

Update on Dual Energy Phase Contrast

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Model

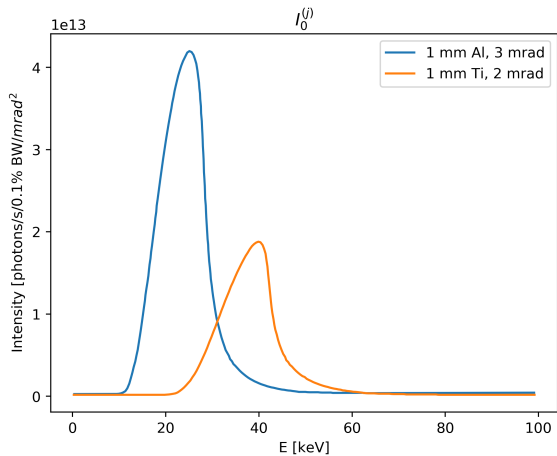
Measured intensity:

$$I_R^{(j)} = \int w(E) I_0^{(j)}(E) T(E) \left(1 + \frac{R_2}{k(E)} \nabla^2 \phi(E) \right) dE$$

with:

- $w(E)$ detector response [$\approx E$]
- $I_0^{(j)}$ entrance intensity for spectrum j [photons/s/0.1%BW/mrad²]
- $T(E)$ transmission factor [unitless]
- R_2 sample-detector distance [≈ 30 cm]
- $k(E)$ wave number [$\frac{2\pi}{\lambda(E)} \approx 10^{11}$ m]
- $\phi(E)$ phase factor [unitless]

Spectra: $I_0^{(j)}(E) \approx 10^{13}$



$\phi(E)$ and $T(E)$

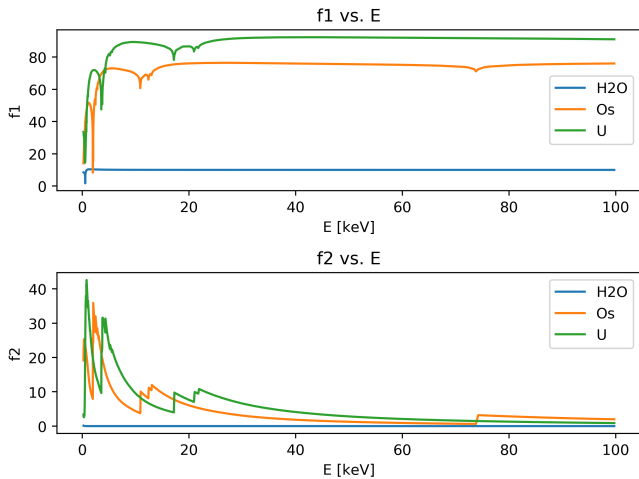
$$\phi(E) = r_e \lambda(E) \sum_i f_1^{(i)}(E) \int_L n_{a,i}(\vec{x}) dl$$

$$T(E) = \exp \left(-2 r_e \lambda(E) \sum_i f_2^{(i)}(E) \int_L n_{a,i}(\vec{x}) dl \right)$$

with:

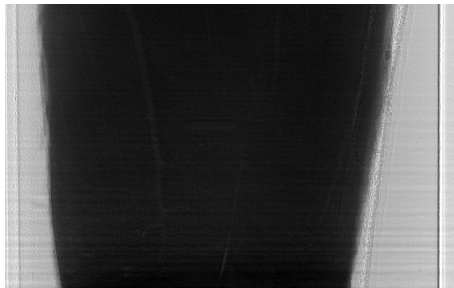
r_e	classical electron radius [$\approx 10^{-15}$ m]
$\lambda(E)$	wavelength [$\approx 10^{-11} - 10^{-9}$ m]
f_1, f_2	oscillation modes per atom [$\approx 10^1 - 10^2$ atom $^{-1}$]
$n_{a,i}(\vec{x})$	“atomic” number density [atoms / cm 3]

f_1 and f_2 from NIST

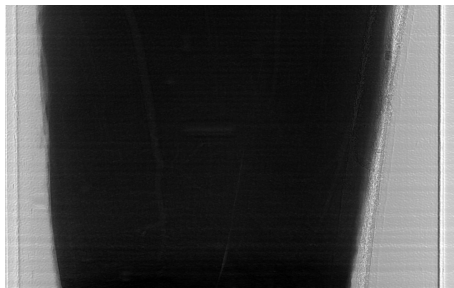


H₂O and Metal Phantoms

Al filter



No filter



$$\int_L n_{a,i}(\vec{x}) dl$$

Normalized phantom images by number densities:

$$\begin{aligned} \int_L n_{a,i}(\vec{x}) dl &\approx \frac{\rho_i N_a}{A_i} \Delta L * \left(\frac{\text{ph}_i(\vec{x})}{\text{mean}\{\text{ph}_i(\vec{x})\}} \right) \\ &\approx 10^{25} [\text{cm}^{-2}] \end{aligned}$$

