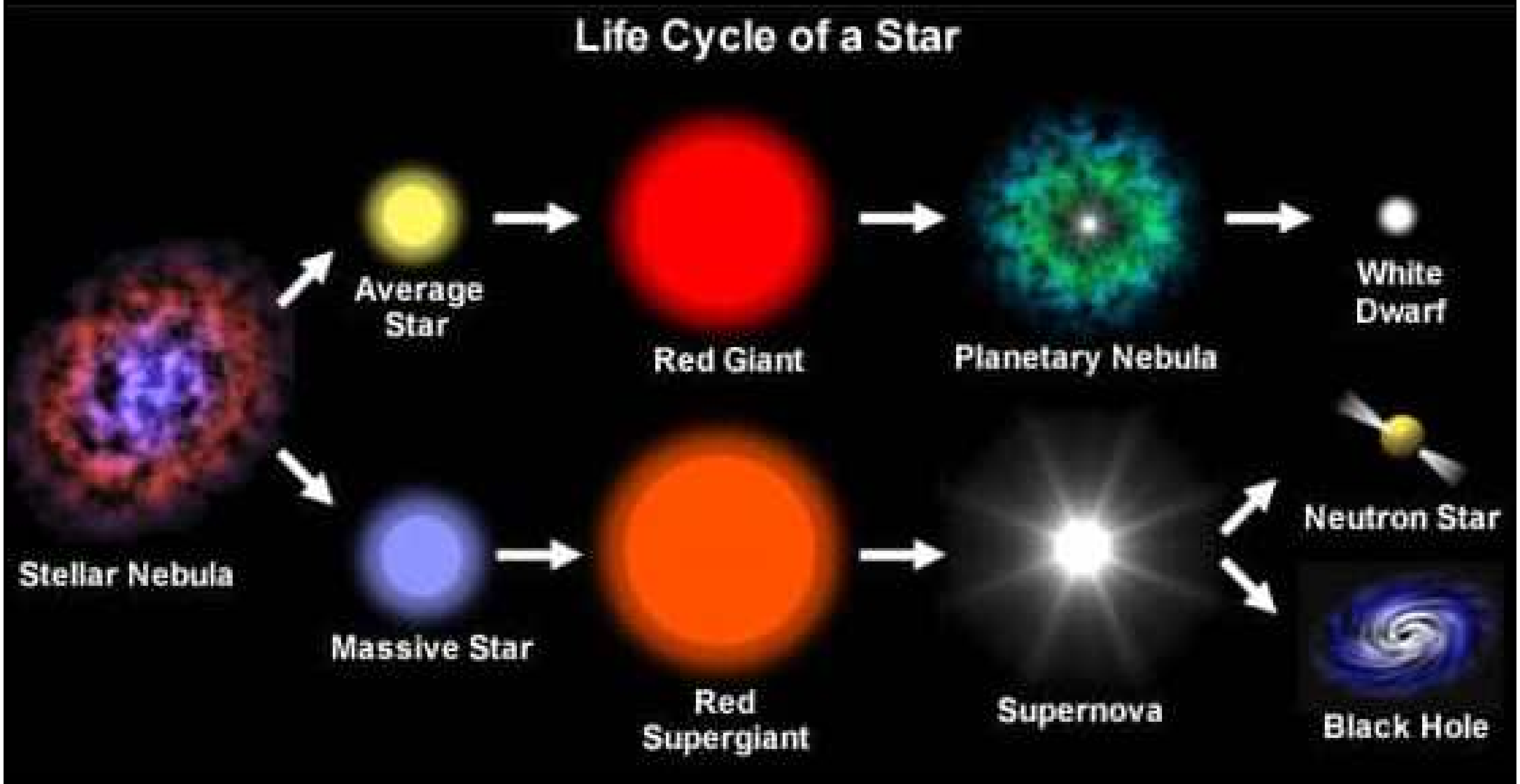
Si-burning

- After O-burning, core = Si + S
- T ~ $(2.7\text{-}3.5)\times10^9$ K (depends on mass)
- Duration ~ 2 weeks
- No further fusion is possible.

$$^{28}_{14}\text{Si} + {}^{4}_{2}\text{He} \rightarrow {}^{32}_{16}\text{S}$$
$$^{32}_{16}\text{S} + {}^{4}_{2}\text{He} \rightarrow {}^{36}_{18}\text{Ar}$$
$$^{36}_{18}\text{Ar} + {}^{4}_{2}\text{He} \rightarrow {}^{40}_{20}\text{Ca}$$
$$^{40}_{20}\text{Ca} + {}^{4}_{2}\text{He} \rightarrow {}^{44}_{22}\text{Ti}$$
$$^{44}_{22}\text{Ti} + {}^{4}_{2}\text{He} \rightarrow {}^{48}_{24}\text{Cr}$$
$$^{48}_{24}\text{Cr} + {}^{4}_{2}\text{He} \rightarrow {}^{52}_{26}\text{Fe}$$
$$^{52}_{26}\text{Fe} + {}^{4}_{2}\text{He} \rightarrow {}^{56}_{28}\text{Ni}$$

https://en.wikipedia.org/wiki/Silicon-burning_process

2. The Evolution of Stars (별의 진화)
2-2 Stellar Evolution (항성 진화)



http://schoolworkhelper.net/types-of-stars/

Sun + Star

Solar surface composition :
X=0.73, Y=0.25, Z=0.02

Star = atmosphere + interior

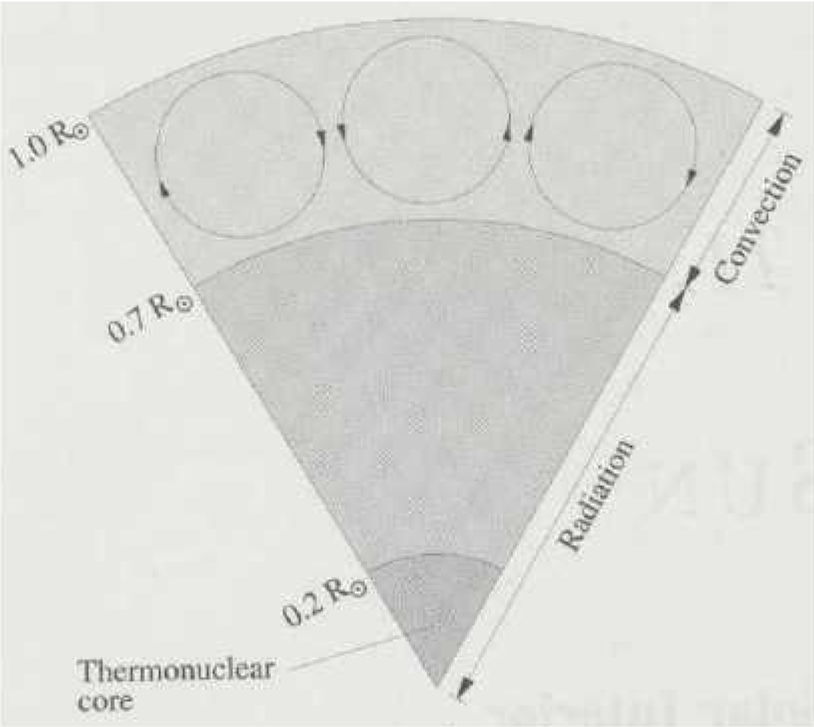
Optical depth < 1	Optical depth > 1 nuclear reaction

※ Optical depth, τ_λ : $d\tau_\lambda = -\kappa_\lambda \rho \, ds$

$\tau_\lambda \gg 1$: optically thick

$\tau_\lambda \ll 1$: optically thin

※ κ_λ : absorption coefficient (opacity)



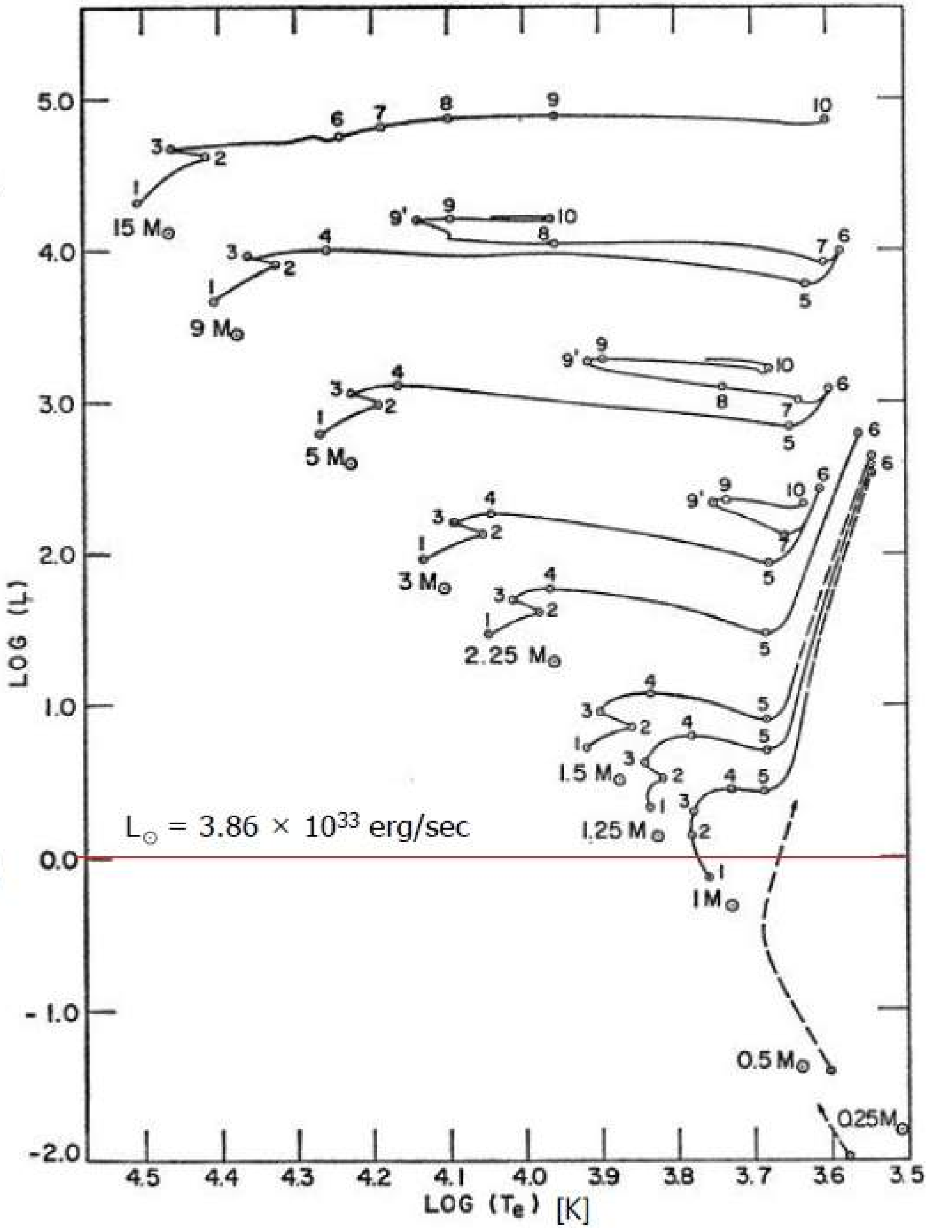
Sun's interior

An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 382

Post-MS Stellar Evolution

Hertzsprung-Russell Diagram of Metal-rich stars
(X=0.708, Y=0.272, Z=0.020)
M = 15, 9, 5, 3, 2.25, 1.5, 1.25, 1, 0.5, 0.25 $M_\odot$
Dashed lines : estimates

