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# **Profiles**

# Breadth-First Search:

Expand Calls: 43.6k, 59.5k, 82.5k, 106k, 173k

Mean: 92.92k Median: 82.5k

Memory: 432MiB, 586MiB, 856MiB, 1.01GiB, 1.65GiB

257k

106k

Mean: 906.8MiB Median: 856MiB

\*puzzle-2\*

\*puzzle-3\*

push

pop

			Time		Al	locatio	ons
Tot / % measured:		75.0s / 3.00%			432MiB / 99.2%		
Section	ncalls	time	%tot	avg	alloc	%tot	avg
expand	43.6k	1.78s	78.8%	40.7μs	262MiB	61.2%	6.16KiB
possibleactions	43.6k	194ms	8.62%	4.45µs	158MiB	36.8%	3.71KiB
create node	58.8k	151ms	6.72%	2.57µs	6.29MiB	1.47%	112B
push	118k	107ms	4.74%	907ns	2.33MiB	0.54%	20.7B
pop	43.6k	24.5ms	1.09%	563ns	0.00B	0.00%	0.00B

			Time		Al	locatio	ons
Tot / % meas	ured:	59	 4s / 0.	65%	1.01	GiB / 1	100%
Section	ncalls	time	%tot	avg	alloc	%tot	avg
expand		2.34s	60.3%	22.1µs	638MiB	61.5%	6.19KiB
create node	128k	524ms		4.09µs	13.7MiB	1.32%	112B
possibleactions	106k	512ms	13.2%	4.85us	382MiB	36.9%	3.71KiB

389ms 10.0% 1.52μs 3.00MiB 0.29%

113ms 2.92% 1.07μs 0.00B 0.00%

12.3B

0.00B

puzzle-4*								
		Time		Al	locatio			
Tot / % measu	Tot / % measured:		243s / 1.31%			MiB / 1		
Section	ncalls	time	%tot	avg	alloc	%tot	avg	
expand	59.5k	2.08s	65.3%	35.0µs	359MiB	61.3%	6.18KiB	
create node	78.8k	404ms	12.6%	5.12µs	8.42MiB	1.44%	112B	
possibleactions	59.5k	401ms	12.6%	6.75µs	215MiB	36.8%	3.71KiB	
push	158k	244ms	7.66%	1.55µs	3.00MiB	0.51%	20.0B	
pop	59.5k	57.8ms	1.81%	972ns	0.00B	0.00%	0.00B	
puzzle-5*								
puzzle-5*			Time		Al	locatio	ns	
puzzle-5* Tot / % measu	ured:		Time 	96%		locatio —— MiB / 9		
Tot / % measu	ured:			06% avg				
Tot / % measo	ncalls	12	4s / 1. %tot	avg	856 alloc	MiB / 9 %tot	5.8% avg	
Tot / % measo Section expand	ncalls	12 time 717ms	4s / 1. %tot 54.9%	avg 8.69µs	856 alloc 507MiB	MiB / 9 %tot 61.8%	5.8% avg 6.29KiB	
Tot / % measonsection  expand possibleactions	ncalls 82.5k 82.5k	12 time 717ms 288ms	4s / 1. %tot 54.9% 22.0%	avg 8.69µs 3.48µs	856 alloc 507MiB 299MiB	MiB / 9 %tot 61.8% 36.4%	5.8% avg 6.29KiB 3.71KiB	
Tot / % measons Section  expand possibleactions create node	ncalls	12 time 717ms	4s / 1. %tot 54.9%	avg 8.69µs	856 alloc 507MiB	MiB / 9 %tot 61.8%	5.8% avg 6.29KiB	
Tot / % measons Section  expand possibleactions create node push	ncalls 82.5k 82.5k 104k	12 time 717ms 288ms 171ms	4s / 1. %tot 54.9% 22.0% 13.1%	avg 8.69µs 3.48µs 1.65µs	856 alloc 507MiB 299MiB 11.5MiB	MiB / 9 %tot 61.8% 36.4% 1.40%	5.8% avg 6.29KiB 3.71KiB 116B	
	ncalls 82.5k 82.5k 104k 207k	717ms 288ms 171ms 101ms	4s / 1. %tot 54.9% 22.0% 13.1% 7.76%	8.69µs 3.48µs 1.65µs 489ns	856 alloc 507MiB 299MiB 11.5MiB 3.33MiB	MiB / 9 %tot 61.8% 36.4% 1.40% 0.41%	5.8% avg 6.29KiB 3.71KiB 116B 16.8B	

Time Allocations

Tot / % measured: 1318s / 0.38% 1.65GiB / 100% Section ncalls %tot alloc %tot time avg avg expand 173k 2.74s 55.4% 15.9µs 1.01GiB 61.6% 6.17KiB 808ms 16.3% 4.68µs 625MiB 37.0% 3.71KiB possibleactions 173k 731ms 14.8% 4.10μs create node 178k 19.0MiB 1.13% 112B push 356k 483ms 9.75% 1.35μs 4.00MiB 0.24% 11.8B pop 173k 188ms 3.80% 1.09µs 0.00B 0.00% 0.00B

#### A\* with Manhattan Distance:

Expand Calls: 2.46k, 8.63k, 12.4k, 67.2k, 3.22M

Mean: 662.1k Median: 12.4k

Memory: 27MiB, 97.2MiB, 144MiB, 758MiB, 35.6GiB

Mean: 7.32GiB Median: 144MiB

\*puzzle-2\*

			Time		A1	locatio	ns
Tot / % meas	ured:	488	 8ms / 49	.9%	144	MiB / 9	7.6%
Section	ncalls	time	%tot	avg	alloc	%tot	avg
		407	40.00	0.50			0.000
dequeue heuristic score	12.4k 33.7k	107ms 53.0ms	43.8% 21.8%	8.58µs 1.57µs	0.00B 16.4MiB	0.00% 11.7%	0.00B 510B
expand	12.4k	46.4ms	19.0%	3.73μs	75.4MiB	53.6%	6.21KiB
possibleactions	12.4k	29.9ms	12.3%	2.41µs	45.0MiB	32.0%	3.71KiB
create node	33.7k	6.96ms	2.86%	206ns	3.60MiB	2.56%	112B
push	12.4k	614µs	0.25%	49.4ns	257KiB	0.18%	21.1B

