

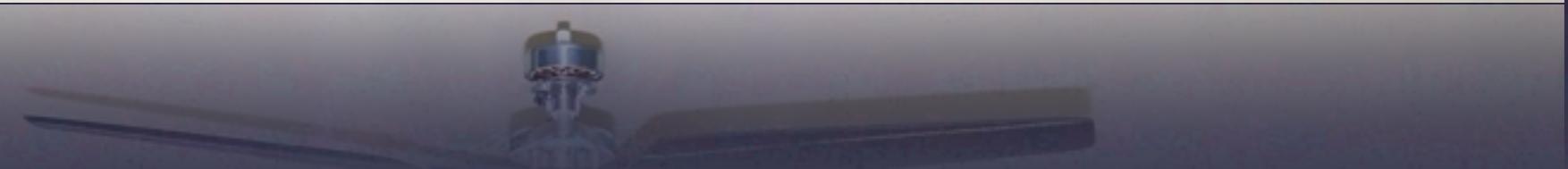
The Power of Isolation



Silviu S. Craciunas and Christoph M. Kirsch
Department of Computer Sciences
University of Salzburg



Safety-critical Real-time Systems





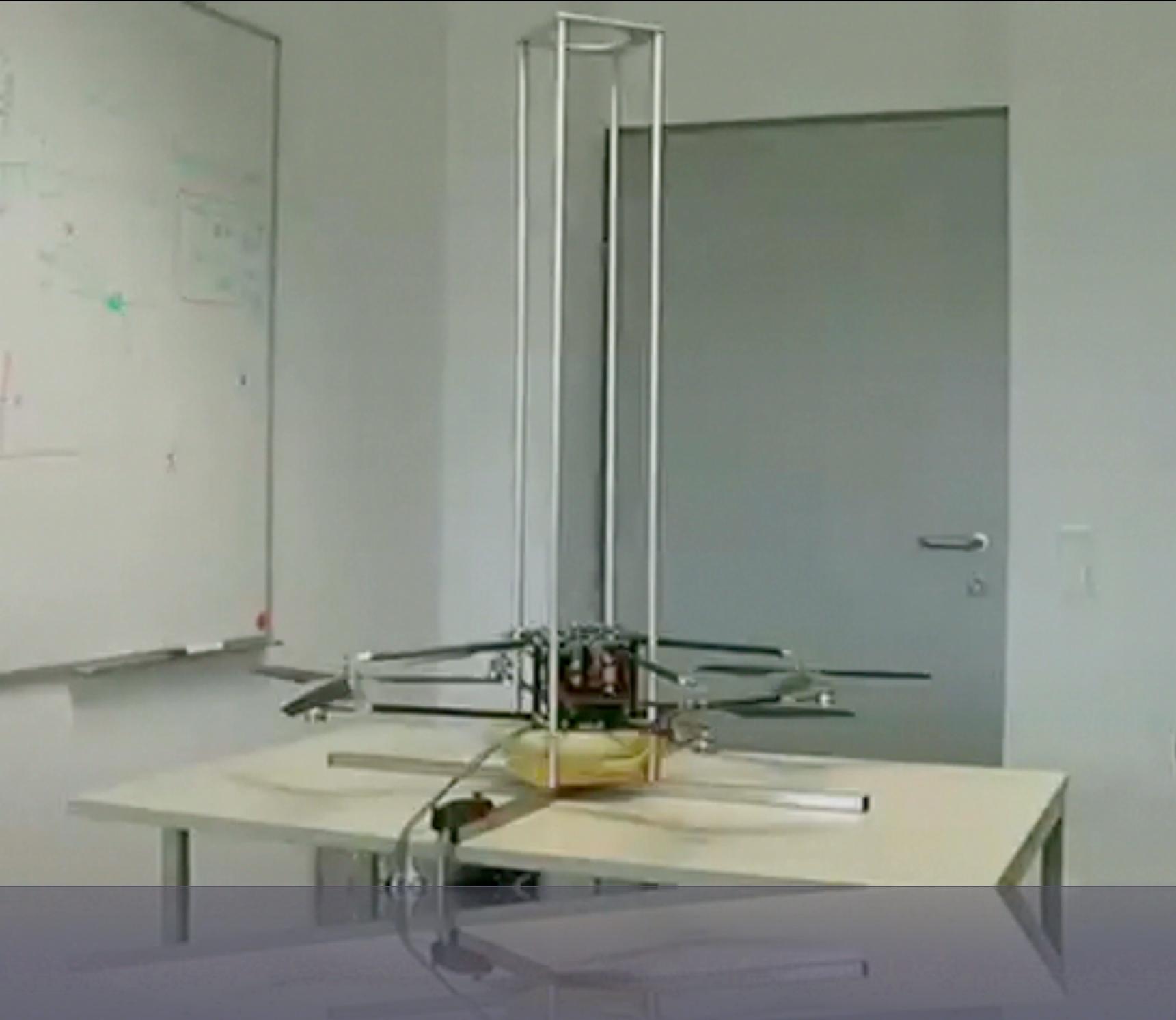
Safety-critical Real-time Systems



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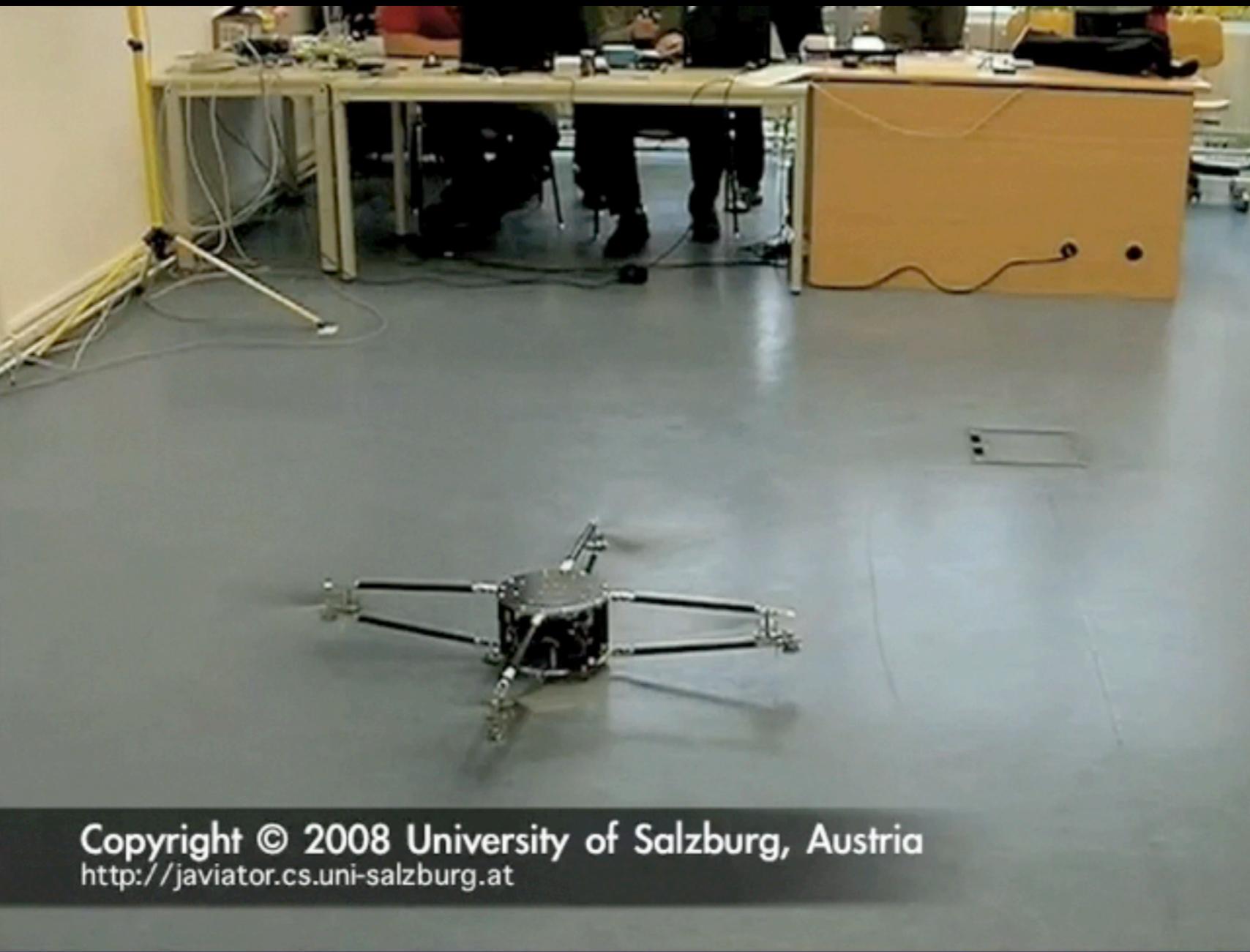


When things go wrong





When things go right...



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Isolation



Isolation

Important aspects for isolation: **time** **space**



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Temporal isolation through CBS [Abeni04], VBS [Craciunas12]



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Spatial isolation through memory management/hardware



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Power isolation?



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Spatial isolation through memory management/hardware

Power isolation?

Is power consumption compositional?



Isolation

Important aspects for isolation: **time** **space**

Temporal isolation through CBS [Abeni04], VBS [Craciunas12]

Spatial isolation through memory management/hardware

Power isolation?

Is power consumption compositional?

Problem: non-linear relationship of power consumption
and processor frequency



Power-aware Real-time Systems



Power-aware Real-time Systems

Adapt system performance to system load



Power-aware Real-time Systems

Adapt system performance to system load

Dynamic Voltage and Frequency Scaling [Pillai01]



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$$p(f) = c_0 + c_1 f^\alpha \quad [\text{Mosse05}]$$



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- Scaling the frequency results in modified execution time
- Deadlines remain the same
- Minimize power while maintaining the real-time properties



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$$f > U f_{max} \text{ [Pillai01]}$$



Approaches



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Measuring the power consumption [Pathak et al.]



Approaches

Measuring the power consumption [Pathak11]

Controlling the power consumption [Cao08]



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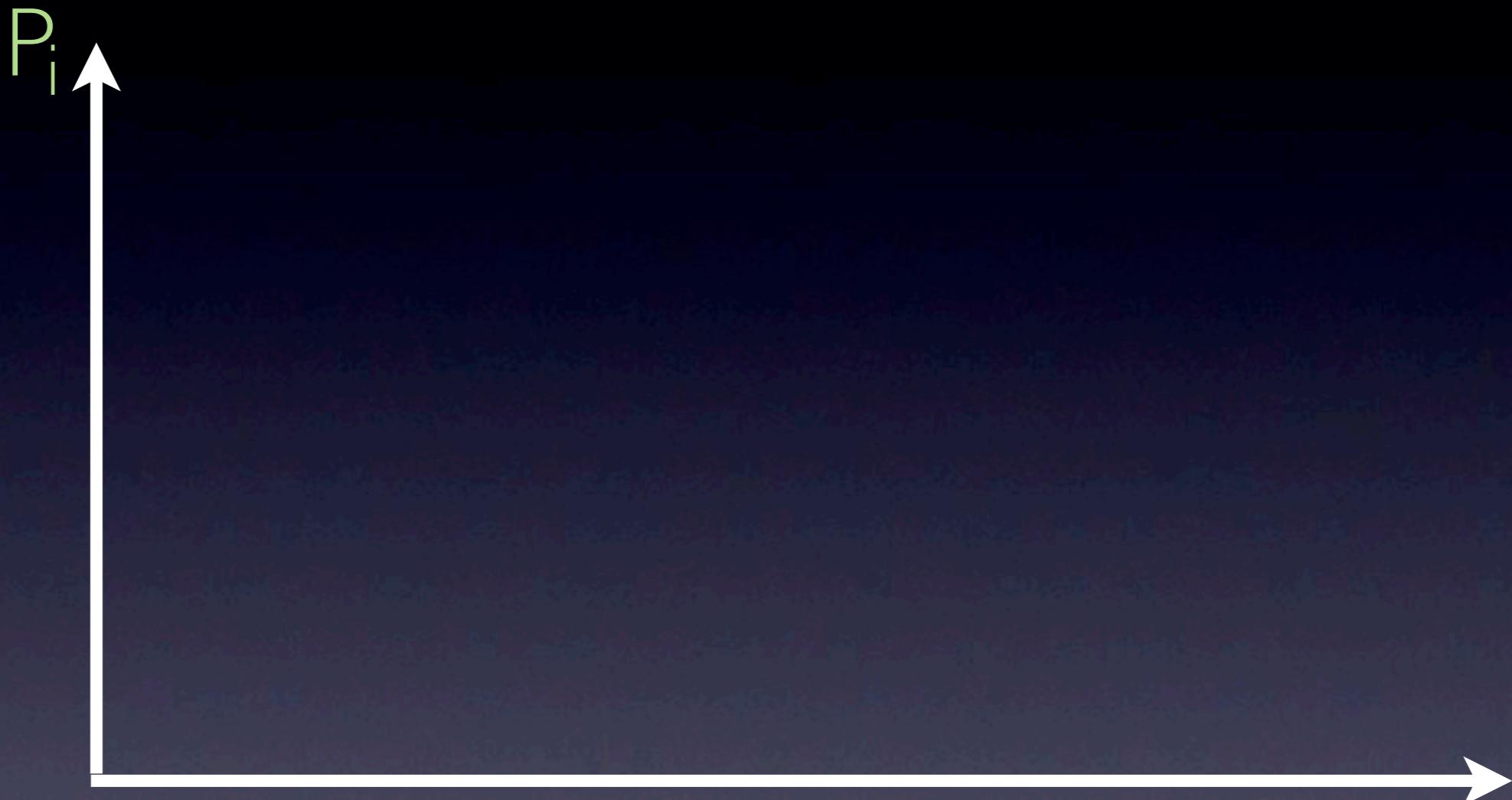
Controlling is fine, but we do not want to
interfere in the schedule



Our approach

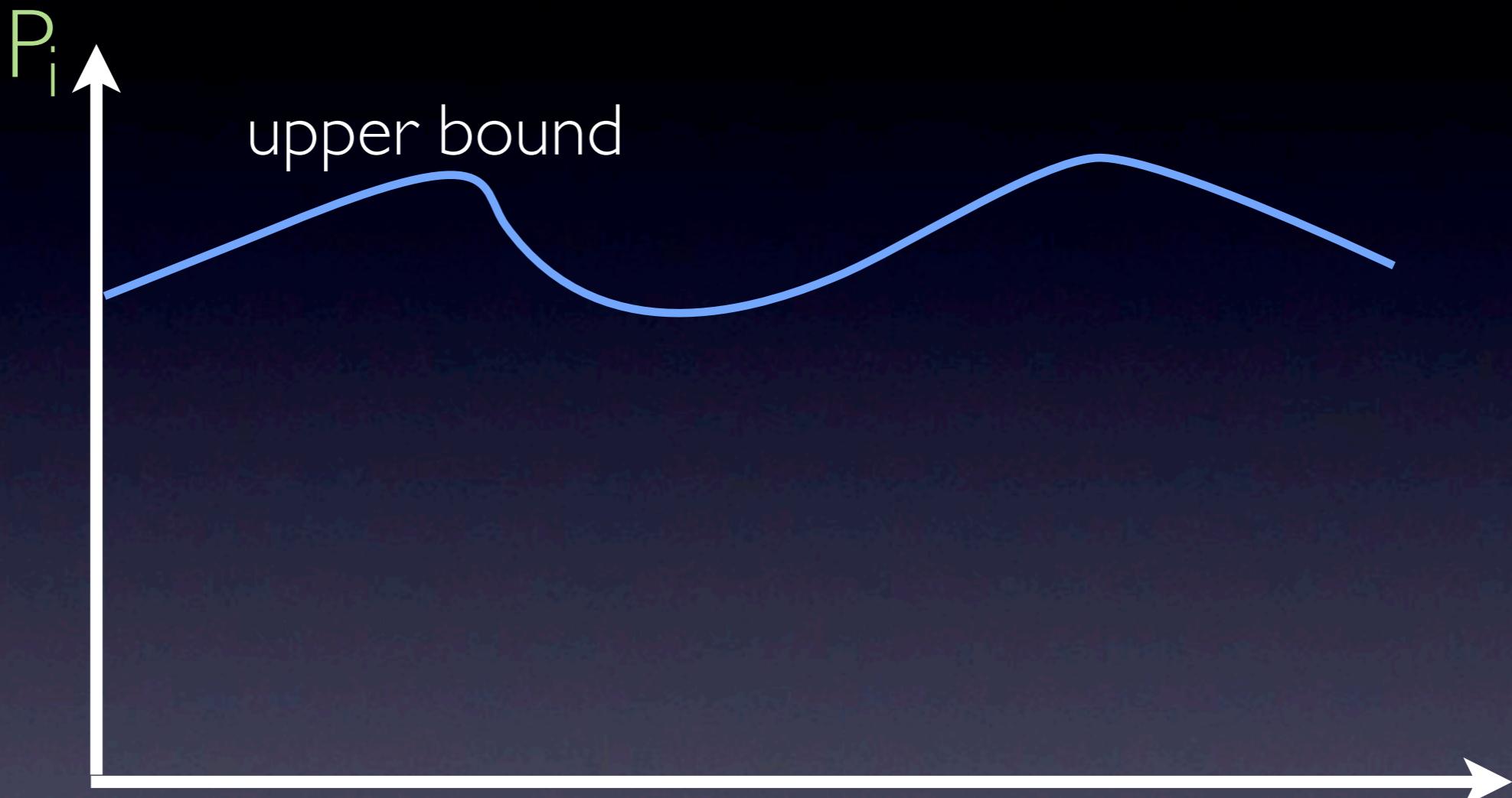


Our approach



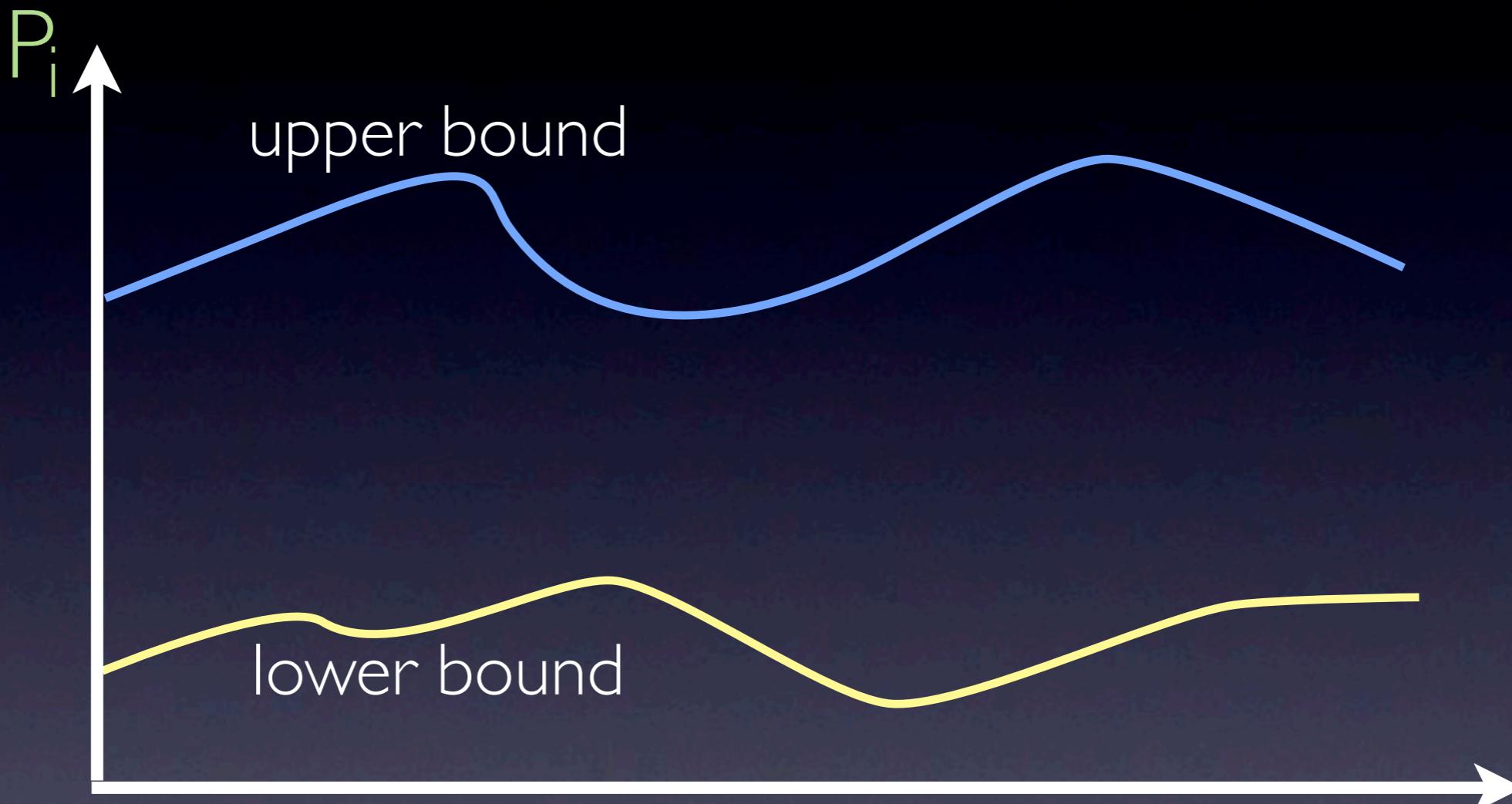


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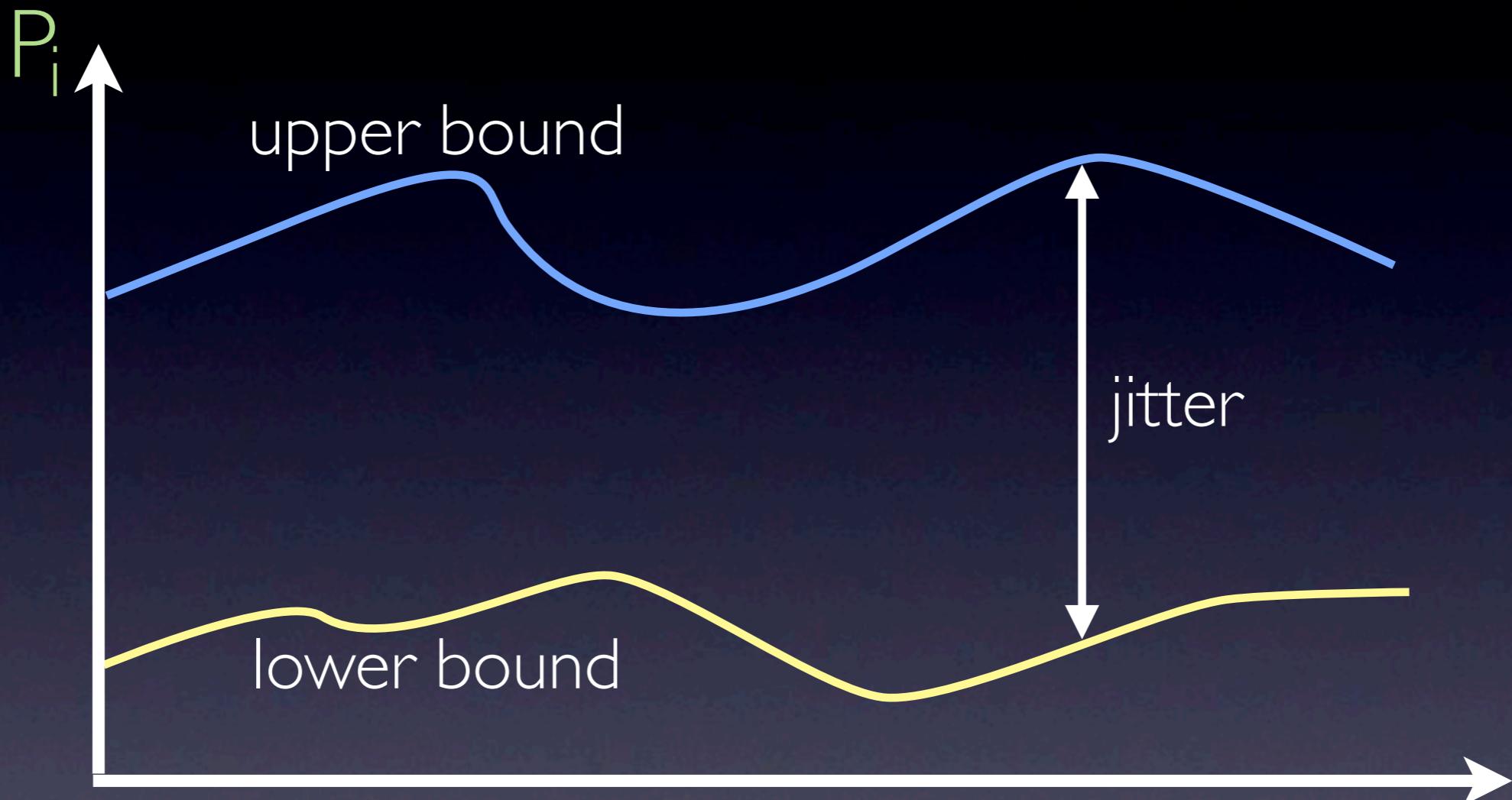


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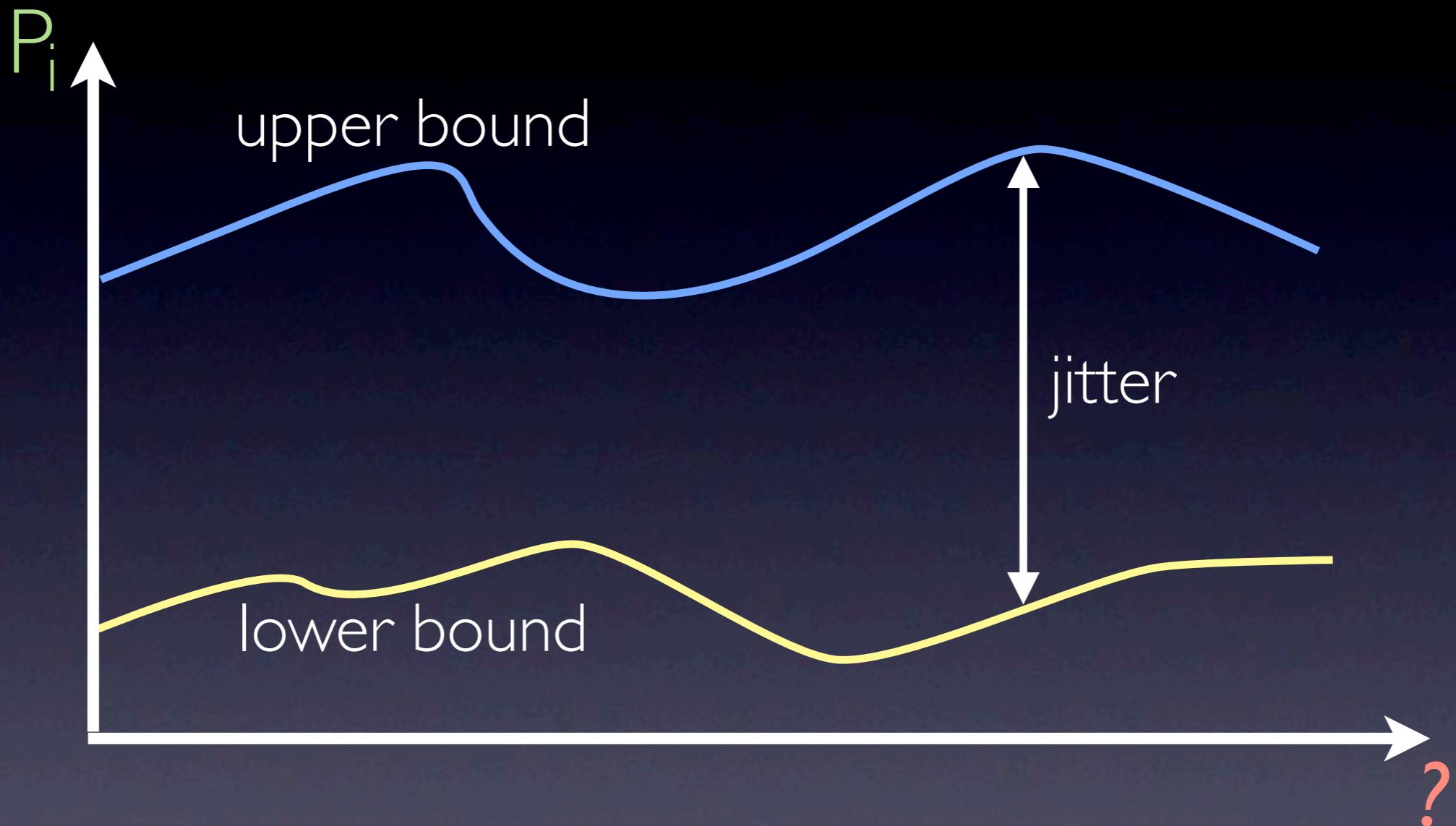