- Sun's L, R, T : increased steadily since it reached the zero-age main sequence (ZAMS) ~4.5 Gyr ago



Iben (1967, ARA&A, 5, 571) Fig 3

Solar Evolution

Sun's center, during its lifetime :
X : 0.71 → 0.34
Y : 0.27 → 0.64
changing the composition and structure

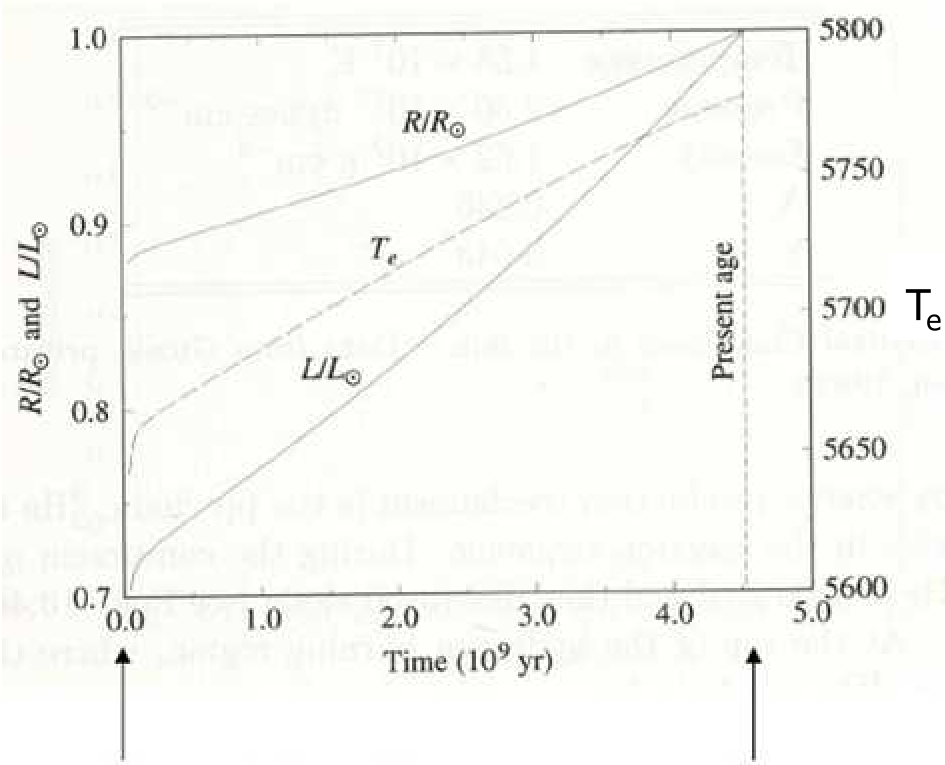
The change in the Sun's central composition
→direct influence on observable L, T_{eff}, and R

L increased by 40%
R increased by >10%

※ Physical parameters of the Solar center
(standard solar model of Joyce Guzik)

Central conditions in the Sun

T_C	**(1.56~) 1.58 ×10^7 K**
P_C	2.50×10^{17} dyne/cm²
ρ_C	162 (150-160) g/cm³
X_C	0.336
Y_C	0.643



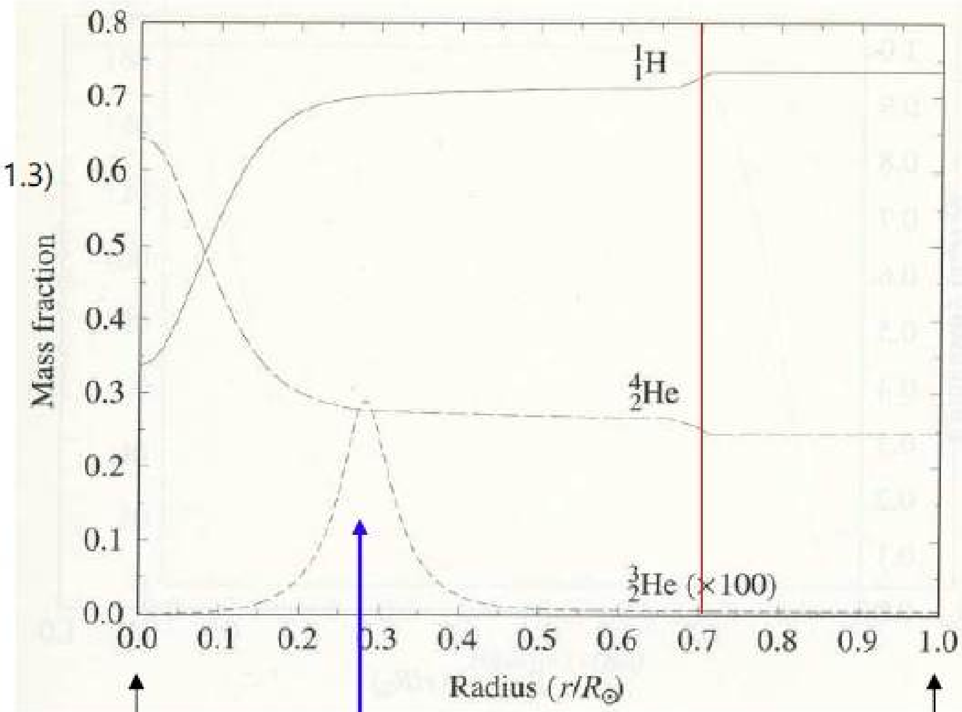
Birth (beginning of the nuclear burning)

Present

L : 1.43 times increase

Solar **composition** structure

(Fig 11.3)



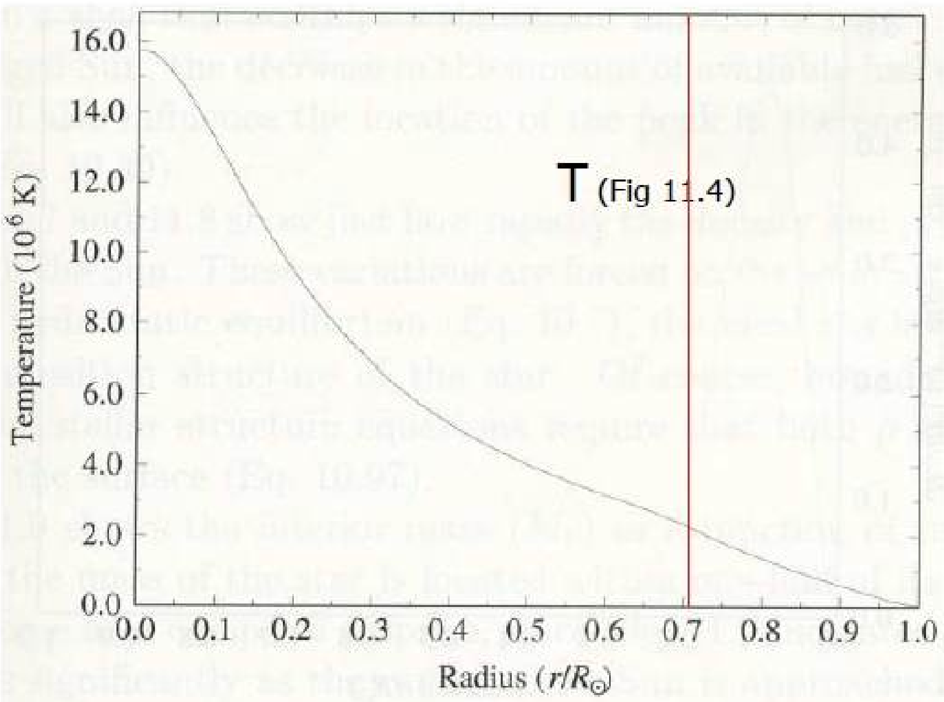
center

surface

Produced more easily than destroyed

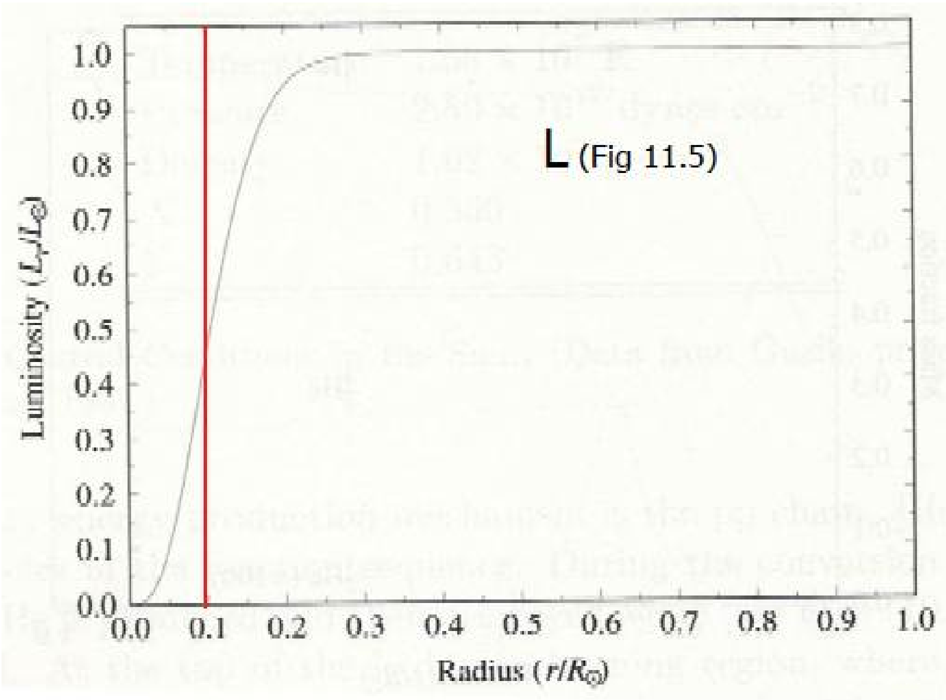
※ $^3_2$He : intermediate species in the pp chain reaction sequence

