Programming Languages: Functional Programming Practicals 0: Functions and Definitions

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You should have installed GHC, with its commandline interface GHCi. Open your favourite text editor, create a new plain text file. The filename extension must end in .hs. This will be your working file for this practical. Type ghci <filename>.hs in the command line to load the working file into GHCi.

1. Define a function myeven::Int \rightarrow Bool that determines whether the input is an even number. You may use the following functions:

```
mod :: Int \rightarrow Int \rightarrow Int, (==) :: Int \rightarrow Int \rightarrow Bool.
```

(Types of the functions written above are not in their most general form.)

- 2. Define a function that computes the area of a circle with given radius r (using 22 / 7 as an approximation to π). The return type of the function might be Float.
- 3. Part-time students in Institute of Information Science are paid NTD 130 per hour. Define a function *payment* :: Int → Int that, when applied to the numbers of weeks a student work, compute the amount of money the Institute has to pay the student.
 - (a) Assume that there are five working days in a week, eight working hours per day. Define *payment*. For clarity, use **let** to define local variables recording number of days worked, number of hours worked, etc.
 - (b) Define *payment* again, but declare the local variables using **where**. Which style do you prefer?
 - (c) The regulation states that students are considered workers, and if a worker works for more than 19 weeks, the Institute has to pay, in addition to the salary, health insurance and pension reserves for the worker. The amount is 6% of the worker's salary.

 Update definition of *payment* in the form:

```
payment :: Int \rightarrow Int
payment weeks | weeks > 19 = ...
| otherwise = ...
```

You may need a function *fromIntegral* to convert Int to Float, and a function *round* that rounds a floating point number to the nearest integer.

In this case, should you use **let** or **where**?

4. More on let.

(a) Guess what the value of *nested* would be. Type it into your working file and evaluated in in GHCi to see whether you guessed right. Note that indentation matters.

(b) Guess what the value of recursive would be. Try it in GHCi.

```
recursive :: Int

recursive = let x = 3

in let x = x + 1

in x.
```

5. Type in the definition of *smaller* into your working file.

```
smaller :: Int \rightarrow Int \rightarrow Int smaller x \ y = \text{if} \ x \leqslant y \text{ then } x \text{ else } y.
```

Then try the following:

- (a) In GHCi, type:t smaller to see the type of smaller.
- (b) Try applying it to some arguments, e.g. smaller 3 4, smaller 3 1.
- (c) Use :t to see the type of *smaller* 3 4.
- (d) Use :t to see the type of *smaller* 3.
- (e) In your working file, define a new function st3 = smaller 3.
- (f) Find out the type of st3 in GHCi. Try st3 4, st3 1. Explain the results you see.
- 6. More practice on curried functions.
 - (a) Define a function *poly* such that *poly* a b c $x = a \times x^2 + b \times x + c$. All the inputs and the result are of type *Float*.
 - (b) Reuse *poly* to define a function *poly1* such that *poly1* $x = x^2 + 2 \times x + 1$.
 - (c) Reuse poly to define a function poly2 such that poly2 a b c = $a \times 2^2 + b \times 2 + c$.
- 7. Type in the definition of *square* in your working file.
 - (a) Define a function *quad* :: Int \rightarrow Int such that *quad* x computes x^4 .

(b) Type in this definition into your working file. Describe, in words, what this function does.

twice
$$:: (a \rightarrow a) \rightarrow (a \rightarrow a)$$

twice $f(x) = f(f(x))$.

- (c) Define quad using twice.
- 8. Replace the previous *twice* with this definition:

twice
$$:: (a \rightarrow a) \rightarrow (a \rightarrow a)$$

twice $f = f \cdot f$.

- (a) Does *quad* still behave the same?
- (b) Explain in words what this operator (⋅) does.
- 9. Functions as arguments, and a quick practice on sectioning.
 - (a) Type in the following definition to your working file, without giving the type.

forktimes
$$f g x = f x \times g x$$
.

Use : *t* in GHCi to find out the type of *forktimes*. You will end up getting a complex type which, for now, can be seen as equivalent to

$$(t \rightarrow Int) \rightarrow (t \rightarrow Int) \rightarrow t \rightarrow Int$$
.

Can you explain this type?

- (b) Define a function that, given input x, use *forktimes* to compute $x^2 + 3 \times x + 2$. **Hint**: $x^2 + 3 \times x + 2 = (x + 1) \times (x + 2)$.
- (c) Type in the following definition into your working file: $lift2 \ h \ f \ g \ x = h \ (f \ x) \ (g \ x)$. Find out the type of lift2. Can you explain its type?
- (d) Use *lift2* to compute $x^2 + 3 \times x + 2$.
- 10. Let the following identifiers have type:

$$f :: Int \rightarrow Char$$

 $g :: Int \rightarrow Char \rightarrow Int$
 $h :: (Char \rightarrow Int) \rightarrow Int \rightarrow Int$
 $x :: Int$
 $y :: Int$
 $c :: Char$

Which of the following expressions are type correct?

1.
$$(g \cdot f) \times c$$

2.
$$(g x \cdot f) y$$

3.
$$(h \cdot g) \times y$$

4.
$$(h \cdot g x) c$$

5.
$$h \cdot g \times c$$

You may type the expressions into Haskell and see whether they type check. To define f, for example, include the following in your working file:

$$f :: Int \rightarrow Char$$

 $f = undefined$

However, it is better if you can explain why the answers are as they are.