## Homework 2

Out: 9.21.16 Due: 10.3.16

## 1. [Asymptotic comparison, 25 points]

For each of these problems enter "yes" or "no" indicating whether A is O, o,  $\Theta$ ,  $\omega$ ,  $\Omega$  of B. Justify your answers.

| A                  | В                                    | О | o | Θ | ω | Ω |
|--------------------|--------------------------------------|---|---|---|---|---|
| 4n log n           | $n \log n + 5$                       |   |   |   |   |   |
| 2 <sup>log n</sup> | $(\log n)^2$                         |   |   |   |   |   |
| n <sup>n</sup>     | n!                                   |   |   |   |   |   |
| n                  | $\sum_{i=0}^{\infty} \frac{50}{7^i}$ |   |   |   |   |   |
| 200 n <sup>9</sup> | e <sup>n</sup>                       |   |   |   |   |   |

## 2. [Asymptotics, 25 points]

Place the following functions from asymptotically smallest to largest. When two functions have the same asymptotic order, put an equal sign between them. Provide an explanation for your ordering.

$$n^5 + 7n, 2^{10}, n \log n, (\log n)^{\log n}, \ln n, n, \sqrt{2}^{\lg n}, 4^{\lg n}, (n+1)!, 2^n$$

## 3. [Algorithmic intuition, 50 points]

Write and briefly explain the following C++ function:

long MaxProduct (string file);

that accepts an input file containing sequences of numbers. Each sequence starts on a new line, may continue on several subsequent lines, contains at most 100 numbers, and ends with the number -999999 (which is not part of the sequence).

The function outputs to the screen the maximum continuous sub-sequence product of up to 3 numbers for each sequence, one output per line. It returns the maximum of all the outputs.

Sample output:

6 120 54

54 The overall max product is: 120

Your program will be compiled with the provided HW2\_Q3\_main.cpp file on the lab

computers.

Try to make your function as efficient as you can.

Submit your solution, in two files: *MaxProduct.cpp*, containing your function, and *MaxProduct.h*, which is required for your code to compile with the provided main file. Make sure to write your name in a comment at the top of the program, and verify that your program compiles with the provided file on the lab computers.