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The exam is composed of 5 multiple choice questions (10 points), 20 short answer questions (50 points), and 2 case problems (40 points). The exam is worth 100 points. Please use the attached answer sheet to write down all the solutions and submit only the answer sheet by April 16th at 8:00 am. Good luck!

Multiple Choice Questions (write A, B, C or D)

1	2	3	4	5
В	В	A	A	C

Short Answer Questions (feel free to enlarge the text box if necessary)

6.

Moving averages – this technique takes the averages of subsets of the data. This technique is mostly used in time series analysis and gets rid of the fluctuations in data to better understand the long-term trend.

Exponential smoothing – this technique is like moving averages except the averages are weighted. In moving averages, each average is equally weighted but in exponential smoothing exponential functions are used to influence the weight of an average over time. This makes the model slightly more responsive to recent observations.

7.

A model that has zero error on its fit to training data is likely a bad model because it is overfit to that data. The goal is to have a model that allows for generality so that it is flexible and responsive to new data. An overfit model doesn't pick up on general trends but instead is really good at understanding the training data.

8.

seq(-10,20,3)

9.

matrix(1:30, nrow = 5, byrow = FALSE)

10.

(224 + 3258) / (3595) = 0.9686

Accuracy = 96.86%

11.

df[c(10,20,30,40,50),c(1,3,5,7,9)]

12.

cor(df\$FARE, df\$DISTANCE)

Correlation coefficient: 0.67

13.

chi <- subset(df, df\$S_CITY == "Chicago IL")

chi

mean(chi\$DISTANCE)

Average distance of flights from Chicago: 891.3778

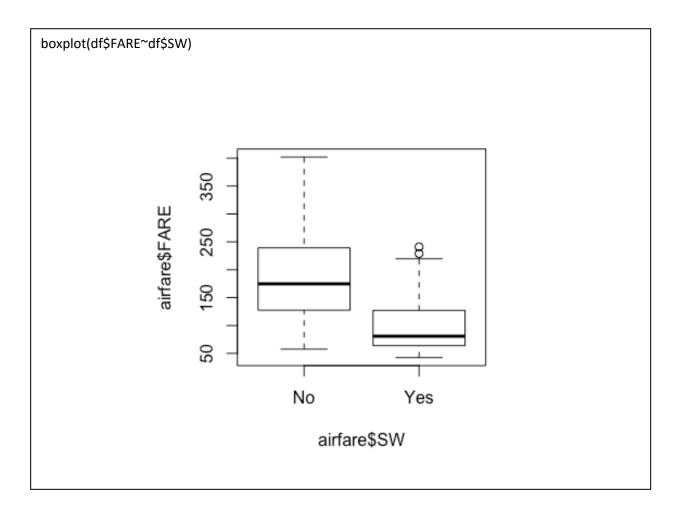
14.

```
sapply(df, class)

df.pca <- prcomp(df[,c(5,6,9:13, 16:18)], scale = TRUE)

summary(df.pca)

Yes, we should scale the data in order to obtain the best results
```



16.

```
actual <- c(15,14,18)

predicted <- c(12,15,16)

mean((actual - predicted)^2)

Output: 4.67
```

17.

```
q_17 <- data.frame(age = c(25, 53), spent = c(350, 420))

q_17

library(philentropy)

distance(q_17, method = "euclidean")

Euclidean Distance: 75.39231
```

18.

The top decile contains the 10% of the population that is the most likely respond. The first bar shows that the top 10% likely to respond have a mean response of over 2. The second bar shows that the next 10% most likely to respond have a mean response of over 1.5. These two groups, 20% of the population, are most likely to respond and will be the most profitable to go after for the new product.

19.

