

1. What is $\sum_{i=0}^{190} i$ $a_1 = 0 + 1$

$$\sum_{i=1}^n a_i = n \cdot \frac{a_1 + a_n}{2}$$
$$= 190 \cdot \frac{1 + 190}{2}$$
$$= \boxed{18,145}$$

2. What is the imag. part of $\frac{1}{1+j}$?

→ from calc. got $-\frac{1}{2}$

$$\frac{1}{1+j} \cdot \frac{1-j}{1-j} = \frac{1-j}{1-(-1)} = \frac{1-j}{2} = \boxed{-\frac{1}{2}}$$

↓

Complex Number Format:

→ Real + Imag. j

$$\underbrace{\frac{1}{2}}_{\text{real}} - \underbrace{\frac{1}{2}}_{\text{imag.}} j$$

3. What is the value of

$$\sum_{i=0}^{\infty} \left(\frac{1}{4}\right)^i$$

geometric series

$$r = \frac{1}{4}$$

$$\text{Eq. } \frac{1}{1 - \frac{1}{4}} = \frac{1}{.75} = \boxed{1.333}$$

4. What is the power of:

$$y = \sin(2\pi t) + \cos(8\pi t)$$

Equation $P_y = \left[\lim_{T \rightarrow \infty} \frac{1}{2T} \right] \int_{-T}^T |x(t)|^2 dt$

$\hookrightarrow b = 2\pi$
 $T = 1$

$\hookrightarrow b = 8\pi$
 $T = \frac{1}{4}$

$T = \frac{2\pi}{b}$

$$P_{y_1} = \left[\lim_{T \rightarrow \infty} \frac{1}{2} \right] \int_{-1}^1 (\sin(2\pi t))^2 dt$$

$\frac{1}{2}$

$$P_{y_1} = \frac{1}{2} \cdot 1 = \frac{1}{2}$$

$$P_{y_2} = \left[\lim_{T \rightarrow \infty} 2 \right] \int_{-\frac{1}{4}}^{\frac{1}{4}} (\cos(8\pi t))^2 dt$$

2

$$P_{y_2} = 2 \cdot \frac{1}{4} = \frac{1}{2}$$

$$P_y = P_{y_1} + P_{y_2} = \frac{1}{2} + \frac{1}{2} = \boxed{1}$$

Power = 1

5.

Question 5

10 / 10 pts

An analog accelerometer with +3V power supply is used to measure acceleration A in range $\pm 2g$. What is the voltage on the analog output pin if acceleration is $A=1g$?

Please use 3 decimal digits of precision.

$$a_0 = \frac{V_{cc}}{2}$$

$$a = a_0 + sg$$

$$s = \frac{V_{cc}}{a_{swing}} \rightarrow \# \text{ of } g's$$

$$V_{cc} = 3V$$

$$a_{swing} = \pm 2g = 4$$

$$g = 1$$

$$a_0 = \frac{3}{2} = 1.5$$

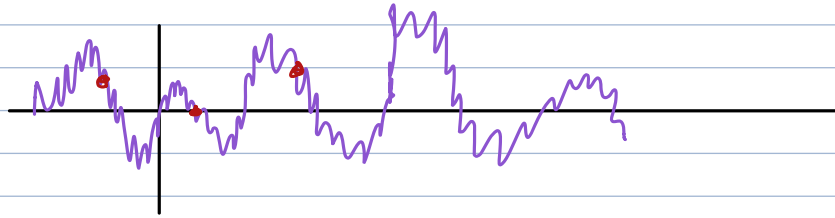
$$s = \frac{3}{4}$$

$$a = \underset{a_0}{1.5} + \underset{s}{0.75} (\underset{g}{1}) = \boxed{2.250V}$$