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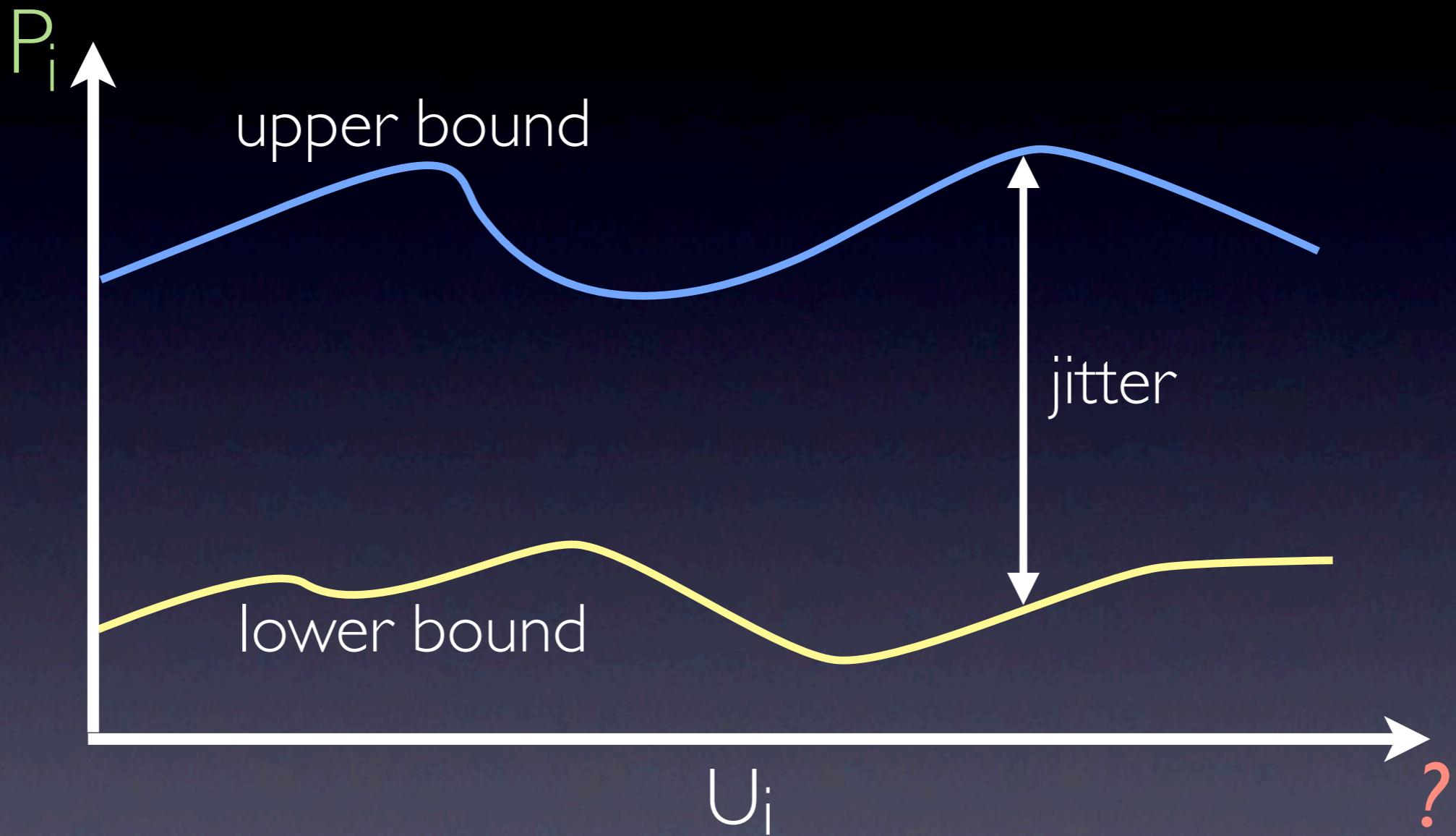


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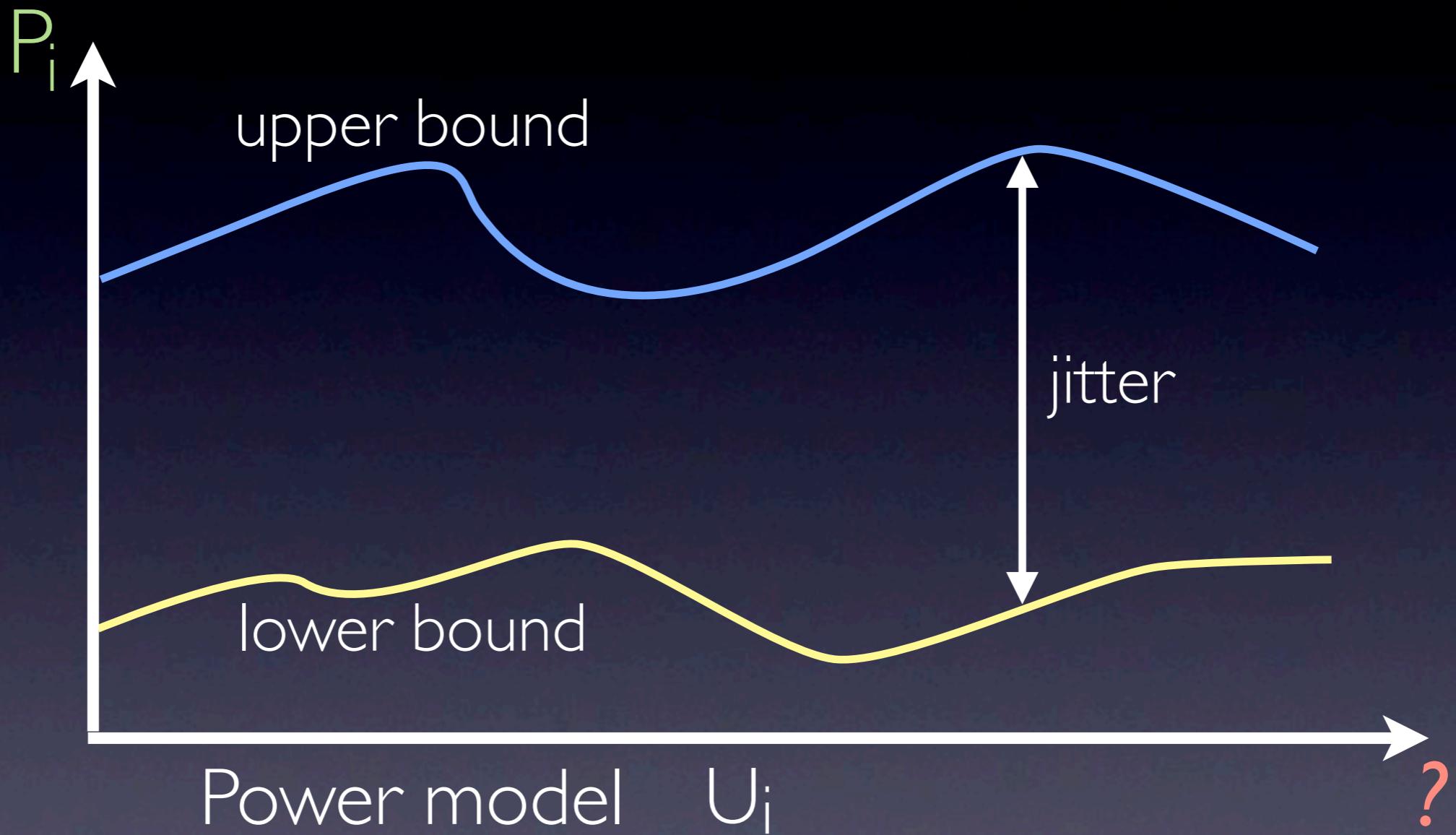


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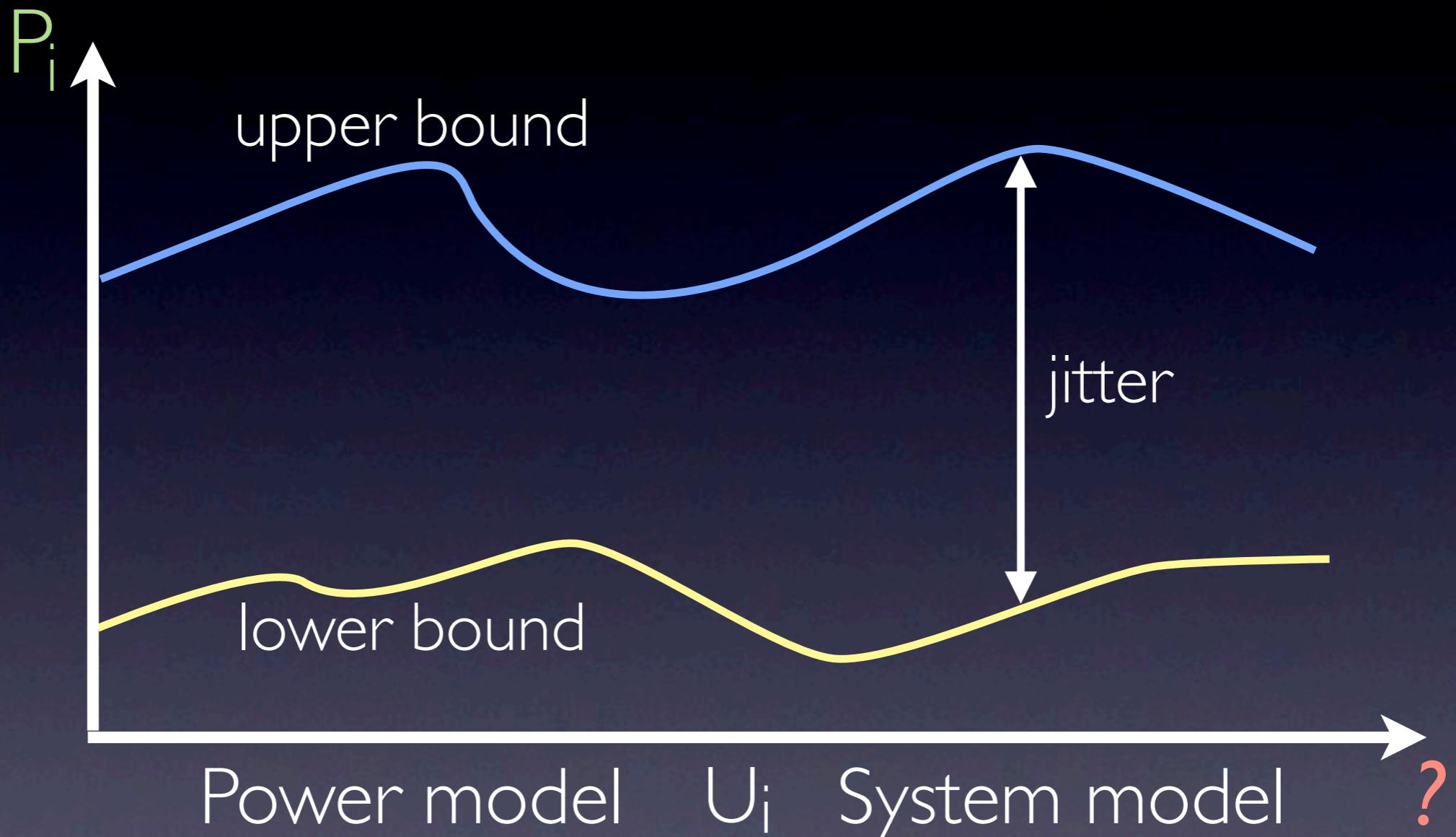


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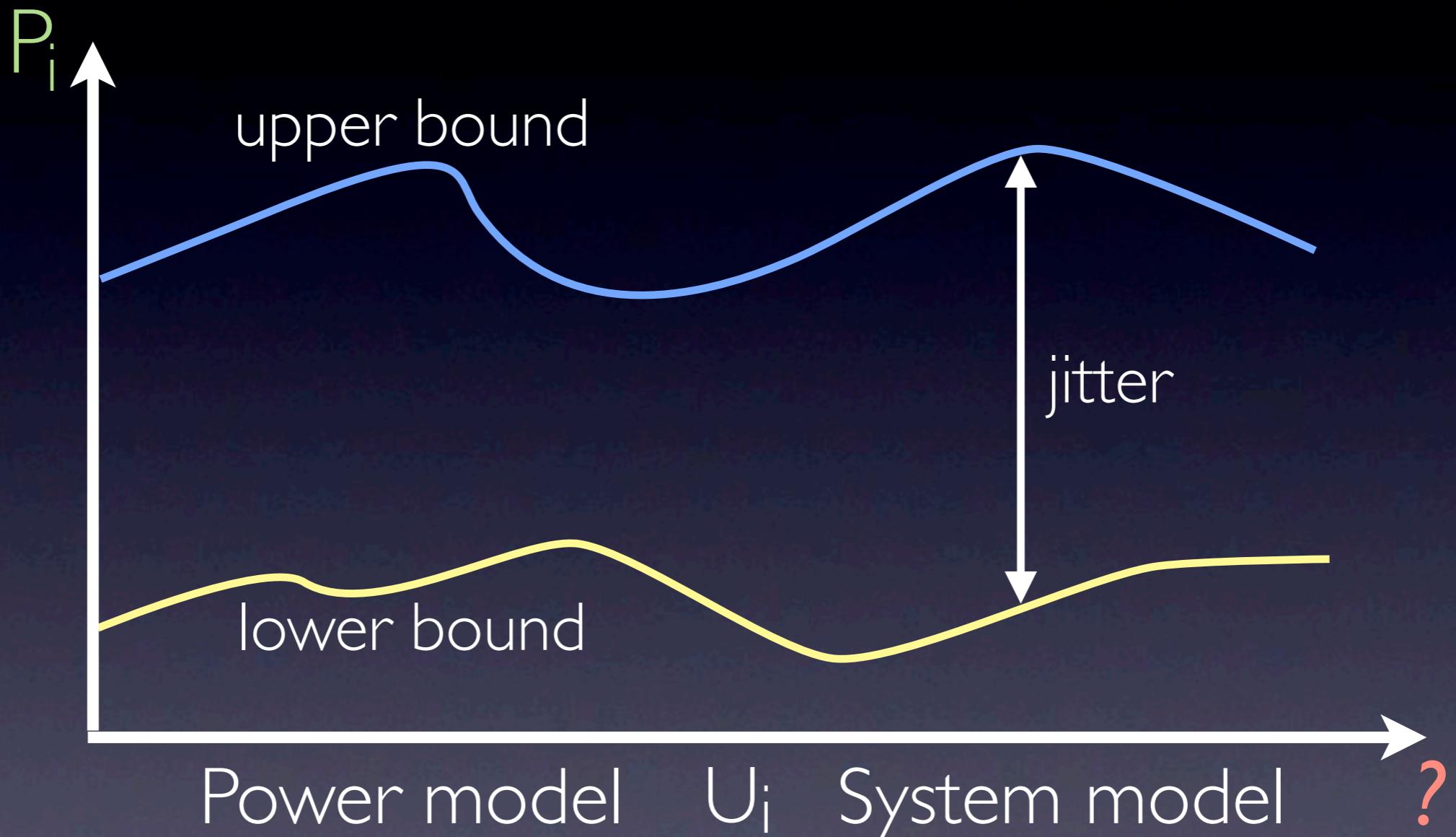


Our approach





Our approach



Lower and upper bounds on the power consumption of a task as functions of task utilization, frequency scaling, and power model.



Our approach



Our approach

Study the compositionality of power consumption (power isolation)



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Isolate power consumption through over-provisioning



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Relationship between the power consumption and the contribution of a single task to this power consumption + the trade-off between quality and cost of power isolation.



Our approach

Study the compositionality of power consumption (power isolation)

Isolate power consumption through over-provisioning

Relationship between the power consumption and the contribution of a single task to this power consumption + the trade-off between quality and cost of power isolation.

We discuss the variance between lower and upper bounds (quality) and the power consumption overhead (cost) of power isolation.



First, the math...



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CPU energy consumption of a EDF system with utilization $U = \sum_{i=1}^n U_i$
running at frequency κf_{max} , $U \leq \kappa \leq 1$
in the interval $[t_0, t_1]$)



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$$t_{idle}c_0 + t_{running}(c_0 + c_1(\kappa f_{max})^\omega)$$



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Two frequency levels



Two frequency levels





Two frequency levels



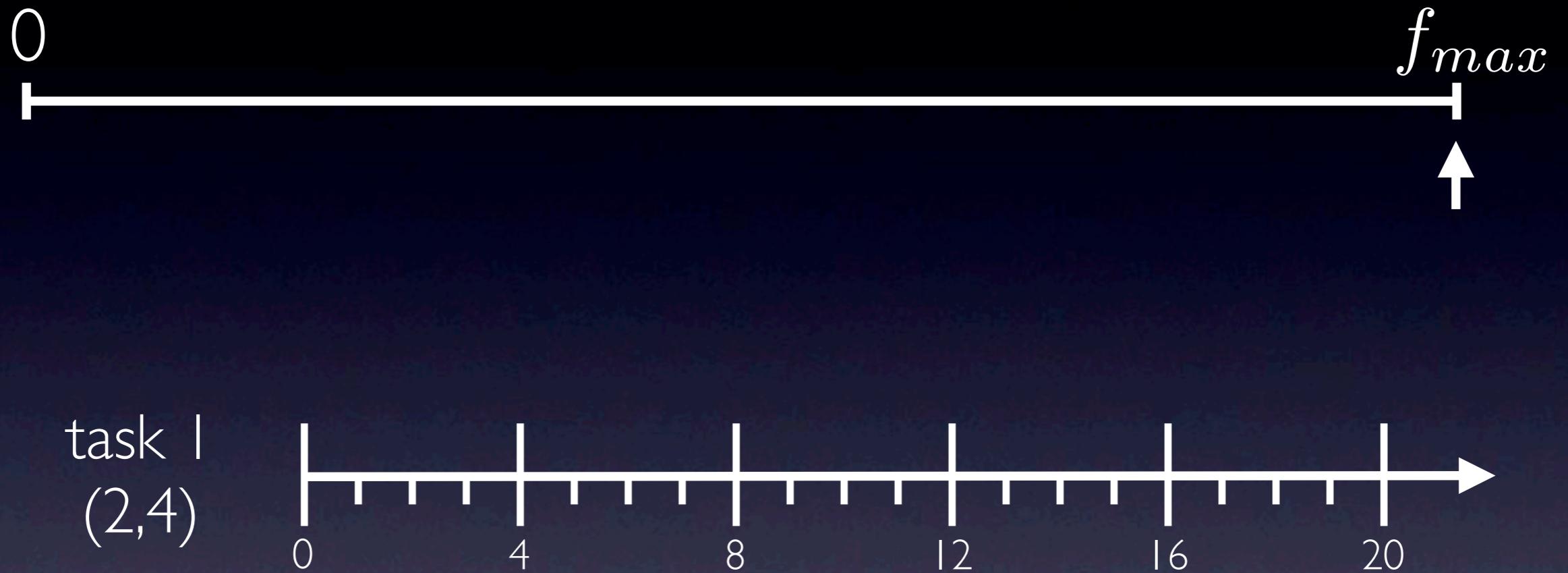


Two frequency levels



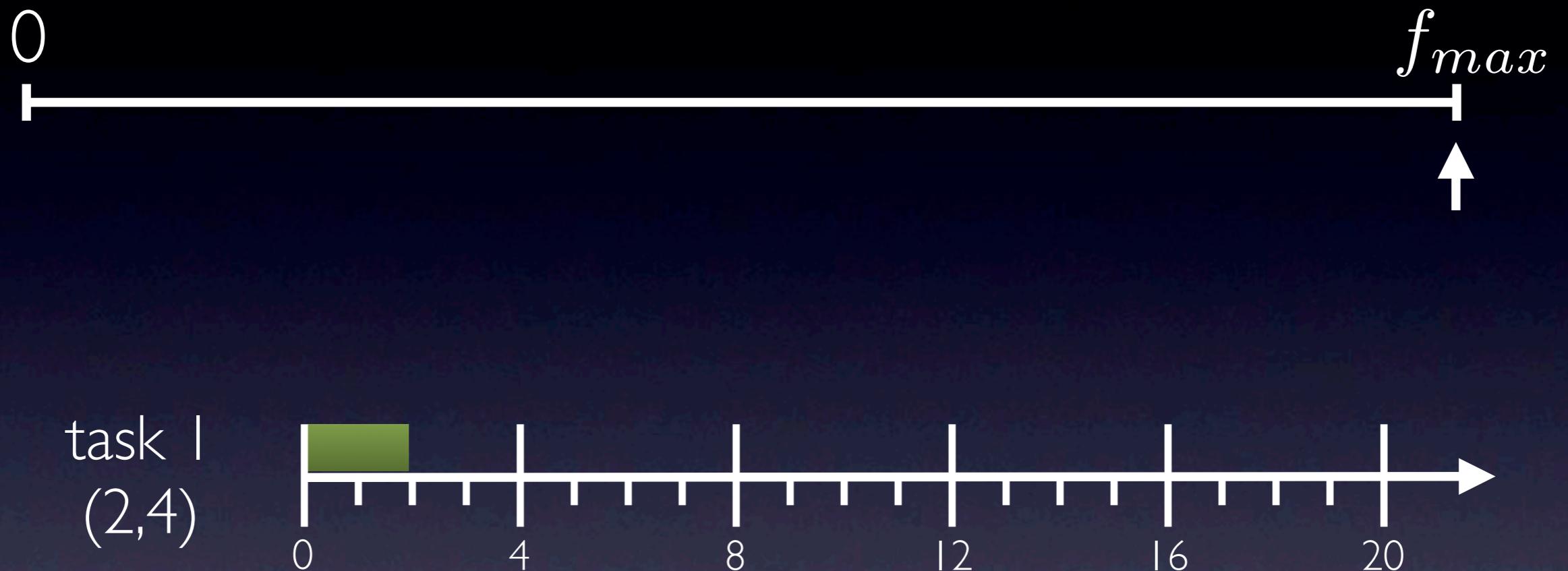


Two frequency levels



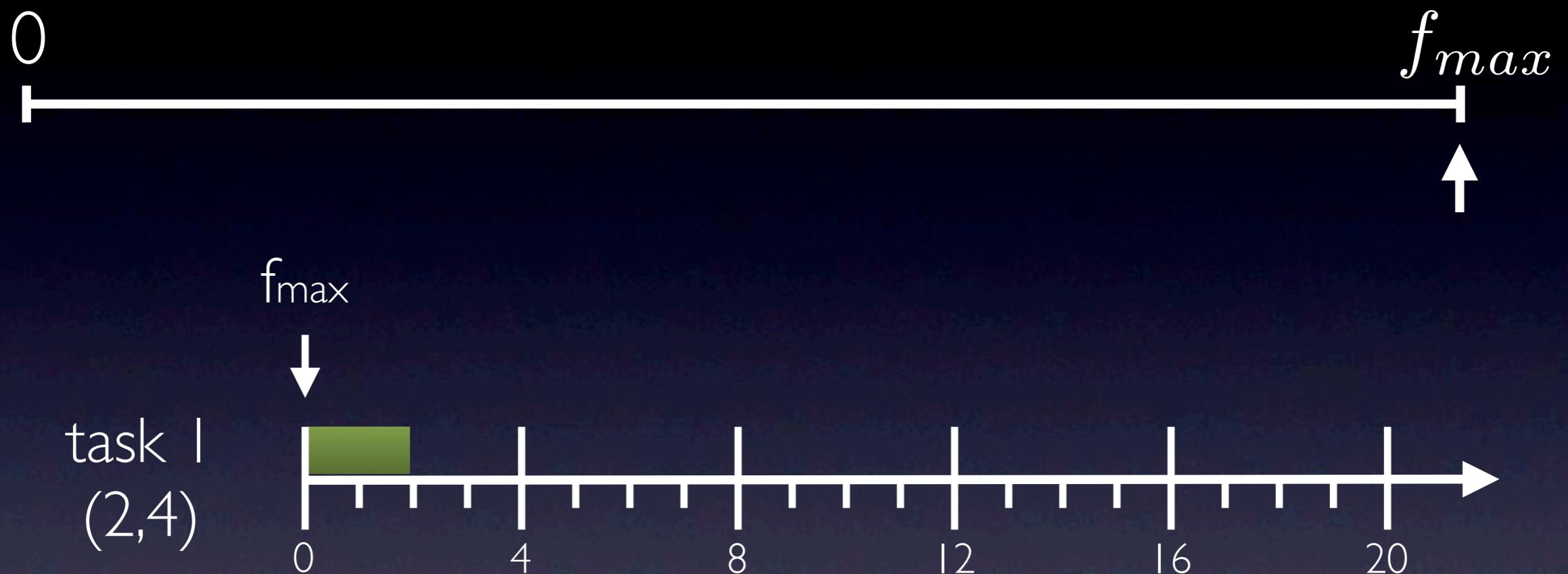


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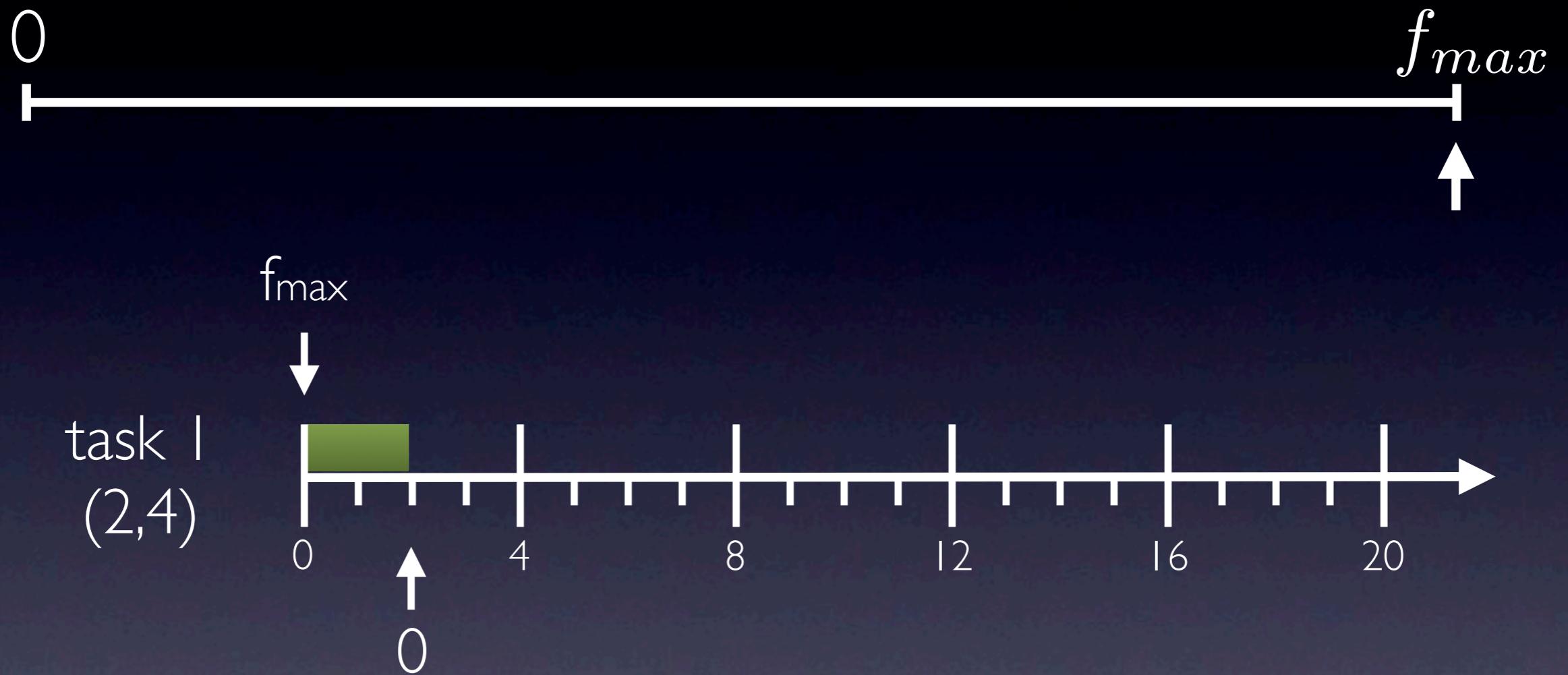


