## Data analyses for Experiment 3

#### Scott Burgess

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This code analyzes the data associated with Experiment 3 and produces Figure 4, 5, and 6 in the manuscript:

Barnes DK, Burgess SC. Fitness consequences of marine larval dispersal: the role of neighborhood density, spatial arrangement, and genetic relatedness on survival, growth, reproduction, and paternity. *Journal of Evolutionary Biology* 

Code finalized September 2024.

Any comments or error reporting, please contact Scott Burgess: sburgess@bio.fsu.edu

#### Load required libraries

```
library('tidyverse')
library('glmmTMB')
library('gridExtra')
library('emmeans')
library('DHARMa')
library('vegan')
sessionInfo()
## R version 4.4.0 (2024-04-24)
## Platform: aarch64-apple-darwin20
## Running under: macOS Sonoma 14.6.1
##
## Matrix products: default
           /Library/Frameworks/R.framework/Versions/4.4-arm64/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/4.4-arm64/Resources/lib/libRlapack.dylib;
                                                                                               LAPACK v
##
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
## time zone: America/New_York
## tzcode source: internal
## attached base packages:
## [1] stats
                graphics grDevices utils
                                               datasets methods
                                                                   base
##
## other attached packages:
  [1] vegan 2.6-6.1
                        lattice 0.22-6 permute 0.9-7
                                                        DHARMa 0.4.6
## [5] emmeans_1.10.2 gridExtra_2.3
                                        glmmTMB_1.1.9
                                                        lubridate_1.9.3
   [9] forcats 1.0.0
                        stringr_1.5.1
                                        dplyr 1.1.4
                                                        purrr 1.0.2
                        tidyr_1.3.1
                                        tibble_3.2.1
                                                        ggplot2_3.5.1
## [13] readr_2.1.5
## [17] tidyverse_2.0.0
```

```
##
## loaded via a namespace (and not attached):
## [1] utf8 1.2.4
                            generics_0.1.3
                                                stringi_1.8.4
## [4] lme4_1.1-35.3
                            hms_1.1.3
                                                digest_0.6.35
## [7] magrittr_2.0.3
                            estimability_1.5.1
                                                evaluate_0.23
## [10] grid 4.4.0
                            timechange_0.3.0
                                                mvtnorm 1.2-5
## [13] fastmap 1.2.0
                            Matrix_1.7-0
                                                mgcv_1.9-1
## [16] fansi_1.0.6
                            scales_1.3.0
                                                numDeriv_2016.8-1.1
## [19] cli_3.6.2
                            rlang_1.1.3
                                                munsell_0.5.1
## [22] splines_4.4.0
                            withr_3.0.0
                                                yaml_2.3.8
## [25] parallel_4.4.0
                            tools_4.4.0
                                                tzdb_0.4.0
                            nloptr_2.0.3
## [28] coda_0.19-4.1
                                                minqa_1.2.7
## [31] colorspace_2.1-0
                            boot_1.3-30
                                                vctrs_0.6.5
## [34] R6_2.5.1
                                                MASS_7.3-60.2
                            lifecycle_1.0.4
## [37] cluster_2.1.6
                                                pillar_1.9.0
                            pkgconfig_2.0.3
## [40] gtable_0.3.5
                            Rcpp_1.0.12
                                                glue_1.7.0
## [43] xfun_0.44
                            tidyselect_1.2.1
                                                rstudioapi_0.16.0
## [46] knitr 1.47
                            xtable_1.8-4
                                                htmltools 0.5.8.1
                                                TMB_1.9.11
## [49] nlme_3.1-164
                            rmarkdown_2.28
## [52] compiler_4.4.0
```

#### Import data from Experiment 3

Phenotypic data

```
dat <- read.csv("Data/Experiment_3.csv")

Paternity data

Paternity_dat_0_9 <- read.table("Data/D0_9_final_Paternity.txt",header=T,sep=",")

Inferred fathers data

BestCluster_0_9 <- read.csv("Data/D0_9_final_BestCluster.csv",header=T)</pre>
```

Full sib family data

```
FSFamily_0_9 <- read.csv("Data/D0_9_final_BestFSFamily.csv")
```