			Time		Al	locatio	ons
Tot / % meas	ured:	372	 ms / 44	.6%	97.2	MiB / 9	7.2%
Section	ncalls	time	%tot	avg	alloc	%tot	avg
dequeue	8.63k	82.9ms	50.0%	9.61µs	0.00B	0.00%	0.00B
expand	8.63k	38.4ms	23.2%	4.45µs	52.1MiB	55.1%	6.18KiB
possibleactions	8.63k	25.2ms	15.2%	2.92µs	31.3MiB	33.1%	3.71KiB
heuristic score	23.1k	12.7ms	7.65%	548ns	8.46MiB		384B
create node push	23.1k 8.63k	5.89ms 652µs	3.55% 0.39%	255ns 75.6ns	2.47MiB 257KiB	2.61% 0.27%	112B 30.4B
*puzzle-4*							
			Time		Al	locatio	ons
				2%		MiB / 9	18 1%
Tot / % meas	ured:	3.4	6s / 44		758	א / מדויוני	0.1%
Tot / % meas	ured: ncalls	3.4 time	6s / 44 %tot	avg	758 alloc	%tot	avg
Section	ncalls	time	%tot	avg	alloc	%tot	avg
Section	ncalls 67.2k	time 882ms	%tot 57.8%	avg 13.1µs	alloc 0.00B	%tot	avg 0.00B
Section  dequeue expand	ncalls 67.2k 67.2k	882ms 304ms	%tot 57.8% 19.9%	avg 13.1µs 4.53µs	alloc 0.00B 410MiB	%tot 0.00% 55.2%	avg 0.00B 6.25KiB
Section  dequeue expand possibleactions	ncalls 67.2k 67.2k 67.2k	882ms 304ms 182ms	%tot 57.8% 19.9% 12.0%	avg 13.1µs 4.53µs 2.72µs	0.00B 410MiB 244MiB	%tot  0.00% 55.2% 32.7%	0.00B 6.25KiB 3.71KiB
Section  dequeue expand	ncalls 67.2k 67.2k	882ms 304ms	%tot 57.8% 19.9%	avg 13.1µs 4.53µs	alloc 0.00B 410MiB	%tot 0.00% 55.2%	avg 0.00B 6.25KiB
dequeue expand possibleactions heuristic score	ncalls  67.2k 67.2k 67.2k 186k	882ms 304ms 182ms 92.1ms	%tot 57.8% 19.9% 12.0% 6.03%	13.1µs 4.53µs 2.72µs 496ns	0.00B 410MiB 244MiB 68.0MiB	%tot  0.00% 55.2% 32.7% 9.14%	0.00B 6.25KiB 3.71KiB 384B

Time

Allocations

\_\_\_\_\_

Tot / % measu	ured:	30	5s / 54	1.6%	35.6	GiB / 9	8.2%
Section	ncalls	time	%tot	avg	alloc	%tot	avg
dequeue	3.22M	84.7s	50.8%	26.3µs	0.00B	0.00%	0.00B
expand	3.22M	37.3s	22.3%	11.6µs	19.3GiB	55.3%	6.29KiB
possibleactions	3.22M	34.9s	20.9%	10.8µs	11.4GiB	32.6%	3.71KiB
heuristic score	9.03M	6.32s	3.79%	700ns	3.23GiB	9.25%	384B
create node	9.03M	3.33s	2.00%	369ns	0.94GiB	2.70%	112B
push	3.22M	302ms	0.18%	93.7ns	33.0MiB	0.09%	10.7B

\*puzzle-6\*

			Time		Al	locatio ——	ns
Tot / % measured:		124ms / 49.5%			27.0MiB / 97.1%		
Section	ncalls	time	%tot	avg	alloc	%tot	avg
dequeue	2.46k	24.8ms	40.5%	10.1µs	0.00B	0.00%	0.00B
expand	2.46k	15.8ms	25.8%	6.42µs	14.4MiB	54.9%	5.99KiB
possibleactions	2.46k	12.2ms	19.9%	4.94µs	8.91MiB	33.9%	3.70KiB
heuristic score	6.09k	5.09ms	8.31%	835ns	2.23MiB	8.49%	384B
create node	6.09k	2.99ms	4.89%	491ns	666KiB	2.48%	112B
push	2.46k	359µs	0.59%	146ns	64.4KiB	0.24%	26.8B

## A\* with Manhattan Distance and Linear Conflict

Expand Calls: 945, 1.13k, 2.05k, 34.2k, 59.3k

Mean: 19.5k Median: 2.05k

Memory: 31.9MiB, 37.6MiB, 72MiB, 1.19GiB, 1.95GiB

Mean: 656k Median: 72MiB

			Time		Al	locatio ——	ns
Tot / % meas	ured:	266	 ms / 82	.9%	72.0	MiB / 9	9.0%
Section	ncalls	time	%tot	avg	alloc	%tot	avg
heuristic score	5.72k	187ms	84.7%	32.7µs	50.5MiB	71.0%	9.05KiB
dequeue	2.05k	17.1ms	7.75%	8.35µs	0.00B	0.00%	0.00B
expand	2.05k	8.68ms	3.93%	4.23µs	12.6MiB	17.6%	6.28KiB
possibleactions	2.05k	5.89ms	2.67%	2.87µs	7.43MiB	10.4%	3.71KiB
create node	5.72k	1.98ms	0.90%	347ns	626KiB	0.86%	112B
push	2.05k	179µs	0.08%	87.5ns	64.4KiB	0.09%	32.2B

<sup>\*</sup>puzzle-3\*

			Time		Al	locatio	ons	
Tot / % meas	ured:	80.0	 ms / 64	1.6%	37.6	MiB / 9	9.1%	
Section	ncalls	time	%tot	avg	alloc	%tot	avg	
heuristic score	3.01k	29.6ms	57.2%	9.84µs	26.0MiB	69.8%	8.86KiB	
dequeue	1.13k	11.0ms	21.4%	9.77µs	0.00B	0.00%	0.00B	
expand	1.13k		9.60%	4.39µs	6.80MiB		6.16KiB	
possibleactions	1.13k	3.84ms	7.42%	3.39µs	4.10MiB	11.0%	3.71KiB	
create node	3.01k	1.98ms	3.82%	658ns	329KiB	0.86%	112B	
push	1.13k	286µs	0.55%	253ns	32.4KiB	0.08%	29.3B	
puzzle-4*			Time		ΔΊ	locatio	ns	
							,	
Tot / % meas	ured:	3.0	3s / 57	7.8%	1.19	GiB / 9	9.1%	
Section	ncalls	time	%tot	avg	alloc	%tot	avg	
heuristic score	95.0k	835ms	47.7%	8.79µs	863MiB	71.5%	9.30KiB	
heuristic score dequeue	95.0k 34.2k	835ms 574ms	47.7% 32.8%	8.79µs 16.8µs	863MiB 0.00B	71.5% 0.00%	9.30KiB 0.00B	
heuristic score dequeue expand	95.0k 34.2k 34.2k	835ms 574ms 162ms	47.7% 32.8% 9.28%	8.79µs 16.8µs 4.75µs	863MiB 0.00B 209MiB	71.5% 0.00% 17.3%	9.30KiB 0.00B 6.27KiB	
heuristic score dequeue expand possibleactions	95.0k 34.2k 34.2k 34.2k	835ms 574ms 162ms 131ms	47.7% 32.8% 9.28% 7.50%	8.79µs 16.8µs 4.75µs 3.84µs	863MiB 0.00B 209MiB 124MiB	71.5% 0.00% 17.3% 10.3%	9.30KiB 0.00B 6.27KiB 3.71KiB	
heuristic score dequeue expand	95.0k 34.2k 34.2k	835ms 574ms 162ms 131ms	47.7% 32.8% 9.28%	8.79µs 16.8µs 4.75µs	863MiB 0.00B 209MiB	71.5% 0.00% 17.3% 10.3%	9.30KiB 0.00B 6.27KiB	
heuristic score dequeue expand possibleactions create node push	95.0k 34.2k 34.2k 34.2k 35.0k	835ms 574ms 162ms 131ms 44.6ms	47.7% 32.8% 9.28% 7.50% 2.55%	8.79µs 16.8µs 4.75µs 3.84µs 470ns	863MiB 0.00B 209MiB 124MiB 10.1MiB	71.5% 0.00% 17.3% 10.3% 0.84%	9.30KiB 0.00B 6.27KiB 3.71KiB 112B	
heuristic score dequeue expand possibleactions create node	95.0k 34.2k 34.2k 34.2k 35.0k	835ms 574ms 162ms 131ms 44.6ms	47.7% 32.8% 9.28% 7.50% 2.55%	8.79µs 16.8µs 4.75µs 3.84µs 470ns	863MiB 0.00B 209MiB 124MiB 10.1MiB	71.5% 0.00% 17.3% 10.3% 0.84%	9.30KiB 0.00B 6.27KiB 3.71KiB 112B	

