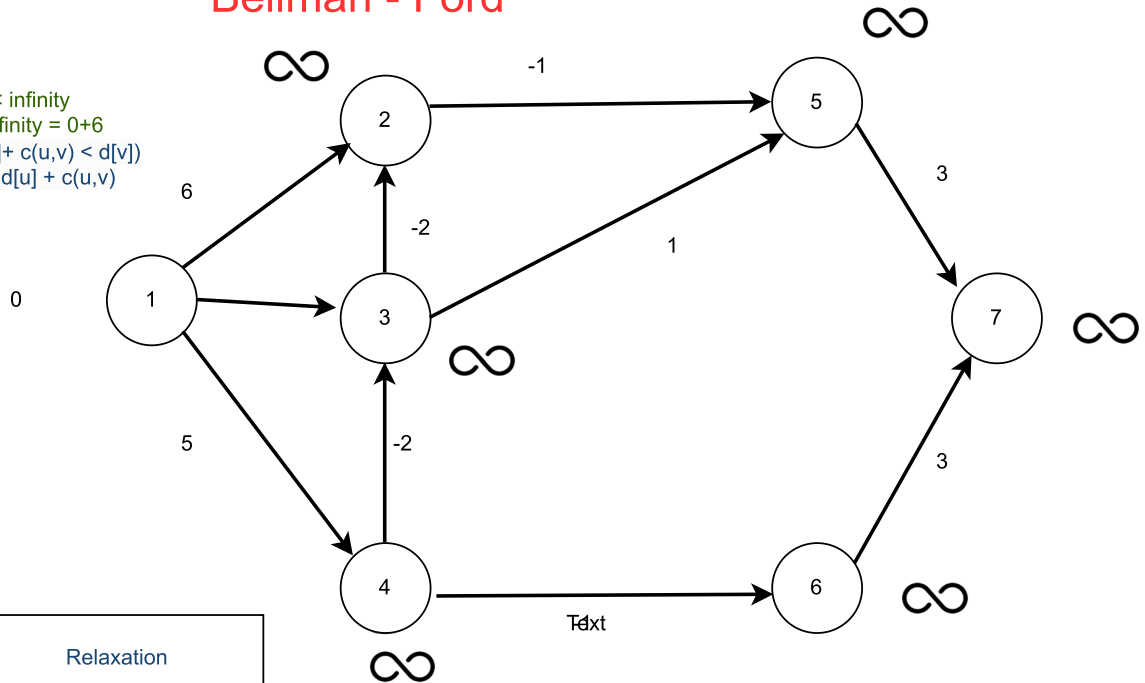


# Single Source Shortest Path Bellman - Ford

$0+6 < \text{infinity}$   
 so  $\text{infinity} = 0+6$   
 if  $(d[u] + c(u,v) < d[v])$   
 $d[v] = d[u] + c(u,v)$



