	g 2012	Name
1/15		
2/10		
3/15		Athens Heaville
4/5		Athena User Name
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6/15		
7/15		Recitation hour
8/10		
Total/100	0	
minutes. Please write your	r name on the top of e	but do not use a computer (or cell phone!). You have 120 each page, and your user name and the hour of the recitation questions in the boxes provided.
1) Are each of th		
1) Are each of th	e following True or Fa	lse? (15 points)
		alse? (15 points) clustering is $O(n^3)$, where n is the number of data points.
1.1. Agglo	omerative hierarchical of	
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1.1. Agglo 1.2. Dynar sorting a l sorted. 1.3. pyla 1.4. Newto	omerative hierarchical of mic programming can list of integers to somet	clustering is $O(n^3)$, where n is the number of data points. be used to reduce the order of algorithmic complexity of thing below n log n, where n is the length of the list to be

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3) Consider the following code.

```
import random, pylab
def throwNeedles(f, xMin, xMax, numNeedles = 10000):
     under = 0.0
     yMax = max(1, f(xMax + 1))
     for x in range(xMin, xMax):
          if f(x) > yMax:
               yMax = f(x)
     for Needles in range(1, numNeedles + 1):
          x = random.choice(range(xMin, xMax + 1))
          if random.choice(range(0, int(round(yMax)))) < f(x):</pre>
              under += 1
     return (under/numNeedles)
def performSim(f, numTrials, numNeedles):
    res = []
    for t in range(numTrials):
        res.append(throwNeedles(f, 0, 100))
   mean = sum(res)/float(len(res))
    print mean
    print max(res) - min(res)
   pylab.hist(res)
def f(x):
    return x
performSim(f, 1000, 100)
```

3.1. With high probability, the first number printed will be approximately,

- a. 0
- b. 0.5
- c. 50
- d. 100
- e. none of the above

3.2. Which of the following values is likely to be closest to the second number printed?

- a. 0
- b. 100
- c. the first number printed
- d. half the first number printed
- e. twice the first number printed

3.3. With high probability the histogram generated will depict,

- a. a uniform distribution
- b. a normal distribution
- c. an exponential distribution
- d. none of the above

(15 points)

4) Many Course 20 students take 6.00 each term. Over the last five years, Cor 6.00 have significantly out performed the rest of the class in the fall terms and performed the rest of the class in the spring terms. The distribution of grades does not differ in the spring and fall terms. Based on these facts, Course 20 actelling students that they are likely to get a better grade if they choose to take this follow from the evidence? Why or why not? (5 points)	significantly under for the entire class dvisors have been

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6) Next to each item in the left colur	nn write the letter labeling the item in the right column that best
matches the item in the left column.	No item in the right column should be used more than once. (15
points)	

polymorphism	a) fast
random walk	b) inheritance
greedy algorithm	c) non-deterministic
hierarchical clustering	d) deterministic
training and test sets	e) unit testing
	f) bell curve
	g) supervised learning
	h) avoid over fitting

The following questions all refer to the code you were asked to study in preparation for this exam. A copy of the posted code is at the end of this quiz. Feel free to detach it.

i) linear regression

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- 7) Give the asymptotic complexity of each of the following functions in the code. Assume that for all the questions self.dimensionality = N.
- a) len(self.attrs) (2 points)
- b) Point.distance(self, other) (2 points)
- c) Cluster.singleLinkageDist(self, other)

Assume that the number of points in self.points is P1 and in other.points is P2. (3 points)

- d) Cluster.update(self, points)
 Assume that the number of points in points is P. (4 points)
- e) ClusterSet.findClosest(self, metric)

Assume that the number of members in self.members is M, metric is singleLinkageDist, and the maximum number of points in any cluster is P. (4 points)

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8) We wish to speed up hierarchical clustering by speeding up the findClosest() function.

Write a new function that finds the closest pair of clusters in self by randomly comparing R pairs of clusters and choosing the closest pair. Hint: ensure that your code does not compare a cluster to itself. (10 points)

- 9) The following questions relate to the code corresponding to kmeans ().
 - (a) Give one possible effect of removing numIters < maxIters in the while loop of kmeans(). (5 points)