Section	ncalls	time	%tot	avg	alloc	%tot	avg	
heuristic score	 155k	1.54s	48.3%	10.0µs	1.37GiB	70.5%	9.27KiB	
dequeue	59.3k	1.09s	34.2%	10.0µs 18.4µs	0.00B	0.00%	0.00B	
expand	59.3k	263ms	8.24%	4.43μs	354MiB	17.8%	6.11KiB	
possibleactions	59.3k	216ms	6.76%	3.64µs	215MiB	10.8%	3.71KiB	
create node	155k	71.7ms	2.25%	3.04μs 464ns	16.5MiB	0.83%	112B	
push	59.3k	6.59ms	0.21%	111ns	1.00MiB	0.05%	17.7B	
	07.0K		0.21%		1.00111			 
rpuzzle-6*								
			Time		Al	locatio	ns	
Tot / % measu	ured:		Time ims / 55	. 6%		locatio —— MiB / 9		
	ured:			.6% avg				
Tot / % measo	ncalls	88.5	ms / 55 %tot	avg	31.9 alloc	MiB / 9 %tot	8.9% avg	
Tot / % measonsection	ncalls	88.5 time	%tot	avg 9.60µs	31.9 alloc 22.1MiB	MiB / 9 %tot 70.0%	8.9% avg 8.81KiB	
Tot / % measonsection  heuristic score dequeue	ncalls 2.56k 945	88.5 time 24.6ms 14.1ms	%tot 50.0% 28.8%	avg 9.60µs 15.0µs	31.9 alloc 22.1MiB 0.00B	MiB / 9 %tot 70.0% 0.00%	8.9% avg 8.81KiB 0.00B	
Tot / % measu Section  heuristic score dequeue expand	ncalls  2.56k 945 945	88.5 time 24.6ms 14.1ms 4.51ms	%tot 50.0% 28.8% 9.16%	avg 9.60µs 15.0µs 4.77µs	31.9 alloc 22.1MiB 0.00B 5.73MiB	MiB / 9 %tot  70.0% 0.00% 18.2%	8.9% avg 8.81KiB 0.00B 6.21KiB	
Tot / % measons Section  heuristic score dequeue expand possibleactions	ncalls  2.56k 945 945 945	88.5 time 24.6ms 14.1ms 4.51ms 3.82ms	50.0% 28.8% 9.16% 7.76%	9.60µs 15.0µs 4.77µs 4.04µs	31.9 alloc 22.1MiB 0.00B 5.73MiB 3.42MiB	MiB / 9 %tot  70.0% 0.00% 18.2% 10.9%	8.9% avg 8.81KiB 0.00B 6.21KiB 3.71KiB	
Tot / % measu Section  heuristic score dequeue expand	ncalls  2.56k 945 945	88.5 time 24.6ms 14.1ms 4.51ms	%tot 50.0% 28.8% 9.16%	avg 9.60µs 15.0µs 4.77µs	31.9 alloc 22.1MiB 0.00B 5.73MiB	MiB / 9 %tot  70.0% 0.00% 18.2%	8.9% avg 8.81KiB 0.00B 6.21KiB	

