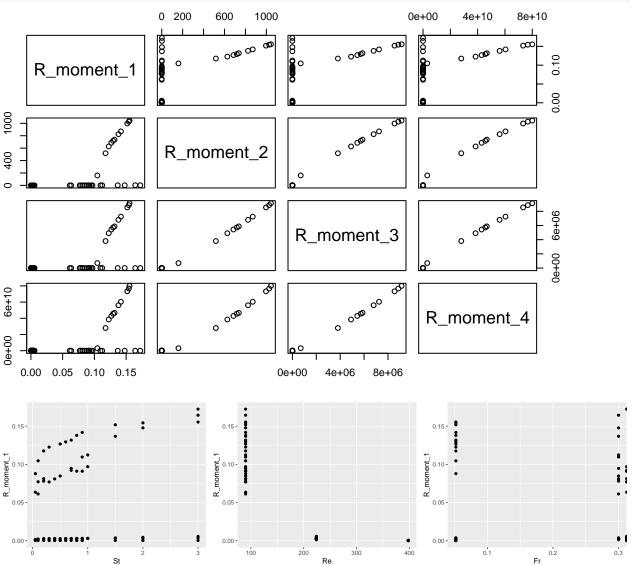
$case_study_report$

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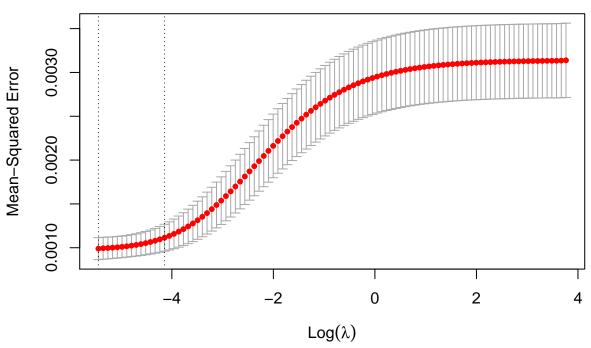




#correlation between predictor variables (in case we need to include interaction effects)
train_predictors <- data.frame(train[,c("Re","Fr","St")])
pairs(train_predictors)</pre>

```
0.05 0.10 0.15 0.20 0.25 0.30
                                                                                   400
                                                         @0000000
                                                                                   300
             Re
                              O
                                                     o
                                                         @00000000
                                                                                   200
                                                                                   100
                                                         @00000000
0.25
                                         Fr
0.15
0.05
              o
                           o
                                                     o
                                                                   St
                                                     0
    0
                                                                                   0.
           200
                  300
                          400
    100
                                                        0.0 0.5 1.0 1.5 2.0 2.5 3.0
#linear regression with factored Re and Fr
train1 <- train
train1$Re <- as.factor(train$Re)</pre>
train1$Fr <- as.factor(train$Fr)</pre>
lm1_m1 <- lm(R_moment_1 ~ St + Fr + Re, data=train1)</pre>
lm2_m1 <- lm(R_moment_2 ~ St + Fr + Re, data=train1)</pre>
lm3_m1 <- lm(R_moment_3 ~ St + Fr + Re, data=train1)</pre>
lm4_m1 <- lm(R_moment_4 ~ St + Fr + Re, data=train1)</pre>
summary(lm1 m1)
##
## lm(formula = R_moment_1 ~ St + Fr + Re, data = train1)
##
## Residuals:
         Min
                     1Q
                           Median
                                                    Max
## -0.038834 -0.008614 0.001702 0.009854 0.039423
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.106488
                            0.003971 26.818 < 2e-16 ***
## St
                            0.002078
                0.012213
                                       5.877 8.42e-08 ***
## Fr0.3
                -0.007623
                            0.004245 -1.796 0.07618 .
                            0.003787 -2.696 0.00849 **
## FrInf
                -0.010210
## Re224
                -0.108091
                            0.003682 -29.353 < 2e-16 ***
## Re398
               -0.111553
                            0.004632 -24.081 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.01529 on 83 degrees of freedom
## Multiple R-squared: 0.9293, Adjusted R-squared: 0.9251
```

```
## F-statistic: 218.2 on 5 and 83 DF, p-value: < 2.2e-16
x <- model.matrix(R_moment_1~St + Fr + Re,data=train_noinf)[,-1]</pre>
y <- train_noinf$R_moment_1</pre>
library(glmnet)
## Loading required package: Matrix
## Attaching package: 'Matrix'
## The following objects are masked from 'package:tidyr':
##
##
       expand, pack, unpack
## Loaded glmnet 4.0-2
grid <- 10^seq(10, -2, length = 100) # grid of values for lambda param
ridge.mod <- glmnet(x, y, alpha = 0, lambda = grid)</pre>
train \leftarrow sample(1:nrow(x), nrow(x)/2)
test <- (-train)</pre>
y.test <- y[test]</pre>
ridge.mod <- glmnet(x[train,], y[train], alpha = 0, lambda = grid, thresh = 1e-12)
ridge.pred <- predict(ridge.mod, s = 4, newx = x[test,])</pre>
mean((ridge.pred - y.test)^2) ## calculate MSE
## [1] 0.003083567
set.seed(1)
cv.out <- cv.glmnet(x[train,], y[train], alpha = 0)</pre>
plot(cv.out)
```



```
bestlam <- cv.out$lambda.min
bestlam</pre>
```

```
## [1] 0.004312608
```

```
ridge.pred <- predict(ridge.mod, s = bestlam, newx = x[test,])
mean((ridge.pred - y.test)^2)</pre>
```

