

NON – IDEAL BUCK CONVERTER

Voltage mode control Transfer functions

PLANT TRANSFER FUNCTION CALCULATIONS

Circuit Equations· (Small – Signal Approximation)

$\langle \mathbf{D}_{on} \rangle :$

$$\begin{aligned} V_L &= V_{in} - I_L \cdot R_{DSon_HS} - I_L \cdot R_L - V_{out} \\ I_c &= I_L - I_{out} \end{aligned}$$

$\langle \mathbf{D}_{off} \rangle :$

$$\begin{aligned} V_L &= - (V_{out} + I_L \cdot (R_{DSon_LS} + R_L)) = - V_{out} - I_L \cdot R_{DSon_LS} - I_L \cdot R_L \\ I_c &= I_L - I_{out} \end{aligned}$$

Transfer Function Analysis

$$\langle V_L \rangle = (D_{on}) \cdot (V_{in} - I_L \cdot R_{DSon_HS} - I_L \cdot R_L - V_{out}) + (D_{off}) \cdot (-V_{out} - I_L \cdot R_{DSon_LS} - I_L \cdot R_L)$$

$$\langle I_c \rangle = (D_{on}) \cdot (I_L - I_{out}) + (D_{off}) \cdot (I_L - I_{out})$$

$$\langle I_{in} \rangle = (D_{on}) \cdot (I_L)$$

DC versions· ($\langle \mathbf{x} \rangle = 0$)

$$\langle V_L \rangle = 0 = D_{on} \cdot V_{in} - D_{on} \cdot I_L \cdot R_{DSon_HS} - D_{on} \cdot I_L \cdot R_L - D_{on} \cdot V_{out} - D_{off} \cdot V_{out} - D_{off} \cdot I_L \cdot R_{DSon_LS} - D_{off} \cdot I_L \cdot R_L \cdot$$

$$0 = D_{on} \cdot V_{in} - D_{on} \cdot I_L \cdot R_{DSon_HS} - I_L \cdot R_L - V_{out} - D_{off} \cdot I_L \cdot R_{DSon_LS}$$

$$V_{out} = D_{on} \cdot V_{in} - D_{on} \cdot I_L \cdot R_{DSon_HS} - I_L \cdot R_L - (1 - D_{on}) \cdot I_L \cdot R_{DSon_LS} = D_{on} \cdot V_{in} - D_{on} \cdot I_L \cdot R_{DSon_HS} - I_L \cdot R_L - I_L \cdot R_{DSon_LS} - D_{on} \cdot I_L \cdot R_{DSon_LS}$$

$$V_{out} = D_{on} \cdot (V_{in} - I_L \cdot R_{DSon_HS} - I_L \cdot R_{DSon_LS}) - I_L \cdot (R_L + R_{DSon_LS})$$

$$\langle I_C \rangle = I_L - I_{out}$$

$$0 = I_L - I_{out}$$

$$I_L = I_{out}$$

$$I_{out} = \frac{V_{out}}{R_{out}}$$

$$V_{out} = D_{on} \cdot (V_{in} - I_{out} \cdot R_{DSon_HS} - I_{out} \cdot R_{DSon_LS}) - I_{out} \cdot (R_L + R_{DSon_LS})$$

$$V_{out} = D_{on} \cdot \left(V_{in} - \frac{V_{out}}{R_{out}} \cdot R_{DSon_HS} - \frac{V_{out}}{R_{out}} \cdot R_{DSon_LS} \right) - \frac{V_{out}}{R_{out}} \cdot (R_L + R_{DSon_LS}) = D_{on} \cdot V_{in} - D_{on} \cdot \frac{V_{out}}{R_{out}} \cdot R_{DSon_HS} - D_{on} \cdot \frac{V_{out}}{R_{out}} \cdot R_{DSon_LS} - \frac{V_{out}}{R_{out}} \cdot (R_L + R_{DSon_LS})$$

$$V_{out} + D_{on} \cdot \frac{V_{out}}{R_{out}} \cdot (R_{DSon_HS} + R_{DSon_LS}) + \frac{V_{out}}{R_{out}} \cdot (R_L + R_{DSon_LS}) = D_{on} \cdot V_{in}$$

$$V_{out} \cdot \left(1 + D_{on} \cdot \frac{(R_{DSon_HS} + R_{DSon_LS})}{R_{out}} + \frac{(R_L + R_{DSon_LS})}{R_{out}} \right) = D_{on} \cdot V_{in}$$

$$V_{out} = \left(\frac{D_{on}}{\left(1 + D_{on} \cdot \frac{(R_{DSon_HS} + R_{DSon_LS})}{R_{out}} + \frac{(R_L + R_{DSon_LS})}{R_{out}} \right)} \right) \cdot V_{in}$$

