3 Generating Training Points with Simplex Sampler

3.1 Summary

Simplex Sampler produces a list of points in the n-dimensional model-parameter space to be used for training an emulator. The algorithms are based on the n-dimensional simplex. For example, in two dimensions the points are arranged in an equilateral triangle, and for three dimensions of parameters points are arranged in a tetrahedron. The program first reads a simple text file that provides the names of model parameters and the range of their prior distribution. Options for Simplex sampler are taken from a separate text file. This enables the User to make choices, such as which algorithm to apply when generating the training points. Simplex Sampler determines the number of training points based on the algorithm. The User is free to run the full model at additional points.

3.2 Simplex Parameters (not model parameters!)

These are parameters representing choices made by the User. Note these are NOT the model parameters, which are then generated by *Simplex Sampler*. If one visits the User's project directory, these parameters are typically stored in the file MY_PROJECT/parameters/simplex_parameters.txt, where the path is either absolute or relative to the project directory. Parameters files can have any name or location. These files are text files in the format. An example of a parameter file is:

#Simplex_LogFileName	simplexlog.txt	# if blank, output to screen
Simplex_TrainType	1	# Must be 1 or 2 or 3
Simplex_RTrain	0.95	# Radius of simplex
Simplex_ModelRunDirName	modelruns	# Directory with training
		point information

For the parameter file, the first string is the parameter name and is followed by the value. Both are single strings (without spaces). The # symbol is used for comments. Each parameter has a default value, which will be used if the parameter is not mentioned in the parameter file. Simplex Sampler has four User-defined parameters.

1. Simplex_TrainType

Possible values are "1", "2" or "3". The default, "1", will position points according to a simplex, i.e. in two dimensions this is an equilateral triangle and in three dimensions, it is a tetrahedron. In n dimensions there are n+1 points separated at equal distances from one another and centered at the origin.

2. Simplex_RTrain

This sets the distance from the origin that the training points will be selected throughout the parameter space. The default is 0.95.

3. Simplex_ModelRunDirName

This sets the path to the directory in which the run files will be created. The default name is modelruns, but the user can change this to anything they want. The path is relative to the project directory, i.e. the directory from which you run the *simplex* command.

4. Simplex_LogFileName

If this is left blank, Simplex Sampler will write output to the string. Otherwise it will write output to a file. Given that Simplex Sampler runs in a few seconds, the program is usually run interactively and output is sent to the screen.

3.3 Specifying Model Parameters and Priors

Before proceeding, Simplex requires information about the parameters, specifically, their ranges. The User enters this information into the file Info/modelpar_info.txt. An example of such a file might be

NuclearCompressibility	gaussian	210	40
ScreeningMass	uniform	0.3	1.2
Viscosity	uniform	0.08	0.3

The first column is the model-parameter name, and the last three parameters describe the range of the parameters, which is usually the prior, assuming the prior is uniform or Gausian. The second entry for each parameter defines whether the range/prior is uniform or gaussian. If the prior is uniform, the next two numbers specify the lower and upper ranges of the parameter. If the range/prior is gaussian, the third entry describes the center of the Gaussian, x_0 , and the fourth entry describes the Gaussian width, σ_0 , where the prior distribution is $\propto \exp\{-(x-x_0)^2/2\sigma_0^2\}$. Simplex will read the information to determine the number of parameters. It will then assign the n points, $\theta_{1...n}$ assuming each dimension of θ varies from -1 to 1, for uniform distributions, or proportional to $e^{-\theta^2/2}$ for Gaussian distributions. The points θ_i are each then converted into x_i by scaling and translating the values according to the ranges/priors defined in the modelpar_info.txt file.

3.4 Training Types

3.4.1 Type 1

Depending on the number of parameters, n, the program creates a simplex in n dimensions. This simplex's vertices will be used to generate $N_{\text{train}} = n + 1$ training points. These points will be scaled by different values so the training points aren't in the same radius. This results in the minimum number of required points for linear fits. Thus, if the model is perfectly linear, this option provides perfect emulation.

3.4.2 Type 2

Depending on the number of parameters, the program first creates a simplex in n dimensions. This simplex's vertices will be used to generate new training points there and along the edges. These points will be scaled to be in different radii from the center. This results in the minimum number of required points for quadratic fits. The net number of training points is then $N_{\text{train}} = n$

n+1+n(n+1)/2. Thus, if the model is perfectly quadratic, this option provides perfect emulation.

3.4.3 Type 3

This training type creates two different simplexes, both centered at the origin. The second simplex is a reflection of the first. The 2-dimensional visualization of this would look like the "Star of David". Finally, one extra training point is added at the origin. The net number of training points is $N_{\text{train}} = 2n + 3$.

3.5 Running Simplex to Generate Training Points

To run Simplex Sampler, first make sure the program is compiled. To compile the programs, change into the MSU_GITHOME/smooth/local/build/ directory and enter the following command,

```
GITHOME_MSU/local/build% cmake .
GITHOME_MSU/local/build% make simplex
```

Next, change into your project directory and run the program.

```
MY_PROJECT% MY_LOCAL/bin/simplex PARAMETER_FILE_NAME
```

Here MY_LOCAL is the path to where the User compiles the main programs into executables, and PARAMETER_FILE_NAME is the name of the simplex parameter file, e.g. parameters/simplex_parameters.txt. Paths are either absolute, or are relative to the project directory.

Simplex_ModelRunDirName parameter. Within the directory, a sub-directory will be created for each training point, named run0/, run1/, run2/···. Within each subdirectory, Simplex creates a file Simplex_ModelRunDirName/runI/mod_parameters.txt for the Ith training point. For example, the run0/mod_parameters.txt file might be

NuclearCompressibility	229.08		
ScreeningMass	0.453		
Viscosity	0.192		

At this point, it is up to the User to run their full model at each training point and create a file runI/obs.txt, which stores values of the observables at those training points as calculated by the full model.