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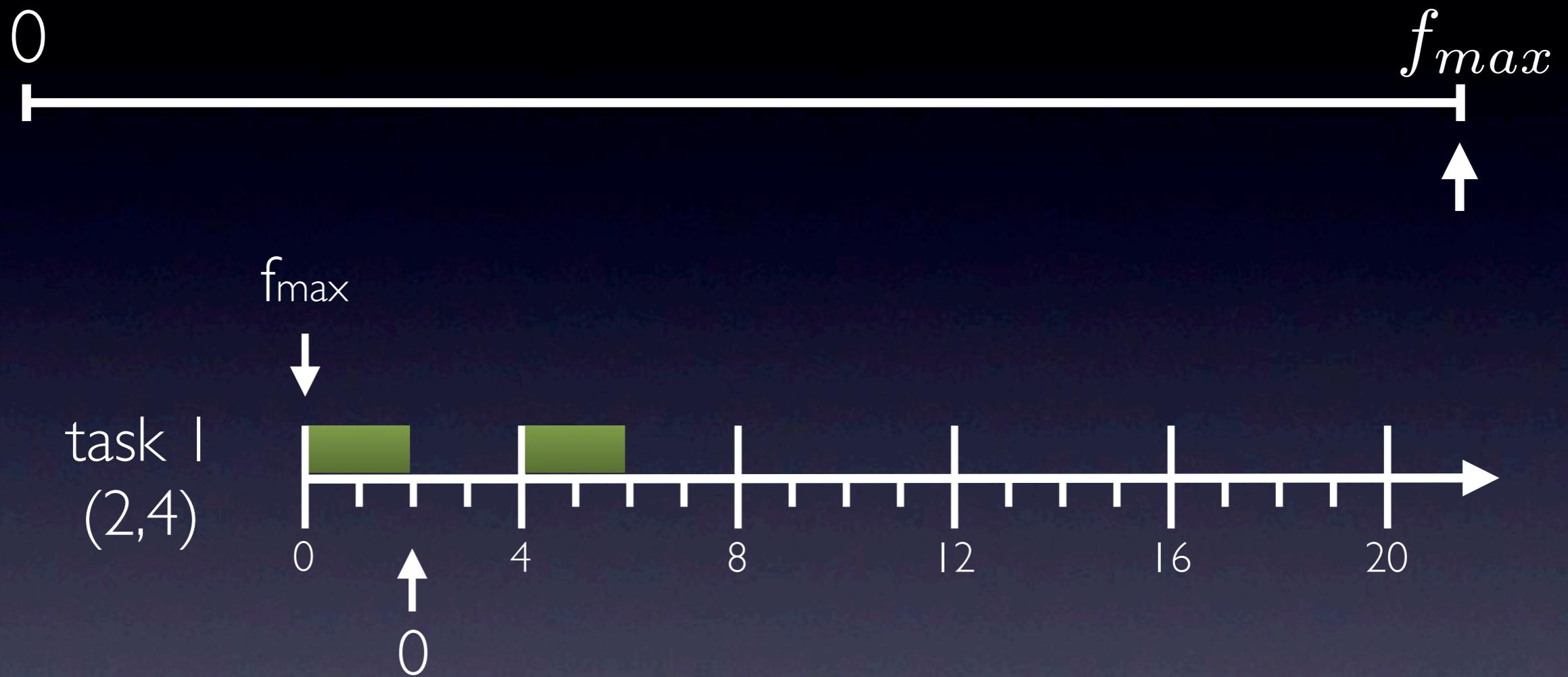


Two frequency levels



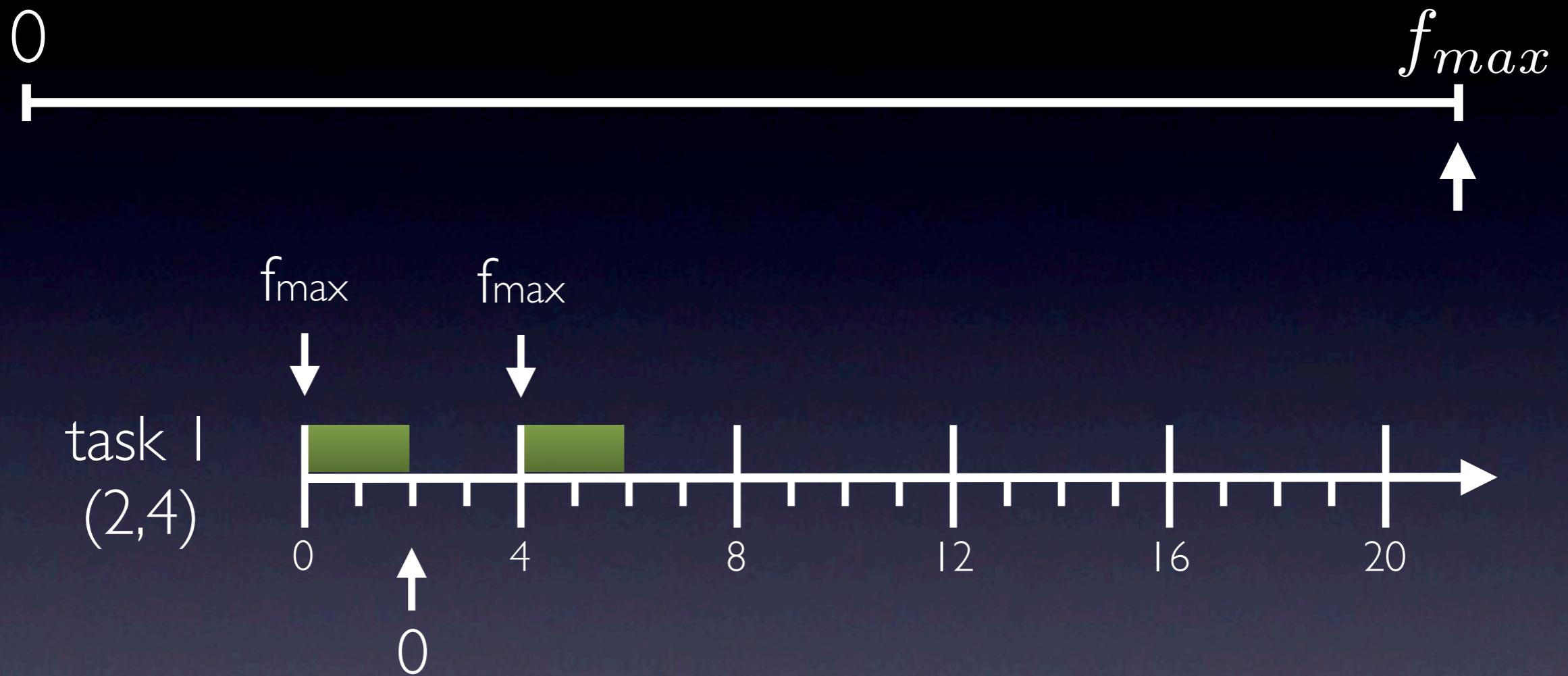


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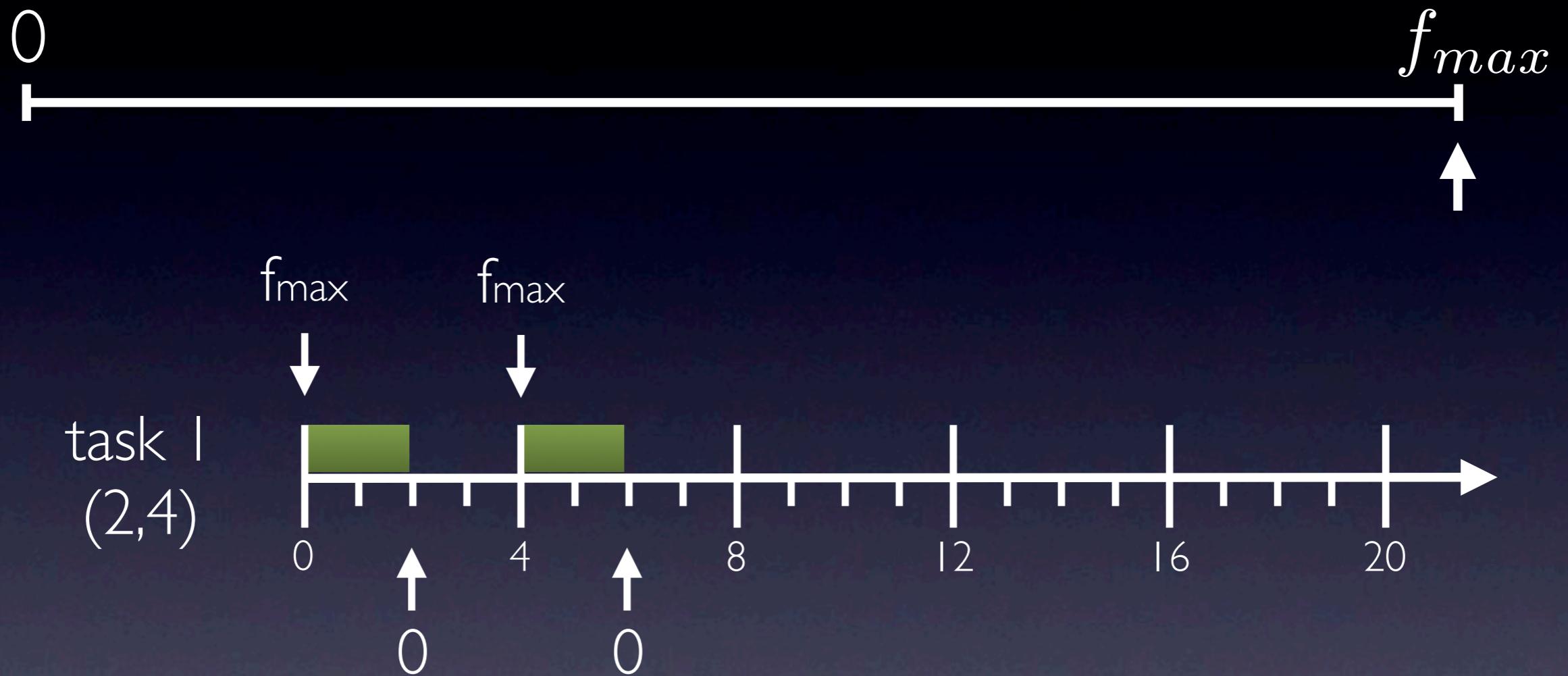


Two frequency levels



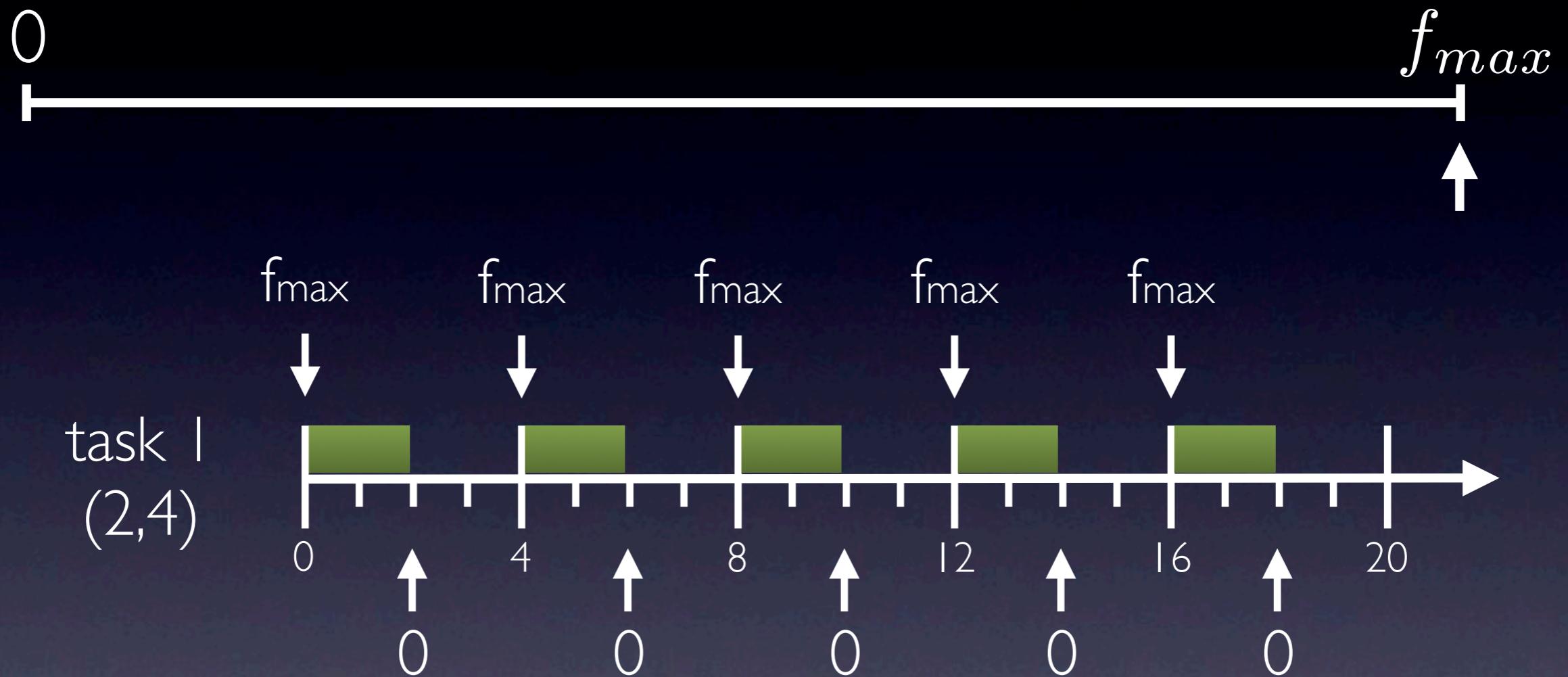


Two frequency levels





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Two frequency levels



$$E(1, U) = (t_1 - t_0)c_1 U f_{max}^\omega$$



Two frequency levels



$$E(1, U) = (t_1 - t_0)c_1 U f_{max} \sum_{i=1}^n \frac{C_i}{T_i}$$



Two frequency levels



$$E(1, U) = (t_1 - t_0)c_1 U f_{max} \sum_{i=1}^n \frac{C_i}{T_i}$$

$$bE_i^u = bE_i^l = E(1, U_i) = (t_1 - t_0)c_1 U_i f_{max}^{\omega}$$



Two frequency levels



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$$E\left(1, \sum_{i=1}^n U_i\right) = \sum_{i=1}^n E(1, U_i)$$



Two frequency levels



$$E(1, U) = (t_1 - t_0)c_1 U f_{max} \sum_{i=1}^n \frac{C_i}{T_i}$$

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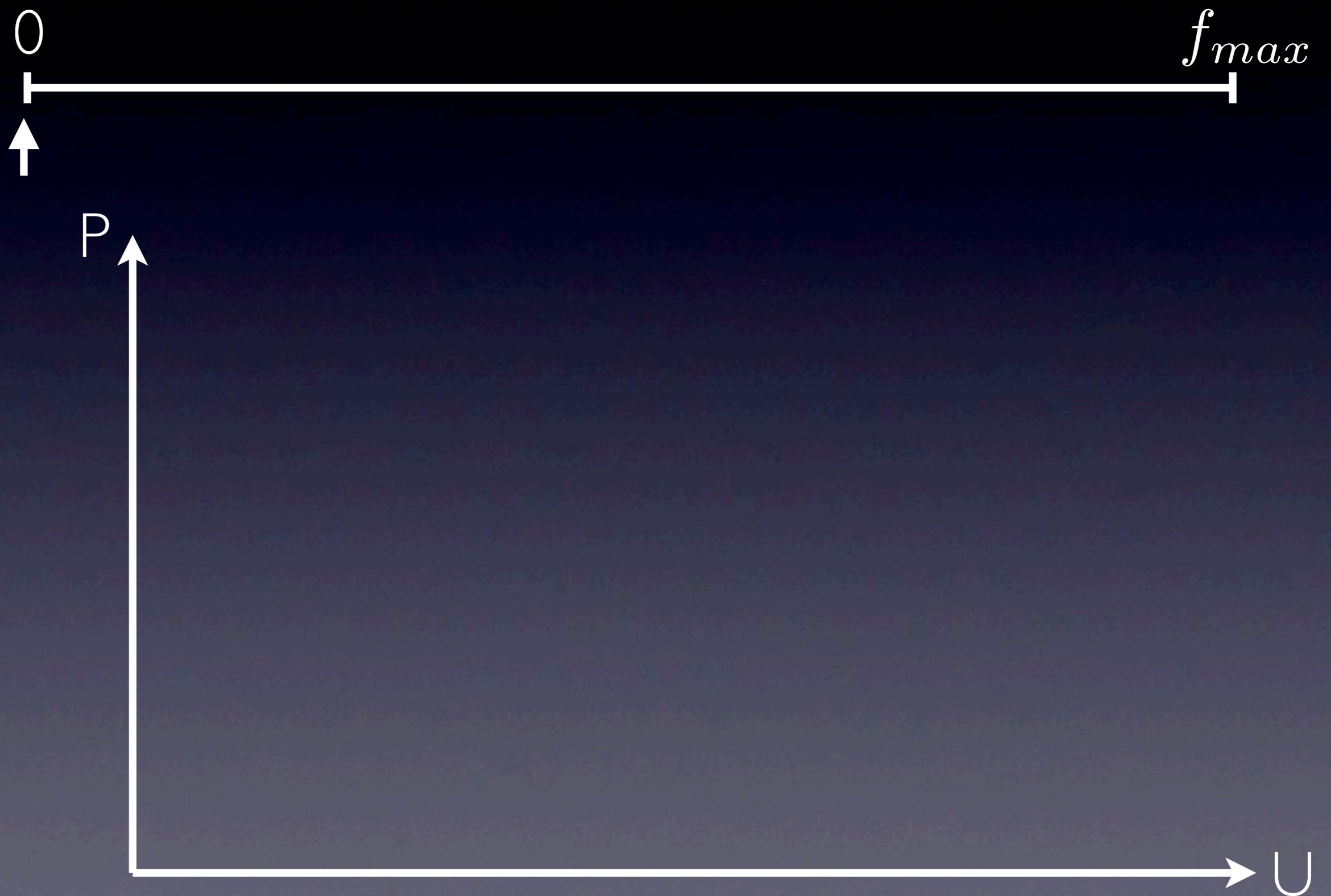
$$E\left(1, \sum_{i=1}^n U_i\right) = \sum_{i=1}^n E(1, U_i)^*$$



Continuous frequency levels

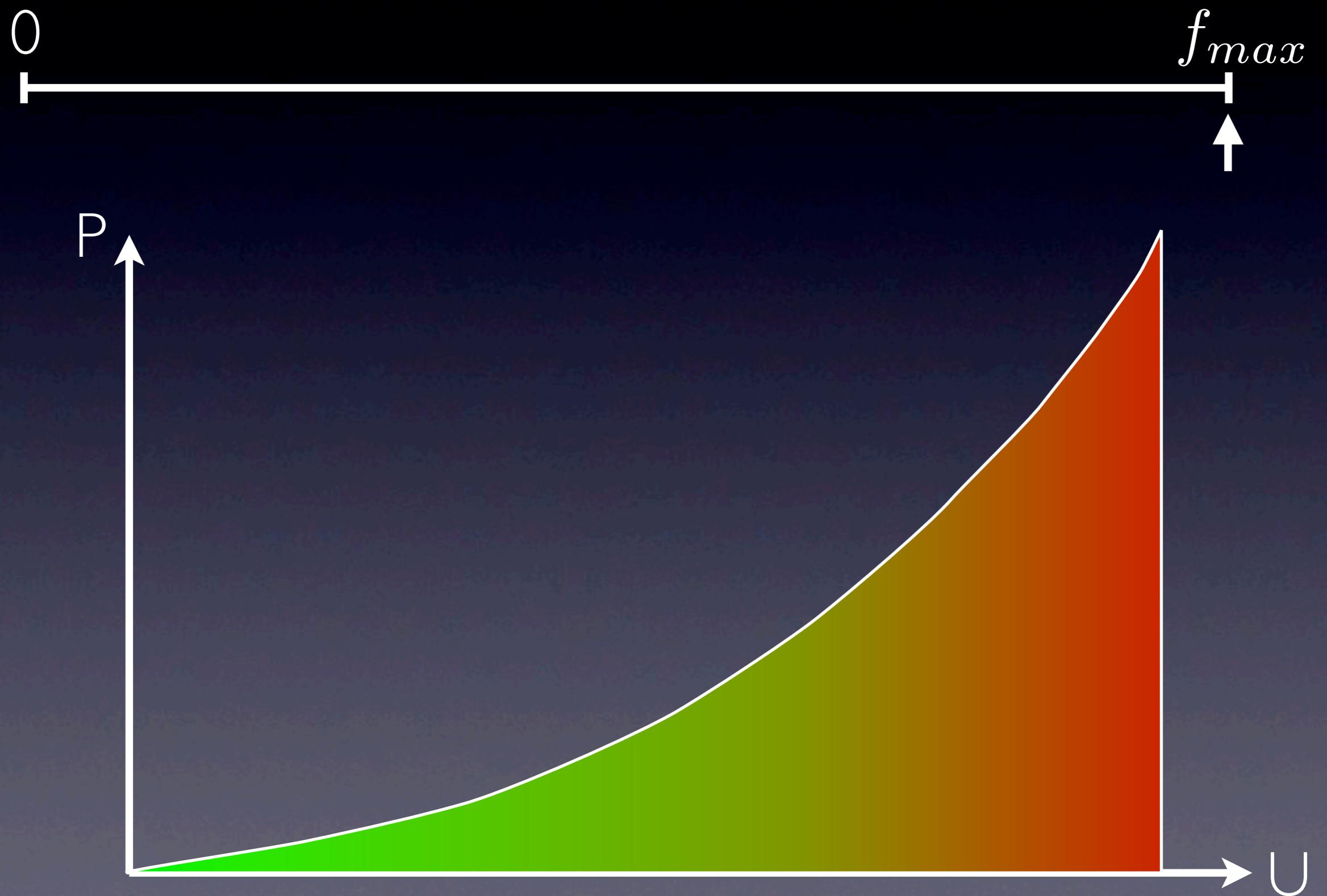


Continuous frequency levels



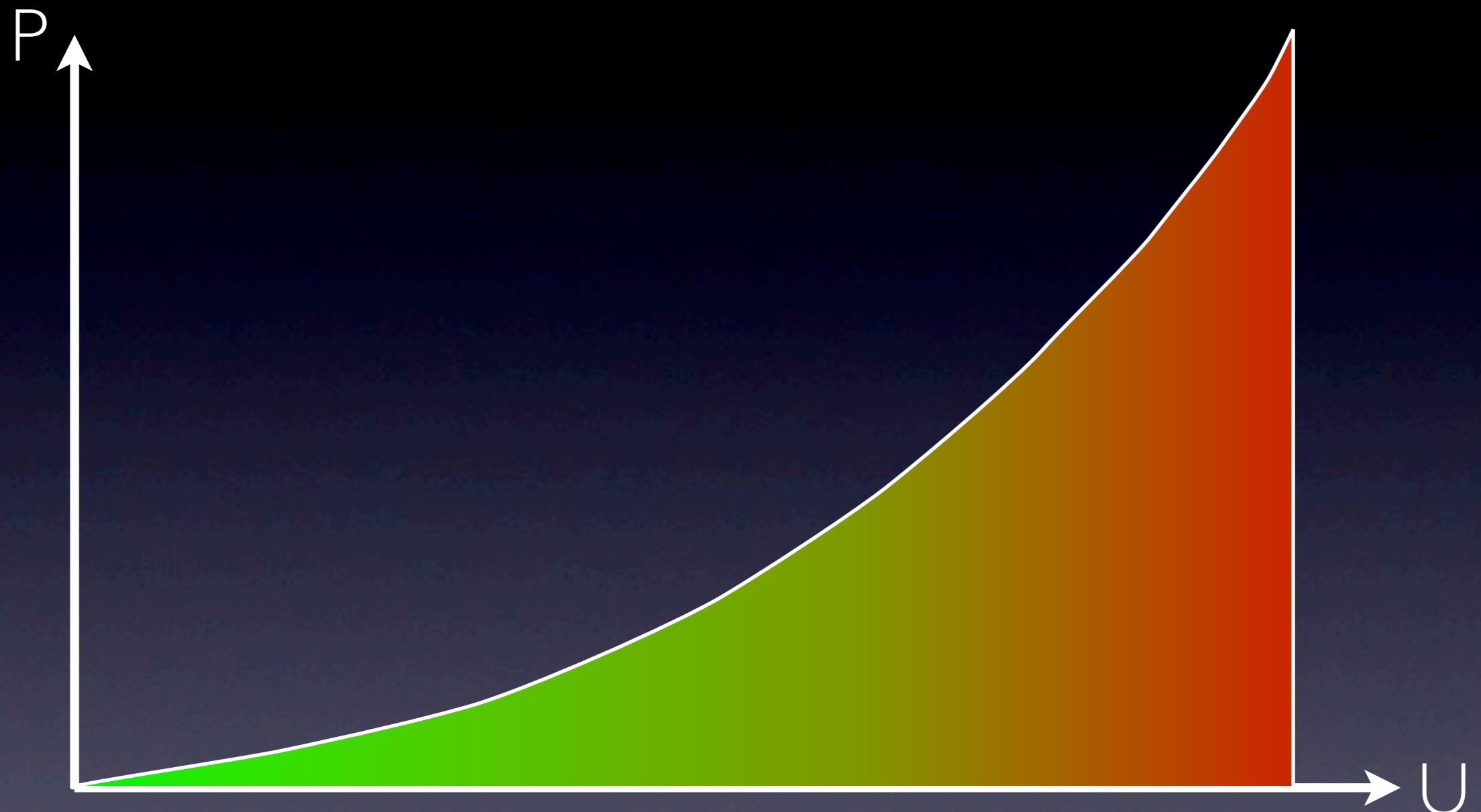


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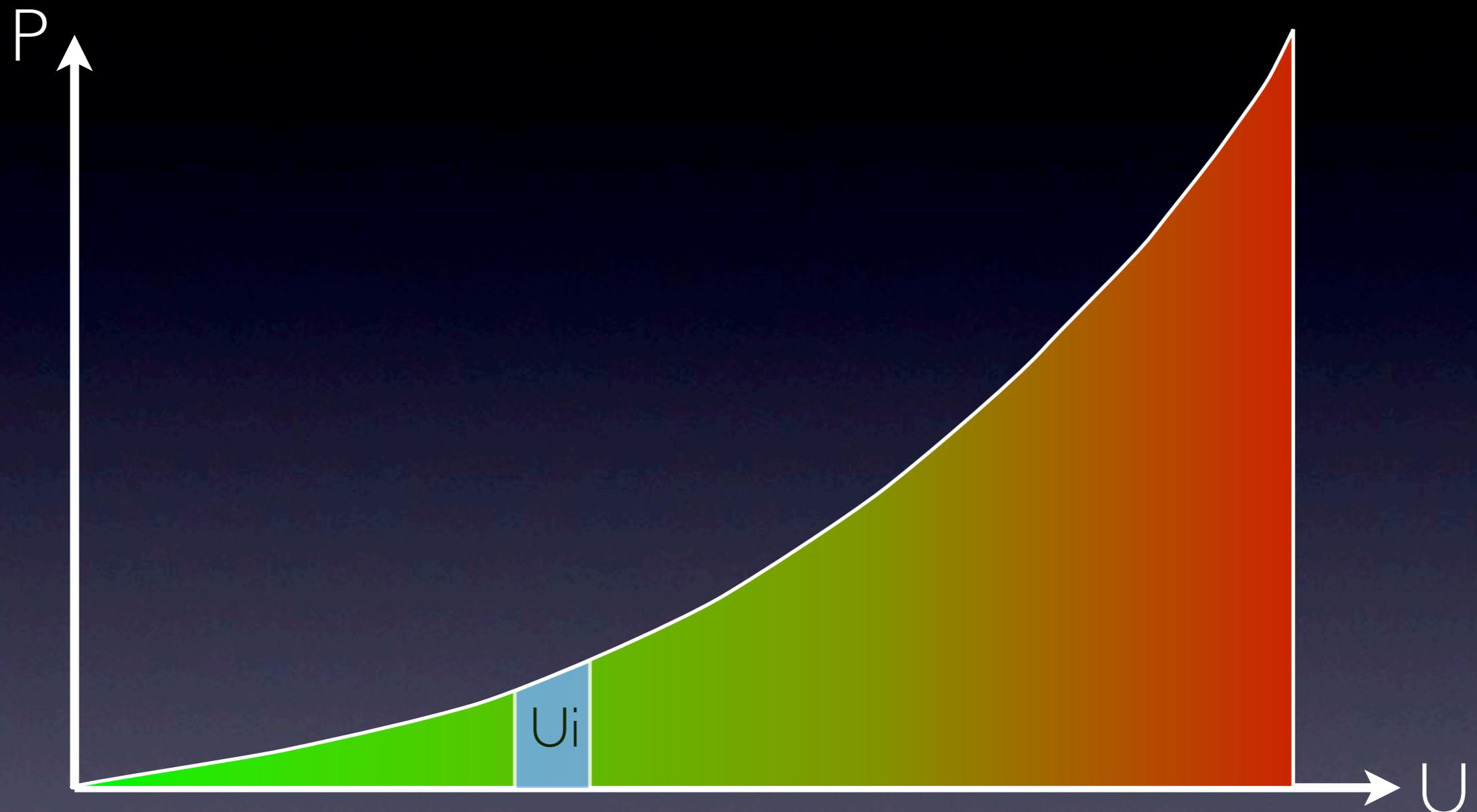


