December 2, 2019

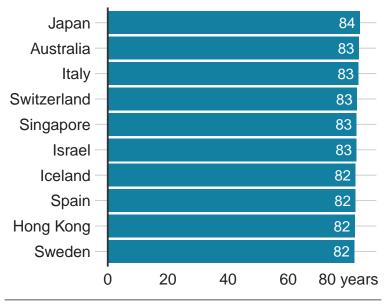
The results below are generated from an R script.

```
# Analysis
# Scott Cohn + Ruja Kambli
# Libraries -----
library(dplyr)
library(tidyverse) # duh.
library(ggplot2) # plotting
library(gridExtra) # plotting options
library(ggsci) # plot color palette
library(ggthemes) # Themes
library(bbplot) # plot style
library(readr) # import csv
library(lmtest) # BP test
library(scales) # Scale x-axis
library(MASS)
library(faraway) # Box-Cox transform / vif
# Colors
COLA <- c("#99d8c9","#66c2a4","#41ae76", "#238b45", "#005824")
COLB <- c("#4eb3d3", "#2b8cbe", "#0868ac","#084081")</pre>
# Import Data -----
life_exp_full <- read_csv("data/life_exp_full.csv")</pre>
## Parsed with column specification:
## cols(
## Country = col_character(),
## 'Birth Rate' = col_double(),
## 'Cancer Rate' = col_double(),
## 'Denque Cases' = col_double(),
## EPI = col_double(),
## GDP = col_double(),
## 'Health Expenditure' = col_double(),
## 'Heart Disease Rate' = col_double(),
## Population = col_double(),
## Area = col_double(),
## 'Pop Density' = col_double(),
## 'Stroke Rate' = col_double(),
## 'Life Expectancy' = col_double()
## )
# Data Transformations -----
```

```
# Capitalize letters in Country var
# Not perfect, but good enough
simpleCap <- function(x) {</pre>
 s <- strsplit(x, " ")[[1]]
 paste(toupper(substring(s, 1,1)), substring(s, 2),
        sep = "", collapse = " ")
}
life_exp_full <- life_exp_full %>%
  mutate(Country = apply(life_exp_full, 1, simpleCap))
# Visualizations ---
# Top 10 life exp by country
topten_lifeexp_country <- life_exp_full %>%
  arrange(desc(`Life Expectancy`)) %>%
  slice(1:10) %>%
  ggplot(aes(x = reorder(Country, `Life Expectancy`),
            y = `Life Expectancy`)) +
  geom_bar(stat = 'identity',
          fill = "#1380A1") +
  \#scale_fill_d3() +
  coord_flip() +
  scale_y_continuous(
   limits = c(0, 85),
   breaks = seq(0, 80, by = 20),
   labels = c("0", "20", "40", "60", "80 years")
  ) +
  geom_hline(yintercept = 0,
             size = 1,
             color = "#333333") +
  geom_label(
    aes(label = round(`Life Expectancy`, 0)),
   hjust = 1,
   vjust = 0.5,
   colour = "white",
   fill = NA,
   label.size = NA,
   family = "Helvetica",
   size = 6
  ) +
  bbc_style() +
  labs(title = "Life Expectancy",
       subtitle = "Top 10 Countries")
# Save graph
finalise_plot(plot_name = topten_lifeexp_country,
              source = "Source: JNYH/Project Luther",
              save_filepath = "figures/topten_lifeexp_country.pdf",
              width pixels = 640,
              height pixels = 450)
```

