# Statistical Inference: Peer Assessment, Part 1

 $S \ C \ NG$ 

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# **Exponential Distribution**

### Synopsis

In this project we will investigate the exponential distribution in R and compare it with the Central Limit Theorem(CLT).

The exponential distribution can be simulated in R with rexp(n, lambda) where lambda is the rate parameter. The mean of exponential distribution is 1/lambda and the standard deviation is also 1/lambda. Set lambda = 0.2 for all of the simulations.

We will investigate the distribution of averages of 40 exponentials with thousand simulations.

## Setup

First of all, the following default settings and libraries are loaded

```
#preset default options for Rmd, codes not shown in report
require(knitr)

## Loading required package: knitr
```

```
opts_chunk$set(cache=TRUE, echo=TRUE)
#load required libraries for data analysis
require(ggplot2)
```

## Loading required package: ggplot2

#### Show the sample mean and compare it to the theoretical mean of the distribution

The following R codes are used for performing 1000 rounds of simulations. For each round, a sample size of 40 random variables under exponential distribution with rate equals lambda (0.2) are generated, and the means for each round are captured in vector exp\_sample\_means. The overall sample mean is calculated after the simulation

```
set.seed(111)
sample_size <- 40
lambda <- 0.2
exp_sample_means = NULL
for(i in 1:1000) exp_sample_means = c(exp_sample_means, mean(rexp(sample_size, rate=lambda)))
mean(exp_sample_means)</pre>
```

## [1] 5.02562

In this assignment, we assume the mean of exponential distribution is 1/lambda, where lambda = 0.2. Therefore, the theorical mean of the exponential distribution is calculated as follows:

```
exp_theo_mean <- 1/lambda
exp_theo_mean</pre>
```

## [1] 5

The sample mean is almost the same as the theorical mean of the distribution

# Show how variable the sample is (via variance) and compare it to the theoretical variance of the distribution

The variance of the sample can be calculated from below

```
var(exp_sample_means)
```

```
## [1] 0.6069798
```

According to Central Limit Theorem (CLT), The theorical variance of the distribution equals the square of theorical standard deviation divided by sample size. In this assignment, the standard deviation is also 1/lambda

```
(1/lambda)^2/sample_size
```

## [1] 0.625

The sample variance is very close to the theorical variance of the distribution

### Show that the distribution is approximately normal

For this point, we focus on the difference between the distribution of a large collection of random exponentials and the distribution of a large collection of averages of 40 exponentials. In order to illustrate this comparison, a histogram of the distribution for our 1000 simulations of 40 exponentials has been plotted, overlay with the theorical normal distribution with mean and standard deviation equals 1/lambda

```
sample_df <- as.data.frame(exp_sample_means)
g <- ggplot(sample_df, aes(x=exp_sample_means))
g <- g + geom_histogram(aes(y = ..density..))
g</pre>
```

## stat\_bin: binwidth defaulted to range/30. Use 'binwidth = x' to adjust this.

