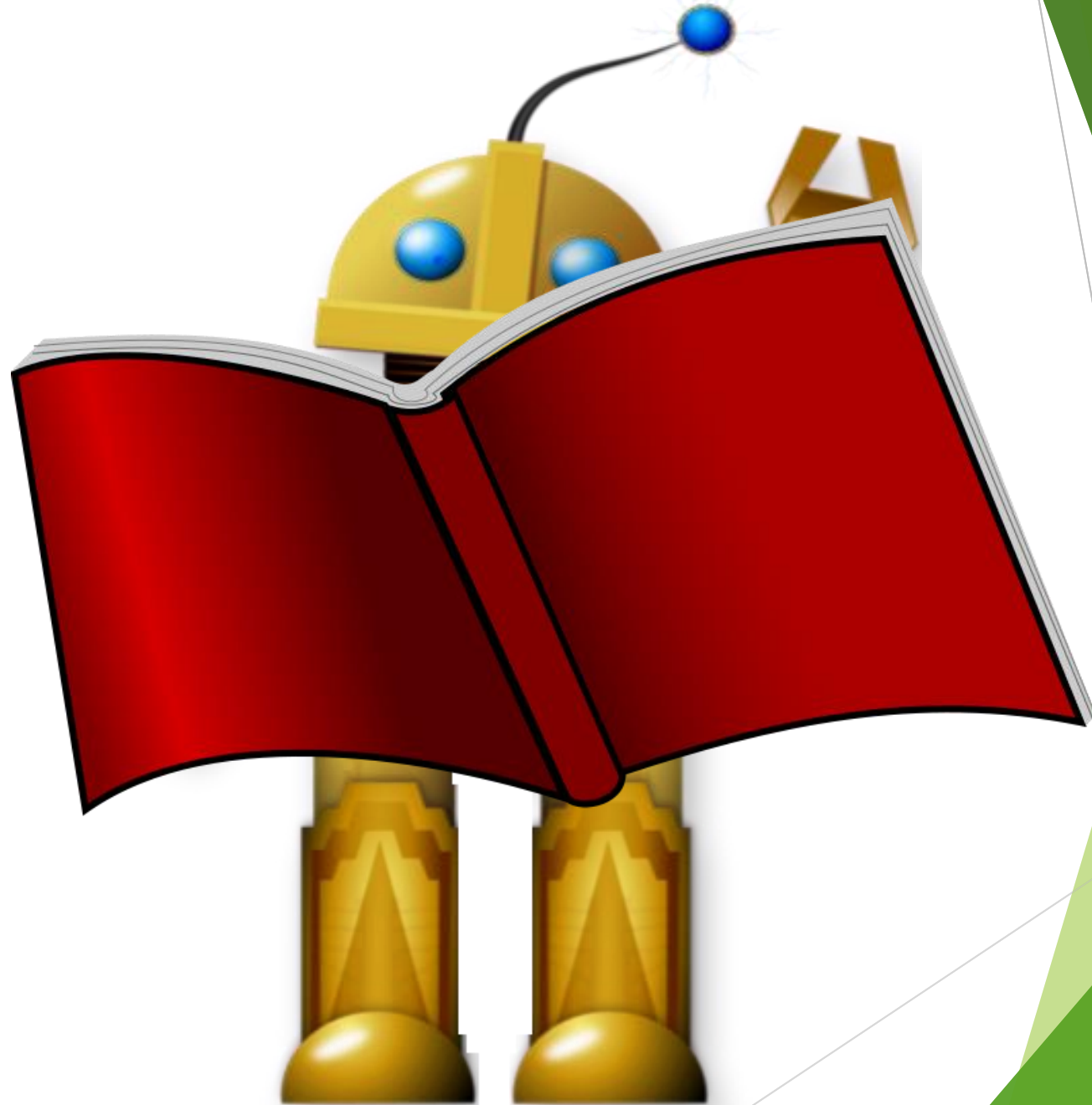


# Review



# Final Exam Logistics

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Wednesday, May 18 at 12:15PM

- 2 hours
- In the classroom
- 1 handwritten cheat sheet (front and back) with your name
- 30% of grade

# Final Exam – 30 points total

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5 points

- Search (Informed and Uninformed), heuristics, Hill Climbing
- Constraint Satisfaction Problems
- Adversarial Search

# Final Exam – 30 points total

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25 points

- First-Order Logic, Conversion to CNF, Resolution
- Default Reasoning: given a KB and default rules, what can we conclude?
- Planning: The Frame Problem, PDDL
- Uncertainty: Joint and Conditional Probabilities, Independence, Bayes' rule, Bayes nets
- Machine Learning:
  - Naïve Bayes Classification, Laplace Smoothing
  - Perceptron, Neural Nets
  - Nearest Neighbor
  - Clustering: K-means
  - Decision Trees

# Review: First Order Logic

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$\forall x \text{ CSMajor}(x) \wedge \text{Took}(x, \text{CS146}) \Rightarrow \exists y \text{ Faculty}(y) \wedge \text{Advisor}(y, x)$

What does this mean in English?

What's the scope of the universal quantifier  $\forall x$ ?

$\forall x \text{ (CSMajor}(x) \wedge \text{Took}(x, \text{CS146}) \Rightarrow \exists y \text{ Faculty}(y) \wedge \text{Advisor}(y, x))$

What's the scope of the existential quantifier  $\exists y$ ?

$\forall x \text{ (CSMajor}(x) \wedge \text{Took}(x, \text{CS146}) \Rightarrow \exists y \text{ (Faculty}(y) \wedge \text{Advisor}(y, x)))$

What implies what?

$\forall x \text{ ((CSMajor}(x) \wedge \text{Took}(x, \text{CS146})) \Rightarrow (\exists y \text{ (Faculty}(y) \wedge \text{Advisor}(y, x))))$

# Review: CNF

---

$$\forall x ((\text{CSMajor}(x) \wedge \text{Took}(x, \text{CS146})) \Rightarrow (\exists y (\text{Faculty}(y) \wedge \text{Advisor}(y, x))))$$

Step 1: Replace  $\alpha \Rightarrow \beta$  with  $\neg\alpha \vee \beta$

$$\forall x (\neg(\text{CSMajor}(x) \wedge \text{Took}(x, \text{CS146})) \vee (\exists y (\text{Faculty}(y) \wedge \text{Advisor}(y, x))))$$

Step 2: Move  $\neg$  inwards: replace  $\neg(P \wedge Q)$  with  $\neg P \vee \neg Q$

$$\forall x ((\neg\text{CSMajor}(x) \vee \neg\text{Took}(x, \text{CS146})) \vee (\exists y (\text{Faculty}(y) \wedge \text{Advisor}(y, x))))$$

Step 3: Standardize variables. Nothing to change.

# Review: CNF

$\forall x ((\neg \text{CSMajor}(x) \vee \neg \text{Took}(x, \text{CS146})) \vee (\exists y (\text{Faculty}(y) \wedge \text{Advisor}(y, x))))$

Step 4: Skolemize. Each **existential variable** is replaced by a Skolem function of the **enclosing universally quantified variable**.

$\forall x ((\neg \text{CSMajor}(x) \vee \neg \text{Took}(x, \text{CS146})) \vee (\exists y (\text{Faculty}(y) \wedge \text{Advisor}(y, x))))$

$\forall x ((\neg \text{CSMajor}(x) \vee \neg \text{Took}(x, \text{CS146})) \vee ((\text{Faculty}(F(x)) \wedge \text{Advisor}(F(x), x))))$

Step 5: Drop universal quantifiers.

$((\neg \text{CSMajor}(x) \vee \neg \text{Took}(x, \text{CS146})) \vee ((\text{Faculty}(F(x)) \wedge \text{Advisor}(F(x), x))))$

Is this CNF?