Life Expectancy

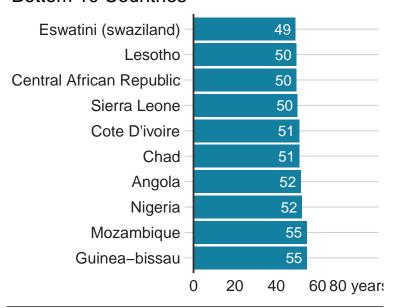
Top 10 Countries



```
#logo_image_path = "placeholder.png")
# Bottom 10 life exp by country
# life_exp_full %>% drop_na(`Life Expectancy`) %>% nrow() = 201 rows w/out NA
bottomten_lifeexp_country <- life_exp_full %>%
  drop_na(`Life Expectancy`) %>%
  arrange(desc(`Life Expectancy`)) %>%
  slice(192:201) %>%
  ggplot(aes(x = reorder(Country, -`Life Expectancy`),
             y = `Life Expectancy`)) +
  geom_bar(stat = 'identity',
          fill = "#1380A1") +
  \#scale_fill_d3() +
  coord_flip() +
  scale_y_continuous(
   limits = c(0, 85),
   breaks = seq(0, 80, by = 20),
    labels = c("0", "20", "40", "60", "80 years")
  geom_hline(yintercept = 0,
             size = 1,
             color = "#333333") +
  geom_label(
    aes(label = round(`Life Expectancy`, 0)),
    hjust = 1,
   vjust = 0.5,
    colour = "white",
    fill = NA,
   label.size = NA,
```

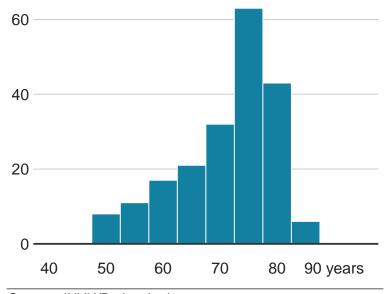
Life Expectancy

Bottom 10 Countries



How life expectancy varies

Distribution of life expectancy

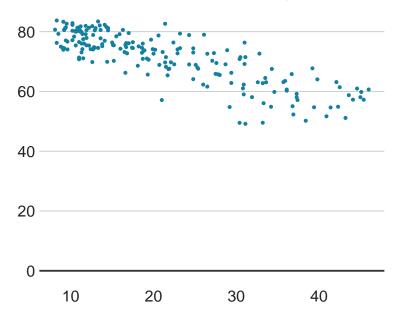


```
labs(title = "How long can we expect to live?",
    subtitle = "Birth Rate vs. Life Expectancy",
    ylab = "Life Expectancy",
    xlab = "Births Per 1000 People")

## Warning: Removed 54 rows containing missing values (geom_point).
```

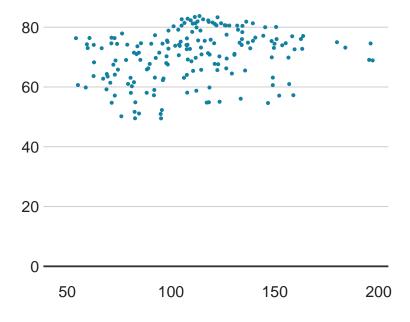
How long can we expect to live

Birth Rate vs. Life Expectancy

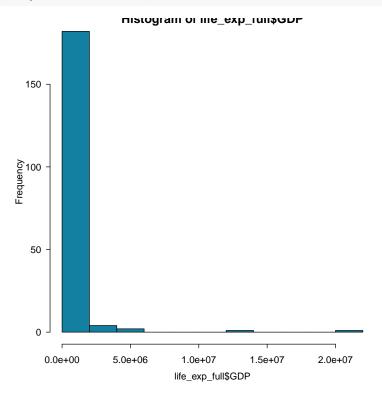


How long do we expect to live

Cancer Rate vs. Life Expectancy



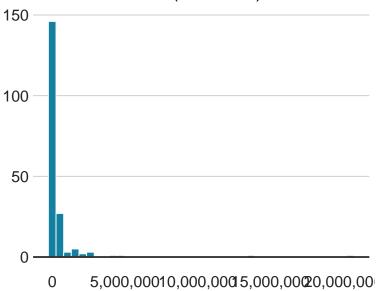
GDP Distribution, Histogram
hist(life_exp_full\$GDP, col = "#1380A1")



```
GDP_distro <- life_exp_full %>%
  ggplot(aes(x = GDP)) +
  geom_histogram(
    color = "white",
   fill = "#1380A1",
   na.rm = TRUE,
   bins = 40
  ) +
  geom_hline(yintercept = 0,
             size = 1,
             color = "#333333") +
 bbc_style() +
  scale_x_continuous(labels = scales::comma) +
  labs(title = "How GDP varies",
       subtitle = "Distribution of GDP (US $ Mil.)")
# Save graph
finalise_plot(plot_name = GDP_distro,
              source = "Source: JNYH/Project Luther",
              save_filepath = "figures/GDP_distro.pdf",
              width_pixels = 640,
              height_pixels = 450)
```