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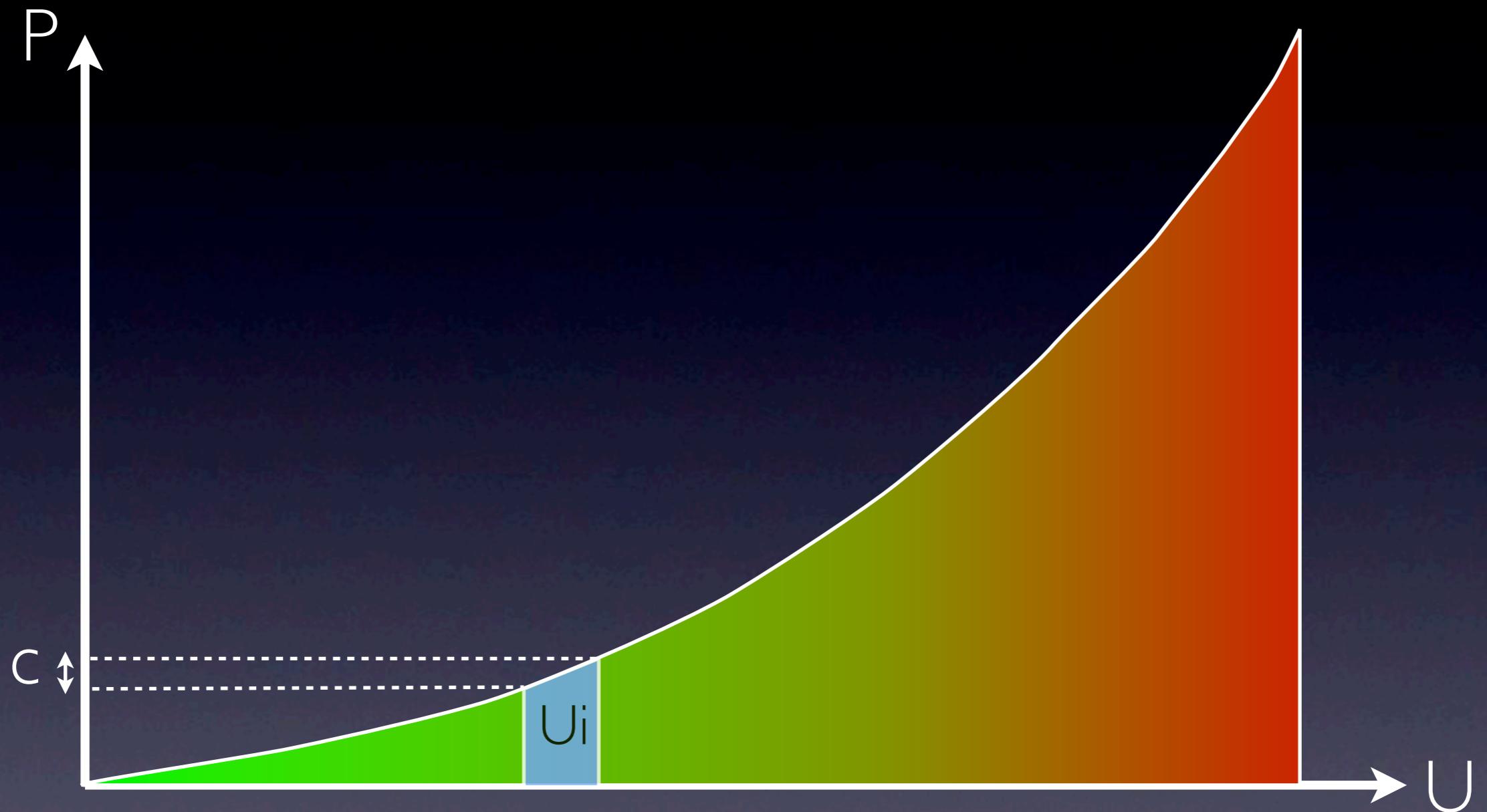


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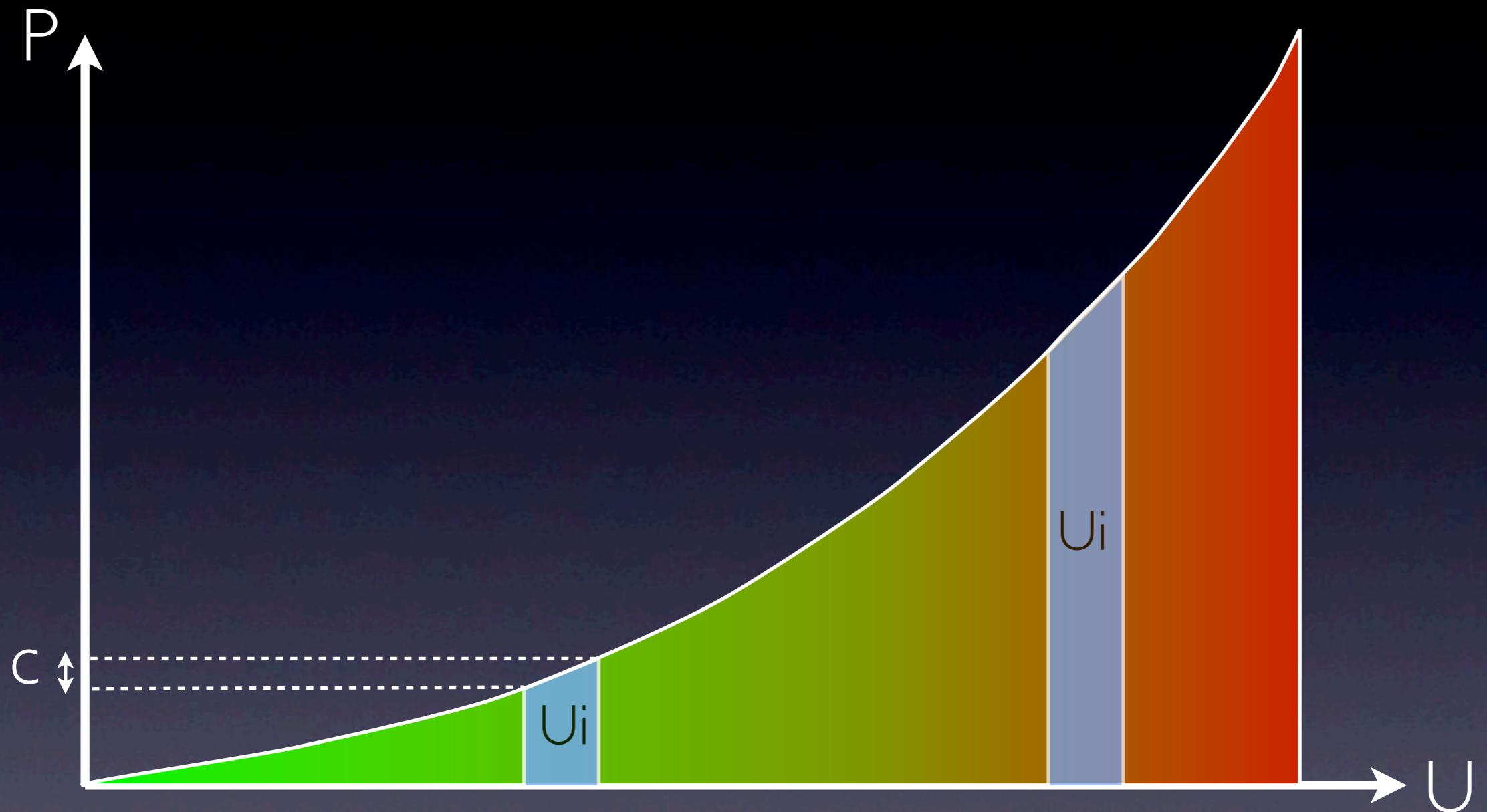


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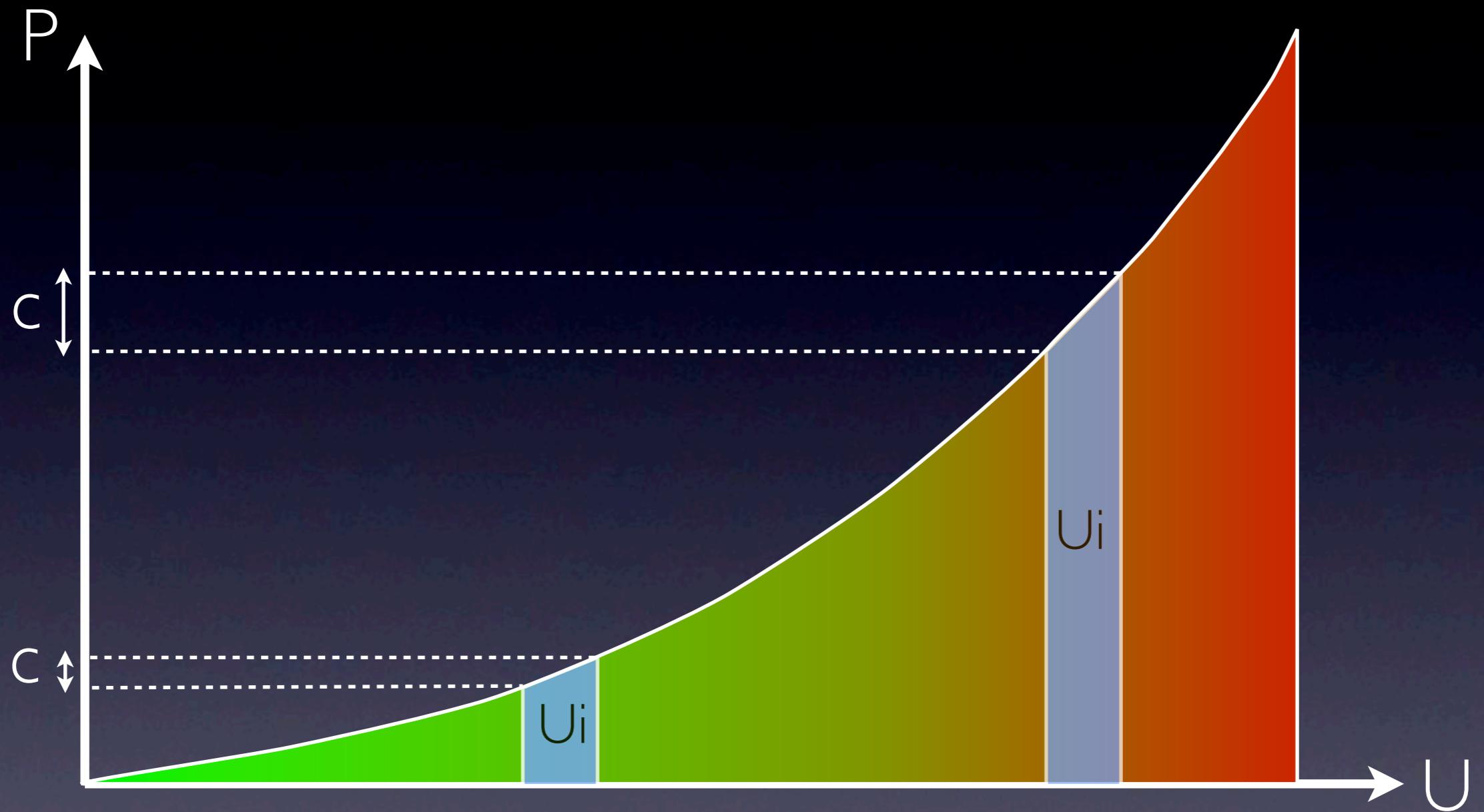


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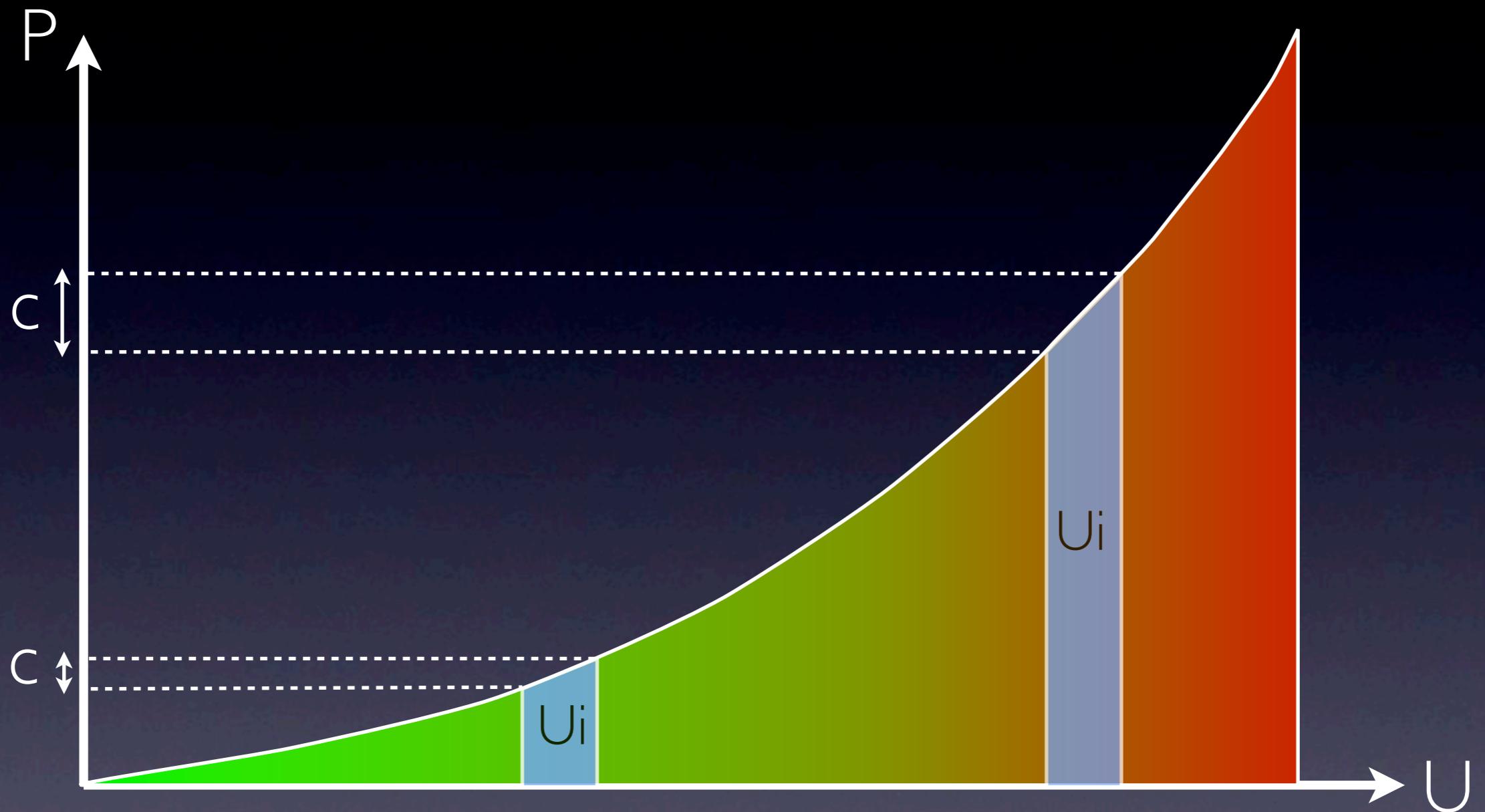


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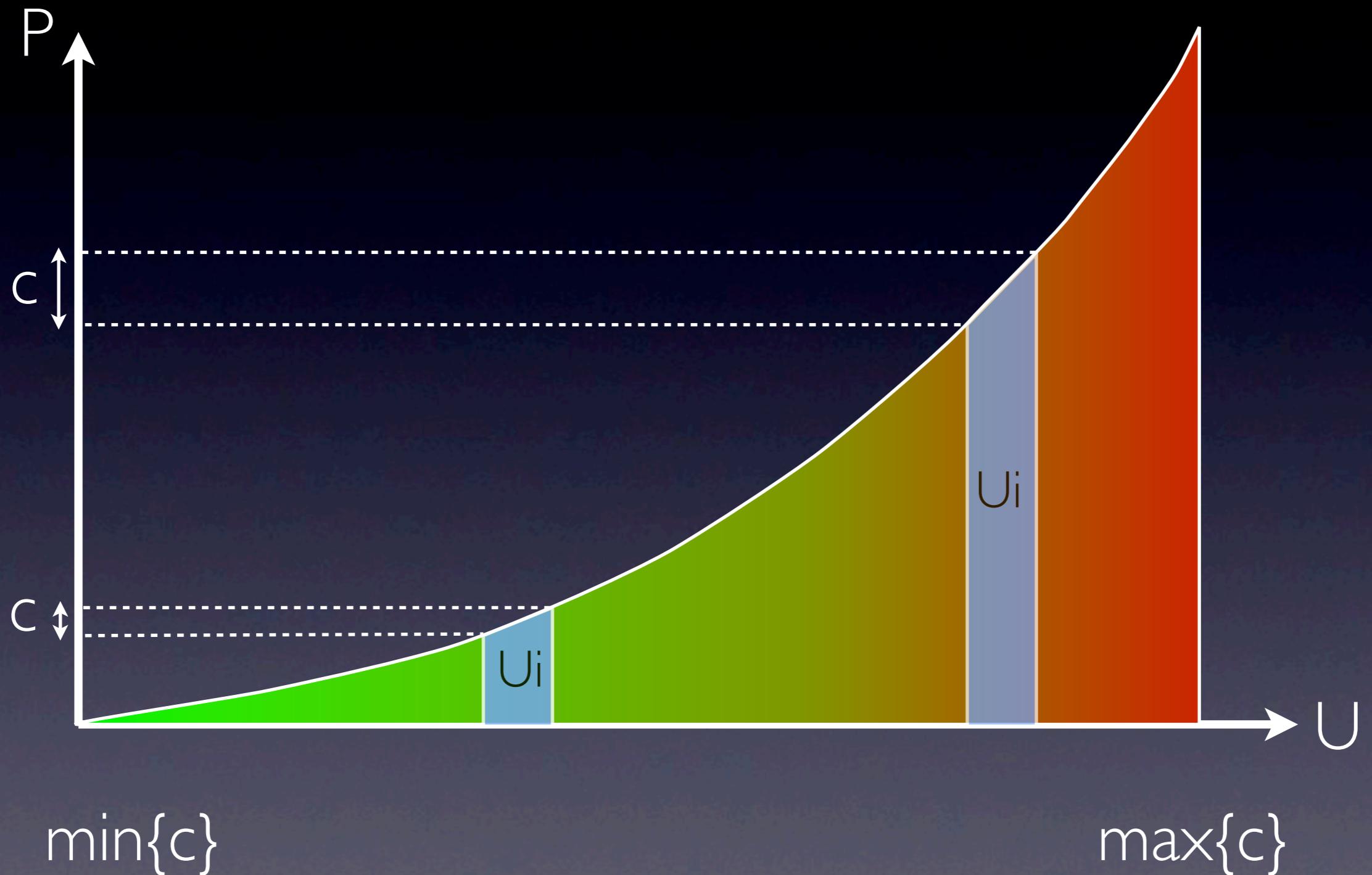


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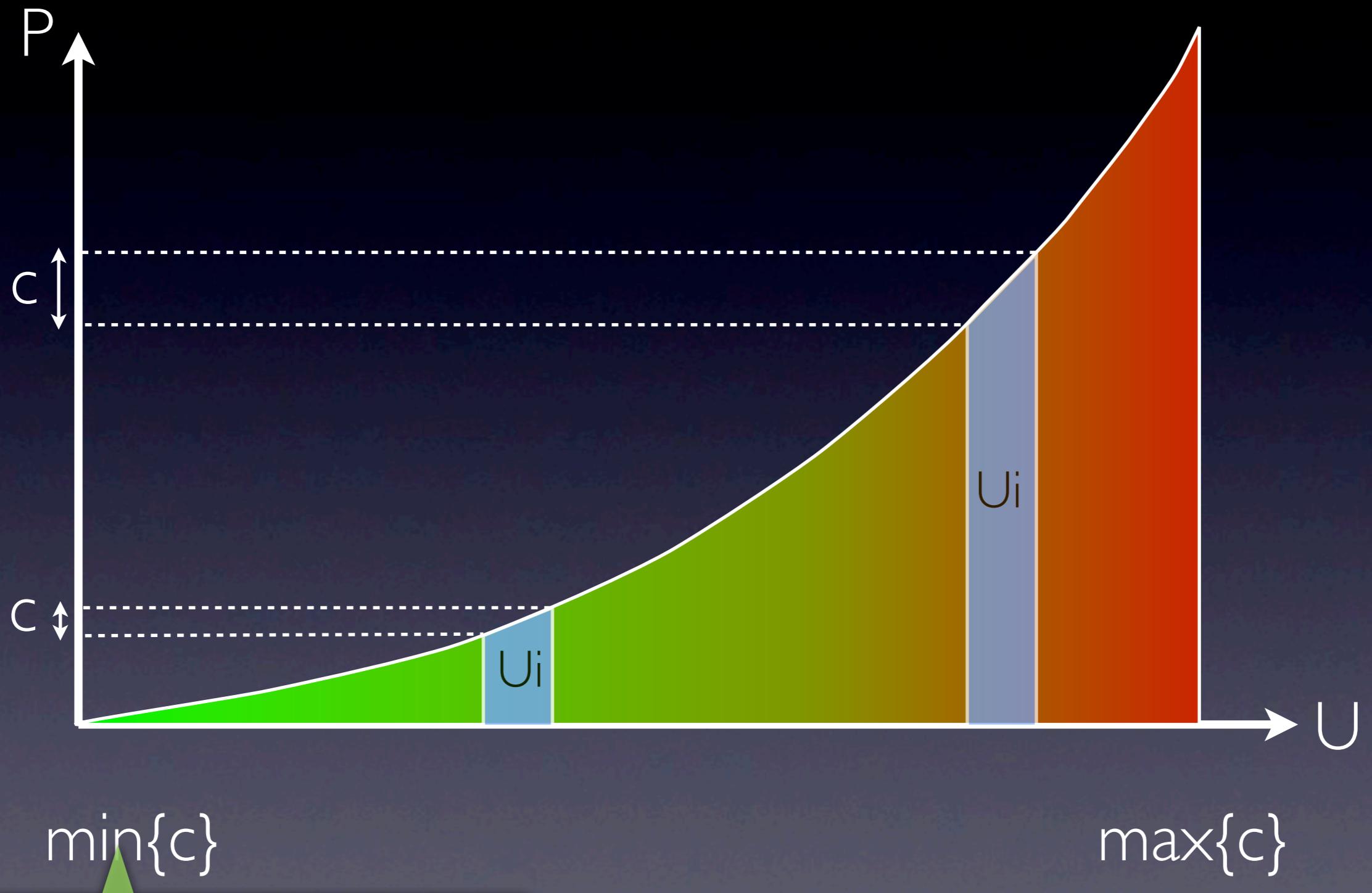


Continuous frequency levels





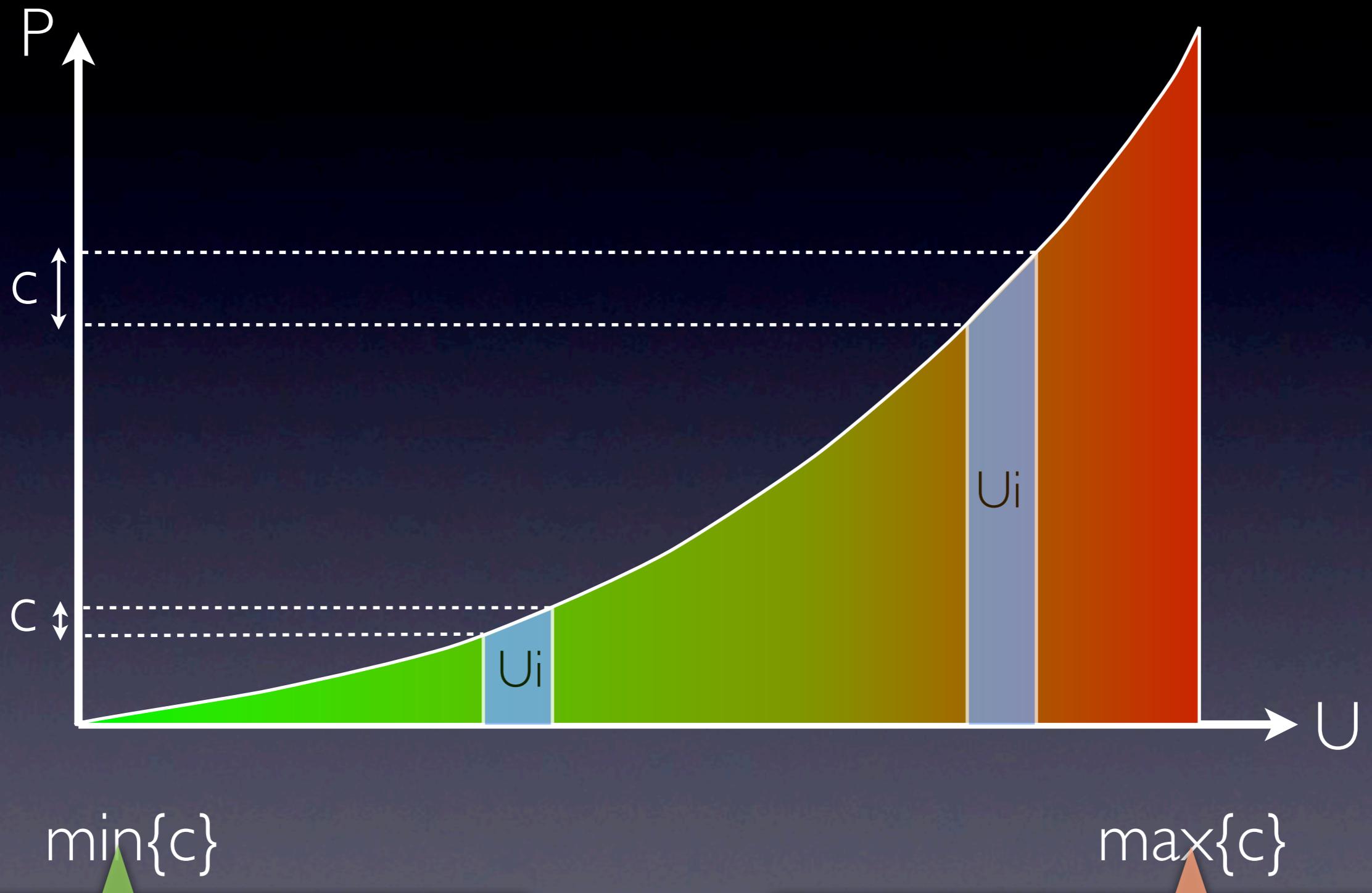
Continuous frequency levels



task i is the only running task



Continuous frequency levels



task i is the only running task

f is switched from $l - U_i$ to l



Continuous frequency levels



Continuous frequency levels

$$E(U, U) = (t_1 - t_0)c_1(f_{max}U)^\omega.$$



Continuous frequency levels

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$$bE_i^l = E(U_i, U_i) = (t_1 - t_0)c_1(f_{max}U_i)^\omega$$



