Package 'Homework3'

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Type Package
Title Homework 3 (bayesian computing) for Biostat778
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Description Rejection sampling, importance sampling and hybrid gibbs
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does importance sampling
Author(s)
Stephen Cristiano

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Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.
## The function is currently defined as
function (beta, lower, upper)
    importance <- function(beta, sigma) {</pre>
        n <- length(beta)</pre>
        hnorm <- function(N, sigma) {</pre>
            replicate(N, qnorm(0.5 * (1 + runif(1)), 0, sqrt(pi/2) *
                 sigma))
        }
        ldhnorm <- function(x, sigma) {</pre>
             d \leftarrow ifelse(x < 0, -Inf, log(2) + dnorm(x, 0, sqrt(pi/2) *
                 sigma, log = TRUE))
             return(d)
        }
        lw <- function(x) beta - ldhnorm(beta, sigma)</pre>
        U <- hnorm(1000, sigma)
        lps \leftarrow lw(U)
        lps \leftarrow lps - max(lps)
        I <- mean(exp(lps) * U)/mean(exp(lps))</pre>
        return(I)
    }
    sigma <- seq(lower, upper, length = 50)</pre>
    postmeans <- sapply(sigma, function(x) importance(beta, x))</pre>
    plot(sigma, postmeans, xlab = "Sigma", ylab = "Posterior mean estimate",
        type = "1", main = "Importance sampling")
  }
```

postpollution

Hierarchical gibbs sampling with metropolis step

Description

hybrid gibbs

Author(s)

Stephen Cristiano

Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (y, x, g, N = 10000, burn = 1000)
{
    tn <- max(g)
    lpost.beta <- function(y, x, alpha, beta, mu, tau2) {</pre>
```

postsample 3

```
mu.i \leftarrow exp(alpha + beta * x)
    -sum(mu.i) + sum(y * log(mu.i)) - 1/(2 * tau2) * (beta -
        mu)^2
lpost.alpha <- function(y, x, alpha, beta, sigma2) {</pre>
    mu.i \leftarrow exp(alpha + beta * x)
    -sum(mu.i) + sum(y * log(mu.i)) - 1/(2 * sigma2) * alpha^2
}
a <- b <- c <- d <- 1
A <- 1
beta <- rep(0, tn)
alpha <- rep(0, tn)
mu <- 0
tau2 <- sigma2 <- 1
MU <- TAU <- SIGMA <- rep(NA, N - burn)
delta = 1.5
for (i in 1:N) {
    for (j in 1:tn) {
        x.j \leftarrow x[g == j]
        y.j \leftarrow y[g == j]
        mu.j \leftarrow exp(alpha[j] + beta[j] * x.j)
         alpha.star <- rnorm(1, alpha[j], sqrt(delta))</pre>
         log.a <- lpost.alpha(y.j, x.j, alpha.star, beta[j],</pre>
             sigma2)
         -lpost.alpha(y.j, x.j, alpha[j], beta[j], sigma2)
         if (log(runif(1)) < log.a) {</pre>
             alpha[j] <- alpha.star</pre>
        beta.star <- rnorm(1, beta[j], sqrt(delta))</pre>
        log.b <- lpost.beta(y.j, x.j, alpha[j], beta.star,</pre>
             mu, tau2)
         -lpost.beta(y.j, x.j, alpha[j], beta[j], mu, tau2)
         if (log(runif(1)) < log.b) {</pre>
             beta[j] <- beta.star</pre>
         }
    beta.h <- mean(beta)</pre>
    alpha.h <- mean(alpha)</pre>
    mu \leftarrow rnorm(1, tn * beta.h/(1/A + tn), sqrt(1/(1/A +
         tn)))
    tau2 \leftarrow 1/rgamma(1, a + tn/2, b + sum((beta - beta.h)^2)/2 +
         tn/(A * (1/A + tn)) * beta.h^2/2)
    sigma2 <- 1/rgamma(1, c + tn/2, d + sum(alpha^2)/2)
    if (i > burn) {
         MU[i - burn] \leftarrow mu
        TAU[i - burn] \leftarrow tau2
        SIGMA[i - burn] <- sigma2</pre>
}
return(list(MU = MU, TAU = TAU, SIGMA = SIGMA))
```

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Description

Rejection sampling

Author(s)

Stephen Cristiano

Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.
## The function is currently defined as
function (y, N, sigma)
    hnorm <- function(N, sigma) {</pre>
        replicate(N, qnorm(0.5 * (1 + runif(1)), 0, sqrt(pi/2)/sigma))
    if (missing(y))
        y <- c(20.100306, 2.272066, 3.796734, 2.265275, 3.480183)
    if (missing(sigma))
        sigma = 0.5
    if (missing(N))
        N = 1000
    mle <- 1/mean(y)</pre>
    lik.max <- prod(pexp(y, mle))</pre>
    post <- NULL
    while (length(post) < N) {</pre>
        u <- runif(1)
        beta <- hnorm(1, sigma)</pre>
        lik <- prod(pexp(y, beta))</pre>
        if (u <= lik/lik.max)</pre>
            post <- append(post, beta)</pre>
    }
    return(post)
```

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