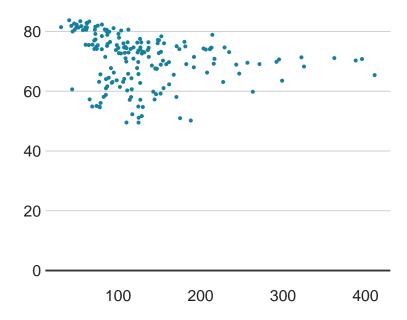
How GDP varies

Distribution of GDP (US \$ Mil.)



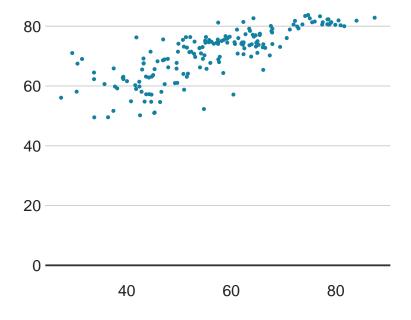
How long do we expect to live

Heart Disease Rate vs. Life Expectancy

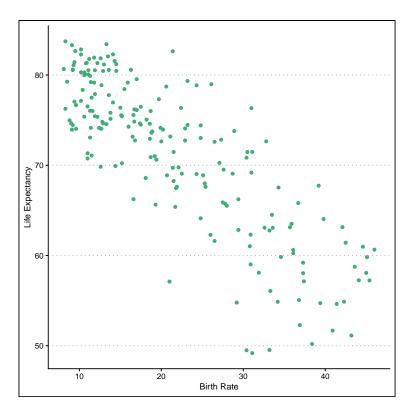


How long do we expect to live

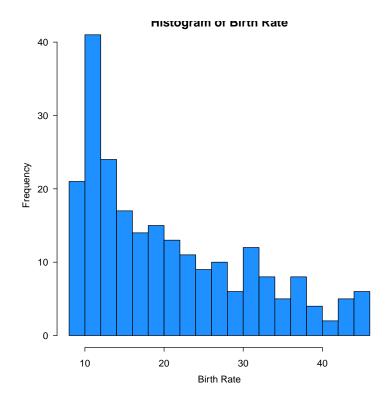
EPI vs. Life Expectancy



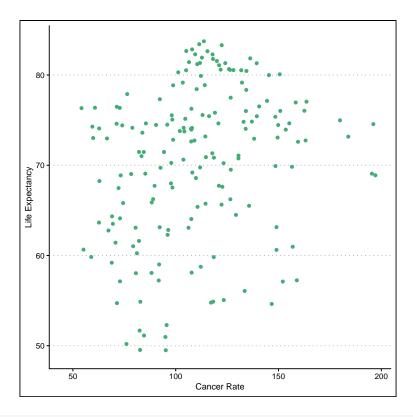
```
# Plot Variables v Life Expectancy ------
# Birth
life_exp_full %>%
    ggplot() +
    geom_point(
        aes(y = `Life Expectancy`, x = `Birth Rate`),
        color = COLA[3]) +
    theme_clean()
## Warning: Removed 54 rows containing missing values (geom_point).
```

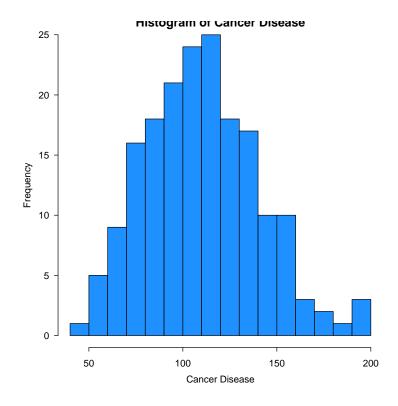


```
hist(life_exp_full$`Birth Rate`,
    xlab = "Birth Rate",
    main = "Histogram of Birth Rate",
    col = "dodgerblue",
    border = "black",
    breaks = 20)
```

