

Data Analytics Study Guide

Why Sample?

Most of Chapter 7 involves finding a statistical measure of a big data set like the mean, and then taking a small sample of the data and finding the mean again, and then comparing the two. Standard deviations, confidence intervals, all are about comparing the numbers we get from a small sample to the numbers we get from the entire data set. Why are we even doing this? If we have all the data, why sample at all?

1. In many cases 'all the data' is changing. Even if you have all the minute-to-minute stock prices for AAPL in your spreadsheet – that dataset is growing every minute. So is the weather data. It's never all in your sheet. You are always going to be sampling, like it or not. These are the statistical tools to do it accurately.
2. From sampling we learn how much **variability** exists between samples. If we took many random samples from the same data, how alike would they be? If you are trying to predict the future – the future data is going to be a 'sample' of the total data. How much will it vary from past samples?

Ch7_PracticeData.xlsm

The 'Actual Data' is the Employee | Salary | Training data from Chapter 7 of the book, expanded to 100 rows. I left my numbers in the sheet for clarity – make a copy, clear out the tables and overwrite them with your own experiments.

1. Start with Actual Data
2. Assign a random number to each row
3. Sort the rows
4. Take the top 30 rows → that's your Random Sample
5. Find the mean of that sample → \bar{x}
6. Find the proportion who said Yes → \bar{p}
7. Compare to the Actual Data

This gives you \bar{x} and \bar{p} for one sample – but it doesn't tell you about variance. Imagine there were 10,000 rows in Actual Data instead of 100. One 30-row sample doesn't tell us enough.

What is a Point Estimator (\bar{x} and \bar{p}) ?

Goal: find the population mean (μ) and proportion (p)

Problem: We don't have all the data (N) so we can't

Solution: Choose a random sample of size n and find the sample mean (\bar{x}) and the sample proportion (\bar{p}). These are called **point estimators**.

| <i>Population Parameter</i> | <i>Point Estimator</i> | <i>Example</i> |
|-----------------------------|-------------------------------|-------------------------------|
| μ (mean) | \bar{x} (sample mean) | \$40,000 avg salary |
| p (proportion) | \bar{p} (sample proportion) | 60% of respondents said 'Yes' |

Ch7_PracticeData.xlsm

What if you **repeated** the steps above 100 times, found 100 \bar{x} (or \bar{p}), and averaged them all together. An average of an average. The **RunSamples** macro generates 100 samples of 30 each and computes \bar{x} and \bar{p} for each sample.

1. Run the 'RandomSamples' Macro
2. Creates a new 'Results' tab with a random number, like 'Results_911'
3. Runs 100 times
4. Each iteration selects 30 row random sample from Actual Data
5. Calculates \bar{x} and \bar{p} for that sample

Range = width of data = largest value – smallest value

Buckets = how many 'ranges' we want to divide the data into

Interval = how 'big' each bucket is

Make a results table like this:

| RANGES | COUNT | FREQUENCY |
|--------|-------|-----------|
| 66600 | | |
| 67604 | | |
| 68608 | | |
| 69613 | | |
| 70617 | | |
| 71621 | | |
| 72625 | | |
| 73630 | | |
| 74634 | | |
| 75638 | | |
| 77000 | | |
| Totals | 0 | 0% |

In the **Count** column use Excel Function to make a Frequency Distribution
=FREQUENCY(<xbar or pbar column> , <ranges column>)

This is a **Relative Frequency Distribution** for the 100 values of xbar (or pbar). It tells us what percentage of the means fell within each range during the trial runs – and for any ‘trial run’ in the future which buckets the mean will *probably* fall into.

RandomSamples runs 100 times. The problem is, there are *many* more than 100 different combinations:

Because there are so many possible samples, any one sample we generate will be arbitrary. Any value for \bar{x} and \bar{p} will be a **random number** which may or may not match the actual population parameter. So in addition to a value for \bar{x} and \bar{p} we have:

Standard Deviation of \bar{x}

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} \quad (7.2)$$

Infinite Population

$$\sigma_{\bar{p}} = \sqrt{\frac{p(1-p)}{n}} \quad (7.5)$$

Then: across all possible random samples of size 30 from our population of 100, the sample mean \bar{x} is expected to vary by ± 2 units from the population mean μ .

But: The right sides of the equations require the population standard deviation (σ) and the actual population proportion (p)

So: We use.....

2. *Estimated* standard deviation

Because we often **don't know** the population σ and p , we calculate the **estimated** standard deviation for \bar{x} and \bar{p} using the sample standard deviation (s) and sample proportion (\bar{p}).

Estimated Standard Deviation of \bar{x}

Infinite Population

$$s_{\bar{x}} = \left(\frac{s}{\sqrt{n}} \right) \quad (7.3)$$

Estimated Standard Deviation of \bar{p}

Infinite Population

$$s_{\bar{p}} = \sqrt{\frac{\bar{p}(1 - \bar{p})}{n}} \quad (7.6)$$

s = sample standard deviation

\bar{p} = sample proportion

Standard Deviation of \bar{x} / \bar{p} = Standard Error (SE)

\bar{x} / \bar{p} is expected to vary by +/- SE from the true population x / p .