# Review: CNF

$(\neg \text{CSMajor}(x) \vee \neg \text{Took}(x, \text{CS146})) \vee (\text{Faculty}(F(x)) \wedge \text{Advisor}(F(x), x))$

Step 6: Distribute  $\vee$  over  $\wedge$ .  $A \vee (B \wedge C)$  is  $(A \vee B) \wedge (A \vee C)$

$(\neg \text{CSMajor}(x) \vee \neg \text{Took}(x, \text{CS146})) \vee (\text{Faculty}(F(x)) \wedge \text{Advisor}(F(x), x))$

$((\neg \text{CSMajor}(x) \vee \neg \text{Took}(x, \text{CS146})) \vee (\text{Faculty}(F(x)) \wedge (\neg \text{CSMajor}(x) \vee \neg \text{Took}(x, \text{CS146}))) \vee \text{Advisor}(F(x), x))$

$(\neg \text{CSMajor}(x) \vee \neg \text{Took}(x, \text{CS146}) \vee \text{Faculty}(F(x)) \wedge \neg \text{CSMajor}(x) \vee \neg \text{Took}(x, \text{CS146}) \vee \text{Advisor}(F(x), x))$



# Machine Learning in Hollywood

















---

Our goal is to predict whether a script/book will lead to a blockbuster movie.

















Our training data set contains:

- 8 scripts/books – we know which ones turned out to be blockbuster movies (commercial success).
- 2 reviewers reading the scripts.

# Naïve Bayes

Movie	Anna	Ryan	Blockbuster?
Inside Out	T 	T 	T \$\$\$\$\$
Zootopia	T 	F 	T \$\$\$\$\$
San Andreas	F 	T 	T \$\$\$\$\$
The Pets Take Over	F 	T 	F ¢
Fieldtrip to Mars	F 	F 	F ¢
Forever	F 	F 	F ¢
Still Here	F 	T 	F ¢
A Happy Robot	F 	T 	F ¢

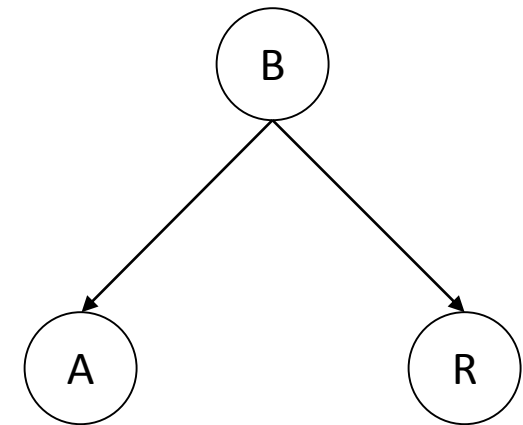
# Naïve Bayes

Movie	Anna	Ryan	Blockbuster?
Inside Out	T 	T 	T \$\$\$\$\$
Zootopia	T 	F 	T \$\$\$\$\$
San Andreas	F 	T 	T \$\$\$\$\$
The Pets Take Over	F 	T 	F ¢
Fieldtrip to Mars	F 	F 	F ¢
Forever	F 	F 	F ¢
Still Here	F 	T 	F ¢
A Happy Robot	F 	T 	F ¢

A: Anna likes the script

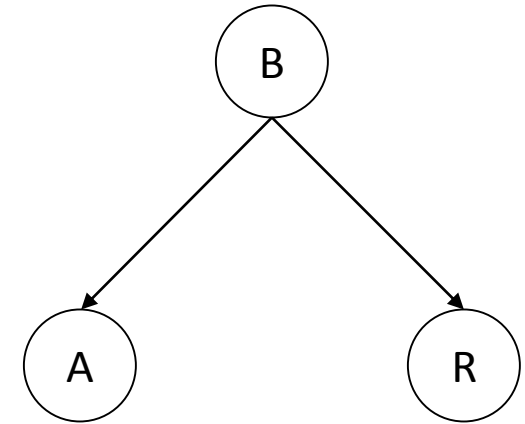
R: Ryan likes the script

B: the movie is a  
blockbuster



# Naïve Bayes - Learning

Movie	Anna	Ryan	Blockbuster?
Inside Out	T 👍	T 👍	T \$\$\$\$\$
Zootopia	T 👍	F 👎	T \$\$\$\$\$
San Andreas	F 👎	T 👍	T \$\$\$\$\$
The Pets Take Over	F 👎	T 👍	F ¢
Fieldtrip to Mars	F 👎	F 👎	F ¢
Forever	F 👎	F 👎	F ¢
Still Here	F 👎	T 👍	F ¢
A Happy Robot	F 👎	T 👍	F ¢



We need to learn:

$$P(+a | +b) = 2/3$$

$$P(+r | +b) = 2/3$$

$$P(+a | -b) = 0$$

$$P(+r | -b) = 3/5$$

$$P(+b) = 3/8$$

# Naïve Bayes - Classification

$$P(+b) = 3/8$$

$$P(+a|+b) = 2/3$$

$$P(+r|+b) = 2/3$$

$$P(+a|-b) = 0$$

$$P(+r|-b) = 3/5$$

We have a new book that Anna likes and Ryan does not like. Should we make a movie?

$$P(+b|+a, -r)?$$

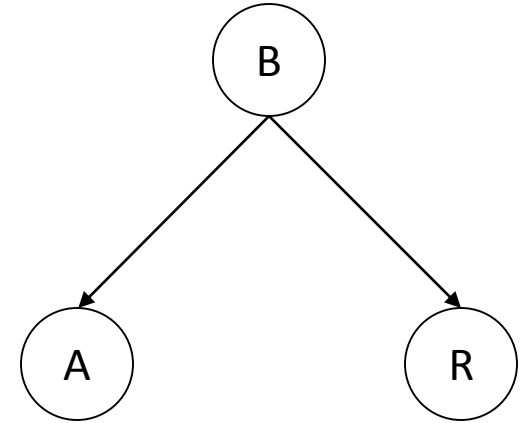
$$P(+b|+a, -r) = \frac{P(+b, +a, -r)}{P(+a, -r)} = \frac{P(+b, +a, -r)}{P(+b, +a, -r) + P(-b, +a, -r)}$$

$$P(+b, +a, -r) = P(+b).P(+a|+b).P(-r|+b) = \dots$$

















$$P(-b, +a, -r) = P(-b).P(+a|-b).P(-r|-b) = 0$$

$$P(+b|+a, -r) = 1 \quad \text{and} \quad P(-b|+a, -r) = 0$$

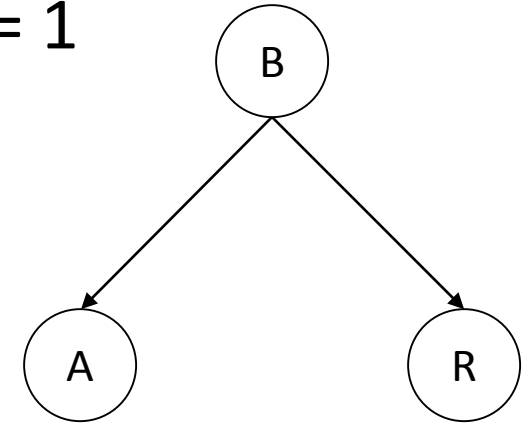
What is the problem here?



# Naïve Bayes with Laplace Smoothing

Movie	Anna	Ryan	Blockbuster?
Inside Out	T 	T 	T \$\$\$\$\$
Zootopia	T 	F 	T \$\$\$\$\$
San Andreas	F 	T 	T \$\$\$\$\$
The Pets Take Over	F 	T 	F ¢
Fieldtrip to Mars	F 	F 	F ¢
Forever	F 	F 	F ¢
Still Here	F 	T 	F ¢
A Happy Robot	F 	T 	F ¢

k = 1



$$P_L(+b) = \frac{3+1}{8+2} = \frac{4}{10}$$

$$P_L(+a|+b) = \frac{2+1}{3+2} = \frac{3}{5}$$

$$P_L(+a|-b) = \frac{0+1}{5+2} = \frac{1}{7}$$

$$P_L(+r|+b) = \frac{2+1}{3+2} = \frac{3}{5}$$

$$P_L(+r|-b) = \frac{3+1}{5+2} = \frac{4}{7}$$

# Naïve Bayes Laplace Smoothing

$$P_L(+b) = \frac{2}{5}$$

$$P_L(+a|+b) = \frac{3}{5}$$

$$P_L(+r|+b) = \frac{3}{5}$$

$$P_L(+a|-b) = \frac{1}{7}$$

$$P_L(+r|-b) = \frac{4}{7}$$

We have a new book that Anna likes and Ryan does not like. Should we make a movie?