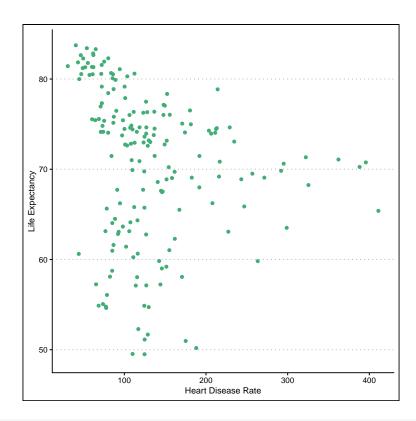


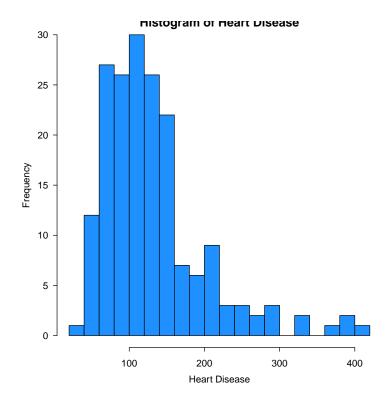
```
# Cancer
life_exp_full %>%
  ggplot() +
  geom_point(
    aes(y = `Life Expectancy`, x = `Cancer Rate`),
    color = COLA[3]) +
  theme_clean()
## Warning: Removed 70 rows containing missing values (geom_point).
```



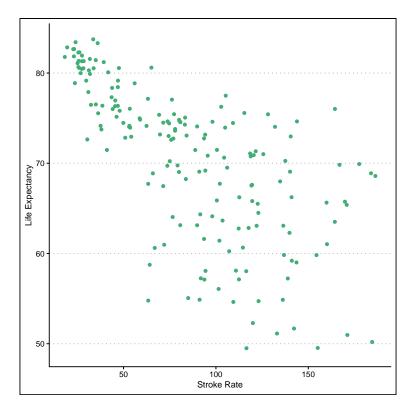


```
# Heart Disease
life_exp_full %>%
ggplot() +
geom_point(
   aes(y = `Life Expectancy`, x = `Heart Disease Rate`),
   color = COLA[3]) +
theme_clean()
## Warning: Removed 70 rows containing missing values (geom_point).
```

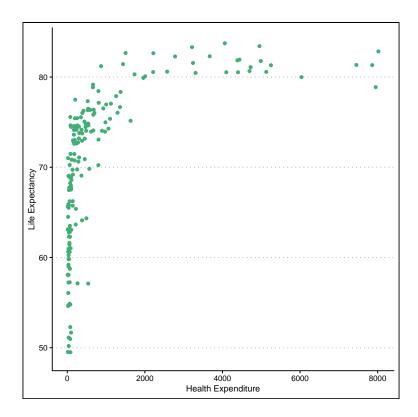




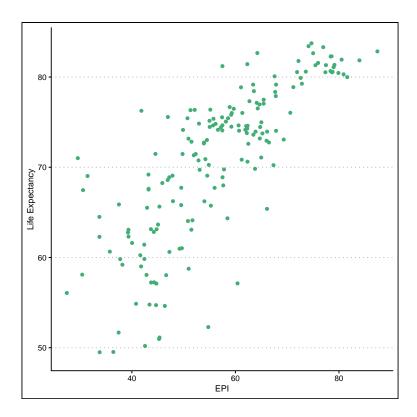
```
# Stroke
life_exp_full %>%
  ggplot() +
  geom_point(
    aes(y = `Life Expectancy`, x = `Stroke Rate`),
    color = COLA[3]) +
  theme_clean()
## Warning: Removed 70 rows containing missing values (geom_point).
```



```
# Health Expenditure
life_exp_full %>%
ggplot() +
geom_point(
   aes(y = `Life Expectancy`, x = `Health Expenditure`),
   color = COLA[3]) +
theme_clean()
## Warning: Removed 76 rows containing missing values (geom_point).
```