## Process phenotypic data

Only use the summed data over all time periods

```
dat <- dat %>% filter(Time_days=="all") %>% select(-Time_days, -Bifurcations, -Zooids)
```

Add ID for focal colonies

```
focals <- c("A","B","D","G")
dat$focal <- ifelse(dat$Position %in% focals, 1, 0)</pre>
```

Create a vector of treatment levels and set the order (for plotting)

```
treatment.vec <- c("alone", "far", "near", "both")
dat$Treatment <- factor(dat$Treatment, levels=treatment.vec)</pre>
```

### Process paternity data

```
# Add sample data to each data frame
brks <- seq(0,160,0.1)
add sample data <- function(d){
  d$MotherID <- rapply(strsplit(d$OffspringID,"_"),function(x) head(x,1))</pre>
  d$FatherID <- rapply(strsplit(d$InferredDad1,"_"),function(x) head(x,1))</pre>
  tmp <- dat[match(d$MotherID,dat$Colony),-1]</pre>
  names(tmp) <- paste0("Mother.",names(tmp))</pre>
  d <- cbind.data.frame(d,tmp)</pre>
  tmp <- dat[match(d$FatherID,dat$Colony),-1]</pre>
  names(tmp) <- paste0("Father.",names(tmp))</pre>
  d <- cbind.data.frame(d,tmp)</pre>
# Calculate euclidean distance between observed parents
  d$Distance <- NA
  for(i in 1:nrow(d)){
    d$Distance[i] <- dist(</pre>
      matrix(d[i,which(names(d) %in% c("Mother.X", "Father.X", "Mother.Y", "Father.Y"))],2,2,byrow=T),meth
  }
  return(d)
Paternity_dat_0_9 <- add_sample_data(Paternity_dat_0_9)</pre>
```

## Calculate the number of offspring sampled per mother

```
OffspringIDs <- BestCluster_0_9$OffspringID
tmp <- rapply(strsplit(OffspringIDs,"_"),function(x) head(x,1))</pre>
MotherID <- pasteO(tmp,"_parent")</pre>
offspring_per_mother <- as.data.frame(table(MotherID))
offspring_per_mother
##
       MotherID Freq
## 1 01b_parent
                  25
## 2 02a_parent
## 3 04a_parent
                  24
## 4 05b_parent
                  26
                  25
## 5 06a_parent
## 6 08a_parent
                 26
## 7 09a_parent
                 24
## 8 12b_parent
                 27
## 9 13b_parent
                 25
## 10 15b parent
                  23
## 11 17a_parent
                 25
## 12 18a_parent
                  25
                  23
## 13 19b_parent
## 14 20a_parent
                  23
## 15 21a_parent
                  24
```

```
## 16 22a_parent 24
## 17 23a_parent 25
## 18 25b_parent 24
## 19 26a_parent 26
## 20 28a_parent 24
## 21 29b_parent 24
## 22 30a_parent 24
## 23 31a_parent 24
## 24 32a_parent 25
## 25 34b_parent 25
```

## How many settlers were genotyped?

```
with(offspring_per_mother,table(Freq))

## Freq
## 23 24 25 26 27
## 3 9 9 3 1

nrow(offspring_per_mother) # mothers

## [1] 25

sum(offspring_per_mother$Freq) # offspring

## [1] 615

nrow(dat) # potential fathers

## [1] 32
```

## Analyze Reproductive Output

#### DHARMa residual

#### Residual vs. predicted QQ plot residuals No significant problems detected 1.00 0. KS test: p = 0.55Deviation n. $\infty$ 0.75 DHARMa residua o. 0 Observed 9 Ö. 0.50 Dispersio (A) est: p= 0.55 Deviation n.s 0.4 0 0 0.25 0.2 Outlier test: p= 1 0 0.00 0 Deviation n.s. 0 0.0 0.0 8.0 0.0 0.4 0.8 0.4 **Expected** Model predictions (rank transformed)

## Object of Class DHARMa with simulated residuals based on 250 simulations with refit = FALSE . See ?D. ## ## Scaled residual values: 0.968 0.2535617 0.1921669 0.408 0.736 0.87259 0.09136761 0.852 0.324 0.20126 Get predicted values for plotting

```
type="response",
se=F))
```

Reproductive output was similar for individuals in all treatments ( $\chi^2 = 8.147$ , df = 6, p = 0.228).