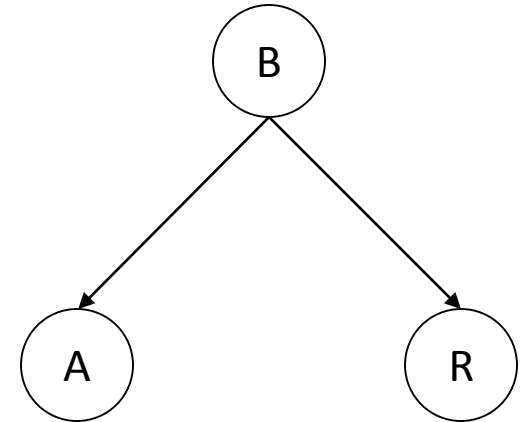
$P(+b|+a, -r)$ ?

$$P(+b|+a, -r) = \frac{P(+b, +a, -r)}{P(+a, -r)} = \frac{P(+b, +a, -r)}{P(+b, +a, -r) + P(-b, +a, -r)}$$

$$P(+b, +a, -r) = P(+b).P(+a|+b).P(-r|+b) = \frac{2}{5} \cdot \frac{3}{5} \cdot \frac{2}{5} = \frac{12}{125}$$

$$P(-b, +a, -r) = P(-b).P(+a|-b).P(-r|-b) = \frac{3}{5} \cdot \frac{1}{7} \cdot \frac{3}{7} = \frac{9}{245}$$

$$P(+b|+a, -r) = 0.72$$



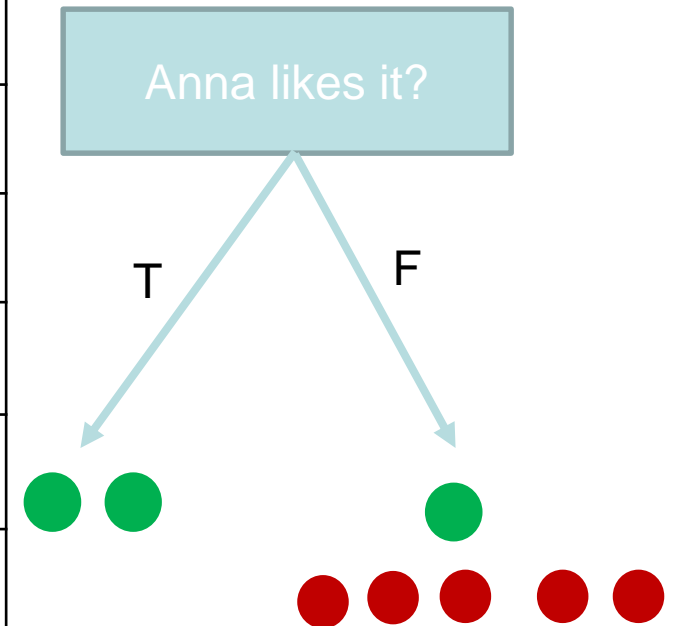
# Decision Tree

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	T	T	T	T
Zootopia	T	F	F	T
San Andreas	F	T	T	T
The Pets Take Over	F	T	F	F
Fieldtrip to Mars	F	F	T	F
Forever	F	F	F	F
Still Here	F	T	F	F
A Happy Robot	F	T	F	F



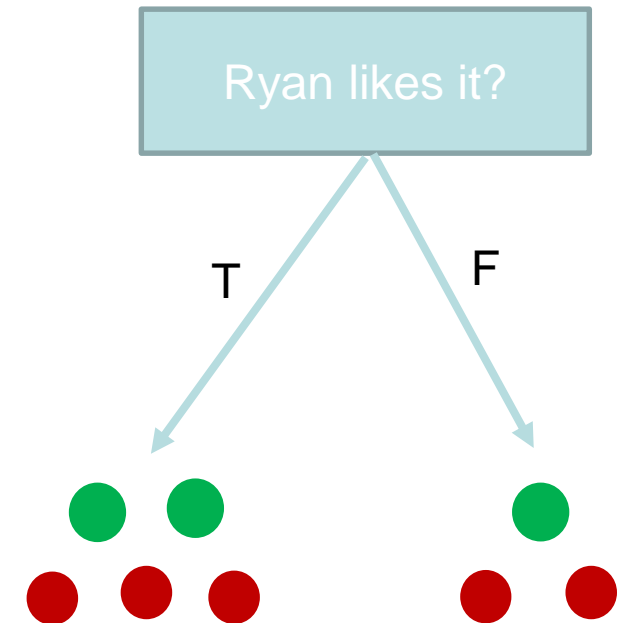
# Learning the Decision Tree

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	T	T	T	T
Zootopia	T	F	F	T
San Andreas	F	T	T	T
The Pets Take Over	F	T	F	F
Fieldtrip to Mars	F	F	T	F
Forever	F	F	F	F
Still Here	F	T	F	F
A Happy Robot	F	T	F	F



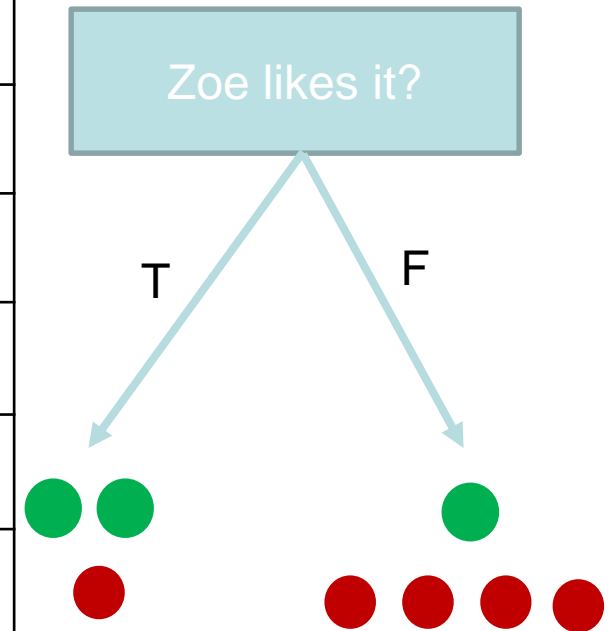
# Learning the Decision Tree

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	T	T	T	T
Zootopia	T	F	F	T
San Andreas	F	T	T	T
The Pets Take Over	F	T	F	F
Fieldtrip to Mars	F	F	T	F
Forever	F	F	F	F
Still Here	F	T	F	F
A Happy Robot	F	T	F	F

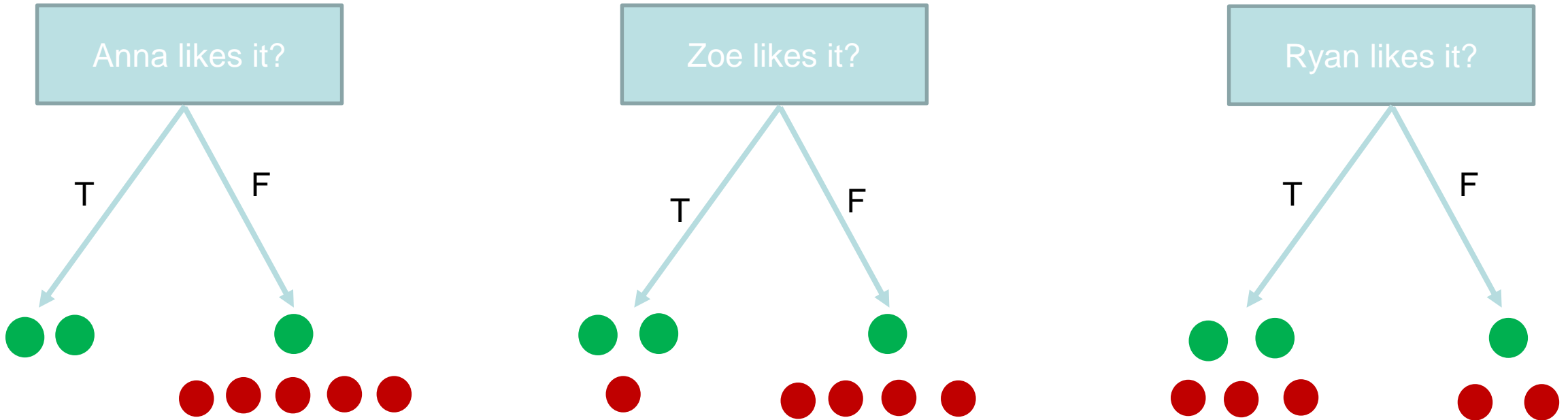


# Learning the Decision Tree

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	T	T	T	T
Zootopia	T	F	F	T
San Andreas	F	T	T	T
The Pets Take Over	F	T	F	F
Fieldtrip to Mars	F	F	T	F
Forever	F	F	F	F
Still Here	F	T	F	F
A Happy Robot	F	T	F	F

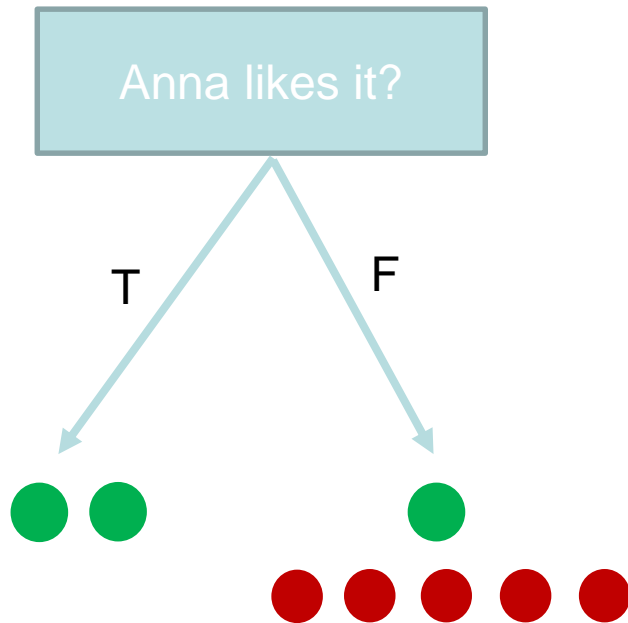


# Learning the Decision Tree



Which one is the most significant feature that will give us the best split at the root of the tree?

# Learning the Decision Tree



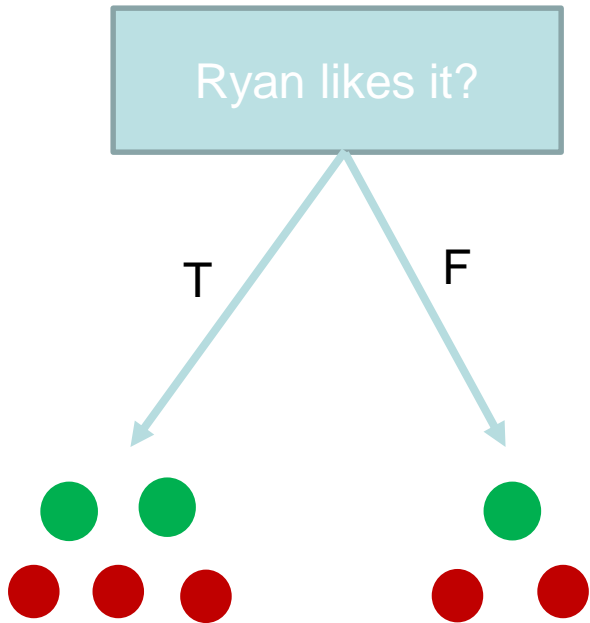
Expected entropy per example over all branches is:

$$\sum_i \frac{p_i + n_i}{p + n} H\left(\left\langle \frac{p_i}{p_i + n_i}, \frac{n_i}{p_i + n_i} \right\rangle\right)$$

$$= 0 + 6/8 H\left(\left\langle 1/6, 5/6 \right\rangle\right)$$

$$= 6/8 (-1/6 \log_2 1/6 - 5/6 \log_2 5/6)$$

# Learning the Decision Tree

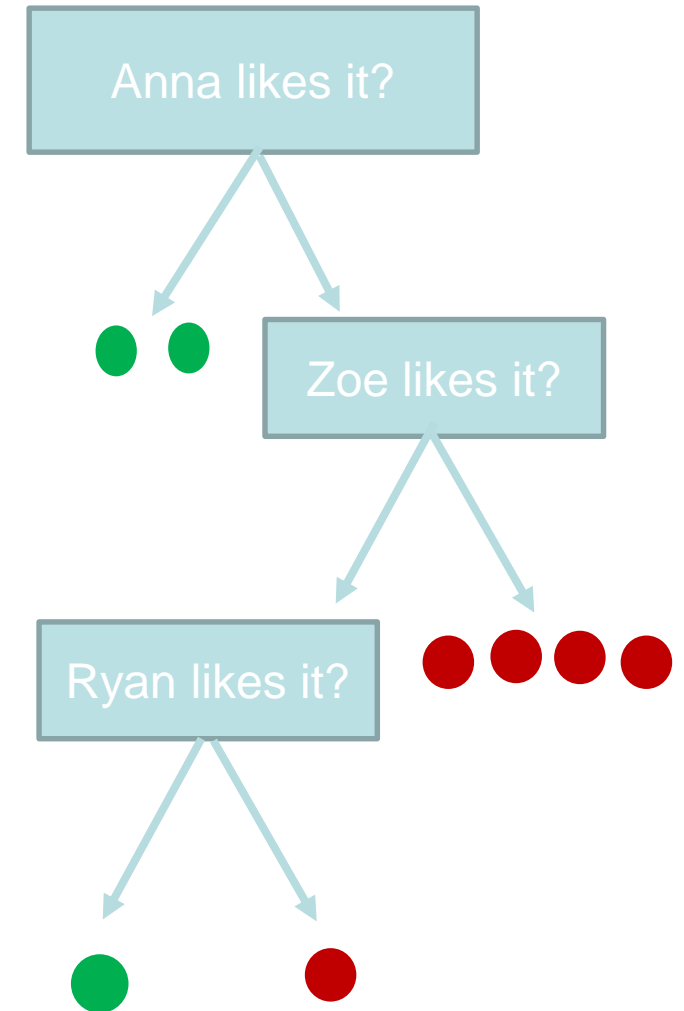


Expected entropy per example over all branches is:

$$\sum_i \frac{p_i + n_i}{p + n} H\left(\left\langle \frac{p_i}{p_i + n_i}, \frac{n_i}{p_i + n_i} \right\rangle\right)$$
$$= 5/8 H(\langle 2/5, 3/5 \rangle) + 3/8 H(\langle 1/3, 2/3 \rangle)$$

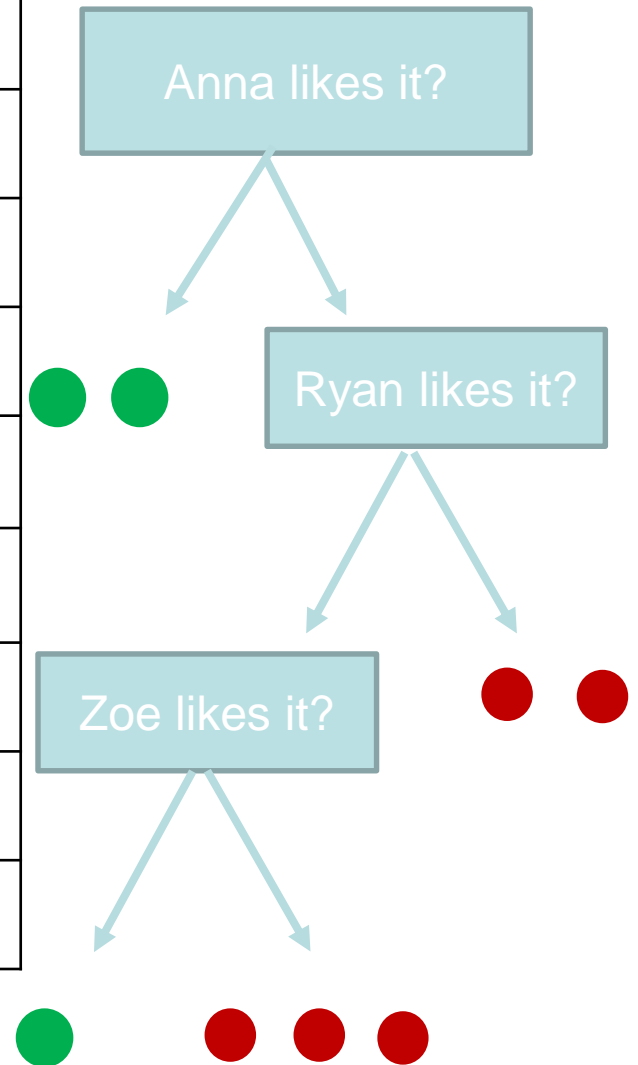
# Learning the Decision Tree

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	T	T	T	T
Zootopia	T	F	F	T
San Andreas	F	T	T	T
The Pets Take Over	F	T	F	F
Fieldtrip to Mars	F	F	T	F
Forever	F	F	F	F
Still Here	F	T	F	F
A Happy Robot	F	T	F	F