Solar **Temp** structure

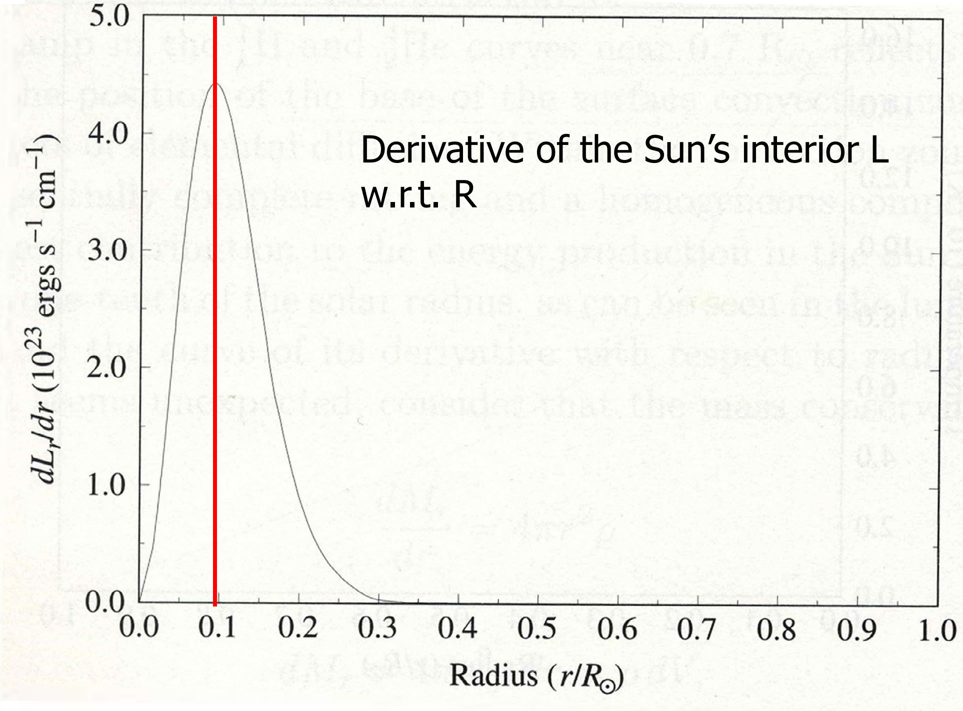


An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 385

Interior Lum of the Sun



Location of the greatest contribution to the E output



Though amount of E liberated per gram of material (ε) decreases steadily from R=0 outward
→ Largest contribution to the total L – in a shell that contains a significant amount of mass

An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 386

Post-MS Stellar Evolution

TABLE III Stellar Lifetimes (yr)[a]

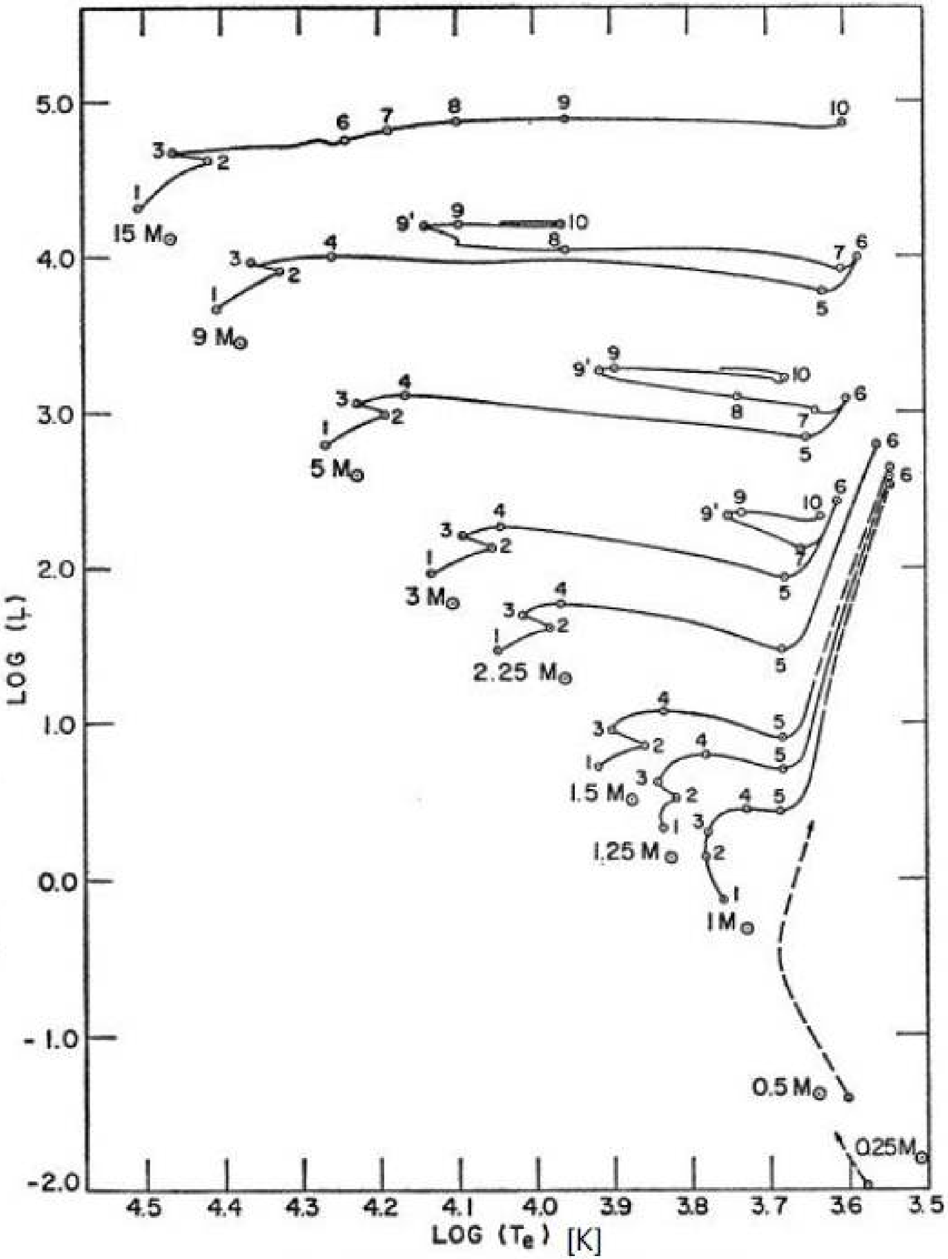
Mass ($M_\odot$) \ Interval ($i-j$)	(1–2)	(2–3)	(3–4)	(4–5)	(5–6)
15	1.010 (7)	2.270 (5)		7.55 (4)	
9	2.144 (7)	6.053 (5)	9.113 (4)	1.477 (5)	6.552 (4)
5	6.547 (7)	2.173 (6)	1.372 (6)	7.532 (5)	4.857 (5)
3	2.212 (8)	1.042 (7)	1.033 (7)	4.505 (6)	4.238 (6)
2.25	4.802 (8)	1.647 (7)	3.696 (7)	1.310 (7)	3.829 (7)
1.5	1.553 (9)	8.10 (7)	3.490 (8)	1.049 (8)	≥2 (8)
1.25	2.803 (9)	1.824 (8)	1.045 (9)	1.463 (8)	≥4 (8)
1.0	7 (9)	2 (9)	1.20 (9)	1.57 (8)	≥1 (9)

[a] Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.

TABLE IV Stellar Lifetimes (yr)[a]

Mass ($M_\odot$) \ Interval ($i-j$)	(6–7)	(7–8)	(8–9)	(9–10)
15	7.17 (5)	6.20 (5)	1.9 (5)	3.5 (4)
9	4.90 (5)	9.50 (4)	3.28 (6)	1.55 (5)
5	6.05 (6)	1.02 (6)	9.00 (6)	9.30 (5)
3	2.51 (7)	4.08 (7)		6.00 (6)

[a] Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.