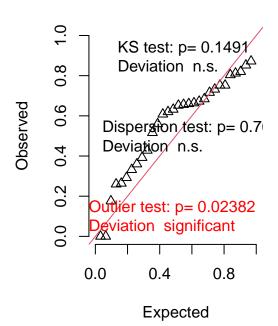
## Analyze Relative Growth Rate

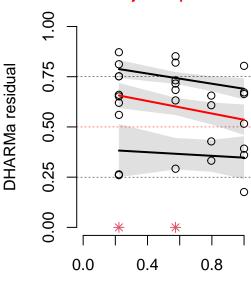
```
m1 <- glmmTMB(rgr40 ~ Treatment + (1|Block), data = dat)</pre>
m2 \leftarrow glmmTMB(rgr40 \sim 1 + (1|Block), data = dat)
result_rgr <- round(anova(m1, m2, test = "Chisq"), 3)</pre>
result_rgr
## Data: dat
## Models:
## m2: rgr40 ~ 1 + (1 | Block), zi=~0, disp=~1
## m1: rgr40 ~ Treatment + (1 | Block), zi=~0, disp=~1
           AIC
## Df
                     BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## m2 3 -141.96 -137.76 73.980 -147.96
## m1 6 -136.90 -128.49 74.448 -148.90 0.936
                                                             0.817
                                                      3
Check model fit
simulateResiduals(fittedModel = m1, plot = T)
```

#### DHARMa residual



# Residual vs. predicted Quantile deviations detected (red curves) Combined adjusted quantile test n.s.





Model predictions (rank transformed)

## Object of Class DHARMa with simulated residuals based on 250 simulations with refit = FALSE . See ?D ## ## Scaled residual values: 0.62 0.652 0.752 0.264 0.672 0.632 0 0.392 0.26 0.684 0 0.872 0.332 0.516 0.

Check influence of outliers

```
outliers <- dat[which(resid(m1) < -0.06), 'Colony']
tmp <- dat %>% filter(!Colony %in% outliers)
m1 <- glmmTMB(rgr40 ~ Treatment + (1|Block), data = tmp)
m2 <- glmmTMB(rgr40 ~ 1 + (1|Block), data = tmp)
round(anova(m1, m2, test = "Chisq"), 3)</pre>
```

```
## Data: tmp
## Models:
## m2: rgr40 ~ 1 + (1 | Block), zi=~0, disp=~1
## m1: rgr40 ~ Treatment + (1 | Block), zi=~0, disp=~1
## Df AIC BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## m2 3 -168.80 -164.8 87.399 -174.80
## m1 6 -164.79 -156.8 88.397 -176.79 1.995 3 0.573
```

No qualitative change.

Relative growth rate was similar for individuals in all treatments ( $\chi^2 = 0.936$ , df = 3, p = 0.817).