Inductor Slope with losses

Up slope :

$$M_1 = \frac{(V_{in} - V_{out} - I_L \cdot (R_{DSon_HS} + R_L))}{L}$$

$$m_1 = \frac{(v_{in} - v_{out} - i_L \cdot (R_{DSon_HS} + R_L))}{L}$$

Down slope :

$$M_2 = -\frac{(V_{out} + I_L \cdot (R_{DSon_LS} + R_L))}{L}$$

$$m_2 = -\frac{(v_{out} + i_L \cdot (R_{DSon_LS} + R_L))}{L}$$

Slope Compensation :

M_a = Device dependent

AC versions

$$\langle Total \rangle = AC + DC$$

$$\langle V_{in} \rangle = V_{in} + v_{in}$$

$$\langle V_L \rangle = V_L + v_L$$

$$\langle D_{on} \rangle = D_{on} + d$$

$$\langle D_{off} \rangle = D_{off} - d$$

$$\langle I_L \rangle = I_L + i_L$$

$$\langle V_{out} \rangle = V_{out} + v_{out}$$

Adding AC Inductor Voltage to formulas

$$\langle V_L + v_L \rangle = (D_{on} + d) \cdot [V_{in} + v_{in} - (I_L + i_L) \cdot R_{DSon_HS} - (I_L + i_L) \cdot R_L - (V_{out} + v_{out})] + (D_{off} - d) \cdot [- (V_{out} + v_{out}) - (I_L + i_L) \cdot R_{DSon_L} - (I_L + i_L) \cdot R_L]$$

$$\begin{aligned} \langle v_L \rangle &= [D_{on} \cdot V_{in} + D_{on} \cdot v_{in} - D_{on} \cdot I_L \cdot R_{DSon_HS} - D_{on} \cdot i_L \cdot R_{DSon_HS} - D_{on} \cdot I_L \cdot R_L - D_{on} \cdot i_L \cdot R_L - D_{on} \cdot V_{out} - D_{on} \cdot v_{out} + d \cdot V_{in} + d \cdot v_{in} - d \cdot I_L \\ &\cdot R_{DSon_HS} - d \cdot i_L \cdot R_{DSon_HS} - d \cdot I_L \cdot R_L - d \cdot i_L \cdot R_L - d \cdot V_{out} - d \cdot v_{out}] + [-D_{off} \cdot V_{out} - D_{off} \cdot v_{out} - D_{off} \cdot I_L \cdot R_{DSon_LS} - D_{off} \cdot i_L \cdot R_{DSon_LS} - D_{off} \cdot I_L \\ &\cdot R_L - D_{off} \cdot i_L \cdot R_L + d \cdot v_{out} + d \cdot I_L \cdot R_{DSon_LS} + d \cdot i_L \cdot R_{DSon_LS} + d \cdot I_L \cdot R_L + d \cdot i_L \cdot R_L] \end{aligned}$$

– Remove DC and very small variables

$$\langle v_L \rangle = [D_{on} \cdot v_{in} - D_{on} \cdot i_L \cdot R_{DSon_HS} - D_{on} \cdot i_L \cdot R_L - D_{on} \cdot v_{out} + d \cdot V_{in} - d \cdot I_L \cdot R_{DSon_HS} - d \cdot I_L \cdot R_L - d \cdot V_{out}] + [-D_{off} \cdot v_{out} - D_{off} \cdot i_L \cdot R_{DSon_LS} - D_{off} \cdot i_L \cdot R_L - d \cdot V_{out} + d \cdot I_L \cdot R_{DSon_LS} + d \cdot i_L \cdot R_L]$$

$$-D_{on} + D_{off} = 1$$

$$\langle v_L \rangle = D_{on} \cdot v_{in} - D_{on} \cdot i_L \cdot R_{DSon_HS} - i_L \cdot R_L - v_{out} + d \cdot V_{in} - d \cdot I_L \cdot R_{DSon_HS} - D_{off} \cdot i_L \cdot R_{DSon_LS} + d \cdot I_L \cdot R_{DSon_LS}$$

$$\langle v_L \rangle = s \cdot L \cdot i_L = D_{on} \cdot v_{in} - i_L (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}) + d (V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS})) - v_{out}$$

$$v_{out} = D_{on} \cdot v_{in} - i_L (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}) + d (V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS})) - s \cdot L \cdot i_L \quad \dots$$

