

CPE 381: Fundamentals of Signals and Systems for Computer Engineers

**Homework #5**

Due: Monday, April 13 at 9:35 am

Please bring hardcopy to the class and upload softcopy to Canvas

**Student name:**

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1 20	2 20	3 16	4 18	5 20	6 6	$\Sigma$

1. (20 points) A discrete time IIR system with input  $x[n]$  and output  $y[n]$  is represented by the equation:

$$y[n] = 0.2 \cdot y[n-2] + x[n] \quad n \geq 0$$

- find the impulse response  $h(n)$  of the system, by assuming that initial conditions are zero ( $y[n]=h[n]=0$ ,  $n<0$ ) and  $x[n]=\delta[n]$ .
- find the impulse response alternatively by using recursive relation between  $x[n]$  and  $y[n]$ .
- plot  $h[n]$  using MATLAB function filter.

2. (20 points) An FIR filter is represented as:

$$y[n] = \sum_{k=0}^5 k \cdot x[n-k]$$

- find and plot the impulse response of this filter.
- is this a causal and stable filter? Explain.
- find and plot the unit-step response  $s[n]$  for this filter.
- what is the maximum value of the output if the maximum input is 5?
- plot  $h[n]$  and  $s[n]$  using MATLAB function filter.

3. (16 points) Let  $x[n] = \{0, 1, 1, 1, 0\}$  and  $h[n] = \{1.5, 1, 0.5\}$ .

Compute and plot the convolution  $y[n] = x[n] * h[n]$ .

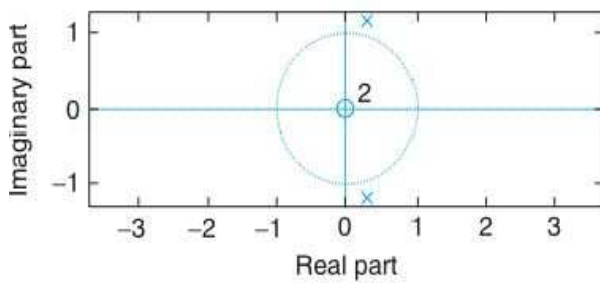
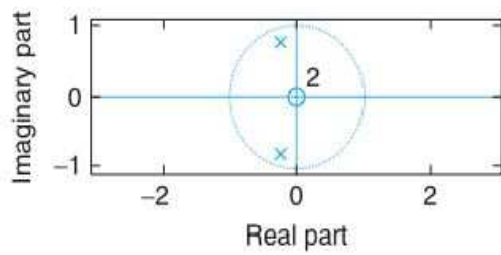
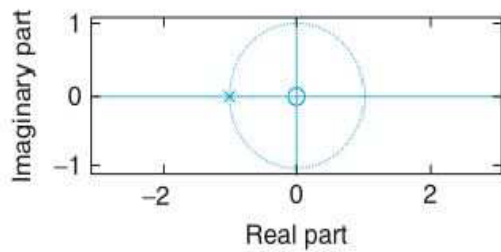
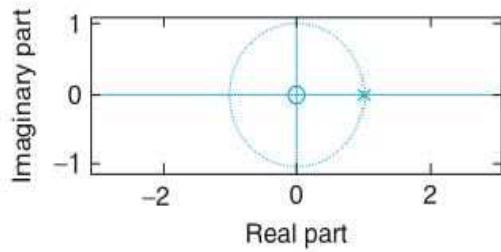
4. (18 points)

a) (6 points) Explain the difference between hard and soft real-time systems.

b) (7 points) Maximum frequency of the input is 600Hz. The microcontroller processes each sample in 1200 clock cycles with clock frequency  $F_c = 1\text{MHz}$ . Can this system run in real-time?

c) (5 points) What is the minimum frequency of the clock that allows real-time operation with 2x oversampling of the input?

5. (20 points) Describe the effect of pole location on the inverse Z-transform for the following cases.



6. (6 points) If  $X(z)$  is the Z-transform of a causal signal  $x[n]$ , then

Initial value is  $x[0] = \underline{\hspace{2cm}}$

Final value is  $\lim_{n \rightarrow \infty} x[n] = \underline{\hspace{2cm}}$