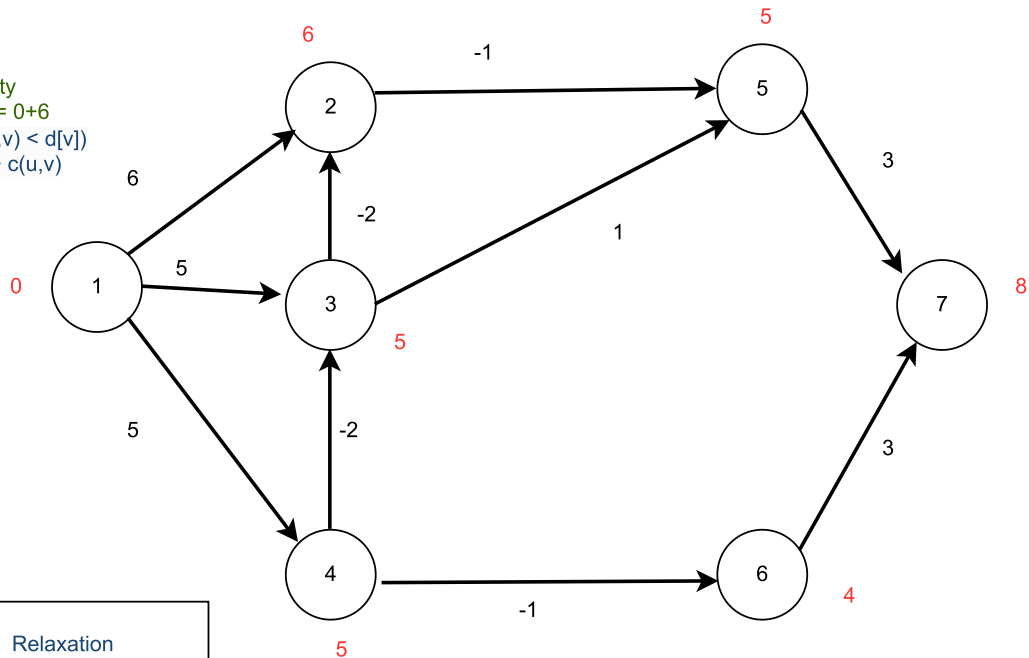
Relaxation

if  $(d[u] + c(u,v) < d[v])$   
 $d[v] = d[u] + c(u,v)$

Edge list = (1,2), (1,3), (1,4), (2,5), (3,2), (3,5), (4,3), (4,6), (5,7), (6,7)



$0+6 < \text{infinity}$   
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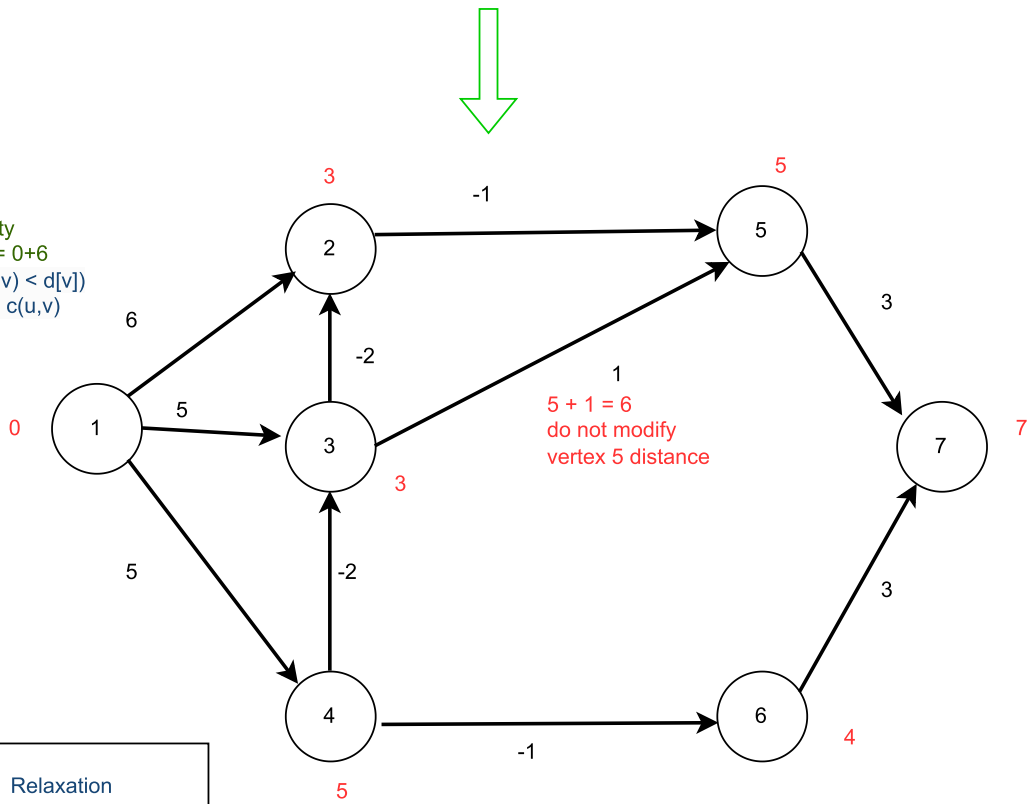


Relaxation

if  $(d[u] + c(u,v) < d[v])$   
 $d[v] = d[u] + c(u,v)$

Edge list = (1,2), (1,3), (1,4), (2,5), (3,2), (3,5), (4,3), (4,6), (5,7), (6,7)