[1] 0.001489969

improvement in the mse

```
x2 <- model.matrix(R_moment_2~ St + Fr + Re,data=train_noinf)[,-1]
y2 <- train_noinf$R_moment_2

library(glmnet)
set.seed(1)
grid <- 10^seq(10, -2, length = 100) # grid of values for lambda param
ridge.mod2 <- glmnet(x2, y2, alpha = 0, lambda = grid)

train2 <- sample(1:nrow(x2), nrow(x2)/2)
test2 <- (-train2)
y.test2 <- y2[test2]

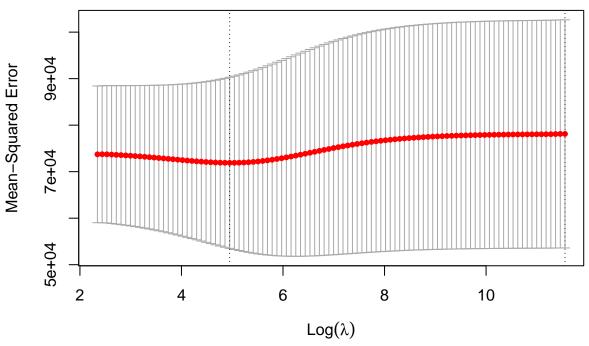
ridge.mod2 <- glmnet(x2[train,], y2[train], alpha = 0, lambda = grid, thresh = 1e-12)
ridge.pred <- predict(ridge.mod, s = 4, newx = x2[test,])
mean((ridge.pred - y.test2)^2) ## calculate MSE</pre>
```

```
## [1] 66957.52
```

```
set.seed(1)
cv.out2 <- cv.glmnet(x2[train2,], y2[train2], alpha = 0)</pre>
```

plot(cv.out2)