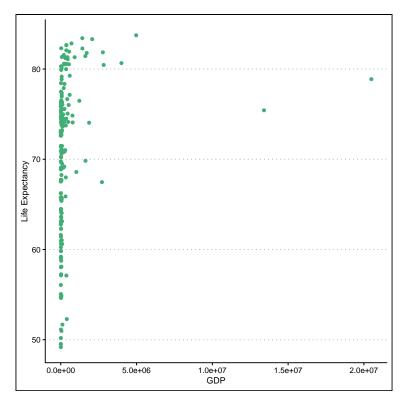


```
# EPI
life_exp_full %>%
  ggplot() +
  geom_point(
   aes(y = `Life Expectancy`, x = EPI),
    color = COLA[3]) +
  theme_clean()
## Warning: Removed 73 rows containing missing values (geom_point).
```



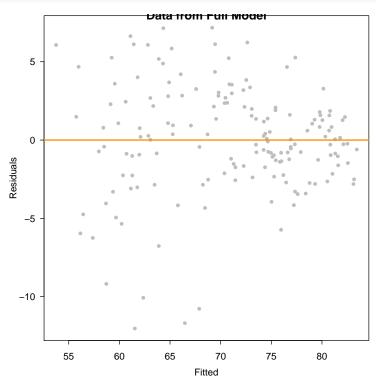
```
# GDP
life_exp_full %>%
  ggplot() +
  geom_point(
    aes(y = `Life Expectancy`, x = GDP),
    color = COLA[3]) +
  theme_clean()

## Warning: Removed 67 rows containing missing values (geom_point).
```



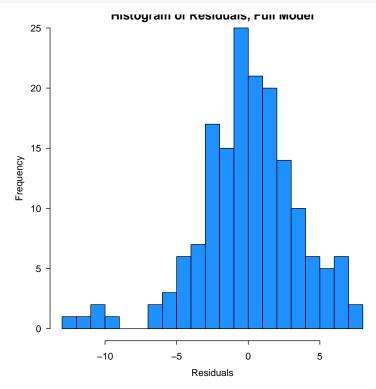
```
# Regressions --
model_full <- lm(</pre>
 `Life Expectancy` ~ `Birth Rate` + `Cancer Rate` + `Heart Disease Rate` + `Stroke Rate` + `Health Exp
 data = life_exp_full
# Testing Model Fit -----
# compare model full and model reduced.
anova(model_red, model_full)
## Analysis of Variance Table
## Model 1: `Life Expectancy` ~ `Birth Rate` + `Stroke Rate` + `Health Expenditure` +
      EPI + GDP
## Model 2: `Life Expectancy` ~ `Birth Rate` + `Cancer Rate` + `Heart Disease Rate` +
      `Stroke Rate` + `Health Expenditure` + EPI + GDP
    Res.Df RSS Df Sum of Sq
## 1 158 1995.2
     156 1963.5 2 31.704 1.2594 0.2867
#F = 0.8399
\# Pr(>F) = 0.5018
# Failed to reject HO: that removed var are zero.
# Diagnostic Checks - Model Full ----
# Model Summary and ANOVA
summary(model_full)
```

```
##
## Call:
## lm(formula = `Life Expectancy` ~ `Birth Rate` + `Cancer Rate` +
      `Heart Disease Rate` + `Stroke Rate` + `Health Expenditure` +
      EPI + GDP, data = life_exp_full)
##
##
## Residuals:
##
       Min
                 1Q
                     Median
                                  3Q
## -12.0296 -1.7375 0.0473 2.1224
                                       7.1708
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       7.637e+01 2.958e+00 25.817 < 2e-16 ***
## `Birth Rate`
                      -4.243e-01 3.881e-02 -10.931 < 2e-16 ***
## `Cancer Rate`
                       -1.507e-02 1.017e-02 -1.482
## `Heart Disease Rate` 2.311e-03 5.156e-03 0.448
                                                      0.655
                       -5.894e-02 1.051e-02 -5.607 9.13e-08 ***
## `Stroke Rate`
## `Health Expenditure` -2.225e-04 2.687e-04 -0.828
                                                     0.409
## EPI
                        1.801e-01 4.050e-02 4.448 1.64e-05 ***
## GDP
                        9.325e-08 1.539e-07 0.606
                                                     0.546
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.548 on 156 degrees of freedom
## (84 observations deleted due to missingness)
## Multiple R-squared: 0.8326, Adjusted R-squared: 0.8251
## F-statistic: 110.8 on 7 and 156 DF, p-value: < 2.2e-16
anova(model_full)
## Analysis of Variance Table
##
## Response: Life Expectancy
##
                        Df Sum Sq Mean Sq F value Pr(>F)
## `Birth Rate`
                        1 8213.0 8213.0 652.5242 < 2.2e-16 ***
## `Cancer Rate`
                        1
                           29.2
                                   29.2 2.3207 0.12969
                        1 276.2
                                  276.2 21.9426 6.072e-06 ***
## `Heart Disease Rate`
                        1 950.8
## `Stroke Rate`
                                  950.8 75.5445 4.620e-15 ***
## `Health Expenditure` 1 45.0
                                   45.0 3.5773 0.06043 .
## EPI
                         1 244.8
                                   244.8 19.4518 1.914e-05 ***
## GDP
                         1
                            4.6
                                    4.6
                                          0.3669
                                                  0.54557
## Residuals
                       156 1963.5
                                    12.6
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# 1 The regression function is linear (the relationship is linear).
# Yes
vif(model full)
                             `Cancer Rate` `Heart Disease Rate`
                                                                     `Stroke Rate`
          `Birth Rate`
                                  1.214850
                                                      1.651303
                                                                           2.617937
              2.177726
## `Health Expenditure`
                                       EPI
                                                            GDP
##
                                  3.685143
                                                      1.226175
              2.712092
# 2 The error terms have a constant variance
```