# Alternate Decision Tree?

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	T	T	T	T
Zootopia	T	F	F	T
San Andreas	F	T	T	T
The Pets Take Over	F	T	F	F
Fieldtrip to Mars	F	F	T	F
Forever	F	F	F	F
Still Here	F	T	F	F
A Happy Robot	F	T	F	F



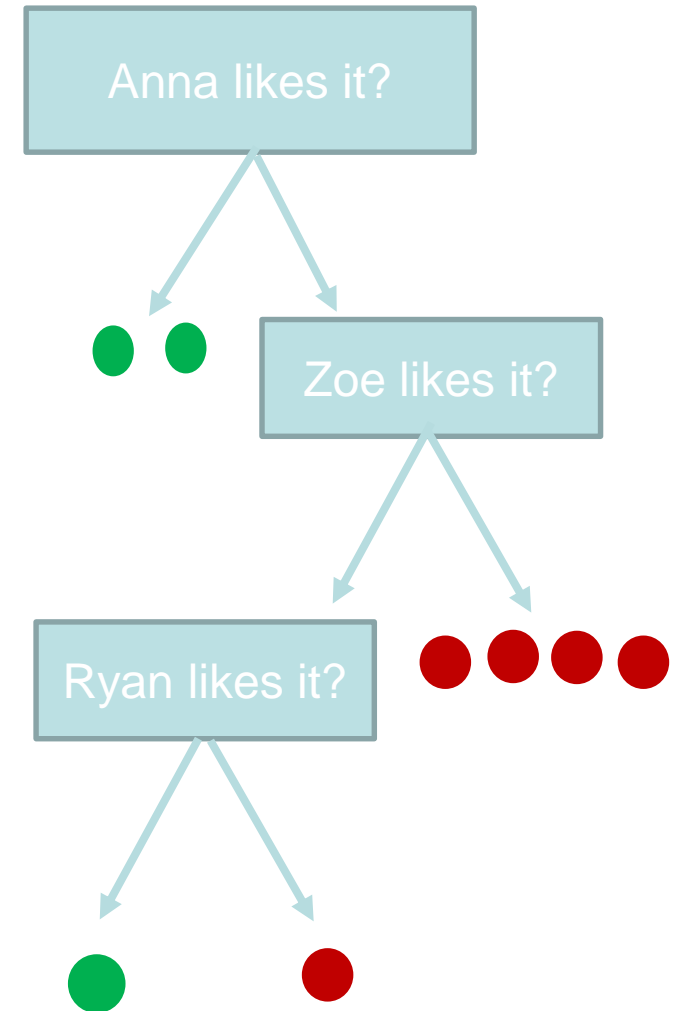


# Classifying with the Decision Tree

We have a new book that Anna likes but Ryan and Zoe do not like. Should we make a movie?

What about a book that neither Anna nor Zoe like?

A book that Anna does not like but Zoe and Ryan like?



# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

Inside Out =

BIAS	:	1
Anna	:	5
Ryan	:	5
Zoe	:	5

$w$

BIAS	:	1
Anna	:	0
Ryan	:	0
Zoe	:	0

$f(x) \cdot w = 1 \geq 0$ , no weight updates

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

Zootopia =

BIAS	:	1
Anna	:	4
Ryan	:	2
Zoe	:	1

$w$

BIAS	:	1
Anna	:	0
Ryan	:	0
Zoe	:	0

$f(x) \cdot w = 1 \geq 0$ , no weight updates

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

San Andreas =

BIAS	:	1
Anna	:	1
Ryan	:	4
Zoe	:	3

$w$

BIAS	:	1
Anna	:	0
Ryan	:	0
Zoe	:	0

$f(x) \cdot w = 1 \geq 0$ , no weight updates

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

The Pets...=

BIAS	:	1
Anna	:	1
Ryan	:	5
Zoe	:	2

$w$

BIAS	:	1
Anna	:	0
Ryan	:	0
Zoe	:	0

$f(x) \cdot w = 1 \geq 0$  should be negative

Update  $w$  (subtract  $f(x)$ )

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

The Pets...=

BIAS	:	1
Anna	:	1
Ryan	:	5
Zoe	:	2

$w$

BIAS	:	0
Anna	:	-1
Ryan	:	-5
Zoe	:	-2

$f(x) \cdot w = 1 \geq 0$  should be negative

Update  $w$  (subtract  $f(x)$ )

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

Fieldtrip...=

BIAS	:	1
Anna	:	1
Ryan	:	2
Zoe	:	4

$w$

BIAS	:	0
Anna	:	-1
Ryan	:	-5
Zoe	:	-2

$f(x) \cdot w = -1 -10 -8 < 0$  weight update



# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

Forever =

BIAS	:	1
Anna	:	2
Ryan	:	1
Zoe	:	2

$w$

BIAS	:	0
Anna	:	-1
Ryan	:	-5
Zoe	:	-2

$f(x) \cdot w < 0$  no weight update

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

Still Here =

BIAS	:	1
Anna	:	1
Ryan	:	3
Zoe	:	2

$w$

BIAS	:	0
Anna	:	-1
Ryan	:	-5
Zoe	:	-2

$f(x) \cdot w < 0$  no weight update

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

Happy Robot=

BIAS	:	1
Anna	:	2
Ryan	:	4
Zoe	:	1

$w$

BIAS	:	0
Anna	:	-1
Ryan	:	-5
Zoe	:	-2

$f(x) \cdot w < 0$  no weight update

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

Inside Out =

BIAS	:	1
Anna	:	5
Ryan	:	5
Zoe	:	5

$w$

BIAS	:	0
Anna	:	-1
Ryan	:	-5
Zoe	:	-2

Second Iteration

$f(x) \cdot w = -5 -25 -10 < 0$  should be positive  
 update weights (add  $f(x)$ )

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

Inside Out =

BIAS	:	1
Anna	:	5
Ryan	:	5
Zoe	:	5

$w$

BIAS	:	1
Anna	:	4
Ryan	:	0
Zoe	:	3

Second Iteration

$f(x) \cdot w = -5 -25 -10 < 0$  should be positive  
 update weights (add  $f(x)$ )

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

Zootopia =

BIAS	:	1
Anna	:	4
Ryan	:	2
Zoe	:	1

$w$

BIAS	:	1
Anna	:	4
Ryan	:	0
Zoe	:	3

Second Iteration

$f(x) \cdot w = 1 + 16 + 3$  no change

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

San Andreas =

BIAS	:	1
Anna	:	1
Ryan	:	4
Zoe	:	3

$w$

BIAS	:	1
Anna	:	4
Ryan	:	0
Zoe	:	3

Second Iteration

$f(x) \cdot w = 1 + 4 + 9$  no change

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

The Pets...=

BIAS	:	1
Anna	:	1
Ryan	:	5
Zoe	:	2

$w$

BIAS	:	1
Anna	:	4
Ryan	:	0
Zoe	:	3

Second Iteration

$f(x) \cdot w = 1 + 4 + 6 > 0$  should be negative  
 update weights (subtract  $f(x)$ )



# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

The Pets...=

BIAS	:	1
Anna	:	1
Ryan	:	5
Zoe	:	2

$w$

BIAS	:	0
Anna	:	3
Ryan	:	-5
Zoe	:	1

Second Iteration

$f(x) \cdot w = 1 + 4 + 6 > 0$  should be negative  
 update weights (subtract  $f(x)$ )

