

The program takes as input y (the rapidity to calculate energy density fluctuations at), and N_{traj} . Then for each of a series of values of the number of gluons A_{max} , it does the following:

1. Calculate all possible random walks of length $\leq A_{\text{max}}$. (CalcPQCount)
2. Generate $N_{\text{traj}}*10$ trajectories by selecting each step weighted by its degeneracy given that the walk must return to $(0,0)$. (FindTrajectory)
3. For each random walk, calculate the quadratic Casimir at each step and use this to find the energy density:

$$\begin{aligned}\epsilon &= \frac{dE}{dy} = \frac{1}{\sqrt{2\pi}\sigma} \int_{-\infty}^{\infty} d\eta \frac{dE}{d\eta} e^{-(\eta-y)^2/2\sigma^2} \\ &= \frac{1}{2} \sum_a \frac{dE}{d\eta} \Big|_{\eta=\eta(a)} \left[\text{erf} \left(\frac{\eta(a+1)-y}{\sqrt{2}\sigma} \right) - \text{erf} \left(\frac{\eta(a)-y}{\sqrt{2}\sigma} \right) \right]\end{aligned}$$

4. Average over all trajectories (which are split into 10 samples to estimate error) to find $\langle \epsilon^n \rangle$, and therefore the cumulant ratios $\omega, S\sigma, K\sigma^2$.
5. Write the ratios to an output file (moments.dat), which can be used with moments.py to graph the ratios over the values of A_{max} .