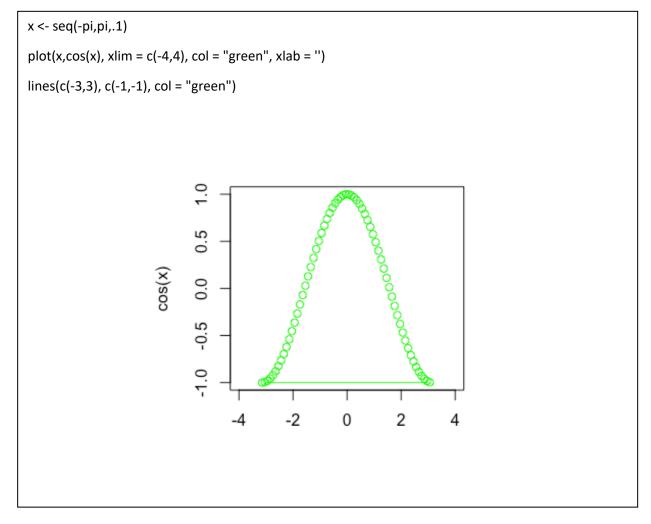
The first thing the model looks at is income. If the customer makes under 99, they are not accepted. If they make over 99, we look at education.

If their education level is under 2 and their family is less than 3 they get rejected. If their education is under 2 and their family is not less than 3 they get accepted.

If their education is 2 or more and their income is less than 117, they get rejected. If their education is 2 or more and their income is not less than 117, they get accepted.

20.

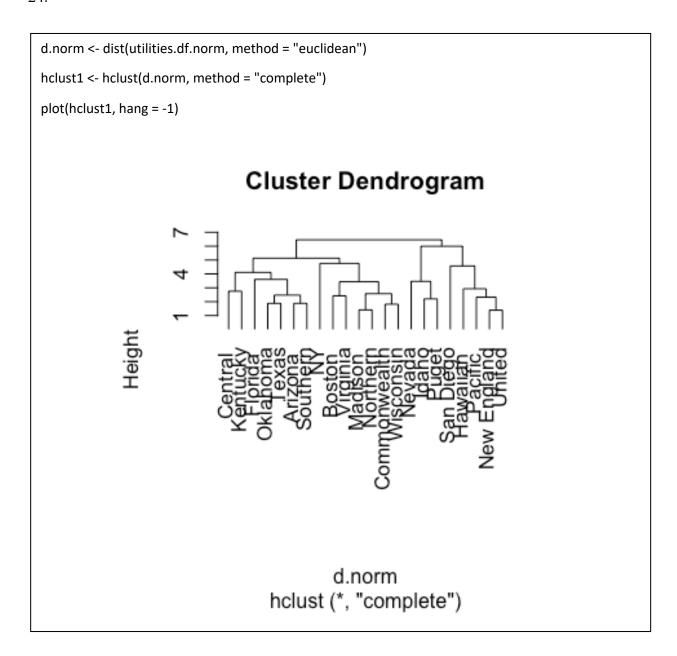
Variable	Quantitative	Qualitative
Your name		X
Your height	X	
Your income	X	
The month in which you were born		X
Your home address house number	X	
The number of texts you send each day	X	
The type of phone you have		X
Your satisfaction with your mobile service provider,	X	
measured on a scale of one to five		