# Perceptron

Movie	Anna	Ryan	Zoe	Blockbuster?
Inside Out	5	5	5	T
Zootopia	4	2	1	T
San Andreas	1	4	3	T
The Pets Take Over	1	5	2	F
Fieldtrip to Mars	1	2	4	F
Forever	2	1	2	F
Still Here	1	3	2	F
A Happy Robot	2	4	1	F

Fieldtrip...=

BIAS	:	1
Anna	:	1
Ryan	:	2
Zoe	:	4

$w$

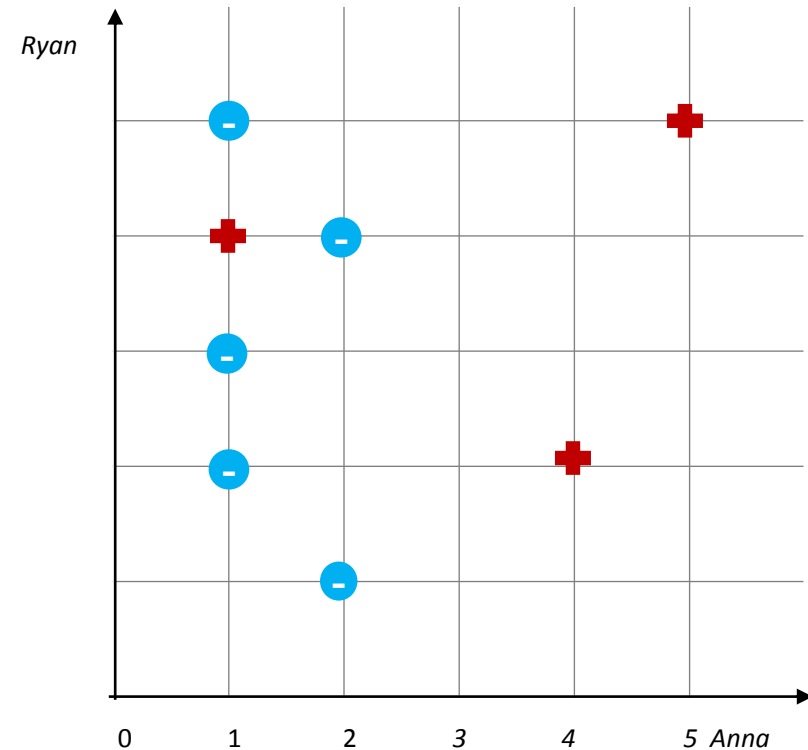
BIAS	:	0
Anna	:	3
Ryan	:	-5
Zoe	:	1

Second Iteration

$f(x) \cdot w = 3 - 10 + 4$  no change ...

# Nearest Neighbor

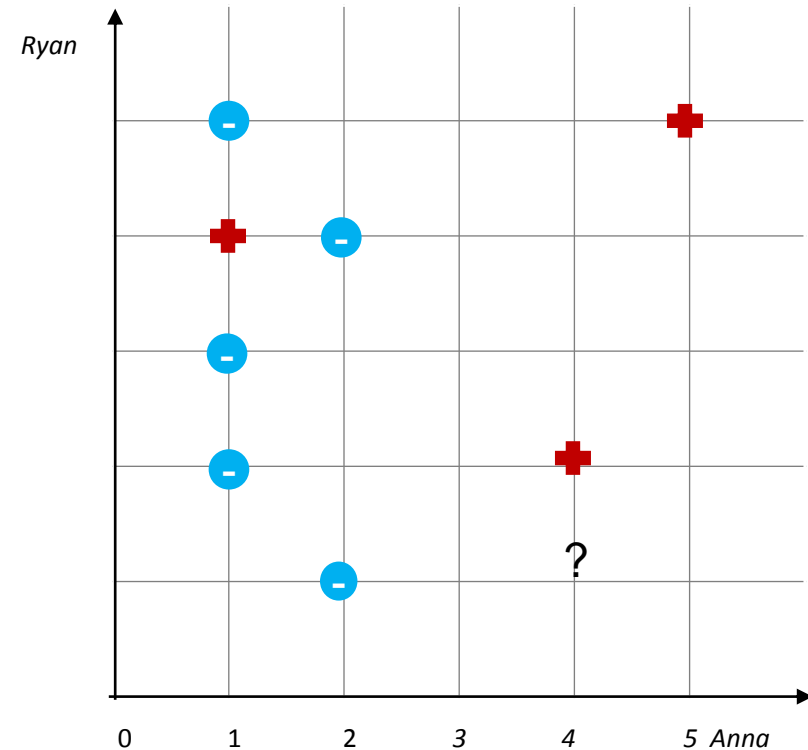
Movie	Anna	Ryan	Blockbuster?
Inside Out	5	5	T
Zootopia	4	2	T
San Andreas	1	4	T
The Pets Take Over	1	5	F
Fieldtrip to Mars	1	2	F
Forever	2	1	F
Still Here	1	3	F
A Happy Robot	2	4	F



We have a new book that Anna likes (+4) and Ryan does not like (+1). Should we make a movie? 1-NN? 3-NN?

# Nearest Neighbor

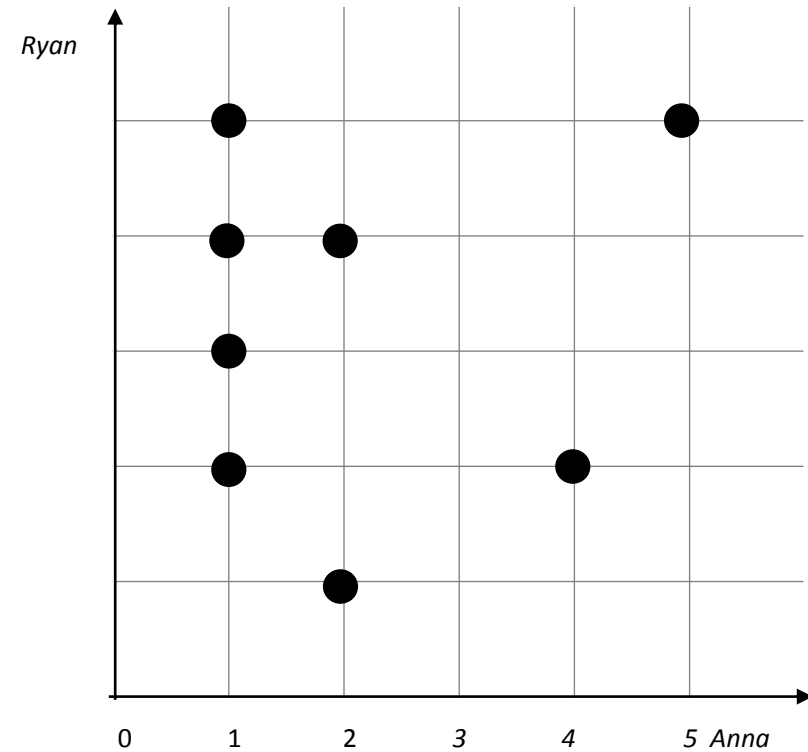
Movie	Anna	Ryan	Blockbuster?
Inside Out	5	5	T
Zootopia	4	2	T
San Andreas	1	4	T
The Pets Take Over	1	5	F
Fieldtrip to Mars	1	2	F
Forever	2	1	F
Still Here	1	3	F
A Happy Robot	2	4	F



We have a new book that Anna likes (+4) and Ryan does not like (+1).  
Should we make a movie? 1-NN? **Yes** 3-NN? **No**

