

# CMSC498F Final

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- 1 Given two observations  $\hat{q}_1$  and  $\hat{q}_2$  with variances  $\sigma_1^2$  and  $\sigma_2^2$  of a normal distributed process with actual value  $q$ . The optimal estimate can be calculated by minimizing the expression  $S = \frac{1}{\sigma_1^2}(\hat{q}_1 - q)^2 + \frac{1}{\sigma_2^2}(\hat{q}_2 - q)^2$ . Calculate  $\hat{q}$  so that  $S$  is minimized.
- 2 An ultrasound sensor measures distance  $x = c \cdot t$ . Here,  $c$  is the speed of sound and  $t$  is the difference in time between emitting and receiving a signal.
  - (a) Let the variance of your time measurement  $t$  be  $\sigma_t^2$ . What can you say about the variance of  $x$ , when  $c$  is assumed to be constant? Hint: how does a change in  $t$  affect  $x$ ?
  - (b) Now assume that also  $c$  is changing depending on location, weather, etc. and can be estimated with variance  $\sigma_c^2$ . What is the variance of  $x$  now?
- 3 SIFT feature description and detection
  - (a) Describe the four computational steps of SIFT feature description and detection.
  - (b) Describe SURF features, and discuss how and why the computations of these features are more efficient than SIFT
  - (c) Describe one other feature detector from the literature.
- 4 Assume the following scene shown in Fig.1 with a background plane of 5m distance and two objects (a rounded rectangle and a triangle) at 1m distance as drawn below.
  - (a) The camera is moving towards the scene with the direction of translation denoted by the red cross (the so-called Focus of Expansion). Draw the flow field qualitatively.
  - (b) What is the aperture problem in computing optical flow? How is it related to the linear constraint on optical flow (brightness con-

straint?) determined by the differential technique for computing flow?

(c) Describe the Lucas Kanade optical flow algorithm.

5 Assume that the ceiling is equipped with infra-red markers that the robot can identify with some certainty. Your task is to develop a probabilistic localization scheme, and you would like to calculate the probability  $p(\text{marker} \rightarrow \text{reading})$  to be close to a certain marker given a certain sensing reading and information about how the robot has moved.

- (a) Derive an expression for  $p(\text{marker} \rightarrow \text{reading})$  assuming that you have an estimate of the probability to correctly identify a marker  $p(\text{reading} \rightarrow \text{marker})$  and the probability  $p(\text{marker})$  of being underneath a specific marker.
- (b) Now assume that the likelihood that you are reading a marker correctly is 90%, that you get a wrong reading is 10% right underneath it is 50% that is equipped with 4 markers. You know with certainty that you started from the entry closest to marker 1 and move right in a straight line. The first reading you get is ?Marker 3?. Calculate the probability to be indeed underneath marker 3.
- (c) Could the robot also possibly be underneath marker 4?