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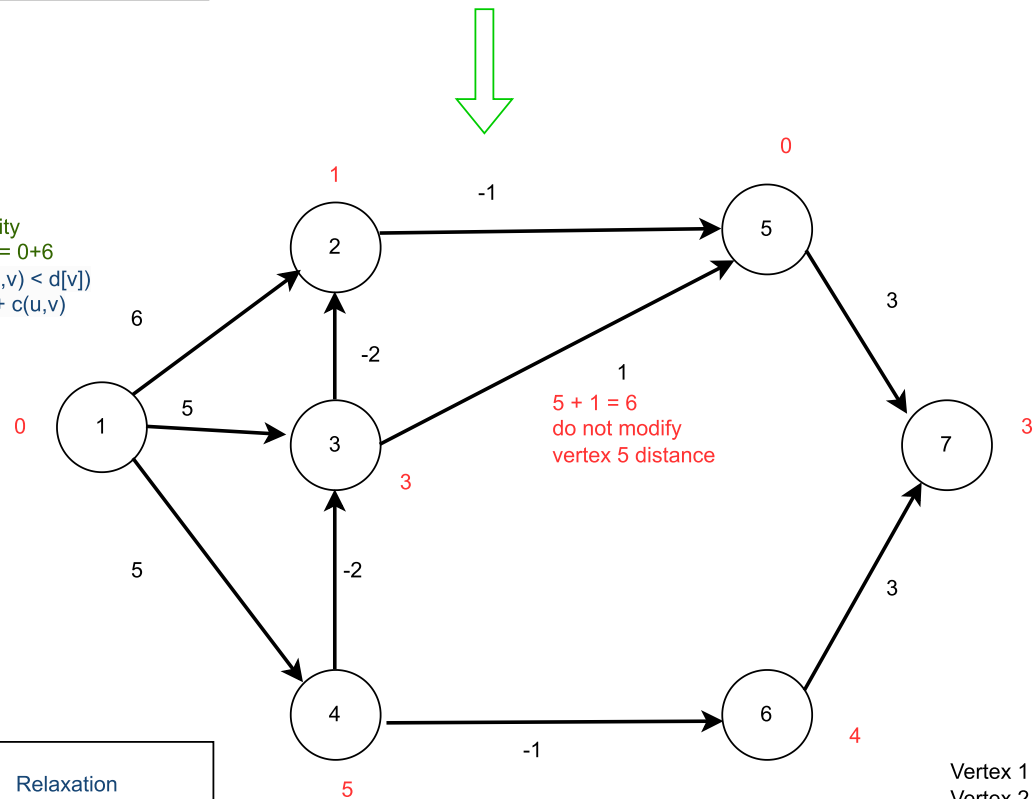


Relaxation

if  $(d[u] + c(u,v) < d[v])$   
 $d[v] = d[u] + c(u,v)$

Edge list = (1,2), (1,3), (1,4), (2,5), (3,2), (3,5), (4,3), (4,6), (5,7), (6,7)

$0+6 < \text{infinity}$   
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Relaxation

if  $(d[u] + c(u,v) < d[v])$   
 $d[v] = d[u] + c(u,v)$

Edge list = (1,2), (1,3), (1,4), (2,5), (3,2), (3,5), (4,3), (4,6), (5,7), (6,7)

Vertex 1 = 0  
 Vertex 2 = 1  
 Vertex 3 = 3  
 Vertex 4 = 5  
 Vertex 5 = 0  
 Vertex 6 = 4  
 Vertex 7 = 3

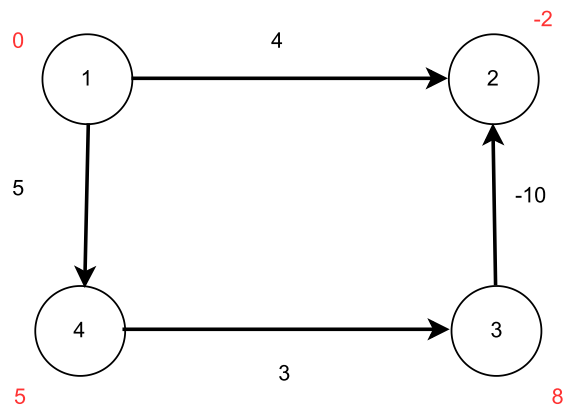
#### Algorithm Efficiency -

--> The runtime for the Bellman-For shortest path algorithm is  $O(VE)$

--> The outer loop (the main iterations) executes  $V-1$  times

--> The algorithm visits each vertex and follows the subset of edges to adjacent vertices, following a total of  $E$  edges across all loop executions.

## Drawback of Bellman-Ford



Edge list = (3,2),(4,3), (1,4), (1,2)

How many times should I relax the edges?