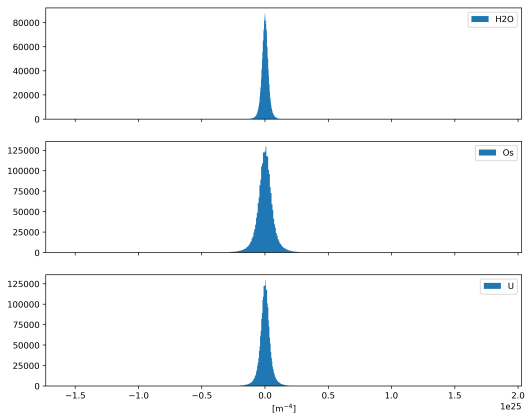
	H ₂ O	U	Os
ρ [g/cm ³]	1.0	19.1	22.59
A [g/mol]	18.03	238.03	190.23

$$N_a = 6.022\text{e}23 \text{ atoms/mole}$$

$$\Delta L = 2.38 \text{ mm}$$

$$\nabla^2 \int_L n_{a,i}(\vec{x}) d\vec{l}$$

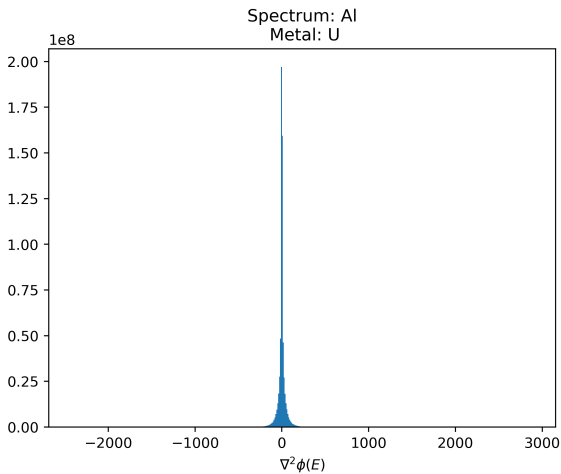
$$\nabla^2 \int n_{a,i}(\vec{x}) d\vec{l}$$



	H ₂ O	Os	U
Mean	4e5	1e6	-1e6
Absolute value mean:	2e23	5e23	3e23
Max:	4e24	2e25	1e25

$$\begin{aligned}
\nabla^2 \phi(E) &= r_e \lambda(E) \sum_i f_1^{(i)}(E) \left[\nabla^2 \int_L n_{a,i}(\vec{x}) dl \right] \\
&\approx [10^{-15} \text{ m}][10^{-11} - 10^{-9} \text{ m}][10^2][10^6 - 10^{25} \text{ m}^{-4}] \\
&\approx 10^{-18} - 10^3 \text{ m}^{-2}
\end{aligned}$$

$$\nabla^2\phi(E)$$



Issue: Small phase term

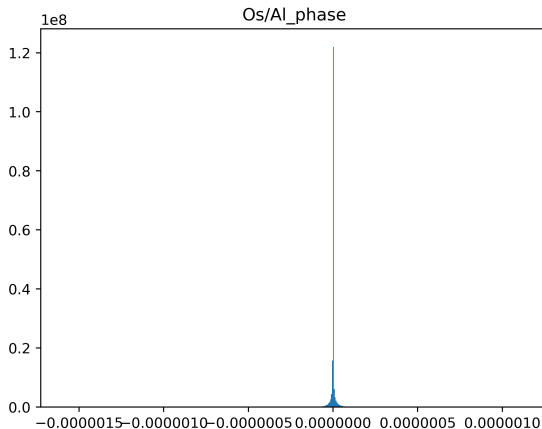
Recall:

$$I_R^{(j)} = \int w(E) I_0^{(j)}(E) T(E) \left(1 + \frac{R_2}{k(E)} \nabla^2 \phi(E) \right) dE$$

Phase term:

$$\begin{aligned} & \frac{R_2}{k(E)} \nabla^2 \phi(E) \\ & \approx \frac{[10^1 \text{ m}]}{[10^{11} \text{ m}^{-1}]} \cdot [10^3 \text{ m}^{-2}] \\ & \approx 10^{-7} \end{aligned}$$

Issue: Small phase term



Mean

7e-26

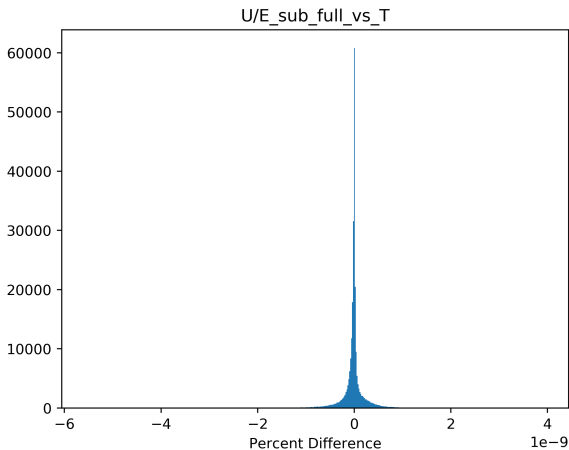
Absolute value mean:

6e-9

Max:

1e-6

Issue: Small phase term



Mean

-1e-11

Absolute value mean:

1e-10

Max:

4e-9