Voltage divider with series impedance

$$v_{out} = D_{on} \cdot v_{in} - i_L (s \cdot L + D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}) + d (V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))$$

Adding AC Capacitor Currents to formulas

$$\langle I_C + i_C \rangle = (D_{on} + d) \cdot ((I_L + i_L) - (I_{out} + i_{out})) + (D_{off} - d) \cdot ((I_L + i_L) - (I_{out} + i_{out}))$$

$$\langle i_C \rangle = [D_{on} \cdot I_L + D_{on} \cdot i_L - D_{on} \cdot I_{out} - D_{on} \cdot i_{out} + d \cdot I_L + d \cdot i_L - d \cdot I_{out} - d \cdot i_{out}] + [D_{off} \cdot I_L + D_{off} \cdot i_L - D_{off} \cdot I_{out} - D_{off} \cdot i_{out} - d \cdot I_L - d \cdot i_L + d \cdot I_{out} + d \cdot i_{out}]$$

$$+ d \cdot i_{out}]$$

$\langle i_c \rangle = i_L - i_{out} \quad \therefore$ Output Capacitor is **in parallel** with v_{out}

Adding Input Currents to formulas

$$\langle I_{in} + i_{in} \rangle = (D_{on} + d) \cdot (I_L + i_L)$$

$$\langle i_{in} \rangle = D_{on} \cdot I_L + D_{on} \cdot i_L + d \cdot I_L + d \cdot i_L$$

$$\langle i_{in} \rangle = D_{on} \cdot i_L + d \cdot I_L$$

Equivalent Circuit from Formulas

$$\text{Output Impedance} = R_{load} \parallel \text{Capacitor}_{out} = \frac{(R_{load}) \cdot \left(\frac{1}{s \cdot C} \right)}{\left(\frac{1}{s \cdot C} + R_{load} \right)} = \frac{R_{load}}{1 + s \cdot R_{load} \cdot C_{out}}$$

$$\text{Series Impedance} = s \cdot L + R \cdot x = s \cdot L + (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}) = s \cdot L + R_L + D_{on} \cdot R_{DSon_HS} + (1 - D_{on}) \cdot R_{DSon_LS} = s \cdot L + (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS}))$$

$$\text{Transfer function voltage divider} = \frac{\left(\frac{R_{load}}{1 + s \cdot R_{load} \cdot C_{out}} \right)}{\left(\frac{R_{load}}{1 + s \cdot R_{load} \cdot C_{out}} \right) + (s \cdot L + (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS})))}$$

$$\begin{aligned} &= \frac{R_{load}}{R_{load} + (s \cdot L + (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS}))) \cdot (1 + s \cdot R_{load} \cdot C_{out})} \\ &= R_{load} / (R_{load} + (s \cdot L + (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS}))) + (s \cdot R_{load} \cdot C_{out})) \cdot (s \cdot L + (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS}))) \\ &= R_{load} / (R_{load} + (s \cdot L + (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS}))) + (s^2 \cdot R_{load} \cdot L \cdot C_{out})) + (s \cdot (R_{load} \cdot C_{out} \cdot (R_L + R_{DSon_LS}))) \end{aligned}$$

$$+ R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS})) = R_{load} / ((R_{load} + R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS})) + s \cdot (L + R_{load} \cdot C_{out} \cdot (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS}))) + (s^2 \cdot R_{load} \cdot L \cdot C_{out}))$$

$$\text{Total Voltage from divider} = D_{on} \cdot v_{in} - d \cdot (V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))$$

$$\text{Transfer function} = (R_{load} / ((R_{load} + R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS})) + s \cdot (L + R_{load} \cdot C_{out} \cdot (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS}))) - R_{DSon_LS})) + (s^2 \cdot R_{load} \cdot L \cdot C_{out})) \cdot (D_{on} \cdot v_{in} - d \cdot (V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS})))$$