## **Solutions**

#### **Breadth-First Search**

```
*puzzle-2*
Step 21:
       [0, 1, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 20:
        [3, 1, 2]
       [0, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 19:
       [3, 1, 2]
       [6, 4, 5]
       [0, 7, 8]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 18:
       [3, 1, 2]
       [6, 4, 5]
       [7, 0, 8]
       Action: (CartesianIndex(3, 2), "UP")
Step 17:
       [3, 1, 2]
       [6, 0, 5]
       [7, 4, 8]
       Action: (CartesianIndex(2, 2), "UP")
Step 16:
       [3, 0, 2]
       [6, 1, 5]
       [7, 4, 8]
       Action: (CartesianIndex(1, 2), "LEFT")
Step 15:
       [0, 3, 2]
       [6, 1, 5]
       [7, 4, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 14:
       [6, 3, 2]
       [0, 1, 5]
       [7, 4, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 13:
       [6, 3, 2]
       [1, 0, 5]
       [7, 4, 8]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 12:
       [6, 3, 2]
       [1, 5, 0]
       [7, 4, 8]
       Action: (CartesianIndex(2, 3), "UP")
Step 11:
       [6, 3, 0]
```

```
[1, 5, 2]
        [7, 4, 8]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 10:
        [6, 0, 3]
        [1, 5, 2]
        [7, 4, 8]
       Action: (CartesianIndex(1, 2), "LEFT")
Step 9:
        [0, 6, 3]
        [1, 5, 2]
        [7, 4, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 8:
        [1, 6, 3]
        [0, 5, 2]
        [7, 4, 8]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 7:
        [1, 6, 3]
        [7, 5, 2]
        [0, 4, 8]
        Action: (CartesianIndex(3, 1), "RIGHT")
Step 6:
        [1, 6, 3]
        [7, 5, 2]
        [4, 0, 8]
       Action: (CartesianIndex(3, 2), "UP")
Step 5:
        [1, 6, 3]
        [7, 0, 2]
        [4, 5, 8]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 4:
        [1, 6, 3]
        [0, 7, 2]
        [4, 5, 8]
       Action: (CartesianIndex(2, 1), "UP")
Step 3:
        [0, 6, 3]
        [1, 7, 2]
        [4, 5, 8]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 2:
        [6, 0, 3]
        [1, 7, 2]
        [4, 5, 8]
        Action: (CartesianIndex(1, 2), "DOWN")
Step 1:
        [6, 7, 3]
        [1, 0, 2]
        [4, 5, 8]
        Action: (CartesianIndex(2, 2), "DOWN")
Step 0:
        [6, 7, 3]
        [1, 5, 2]
        [4, 0, 8]
        Action: nothing
```

```
*puzzle-3*
Step 24:
       [0, 1, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 23:
       [1, 0, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 22:
       [1, 4, 2]
       [3, 0, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 21:
       [1, 4, 2]
       [0, 3, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 20:
       [1, 4, 2]
       [6, 3, 5]
       [0, 7, 8]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 19:
       [1, 4, 2]
       [6, 3, 5]
       [7, 0, 8]
       Action: (CartesianIndex(3, 2), "UP")
Step 18:
       [1, 4, 2]
       [6, 0, 5]
       [7, 3, 8]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 17:
       [1, 4, 2]
       [6, 5, 0]
       [7, 3, 8]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 16:
       [1, 4, 2]
       [6, 5, 8]
       [7, 3, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 15:
       [1, 4, 2]
       [6, 5, 8]
       [7, 0, 3]
       Action: (CartesianIndex(3, 2), "UP")
Step 14:
       [1, 4, 2]
       [6, 0, 8]
       [7, 5, 3]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 13:
       [1, 4, 2]
       [0, 6, 8]
```

```
[7, 5, 3]
       Action: (CartesianIndex(2, 1), "UP")
Step 12:
       [0, 4, 2]
       [1, 6, 8]
       [7, 5, 3]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 11:
       [4, 0, 2]
       [1, 6, 8]
       [7, 5, 3]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 10:
       [4, 2, 0]
        [1, 6, 8]
       [7, 5, 3]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 9:
       [4, 2, 8]
       [1, 6, 0]
       [7, 5, 3]
       Action: (CartesianIndex(2, 3), "LEFT")
Step 8:
       [4, 2, 8]
       [1, 0, 6]
       [7, 5, 3]
       Action: (CartesianIndex(2, 2), "UP")
Step 7:
       [4, 0, 8]
       [1, 2, 6]
       [7, 5, 3]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 6:
       [4, 8, 0]
       [1, 2, 6]
       [7, 5, 3]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 5:
       [4, 8, 6]
       [1, 2, 0]
       [7, 5, 3]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 4:
       [4, 8, 6]
       [1, 2, 3]
       [7, 5, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 3:
       [4, 8, 6]
       [1, 2, 3]
       [7, 0, 5]
       Action: (CartesianIndex(3, 2), "UP")
Step 2:
       [4, 8, 6]
        [1, 0, 3]
       [7, 2, 5]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 1:
        [4, 8, 6]
```

```
[0, 1, 3]
       [7, 2, 5]
       Action: (CartesianIndex(2, 1), "UP")
Step 0:
       [0, 8, 6]
       [4, 1, 3]
       [7, 2, 5]
       Action: nothing
*puzzle-4*
Step 22:
       [0, 1, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 21:
       [3, 1, 2]
       [0, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 20:
       [3, 1, 2]
       [4, 0, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "UP")
Step 19:
       [3, 0, 2]
       [4, 1, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 18:
       [3, 2, 0]
       [4, 1, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 17:
       [3, 2, 5]
       [4, 1, 0]
       [6, 7, 8]
       Action: (CartesianIndex(2, 3), "LEFT")
Step 16:
       [3, 2, 5]
       [4, 0, 1]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 15:
       [3, 2, 5]
       [0, 4, 1]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "UP")
Step 14:
       [0, 2, 5]
       [3, 4, 1]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 13:
       [2, 0, 5]
       [3, 4, 1]
       [6, 7, 8]
```

```
Action: (CartesianIndex(1, 2), "DOWN")
Step 12:
       [2, 4, 5]
       [3, 0, 1]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "DOWN")
Step 11:
       [2, 4, 5]
       [3, 7, 1]
       [6, 0, 8]
       Action: (CartesianIndex(3, 2), "RIGHT")
Step 10:
       [2, 4, 5]
       [3, 7, 1]
       [6, 8, 0]
       Action: (CartesianIndex(3, 3), "UP")
Step 9:
       [2, 4, 5]
       [3, 7, 0]
       [6, 8, 1]
       Action: (CartesianIndex(2, 3), "UP")
Step 8:
       [2, 4, 0]
       [3, 7, 5]
       [6, 8, 1]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 7:
       [2, 0, 4]
       [3, 7, 5]
       [6, 8, 1]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 6:
       [2, 7, 4]
       [3, 0, 5]
       [6, 8, 1]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 5:
       [2, 7, 4]
       [0, 3, 5]
        [6, 8, 1]
       Action: (CartesianIndex(2, 1), "UP")
Step 4:
       [0, 7, 4]
       [2, 3, 5]
       [6, 8, 1]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 3:
       [7, 0, 4]
       [2, 3, 5]
       [6, 8, 1]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 2:
       [7, 3, 4]
       [2, 0, 5]
       [6, 8, 1]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 1:
       [7, 3, 4]
       [2, 5, 0]
```

```
[6, 8, 1]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 0:
       [7, 3, 4]
       [2, 5, 1]
       [6, 8, 0]
       Action: nothing
*puzzle-5*
Step 23:
       [0, 1, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 22:
       [3, 1, 2]
       [0, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 21:
       [3, 1, 2]
       [4, 0, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 20:
       [3, 1, 2]
       [4, 5, 0]