# Clustering

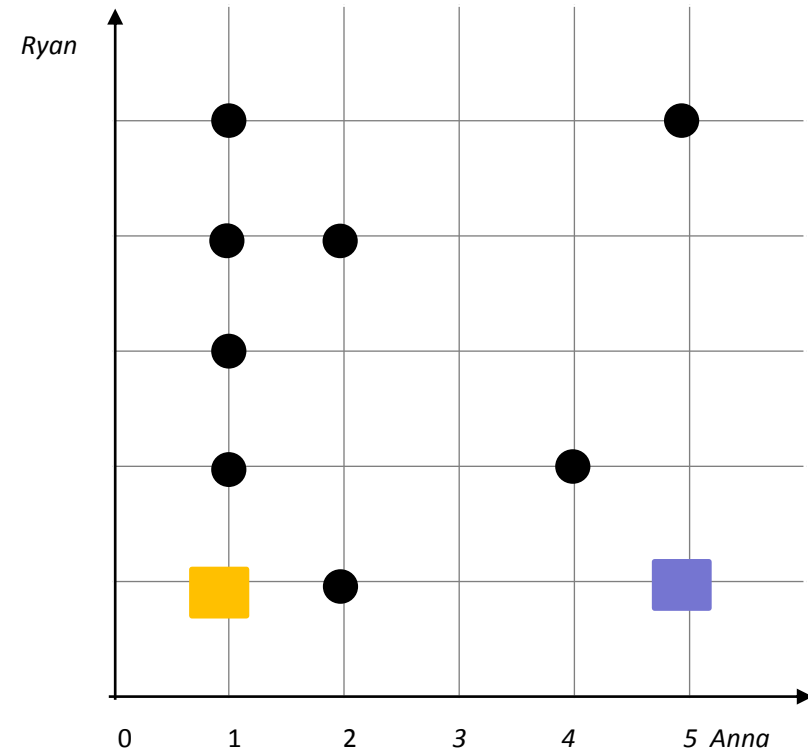
Movie	Anna	Ryan
Inside Out	5	5
Zootopia	4	2
San Andreas	1	4
The Pets Take Over	1	5
Fieldtrip to Mars	1	2
Forever	2	1
Still Here	1	3
A Happy Robot	2	4



Clustering: unsupervised learning – no labels  
K-means  $k = 2$

# Clustering

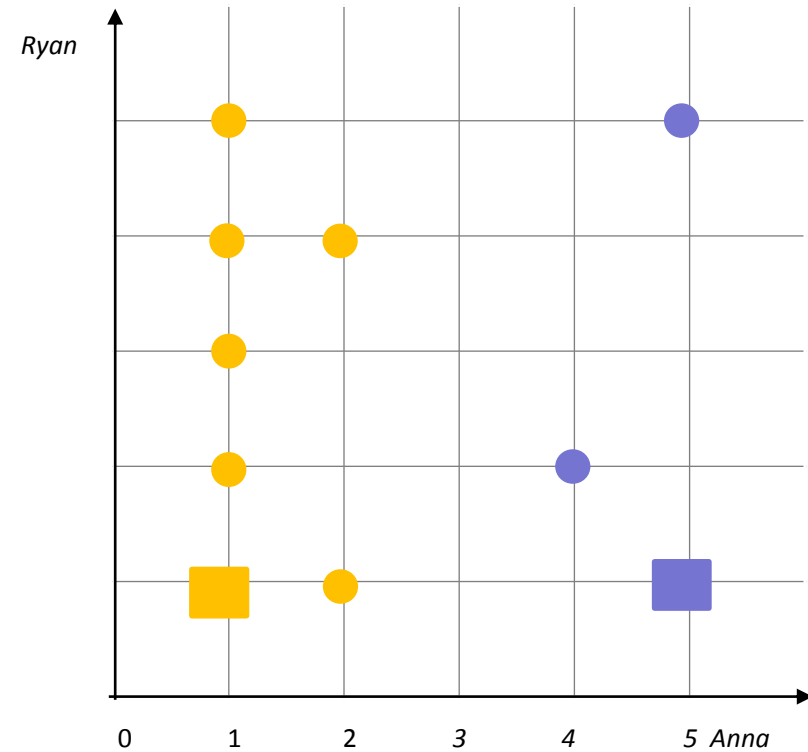
Movie	Anna	Ryan
Inside Out	5	5
Zootopia	4	2
San Andreas	1	4
The Pets Take Over	1	5
Fieldtrip to Mars	1	2
Forever	2	1
Still Here	1	3
A Happy Robot	2	4



Clustering: unsupervised learning – no labels  
K-means  $k = 2$

# Clustering

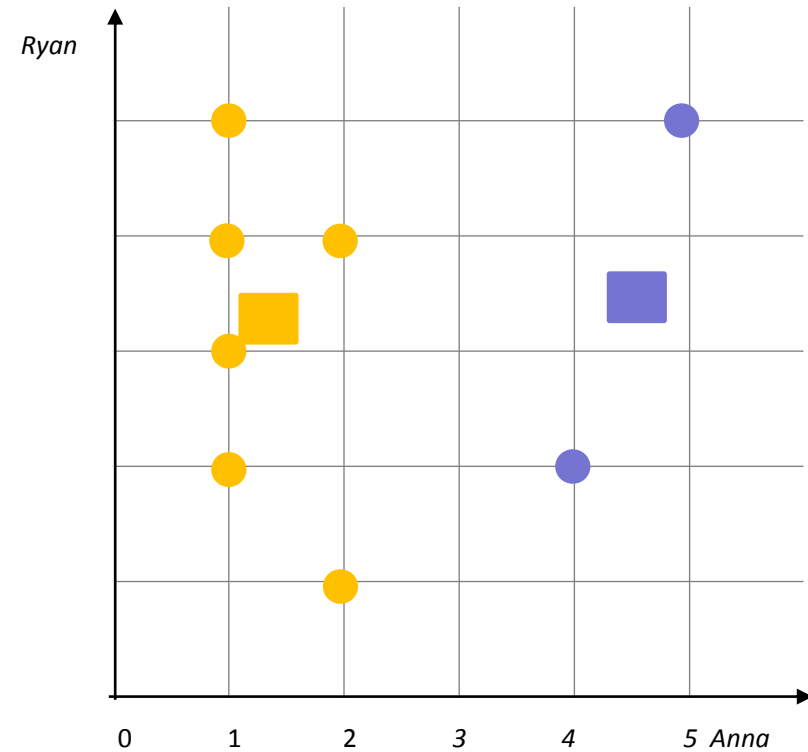
Movie	Anna	Ryan
Inside Out	5	5
Zootopia	4	2
San Andreas	1	4
The Pets Take Over	1	5
Fieldtrip to Mars	1	2
Forever	2	1
Still Here	1	3
A Happy Robot	2	4



Clustering: unsupervised learning – no labels  
K-means  $k = 2$

# Clustering

Movie	Anna	Ryan
Inside Out	5	5
Zootopia	4	2
San Andreas	1	4
The Pets Take Over	1	5
Fieldtrip to Mars	1	2
Forever	2	1
Still Here	1	3
A Happy Robot	2	4



To calculate the new position of the means:

Yellow  $(1+1+1+1+2+2)/6 = 4/3$

Blue  $(4+5)/2 = 9/2$

$(1+2+3+4+4+5)/6 = 19/6$

$(2+5)/2 = 7/2$



# PDDL

Goal( $\text{Has}(\text{Zoe}, d) \wedge \text{IsColdDrink}(d)$  )

Action( $\text{Buy}(\text{person}, \text{store}, \text{item})$ ,

PRECOND:  $\text{At}(\text{person}, \text{store}) \wedge \text{Sells}(\text{store}, \text{item}) \wedge$   
 $\text{HasCreditCard}(\text{person})$

EFFECT:  $\text{Has}(\text{person}, \text{item})$ )

$\text{At}(\text{person}, \text{store})$ ,  
 $\text{Sells}(\text{store}, \text{item})$ ,  
 $\text{HasCreditCard}(\text{person})$  are  
not included in the effects  
because they have not  
changed.



