

Step	<b>Algorithm:</b> $[y] := \text{SYMV\_L\_UNB\_VAR5}(A, x, y)$
1a	$y = \hat{y}$
4	$A \rightarrow \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right), y \rightarrow \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right)$ <p>where <math>A_{BR}</math> is <math>0 \times 0</math>, <math>x_B</math> has 0 rows, <math>y_B</math> has 0 rows</p>
2	$\left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) = \left( \begin{array}{c} \hat{y}_T \\ \hline \hat{y}_B + A_{BR}x_B \end{array} \right)$
3	<b>while</b> $m(A_{BR}) < m(A)$ <b>do</b>
2,3	$\left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) = \left( \begin{array}{c} \hat{y}_T \\ \hline \hat{y}_B + A_{BR}x_B \end{array} \right) \wedge m(A_{BR}) < m(A)$
5a	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \rightarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \rightarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$ <p>where <math>\alpha_{11}</math> is <math>1 \times 1</math>, <math>\chi_1</math> has 1 row, <math>\psi_1</math> has 1 row</p>
6	$\left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right) = \left( \begin{array}{c} \hat{y}_0 \\ \hline \hat{\psi}_1 \\ \hline \hat{y}_2 + A_{22}x_2 \end{array} \right)$
8	$\psi_1 := \psi_1 + a_{11}\chi_1 + a_{21}^T x_2$ $y_2 := y_2 + a_{21}\chi_1$
5b	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$
7	$\left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right) = \left( \begin{array}{c} \hat{y}_0 \\ \hline \hat{\psi}_1 + a_{11}\chi_1 + a_{21}^T x_2 \\ \hline \hat{y}_2 + a_{21}\chi_1 + A_{22}x_2 \end{array} \right)$
2	$\left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) = \left( \begin{array}{c} \hat{y}_T \\ \hline \hat{y}_B + A_{BR}x_B \end{array} \right)$
	<b>endwhile</b>
2,3	$\left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) = \left( \begin{array}{c} \hat{y}_T \\ \hline \hat{y}_B + A_{BR}x_B \end{array} \right) \wedge \neg(m(A_{BR}) < m(A))$
1b	$[y] = \text{symv.l}(A, x, \hat{y}) = Ax + \hat{y}$

**Algorithm:**  $[y] := \text{SYMV\_L\_UNB\_VAR5}(A, x, y)$

$$A \rightarrow \left( \begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right), y \rightarrow \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right)$$

**where**  $A_{BR}$  is  $0 \times 0$ ,  $x_B$  has 0 rows,  $y_B$  has 0 rows

**while**  $m(A_{BR}) < m(A)$  **do**

$$\left( \begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \rightarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \rightarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$$

**where**  $\alpha_{11}$  is  $1 \times 1$ ,  $\chi_1$  has 1 row,  $\psi_1$  has 1 row

$$\psi_1 := \psi_1 + a_{11}\chi_1 + a_{21}^T x_2 \quad y_2 := y_2 + a_{21}\chi_1$$

$$\left( \begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$$

**endwhile**

Step	Algorithm: $[y] := \text{SYMV\_L\_UNB\_VAR5}(A, x, y)$
1a	$y = \hat{y}$
4	where
2	
3	while do
2,3	$\wedge$
5a	where
6	
8	
5b	
7	
2	
	endwhile
2,3	$\wedge \neg( \quad )$
1b	$[y] = \text{symv.l}(A, x, \hat{y}) = Ax + \hat{y}$