Iben (1967, ARA&A, 5, 571) Fig 3

Post-MS Stellar Evolution

TABLE III STELLAR LIFETIMES (yr)[a]

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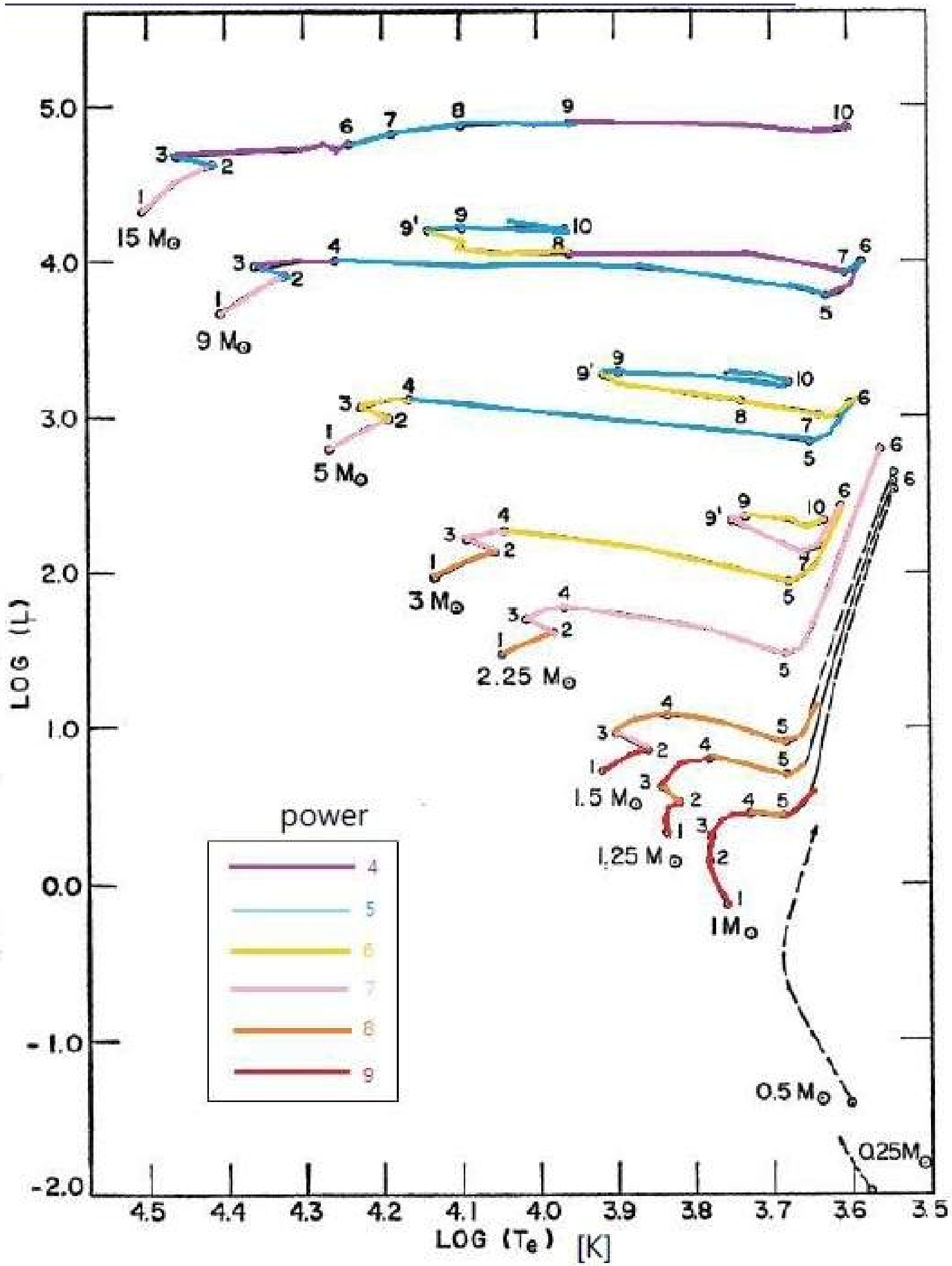
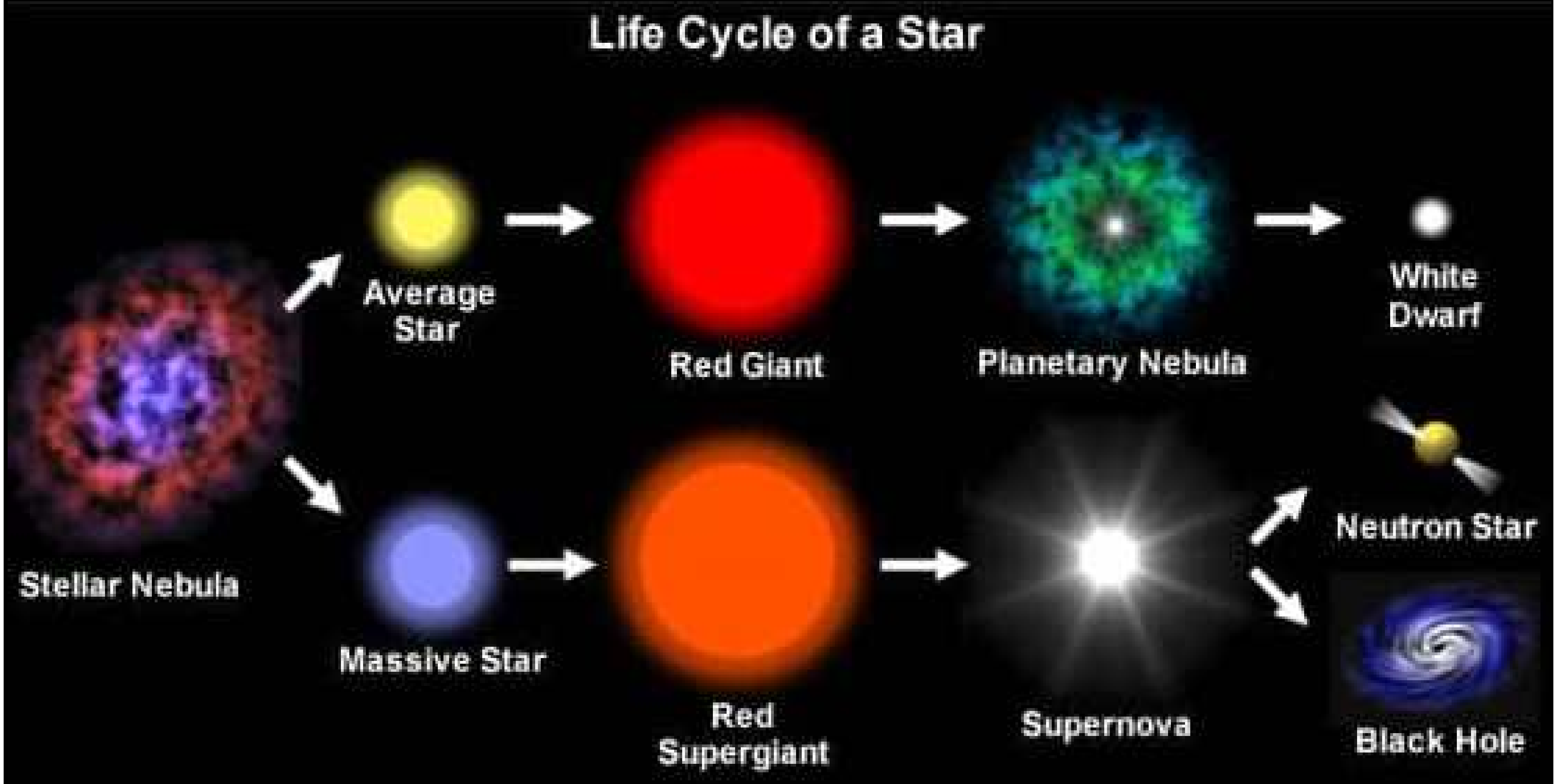


Iben (1967, ARA&A, 5, 571) Fig 3

2. The Evolution of Stars (별의 진화)
2-3 Post-Main-Sequence Evolution (주계열 이후 진화)



http://schoolworkhelper.net/types-of-stars/

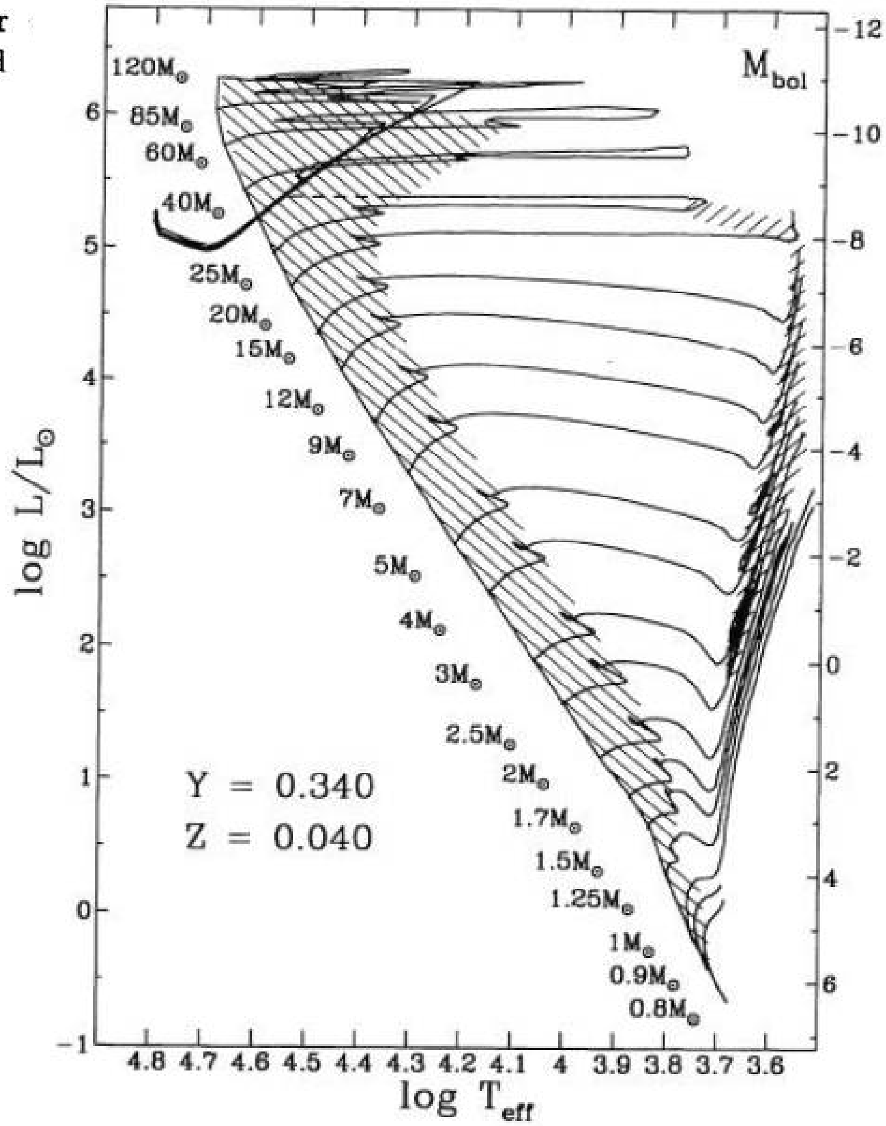
Post-MS Stellar Evolution

D. Schaerer, C. Charbonnel, G. Meynet, A. Maeder and G. Schaller
Geneva Observatory, CH-1290 Sauverny, Switzerland

1993 *Astron. Astrophys. Suppl. Ser.* **102**, 339

Grids of stellar models.
IV. From 0.8 to 120 $M_\odot$ at $Z = 0.040$

Stellar evolution isochrones
- Padova (Bressan+12 MN 427 127)
- Geneva
- VandenBerg (83 ApJS 51 29)
- Yonsei-Yale (Y^2) (Demarque+04 ApJS 155 667)
- Dartmouth (Dotter+07 ApJ 666 403)
- Modules for Experiments in Stellar Astrophysics (MESA) (Paxton+11 ApJS 192 3)
- MESA Isochrones and Stellar Tracks (MIST) (Dotter 16 ApJS 222 8)
- Yunnan-III (Zhang+13 MN 428 3390)



