

5. ~~A~~ Kinematics challenge:

A stone is dropped from $\approx 45\text{m}$ high cliff. At the same ~~time~~ instant, a second stone is thrown upward from the base of the cliff with a speed of 15m/s .

a) At what height above the ground do the stones pass each other?

$$a = -9.8 \text{ m/s}^2$$

$$h(\text{of cliff}) = 45\text{m}$$

Stone A (falling)

$$-v_{A_0} = 0\text{m/s} \text{ (initial velocity)} \rightarrow y_A(t) = 45 - \frac{1}{2}gt^2$$

$$-y_{A_0} = 45\text{m} \text{ (initial height)} \quad = 45 - 4.9t^2$$

Stone B (rising)

$$-v_{B_0} = 15\text{m/s} \uparrow \text{ (initial velocity)}$$

$$-y_{B_0} = 0\text{m} \text{ (initial height)} \rightarrow y_B(t) = v_{B_0}t + \frac{1}{2}gt^2$$

$$\rightarrow y_B = 15(3) - 4.9(3)^2 = 45 - 44.1 = \boxed{0.9\text{m}} \quad = 15t - 44.1t^2$$

b) How much time after release does this occur?

$$y_A(t) = y_B(t)$$

$$45 - 4.9t^2 = 15t - 4.9t^2$$

$$\frac{45}{35} = \frac{15t}{15} \rightarrow \boxed{t = 3\text{s}}$$

4. Relative velocity:

A river flows east at 2 m/s. A boat heads North at 4 m/s relative to the water.

a) what is the boat's speed relative to the ground?

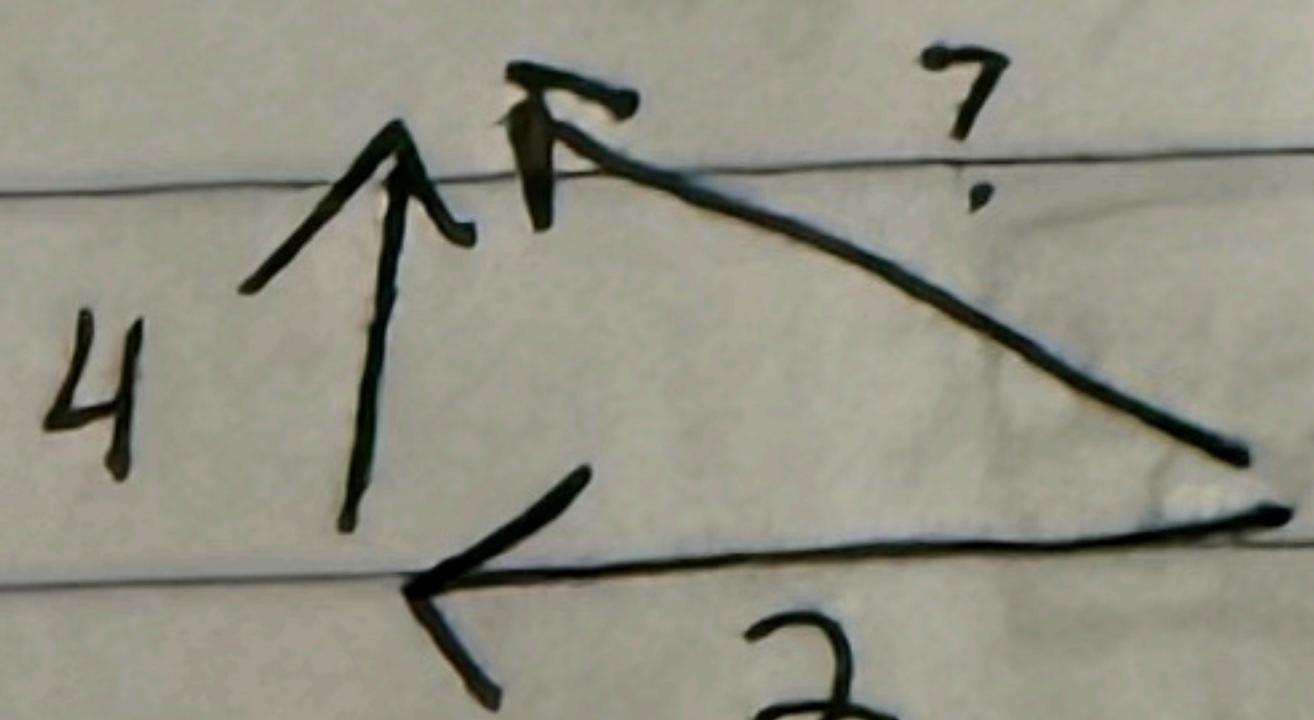
$$V_r = 2 \text{ m/s} \text{ (River that flows east)}$$

