

Programming Languages: Imperative Program Construction

Practicals 6: Loop Constuction II

Shin-Cheng Mu

Autumn Term, 2021

1. Recall the maximum segment sum problem. What if we want to compute the maximum sum of *non-empty* segments?
 - (a) How would you write the specification? Does the specification still make sense with N being constrained only by $0 \leq N$?
 - (b) Derive a program solving the problem.
2. Recall the derivation of the maximum segment sum problem. Assuming that we had instead used the loop invariant $P_0 \wedge P_1 \wedge Q$, where

$$\begin{aligned} P_0 &\equiv r = \langle \uparrow p \ q : 0 \leq p \leq q \leq n : \text{sum } p \ q \rangle \ , \\ P_1 &\equiv s = \langle \uparrow p : 0 \leq p \leq n+1 : \text{sum } p \ (n+1) \rangle \ , \\ Q &\equiv 0 \leq n \leq N \ . \end{aligned}$$

Can you construct a program using the invariant above? What if the array is non-empty, that is, $1 \leq N$?

3. Derive a solution for:

```
con  $N : \text{Int}\{N \geq 0\}; a : \text{array}[0..N) \text{ of } \text{Int}$   
var  $r : \text{Int}$   
 $S$   
 $\{r = \langle \uparrow i, j : 0 \leq i < j < N : a[i] - a[j] \rangle\}$  .
```

4. Derive a solution for:

```
con  $N : \text{Int}\{N \geq 1\}; a : \text{array}[0..N) \text{ of } \text{Int}$   
var  $r : \text{Int}$   
 $S$   
 $\{r = \langle \#i, j : 0 \leq i < j < N : a[i] \times a[j] \geq 0 \rangle\}$  .
```