# PDDL

Goal( $\text{Has}(\text{Zoe}, d) \wedge \text{IsColdDrink}(d)$  )

Action( $\text{Buy}(\text{person}, \text{store}, \text{item})$ ,

PRECOND:  $\text{At}(\text{person}, \text{store}) \wedge \text{Sells}(\text{store}, \text{item}) \wedge$   
 $\text{HasCreditCard}(\text{person})$

EFFECT:  $\text{Has}(\text{person}, \text{item})$ )

Action( $\text{Go}(\text{person}, \text{from}, \text{to})$ ,

PRECOND:  $\text{At}(\text{person}, \text{from})$

EFFECT:  $\neg \text{At}(\text{person}, \text{from}) \wedge \text{At}(\text{person}, \text{to})$ )

Init( $\text{At}(\text{Zoe}, \text{DH}) \wedge \text{HasCreditCard}(\text{Zoe}) \wedge \text{Sells}(\text{JambaJuice}, \text{Smoothie}) \wedge$   
 $\text{IsColdDrink}(\text{Smoothie}) \wedge \text{IsColdDrink}(\text{Lemonade})$ )

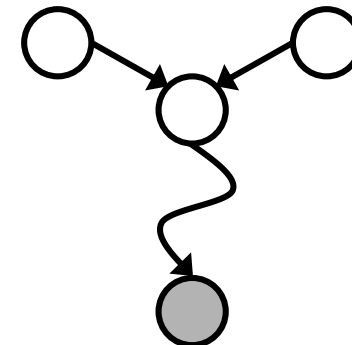
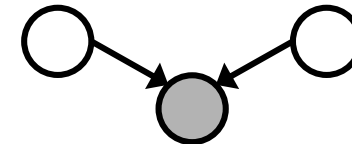
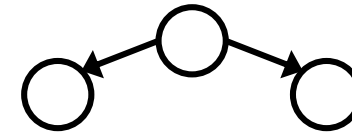
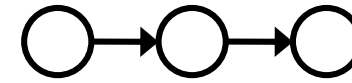
Solution:  $[\text{Go}(\text{Zoe}, \text{DH}, \text{JambaJuice}), \text{Buy}(\text{Zoe}, \text{Smoothie})]$



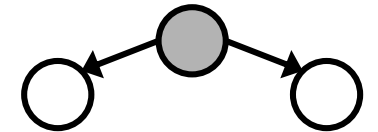
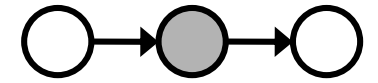
# Independence

- Are X and Y conditionally independent given evidence variables Z?
  - Consider **all** (undirected) paths from X to Y
  - **No active paths** = independence!
  - X and Y “d-separated” by Z
- A path is active if each triple is active.
- All it takes to block a path is a single inactive segment

Active Triples



Inactive Triples



# Independence

$A \perp\!\!\!\perp D \mid B$  ?

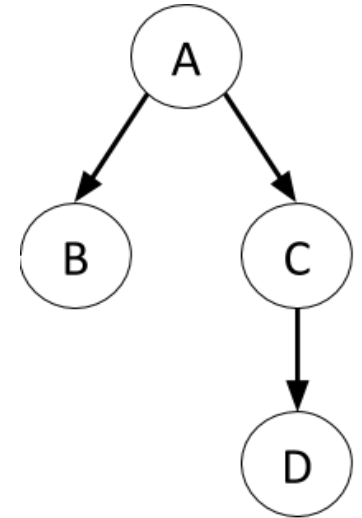
Consider all (undirected) paths from A to D:

- only one –ACD

The path includes one triplet only (ACD)

- ACD is active

Active path => No independence



# Independence

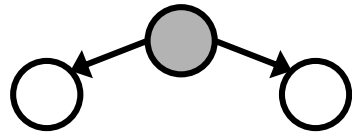
$B \perp\!\!\!\perp D \mid A$  ?

Consider all (undirected) paths from B to D:

- only one – BACD

The path includes triplets BAC and ACD

BAC is inactive

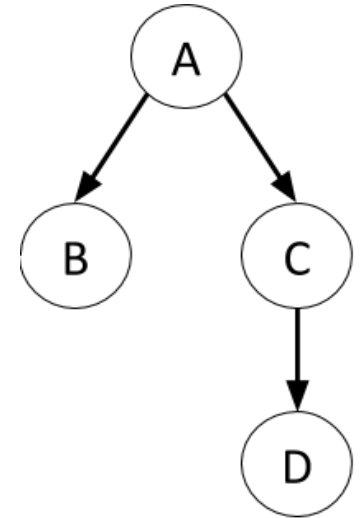


All it takes to block a path is a single inactive segment

- BACD is inactive

No active paths => independence

$B \perp\!\!\!\perp D \mid A$



# Independence

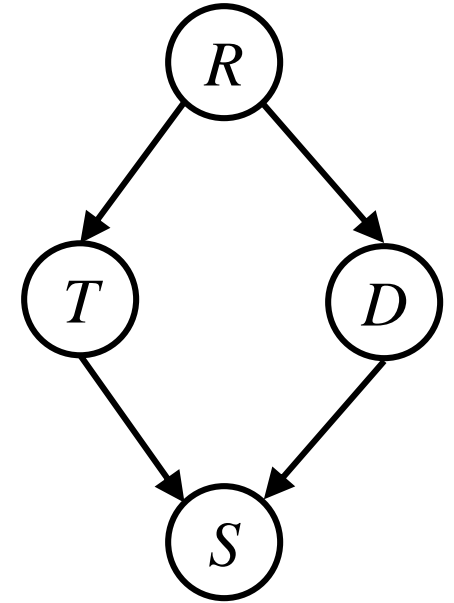
$T \perp\!\!\!\perp D?$

Consider all (undirected) paths from T to D

There are two paths: TSD and TRD

TSD inactive

TRD active => *No independence*



# Independence

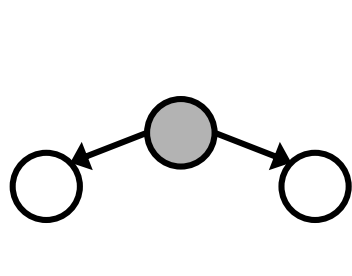
$T \perp\!\!\!\perp D \mid R$ ?

Consider all (undirected) paths from T to D

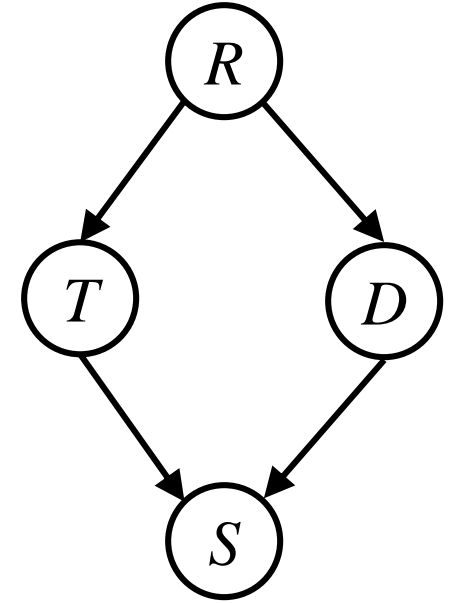
There are two paths: TSD and TRD

TSD inactive

TRD inactive



No active paths => independence



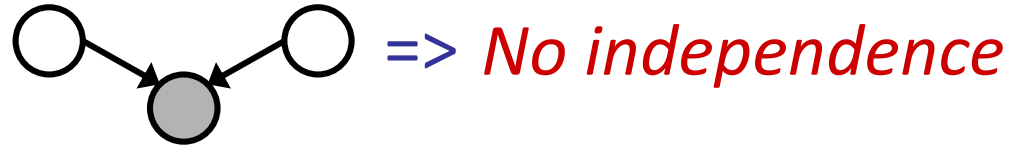
# Independence

$T \perp\!\!\!\perp D \mid R, S?$

Consider all (undirected) paths from T to D

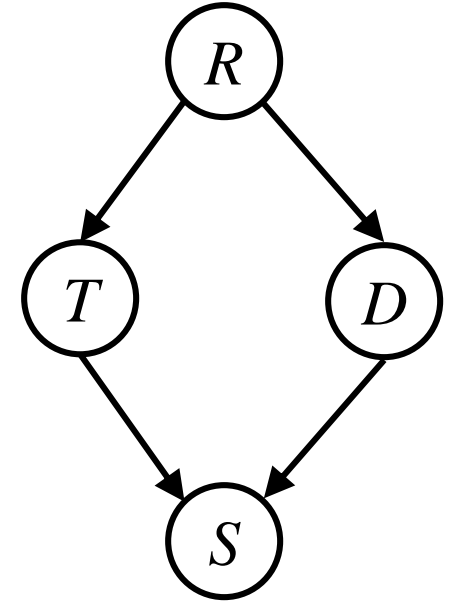
TSD and TRD

TSD active



TRD inactive

One active path  $\Rightarrow$  No independence





# The End

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- Good luck on the Final!
- Have a great summer!
- If you're interested in grading for CS 156 in the fall, please let me know.