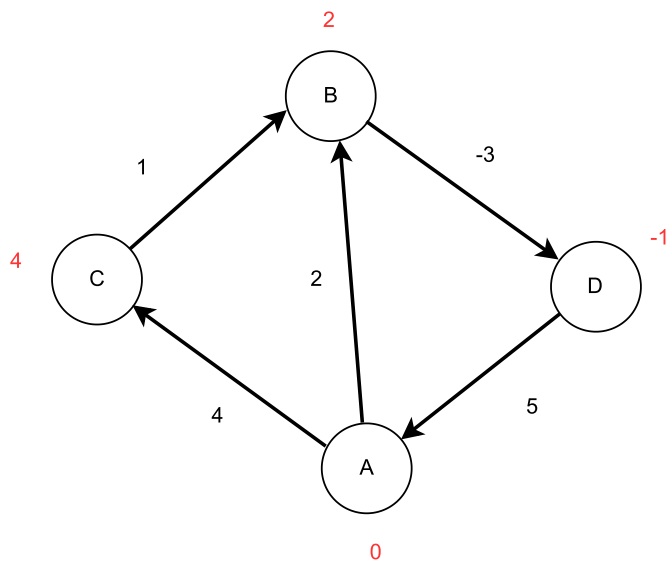
$n = 4 - 1 = 3$  times

1 = 0  
2 = (-2)  
3 = 8  
4 = 5

## Practice

Start Vertex = B

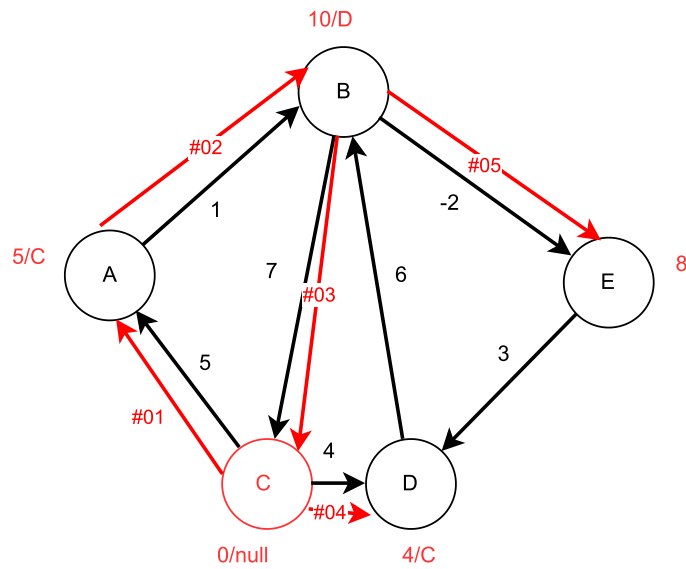
Each Loop in the algorithm visits vertices in the graph in the following order: A, B, C, D



## Practice

Start Vertex = C

Each Loop in the algorithm visits vertices in the graph in the following order: A, B, C, D, E

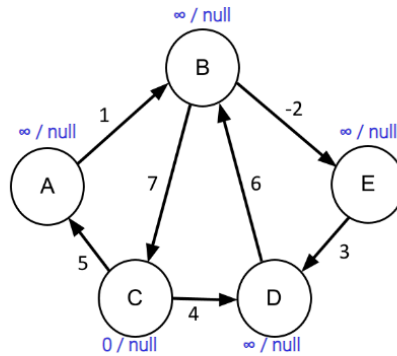


## 12.10.1: Bellman-Ford's shortest path.

3207

[Jump to level 1](#)

The Bellman-Ford algorithm is run on the following graph. The start vertex is C. Assume each loop of the algorithm visits vertices in the graph in the following order: A, B, C, D, E.



What are A's values after the first iteration?  /  Enter inf for  $\infty$ .

What are B's values after the first iteration?  /

What are D's values after the first iteration?  /

What are E's values after the first iteration?  /

1	2	3	4
---	---	---	---

Check

Next

✗ Each incorrect answer is highlighted.

Expected:

A: 5 / C

B: 10 / D

D: 4 / C

E: inf / null

A is visited first: B is adjacent, but A's current distance is  $\infty$ , so a path through A will not change B. So B remains  $\infty$  / null.

B is visited next: No updates occur as B's current distance is  $\infty$ .

C is visited next: A is updated to  $0 + 5 = 5$  / C, and D is updated to  $0 + 4 = 4$  / C.

D is visited next: B is updated to  $4 + 6 = 10$  / D.

E is visited last: No updates occur as E's current distance is  $\infty$ .