       [6, 7, 8]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 19:
        [3, 1, 2]
        [4, 5, 8]
       [6, 7, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 18:
       [3, 1, 2]
       [4, 5, 8]
       [6, 0, 7]
       Action: (CartesianIndex(3, 2), "LEFT")
Step 17:
       [3, 1, 2]
       [4, 5, 8]
       [0, 6, 7]
       Action: (CartesianIndex(3, 1), "UP")
Step 16:
       [3, 1, 2]
       [0, 5, 8]
       [4, 6, 7]
       Action: (CartesianIndex(2, 1), "UP")
Step 15:
       [0, 1, 2]
       [3, 5, 8]
       [4, 6, 7]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 14:
       [1, 0, 2]
       [3, 5, 8]
       [4, 6, 7]
       Action: (CartesianIndex(1, 2), "DOWN")
```

```
Step 13:
        [1, 5, 2]
        [3, 0, 8]
       [4, 6, 7]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 12:
        [1, 5, 2]
        [3, 8, 0]
        [4, 6, 7]
       Action: (CartesianIndex(2, 3), "UP")
Step 11:
        [1, 5, 0]
        [3, 8, 2]
        [4, 6, 7]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 10:
       [1, 0, 5]
       [3, 8, 2]
        [4, 6, 7]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 9:
        [1, 8, 5]
        [3, 0, 2]
        [4, 6, 7]
        Action: (CartesianIndex(2, 2), "LEFT")
Step 8:
       [1, 8, 5]
        [0, 3, 2]
        [4, 6, 7]
        Action: (CartesianIndex(2, 1), "DOWN")
Step 7:
        [1, 8, 5]
        [4, 3, 2]
        [0, 6, 7]
        Action: (CartesianIndex(3, 1), "RIGHT")
Step 6:
        [1, 8, 5]
        [4, 3, 2]
        [6, 0, 7]
       Action: (CartesianIndex(3, 2), "RIGHT")
Step 5:
        [1, 8, 5]
        [4, 3, 2]
        [6, 7, 0]
        Action: (CartesianIndex(3, 3), "UP")
Step 4:
        [1, 8, 5]
        [4, 3, 0]
        [6, 7, 2]
        Action: (CartesianIndex(2, 3), "UP")
Step 3:
        [1, 8, 0]
        [4, 3, 5]
        [6, 7, 2]
        Action: (CartesianIndex(1, 3), "LEFT")
Step 2:
        [1, 0, 8]
        [4, 3, 5]
        [6, 7, 2]
```

```
Action: (CartesianIndex(1, 2), "DOWN")
Step 1:
       [1, 3, 8]
       [4, 0, 5]
       [6, 7, 2]
       Action: (CartesianIndex(2, 2), "DOWN")
Step 0:
       [1, 3, 8]
       [4, 7, 5]
       [6, 0, 2]
       Action: nothing
A* with Manhattan Distance
       [0, 1, 2]
       [3, 4, 5]
```

```
*puzzle-2*
Step 21:
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 20:
       [3, 1, 2]
       [0, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 19:
       [3, 1, 2]
       [4, 0, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "DOWN")
Step 18:
       [3, 1, 2]
       [4, 7, 5]
       [6, 0, 8]
       Action: (CartesianIndex(3, 2), "LEFT")
Step 17:
       [3, 1, 2]
       [4, 7, 5]
       [0, 6, 8]
       Action: (CartesianIndex(3, 1), "UP")
Step 16:
       [3, 1, 2]
       [0, 7, 5]
       [4, 6, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 15:
       [3, 1, 2]
       [7, 0, 5]
       [4, 6, 8]
       Action: (CartesianIndex(2, 2), "UP")
Step 14:
       [3, 0, 2]
       [7, 1, 5]
       [4, 6, 8]
       Action: (CartesianIndex(1, 2), "LEFT")
Step 13:
       [0, 3, 2]
       [7, 1, 5]
```

```
[4, 6, 8]
        Action: (CartesianIndex(1, 1), "DOWN")
Step 12:
        [7, 3, 2]
        [0, 1, 5]
        [4, 6, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 11:
        [7, 3, 2]
        [1, 0, 5]
        [4, 6, 8]
        Action: (CartesianIndex(2, 2), "DOWN")
Step 10:
        [7, 3, 2]
        [1, 6, 5]
        [4, 0, 8]
        Action: (CartesianIndex(3, 2), "LEFT")
Step 9:
        [7, 3, 2]
        [1, 6, 5]
        [0, 4, 8]
        Action: (CartesianIndex(3, 1), "UP")
Step 8:
       [7, 3, 2]
        [0, 6, 5]
        [1, 4, 8]
        Action: (CartesianIndex(2, 1), "RIGHT")
Step 7:
        [7, 3, 2]
        [6, 0, 5]
        [1, 4, 8]
        Action: (CartesianIndex(2, 2), "RIGHT")
Step 6:
       [7, 3, 2]
        [6, 5, 0]
        [1, 4, 8]
        Action: (CartesianIndex(2, 3), "UP")
Step 5:
        [7, 3, 0]
        [6, 5, 2]
        [1, 4, 8]
        Action: (CartesianIndex(1, 3), "LEFT")
Step 4:
        [7, 0, 3]
        [6, 5, 2]
        [1, 4, 8]
        Action: (CartesianIndex(1, 2), "LEFT")
Step 3:
        [0, 7, 3]
        [6, 5, 2]
        [1, 4, 8]
        Action: (CartesianIndex(1, 1), "DOWN")
Step 2:
        [6, 7, 3]
        [0, 5, 2]
        [1, 4, 8]
        Action: (CartesianIndex(2, 1), "DOWN")
Step 1:
        [6, 7, 3]
```

```
[1, 5, 2]
       [0, 4, 8]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 0:
       [6, 7, 3]
       [1, 5, 2]
       [4, 0, 8]
       Action: nothing
*puzzle-3*
Step 24:
       [0, 1, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 23:
       [1, 0, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 22:
       [1, 4, 2]
       [3, 0, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 21:
       [1, 4, 2]
       [0, 3, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 20:
       [1, 4, 2]
       [6, 3, 5]
       [0, 7, 8]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 19:
       [1, 4, 2]
       [6, 3, 5]
       [7, 0, 8]
       Action: (CartesianIndex(3, 2), "UP")
Step 18:
       [1, 4, 2]
       [6, 0, 5]
       [7, 3, 8]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 17:
       [1, 4, 2]
       [6, 5, 0]
       [7, 3, 8]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 16:
       [1, 4, 2]
       [6, 5, 8]
       [7, 3, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 15:
       [1, 4, 2]
       [6, 5, 8]
       [7, 0, 3]
```

```
Action: (CartesianIndex(3, 2), "UP")
Step 14:
       [1, 4, 2]
       [6, 0, 8]
       [7, 5, 3]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 13:
       [1, 4, 2]
       [0, 6, 8]
       [7, 5, 3]
       Action: (CartesianIndex(2, 1), "UP")
Step 12:
       [0, 4, 2]
       [1, 6, 8]
       [7, 5, 3]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 11:
       [4, 0, 2]
       [1, 6, 8]
       [7, 5, 3]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 10:
       [4, 2, 0]
       [1, 6, 8]
       [7, 5, 3]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 9:
        [4, 2, 8]
       [1, 6, 0]
       [7, 5, 3]
       Action: (CartesianIndex(2, 3), "LEFT")
Step 8:
       [4, 2, 8]
       [1, 0, 6]
       [7, 5, 3]
       Action: (CartesianIndex(2, 2), "UP")
Step 7:
       [4, 0, 8]
       [1, 2, 6]
       [7, 5, 3]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 6:
       [4, 8, 0]
       [1, 2, 6]
       [7, 5, 3]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 5:
       [4, 8, 6]
       [1, 2, 0]
       [7, 5, 3]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 4:
       [4, 8, 6]
       [1, 2, 3]
       [7, 5, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 3:
       [4, 8, 6]
       [1, 2, 3]
```

```
[7, 0, 5]
       Action: (CartesianIndex(3, 2), "UP")
Step 2:
       [4, 8, 6]
       [1, 0, 3]
       [7, 2, 5]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 1:
       [4, 8, 6]
       [0, 1, 3]
       [7, 2, 5]
       Action: (CartesianIndex(2, 1), "UP")
Step 0:
       [0, 8, 6]
       [4, 1, 3]
       [7, 2, 5]
       Action: nothing
*puzzle-4*
Step 22:
       [0, 1, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 21:
       [3, 1, 2]
       [0, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 20:
       [3, 1, 2]
       [4, 0, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "UP")
Step 19:
       [3, 0, 2]
       [4, 1, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 18:
       [3, 2, 0]
       [4, 1, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 17:
       [3, 2, 5]
       [4, 1, 0]
       [6, 7, 8]
       Action: (CartesianIndex(2, 3), "LEFT")
Step 16:
       [3, 2, 5]
       [4, 0, 1]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 15:
       [3, 2, 5]
       [0, 4, 1]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "UP")
```

```
Step 14:
        [0, 2, 5]
        [3, 4, 1]
        [6, 7, 8]
        Action: (CartesianIndex(1, 1), "RIGHT")
Step 13:
        [2, 0, 5]
        [3, 4, 1]
        [6, 7, 8]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 12:
        [2, 4, 5]
        [3, 0, 1]
        [6, 7, 8]
       Action: (CartesianIndex(2, 2), "DOWN")
Step 11:
       [2, 4, 5]
        [3, 7, 1]
        [6, 0, 8]
        Action: (CartesianIndex(3, 2), "RIGHT")
Step 10:
        [2, 4, 5]
        [3, 7, 1]
        [6, 8, 0]
        Action: (CartesianIndex(3, 3), "UP")
Step 9:
       [2, 4, 5]
        [3, 7, 0]
        [6, 8, 1]
        Action: (CartesianIndex(2, 3), "UP")
Step 8:
        [2, 4, 0]
        [3, 7, 5]
        [6, 8, 1]
        Action: (CartesianIndex(1, 3), "LEFT")
Step 7:
        [2, 0, 4]
        [3, 7, 5]
        [6, 8, 1]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 6:
        [2, 7, 4]
        [3, 0, 5]
        [6, 8, 1]
        Action: (CartesianIndex(2, 2), "LEFT")
Step 5:
        [2, 7, 4]
        [0, 3, 5]
        [6, 8, 1]
       Action: (CartesianIndex(2, 1), "UP")
Step 4:
        [0, 7, 4]
        [2, 3, 5]
        [6, 8, 1]
        Action: (CartesianIndex(1, 1), "RIGHT")
Step 3:
        [7, 0, 4]
        [2, 3, 5]
        [6, 8, 1]
```

```
Action: (CartesianIndex(1, 2), "DOWN")
Step 2:
       [7, 3, 4]
       [2, 0, 5]
       [6, 8, 1]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 1:
       [7, 3, 4]
       [2, 5, 0]
       [6, 8, 1]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 0:
       [7, 3, 4]
       [2, 5, 1]
       [6, 8, 0]
       Action: nothing
*puzzle-5*
Step 23:
       [0, 1, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 22:
       [3, 1, 2]
       [0, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 21:
       [3, 1, 2]
       [4, 0, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 20:
       [3, 1, 2]
       [4, 5, 0]
       [6, 7, 8]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 19:
       [3, 1, 2]
       [4, 5, 8]
       [6, 7, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 18:
       [3, 1, 2]
       [4, 5, 8]
       [6, 0, 7]
       Action: (CartesianIndex(3, 2), "LEFT")
Step 17:
       [3, 1, 2]
       [4, 5, 8]
       [0, 6, 7]
       Action: (CartesianIndex(3, 1), "UP")
Step 16:
       [3, 1, 2]
       [0, 5, 8]
       [4, 6, 7]
       Action: (CartesianIndex(2, 1), "UP")
Step 15:
```

```
[0, 1, 2]
       [3, 5, 8]
       [4, 6, 7]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 14:
       [1, 0, 2]
       [3, 5, 8]
       [4, 6, 7]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 13:
       [1, 5, 2]
       [3, 0, 8]
       [4, 6, 7]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 12:
       [1, 5, 2]
       [3, 8, 0]
       [4, 6, 7]
       Action: (CartesianIndex(2, 3), "UP")
Step 11:
       [1, 5, 0]
       [3, 8, 2]
       [4, 6, 7]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 10:
       [1, 0, 5]
       [3, 8, 2]
       [4, 6, 7]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 9:
       [1, 8, 5]
       [3, 0, 2]
       [4, 6, 7]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 8:
       [1, 8, 5]
       [0, 3, 2]
       [4, 6, 7]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 7:
       [1, 8, 5]
       [4, 3, 2]
       [0, 6, 7]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 6:
       [1, 8, 5]
       [4, 3, 2]
       [6, 0, 7]
       Action: (CartesianIndex(3, 2), "RIGHT")
Step 5:
       [1, 8, 5]
       [4, 3, 2]
       [6, 7, 0]
       Action: (CartesianIndex(3, 3), "UP")
Step 4:
       [1, 8, 5]
       [4, 3, 0]
       [6, 7, 2]
       Action: (CartesianIndex(2, 3), "UP")
```

```
Step 3:
        [1, 8, 0]
        [4, 3, 5]
        [6, 7, 2]
        Action: (CartesianIndex(1, 3), "LEFT")
Step 2:
        [1, 0, 8]
        [4, 3, 5]
        [6, 7, 2]
        Action: (CartesianIndex(1, 2), "DOWN")
Step 1:
        [1, 3, 8]
        [4, 0, 5]
        [6, 7, 2]
        Action: (CartesianIndex(2, 2), "DOWN")
Step 0:
       [1, 3, 8]
        [4, 7, 5]
        [6, 0, 2]
       Action: nothing
*puzzle-6*
Step 28:
        [0, 1, 2]
        [3, 4, 5]
        [6, 7, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 27:
        [3, 1, 2]
        [0, 4, 5]
        [6, 7, 8]
        Action: (CartesianIndex(2, 1), "DOWN")
Step 26:
       [3, 1, 2]
        [6, 4, 5]
        [0, 7, 8]
        Action: (CartesianIndex(3, 1), "RIGHT")
Step 25:
       [3, 1, 2]
        [6, 4, 5]
        [7, 0, 8]
        Action: (CartesianIndex(3, 2), "RIGHT")
Step 24:
       [3, 1, 2]
        [6, 4, 5]
        [7, 8, 0]
        Action: (CartesianIndex(3, 3), "UP")
Step 23:
        [3, 1, 2]
        [6, 4, 0]
        [7, 8, 5]
        Action: (CartesianIndex(2, 3), "UP")
Step 22:
        [3, 1, 0]
        [6, 4, 2]
        [7, 8, 5]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 21:
        [3, 0, 1]
```

```
[6, 4, 2]
       [7, 8, 5]
       Action: (CartesianIndex(1, 2), "LEFT")
Step 20:
        [0, 3, 1]
       [6, 4, 2]
        [7, 8, 5]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 19:
       [6, 3, 1]
       [0, 4, 2]
       [7, 8, 5]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 18:
       [6, 3, 1]
       [7, 4, 2]
       [0, 8, 5]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 17:
       [6, 3, 1]
       [7, 4, 2]
       [8, 0, 5]
       Action: (CartesianIndex(3, 2), "RIGHT")
Step 16:
       [6, 3, 1]
       [7, 4, 2]
       [8, 5, 0]
       Action: (CartesianIndex(3, 3), "UP")
Step 15:
       [6, 3, 1]
       [7, 4, 0]
       [8, 5, 2]
       Action: (CartesianIndex(2, 3), "UP")
Step 14:
        [6, 3, 0]
       [7, 4, 1]
       [8, 5, 2]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 13:
       [6, 0, 3]
       [7, 4, 1]
       [8, 5, 2]
       Action: (CartesianIndex(1, 2), "LEFT")
Step 12:
       [0, 6, 3]
       [7, 4, 1]
       [8, 5, 2]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 11:
       [7, 6, 3]
       [0, 4, 1]
       [8, 5, 2]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 10:
       [7, 6, 3]
       [8, 4, 1]
       [0, 5, 2]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 9:
```

```
[7, 6, 3]
       [8, 4, 1]
       [5, 0, 2]
       Action: (CartesianIndex(3, 2), "RIGHT")
Step 8:
       [7, 6, 3]
       [8, 4, 1]
       [5, 2, 0]
       Action: (CartesianIndex(3, 3), "UP")
Step 7:
       [7, 6, 3]
       [8, 4, 0]
       [5, 2, 1]
       Action: (CartesianIndex(2, 3), "UP")
Step 6:
       [7, 6, 0]
       [8, 4, 3]
       [5, 2, 1]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 5:
        [7, 0, 6]
        [8, 4, 3]
       [5, 2, 1]
       Action: (CartesianIndex(1, 2), "LEFT")
Step 4:
       [0, 7, 6]
       [8, 4, 3]
       [5, 2, 1]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 3:
       [8, 7, 6]
       [0, 4, 3]
       [5, 2, 1]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 2:
       [8, 7, 6]
       [5, 4, 3]
       [0, 2, 1]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 1:
       [8, 7, 6]
       [5, 4, 3]
       [2, 0, 1]
       Action: (CartesianIndex(3, 2), "RIGHT")
Step 0:
       [8, 7, 6]
       [5, 4, 3]
       [2, 1, 0]
       Action: nothing
```