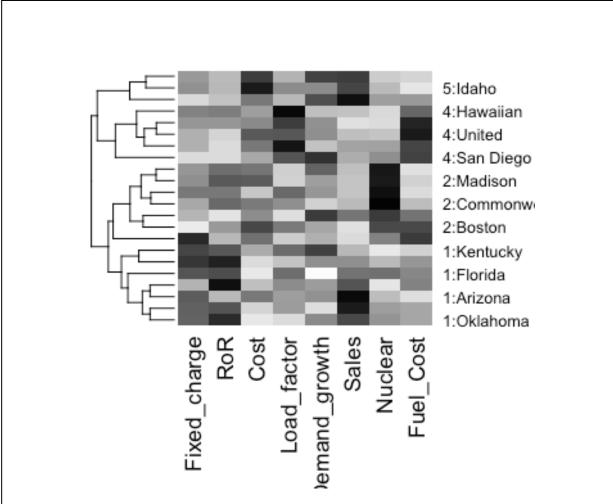


22.

```
    The logit as a function of the predictors: LOGIT = (-24.721+89.834*TotExp.+9.371*TotLns)
    The odds as a function of the predictors: ODDS = e^(-24.721+89.834*TotExp.+9.371*TotLns) = e^LOGIT
    The probability as a function of the predictors: PROB = 1 / (1+ e^(-24.721+89.834*TotExp.+9.371*TotLns)) = 1/(1+odds)
```

```
util <- read.csv("Utilities(1).csv")
row.names(util) <- util[,1]
util <- util[,-1]
utilities.df.norm <- sapply(util, scale)
row.names(utilities.df.norm) <- row.names(util)</pre>
```





Cluster 1: High sales, RoR & Fixed charge ++ low cost, nuclear, and fuel cost

Cluster 2: High nuclear & RoR ++ low sales and fuel cost

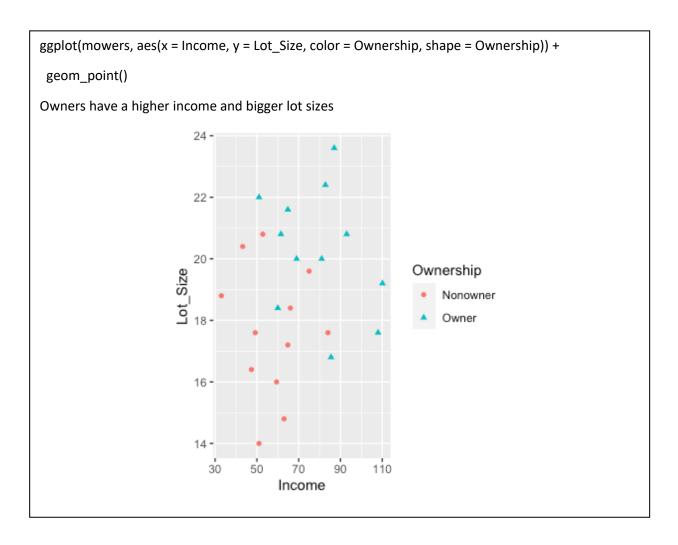
Cluster 3: High fuel cost and fixed charge ++ low RoR and sales

Cluster 4: High fuel cost and load factor ++ low nuclear and sales

Cluster 5: High sales and cost ++ low fuel cost and RoR

Case Problems

26. a



26. b

log.reg <- glm(Ownership ~., data = mowers, family = "binomial")
summary(log.reg)</pre>

The income coefficient is .1109 and this shows that it is a less impactful variable than Lot_size (coefficient = 0.9638). Therefore, lot_size is a more informative when predicting ownership.

26. c

Among nonowners, the model classified 10/12 (83.3%) correctly. The accuracy is 83.3%

26. d

To increase the percentage of correctly classified nonowners, the cutoff probability should be increased. That way higher probabilities are included in the nonowner category. Note that this will cause more improperly categorized owners though if the cutoff is too high.

26. e

Our model predicted at 0.497216567 that this person is a homeowner. That means the model would predict this person is not a homeowner at a 0.5 cutoff.

26. f

94.8 = 0.497907123

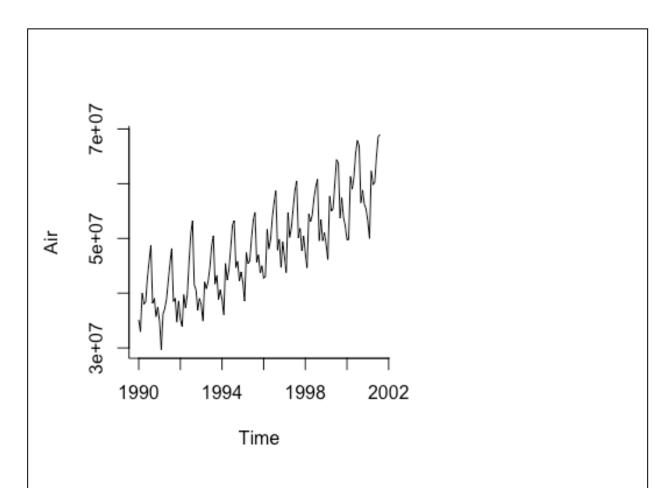
94.9 = 0.500678575

The minimum income with 16k sq ft to be classified as an owner is 94.9.