## Remove offspring from full sib families with Inclusion probabilities < 0.7

```
tmp <- FSFamily_0_9 %>% filter(Prob.Inc.. < 0.7)</pre>
offspring_to_exclude <- c(tmp$Member1,tmp$Member2)
BestCluster_0_9 <- BestCluster_0_9 %% filter(!(OffspringID %in% offspring_to_exclude))</pre>
How many kept and excluded?
nrow(FSFamily_0_9) # number of full sib families
## [1] 528
nrow(FSFamily_0_9 %% filter(Prob.Inc.. > 0.7)) # number of full sib families with high confidence
## [1] 511
(nrow(FSFamily_0_9 % filter(Prob.Inc.. > 0.7)) / nrow(FSFamily_0_9)) * 100 # %
## [1] 96.7803
# number of full sib families with very high confidence (1)
nrow(FSFamily_0_9 %>% filter(Prob.Inc.. == 1))
## [1] 466
(nrow(FSFamily_0_9 %>% filter(Prob.Inc.. == 1)) / nrow(FSFamily_0_9)) * 100 # %
## [1] 88.25758
nrow(tmp) # number full sib families excluded
## [1] 17
length(offspring_to_exclude) # number offspring excluded
## [1] 34
length(unique(BestCluster_0_9$MotherID)) # From this many mothers
## [1] 25
nrow(BestCluster_0_9) # this many offspring
## [1] 581
length(unique(BestCluster_0_9$FatherID)) # were sired by this many fathers
## [1] 291
# this many of which were from outside the array
BestCluster_0_9 %>% filter(grepl("#",FatherID)) %>% summarize(n=n_distinct(FatherID))
##
      n
## 1 286
# this many offspring sired by colonies in the array
BestCluster_0_9 %>% filter(!(grepl("#",FatherID))) %>% summarize(n=n())
```

```
##
## 1 13
BestCluster_0_9 %>% group_by(FatherID) %>%
  summarize(n=n_distinct(MotherID)) %>% count(n)
## Storing counts in `nn`, as `n` already present in input
## i Use `name = "new_name"` to pick a new name.
## # A tibble: 4 x 2
##
         n
             nn
##
     <int> <int>
## 1
         1 126
## 2
         2 114
         3
## 3
             46
## 4
         4
               5
Calculate the number of unique sires per focal colony
n fathers <- function(d){</pre>
  d$Mother_ID <- rapply(strsplit(d$MotherID,"_"),function(x) head(x,1))</pre>
  foo1 <- d %>%
    group_by(Mother_ID,FatherID) %>%
    summarise(n=n()) %>%
    mutate(freq=n/sum(n)) %>%
    ungroup()
  foo2 <- foo1 %>% group_by(Mother_ID) %>%
    summarise(nGenotyped=sum(n),
              UniqueNumberFather=n_distinct(FatherID))
  foo2$standardized.n.father <- with(foo1, tapply(n, Mother_ID, vegan::rarefy, sample=19))</pre>
  foo2$standardized.n.father <- round(foo2$standardized.n.father,3)</pre>
    # add sample info
  foo2 <- cbind.data.frame(foo2,dat[match(foo2$Mother_ID,dat$Colony),c(1:7,12)])</pre>
  foo2
}
n.fathers_0_9 <- n_fathers(d=BestCluster_0_9)</pre>
sort(n.fathers_0_9$standardized.n.father)
## [1] 5.130 15.567 15.761 15.928 16.522 16.779 16.844 17.141 17.286 17.290
## [11] 17.371 17.519 17.519 17.648 17.761 17.761 17.761 18.000 18.380 18.380
## [21] 18.430 18.430 18.430 18.430 19.000
sort(n.fathers_0_9$UniqueNumberFather)
```

n.fathers\_0\_9\$standardized.prop.father <- n.fathers\_0\_9\$standardized.n.father / 20
# make the 1's 0.9999 so can fit beta glmm
n.fathers\_0\_9\$standardized.prop.father <- ifelse(n.fathers\_0\_9\$standardized.prop.father == 1,</pre>

[1] 6 17 18 18 19 19 19 19 20 20 20 21 21 22 22 22 22 23 23 24 24 24 24 24

Calculate proportion for a beta glmm

```
0.99999,
n.fathers_0_9$standardized.prop.father)
```

## Analyze Number of Unique Sires per Mother

```
m1 <- glmmTMB(standardized.prop.father ~ Treatment +
                 (1|Block),
               family = 'beta_family',
               data = n.fathers_0_9)
m2 <- glmmTMB(standardized.prop.father ~ 1 +</pre>
                 (1|Block),
              family = 'beta_family',
              data = n.fathers_0_9)
result_sires <- round(anova(m1, m2, test = "Chisq"), 3)
result_sires
## Data: n.fathers_0_9
## Models:
## m2: standardized.prop.father ~ 1 + (1 | Block), zi=~0, disp=~1
## m1: standardized.prop.father ~ Treatment + (1 | Block), zi=~0, disp=~1
      Df
             AIC
                      BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## m2 3 -42.865 -39.209 24.433 -48.865
## m1 6 -39.368 -32.054 25.684 -51.368 2.502
                                                       3
                                                              0.475
Get predicted values for plotting
predictions_sires = data.frame(Treatment = treatment.vec)
p <- emmeans(m1, ~ Treatment,</pre>
             component = "cond",
             type = "response")
predictions_sires$fit <- summary(p)$response * 20</pre>
predictions_sires$lwr <- summary(p)$asymp.LCL * 20</pre>
predictions_sires$upr <- summary(p)$asymp.UCL * 20</pre>
nd <- expand.grid(Treatment = treatment.vec,</pre>
                  Block = rownames(coef(m1)$cond$Block))
block_effects_sires <- data.frame(nd,</pre>
                                 fit = predict(m1,
                                                newdata = nd,
                                                type="response",
                                                se=F))
block_effects_sires$fit <- block_effects_sires$fit * 20</pre>
```