$$\mathbf{G}_{v \cdot v} \big|_{d=0} \text{ in}$$

$$\underline{\text{Input-to-output Transfer Functions}} = \left(\frac{v_{out}}{v_{in}} \right) = ((R_{load} \cdot D_{on}) / ((R_{load} + R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS})) + s \cdot (L + R_{load} \cdot C_{out} \cdot (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS}))) + (s^2 \cdot R_{load} \cdot L \cdot C_{out}))) = \left(\left(\left(\frac{V_{out}}{I_{out}} \right) \cdot D_{on} \right) / \left(\left(\left(\frac{V_{out}}{I_{out}} \right) + R_L + R_{DSon_LS} \right) \cdot C_{out} \cdot (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS})) + \left(s^2 \cdot \left(\frac{V_{out}}{I_{out}} \right) \cdot L \cdot C_{out} \right) \right) \right)$$

$$R_{load} = \frac{V_{out}}{I_{out}}$$

$$\mathbf{G}_{v \cdot d} \big|_{v_{in}=0} \text{ out}$$

$$\underline{\text{Control-to-output Transfer function}} = \left(\frac{v_{out}}{d} \right) = \left(R_{load} \cdot (V_{in} + I_L \cdot (R_{DSon_LS} - R_{DSon_HS})) / ((R_{load} + R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS}))) \right)$$

$$- R_{DSon_LS})) + s \cdot (L + R_{load} \cdot C_{out} \cdot (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS}))) + (s^2 \cdot R_{load} \cdot L \cdot C_{out})) = \left(\left(\left(\frac{V_{out}}{I_{out}} \right) \right) \cdot (V_{in} + I_L \cdot (R_{DSon_LS} - R_{DSon_HS})) / \left(\left(\left(\left(\frac{V_{out}}{I_{out}} \right) + R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS} \right) \right) \cdot C_{out} \cdot (R_L + R_{DSon_LS} + D_{on} \cdot (R_{DSon_HS} - R_{DSon_LS})) + \left(s \cdot \left(L + \left(\frac{V_{out}}{I_{out}} \right) \cdot L \cdot C_{out} \right) \right) \right) \right)$$

$$\cdot (R_{DSon_HS} - R_{DSon_LS})) \Big) + \left(s^2 \cdot \left(\frac{V_{out}}{I_{out}} \right) \cdot L \cdot C_{out} \right) \Big) \Big) =$$

Converter Transfer functions

$$\mathbf{G}_{i_L \cdot d} \Big|_{v_{in} = 0}$$

Circuit model

$$R_x = (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS})$$

$$V_x = d \cdot (V_{in} + I_L \cdot (R_{DSon_LS} - R_{DSon_HS}))$$

$$Impedance = R_x + s \cdot L + \frac{R_{out}}{1 + s \cdot C \cdot R_{out}}$$

$$i_L = \frac{V_x}{\left(R_x + s \cdot L + \frac{R_{out}}{1 + s \cdot C \cdot R_{out}} \right)} = \frac{d \cdot (V_{in} + I_L \cdot (R_{DSon_LS} - R_{DSon_HS}))}{\left(D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS} + s \cdot L + \frac{R_{out}}{1 + s \cdot C \cdot R_{out}} \right)}$$

$$i_L = \frac{d \cdot (V_{in} + I_L \cdot (R_{DSon_LS} - R_{DSon_HS})) \cdot (1 + s \cdot C \cdot R_{out})}{(D_{on} \cdot R_{DSon_HS} \cdot (1 + s \cdot C \cdot R_{out}) + R_L \cdot (1 + s \cdot C \cdot R_{out}) + D_{off} \cdot R_{DSon_LS} \cdot (1 + s \cdot C \cdot R_{out}) + s \cdot L \cdot (1 + s \cdot C \cdot R_{out}) + R_{out})}$$

$$\begin{aligned} \frac{i_L}{d} = & (V_{in} + I_L \cdot (R_{DSon_LS} - R_{DSon_HS}) + s \cdot C \cdot R_{out} \cdot V_{in} + s \cdot C \cdot R_{out} \cdot I_L \cdot (R_{DSon_LS} - R_{DSon_HS})) / (((D_{on} \cdot R_{DSon_HS} + s \cdot C \cdot R_{out} \cdot D_{on} \cdot R_{DSon_HS}) \\ & + (R_L + s \cdot C \cdot R_{out} \cdot R_L) + (D_{off} \cdot R_{DSon_LS} + s \cdot C \cdot R_{out} \cdot (D_{off} \cdot R_{DSon_LS})) + (s \cdot L + s \cdot C \cdot R_{out} \cdot (s \cdot L)) + R_{out})) \end{aligned}$$

