

H.W. #5 Diffie-Hellman

1. How the Diffie-Hellman protocol works is that two people can share a message across an insecure network by both using two values g and p . p is an incredibly large prime integer while g is an integer less than p and for every number n such that $0 < n < p$, there is a power k of g such that $n = g^k \pmod{p}$. Alice and Bob each generate a secret value only they know, a and b , respectively. Alice then relays the value $g^a \pmod{p}$ to Bob and Bob relays the value $g^b \pmod{p}$ to Alice. Each of them then use the number they were given, raise it to their own secret value, then mod it by p . By the distributive property of mods and powers, both Alice and Bob will have the same value of $g^{ab} \pmod{p}$ as their final number, which is the shared secret key k . No passive attacker overhearing their exchange can guess what k is.
2. Mallory could intercept and change some values that are exchanged between Alice and Bob. Mallory could replace the public values of g and p as they move from one person to the next so she can know what k will be for both people. Mallory could also simply stop both messages from moving from one person to the next and give 1 to both Alice and Bob so that no matter what the values of a and b are both will end up with 1 as k .
3. p should be 1024 – 2048 bits in order to be considered safe.
Source: <http://security.stackexchange.com/questions/47204/dh-parameters-recommended-size>
4. The recommended size of p in DH is much larger than the recommended key size for AES because DH is an asymmetric algorithm while AES is a symmetric algorithm. In an asymmetric algorithm, the strength of the key is based off of the modulus' resistance to factorization into its prime components, which is roughly $O((\log n)^{2/3})$. In symmetric algorithms the strength of the key is based upon its resistance to brute-force attacks because the key is literally just a random number and that complexity is $O(2^n)$.
Source: <http://crypto.stackexchange.com/questions/6236/why-does-the-recommended-key-size-between-symmetric-and-asymmetric-encryption-di>