3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3

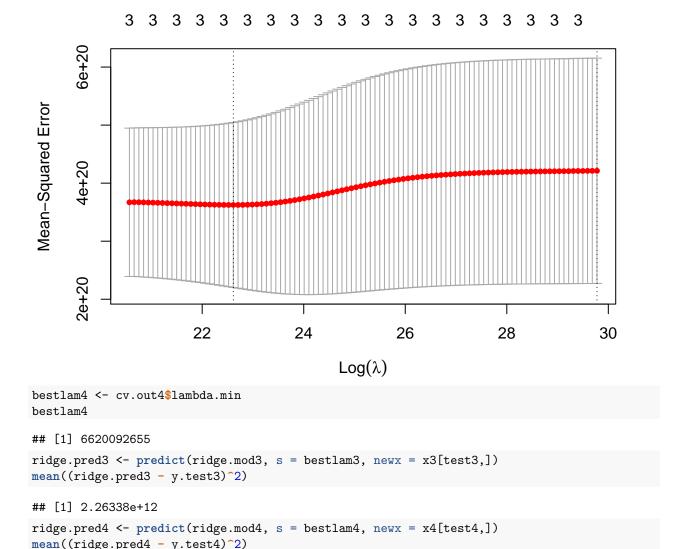


```
bestlam2 <- cv.out2$lambda.min
bestlam2
## [1] 141.1089
ridge.pred2 <- predict(ridge.mod2, s = bestlam2, newx = x2[test2,])</pre>
mean((ridge.pred2 - y.test2)^2)
## [1] 46952.88
x3 <- model.matrix(R_moment_3~St + Fr + Re,data=train_noinf)[,-1]</pre>
y3 <- train_noinf$R_moment_3
ridge.mod3 <- glmnet(x3, y3, alpha = 0, lambda = grid)</pre>
train3 <- sample(1:nrow(x3), nrow(x3)/2)</pre>
test3 <- (-train3)
y.test3 <- y[test3]
ridge.mod3 <- glmnet(x3[train3,], y3[train3], alpha = 0, lambda = grid, thresh = 1e-12)
ridge.pred3 <- predict(ridge.mod3, s = 4, newx = x3[test3,])</pre>
mean((ridge.pred3 - y.test3)^2) ## calculate MSE
## [1] 2.924727e+12
x4 <- model.matrix(R_moment_4~St + Fr + Re,data=train_noinf)[,-1]
y4 <- train_noinf$R_moment_4
```

ridge.mod4 <- glmnet(x4, y4, alpha = 0, lambda = grid)

```
train4 <- sample(1:nrow(x4), nrow(x4)/2)
test4 <- (-train4)</pre>
y.test4 <- y[test4]</pre>
ridge.mod4 \leftarrow glmnet(x4[train4,], y4[train4], alpha = 0, lambda = grid, thresh = 1e-12)
ridge.pred4 <- predict(ridge.mod4, s = 4, newx = x4[test4,])</pre>
mean((ridge.pred4 - y.test4)^2) ## calculate MSE
## [1] 1.702767e+20
set.seed(1)
cv.out3 <- cv.glmnet(x3[train3,], y3[train3], alpha = 0)</pre>
plot(cv.out3)
              3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
      8e+12
Mean-Squared Error
      6e+12
      4e+12
                                                16
                 12
                                14
                                                                18
                                                                                20
                                               Log(\lambda)
bestlam3 <- cv.out3$lambda.min</pre>
bestlam3
## [1] 407052.8
cv.out4 <- cv.glmnet(x4[train4,], y4[train4], alpha = 0)</pre>
```

plot(cv.out4)



[1] 1.20962e+20

improvement? still large

Introduction

Turbulence is highly versatile motion that is often times difficult to predict and understanding fluid motion and its effect on natural problems poses a great challenge. Interpreting turbulence data is an incredibly important task in the engineering from understanding the cosmos to the cosmic cycle.

Parametric modeling is effective when we want to compactly represent features as model parameters. Unlike certain "black box" machine learning techniques, it offers a higher level of interpretability, which is especially useful for a practical setting. Rather than simply outputting a classification result, a parametric model allows us to investigate in more detail which aspects of turbulence differ between high and low particle cluster volumes.

In our project, we use linear and (...) and apply it to interpret the difference in model parameters in order to achieve the following objectives:

1. Build a model that predict its particle cluster volume distribution in terms of the moments.

 $2. \ \, \text{Investigate and interpret how model parameters affects the probability distribution for particle cluster volumes}$

Methodology

Results

Conclusion