The number of standardized unique sires per colony did not differ among treatments ( $\chi^2 = 2.502$ , df = 3, p = 0.475).

### Calculate the proportion of offspring from an assigned father

Get the mother ID's with an assigned father

```
offspring.proportion <- function(a,b){
# Get the maternal ID for offspring with a father in the array
   d1 <- a %>%
    distinct(MotherID, .keep_all=T)
# Add mother and father ID's to BestCluster data frame
  b$Mother_ID <- rapply(strsplit(b$MotherID,"_"),function(x) head(x,1))
  b$Father_ID <- rapply(strsplit(b$FatherID,"_"),function(x) head(x,1))
# Get the data from BestCluster for offspring with a father in the array
# and calculate the number and frequency of offspring
# per mother-father combination
 d2 <- b %>%
   filter(Mother_ID %in% d1$MotherID) %>%
    group_by(Mother_ID,Father_ID) %>%
   summarise(n=n()) %>%
   mutate(freq=n/sum(n)) %>%
   ungroup()
# Calculate the max frequency of fathers per mother
  d3 <- d2 %>%
    group_by(Mother_ID) %>%
   mutate(max.freq=max(freq)) %>%
   ungroup()
# Collect and arrange data
  d4 <- d3[grep("#",d3$Father_ID,invert=T),]</pre>
  d5 <- cbind.data.frame(d4, d1[match(d4$Mother ID,d1$MotherID),])
  d6 <- d5 %>% select(Mother ID, Father ID,
                      n, freq, max.freq,
                      ProbDad1,
                      Mother.Block, Mother.Treatment, Mother.Position, Mother.Direction,
                      Father.Block, Father.Treatment, Father.Position, Father.Direction)
  d6
}
offspring.proportion_0_9 <- offspring.proportion(Paternity_dat_0_9, BestCluster_0_9)
offspring.proportion_0_9
##
       Mother ID Father ID n
                                   freq
                                          max.freq ProbDad1 Mother.Block
```

```
## 2
                       03a 2 0.08695652 0.08695652
                                                           1
## 2.1
             02a
                       12b 1 0.04347826 0.08695652
                                                           1
                                                                        3
## 6
             06a
                       20a 2 0.08000000 0.08000000
                                                           1
                                                                        4
## 9
             09a
                       12b 1 0.04545455 0.09090909
                                                                        2
## 19
             20a
                       06a 4 0.19047619 0.19047619
                                                           1
## 21
             22a
                       12b 2 0.09090909 0.13636364
                       05b 1 0.04166667 0.04166667
## 25
       Mother.Treatment Mother.Position Mother.Direction Father.Block
## 2
                                                        С
                   both
                                      D
## 2.1
                   both
                                      D
                                                        С
                                                                     3
## 6
                   near
                                      Η
                                                        S
                                                                     4
## 9
                   both
                                      F
                                                        S
                                                                     2
                                      G
                                                        С
## 19
                   near
                                                                     4
## 21
                   both
                                      D
```

```
## 25
                    far
                                                                     4
##
      Father.Treatment Father.Position Father.Direction
## 2
                   both
                                      Ε
## 2.1
                   both
                                      Ε
                                                        N
## 6
                   near
                                      G
                                                        C
## 9
                   both
                                      Ε
                                                        S
## 19
                   near
                                      Η
                                                        S
## 21
                   both
                                      Ε
                                                        S
## 25
                                                        N
# Out of 511 offspring with full sib inclusion probabilities > 0.7,
# 13 (2.5%) offspring were assigned paternity from one of
# five candidate fathers in the experimental array
sum(offspring.proportion_0_9$n)
## [1] 13
length(unique(offspring.proportion_0_9$Father_ID))
## [1] 5
offspring.proportion_0_9 %>% count(Father_ID)
     Father_ID n
##
## 1
           03a 1
## 2
           05b 1
## 3
           06a 1
## 4
           12b 3
## 5
           20a 1
Paternity_dat_0_9 %>% count(Distance)
    Distance n
## 1 0.15000 10
## 2 0.85000 1
## 3 1.00000 1
## 4 70.00016 1
```

