with(linalg):

A := matrix(3, 3, [1, -2, 2, -2, 1, 2, 2, 2, 1]);

$$A := \begin{bmatrix} 1 & -2 & 2 \\ -2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix} \tag{1}$$

eigenvectors(A);

$$[-3, 1, \{[-1 \ -1 \ 1]\}], [3, 2, \{[-1 \ 1 \ 0], [1 \ 0 \ 1]\}]$$
 (2)

charpoly(A, λ);

$$\lambda^3 - 3\lambda^2 - 9\lambda + 27 \tag{3}$$

solve for lambda

$$[[\lambda = -3], [\lambda = 3], [\lambda = 3]]$$
(4)