6. Is this periodic?

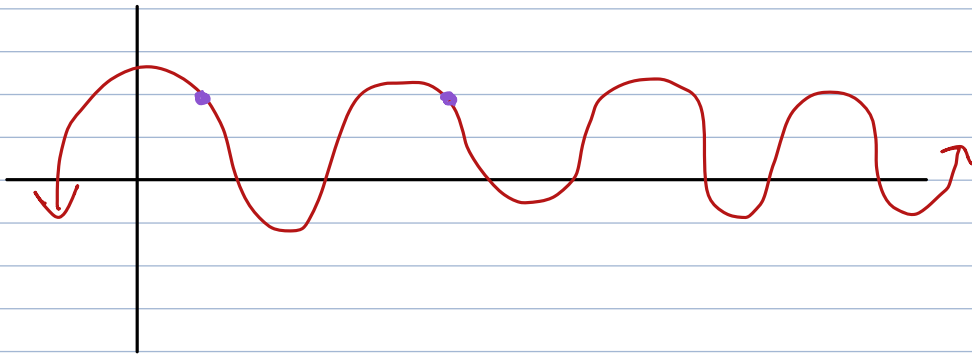
$$y = 3 \sin(6\pi t) + 4 \cos(3t)$$

False



How to be periodic

1. has to be defined from $-\infty$ to ∞
↳ no discontinuities
2. have to get to the same value after each period.

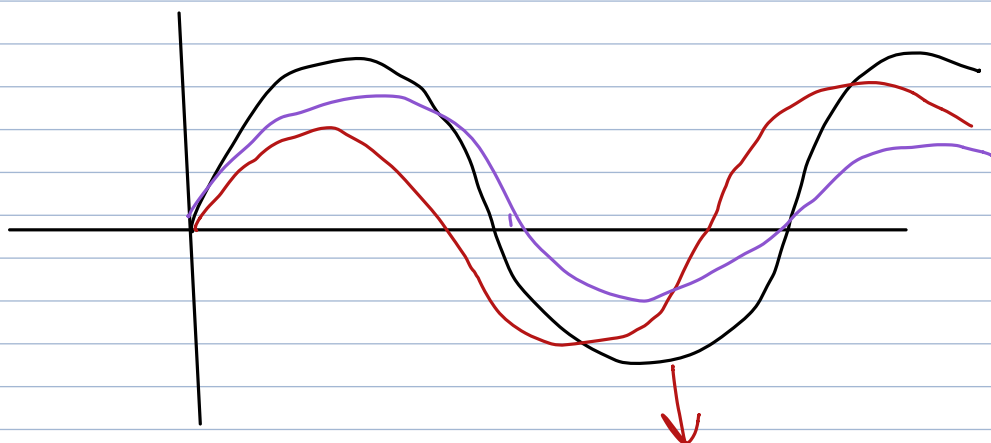


7. Is this even, odd, or neither

$$y = \sin\left(2\pi t + \frac{\pi}{4}\right)$$

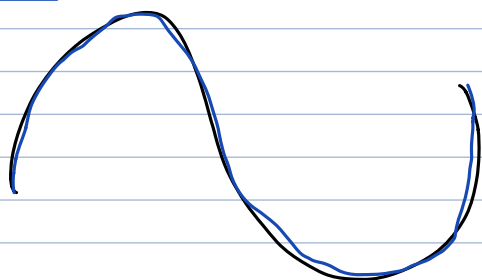
neither

even: try $\sin(-2\pi t + \frac{\pi}{4})$
odd: try: $-\sin(-2\pi t + \frac{\pi}{4})$



Wanted to match this

Ex.



$x(t)$

$x(-t)$

→ even

8. If $x(t)$ is the input, how is this modulated?

$$y = A \cdot \sin(2\pi \cdot x(t) \cdot t + \frac{\pi}{3})$$

Normal form:

Freq. Modulated

$$y = A \cdot \sin(\Omega_0 t + \theta)$$

\downarrow \downarrow \downarrow
amp. freq. phase

→ modulation depends on what
your change is attached to.
inputs

Amp. modulation Ex.

$$y = A \cdot x(t) \sin(2\pi t + \frac{\pi}{3})$$

Phase mod.

$$y = 3A \cos(3t + \frac{\pi}{4} x(t))$$

Not Mod.

$$y = A \sin(2\pi t + \frac{\pi}{3})$$

9. For inductor w/ inductance L ,
what is the complex impedance
in the Laplace domain?

Circuit
Element

Complex imp.
in Laplace

R

R

L

Ls

$\rightarrow C$

$\frac{1}{Cs}$

10. Is this right?

$$x(t) = \sin(3t)$$

$$X(s) = \mathcal{L}[x(t)] = \frac{1}{s^2 + 9}$$

Property: $\mathcal{L}[\sin(at)] = \frac{a}{s^2 + a^2}$

$$\sin(3t) \rightarrow a = 3$$

$$\text{true answer: } \frac{3}{s^2 + 9}$$

False