Step	Algorithm: $[y] := \text{SYMV\_L\_UNB\_VAR5}(A, x, y)$
1a	$y = \hat{y}$
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	where
2	$\left( \frac{y_T}{y_B} \right) = \left( \frac{\hat{y}_T}{\hat{y}_B + A_{BR}x_B} \right)$
3	while do
2,3	$\left( \frac{y_T}{y_B} \right) = \left( \frac{\hat{y}_T}{\hat{y}_B + A_{BR}x_B} \right) \wedge$
5a	
	where
6	
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5b	
7	
2	$\left( \frac{y_T}{y_B} \right) = \left( \frac{\hat{y}_T}{\hat{y}_B + A_{BR}x_B} \right)$
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3	while $m(A_{BR}) < m(A)$ do
2,3	$\left( \frac{y_T}{y_B} \right) = \left( \frac{\hat{y}_T}{\hat{y}_B + A_{BR}x_B} \right) \wedge m(A_{BR}) < m(A)$
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2,3	$\left( \frac{y_T}{y_B} \right) = \left( \frac{\hat{y}_T}{\hat{y}_B + A_{BR}x_B} \right) \wedge \neg(m(A_{BR}) < m(A))$
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2	$\begin{pmatrix} y_T \\ y_B \end{pmatrix} = \begin{pmatrix} \hat{y}_T \\ \hat{y}_B + A_{BR}x_B \end{pmatrix}$
3	while $m(A_{BR}) < m(A)$ do
2,3	$\begin{pmatrix} y_T \\ y_B \end{pmatrix} = \begin{pmatrix} \hat{y}_T \\ \hat{y}_B + A_{BR}x_B \end{pmatrix} \wedge m(A_{BR}) < m(A)$
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5a	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \rightarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \rightarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$ where $\alpha_{11}$ is $1 \times 1$ , $\chi_1$ has 1 row, $\psi_1$ has 1 row
6	
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5b	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$
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	<b>endwhile</b>
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6	$\left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right) = \left( \begin{array}{c} \hat{y}_0 \\ \hline \hat{\psi}_1 \\ \hline \hat{y}_2 + A_{22}x_2 \end{array} \right)$
8	$\psi_1 := \psi_1 + a_{11}\chi_1 + a_{21}^T x_2$ $y_2 := y_2 + a_{21}\chi_1$
5b	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$
7	$\left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right) = \left( \begin{array}{c} \hat{y}_0 \\ \hline \hat{\psi}_1 + a_{11}\chi_1 + a_{21}^T x_2 \\ \hline \hat{y}_2 + a_{21}\chi_1 + A_{22}x_2 \end{array} \right)$
2	$\left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) = \left( \begin{array}{c} \hat{y}_T \\ \hline \hat{y}_B + A_{BR}x_B \end{array} \right)$
	<b>endwhile</b>
2,3	$\left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) = \left( \begin{array}{c} \hat{y}_T \\ \hline \hat{y}_B + A_{BR}x_B \end{array} \right) \wedge \neg(m(A_{BR}) < m(A))$
1b	$[y] = \text{symv.l}(A, x, \hat{y}) = Ax + \hat{y}$

Step	<b>Algorithm:</b> $[y] := \text{SYMV\_L\_UNB\_VAR5}(A, x, y)$
	$A \rightarrow \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right), y \rightarrow \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right)$ <p><b>where</b> <math>A_{BR}</math> is <math>0 \times 0</math>, <math>x_B</math> has 0 rows, <math>y_B</math> has 0 rows</p>
	<b>while</b> $m(A_{BR}) < m(A)$ <b>do</b>
	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \rightarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \rightarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$ <p><b>where</b> <math>\alpha_{11}</math> is <math>1 \times 1</math>, <math>\chi_1</math> has 1 row, <math>\psi_1</math> has 1 row</p>
	$\psi_1 := \psi_1 + a_{11}\chi_1 + a_{21}^T x_2$ $y_2 := y_2 + a_{21}\chi_1$
	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$
	<b>endwhile</b>

**Algorithm:**  $[y] := \text{SYMV\_L\_UNB\_VAR5}(A, x, y)$

$$A \rightarrow \left( \begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right), y \rightarrow \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right)$$

**where**  $A_{BR}$  is  $0 \times 0$ ,  $x_B$  has 0 rows,  $y_B$  has 0 rows

**while**  $m(A_{BR}) < m(A)$  **do**

$$\left( \begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \rightarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \rightarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$$

**where**  $\alpha_{11}$  is  $1 \times 1$ ,  $\chi_1$  has 1 row,  $\psi_1$  has 1 row

$$\psi_1 := \psi_1 + a_{11}\chi_1 + a_{21}^T x_2 \quad y_2 := y_2 + a_{21}\chi_1$$

$$\left( \begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ \hline x_B \end{array} \right) \leftarrow \left( \begin{array}{c} x_0 \\ \hline \chi_1 \\ \hline x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ \hline y_B \end{array} \right) \leftarrow \left( \begin{array}{c} y_0 \\ \hline \psi_1 \\ \hline y_2 \end{array} \right)$$

**endwhile**