$$\begin{aligned}
\frac{i_L}{d} &= \frac{(V_{\text{in}} + I_L \cdot (R_{\text{DSon_LS}} - R_{\text{DSon_HS}}) + s \cdot C \cdot R_{\text{out}} \cdot V_{\text{in}} + s \cdot C \cdot R_{\text{out}} \cdot I_L \cdot (R_{\text{DSon_LS}} - R_{\text{DSon_HS}}))}{((D_{\text{on}} \cdot R_{\text{DSon_HS}} + R_L + D_{\text{off}} \cdot R_{\text{DSon_LS}} + R_{\text{out}}) + s \cdot (C \cdot R_{\text{out}} \cdot R_L + C \cdot R_{\text{out}} \cdot D_{\text{on}} \cdot R_{\text{DSon_HS}} + C \cdot R_{\text{out}} \cdot D_{\text{off}} \cdot R_{\text{DSon_LS}} + L) + s^2 \cdot L \cdot C \cdot R_{\text{out}})} \\
\frac{i_L}{d} &= \frac{(V_{\text{in}} + I_L \cdot (R_{\text{DSon_LS}} - R_{\text{DSon_HS}}) + s \cdot C \cdot R_{\text{out}} \cdot (V_{\text{in}} + I_L \cdot (R_{\text{DSon_LS}} - R_{\text{DSon_HS}})))}{((D_{\text{on}} \cdot R_{\text{DSon_HS}} + R_L + D_{\text{off}} \cdot R_{\text{DSon_LS}} + R_{\text{out}}) + s \cdot (C \cdot R_{\text{out}} \cdot (R_L + D_{\text{on}} \cdot R_{\text{DSon_HS}} + D_{\text{off}} \cdot R_{\text{DSon_LS}}) + L) + s^2 \cdot L \cdot C \cdot R_{\text{out}})} \\
\frac{i_L}{d} &= \frac{(V_{\text{in}} + I_L \cdot (R_{\text{DSon_LS}} - R_{\text{DSon_HS}}) + s \cdot C \cdot R_{\text{out}} \cdot (V_{\text{in}} + I_L \cdot (R_{\text{DSon_LS}} - R_{\text{DSon_HS}})))}{((D_{\text{on}} \cdot R_{\text{DSon_HS}} + R_L + (1 - D_{\text{on}}) \cdot R_{\text{DSon_LS}} + R_{\text{out}}) + s \cdot (C \cdot R_{\text{out}} \cdot (R_L + D_{\text{on}} \cdot R_{\text{DSon_HS}} + (1 - D_{\text{on}}) \cdot R_{\text{DSon_LS}}) + L) + s^2 \cdot L \cdot C \cdot R_{\text{out}})}
\end{aligned}$$

$$\frac{i_L}{d}$$

$$= ((V_{\text{in}} + I_L \cdot (R_{\text{DSon_LS}} - R_{\text{DSon_HS}}) + s \cdot C \cdot R_{\text{out}} \cdot (V_{\text{in}} + I_L \cdot (R_{\text{DSon_LS}} - R_{\text{DSon_HS}}))) / (((D_{\text{on}} \cdot R_{\text{DSon_HS}} + R_L + R_{\text{DSon_LS}} - D_{\text{on}} \cdot R_{\text{DSon_LS}} + R_{\text{out}}) + s \cdot (C \cdot R_{\text{out}} \cdot (R_L + D_{\text{on}} \cdot R_{\text{DSon_HS}} + R_{\text{DSon_LS}} - D_{\text{on}} \cdot R_{\text{DSon_LS}}) + L) + s^2 \cdot L \cdot C \cdot R_{\text{out}})))$$

$$\frac{i_L}{d} = \frac{(V_{\text{in}} + I_L \cdot (R_{\text{DSon_LS}} - R_{\text{DSon_HS}}) + s \cdot C \cdot R_{\text{out}} \cdot (V_{\text{in}} + I_L \cdot (R_{\text{DSon_LS}} - R_{\text{DSon_HS}})))}{((D_{\text{on}} \cdot (R_{\text{DSon_HS}} - R_{\text{DSon_LS}}) + R_L + R_{\text{DSon_LS}} + R_{\text{out}}) + s \cdot (C \cdot R_{\text{out}} \cdot (R_L + D_{\text{on}} \cdot (R_{\text{DSon_HS}} - R_{\text{DSon_LS}}) + L) + s^2 \cdot L \cdot C \cdot R_{\text{out}}))}$$