Continuous frequency levels

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$$bE_i^u = E(1, 1) - E(1 - U_i, 1 - U_i)$$

$$= (t_1 - t_0)c_1 f_{max}^\omega (1 - (1 - U_i)^\omega)$$



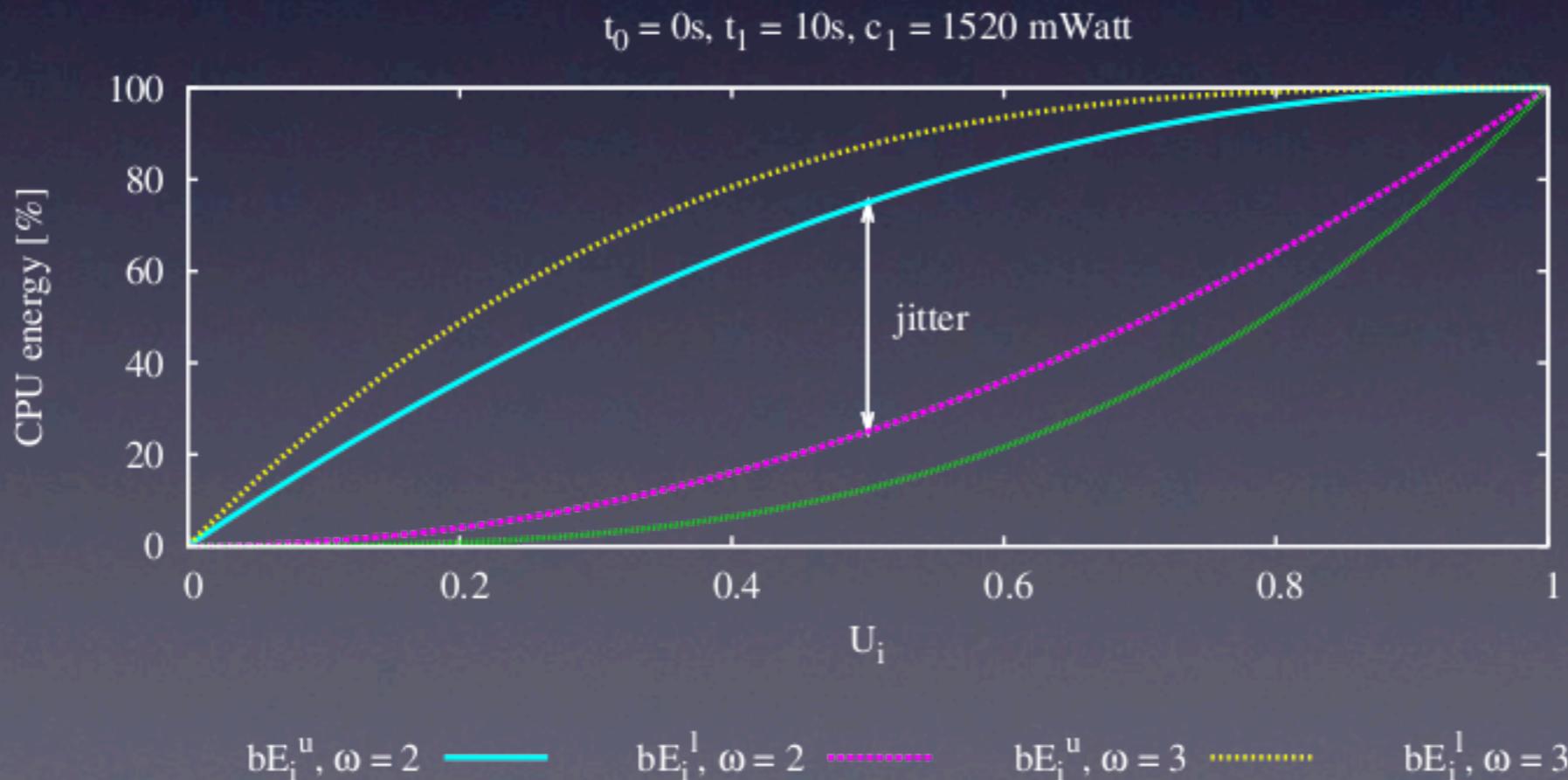
Continuous frequency levels

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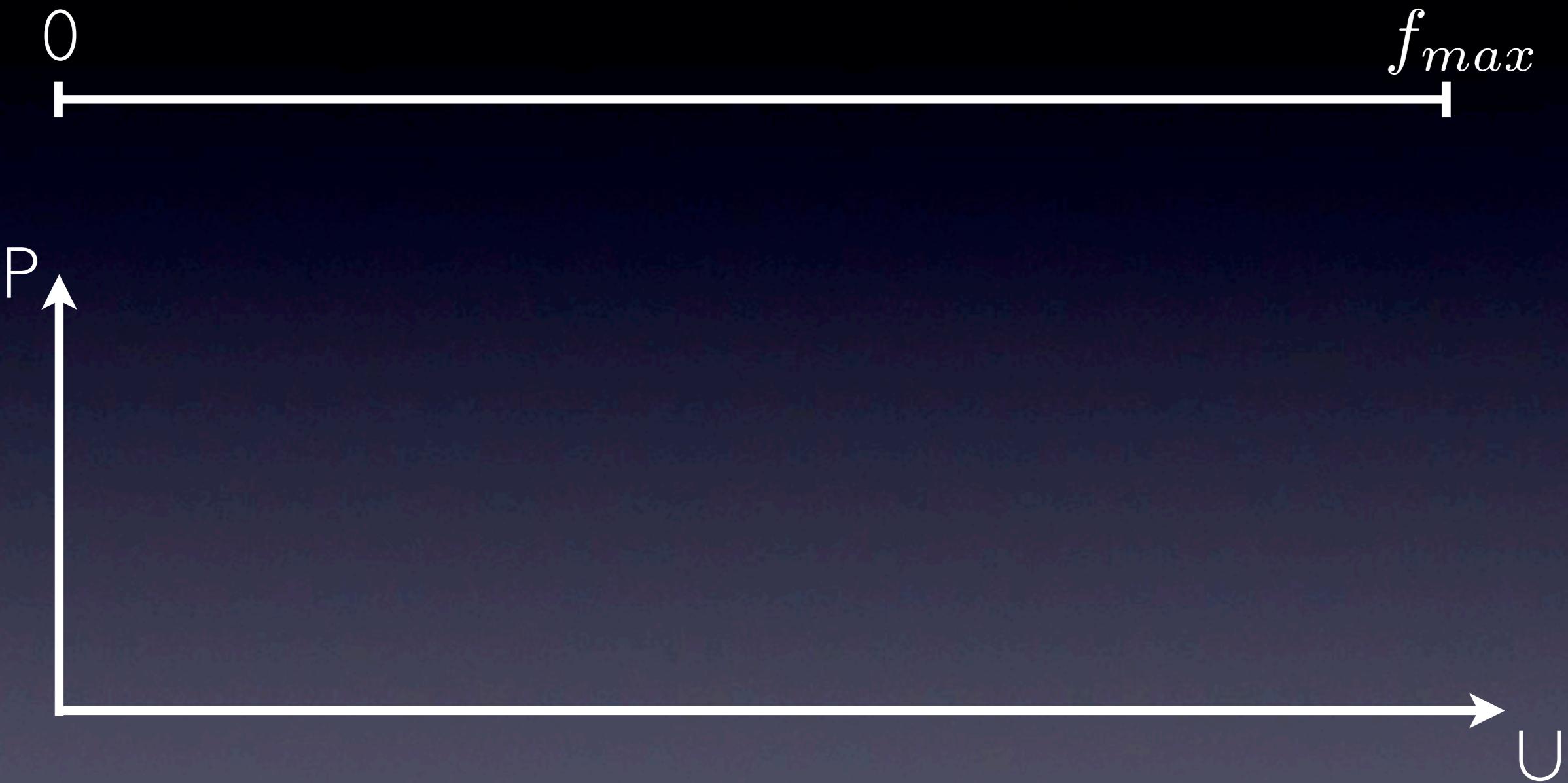




Discrete frequency levels

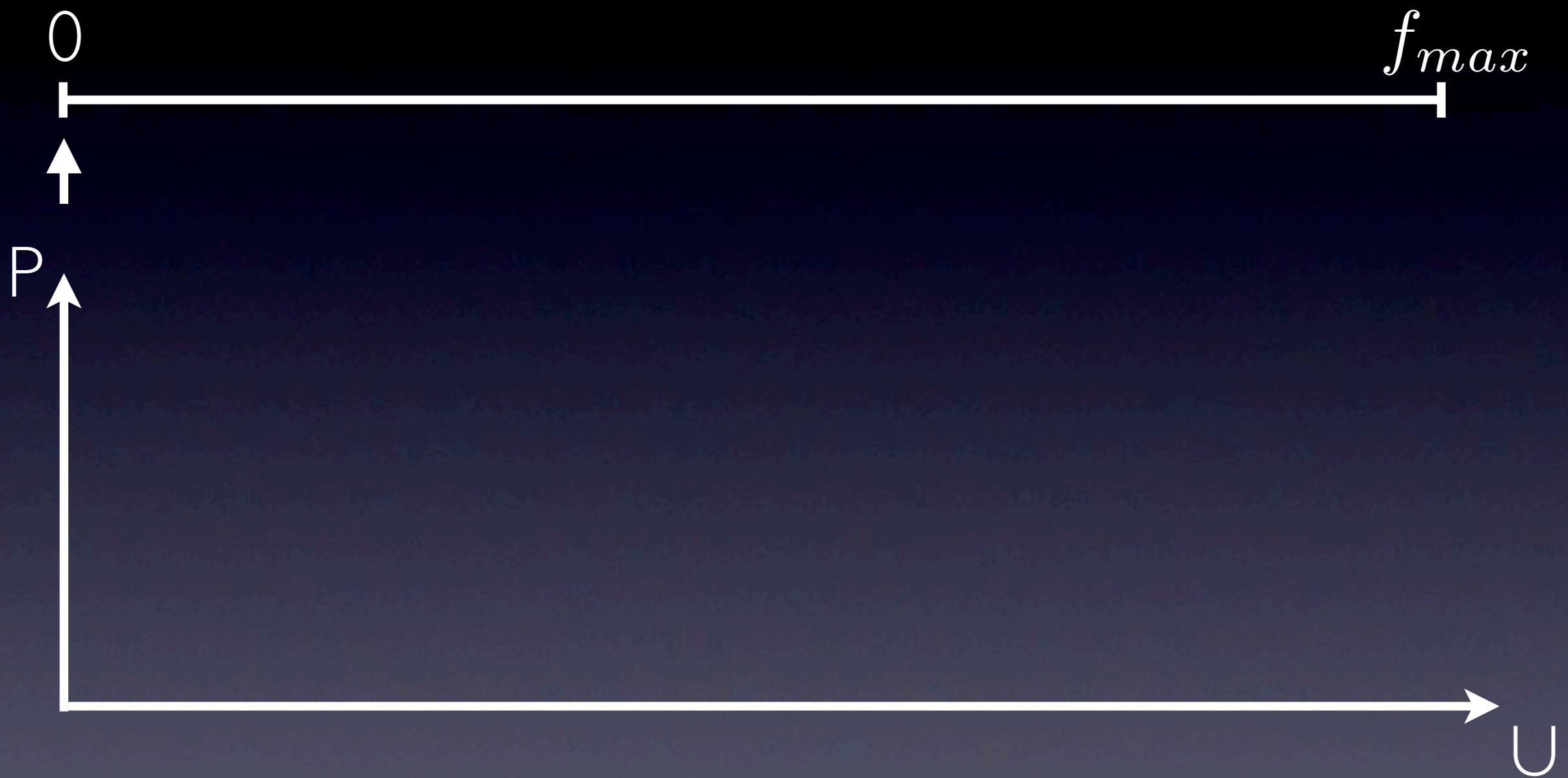


Discrete frequency levels



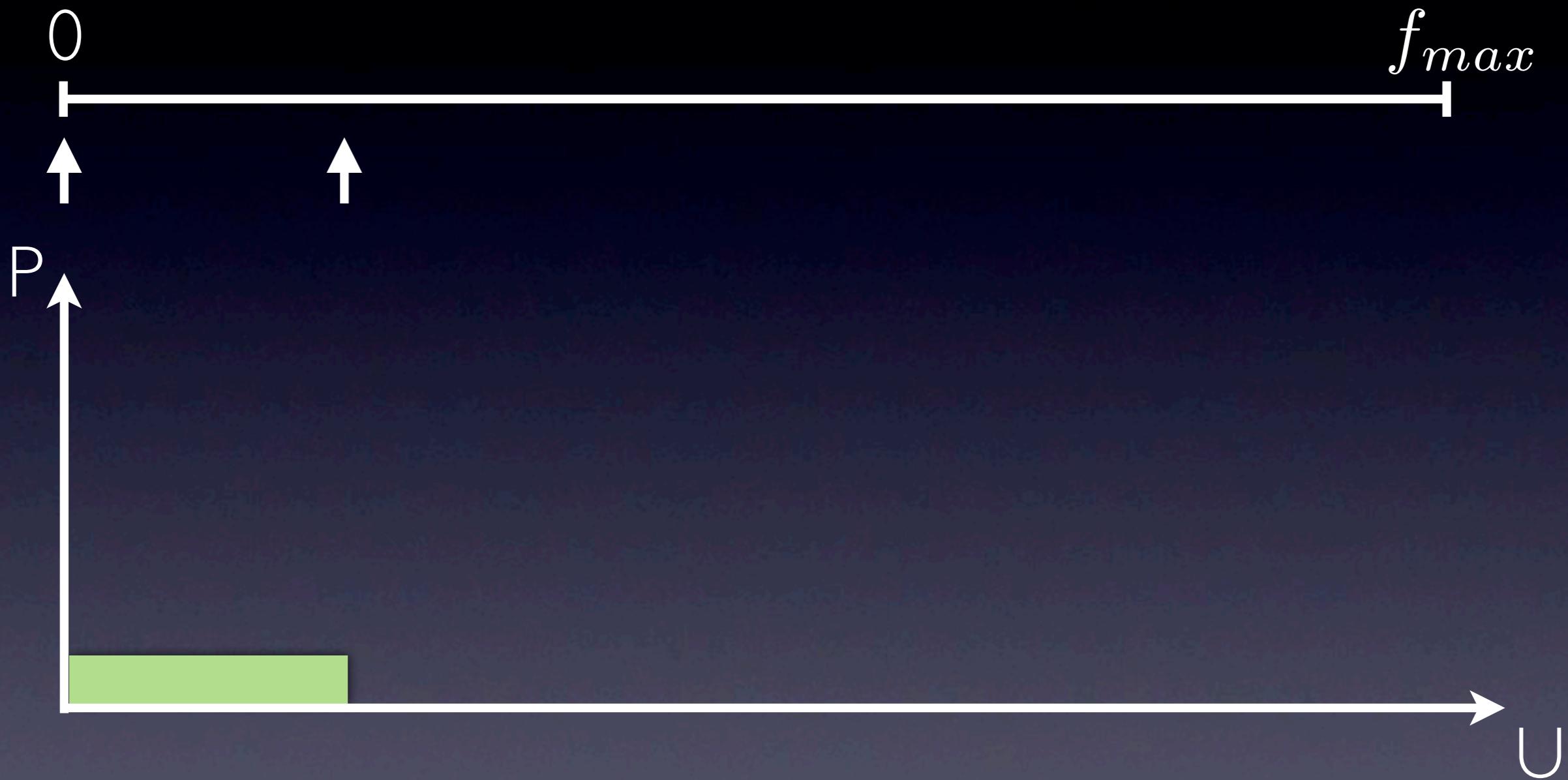


Discrete frequency levels



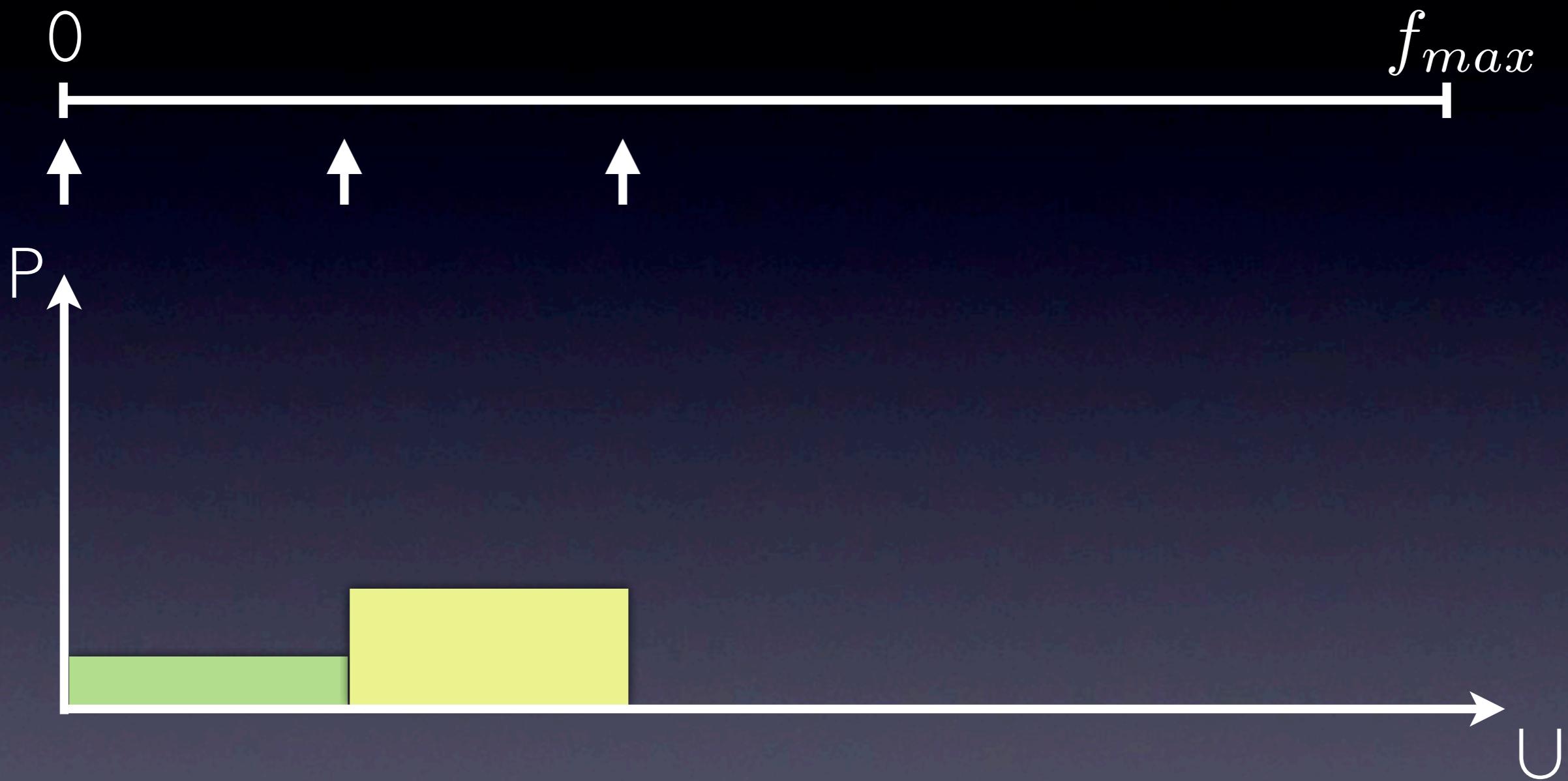


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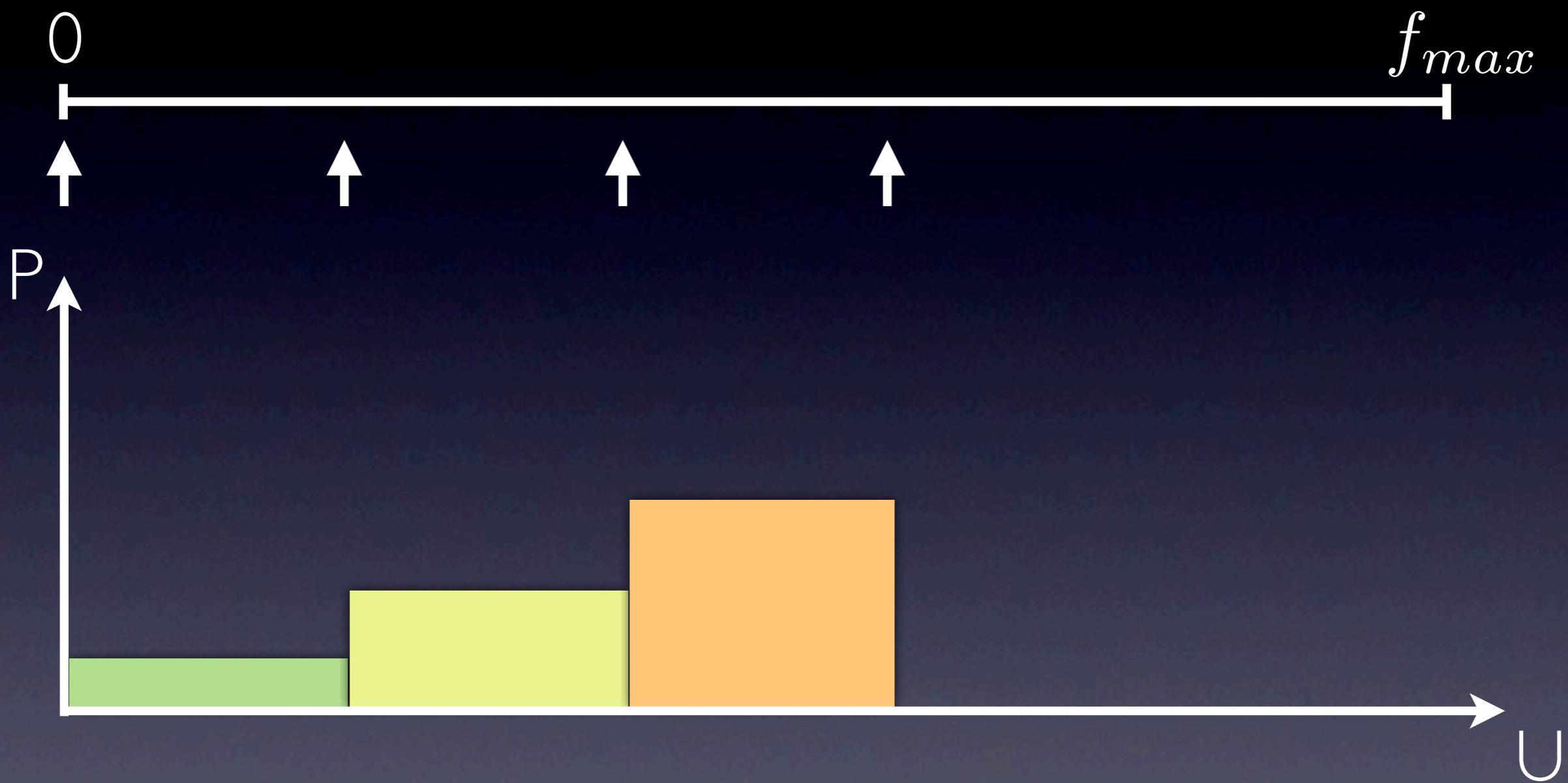


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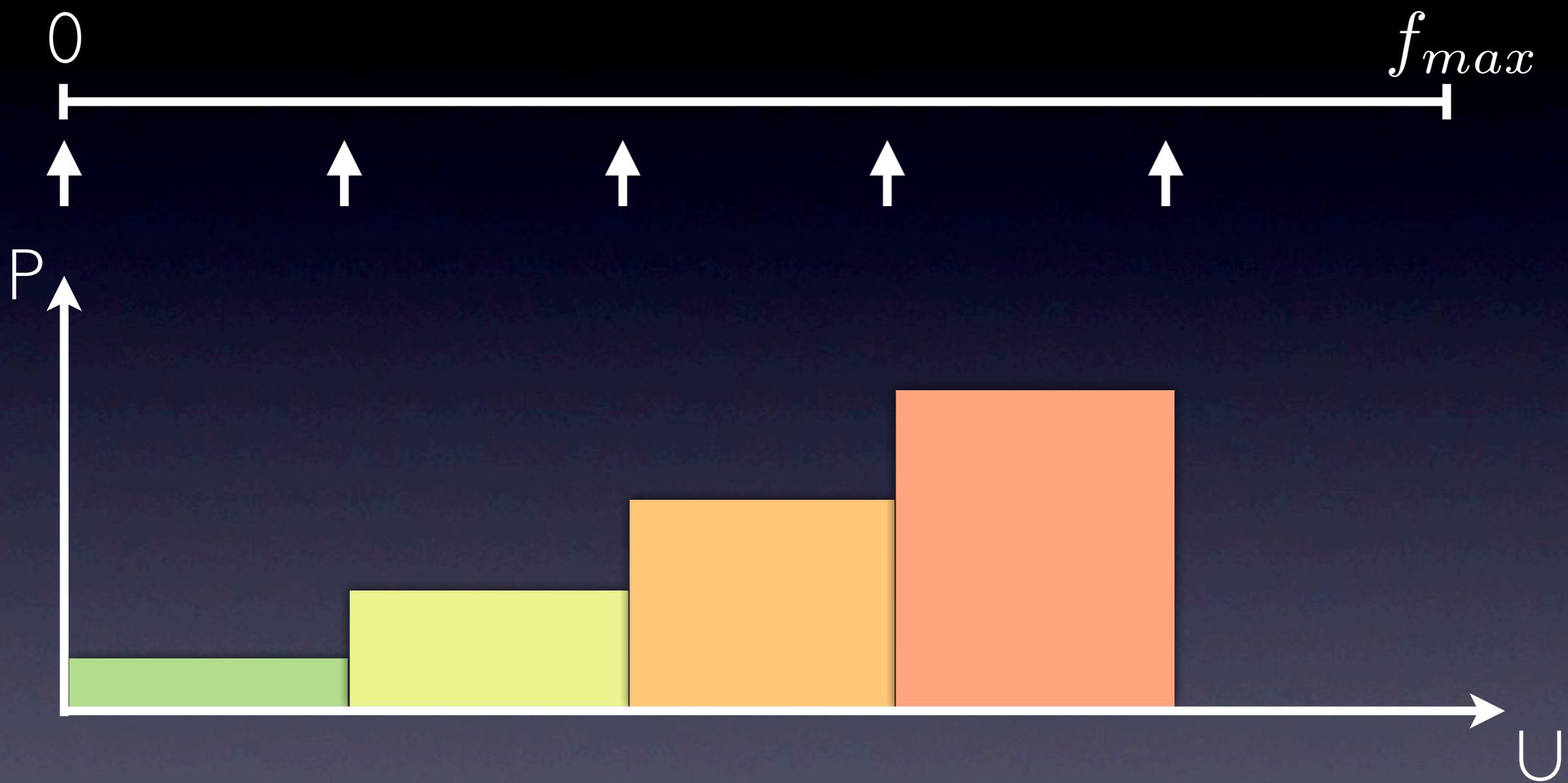


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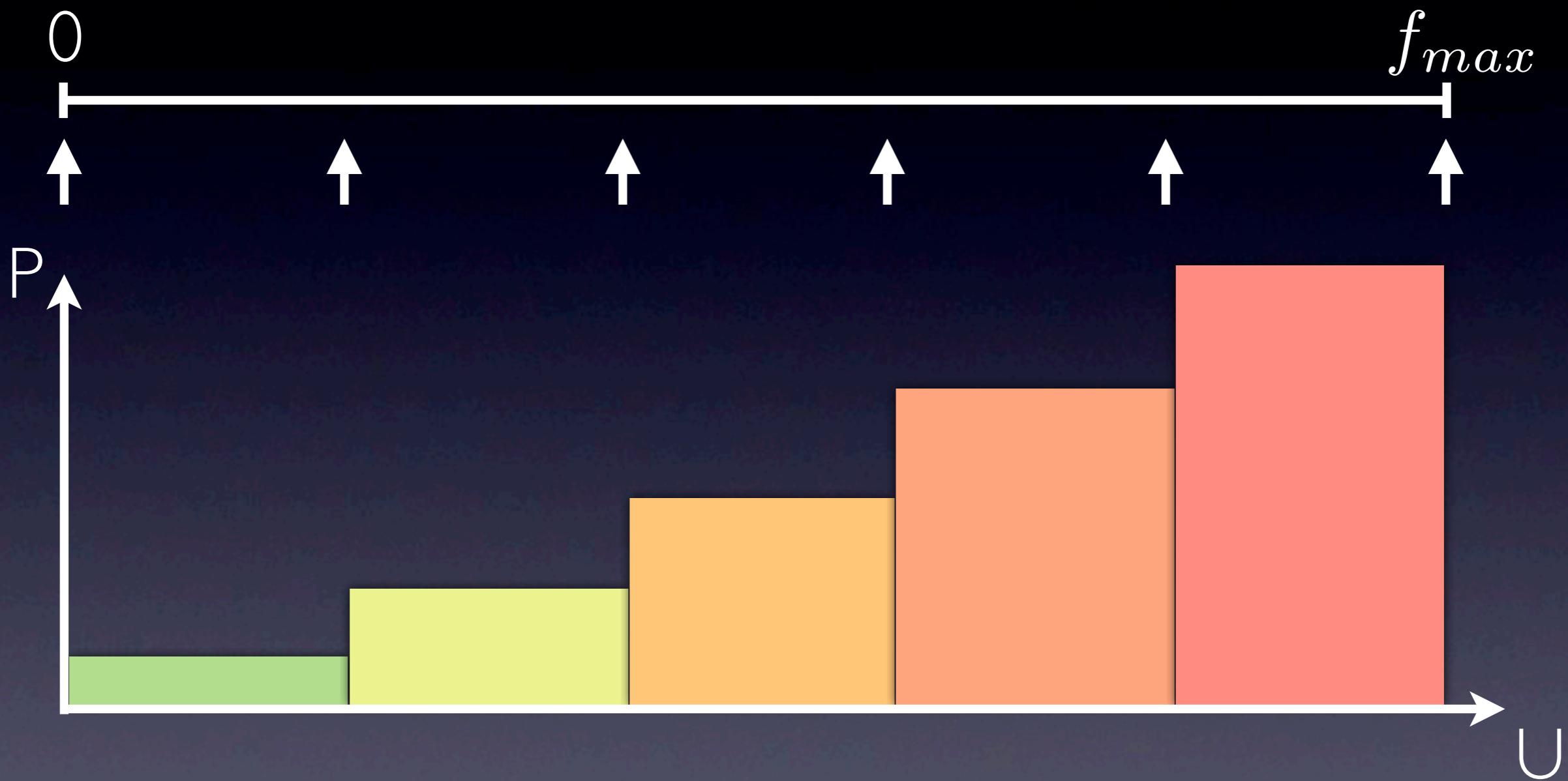