26. g

```
mowers <- read.csv("RidingMowers(1).csv")
## A
library(ggplot2)
ggplot(mowers, aes(x = Income, y = Lot_Size, color = Ownership, shape = Ownership)) +
geom_point()
## B
log.reg <- glm(Ownership ~ Income + Lot_Size, data = mowers, family = "binomial")
summary(log.reg)
#income coef 0.1109
#lot size coef 0.9638
## C
pred <- predict(log.reg, newdata = mowers, type = "response")</pre>
library(caret)
confusionMatrix(as.factor(ifelse(pred > 0.5, "Owner", "Nonowner")), mowers$Ownership)
## D
# Responded on the test
## E
library(tidyverse)
mowers1 <- mowers %>% add_row(Income = 60, Lot_Size = 20)
pred1 <- predict(log.reg, newdata = mowers1, type = "response")</pre>
pred1
## F
mowers2 <- mowers %>% add_row(Income = 94.9, Lot_Size = 16)
pred2 <- predict(log.reg, newdata = mowers2, type = "response")</pre>
pred2
```

27. a



We can see a general upward trend from 1990 to 2001. While there are some seasonal and predictable cyclic trends, overall the trend is upward. It would take a major event, like 9-11, to cause this upward trend to be distrupted.

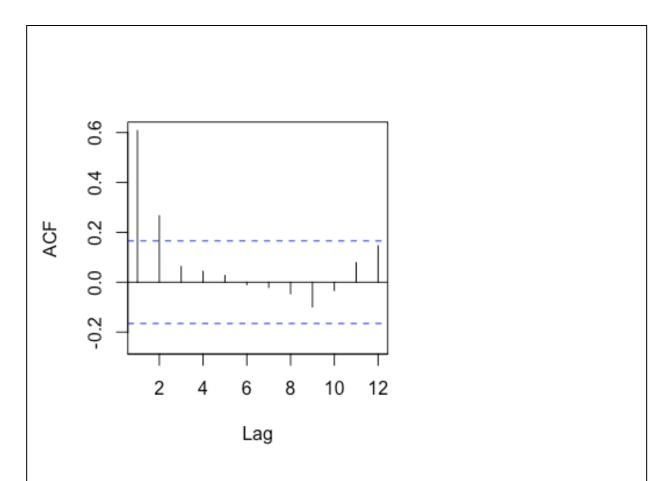
27. b

```
Call:
tslm(formula = air_train ~ trend + season, lambda = 0)
Residuals:
   Min
          1Q Median
                         3Q
                               Max
-0.101591 -0.017260 -0.002175  0.017248  0.083200
Coefficients:
       Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.732e+01 1.011e-02 1713.044 < 2e-16 ***
trend
        3.604e-03 6.595e-05 54.640 < 2e-16 ***
season2 -6.519e-02 1.286e-02 -5.069 1.38e-06 ***
season3 1.338e-01 1.286e-02 10.407 < 2e-16 ***
season4 8.473e-02 1.286e-02 6.588 1.07e-09 ***
         1.105e-01 1.286e-02 8.595 2.61e-14 ***
season5
         1.884e-01 1.286e-02 14.642 < 2e-16 ***
season6
         2.501e-01 1.287e-02 19.439 < 2e-16 ***
season7
         2.731e-01 1.287e-02 21.221 < 2e-16 ***
season8
         7.314e-02 1.315e-02 5.562 1.50e-07 ***
season9
season10 1.029e-01 1.315e-02 7.823 1.74e-12 ***
season11 1.361e-02 1.315e-02 1.035 0.302718
season12 5.188e-02 1.315e-02 3.944 0.000132 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.0315 on 127 degrees of freedom
Multiple R-squared: 1, Adjusted R-squared: 1
F-statistic: 8.792e+17 on 12 and 127 DF, p-value: < 2.2e-16
```