$$G_{i \cdot d} \big|_{v_{\text{in}}=0}$$

Circuit model

Peak Current Mode Control Transfer Functions

$\langle i_L \rangle = i_{control}$ average i_L is the same as control current in a stable system

$$\langle v_L \rangle = s \cdot L \cdot i_L = D_{on} \cdot v_{in} - i_L \cdot (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}) + d \cdot (V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS})) - v_{out}$$

$$s \cdot L \cdot i_{control} = D_{on} \cdot v_{in} - i_{control} \cdot (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}) + d \cdot (V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS})) - v_{out}$$

$$d \cdot (V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS})) = s \cdot L \cdot i_{control} - D_{on} \cdot v_{in} + i_{control} \cdot (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}) + v_{out}$$

$$\begin{aligned} d &= \frac{s \cdot L \cdot i_{control} - D_{on} \cdot v_{in} + i_{control} \cdot (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}) + v_{out}}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))} \\ &= \frac{(s \cdot L + (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS})) \cdot i_{control} - D_{on} \cdot v_{in} + v_{out}}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))} = \left(\frac{(s \cdot L + (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}))}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))} \right) \cdot i_{control} \\ &\quad - \frac{D_{on}}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))} \cdot v_{in} + \frac{1}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))} \cdot v_{out} \end{aligned}$$

$$\langle i_c \rangle = i_{cap} = i_L - i_{out} = i_{control} - i_{out}$$

$$\begin{aligned} \langle i_{in} \rangle &= D_{on} \cdot i_L + d \cdot I_L = D_{on} \cdot i_{control} + d \cdot I_L = D_{on} \cdot i_L + I_L \cdot \frac{(s \cdot L + (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS})) \cdot i_{control} - D_{on} \cdot v_{in} + v_{out}}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))} = \left(D_{on} \right. \\ &\quad \left. + \frac{(s \cdot L + (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}))}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))} \right) \cdot i_{control} - \left(\frac{D_{on}}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))} \right) \cdot v_{in} \\ &\quad \left. + \left(\frac{1}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))} \right) \cdot v_{out} \right) \end{aligned}$$

$$\langle i_{in} \rangle = A \cdot i_{control} - B \cdot v_{in} + C \cdot v_{out}$$

$$A = D_{on} + \frac{(s \cdot L + (D_{on} \cdot R_{DSon_HS} + R_L + D_{off} \cdot R_{DSon_LS}))}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))} = D_{on} + \frac{s \cdot L + (D_{on} \cdot R_{DSon_HS} + R_L + R_{DSon_LS} - D_{on} \cdot R_{DSon_LS})}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))}$$

$$B = \frac{D_{on}}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))}$$

$$C = \frac{1}{(V_{in} + I_L \cdot (-R_{DSon_HS} + R_{DSon_LS}))}$$

$$\langle i_c \rangle = i_{control} - i_{out} = i_{control} - \frac{V_{out}}{R_{out}}$$

$$s \cdot C \cdot v_{out} = i_{cap} = i_{control} - \frac{V_{out}}{R_{out}}$$

More Accurate Model of Peak Current Mode Control·(m_L does not perturb)

$$\langle i_L \rangle = \langle i_{control} \rangle - m_a \cdot d \cdot T_s - d \cdot \frac{m_1 \cdot d \cdot T_s}{2} - d' \cdot \frac{m_2 \cdot d' \cdot T_s}{2}$$

$$\langle i_L \rangle = \langle i_{control} \rangle - m_a \cdot d \cdot T_s - m_1 \cdot \frac{d^2 \cdot T_s}{2} - m_2 \cdot \frac{d'^2 \cdot T_s}{2}$$

$$\langle I_L + i_L \rangle = \langle I_{control} + i_{control} \rangle - M_a \cdot T_s \cdot (D_{on} + d) - \frac{T_s}{2} \cdot (M_1 + m_1) \cdot (D_{on} + d)^2 - \frac{T_s}{2} \cdot (M_2 + m_2) \cdot (D_{off} - d)^2$$

$$\langle i_L \rangle = \langle i_{control} \rangle - M_a \cdot T_s \cdot D_{on} - M_a \cdot T_s \cdot d - \frac{T_s}{2} \cdot (M_1 + m_1) (D_{on}^2 + 2 \cdot D_{on} \cdot d + d^2) - \frac{T_s}{2} \cdot (M_2 + m_2) \cdot (D_{off}^2 - 2 \cdot D_{off} \cdot d - d^2)$$