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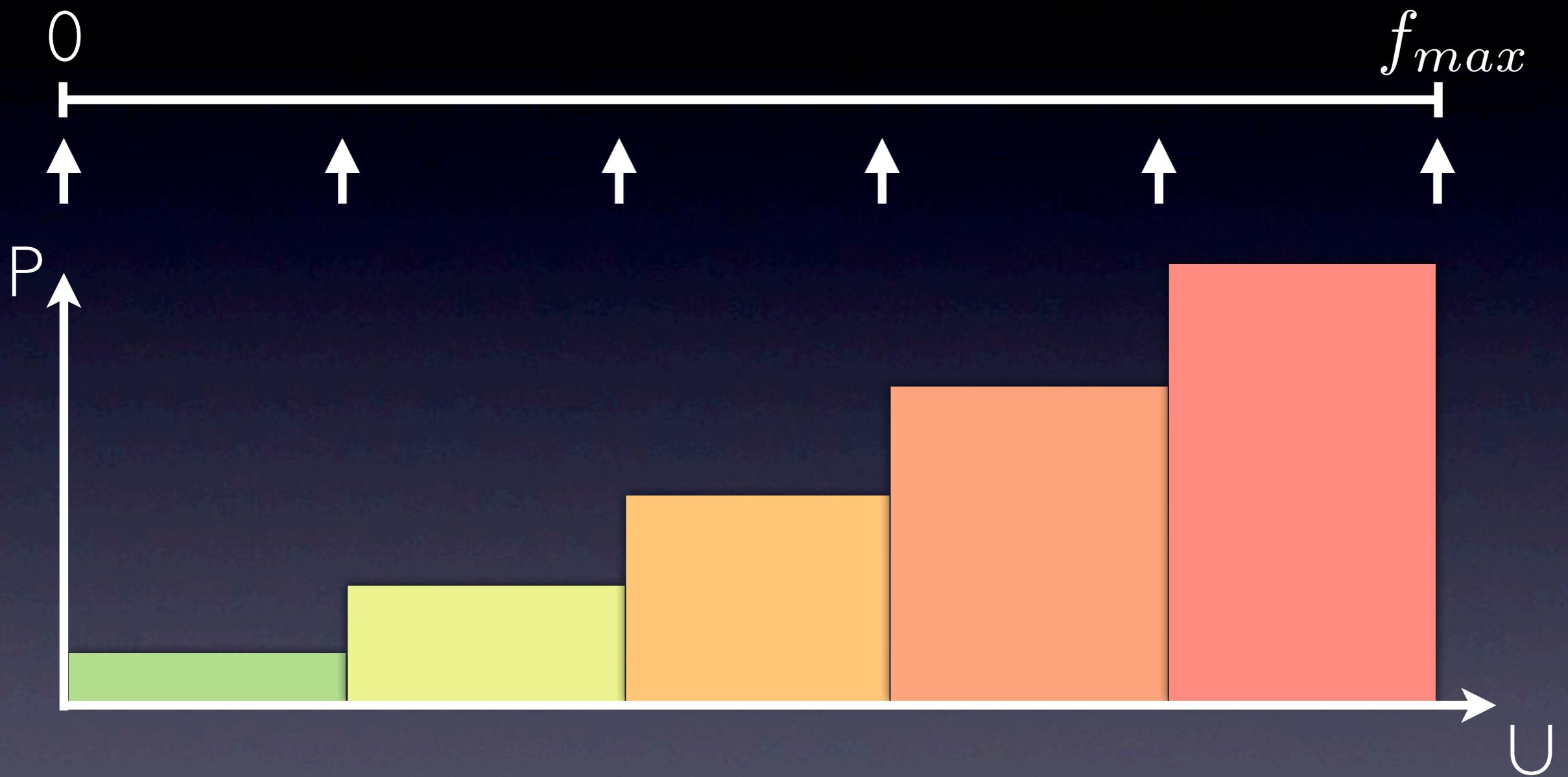


Discrete frequency levels





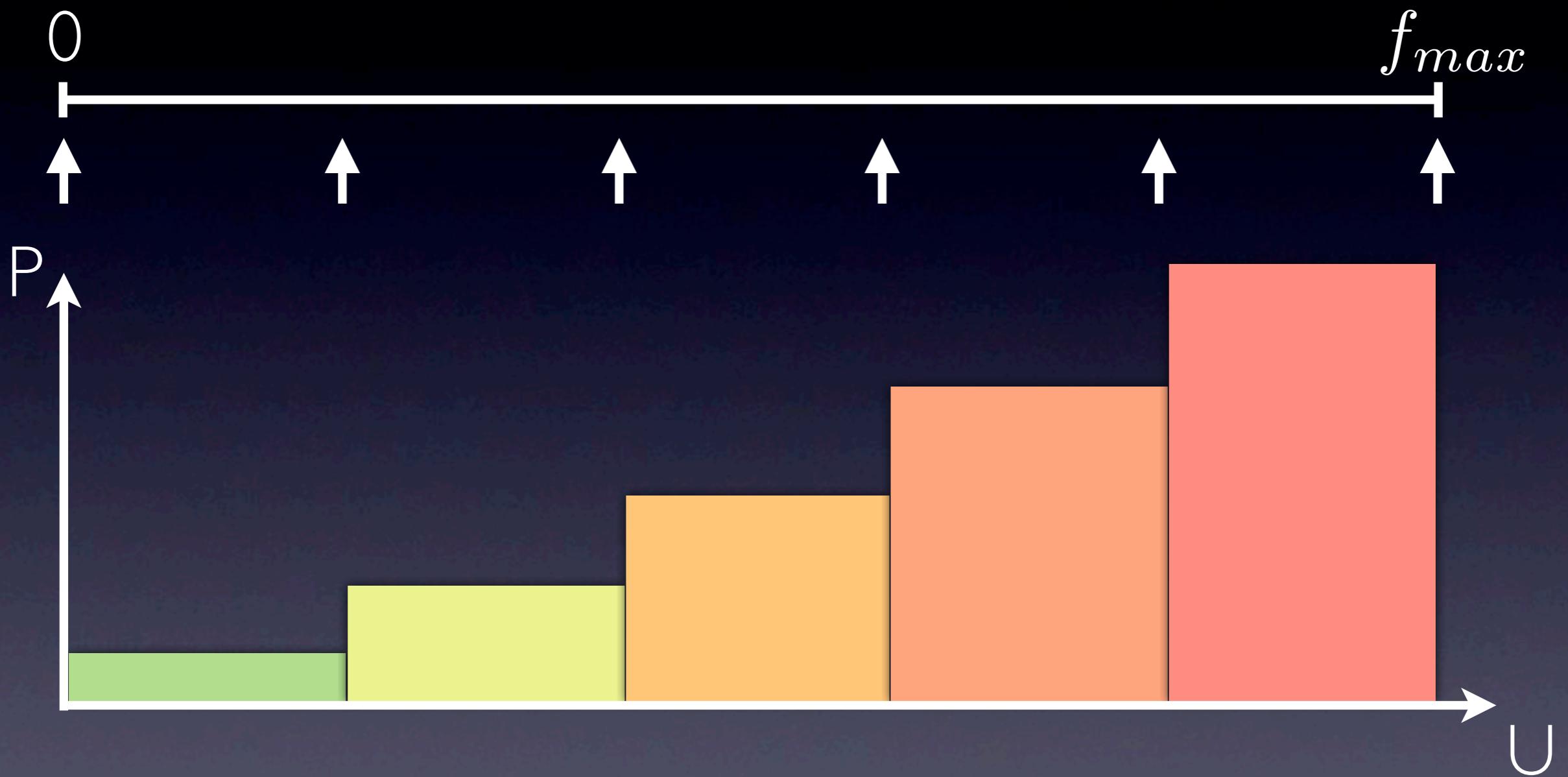
Discrete frequency levels



Minimum contribution of task i to the power consumption



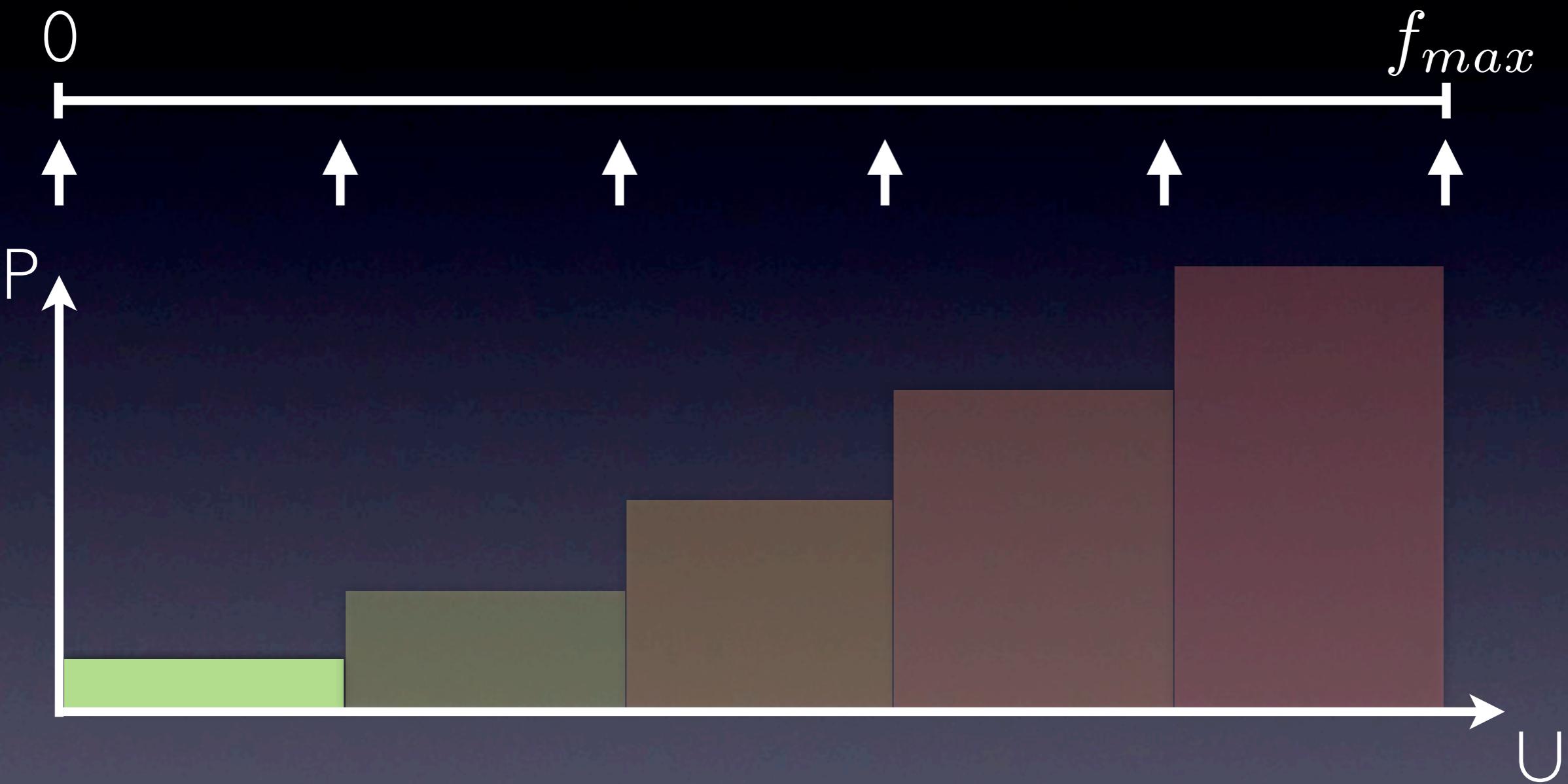
Discrete frequency levels



Minimum contribution of task i to the power consumption
Maximum contribution of task i to the power consumption

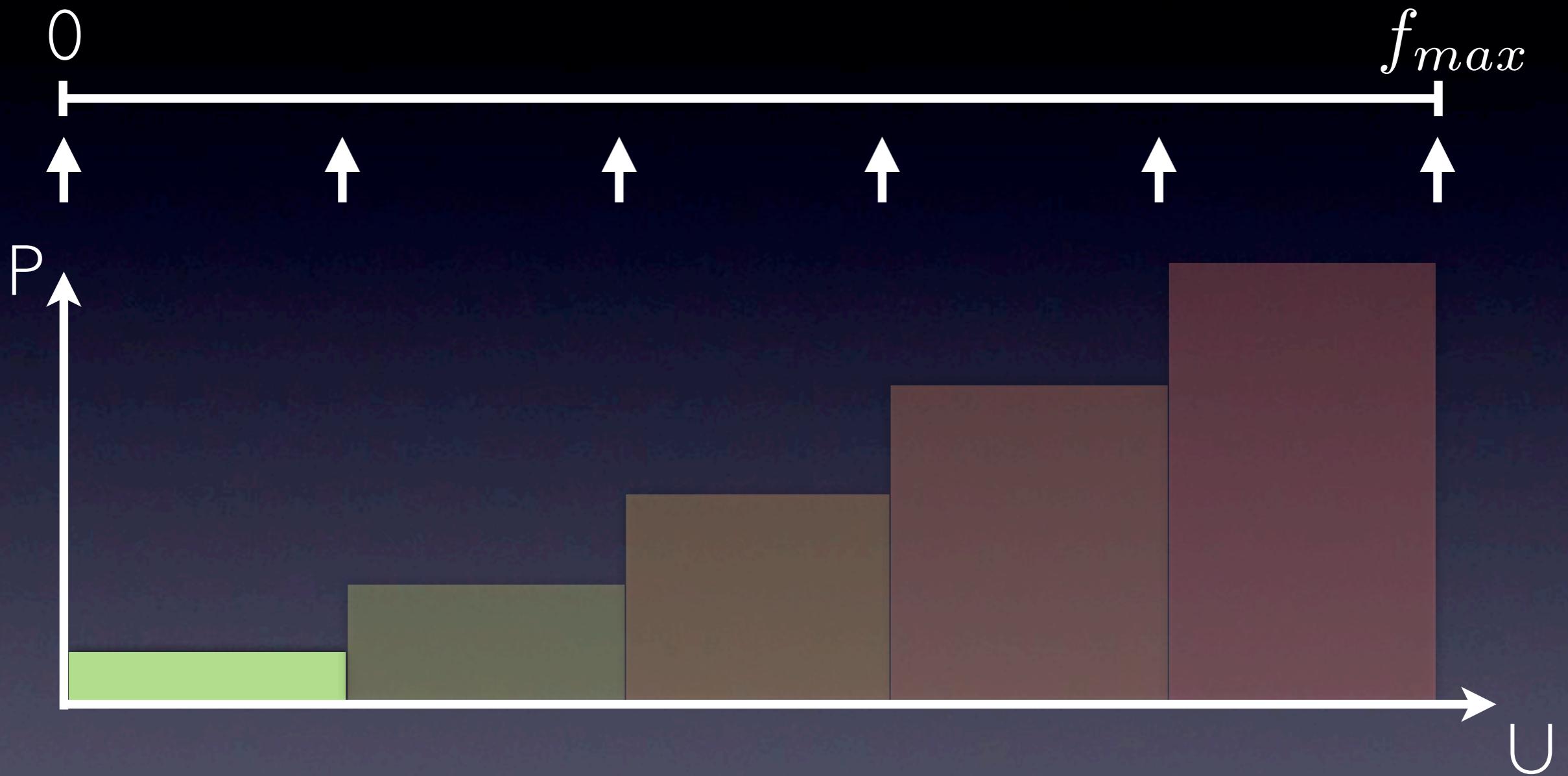


Minimum Contribution





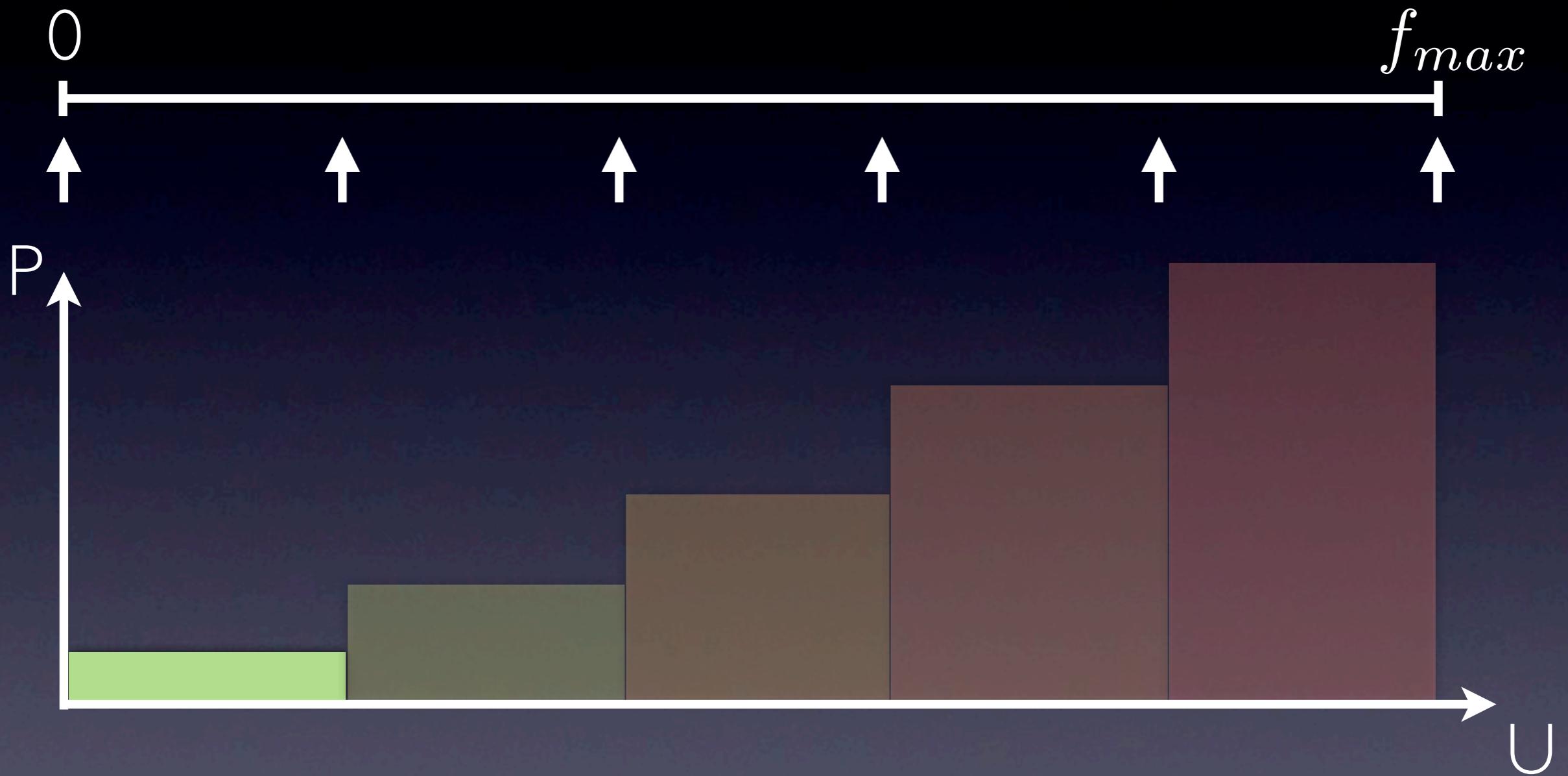
Minimum Contribution



Task i is the only task in the system



Minimum Contribution

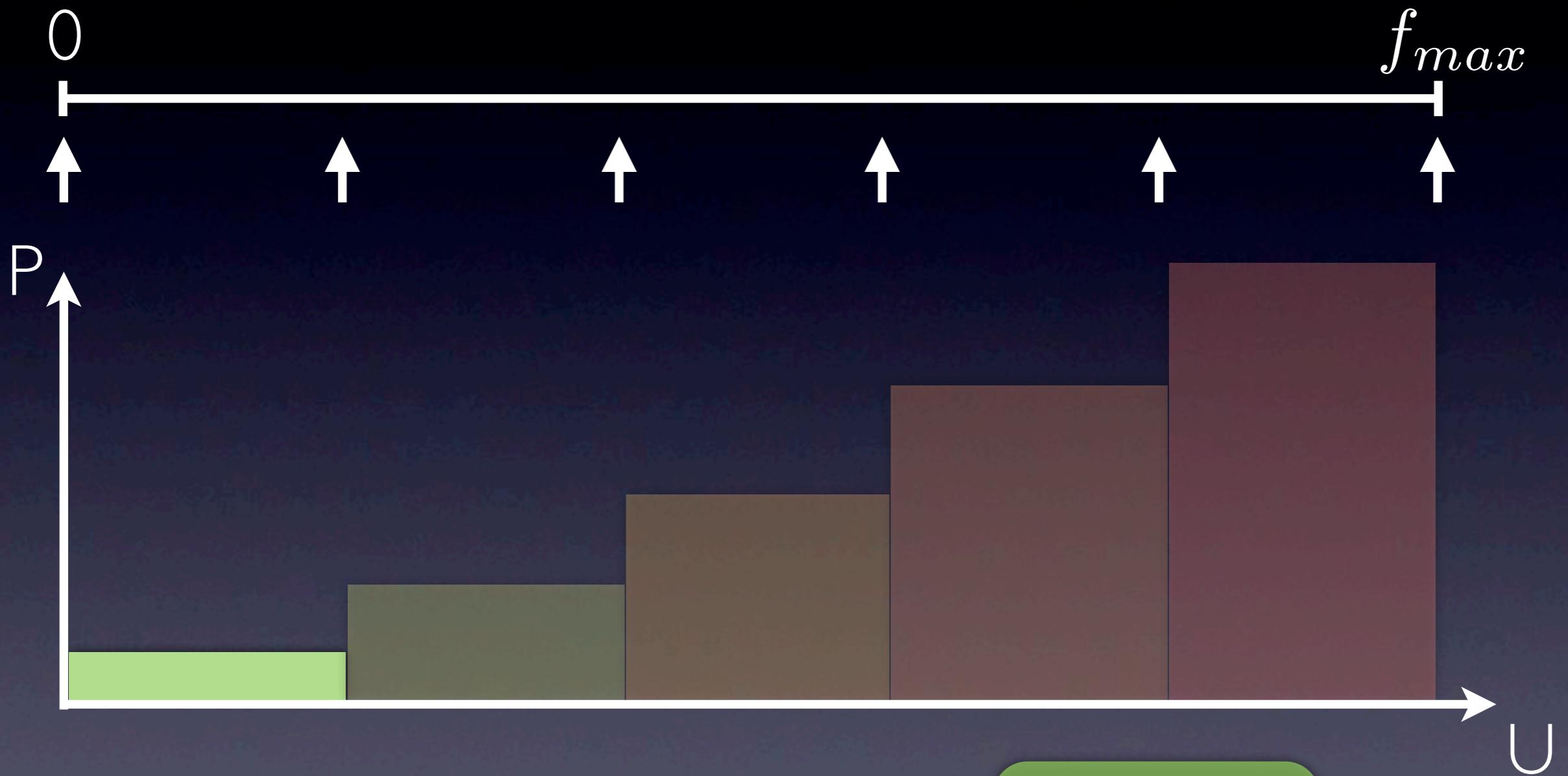


Task i is the only task in the system

$$bE_i^l = (t_1 - t_0)c_1 \frac{U_i}{\kappa_l} (\kappa_l f_{max})^\omega$$



Minimum Contribution

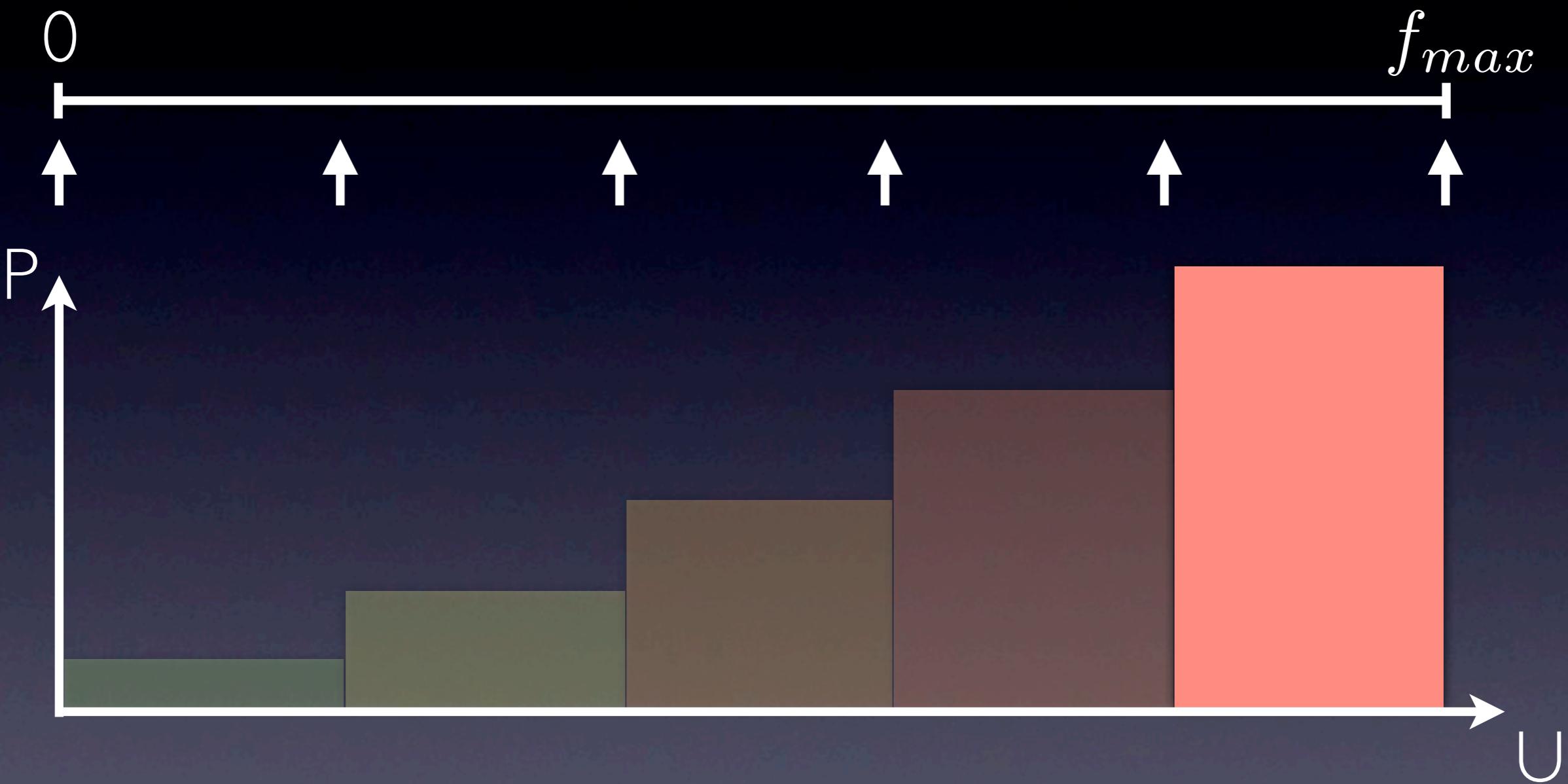


Task i is the only task in the system $\kappa_{l-1} < U_i \leq \kappa_l$

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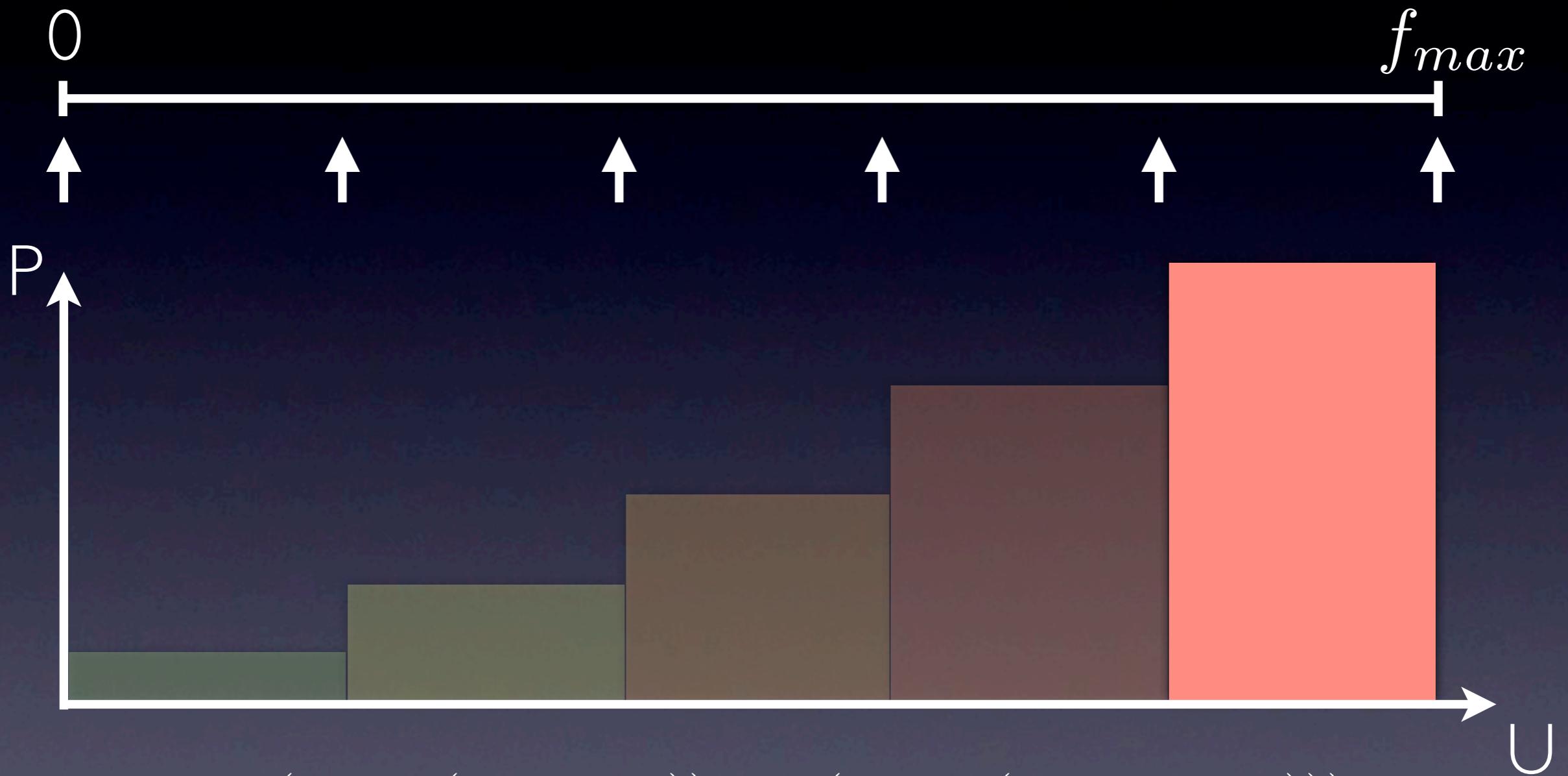