What's a Sampling Distribution?

Problem: We still don't have the actual population mean (x) and proportion (p)

So we imagine a huge set containing all the possible random samples – and all the possible sample means. And we create a chart showing how likely each mean is by how common it is in the set (its frequency). Most of the means cluster in the middle, and therefore have the highest frequency. The outlier means are distributed along the edges with very low frequency because they occur very seldomly. This is the **sampling distribution**.

The SE gives us how spread apart the values are from the middle. A small SE means the xbars are clustered near the center. A large SE means they are spread out across the distribution.

If the sample size is small relative to the population the SE will be large, to account for outlier sample means. As the sample size increases to match the population, SE decreases, the spread becomes narrower, and the xbars/pbars vary less and less from actual x/p .

Sampling Distribution

Ingredients:

1. Expected value population param (if available)
 sample param (if not)
2. Standard Error standard deviation of \bar{x} or \bar{p}
3. Probability distribution (Normal if $n \geq 30$)

What is a Normal Distribution?

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If the distribution is 'normal' we know it's a bell curve and we know the intervals. For any normally distributed random variable, 90% of the values lie within 1.645 standard deviations of the mean, 95% of the values lie within 1.960 standard deviations of the mean, and 99% of the values lie within 2.576 standard deviations of the mean.

sample mean = population mean

sample std dev (Standard Error) = population std dev /

sqrt(sample size)

←----- 90% Confidence Interval -----→

(1.645 * SE) - (1.645 * SE) sample mean +

we call 1.645 in this case the **z-value**.

Problem: Usually we don't know the population std dev (b/c we don't have all the data) so we need another statistical tool to estimate the Standard Error.

What is the T-value?

Estimate the Standard Error using the *sample* standard deviation (s).

$$SE' = s / \text{sqrt}(n)$$

s = sample standard deviation

n = sample size

AND THEN get the T-Value

Excel: $t = T.INV.2T(1 - \text{confidence}, \text{degrees})$

Ingredients:

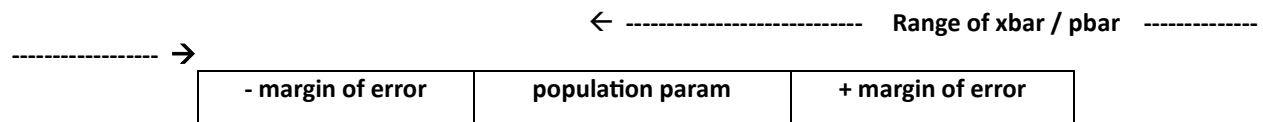
1 - confidence = .05 (100 - .05 = 95%)

probability)

n = sample size

degrees of freedom = $n - 1$

What is Margin of Error?



$$ME = t * SE'$$

$$t =$$

T-value (for 95%)

$$SE' =$$

estimated Standard Error

95% Confidence interval = $\bar{x} \pm ME$

| Savings | Count | xbar | StdDev | StdError | n | critical v | ME | 95% Confidence |
|---------|-------|-------|--------|----------|----|------------|--------|----------------|
| 92 | 20 | 71.00 | 22.351 | 4.998 | 20 | 2.086 | 10.425 | 81.425 |
| 34 | | | | | | | | 71.00 |
| 40 | | | | | | | | 60.575 |
| 105 | | | | | | | | |
| 83 | | | | | | | | |
| 55 | | | | | | | | |
| 56 | | | | | | | | |
| 49 | | | | | | | | |
| 40 | | | | | | | | |
| 76 | | | | | | | | |
| 48 | | | | | | | | |
| 96 | | | | | | | | |
| 93 | | | | | | | | |
| 74 | | | | | | | | |
| 73 | | | | | | | | |
| 78 | | | | | | | | |
| 93 | | | | | | | | |
| 100 | | | | | | | | |
| 53 | | | | | | | | |
| 82 | | | | | | | | |

When To Use: The Finite Population Correction Factor

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Estimated Standard Deviation of \bar{x}

Finite Population

$$s_{\bar{x}} = \sqrt{\frac{N-n}{N-1}} \left(\frac{s}{\sqrt{n}} \right)$$

Infinite Population

$$s_{\bar{x}} = \left(\frac{s}{\sqrt{n}} \right) \quad (7.3)$$

Estimated Standard Deviation of \bar{p}

Finite Population

$$s_{\bar{p}} = \sqrt{\frac{N-n}{N-1}} \sqrt{\frac{\bar{p}(1-\bar{p})}{n}}$$

Infinite Population

$$s_{\bar{p}} = \sqrt{\frac{\bar{p}(1-\bar{p})}{n}} \quad (7.6)$$

Compare the sample size (n) to the population size (N).

$n/N > 0.05 \rightarrow$ sample is a large % of the total
use the correction factor

$n/N \leq 0.05 \rightarrow$ sample is a small % of the total
don't use

comparison

total might as well be infinite by