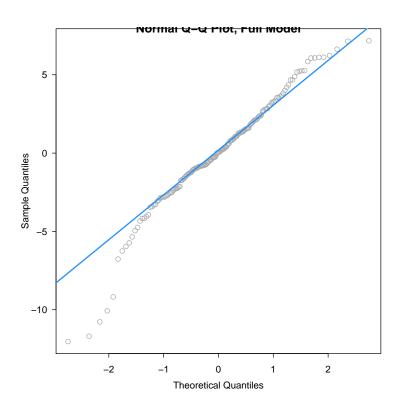


```
# Looks like it has a inverse parabolic shape
# 3 The error terms are independent (there is no relationship among the error terms).
# Breusch-Pagan Test for Homoskedasticity
bptest(model_full)
##
##
   studentized Breusch-Pagan test
## data: model_full
## BP = 20.003, df = 7, p-value = 0.005563
# For model_full we see a small p-value, so we reject the null hypothesis of
      homoskedasticity is rejected and heteroskedasticity assumed.
# The constant variance assumption is violated.
# This matches our findings with a fitted versus residuals plot.
# 4 The error terms are normally distributed
hist(resid(model_full),
     xlab
           = "Residuals",
     main
          = "Histogram of Residuals, Full Model",
```

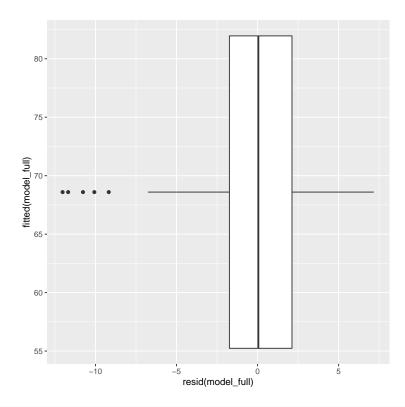
```
col = "dodgerblue",
border = "black",
breaks = 20)
```



```
# It does have a rough bell shape, however, it also has a semi-sharp peak.
# Q-Q Plot
qqnorm(resid(model_full), main = "Normal Q-Q Plot, Full Model", col = "darkgrey")
qqline(resid(model_full), col = "dodgerblue", lwd = 2)
```