## Make Figure 4

```
alpha = 0.4,
               color = "grey") +
  geom_linerange(data = predictions_reprod,
                 aes(ymin = lwr,
                     ymax = upr)) +
  geom_point() +
  labs(y = "Reproductive output\n(number of settlers)",
       title = "a)") +
  theme classic() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1))
# Panel B
panel_B <- ggplot(data = predictions_sires,</pre>
                  aes(x = Treatment,
                      y = fit)) +
  # geom_jitter(data = block_effects_sires,
               aes(x = Treatment,
  #
                   y = fit),
  #
               width = 0.05,
               alpha = 0.4,
               color = "grey") +
  geom_linerange(aes(ymin = lwr,
                     ymax = upr)) +
  geom_point() +
  ylim(0, 20) +
  labs(y = "Standardized number\nof sires per colony",
       title = "b)") +
  theme_classic() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1))
tmp <- offspring.proportion_0_9 %>% filter(Mother.Block==Father.Block)
# far
y1 <- tmp %>% filter(Mother.Position=="B" & Father.Position == "C" |
                         Mother.Position=="C" & Father.Position == "B")
# near
y2 <- tmp %>% filter(Mother.Position=="G" & Father.Position %in% c("H"))
# both
y3 <- tmp %>% filter(Mother.Position=="D" & Father.Position %in% c("E","F"))
tmp <- rbind.data.frame(y1, y2, y3)</pre>
panel_C <- ggplot(data = tmp,</pre>
                  aes(x = Father.Treatment,
                      y = freq)) +
  geom_point() +
# for Mother_ID 02a, there were two fathers from the same block
    geom_linerange(data = tmp %>% filter(Mother_ID == "02a"),
                 aes(ymin = freq,
                     ymax = max.freq)) +
  labs(x = "Treatment",
```

```
y = "Proportion of offspring\nsired by nearest colony",
          title = "c)") +
   scale_x_discrete(label = c("far", "near", "both\n(far)")) +
   theme classic() +
   theme(axis.text.x = element_text(angle = 45, hjust = 1))
grid.arrange(panel_A, panel_B, panel_C,
                  nrow = 1,
                  ncol = 3)
                                                                             Proportion of offspring sired by nearest colony
                                                 b)
                                                                                          c)
             a)
                                       Standardized number
Reproductive output (number of settlers)
                                          sires per colony
      2500
                                             20
      2000
                                                                                    0.16
                                             15
       1500
                                                                                    0.12
                                             10
       1000
                                                                                    0.08
                                               5
        500
                                                                                    0.04
                                               0
```

