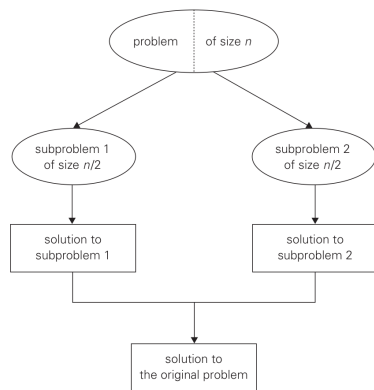


Divide-and-Conquer



- General divide and conquer recurrence.

**ALGORITHM** *Mergesort*( $A[0..n-1]$ )

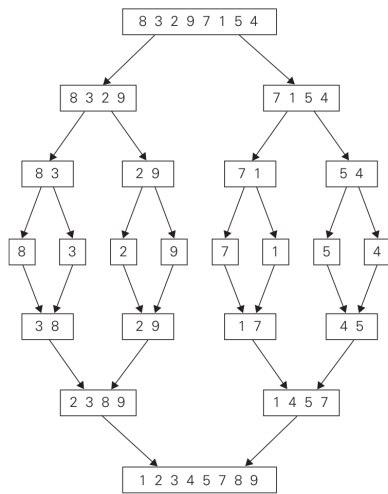
//Sorts array  $A[0..n-1]$  by recursive mergesort  
 //Input: An array  $A[0..n-1]$  of orderable elements  
 //Output: Array  $A[0..n-1]$  sorted in nondecreasing order  
**if**  $n > 1$   
   copy  $A[0..\lfloor n/2 \rfloor - 1]$  to  $B[0..\lfloor n/2 \rfloor - 1]$   
   copy  $A[\lfloor n/2 \rfloor..n-1]$  to  $C[0..\lceil n/2 \rceil - 1]$   
   *Mergesort*( $B[0..\lfloor n/2 \rfloor - 1]$ )  
   *Mergesort*( $C[0..\lceil n/2 \rceil - 1]$ )  
   *Merge*( $B, C, A$ ) //see below

*merge!*

**ALGORITHM** *Merge*( $B[0..p-1], C[0..q-1], A[0..p+q-1]$ )

//Merges two sorted arrays into one sorted array  
 //Input: Arrays  $B[0..p-1]$  and  $C[0..q-1]$  both sorted  
 //Output: Sorted array  $A[0..p+q-1]$  of the elements of  $B$  and  $C$   
 $i \leftarrow 0$ ;  $j \leftarrow 0$ ;  $k \leftarrow 0$   
**while**  $i < p$  **and**  $j < q$  **do**  
   **if**  $B[i] \leq C[j]$   
      $A[k] \leftarrow B[i]$ ;  $i \leftarrow i + 1$   
   **else**  $A[k] \leftarrow C[j]$ ;  $j \leftarrow j + 1$   
    $k \leftarrow k + 1$   
**if**  $i = p$   
   copy  $C[j..q-1]$  to  $A[k..p+q-1]$   
**else** copy  $B[i..p-1]$  to  $A[k..p+q-1]$

Example!



Efficiency: