

Ohm's Law

$$V_2 = 2 I_2$$

$$V_3 = -8 I_3$$

$$\begin{aligned} V_2 &= 2V \\ V_3 &= 8V \end{aligned}$$

KCL

$$\textcircled{1} \quad I_1 = I_2$$

$$\textcircled{2} \quad I_2 + I_3 = 0$$

$$\textcircled{3} \quad 0 = I_1 + I_3$$

$$I_1 = I_2 = -I_3$$

KVL

$$10 - V_2 - V_3 = 0$$

$$10 - (2I_2) - (-8I_3) = 0$$

$$10 - (2(-I_3)) - (-8I_3) = 0$$

$$10 + 2I_3 + 8I_3 = 0$$

$$10I_3 = -10$$

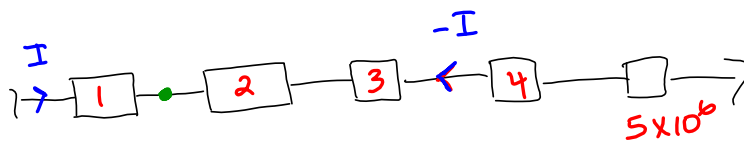
$$I_3 = -1A$$

$$I_2 = 1A$$

$$I_1 = 1A$$

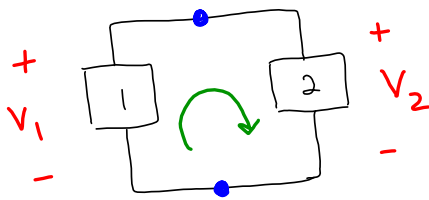
Series & Parallel Connections

- when a node only has two element connected, we say those elements are connected in series.
- when element are in series, they experience the same current.



Parallel Connection

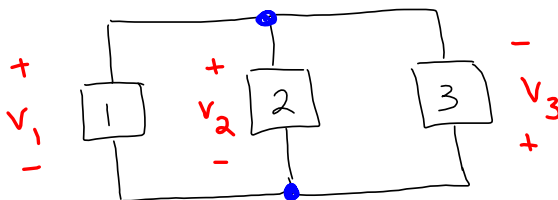
Elements that share the same two nodes are in parallel & thus have the same voltage.



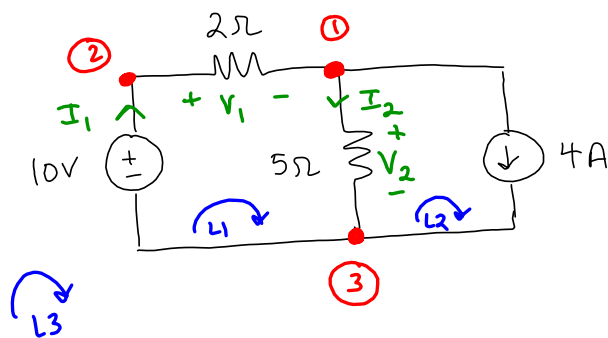
by KVL:

$$+V_1 - V_2 = 0$$

$$V_1 = V_2$$



$$V_1 = V_2 = -V_3$$



Use Brute Force to find all voltages & currents and powers.

KCL

$$\textcircled{1} \quad I_1 = I_2 + 4$$

$$\textcircled{3} \quad 4 + I_2 = I_1$$

Ohm's Law

$$V_1 = 2I_1$$

$$V_2 = 5I_2$$

KVL

$$\textcircled{L1} \quad 10 - V_1 - V_2 = 0$$

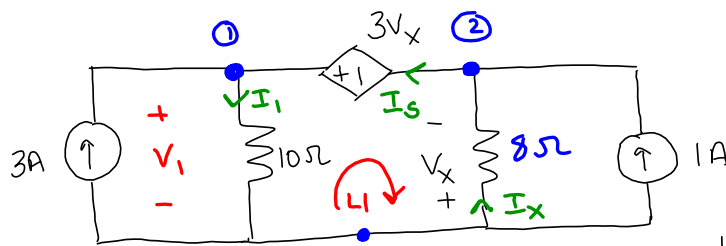
$$\textcircled{L3} \quad 10 - V_1 - V_2 = 0$$

$$2I_1 + 5I_2 = 10$$

$$I_1 - I_2 = 4$$

$$I_1 = 4.29 \text{ A} \quad V_1 = 8.57 \text{ V}$$

$$I_2 = 0.29 \text{ A} \quad V_2 = 1.43 \text{ V}$$



Find all currents,
voltages + powers.

KCL

$$\textcircled{1} \quad I_S + 3 = I_1$$

$$\textcircled{2} \quad I_x + 1 = I_S$$

KVL

$$\textcircled{L1} \quad V_1 - 3V_x + V_x = 0$$

Ohm's Law

$$V_1 = 10 I_1$$

$$V_x = 8 I_x$$

$$I_1 - I_S = 3$$

$$-I_x + I_S = 1$$

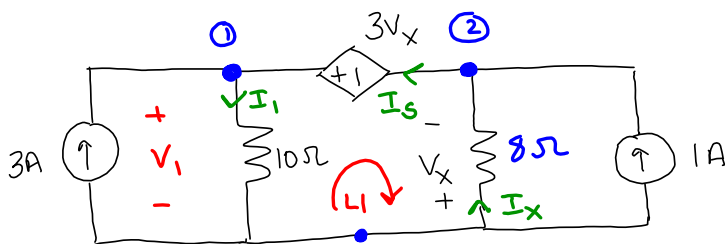
$$10 I_1 - 16 I_x = 0$$

$$I_x = 3.33 \text{ A} \quad I_S = 2.33 \text{ A}$$

$$I_1 = 5.33 \text{ A}$$

$$V_1 = 53.33 \text{ V}$$

$$V_x = 26.67 \text{ V}$$



$$\begin{aligned} I_x &= 3.33 \text{ A} & I_s &= 2.33 \text{ A} \\ I_1 &= 5.33 \text{ A} & V_x &= 26.67 \text{ V} \\ V_1 &= 53.33 \text{ V} \end{aligned}$$

Sources : $P = VI$

$$3\text{A} : P = V_1(3) = 160 \text{ W, Del}$$

$$\begin{aligned} 1\text{A} : P &= V_x(1) = 26.67 \text{ W, Abs} \\ P_1 &= -26.67 \text{ W, Del} \end{aligned}$$

$$3V_x : P = (3V_x)(I_s) = 186.67 \text{ W, Del}$$

Resistors : $P = I^2 R$

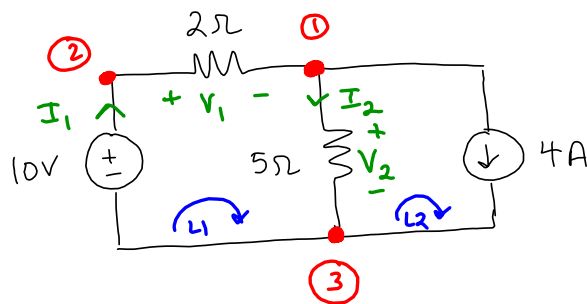
$$\begin{aligned} 10\Omega : P &= I_1^2(10) \\ &= 284.44 \text{ W, Abs} \end{aligned}$$

$$\begin{aligned} 8\Omega : P &= I_x^2(8) \\ &= 88.89 \text{ W, Abs} \end{aligned}$$

$$\Sigma P_{\text{del}} = 373.33 \text{ W}$$



$$\Sigma P_{\text{abs}} = 373.33$$



$$I_1 = 4.29 \text{ A} \quad V_2 = 1.43 \text{ V}$$

$$I_2 = 0.29 \text{ A} \quad V_1 = 8.57 \text{ V}$$

Sources $P = VI$

$$10\text{V} : P = (10) I_1 = 42.86 \text{ W, D}$$

$$4\text{A} : P = (V_2)(4) = 5.71 \text{ W, A}$$

$$= -5.71 \text{ W, D}$$

$$\sum P_{\text{Del}} = 37.15 \text{ W}$$

Resistors $\rightarrow P = I^2 R$

$$2\Omega : P = I_1^2 (2) = 36.73 \text{ W, A}$$

$$5\Omega : P = I_2^2 (5) = 0.403 \text{ W, A}$$

$$\sum P_{\text{abs}} = 37.14 \text{ W}$$



Linearly Independent

$$2x + 3y = 6$$

$$4x + 6y = 12$$