27. c

February and August are both statistically significant at a high level – ie *** or a < 0.001 level. With a low p-value, we can reject the null hypothesis.

27. d



There isn't really a pattern (perhaps something cubic) but no consistent upward or downward pattern would suggest that there is no significant autocorrelation. Additionally, there values are relatively low (mostly under +/-0.4 so we can assume low serial correlation.

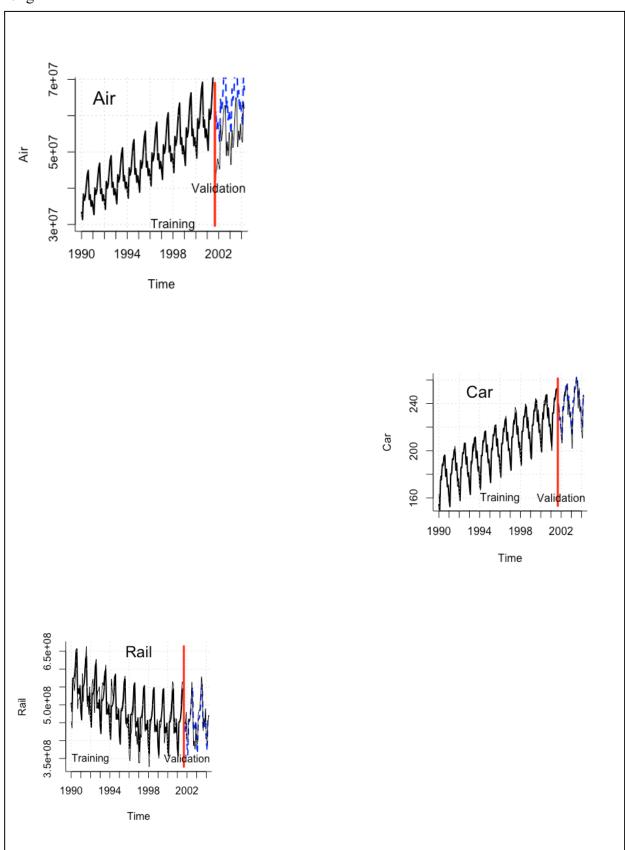
27. e

```
Call:
tslm(formula = rail_train ~ poly(trend, 2, raw = TRUE) + season)
Residuals:
   Min
          1Q Median 3Q Max
-83002973 -17124784 2921271 18582765 74299534
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                 506417584 10859233 46.635 < 2e-16 ***
(Intercept)
poly(trend, 2, raw = TRUE)1 -2025825 246700 -8.212 2.22e-13 ***
poly(trend, 2, raw = TRUE)2 8010 1695 4.725 6.04e-06 ***
season2
                 -21471834 11913374 -1.802 0.073884 .
                  73933460 11913852 6.206 7.23e-09 ***
season3
                  73730823 11914641 6.188 7.87e-09 ***
season4
                  84066907 11915737 7.055 1.02e-10 ***
season5
                 108355984 11917142 9.092 1.75e-15 ***
season6
                 158005456 11918857 13.257 < 2e-16 ***
season7
                 165851861 11920888 13.913 < 2e-16 ***
season8
                  42825983 12191216 3.513 0.000616 ***
season9
                 58146152 12192117 4.769 5.02e-06 ***
season10
                 44863290 12193188 3.679 0.000345 ***
season11
                  70687301 12194431 5.797 5.12e-08 ***
season12
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 29180000 on 126 degrees of freedom
Multiple R-squared: 0.8442, Adjusted R-squared: 0.8281
F-statistic: 52.5 on 13 and 126 DF, p-value: < 2.2e-16
```

