

Step	Algorithm:
1a	
4	where
2	
3	while do
2,3	\wedge
5a	where
6	
8	
5b	
7	
2	
	endwhile
2,3	$\wedge \neg(\quad)$
1b	

Step	Algorithm: $[y] := \text{SYMV_L_UNB_VAR4}(A, x, y)$
1a	$y = \hat{y}$
4	$A \rightarrow \left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right), y \rightarrow \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right)$ <p>where A_{TL} is 0×0, x_T has 0 rows, y_T has 0 rows</p>
2	$\left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) = \left(\begin{array}{c} \hat{y}_T + A_{TL}x_T + A_{BL}^T x_B \\ \hline \hat{y}_B + A_{BL}x_T \end{array} \right)$
3	while $m(A_{TL}) < m(A)$ do
2,3	$\left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) = \left(\begin{array}{c} \hat{y}_T + A_{TL}x_T + A_{BL}^T x_B \\ \hline \hat{y}_B + A_{BL}x_T \end{array} \right) \wedge m(A_{TL}) < m(A)$
5a	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right) \rightarrow \left(\begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) \rightarrow \left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$ <p>where α_{11} is 1×1, χ_1 has 1 row, ψ_1 has 1 row</p>
6	$\left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right) = \left(\begin{array}{c} \hat{y}_0 + A_{00}x_0 + (a_{10}^T)T\chi_1 + A_{20}^T x_2 \\ \hline \hat{\psi}_1 + a_{10}^T x_0 \\ \hline \hat{y}_2 + A_{20}x_0 \end{array} \right)$
8	$\left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right) := \left(\begin{array}{c} y_0 \\ \hline \psi_1 + a_{11}\chi_1 + a_{21}^T x_2 \\ \hline y_2 + a_{21}\chi_1 \end{array} \right)$
5b	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left(\begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$
7	$\left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right) = \left(\begin{array}{c} \hat{y}_0 + A_{00}x_0 + (a_{10}^T)T\chi_1 + A_{20}^T x_2 \\ \hline \hat{\psi}_1 + a_{10}^T x_0 + a_{11}\chi_1 + a_{21}^T x_2 \\ \hline \hat{y}_2 + A_{20}x_0 + a_{21}\chi_1 \end{array} \right)$
2	$\left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) = \left(\begin{array}{c} \hat{y}_T + A_{TL}x_T + A_{BL}^T x_B \\ \hline \hat{y}_B + A_{BL}x_T \end{array} \right)$
	endwhile
2,3	$\left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) = \left(\begin{array}{c} \hat{y}_T + A_{TL}x_T + A_{BL}^T x_B \\ \hline \hat{y}_B + A_{BL}x_T \end{array} \right) \wedge \neg(m(A_{TL}) < m(A))$
1b	$[y] = \text{Symv_l}(A, x, \hat{y})$

Algorithm: $[y] := \text{SYMV_L_UNB_VAR4}(A, x, y)$

$$A \rightarrow \left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right), y \rightarrow \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right)$$

where A_{TL} is 0×0 , x_T has 0 rows, y_T has 0 rows

while $m(A_{TL}) < m(A)$ **do**

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right) \rightarrow \left(\begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) \rightarrow \left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$$

where α_{11} is 1×1 , χ_1 has 1 row, ψ_1 has 1 row

$$\left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right) := \left(\begin{array}{c} y_0 \\ \hline \psi_1 + a_{11}\chi_1 + a_{21}^T x_2 \\ \hline y_2 + a_{21}\chi_1 \end{array} \right)$$

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left(\begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$$

endwhile

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5b	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left(\begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$
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3	while $m(A_{TL}) < m(A)$ do
2,3	$\left(\begin{array}{c} y_T \\ y_B \end{array} \right) = \left(\begin{array}{c} \hat{y}_T + A_{TL}x_T + A_{BL}^T x_B \\ \hat{y}_B + A_{BL}x_T \end{array} \right) \wedge m(A_{TL}) < m(A)$
5a	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ x_B \end{array} \right) \rightarrow \left(\begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ y_B \end{array} \right) \rightarrow \left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$ where α_{11} is 1×1 , χ_1 has 1 row, ψ_1 has 1 row
6	$\left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right) = \left(\begin{array}{c} \hat{y}_0 + A_{00}x_0 + (a_{10}^T)T\chi_1 + A_{20}^T x_2 \\ \hat{\psi}_1 + a_{10}^T x_0 \\ \hat{y}_2 + A_{20}x_0 \end{array} \right)$
8	$\left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right) := \left(\begin{array}{c} y_0 \\ \psi_1 + a_{11}\chi_1 + a_{21}^T x_2 \\ y_2 + a_{21}\chi_1 \end{array} \right)$
5b	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ x_B \end{array} \right) \leftarrow \left(\begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ y_B \end{array} \right) \leftarrow \left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$
7	$\left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right) = \left(\begin{array}{c} \hat{y}_0 + A_{00}x_0 + (a_{10}^T)T\chi_1 + A_{20}^T x_2 \\ \hat{\psi}_1 + a_{10}^T x_0 + a_{11}\chi_1 + a_{21}^T x_2 \\ \hat{y}_2 + A_{20}x_0 + a_{21}\chi_1 \end{array} \right)$
2	$\left(\begin{array}{c} y_T \\ y_B \end{array} \right) = \left(\begin{array}{c} \hat{y}_T + A_{TL}x_T + A_{BL}^T x_B \\ \hat{y}_B + A_{BL}x_T \end{array} \right)$
	endwhile
2,3	$\left(\begin{array}{c} y_T \\ y_B \end{array} \right) = \left(\begin{array}{c} \hat{y}_T + A_{TL}x_T + A_{BL}^T x_B \\ \hat{y}_B + A_{BL}x_T \end{array} \right) \wedge \neg(m(A_{TL}) < m(A))$
1b	$[y] = \text{Symv_l}(A, x, \hat{y})$

Step	Algorithm: $[y] := \text{SYMV_L_UNB_VAR4}(A, x, y)$
	$A \rightarrow \left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right), y \rightarrow \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right)$ <p>where A_{TL} is 0×0, x_T has 0 rows, y_T has 0 rows</p>
	while $m(A_{TL}) < m(A)$ do
	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right) \rightarrow \left(\begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) \rightarrow \left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$ <p>where α_{11} is 1×1, χ_1 has 1 row, ψ_1 has 1 row</p>
	$\left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right) := \left(\begin{array}{c} y_0 \\ \hline \psi_1 + a_{11}\chi_1 + a_{21}^T x_2 \\ \hline y_2 + a_{21}\chi_1 \end{array} \right)$
	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left(\begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$
	endwhile

Algorithm: $[y] := \text{SYMV_L_UNB_VAR4}(A, x, y)$

$$A \rightarrow \left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right), y \rightarrow \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right)$$

where A_{TL} is 0×0 , x_T has 0 rows, y_T has 0 rows

while $m(A_{TL}) < m(A)$ **do**

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right) \rightarrow \left(\begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) \rightarrow \left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$$

where α_{11} is 1×1 , χ_1 has 1 row, ψ_1 has 1 row

$$\left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right) := \left(\begin{array}{c} y_0 \\ \hline \psi_1 + a_{11}\chi_1 + a_{21}^T x_2 \\ \hline y_2 + a_{21}\chi_1 \end{array} \right)$$

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left(\begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left(\begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$$

endwhile