Maximum Contribution





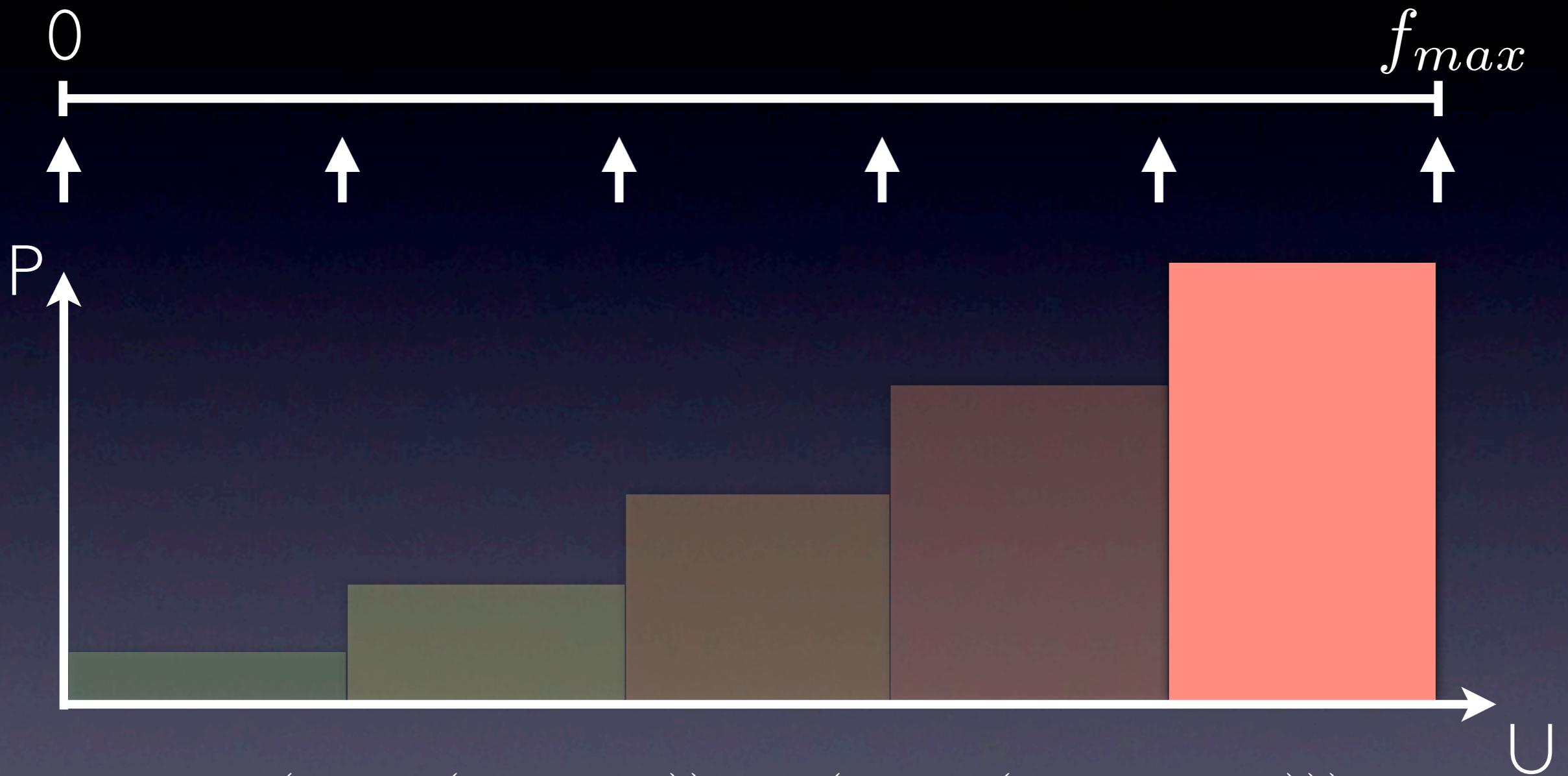
Maximum Contribution



$$E(1, \min(\kappa + U_i, 1)) - E(\kappa, \min(\kappa_{u-1}, \kappa_{m-2})))$$



Maximum Contribution

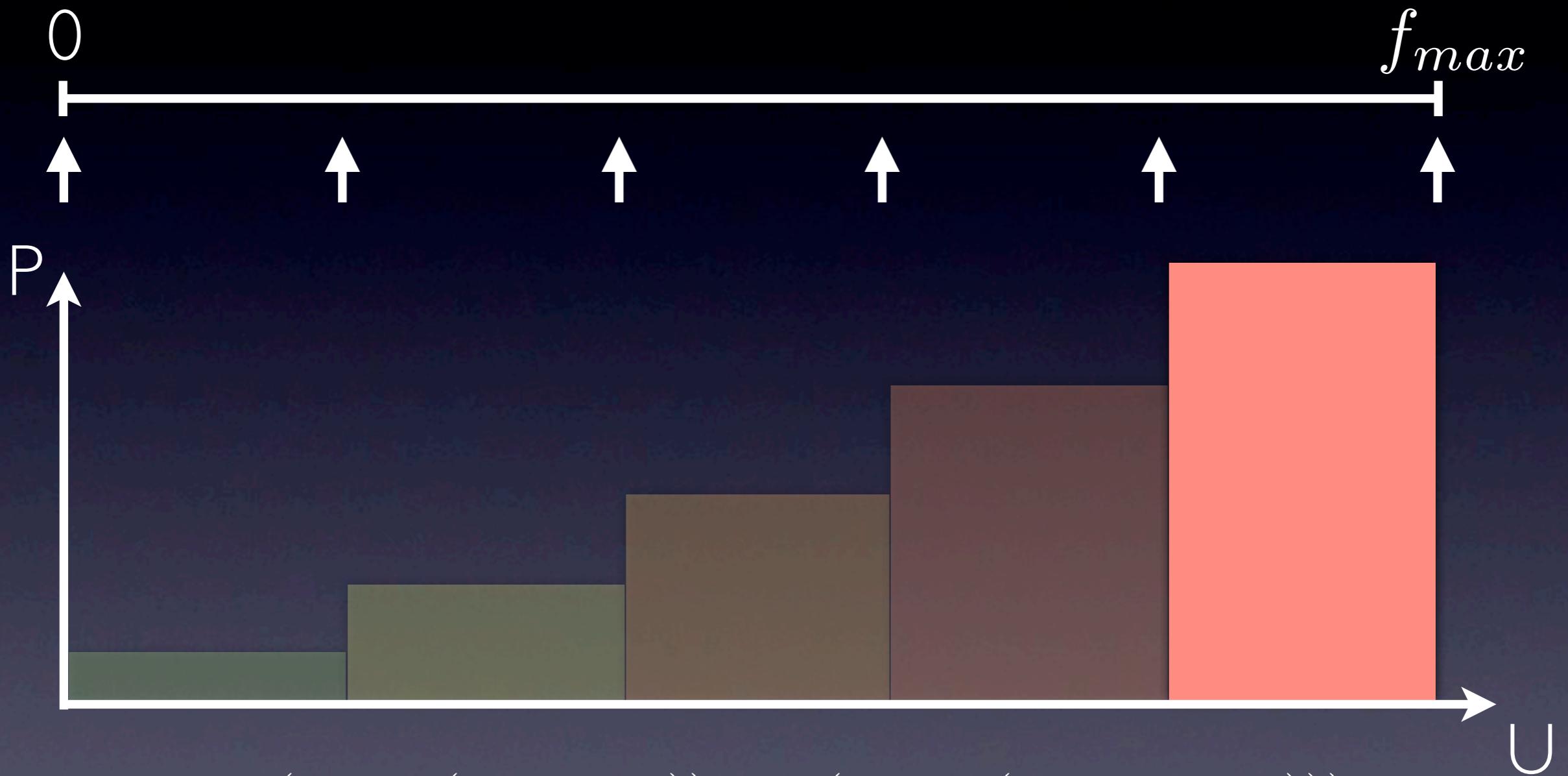


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Maximum Contribution

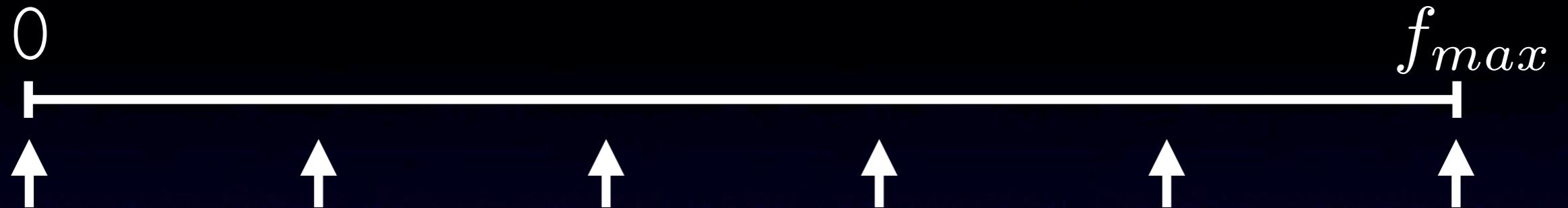


$$E(1, \min(\kappa + U_i, 1)) - E(\kappa, \min(\kappa_{u-1}, \kappa_{m-2})))$$

$$\kappa = \min(\kappa_u, \kappa_{m-1})$$
$$\kappa_{u-1} < 1 - U_i \leq \kappa_u$$



Discrete Frequencies - Bounds



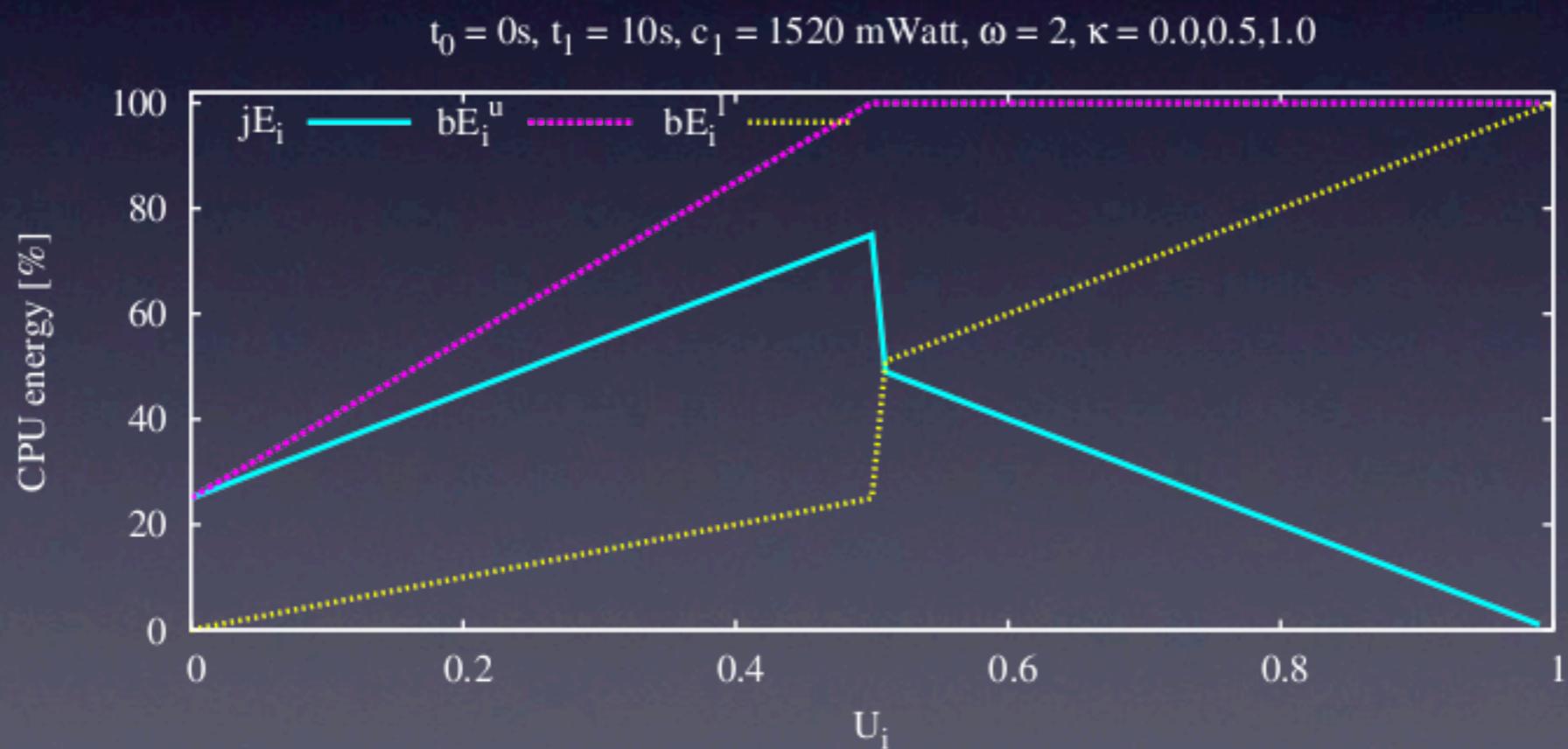
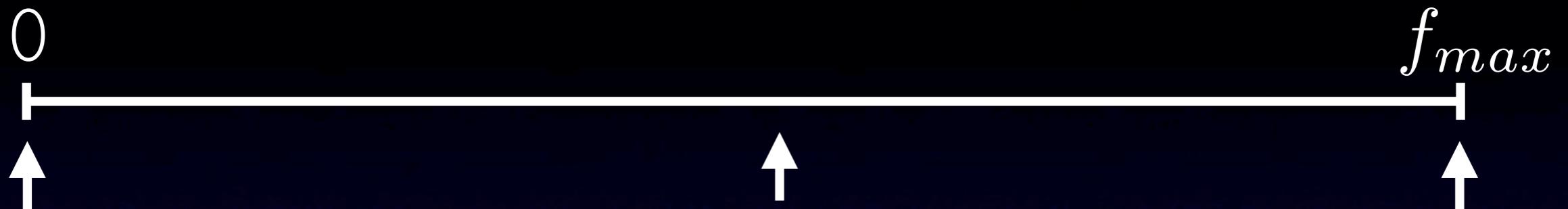
$$bE_i^u = (t_1 - t_0)c_1 f_{max}^\omega (\min(\kappa + U_i, 1)$$

$$-\kappa^\omega \max\left(1 - \frac{U_i}{\kappa}, \min(\kappa_{u-1}, \kappa_{m-2})\right))$$

$$bE_i^l = (t_1 - t_0)c_1 \frac{U_i}{\kappa_l} (\kappa_l f_{max})^\omega$$

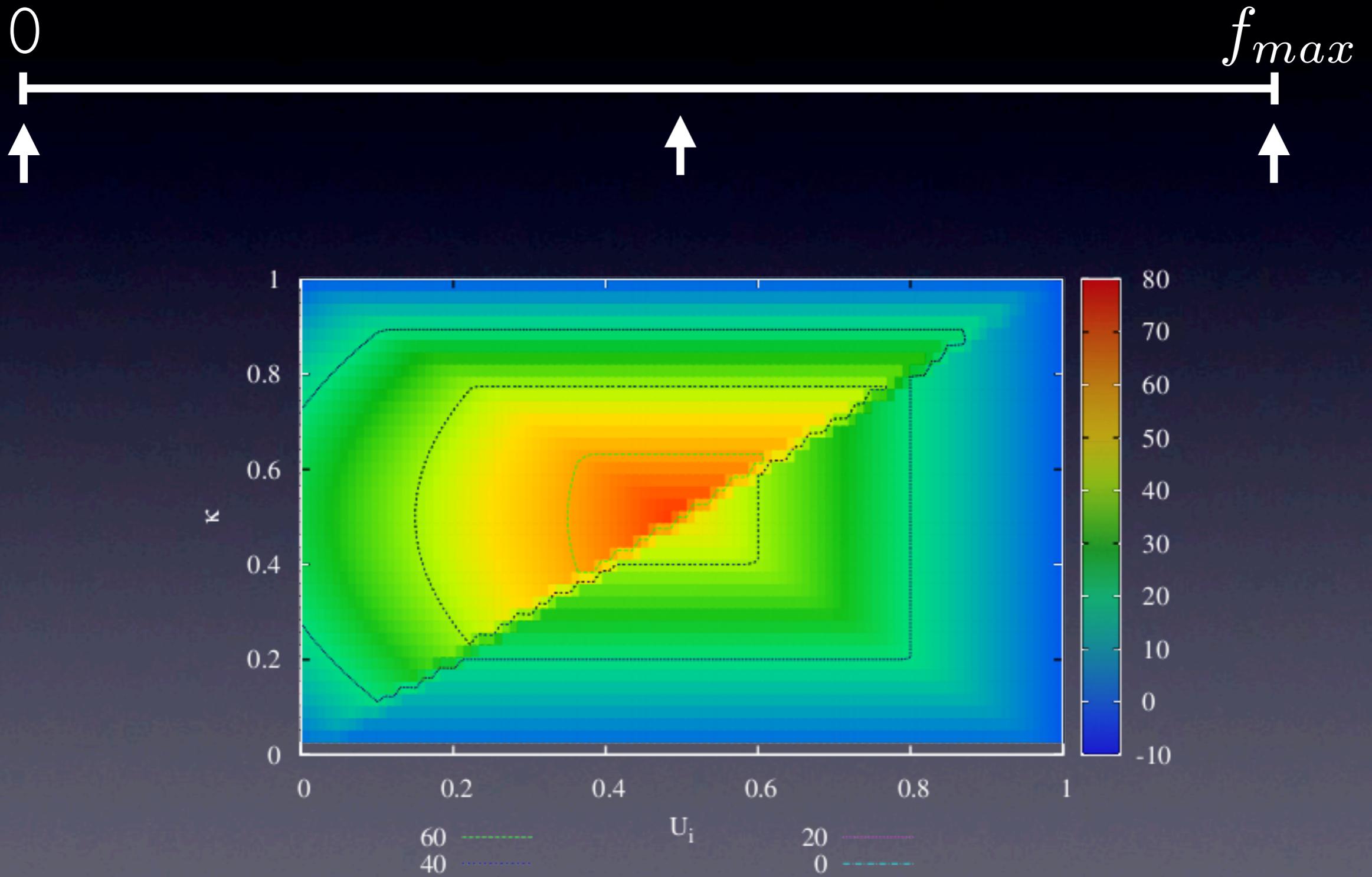


3 discrete frequencies - bounds



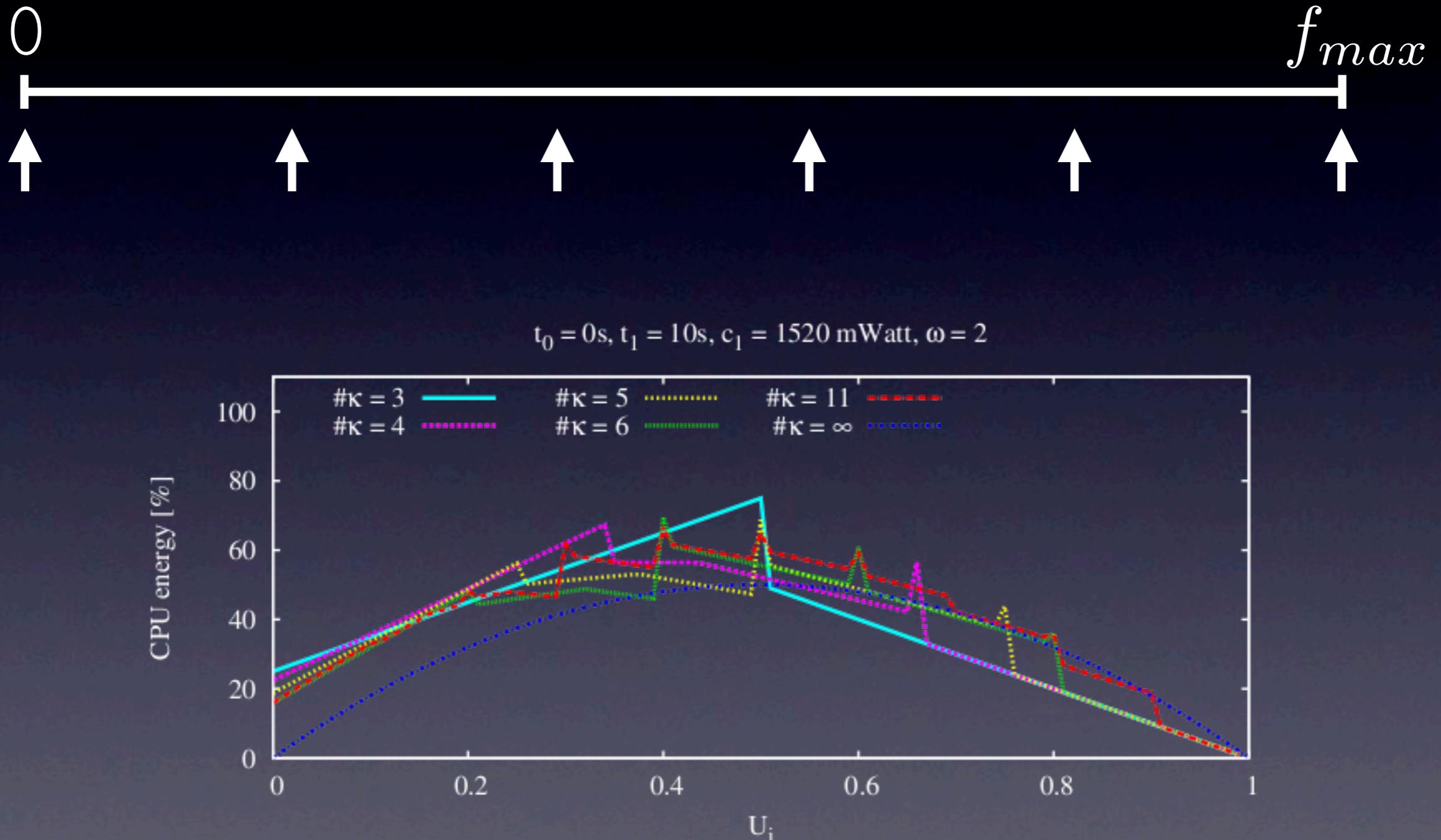


3 discrete frequencies - jitter





Discrete Frequencies - Jitter





Cost of power isolation



Cost of power isolation

Difference between the optimal and actual power consumption



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Optimal is achieved with infinite frequency levels



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The cost of power isolation depends on

- the sum of task utilizations
- the utilization of the considered task
- the number of available frequency levels
- the distribution of the frequency levels in the interval $[0, f_{\max}]$