27. f

```
Call:
tslm(formula = car_train ~ trend + season)
Residuals:
  Min 1Q Median 3Q Max
-6.2254 -1.5725 -0.1145 1.0383 8.9699
Coefficients:
      Estimate Std. Error t value Pr(>|t|)
trend
        0.429216  0.005265  81.516  < 2e-16 ***
season2 -7.348382 1.026645 -7.158 5.83e-11 ***
season3
         20.207402 1.026685 19.682 < 2e-16 ***
         19.749020 1.026753 19.234 < 2e-16 ***
season4
         31.898138 1.026847 31.064 < 2e-16 ***
season5
         30.924755 1.026969 30.113 < 2e-16 ***
season6
         38.353873 1.027117 37.341 < 2e-16 ***
season7
         38.717158 1.027293 37.689 < 2e-16 ***
season8
         20.587781 1.049757 19.612 < 2e-16 ***
season9
season10 26.104020 1.049823 24.865 < 2e-16 ***
season11 10.688441 1.049916 10.180 < 2e-16 ***
season12 11.857407 1.050035 11.292 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 2.515 on 127 degrees of freedom
Multiple R-squared: 0.989, Adjusted R-squared: 0.9879
F-statistic: 948.4 on 12 and 127 DF, p-value: < 2.2e-16
```





27. h

9-11 dramatically effected air travel usage. You can see in the graphic that the numbers after 9-11 are dramatically lower than predicted. Car and rail usage went relatively unchanged though. You can barely even see the blue predicted line of car and rail because the actual numbers go right over the predicted. Air was definitely very effected though.

27. i

Air

```
df <- read.csv("Sept11Travel.csv")</pre>
names(df)[names(df) == "Air.RPM..000s."] <- "Air"
names(df)[names(df) == "Rail.PM"] <- "Rail"
names(df)[names(df) == "VMT..billions."] <- "Vehicle"
## A
library(forecast)
air.ts <- ts(df$Air,start = c(1990,1),end = c(2004,4),freq=12)
rail.ts <- ts(df\$Rail,start = c(1990,1),end = c(2004,4),freq=12)
vehicle.ts <- ts(df$Vehicle,start = c(1990,1),end = c(2004,4),freq=12)
nValid <- 32
air_train <- window(air.ts, start = c(1990,1), end = c(2001,8))
air_valid \leftarrow window(air.ts, start = c(2001,9), end = c(2004,4))
plot(air_train,xlab="Time",ylab="Air",ylim=c(min(df$Air), max(df$Air)),bty="l")
## B
train.lm.season <- tslm(air_train ~ trend + season, lambda = 0)
train.lm.season.pred <- forecast(train.lm.season, h=nValid, level=0)
print(summary(train.lm.season))
## C Done
## D
Acf(train.lm.season$residuals,lag.max=12, main="")
## E
rail\_train \leftarrow window(rail.ts, start = c(1990,1), end = c(2001,8))
rail\_valid \leftarrow window(rail.ts, start = c(2001,9), end = c(2004,4))
train.lm.quad <- tslm(rail_train ~ poly(trend, 2, raw=TRUE) + season)
train.lm.quad.pred <- forecast(train.lm.quad, h=nValid, level=0)
print(summary(train.lm.quad))
## F
car_train \leftarrow window(vehicle.ts, start = c(1990,1), end = c(2001,8))
car_valid \leftarrow window(vehicle.ts, start = c(2001,9), end = c(2004,4))
train.linear.season <- tslm(car_train ~ trend + season)
train.linear.pred <- forecast(train.linear.season, h=nValid, level=0)
print(summary(train.linear.season))
## G
```