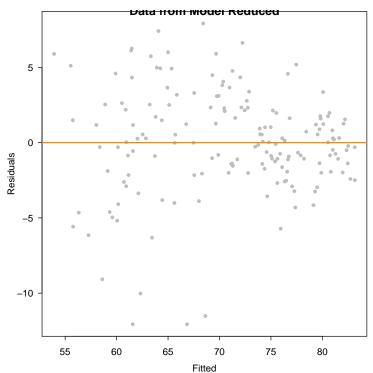


```
# Deviates in smaller quantiles
# For Model Full, we have a suspect Q-Q plot.
# We would probably not believe the errors follow a normal distribution.
# Shapiro-Wilk Test
shapiro.test(resid(model_full))
   Shapiro-Wilk normality test
##
##
## data: resid(model full)
## W = 0.96343, p-value = 0.0002576
\# p = 7.152e-05
# A small p-value indicates we believe there is only a small probability
# the data could have been sampled from a normal distribution.
#RK 5 Outlier Check Via Boxplots- how should we deal with those outliers? Which countries are they?
outlierAssumption <- ggplot(model_full, aes(x=fitted(model_full), y=resid(model_full))) +</pre>
  geom boxplot() +
  coord_flip()
outlierAssumption
## Warning: Continuous x aesthetic - did you forget aes(group=...)?
```



```
# 6 There is no important predictor that have been omitted from the model
# RK I think for this one since she's just looking for a logical explanation, we can say
# that there very well maybe be other factors that are contributing to the life expectancy
# of a country, but it is impossible to state them all. I'm going to put a better explanation
# and possible alternative predictors in the actual paper.
# Diagnostic Checks - Model Reduced -
# Model Summary and ANOVA
summary(model_red)
##
## Call:
## lm(formula = `Life Expectancy` ~ `Birth Rate` + `Stroke Rate` +
       `Health Expenditure` + EPI + GDP, data = model_full$model)
##
##
## Residuals:
       Min
                  1Q
                      Median
## -12.0656 -1.8950
                      0.0142
                                2.1378
                                         7.9142
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
                         7.523e+01 2.868e+00 26.228 < 2e-16 ***
## (Intercept)
## `Birth Rate`
                        -4.158e-01 3.763e-02 -11.052 < 2e-16 ***
## `Stroke Rate`
                        -5.863e-02 8.794e-03 -6.667 4.14e-10 ***
## `Health Expenditure` -2.300e-04 2.617e-04 -0.879
                                                        0.381
## EPI
                         1.725e-01 3.872e-02
                                                4.456 1.57e-05 ***
## GDP
                         8.809e-08 1.542e-07
                                                0.571
                                                         0.569
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.554 on 158 degrees of freedom
## Multiple R-squared: 0.8299, Adjusted R-squared: 0.8245
## F-statistic: 154.1 on 5 and 158 DF, p-value: < 2.2e-16
anova(model red)
## Analysis of Variance Table
##
## Response: Life Expectancy
                        Df Sum Sq Mean Sq F value
## `Birth Rate`
                         1 8213.0 8213.0 650.3884 < 2.2e-16 ***
## `Stroke Rate`
                         1 1233.4
                                  1233.4 97.6747 < 2.2e-16 ***
## `Health Expenditure`
                                     34.0
                                            2.6914
                                                      0.1029
                             34.0
                         1
## EPI
                            247.5
                                    247.5 19.5972 1.776e-05 ***
                         1
## GDP
                         1
                              4.1
                                      4.1
                                            0.3265
                                                      0.5685
## Residuals
                       158 1995.2
                                     12.6
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Fitted vs Residuals --- model_red
plot(fitted(model_red), resid(model_red), col = "grey", pch = 20,
    xlab = "Fitted", ylab = "Residuals", main = "Data from Model Reduced")
abline(h = 0, col = "darkorange", lwd = 2)
```



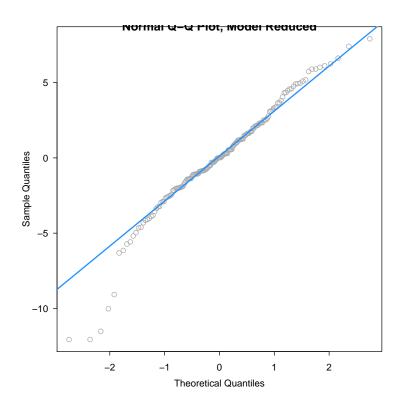
```
# Looks like it has a inverse parabolic shape
# Breusch-Pagan Test for Homoskedasticity
bptest(model_red)
```

```
##
##
   studentized Breusch-Pagan test
##
## data: model_red
## BP = 18.747, df = 5, p-value = 0.002142
# For model_red we see a small p-value, so we reject the null of homoskedasticity.
# The constant variance assumption is violated.
# This matches our findings with a fitted versus residuals plot.
# Normality of errors
hist(resid(model_red),
     xlab = "Residuals",
     main = "Histogram of Residuals, Model Reduced",
     col = "darkorange",
     border = "dodgerblue",
   breaks = 20)
```