Schaerer et al (1993, A&AS, 102, 339) – Fig 1

Hatched areas : slow phases of nuclear burning

Post-MS Stellar Evolution

D. Schaerer, C. Charbonnel, G. Meynet, A. Maeder and G. Schaller
Geneva Observatory, CH-1290 Sauverny, Switzerland
1993 *Astron. Astrophys. Suppl. Ser.* **102**, 339

Grids of stellar models.
IV. From 0.8 to 120 $M_\odot$ at $Z = 0.040$

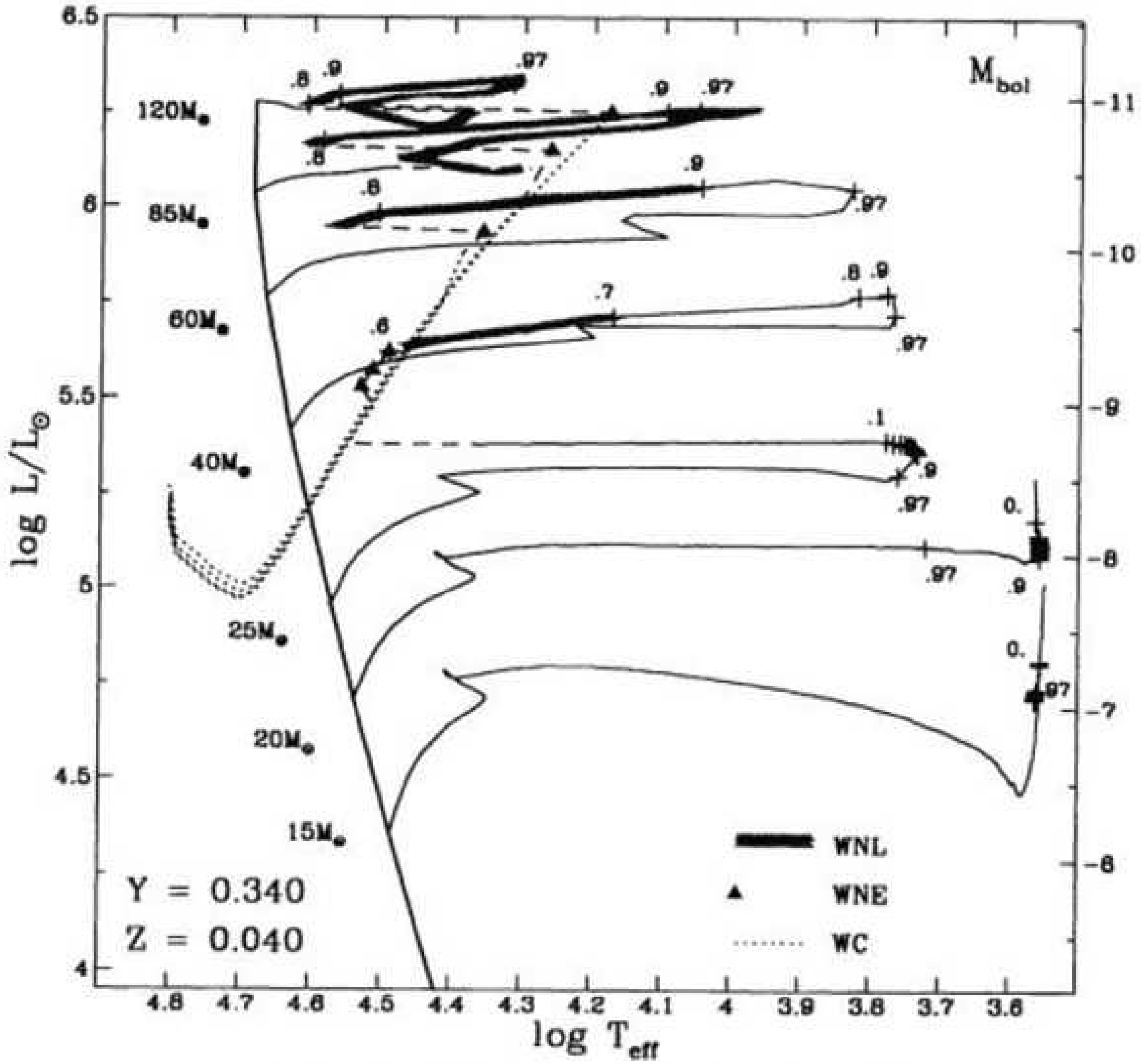
HRD of massive stars (15 – 120 $M_\odot$) with Z=0.040

Yc (central He content) : 0.97, 0.90, 0.80, 0.70, 0.60, ---, 0.10, 0

Wolf-Rayet stars

- Hot : T_{eff} = 30,000 – 200,000 K
- Broad emission lines of He I, He II, C III, C IV, N III, N V
- Very high surface enhancement of heavy elements (He etc.), depletion of hydrogen
- Strong stellar winds

WN Early (WN2 – WN6)
WN Late (WN6 – WN9)
WC



Schaerer et al (1993, A&AS, 102, 339) – Fig 3

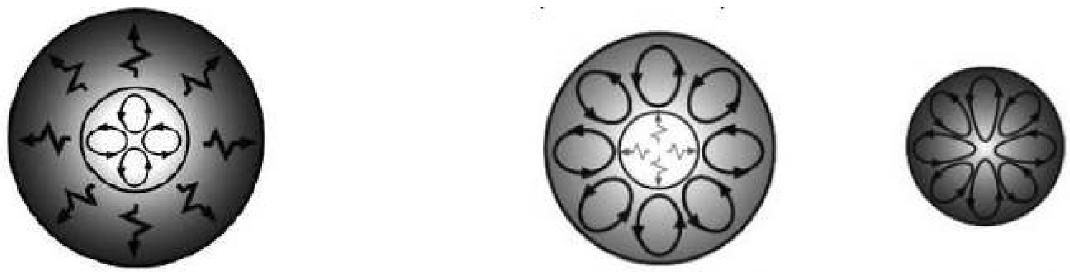
Characteristics of MS Stars

$M > 1.5\ M_{\odot}$	$M < 1.5\ M_{\odot}$
$T_c > 2 \times 10^7$ K	$T_c < 2 \times 10^7$ K
CNO cycle	PP chain
Energy production rate : $\varepsilon_{CNO} \propto T^{19.9}$ --> Production of most E near the center	$\varepsilon_{CNO} \propto T^4$ --> E source is not concentrated to the center
core : convective	core : radiative
envelope : radiation	envelope : H-convection

The more massive,
the larger convective core.

$\xleftarrow{\hspace{2em}}$ mass

As mass decreases,
H-convection zone deepens.



$M > 1.5 M_{\odot}$ $\quad$ $0.5 M_{\odot} < M < 1.5 M_{\odot}$ $\quad$ $M < 0.5 M_{\odot}$

https://ase.tufts.edu/cosmos/view_picture.asp?id=1409

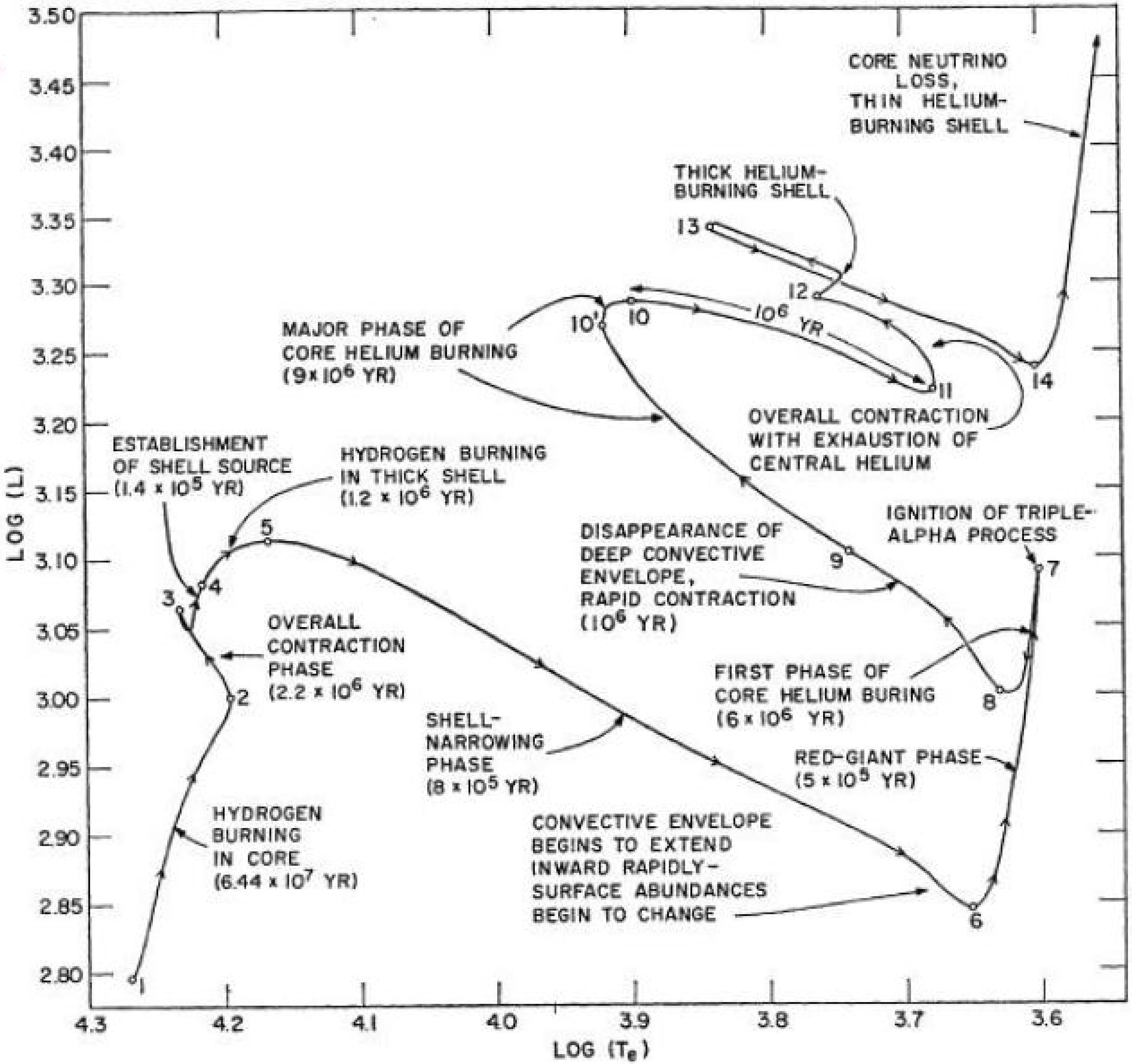
Dominant energy transport mode :