If part g is unreadable, here is the code:

df <- read.csv("Sept11Travel.csv")</pre> names(df)[names(df) == "Air.RPM..000s."] <- "Air" names(df)[names(df) == "Rail.PM"] <- "Rail" names(df)[names(df) == "VMT..billions."] <- "Vehicle"</pre> ## A library(forecast) air.ts <- ts(df\$Air,start = c(1990,1),end = c(2004,4),freq=12) rail.ts <- ts(df\Rail,start = c(1990,1),end = c(2004,4),freq=12) vehicle.ts <- ts(df\$Vehicle,start = c(1990,1),end = c(2004,4),freq=12) nValid <- 32air train <- window(air.ts, start = c(1990,1), end = c(2001,8)) air valid <- window(air.ts, start = c(2001,9), end = c(2004,4)) plot(air train,xlab="Time",ylab="Air",ylim=c(min(df\$Air), max(df\$Air)),bty="l") ## B train.lm.season \leftarrow tslm(air train \sim trend + season, lambda = 0) train.lm.season.pred <- forecast(train.lm.season, h=nValid, level=0) print(summary(train.lm.season)) ## C Done ## **D** Acf(train.lm.season\$residuals,lag.max=12, main="") ## E rail train \leftarrow window(rail.ts, start = c(1990,1), end = c(2001,8)) rail valid \leftarrow window(rail.ts, start = c(2001,9), end = c(2004,4))

```
train.lm.quad <- tslm(rail train ~ poly(trend, 2, raw=TRUE) + season)
train.lm.quad.pred <- forecast(train.lm.quad, h=nValid, level=0)
print(summary(train.lm.quad))
## F
car train \leftarrow window(vehicle.ts, start = c(1990,1), end = c(2001,8))
car valid \leftarrow window(vehicle.ts, start = c(2001,9), end = c(2004,4))
train.linear.season <- tslm(car train ~ trend + season)
train.linear.pred <- forecast(train.linear.season, h=nValid, level=0)
print(summary(train.linear.season))
## G
# Air
plot(train.lm.season.pred, ylab = "Air", ,bty='l',xlab = "Time",xaxt="n",
ylim=c(min(df$Air), max(df$Air)), xlim = c(1990,2004), main = "", flty = 2)
axis(1, at = seq(1990, 2004, 1))
lines(train.lm.season\$fitted, lwd = 2)
lines(air valid)
grid()
lines(c(2001.67, 2001.67), c(min(df$Air), max(df$Air)),lwd=3,col="red")
text(1998, 30000000, "Training",cex=1)
text(2002, 40000000, "Validation",cex=1)
text(1992, 65000000, "Air", cex=1.5)
# Rail
plot(train.lm.quad.pred, vlab = "Rail", .btv='l'.xlab = "Time",xaxt="n",
ylim=c(min(df\$Rail), max(df\$Rail)), xlim=c(1990,2004), main="", flty=2)
axis(1, at = seq(1990, 2004, 1))
lines(train.lm.quad\$fitted, lwd = 2)
lines(rail valid)
grid()
lines(c(2001.67, 2001.67), c(min(df$Rail), max(df$Rail)),lwd=3,col="red")
text(1992, 350000000, "Training", cex=1)
```

```
text(2002, 350000000, "Validation",cex=1)

text(1997, 650000000, "Rail", cex=1.5)

# Car

plot(train.linear.pred, ylab = "Car", ,bty='l',xlab = "Time",xaxt="n",
    ylim=c(min(df$Vehicle), max(df$Vehicle)),xlim = c(1990,2004), main = "", flty = 2)

axis(1, at = seq(1990, 2004, 1))

lines(train.linear.season$fitted, lwd = 2)

lines(car_valid)

grid()

lines(c(2001.67, 2001.67), c(min(df$Vehicle), max(df$Vehicle)),lwd=3,col="red")

text(1996, 160, "Training",cex=1)

text(2002, 160, "Validation",cex=1)

text(1994, 250, "Car", cex=1.5)
```