(b) Rather than checking to see if the biggestChange is >= cutoff as in the current kmeans(), we checked if the averageChange is >= cutoff, would the number of iterations increase or decrease? Would the value of maxDist increase or decrease at the end of the algorithm? Explain briefly. (5 points)

```
Attached: code for study
#Code shared across examples
import pylab, random, string, copy
class Point(object):
         init (self, name, originalAttrs, normalizedAttrs = None):
        """normalizedAttrs and originalAttrs are both arrays""
        self.name = name
        self.unNormalized = originalAttrs
        if normalizedAttrs == None:
            self.attrs = originalAttrs
        else:
            self.attrs = normalizedAttrs
    def dimensionality(self):
        return len(self.attrs)
    def getAttrs(self):
        return self.attrs
    def getOriginalAttrs(self):
        return self.unNormalized
    def distance(self, other):
        #Euclidean distance metric
        result = 0.0
        for i in range(self.dimensionality()):
            result += (self.attrs[i] - other.attrs[i])**2
        return result ** 0.5
    def getName(self):
        return self.name
    def toStr(self):
        return self.name + str(self.attrs)
        __str__(self):
        return self.name
class Cluster(object):
         _init__(self, points, pointType):
        self.points = points
        self.pointType = pointType
        self.centroid = self.computeCentroid()
    def singleLinkageDist(self, other):
        minDist = self.points[0].distance(other.points[0])
        for p1 in self.points:
            for p2 in other.points:
                if p1.distance(p2) < minDist:</pre>
                    minDist = p1.distance(p2)
        return minDist
    def maxLinkageDist(self, other):
        maxDist = self.points[0].distance(other.points[0])
        for p1 in self.points:
            for p2 in other.points:
                if p1.distance(p2) > maxDist:
                    maxDist = p1.distance(p2)
        return maxDist
    def averageLinkageDist(self, other):
        totDist = 0.0
        for p1 in self.points:
            for p2 in other.points:
                totDist += p1.distance(p2)
        return totDist/(len(self.points)*len(other.points))
    def update(self, points):
        oldCentroid = self.centroid
        self.points = points
        if len(points) > 0:
            self.centroid = self.computeCentroid()
            return oldCentroid.distance(self.centroid)
        else:
            return 0.0
    def members(self):
        return self.points[:]
    def isIn(self, name):
        for p in self.points:
            if p.getName() == name:
                return True
        return False
    def toStr(self):
        result = '
        for p in self.points:
```

```
result = result + p.toStr() + ', '
        return result[:-2]
    def
        __str__(self):
        names = []
        for p in self.points:
            names.append(p.getName())
        names.sort()
        result = ''
        for p in names:
            result = result + p + ', '
        return result[:-2]
    def getCentroid(self):
        return self.centroid
    def computeCentroid(self):
        dim = self.points[0].dimensionality()
        totVals = pylab.array([0.0]*dim)
        for p in self.points:
            totVals += p.getAttrs()
        centroid = self.pointType('mean',
                                    totVals/float(len(self.points)),
                                    totVals/float(len(self.points)))
        return centroid
class ClusterSet(object):
         __init___(self, pointType):
        self.members = []
    def add(self, c):
        if c in self.members:
            raise ValueError
        self.members.append(c)
    def getClusters(self):
        return self.members[:]
    def mergeClusters(self, c1, c2):
        points = []
        for p in c1.members():
            points.append(p)
        for p in c2.members():
            points.append(p)
        newC = Cluster(points, type(p))
        self.members.remove(c1)
        self.members.remove(c2)
        self.add(newC)
        return c1, c2
    def findClosest(self, metric):
        minDistance = metric(self.members[0], self.members[1])
        toMerge = (self.members[0], self.members[1])
        for c1 in self.members:
            for c2 in self.members:
                if c1 == c2:
                    continue
                if metric(c1, c2) < minDistance:</pre>
                    minDistance = metric(c1, c2)
                    toMerge = (c1, c2)
        return toMerge
    def mergeOne(self, metric, toPrint = False):
        if len(self.members) == 1:
            return None
        if len(self.members) == 2:
            return self.mergeClusters(self.members[0],
                                       self.members[1])
        toMerge = self.findClosest(metric)
        if toPrint:
            print 'Merged'
            print ' ' + str(toMerge[0])
            print 'with'
            print ' ' + str(toMerge[1])
        self.mergeClusters(toMerge[0], toMerge[1])
        return toMerge
    def mergeN(self, metric, numClusters = 1, history = [],
               toPrint = False):
        assert numClusters >= 1
        while len(self.members) > numClusters:
            merged = self.mergeOne(metric, toPrint)
            history.append(merged)
```

```
return history
   def numClusters(self):
       return len(self.members) + 1
       __str__(self):
result = ''
       for c in self.members:
           result = result + str(c) + '\n'
       return result
#Mammal's teeth example
class Mammal(Point):
         _init__(self, name, originalAttrs, scaledAttrs = None):
       Point.__init__(self, name, originalAttrs, originalAttrs)
   def scaleFeatures(self, key):
       '1/range': [1/3.0,1/3.0,1.0,1.0,1/4.0,1/4.0,1/5.0,1/5.0]}
       scaledFeatures = []
       features = self.getOriginalAttrs()
       for i in range(len(features)):
           scaledFeatures.append(features[i]*scaleDict[key][i])
       self.attrs = scaledFeatures
def readMammalData(fName):
   dataFile = open(fName, 'r')
   teethList = []
   nameList = []
   for line in dataFile:
       if len(line) == 0 or line[0] == '#':
           continue
       dataLine = string.split(line)
       teeth = dataLine.pop(-1)
       features = []
       for t in teeth:
           features.append(float(t))
       name = ''
       for w in dataLine:
           name = name + w + ' '
       name = name[:-1]
       teethList.append(features)
       nameList.append(name)
   return nameList, teethList
def buildMammalPoints(fName, scaling):
   nameList, featureList = readMammalData(fName)
   points = []
   for i in range(len(nameList)):
       point = Mammal(nameList[i], pylab.array(featureList[i]))
       point.scaleFeatures(scaling)
       points.append(point)
   return points
#Use hierarchical clustering for mammals teeth
def test0(numClusters = 2, scaling = 'identity', printSteps = False,
         printHistory = True):
   points = buildMammalPoints('mammalTeeth.txt', scaling)
   cS = ClusterSet(Mammal)
   for p in points:
       cS.add(Cluster([p], Mammal))
   history = cS.mergeN(Cluster.maxLinkageDist, numClusters,
                       toPrint = printSteps)
   if printHistory:
       print ''
       for i in range(len(history)):
           names1 = []
           for p in history[i][0].members():
               names1.append(p.getName())
           names2 = []
           for p in history[i][1].members():
               names2.append(p.getName())
           print 'Step', i, 'Merged', names1, 'with', names2
           print ''
   clusters = cS.getClusters()
   print 'Final set of clusters:'
```

```
index = 0
    for c in clusters:
        print ' C' + str(index) + ':', c
        index += 1
def kmeans(points, k, cutoff, pointType, maxIters = 100,
           toPrint = False):
    #Get k randomly chosen initial centroids
    initialCentroids = random.sample(points, k)
    clusters = []
    #Create a singleton cluster for each centroid
    for p in initialCentroids:
        clusters.append(Cluster([p], pointType))
    numIters = 0
    biggestChange = cutoff
    while biggestChange >= cutoff and numIters < maxIters:</pre>
        #Create a list containing k empty lists
        newClusters = []
        for i in range(k):
            newClusters.append([])
        for p in points:
            #Find the centroid closest to p
            smallestDistance = p.distance(clusters[0].getCentroid())
            index = 0
            for i in range(k):
                distance = p.distance(clusters[i].getCentroid())
                if distance < smallestDistance:</pre>
                    smallestDistance = distance
                    index = i
            #Add p to the list of points for the appropriate cluster
            newClusters[index].append(p)
        #Upate each cluster and record how much the centroid has changed
        biggestChange = 0.0
        for i in range(len(clusters)):
            change = clusters[i].update(newClusters[i])
            biggestChange = max(biggestChange, change)
        numIters += 1
    #Calculate the coherence of the least coherent cluster
    maxDist = 0.0
    for c in clusters:
        for p in c.members():
            if p.distance(c.getCentroid()) > maxDist:
                maxDist = p.distance(c.getCentroid())
    print 'Number of iterations =', numIters, 'Max Diameter =', maxDist
    return clusters, maxDist
def test1(k = 2, cutoff = 0.0001, numTrials = 1, printSteps = False,
          printHistory = False):
    points = buildMammalPoints('mammalTeeth.txt', '1/max')
    if printSteps:
        print 'Points:'
        for p in points:
            attrs = p.getOriginalAttrs()
            for i in range(len(attrs)):
                attrs[i] = round(attrs[i], 2)
            print '
                     ', p, attrs
    numClusterings = 0
    bestDiameter = None
   while numClusterings < numTrials:</pre>
        clusters, maxDiameter = kmeans(points, k, cutoff, Mammal)
        if bestDiameter == None or maxDiameter < bestDiameter:</pre>
            bestDiameter = maxDiameter
            bestClustering = copy.deepcopy(clusters) #Note deepcopy
        if printHistory:
            print 'Clusters:'
            for i in range(len(clusters)):
                print ' C' + str(i) + ':', clusters[i]
        numClusterings += 1
    print '\nBest Clustering'
    for i in range(len(bestClustering)):
        print ' C' + str(i) + ':', bestClustering[i]
```