- Low temperature gradient, low opacity → radiation
- Steep temperature gradient → convection

Post-MS Stellar Evolution

- Evolutionary path of a 5 $M_\odot$ metal-rich star in the HRD

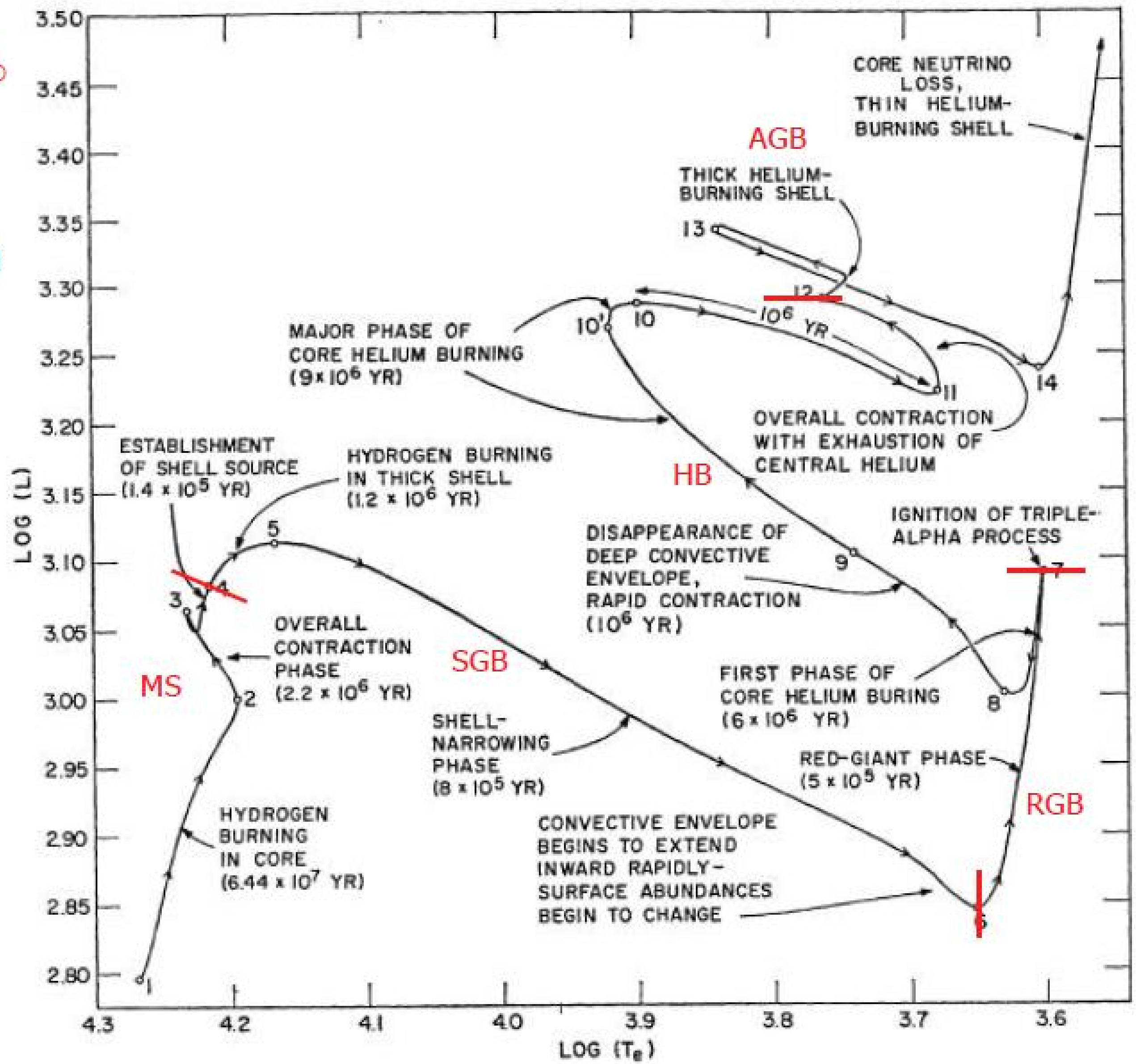
- From ZAMS
to the asymptotic giant branch (AGB)



Iben (1967, ARA&A, 5, 571) Fig. 1

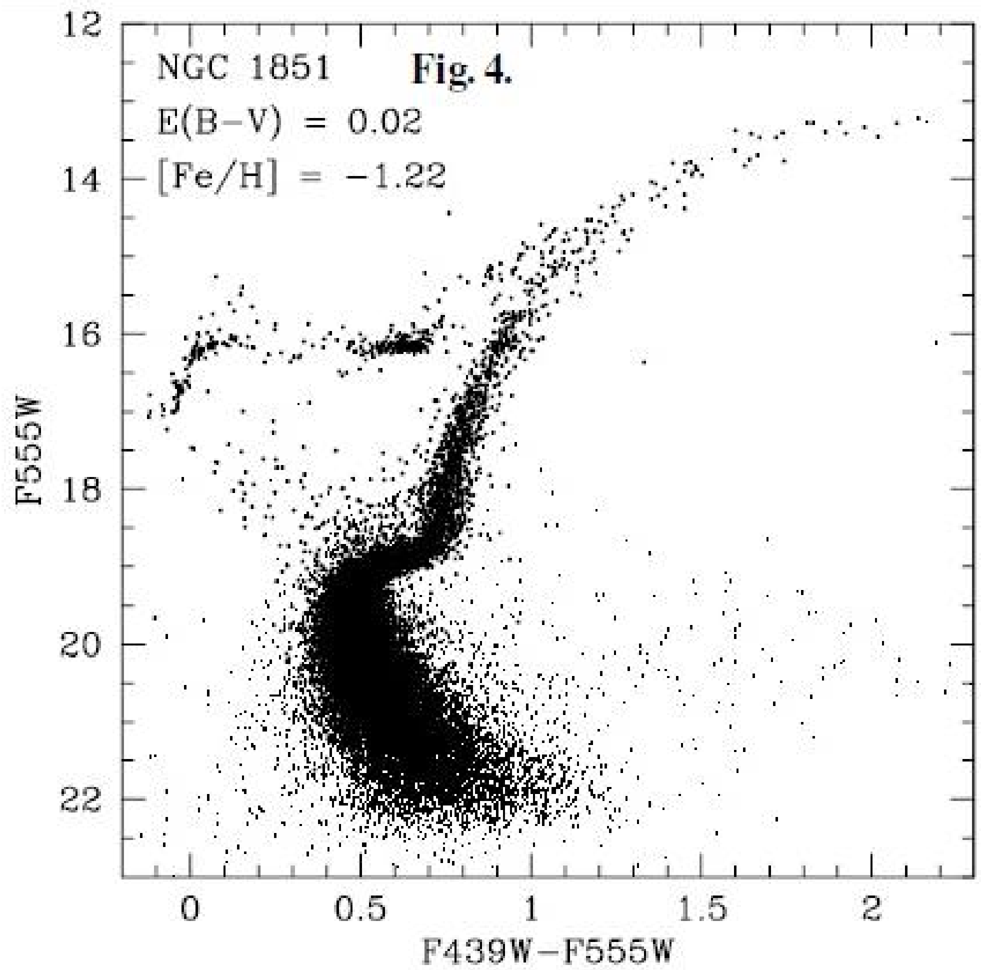
Post-MS Stellar Evolution

- Evolutionary path of a 5 $M_\odot$ metal-rich star in the HRD
- From ZAMS to the asymptotic giant branch (AGB)

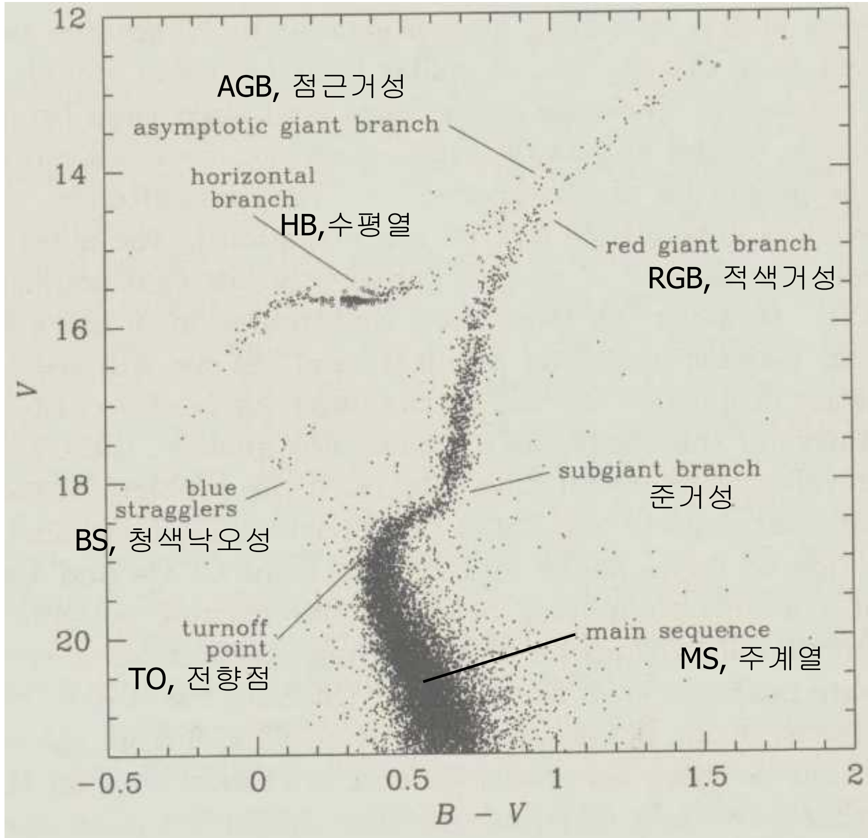


Iben (1967, ARA&A, 5, 571) Fig. 1

Color-Magnitude Diagrams for globular clusters (GCs)