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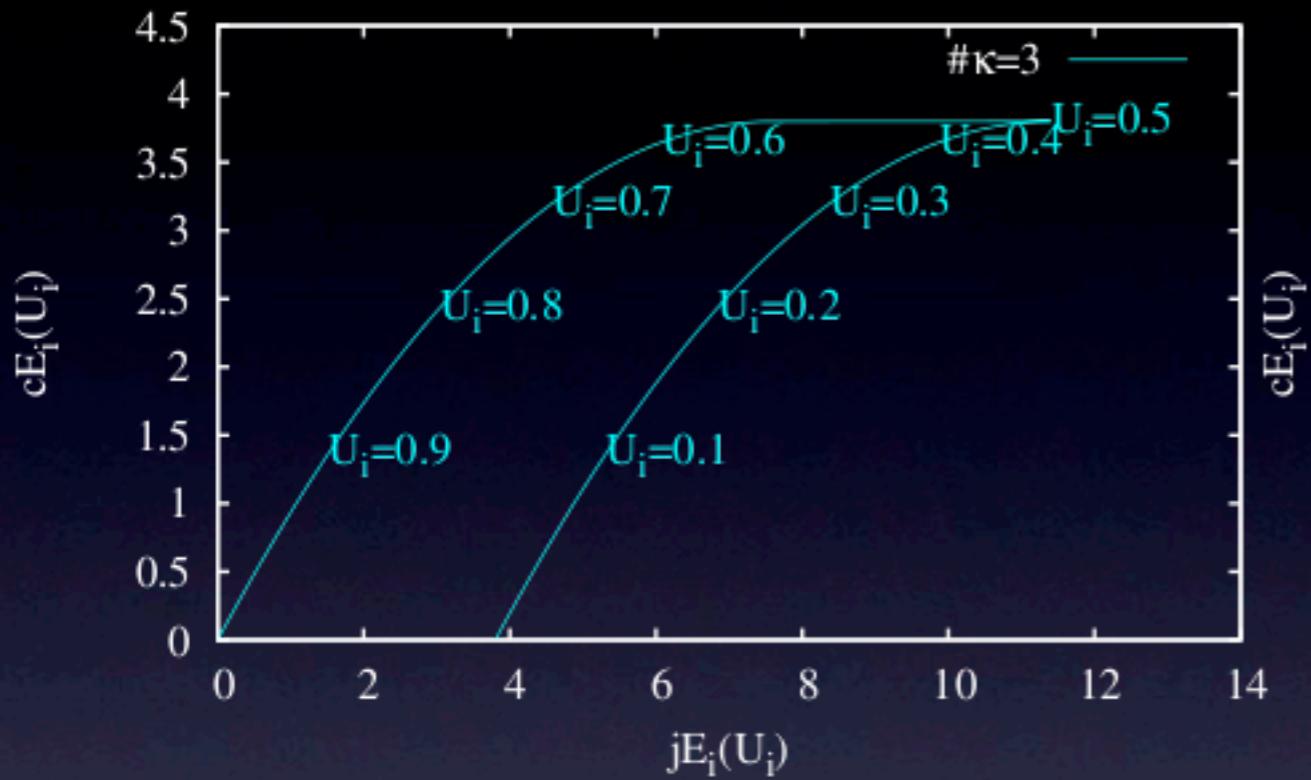
- the sum of task utilizations
- the utilization of the considered task
- the number of available frequency levels
- the distribution of the frequency levels in the interval $[0, f_{\max}]$

$$cE_i = (t_1 - t_0)c_1 f_{\max}^{\omega} U_i (1 - U_i^{\omega-1})$$

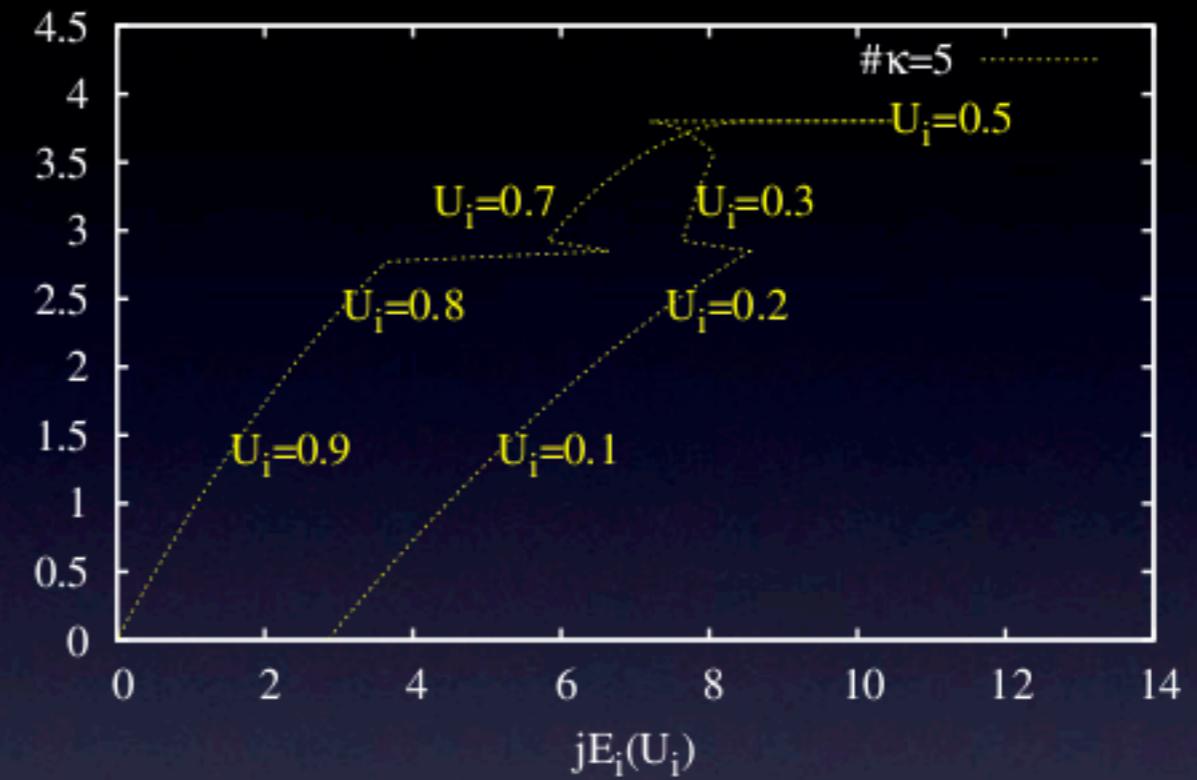


Cost of power isolation

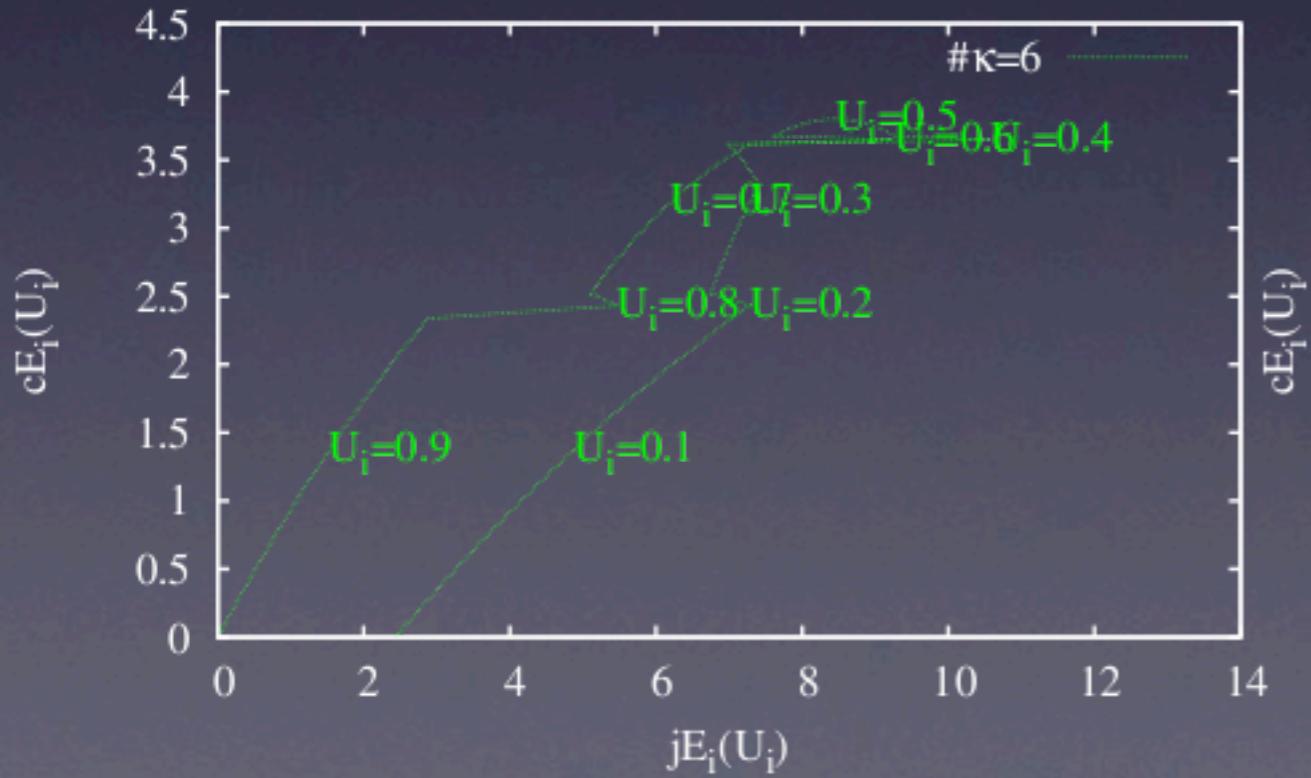
$t_0 = 0s, t_1 = 10s, c_1 = 1520 \text{ mWatt}, \omega = 2$



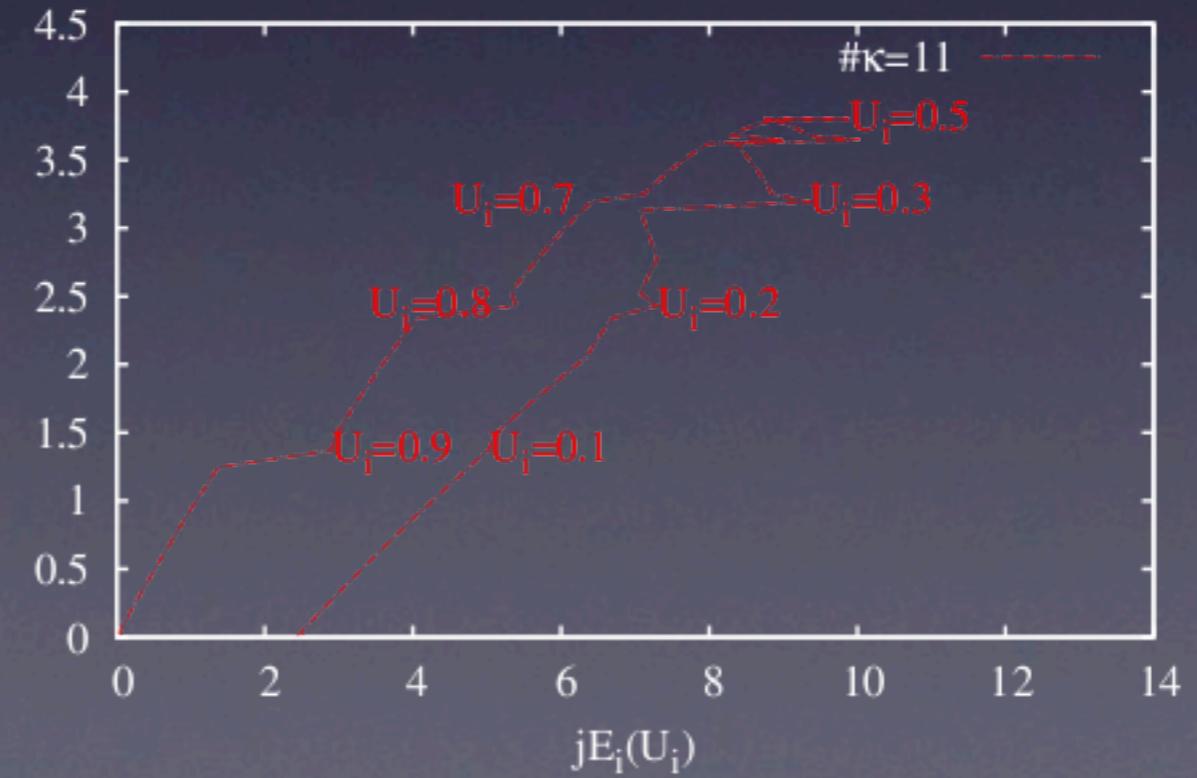
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Conclusion



Conclusion

Lower and upper bounds on the individual power consumption



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Quality of power isolation



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Full temporal [Craciunas12], spatial [Craciunas08], and power isolation of tasks



Conclusion

Lower and upper bounds on the individual power consumption

Quality of power isolation

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Full temporal [Craciunas12], spatial [Craciunas08], and power isolation of tasks

The key insight is that there appears to be a fundamental trade-off between quality and cost of time, space, and power isolation

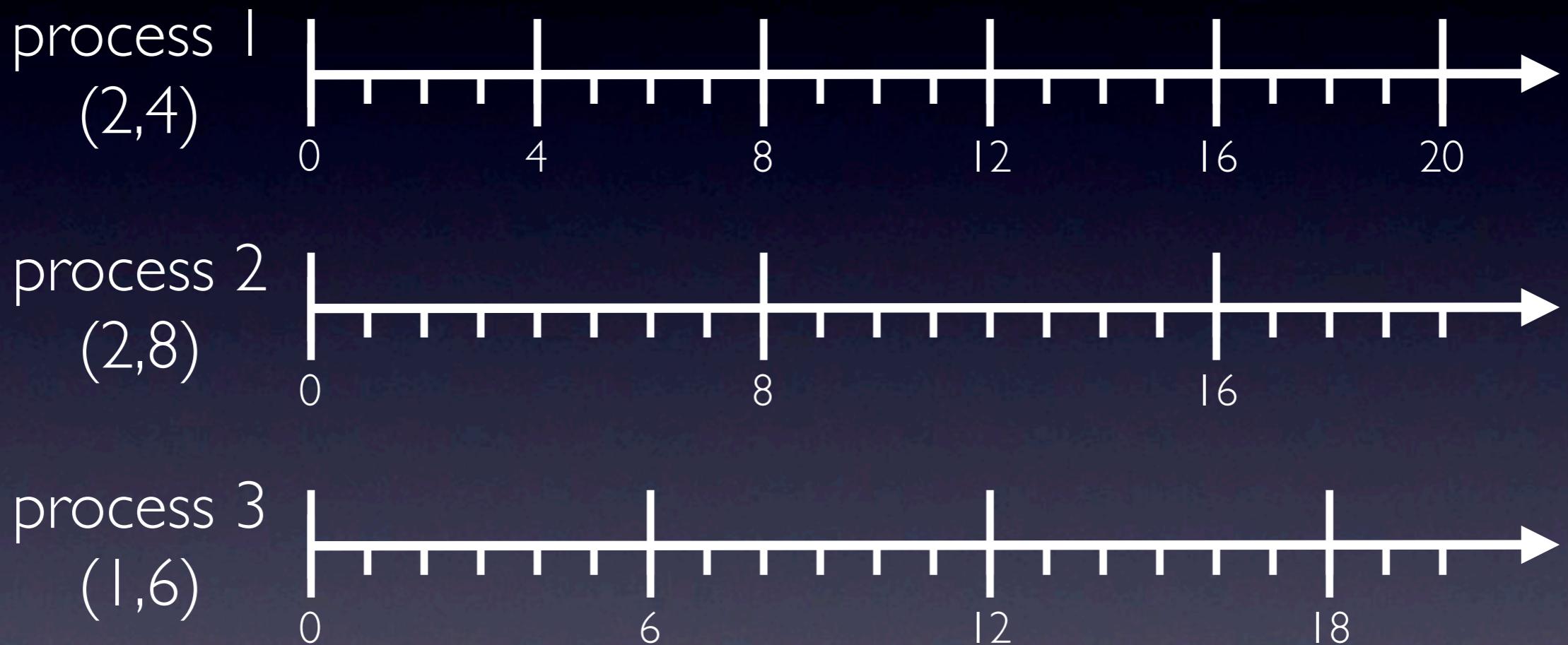


Thank you

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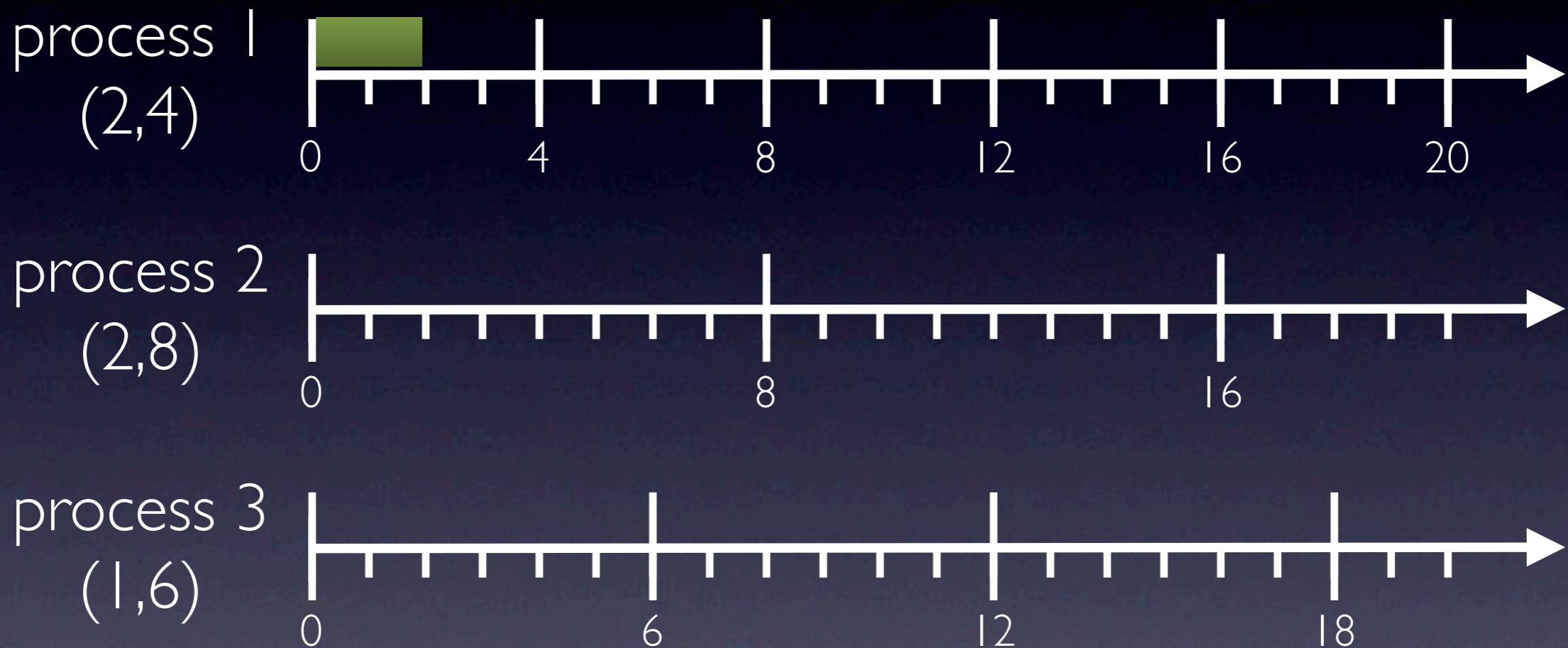
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[Liu and Layland73]



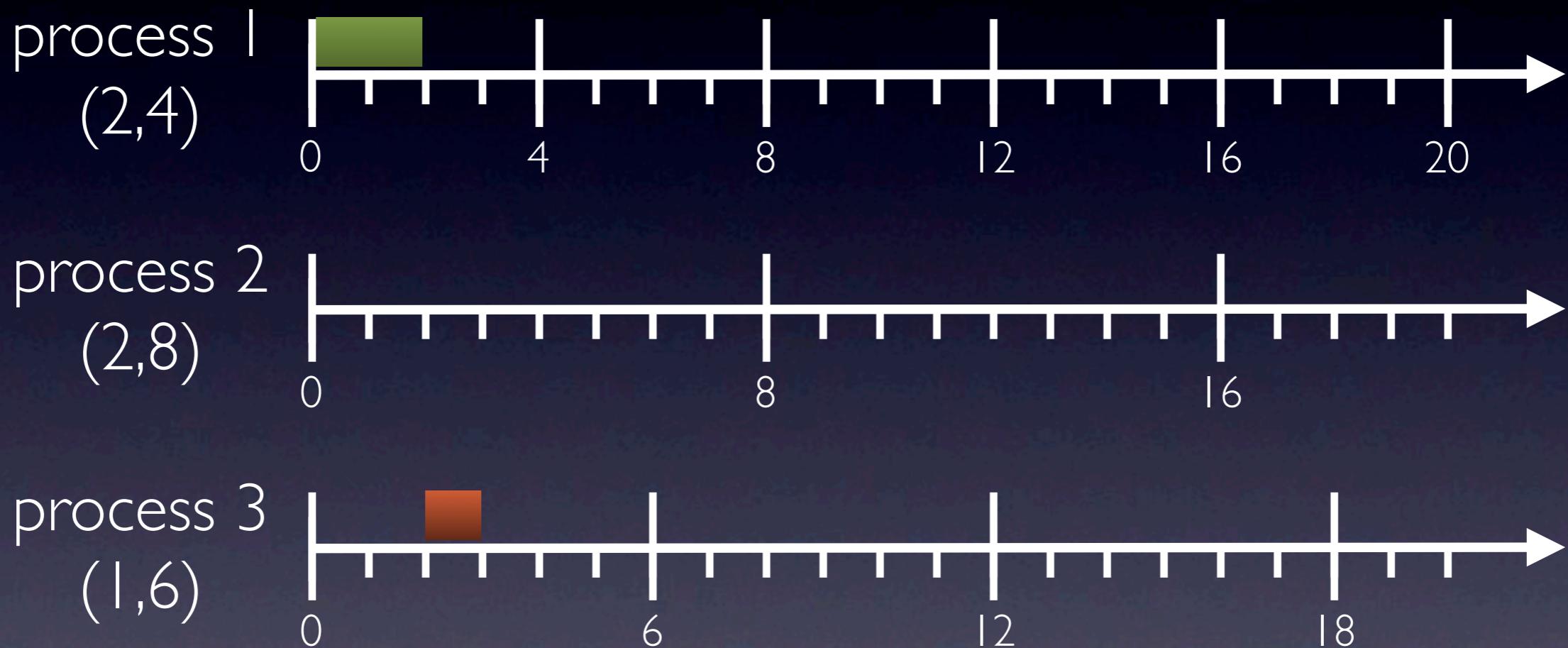
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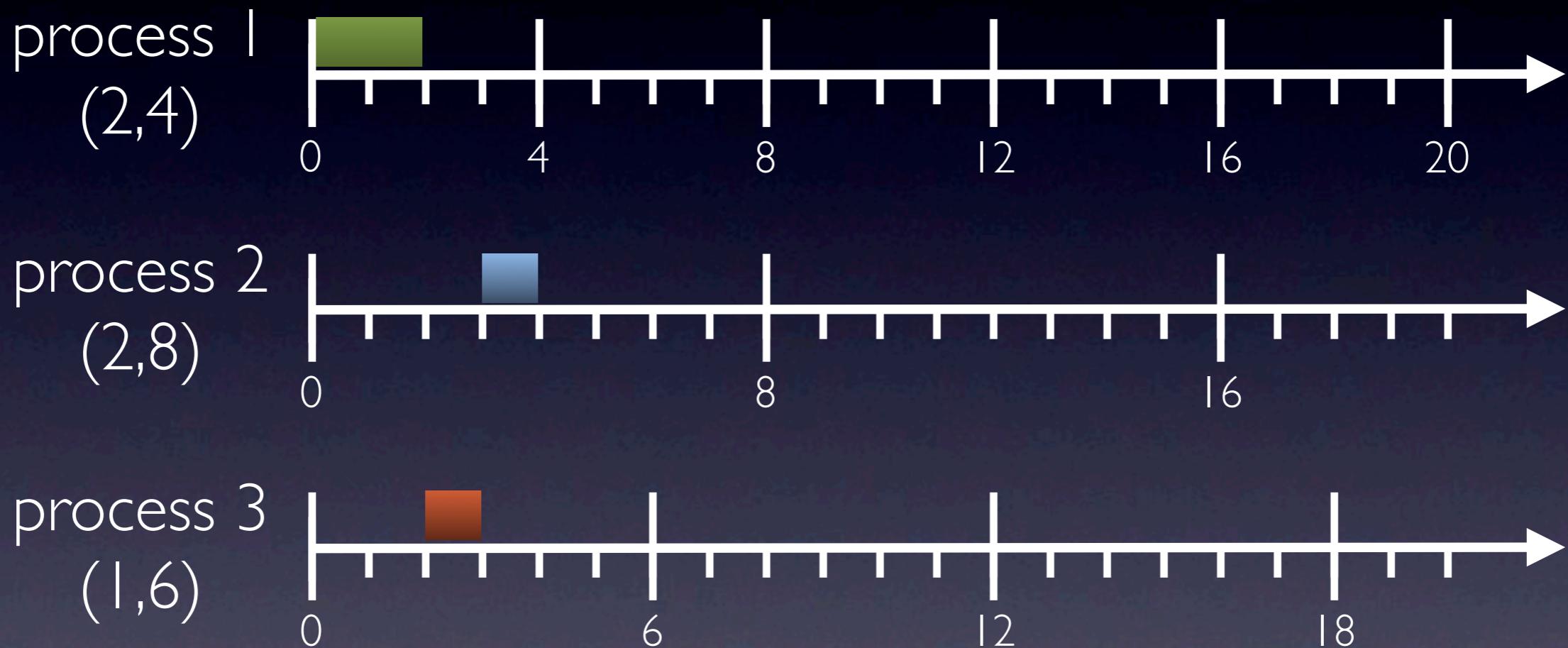
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[Liu and Layland73]



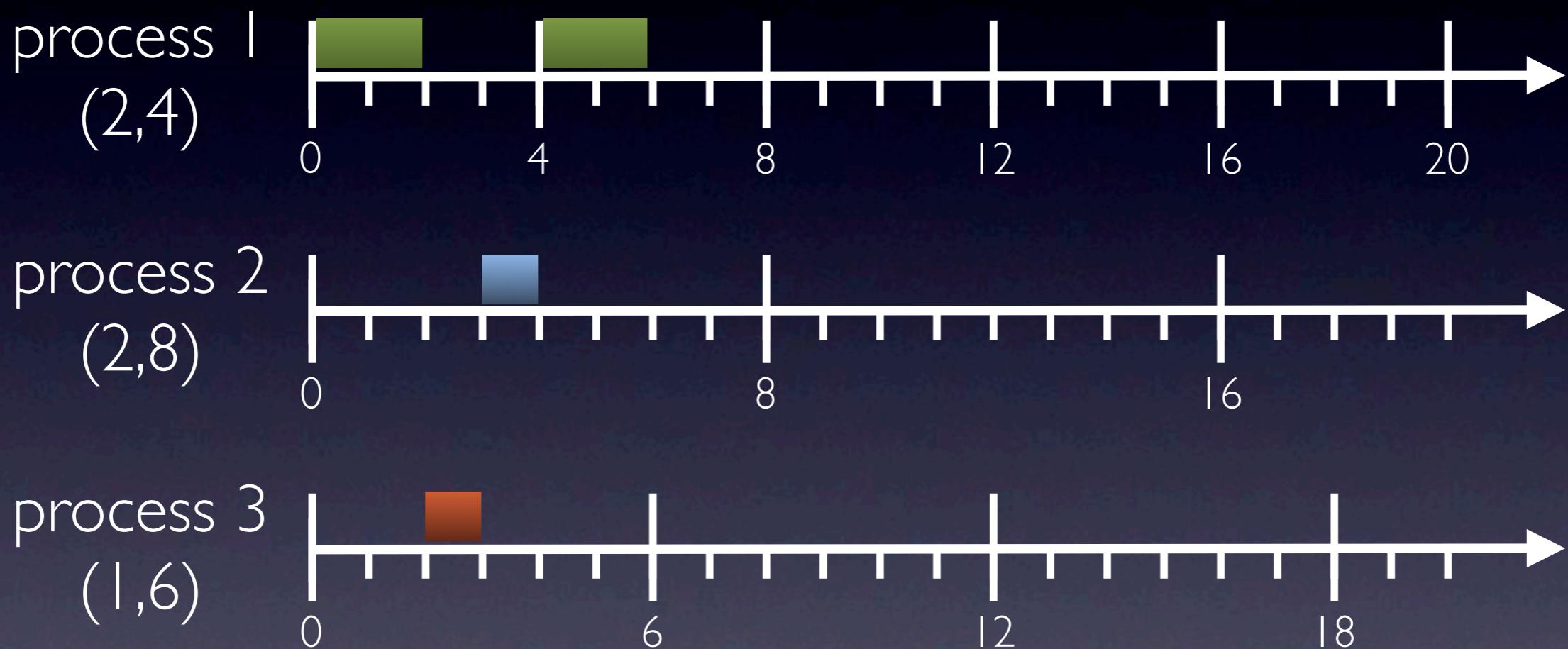
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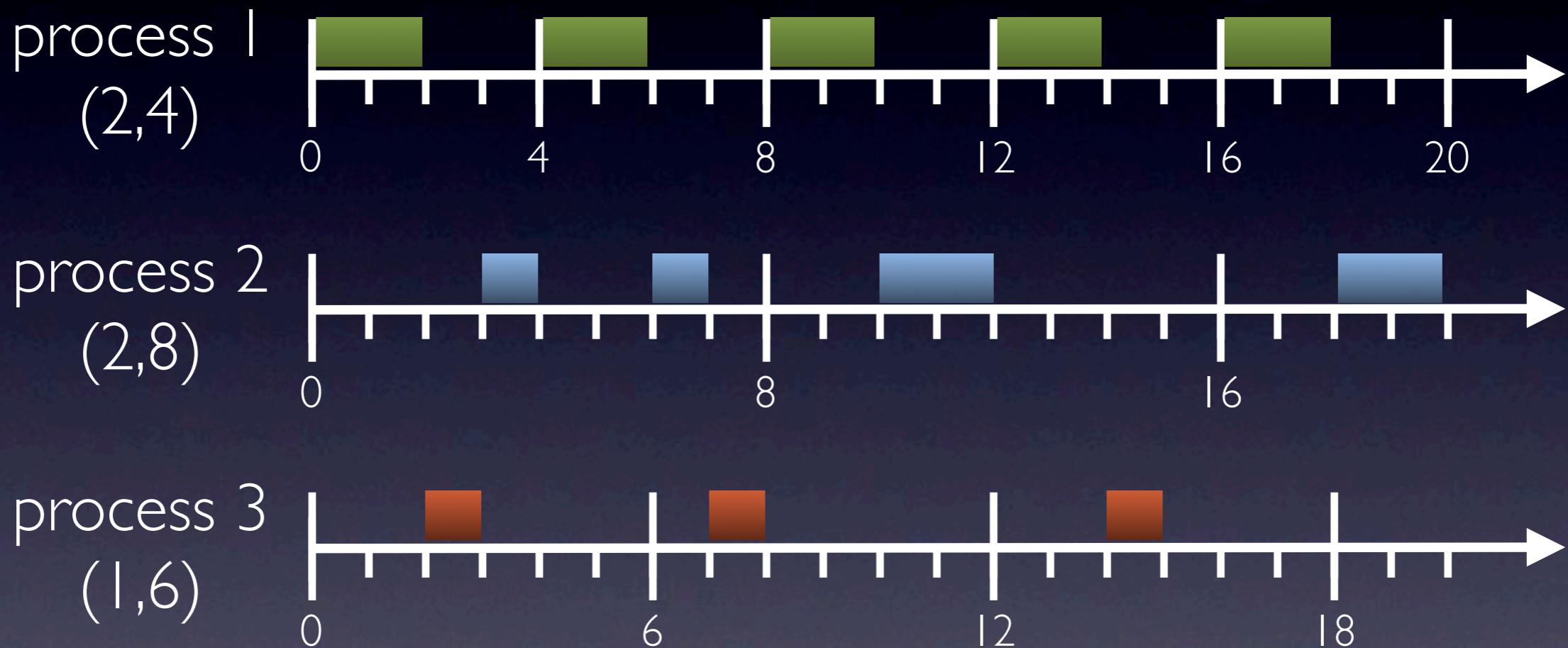
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