TISTOGIAMI OI RESIDUAIS, IVIOUEI REDUCEU 20 15 -10 -5 0 Residuals

```
# It does have a rough bell shape, however, it also has a very sharp peak.

# Q-Q Plot
qqnorm(resid(model_red), main = "Normal Q-Q Plot, Model Reduced", col = "darkgrey")
qqline(resid(model_red), col = "dodgerblue", lwd = 2)
```



The R session information (including the OS info, R version and all packages used):

```
## R version 3.6.1 (2019-07-05)
## Platform: x86_64-apple-darwin15.6.0 (64-bit)
## Running under: macOS Catalina 10.15.1
##
## Matrix products: default
## BLAS: /System/Library/Frameworks/Accelerate.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/vecLib.framework/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/Versions/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/A/Frameworks/
```

```
## LAPACK: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRlapack.dylib
##
## locale:
## [1] en US.UTF-8/en US.UTF-8/en US.UTF-8/C/en US.UTF-8/en US.UTF-8
## attached base packages:
## [1] stats
                graphics grDevices utils
                                            datasets methods
                                                               base
## other attached packages:
## [1] faraway_1.0.7 MASS_7.3-51.4 scales_1.0.0
                                                    lmtest_0.9-37 zoo_1.8-6
## [6] bbplot_0.2
                  ggthemes_4.2.0 ggsci_2.9
                                                    gridExtra_2.3 forcats_0.4.0
## [11] stringr_1.4.0 purrr_0.3.3
                                     readr_1.3.1
                                                    tidyr_1.0.0
                                                                   tibble_2.1.3
## [16] ggplot2_3.2.1 tidyverse_1.2.1 dplyr_0.8.3
                                                    knitr_1.26
##
## loaded via a namespace (and not attached):
## [1] Rcpp 1.0.3 lubridate 1.7.4 lattice 0.20-38
                                                            png 0.1-7
## [5] statquotes_0.2.2 assertthat_0.2.1 zeallot_0.1.0
                                                             packrat_0.5.0
## [9] R6 2.4.1
                         cellranger 1.1.0 backports 1.1.5
                                                             evaluate 0.14
## [13] httr_1.4.0
                                           pillar_1.4.2
                       highr_0.8
                                                             rlang_0.4.1
## [17] lazyeval 0.2.2 readxl 1.3.1
                                           minqa_1.2.4
                                                             rstudioapi 0.10
## [21] nloptr 1.2.1
                       Matrix 1.2-17
                                           labeling 0.3
                                                             splines 3.6.1
                                           tinytex_0.17
## [25] lme4 1.1-21
                        tidytext 0.2.1
                                                             munsell 0.5.0
## [29] broom_0.5.2
                       compiler_3.6.1
                                           janeaustenr_0.1.5 modelr_0.1.4
## [33] xfun_0.11
                         pkgconfig_2.0.3
                                           tidyselect_0.2.5
                                                             ggpubr_0.2.4
                         withr_2.1.2
                                           SnowballC_0.6.0
                                                             grid_3.6.1
## [37] crayon_1.3.4
                                           gtable_0.3.0
## [41] nlme_3.1-140
                                                             lifecycle_0.1.0
                         jsonlite_1.6
## [45] magrittr_1.5
                         tokenizers_0.2.1
                                           cli_1.1.0
                                                             stringi_1.4.3
## [49] ggsignif_0.6.0
                        xm12_1.2.0
                                           ellipsis_0.3.0
                                                             generics_0.0.2
                    cowplot_1.0.0
## [53] vctrs_0.2.0
                                           boot_1.3-22
                                                             wordcloud_2.6
## [57] RColorBrewer_1.1-2 tools_3.6.1
                                           glue_1.3.1
                                                             hms_0.5.0
## [61] colorspace_1.4-1 rvest_0.3.4
                                           haven_2.1.1
Sys.time()
## [1] "2019-12-02 11:30:08 EST"
```