Piotto et al. (2002, A&A, 391, 945)

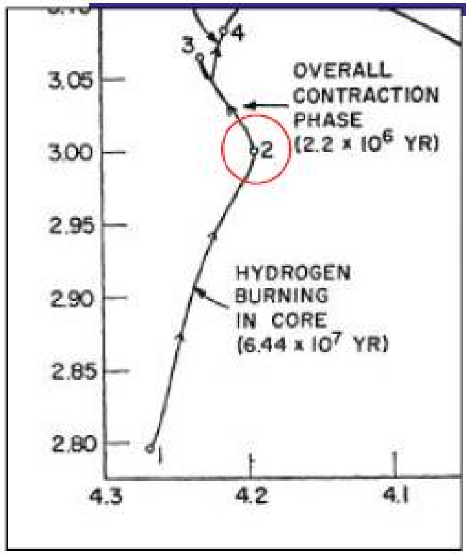


GC M3 (NGC 5272) [Fe/H]=-1.34
(variables=open circles)

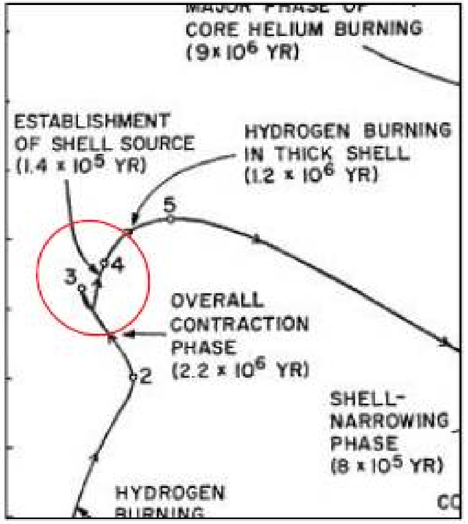
Galactic Astronomy (J. Binney & M. Merrifield, 1998) p. 334

Forbes & Bridges 10 MN 404 1203 (Accreted vs. in situ MW GCs)

5 $M_{\odot}$ star - structure



- At point 2 : near depletion of H fuel in the core
- During 2 → 3 : overall contraction (Core H mass fraction X : reduced to 0.01)

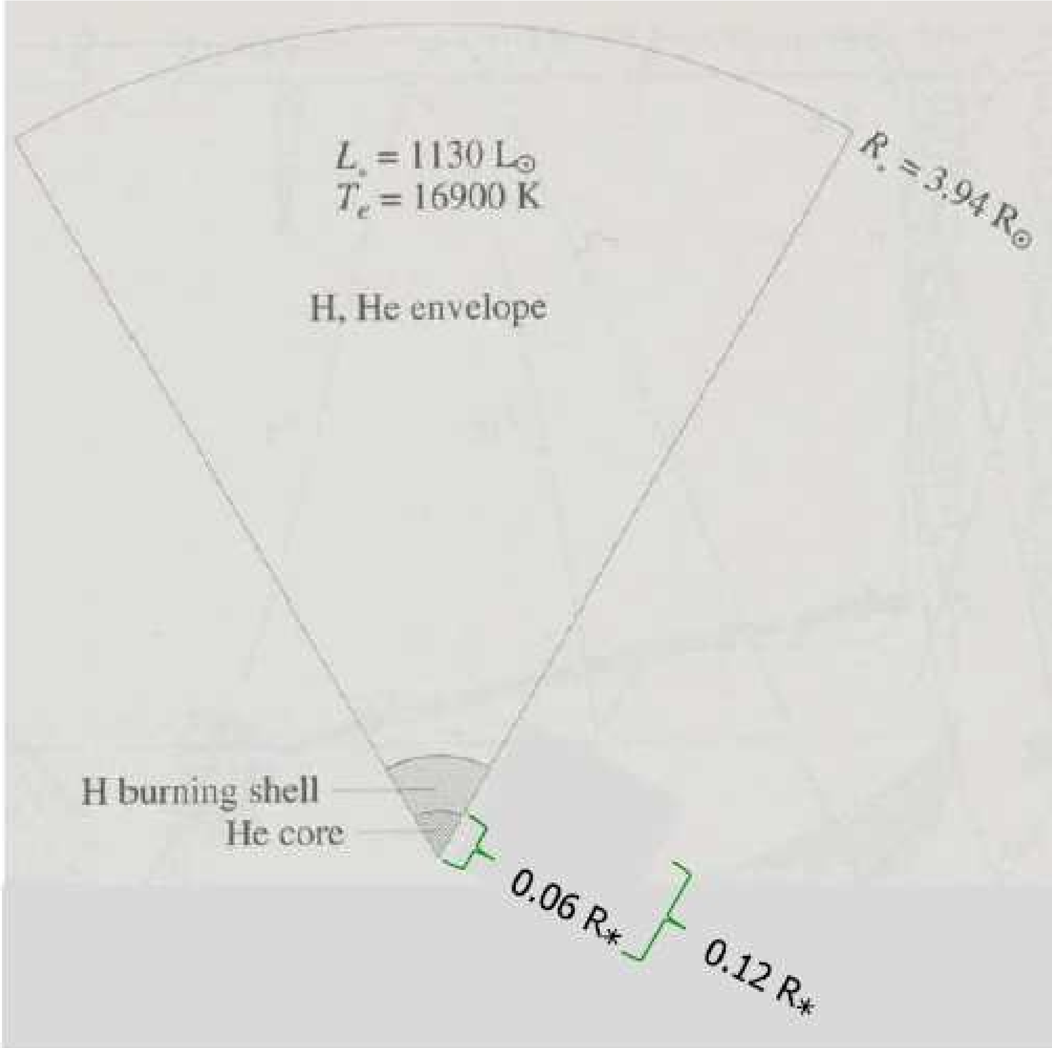


- During 3 → 4 : establishment of shell source - H burning begins in a thick shell
  - Rapid shell ignition → overlying **envelope** absorbs some or much of the E release by the shell → envelope slightly **expands**

5 $M_\odot$ star approaching the RGB

Shortly after point 3 :

H shell burning

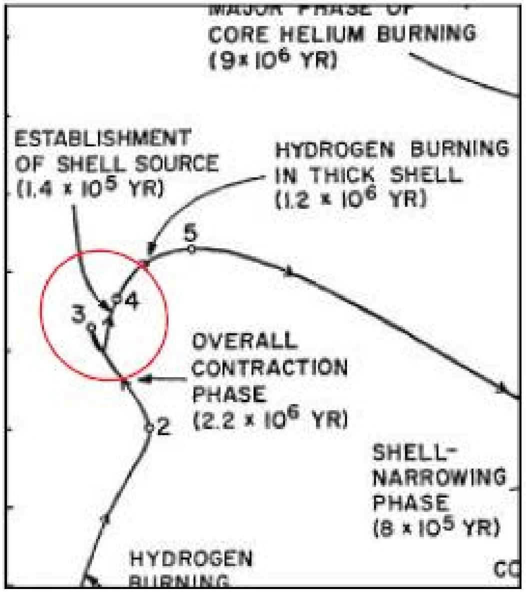


An Introduction to Modern Astrophysics (2nd edition), Bradley W. Carroll & Dale A. Ostlie (1996), p. 498

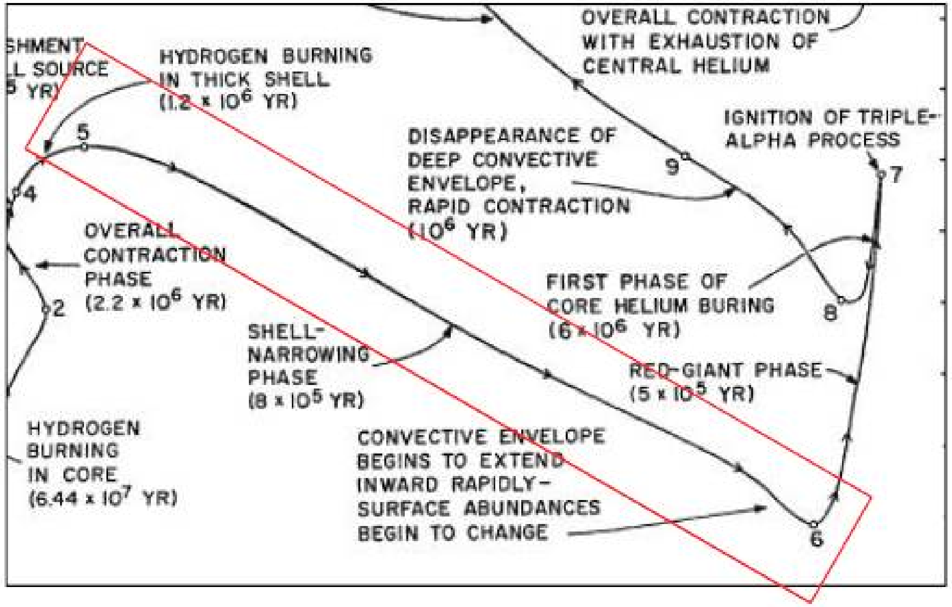
Evolution beyond point 3

- Generated energy → goes into slow expansion of the envelope
- T_{eff} decreases slightly, evolutionary track bens to the right

- Redward locus = subgiant branch



Sub Giant Branch (SGB) : 5 $M_{\odot}$ star



- During point 5 → 6 :
  - **Envelope expands** (absorbing much of the shell's E, before it reaches the surface)
  - → L decreases, effective T decreases, photospheric optacity increases (H^- ion)
  - → convection zone begins to develop near the surface