$$\langle i_L \rangle = \langle i_{control} \rangle - M_a \cdot T_s \cdot d - \frac{T_s}{2} \cdot M_1 \cdot D_{on}^2 - T_s \cdot M_1 \cdot D_{on} \cdot d - \frac{T_s}{2} \cdot M_1 \cdot d^2 - \frac{T_s}{2} \cdot M_2 \cdot D_{off}^2 + T_s \cdot M_2 \cdot D_{off}$$

$$\cdot d + \frac{T_s}{2} \cdot M_2 \cdot d^2 - \frac{T_s}{2} \cdot m_2 \cdot D_{off}^2 + T_s \cdot m_2 \cdot D_{off} \cdot d + \frac{T_s}{2} \cdot m_2 \cdot d^2$$

$$\begin{aligned} \langle i_L \rangle = & \langle i_{control} \rangle - M_a \cdot T_s \cdot d - M_1 \cdot T_s \cdot D_{on} \cdot d - \frac{T_s}{2} \cdot m_1 \cdot D_{on}^2 + M_2 \cdot T_s \cdot D_{off} \cdot d - \frac{T_s}{2} \cdot m_2 \cdot D_{off}^2 = \langle i_{control} \rangle - M_a \cdot T_s \cdot d - M_1 \cdot T_s \cdot D_{on} \cdot d \\ & - \frac{T_s}{2} \cdot D_{on}^2 \cdot m_1 - \frac{T_s}{2} \cdot D_{off}^2 \cdot m_2 \end{aligned}$$

$$\langle i_L \rangle = \langle i_{control} \rangle - M_a \cdot T_s \cdot d - \frac{T_s}{2} \cdot D_{on}^2 \cdot m_1 - \frac{T_s}{2} \cdot D_{off}^2 \cdot m_2$$

$$\begin{aligned} d = & \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle - \frac{T_s}{2} \cdot D_{on}^2 \cdot m_1 - \frac{T_s}{2} \cdot D_{off}^2 \cdot m_2 \right) = \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle - \frac{T_s}{2} \cdot D_{on}^2 \cdot \left(\frac{v_{in} - v_{out} - i_L \cdot (R_{DSon_HS} + R_L)}{L} \right) \right) \\ & - \frac{T_s}{2} \cdot D_{off}^2 \cdot \left(- \frac{(v_{out} + i_L \cdot (R_{DSon_LS} + R_L))}{L} \right) \end{aligned}$$

$$\begin{aligned} d = & \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle - \frac{T_s}{2} \cdot D_{on}^2 \cdot \left(\frac{v_{in}}{L} \right) + \frac{T_s}{2} \cdot D_{on}^2 \cdot \left(\frac{v_{out}}{L} \right) + \frac{T_s}{2} \cdot D_{on}^2 \cdot i_L \cdot \frac{(R_{DSon_HS} + R_L)}{L} + \frac{T_s}{2} \cdot D_{off}^2 \cdot \left(\frac{v_{out}}{L} \right) + \frac{T_s}{2} \cdot D_{off}^2 \cdot i_L \right. \\ & \cdot \left. \left(\frac{(R_{DSon_LS} + R_L)}{L} \right) \right) \end{aligned}$$

$$\begin{aligned} d = & \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle \cdot \left(1 + \frac{T_s}{2} \cdot D_{on}^2 \cdot \frac{(R_{DSon_HS} + R_L)}{L} + D_{off}^2 \cdot \frac{(R_{DSon_LS} + R_L)}{L} \right) + v_{out} \cdot \left(\frac{T_s}{2} \cdot \left(\frac{D_{on}^2 + D_{off}^2}{L} \right) \right) - v_{in} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \right) \end{aligned}$$

$$\begin{aligned} d = & \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle \cdot \left(1 + \frac{T_s}{2} \cdot D_{on}^2 \cdot \frac{(R_{DSon_HS} + R_L)}{L} + (1 - D_{on})^2 \cdot \frac{(R_{DSon_LS} + R_L)}{L} \right) + v_{out} \cdot \left(\frac{T_s}{2} \cdot \left(\frac{D_{on}^2 + (1 - D_{on})^2}{L} \right) \right) \right) \\ & - v_{in} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \end{aligned}$$

$$d = \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle \cdot \left(1 + \frac{T_s}{2} \cdot \left(D_{on}^2 \cdot \frac{(R_{DSon_HS} + R_L)}{L} + (1 - 2 \cdot D_{on} - D_{on}^2) \cdot \frac{(R_{DSon_LS} + R_L)}{L} \right) \right) + v_{out} \cdot \left(\frac{T_s}{2} \right) \right) \cdot \left(\frac{D_{on}^2 + (1 - 2 \cdot D_{on} - D_{on}^2)}{L} \right) - v_{in} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \right)$$