### A\* with Manhattan Distance and Linear Conflict

```
*puzzle-2*
Step 21:
        [0, 1, 2]
        [3, 4, 5]
        [6, 7, 8]
        Action: (CartesianIndex(1, 1), "DOWN")
```

```
Step 20:
        [3, 1, 2]
       [0, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 19:
       [3, 1, 2]
       [6, 4, 5]
       [0, 7, 8]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 18:
       [3, 1, 2]
       [6, 4, 5]
       [7, 0, 8]
       Action: (CartesianIndex(3, 2), "UP")
Step 17:
       [3, 1, 2]
       [6, 0, 5]
       [7, 4, 8]
       Action: (CartesianIndex(2, 2), "UP")
Step 16:
       [3, 0, 2]
       [6, 1, 5]
       [7, 4, 8]
       Action: (CartesianIndex(1, 2), "LEFT")
Step 15:
       [0, 3, 2]
       [6, 1, 5]
       [7, 4, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 14:
       [6, 3, 2]
       [0, 1, 5]
       [7, 4, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 13:
       [6, 3, 2]
       [1, 0, 5]
       [7, 4, 8]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 12:
       [6, 3, 2]
       [1, 5, 0]
       [7, 4, 8]
       Action: (CartesianIndex(2, 3), "UP")
Step 11:
       [6, 3, 0]
       [1, 5, 2]
       [7, 4, 8]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 10:
       [6, 0, 3]
       [1, 5, 2]
       [7, 4, 8]
       Action: (CartesianIndex(1, 2), "LEFT")
Step 9:
       [0, 6, 3]
       [1, 5, 2]
       [7, 4, 8]
```

```
Action: (CartesianIndex(1, 1), "DOWN")
Step 8:
       [1, 6, 3]
       [0, 5, 2]
       [7, 4, 8]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 7:
       [1, 6, 3]
       [7, 5, 2]
       [0, 4, 8]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 6:
       [1, 6, 3]
       [7, 5, 2]
       [4, 0, 8]
       Action: (CartesianIndex(3, 2), "UP")
Step 5:
       [1, 6, 3]
       [7, 0, 2]
       [4, 5, 8]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 4:
       [1, 6, 3]
       [0, 7, 2]
       [4, 5, 8]
       Action: (CartesianIndex(2, 1), "UP")
Step 3:
       [0, 6, 3]
       [1, 7, 2]
       [4, 5, 8]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 2:
       [6, 0, 3]
       [1, 7, 2]
       [4, 5, 8]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 1:
       [6, 7, 3]
       [1, 0, 2]
       [4, 5, 8]
       Action: (CartesianIndex(2, 2), "DOWN")
Step 0:
       [6, 7, 3]
       [1, 5, 2]
       [4, 0, 8]
       Action: nothing
*puzzle-3*
Step 24:
       [0, 1, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 23:
       [1, 0, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 22:
```

```
[1, 4, 2]
       [3, 0, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 21:
       [1, 4, 2]
       [0, 3, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "DOWN")
Step 20:
       [1, 4, 2]
       [6, 3, 5]
       [0, 7, 8]
       Action: (CartesianIndex(3, 1), "RIGHT")
Step 19:
       [1, 4, 2]
       [6, 3, 5]
       [7, 0, 8]
       Action: (CartesianIndex(3, 2), "RIGHT")
Step 18:
        [1, 4, 2]
        [6, 3, 5]
       [7, 8, 0]
       Action: (CartesianIndex(3, 3), "UP")
Step 17:
       [1, 4, 2]
       [6, 3, 0]
       [7, 8, 5]
       Action: (CartesianIndex(2, 3), "LEFT")
Step 16:
       [1, 4, 2]
       [6, 0, 3]
       [7, 8, 5]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 15:
       [1, 4, 2]
       [0, 6, 3]
       [7, 8, 5]
       Action: (CartesianIndex(2, 1), "UP")
Step 14:
       [0, 4, 2]
       [1, 6, 3]
       [7, 8, 5]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 13:
       [4, 0, 2]
       [1, 6, 3]
       [7, 8, 5]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 12:
       [4, 6, 2]
       [1, 0, 3]
       [7, 8, 5]
       Action: (CartesianIndex(2, 2), "DOWN")
Step 11:
       [4, 6, 2]
       [1, 8, 3]
       [7, 0, 5]
       Action: (CartesianIndex(3, 2), "RIGHT")
```

```
Step 10:
        [4, 6, 2]
        [1, 8, 3]
        [7, 5, 0]
       Action: (CartesianIndex(3, 3), "UP")
Step 9:
        [4, 6, 2]
        [1, 8, 0]
        [7, 5, 3]
       Action: (CartesianIndex(2, 3), "UP")
Step 8:
        [4, 6, 0]
        [1, 8, 2]
        [7, 5, 3]
        Action: (CartesianIndex(1, 3), "LEFT")
Step 7:
       [4, 0, 6]
        [1, 8, 2]
        [7, 5, 3]
        Action: (CartesianIndex(1, 2), "DOWN")
Step 6:
        [4, 8, 6]
        [1, 0, 2]
        [7, 5, 3]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 5:
       [4, 8, 6]
        [1, 2, 0]
        [7, 5, 3]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 4:
        [4, 8, 6]
        [1, 2, 3]
        [7, 5, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 3:
        [4, 8, 6]
        [1, 2, 3]
        [7, 0, 5]
       Action: (CartesianIndex(3, 2), "UP")
Step 2:
        [4, 8, 6]
        [1, 0, 3]
       [7, 2, 5]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 1:
        [4, 8, 6]
        [0, 1, 3]
        [7, 2, 5]
       Action: (CartesianIndex(2, 1), "UP")
Step 0:
        [0, 8, 6]
        [4, 1, 3]
        [7, 2, 5]
       Action: nothing
*puzzle-4*
Step 22:
        [0, 1, 2]
```

```
[3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 21:
       [3, 1, 2]
       [0, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 20:
       [3, 1, 2]
       [4, 0, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "UP")
Step 19:
       [3, 0, 2]
       [4, 1, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 18:
       [3, 2, 0]
       [4, 1, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 17:
       [3, 2, 5]
       [4, 1, 0]
       [6, 7, 8]
       Action: (CartesianIndex(2, 3), "LEFT")
Step 16:
       [3, 2, 5]
       [4, 0, 1]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 15:
       [3, 2, 5]
       [0, 4, 1]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "UP")
Step 14:
       [0, 2, 5]
       [3, 4, 1]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 13:
       [2, 0, 5]
       [3, 4, 1]
       [6, 7, 8]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 12:
       [2, 4, 5]
       [3, 0, 1]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "DOWN")
Step 11:
       [2, 4, 5]
       [3, 7, 1]
       [6, 0, 8]
       Action: (CartesianIndex(3, 2), "RIGHT")
Step 10:
```

```
[2, 4, 5]
       [3, 7, 1]
       [6, 8, 0]
       Action: (CartesianIndex(3, 3), "UP")
Step 9:
       [2, 4, 5]
       [3, 7, 0]
       [6, 8, 1]
       Action: (CartesianIndex(2, 3), "UP")
Step 8:
       [2, 4, 0]
       [3, 7, 5]
       [6, 8, 1]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 7:
       [2, 0, 4]
       [3, 7, 5]
       [6, 8, 1]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 6:
        [2, 7, 4]
        [3, 0, 5]
       [6, 8, 1]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 5:
       [2, 7, 4]
       [0, 3, 5]
       [6, 8, 1]
       Action: (CartesianIndex(2, 1), "UP")
Step 4:
       [0, 7, 4]
       [2, 3, 5]
       [6, 8, 1]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 3:
       [7, 0, 4]
       [2, 3, 5]
       [6, 8, 1]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 2:
       [7, 3, 4]
       [2, 0, 5]
       [6, 8, 1]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 1:
       [7, 3, 4]
       [2, 5, 0]
       [6, 8, 1]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 0:
       [7, 3, 4]
       [2, 5, 1]
       [6, 8, 0]
       Action: nothing
*puzzle-5*
Step 23:
       [0, 1, 2]
       [3, 4, 5]
```

```
[6, 7, 8]
       Action: (CartesianIndex(1, 1), "DOWN")
Step 22:
       [3, 1, 2]
       [0, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 1), "RIGHT")
Step 21:
       [3, 1, 2]
       [4, 0, 5]
       [6, 7, 8]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 20:
       [3, 1, 2]
       [4, 5, 0]
       [6, 7, 8]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 19:
       [3, 1, 2]
       [4, 5, 8]
       [6, 7, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 18:
       [3, 1, 2]
       [4, 5, 8]
       [6, 0, 7]
       Action: (CartesianIndex(3, 2), "LEFT")
Step 17:
       [3, 1, 2]
       [4, 5, 8]
       [0, 6, 7]
       Action: (CartesianIndex(3, 1), "UP")
Step 16:
       [3, 1, 2]
       [0, 5, 8]
       [4, 6, 7]
       Action: (CartesianIndex(2, 1), "UP")
Step 15:
       [0, 1, 2]
       [3, 5, 8]
       [4, 6, 7]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 14:
       [1, 0, 2]
       [3, 5, 8]
       [4, 6, 7]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 13:
       [1, 5, 2]
       [3, 0, 8]
       [4, 6, 7]
       Action: (CartesianIndex(2, 2), "RIGHT")
Step 12:
       [1, 5, 2]
       [3, 8, 0]
       [4, 6, 7]
       Action: (CartesianIndex(2, 3), "UP")
Step 11:
       [1, 5, 0]
```

```
[3, 8, 2]
        [4, 6, 7]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 10:
        [1, 0, 5]
        [3, 8, 2]
        [4, 6, 7]
       Action: (CartesianIndex(1, 2), "DOWN")
Step 9:
       [1, 8, 5]
        [3, 0, 2]
        [4, 6, 7]
       Action: (CartesianIndex(2, 2), "LEFT")
Step 8:
        [1, 8, 5]
        [0, 3, 2]
        [4, 6, 7]
        Action: (CartesianIndex(2, 1), "DOWN")
Step 7:
        [1, 8, 5]
        [4, 3, 2]
        [0, 6, 7]
        Action: (CartesianIndex(3, 1), "RIGHT")
Step 6:
        [1, 8, 5]
        [4, 3, 2]
        [6, 0, 7]
       Action: (CartesianIndex(3, 2), "RIGHT")
Step 5:
        [1, 8, 5]
        [4, 3, 2]
        [6, 7, 0]
       Action: (CartesianIndex(3, 3), "UP")
Step 4:
        [1, 8, 5]
        [4, 3, 0]
        [6, 7, 2]
       Action: (CartesianIndex(2, 3), "UP")
Step 3:
        [1, 8, 0]
        [4, 3, 5]
        [6, 7, 2]
       Action: (CartesianIndex(1, 3), "LEFT")
Step 2:
        [1, 0, 8]
        [4, 3, 5]
        [6, 7, 2]
        Action: (CartesianIndex(1, 2), "DOWN")
Step 1:
        [1, 3, 8]
        [4, 0, 5]
        [6, 7, 2]
        Action: (CartesianIndex(2, 2), "DOWN")
Step 0:
        [1, 3, 8]
        [4, 7, 5]
        [6, 0, 2]
        Action: nothing
```

```
*puzzle-6*
Step 28:
       [0, 1, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 27:
       [1, 0, 2]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 26:
       [1, 2, 0]
       [3, 4, 5]
       [6, 7, 8]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 25:
       [1, 2, 5]
       [3, 4, 0]
       [6, 7, 8]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 24:
       [1, 2, 5]
       [3, 4, 8]
       [6, 7, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 23:
       [1, 2, 5]
       [3, 4, 8]
       [6, 0, 7]
       Action: (CartesianIndex(3, 2), "LEFT")
Step 22:
       [1, 2, 5]
       [3, 4, 8]
       [0, 6, 7]
       Action: (CartesianIndex(3, 1), "UP")
Step 21:
       [1, 2, 5]
       [0, 4, 8]
       [3, 6, 7]
       Action: (CartesianIndex(2, 1), "UP")
Step 20:
       [0, 2, 5]
       [1, 4, 8]
       [3, 6, 7]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 19:
       [2, 0, 5]
       [1, 4, 8]
       [3, 6, 7]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 18:
       [2, 5, 0]
       [1, 4, 8]
       [3, 6, 7]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 17:
       [2, 5, 8]
       [1, 4, 0]
```

```
[3, 6, 7]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 16:
       [2, 5, 8]
       [1, 4, 7]
       [3, 6, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 15:
       [2, 5, 8]
       [1, 4, 7]
       [3, 0, 6]
       Action: (CartesianIndex(3, 2), "LEFT")
Step 14:
       [2, 5, 8]
        [1, 4, 7]
       [0, 3, 6]
       Action: (CartesianIndex(3, 1), "UP")
Step 13:
       [2, 5, 8]
       [0, 4, 7]
       [1, 3, 6]
       Action: (CartesianIndex(2, 1), "UP")
Step 12:
       [0, 5, 8]
       [2, 4, 7]
       [1, 3, 6]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 11:
       [5, 0, 8]
       [2, 4, 7]
       [1, 3, 6]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 10:
       [5, 8, 0]
       [2, 4, 7]
       [1, 3, 6]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 9:
       [5, 8, 7]
       [2, 4, 0]
       [1, 3, 6]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 8:
       [5, 8, 7]
       [2, 4, 6]
       [1, 3, 0]
       Action: (CartesianIndex(3, 3), "LEFT")
Step 7:
       [5, 8, 7]
       [2, 4, 6]
       [1, 0, 3]
       Action: (CartesianIndex(3, 2), "LEFT")
Step 6:
       [5, 8, 7]
        [2, 4, 6]
       [0, 1, 3]
       Action: (CartesianIndex(3, 1), "UP")
Step 5:
       [5, 8, 7]
```

```
[0, 4, 6]
       [2, 1, 3]
       Action: (CartesianIndex(2, 1), "UP")
Step 4:
       [0, 8, 7]
       [5, 4, 6]
       [2, 1, 3]
       Action: (CartesianIndex(1, 1), "RIGHT")
Step 3:
       [8, 0, 7]
       [5, 4, 6]
       [2, 1, 3]
       Action: (CartesianIndex(1, 2), "RIGHT")
Step 2:
       [8, 7, 0]
       [5, 4, 6]
       [2, 1, 3]
       Action: (CartesianIndex(1, 3), "DOWN")
Step 1:
       [8, 7, 6]
       [5, 4, 0]
       [2, 1, 3]
       Action: (CartesianIndex(2, 3), "DOWN")
Step 0:
       [8, 7, 6]
       [5, 4, 3]
       [2, 1, 0]
       Action: nothing
```