- Base of the convection zone → extends down into regions where the chemical composition has been modified by nuclear processes

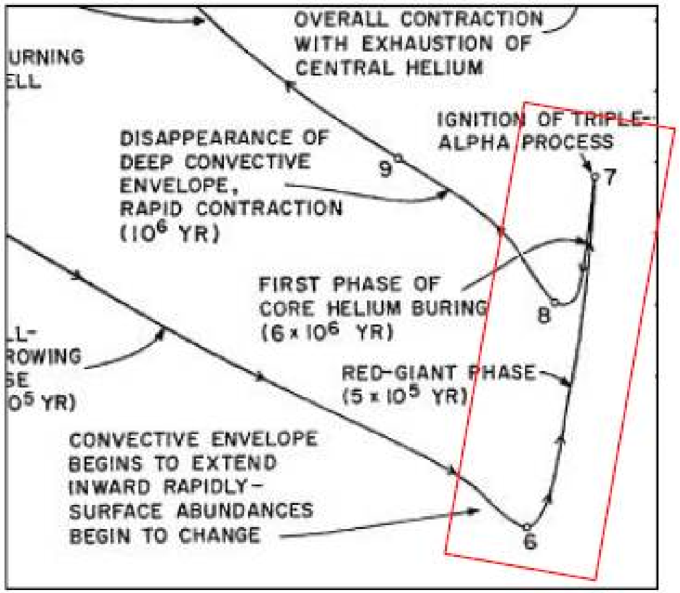
- Surface convection zone encounters these chemically modified regions

→Processed material become mixed

→Photosphere composition change (Li ↓, ${}^{3}_{2}He$ ↑)

"First dredge-up" begins at point 6

5 $M_\odot$ star at the RGB



- During 6 → 7

: core continues to contract – degenerate He

→ (narrowing) H-b shell E-production rate ↑

→ L↑, R ↑

→ vertical evolution, "**red giant branch (RGB)**"

- At point 7 :

- $T_c = 1.3 \times 10^8$ K
- $\rho_c = 7700$ g/cm^3
- High central T and density → quantum-mechanical tunneling through the Coulomb barrier (acting between $^4_2$He nuclei) becomes effective

  → triple-α process begins

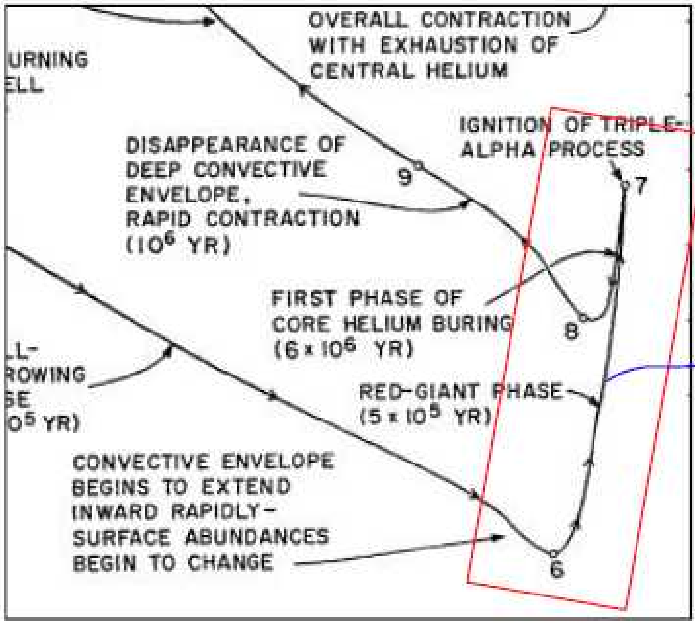
- Slow ignition of He-burning phase!
- New source of E → core expands

→ Shell E-generation rate decreases

→ L ↓

and envelope contracts, T_{eff} ↑

※ For low mass stars of $M < 2 M_\odot$



- As He-core continues to collapse

→ Core becomes strongly electron-degenerate

- T, ρ become high enough

to initiate the triple-α process (10^8 K, 10^4 g/cm^3)

→ Explosive E release!

(core) helium flash

- Luminosity ~$10^{11} L_\odot$

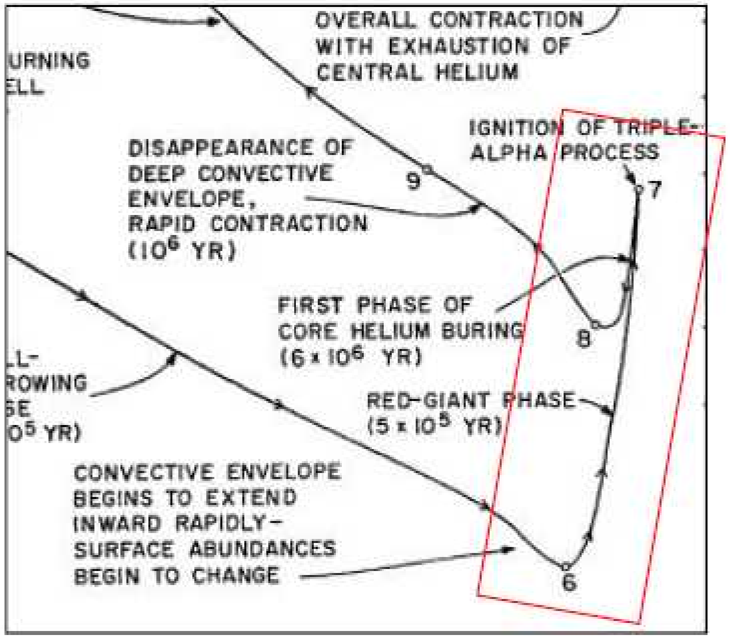
→ For only a few seconds!

(most of the E never reaches the surface)

→ E "lifts" the degeneracy and

absorbed by the overlying layers of the envelope (possibly cause some mass loss)

※ For low mass stars of M < 2 $M_\odot$



- **(core) helium flash**

: Nearly constant mass – function of metallicity

~1.6 $M_\odot$ for population I stars

~1 $M_\odot$ for population II stars

- For pop II stars (ages 2-15 Gyr),

if metallicity is same

→ bolometric luminosity is ~ constant

(varies only by ~ 0.1 mag)

→ TRGB (tip of the red giant branch)

: distance indicator for old, resolved galaxies

TRGB (tip of the red giant branch)

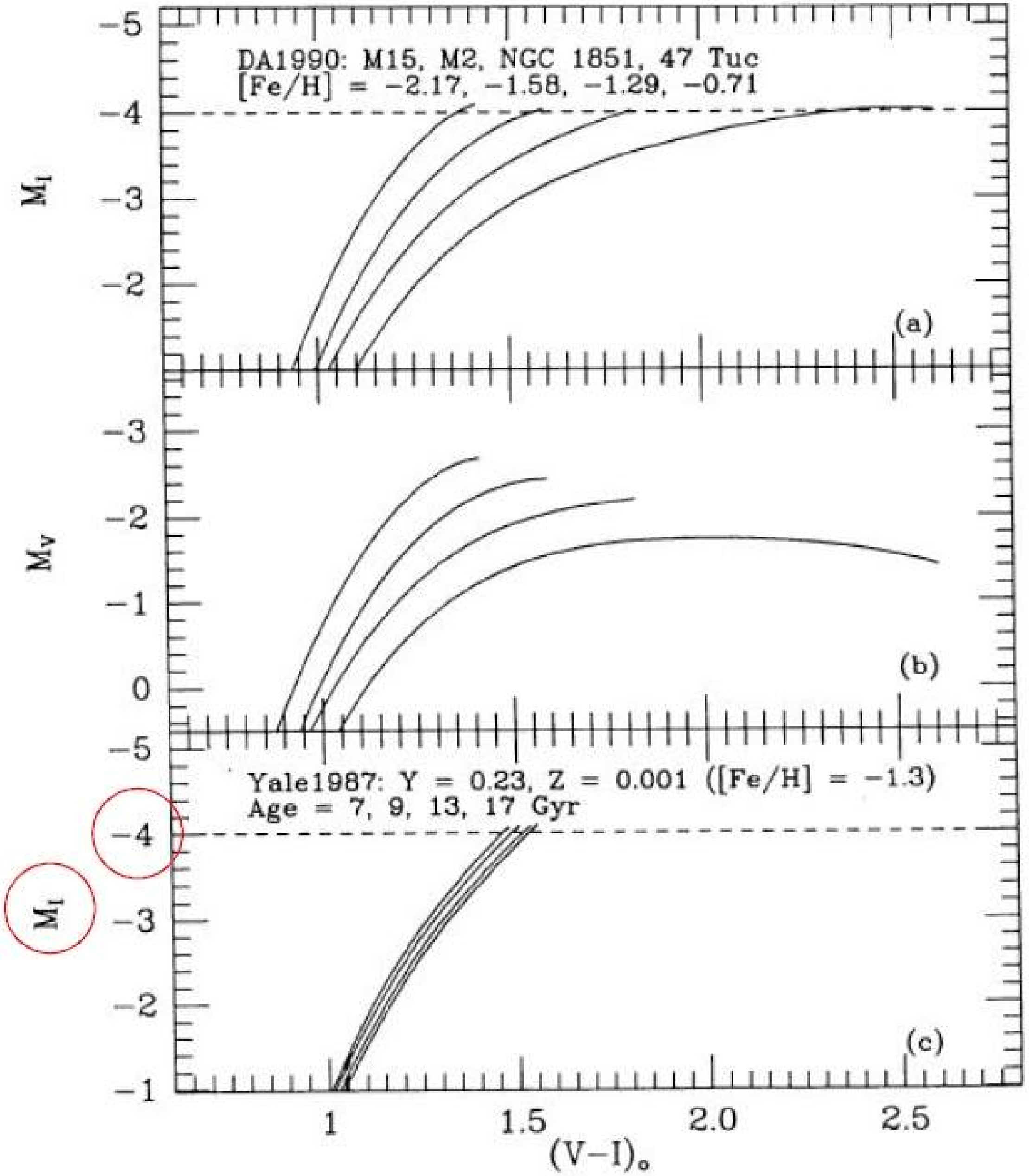


Fig. 1

Lee et al. (1993, ApJ, 417, 553)