$$d = \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle \cdot \left(1 + \frac{T_s}{2} \cdot \left(D_{on}^2 \cdot \frac{(R_{DSon_HS} + R_L)}{L} + (1 - 2 \cdot D_{on} - D_{on}^2) \cdot \frac{(R_{DSon_LS} + R_L)}{L} \right) \right) + v_{out} \cdot \left(\frac{T_s}{2} \right) \right) \cdot \left(\frac{(1 - 2 \cdot D_{on})}{L} \right) - v_{in} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \right)$$

$$d = \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle \cdot \left(1 + \frac{T_s}{2} \cdot \left(D_{on}^2 \cdot \frac{(R_{DSon_HS} + R_L)}{L} + \frac{(R_{DSon_LS} + R_L)}{L} - 2 \cdot D_{on} \cdot \frac{(R_{DSon_LS} + R_L)}{L} - D_{on}^2 \right) \right) \right) \cdot \left(\frac{R_{DSon_LS} + R_L}{L} \right) + v_{out} \cdot \left(\frac{T_s}{2} \cdot \frac{(1 - 2 \cdot D_{on})}{L} \right) - v_{in} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \right)$$

$$d = \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle \cdot \left(1 + \frac{T_s}{2} \cdot \left(D_{on}^2 \cdot \frac{R_{DSon_HS}}{L} + \frac{R_L}{L} + \frac{R_{DSon_LS}}{L} - 2 \cdot D_{on} \cdot \frac{R_{DSon_LS}}{L} - D_{on}^2 \cdot \frac{R_{DSon_LS}}{L} - \frac{R_L}{L} \right) \right) + v_{out} \cdot \left(\frac{T_s}{2} \cdot \frac{(1 - 2 \cdot D_{on})}{L} \right) - v_{in} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \right) \cdot \left(\frac{D_{on}^2 \cdot \frac{R_L}{L}}{L} \right)$$

$$d = \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle \cdot \left(1 + \frac{T_s}{2} \cdot \left(D_{on}^2 \cdot \frac{R_{DSon_HS}}{L} + \frac{R_L}{L} + \frac{R_{DSon_LS}}{L} - 2 \cdot D_{on} \cdot \frac{R_{DSon_LS}}{L} - D_{on}^2 \cdot \frac{R_{DSon_LS}}{L} \right) \right) + v_{out} \right) \cdot \left(\frac{T_s}{2} \cdot \frac{(1 - 2 \cdot D_{on})}{L} \right) - v_{in} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \right)$$

$$d = \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle \cdot \left(1 + \frac{T_s}{2} \cdot \left(D_{on}^2 \cdot \frac{R_{DSon_HS}}{L} - D_{on}^2 \cdot \frac{R_{DSon_LS}}{L} + \frac{R_{DSon_LS}}{L} - 2 \cdot D_{on} \cdot \frac{R_{DSon_LS}}{L} + \frac{R_L}{L} - 2 \cdot D_{on} \cdot \frac{R_L}{L} \right) \right) + v_{out} \right)$$

$$\cdot \left(\frac{T_s}{2} \cdot \frac{(1 - 2 \cdot D_{on})}{L} \right) - v_{in} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \Bigg)$$

$$d = \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle \cdot \left(1 + \frac{T_s}{2} \cdot \left(D_{on}^2 \cdot \left(\frac{R_{DSon_HS} - R_{DSon_LS}}{L} + (1 - 2 \cdot D_{on}) \cdot \frac{R_L}{L} \right) \right) + v_{out} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \right) - v_{in} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \right)$$

$$d = \frac{1}{M_a \cdot T_s} \cdot \left(\langle i_{control} \rangle - \langle i_L \rangle \cdot \left(1 + \frac{T_s}{2} \cdot \left(D_{on}^2 \cdot \left(\frac{R_{DSon_HS} - R_{DSon_LS}}{L} + (1 - 2 \cdot D_{on}) \cdot \left(\frac{R_{DSon_LS} + R_L}{L} \right) \right) \right) + v_{out} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \right) - v_{in} \cdot \left(\frac{T_s}{2} \cdot \frac{D_{on}^2}{L} \right) \right)$$

controller transfer function · (not plant function)