**Treatment** 

Treatment

## pdf ##

alone

Treatment

## Make Figure 5 (Inclusion and exclusion probabilities)

alone

```
# Set breaks for plotting
brks <- seq(0,1,0.05)
# Get frequency of Inclusion probabilities
Inc <- with(FSFamily_0_9, hist(Prob.Inc..,</pre>
                                 breaks = brks,
                                 plot = F)
# Get frequency of Exclusion probabilities
Exc <- with(FSFamily_0_9,hist(Prob.Exc..,</pre>
                                breaks = brks,
                                plot = F))
# Panel A
d <- cbind.data.frame(mids = Inc$mids, counts = Inc$counts)</pre>
y <- d %>% filter(counts>0)
panel_A <- ggplot() +</pre>
  geom_col(data = y %>% filter(mids < 0.7),</pre>
            aes(x = mids,
                y = counts),
           fill = "grey",
           show.legend = F) +
  xlim(0,1) + ylim(0,max(y$counts)) +
  geom_col(data = y %>% filter(mids >= 0.7),
           aes(x = mids,
```

```
y = counts),
                                                 fill = "black",
                                                 show.legend = F) +
        labs(x = "Inclusion\nprobability",
                               y = "Frequency of \nfull sib families",
                               title = "a)") +
        theme_classic()
# Panel B
d <- cbind.data.frame(mids = Exc$mids, counts = Exc$counts)</pre>
y <- d %>% filter(counts>0)
panel_B <- ggplot() +</pre>
         geom_col(data = y,
                                                 aes(x = mids,
                                                                  y = counts),
                                                 fill = "black",
                                                 show.legend = F) +
        xlim(0,1) +
         labs(x = "Exlusion\nprobability",
                               y = "",
                               title = "b") +
         theme_classic()
grid.arrange(panel_A, panel_B, nrow = 1, ncol = 2)
                                                                                                                                                        b
                                       a)
Freduency of 400 and 100 and 1
                                                                                                                                      500 -
                                                                                                                                       400
                                                                                                                                      300
                                                                                                                                      200
                                                                                                                                        100
                                   0.00 0.25 0.50 0.75 1.00
                                                                                                                                                    0.00 0.25 0.50 0.75 1.00
                                                          Inclusion
                                                                                                                                                                                 Exlusion
                                                       probability
                                                                                                                                                                             probability
## pdf
##
                 2
```

# Calculate the frequency of potential and observed distances between parents

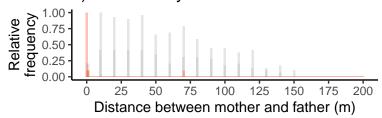
```
brks <- seq(0,200,0.1)
# # Potential distances
tmp <- dat %>% select("X", "Y")
```

```
mat <- dist(tmp, diag = T)</pre>
possible_distances <- mat[lower.tri(mat, diag = T)]</pre>
a <- hist(possible_distances, breaks = brks, plot = F)</pre>
possible_density <- data.frame(density = a$density / max(a$density),
                                 mids = a$mids)
# Observed
density_freq <- function(d){</pre>
  b <- hist(d$Distance,breaks=brks,plot=F)</pre>
  data.frame(n = b$counts,
              density = b$density / max(b$density),
              mids = b$mids)
}
observed_density_0_9 <- density_freq(Paternity_dat_0_9)
possible_density$Metric <- "Potential"</pre>
observed_density_0_9$Metric <- "Observed"
density_data <- rbind.data.frame(possible_density, observed_density_0_9[,-1])</pre>
density_data$Metric <- factor(density_data$Metric,</pre>
                                levels = c("Potential", "Observed"))
```

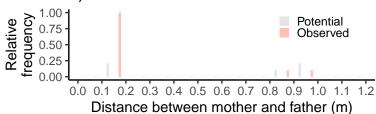
## Make Figure 6

```
panel_A <- ggplot() +</pre>
  geom_col(data = density_data,
                  aes(x = mids,
                      y = density,
                      fill = Metric),
           width = 3,
           alpha = 0.4,
           position_dodge(0.01)) +
  labs(x = "Distance between mother and father (m)",
       y = "Relative\nfrequency",
       title = "a) Whole array") +
  scale_fill_manual(name = 'd',
                    breaks = c('Potential','Observed'),
                    values = c('Potential' = 'grey',
                                'Observed' = 'tomato')) +
  scale_x_continuous(breaks = seq(0,300,25)) +
  theme_classic() +
  theme(legend.position = 'none')
panel_B <- ggplot() +</pre>
  geom_col(data = density_data %>% filter(mids < 1.2),</pre>
                  aes(x = mids,
                      y = density,
                      fill = Metric),
           width = 0.02,
           alpha = 0.4,
           position_dodge(0.1)) +
  labs(x = "Distance between mother and father (m)",
       y = "Relative\nfrequency",
```

## a) Whole array



## b) Within treatments



## pdf ## 2