$$V_b = 4 \text{ m/s} \text{ (boat that moves North)}$$

$$V = \sqrt{V_r^2 + V_b^2} = \sqrt{(2)^2 + (4)^2} = \sqrt{4 + 16} = \sqrt{20}$$

$$\boxed{V = 4.47 \text{ m/s}}$$

b) At what angle (relative to North) does it move as seen from the shore?



$$\tan \theta = \frac{\text{opp.}}{\text{adj.}} = \tan \theta = \frac{4}{2}$$

$$\theta = \tan^{-1}\left(\frac{4}{2}\right)$$

$$\theta = \tan^{-1}\left(\frac{1}{2}\right)$$

$$\boxed{\theta = 26.6^\circ}$$

3. Projectile (2D):

A soccer ball is kicked from ground level at 18 m/s at a 30° angle above the horizontal.

a) How long is the ball in the air?

$$V_0 = 18 \text{ m/s}$$

$$\theta = 30^\circ$$

$$g = 9.8 \text{ m/s}^2$$

$$V_{0x} = V_0 \cos(\theta) = 18 \cos(30^\circ) = 18 \times 0.866 = 15.59 \text{ m/s}$$

$$V_{0y} = V_0 \sin(\theta) = 18 \sin(30^\circ) = 18 \times 0.5 = 9.00 \text{ m/s}$$

$$t = \frac{2V_{0y}}{g} = \frac{2(9)}{9.8} = \frac{18}{9.8} = \boxed{1.84 \text{ s}}$$

b) How far does it travel horizontally before hitting the ground?

$$x = V_{0x} \cdot t = 15.59 \times 1.84 = \boxed{28.7 \text{ m}}$$

2. Free Fall:

A ball is thrown straight upward with an initial speed of 12 m/s.

a) How long does it take to reach its highest point?

$$V_0 = 12 \text{ m/s} \uparrow$$

$$a = -9.8 \text{ m/s}^2$$

V = 0 m/s - stops at top

$$V = V_0 + at$$

$$0 = 12 + (-9.8)t$$

$$\frac{-12}{-9.8} = \frac{-9.8t}{9.8}$$

$$1.22 = t$$

$$t = 1.22 \text{ s}$$

b) What is the maximum height it reaches?

$$x = V_0 t + \frac{1}{2} a t^2$$

$$x = (12)(1.22) + \frac{1}{2}(-9.8)(1.22)^2$$

$$x = 14.64 - 7.29$$

$$x = 7.35 \text{ m}$$

1. Constant acceleration (1D):

A car starts from rest and accelerates uniformly at 2.5 m/s^2 for 8 seconds.

a) what is it's final velocity?

v_0 (initial) = 0 - Starts from rest

$$a = 2.5 \text{ m/s}^2$$

$$t = 8 \text{ sec.}$$

$$v = v_0 + at$$

$$v = 0 + (2.5)(8)$$

$$\boxed{v = 20 \text{ m/s}}$$

b) How far does it travel in this time?

$$x = v_0 t + \frac{1}{2} a t^2$$

$$x = 0 + \frac{1}{2}(2.5)(8)^2$$

$$x = (1.25)(64)$$

$$\boxed{x = 80 \text{ m}}$$