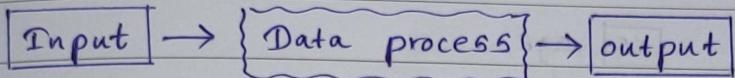


Algorithm and Data Structure.

2022.10.05.

concept of computing



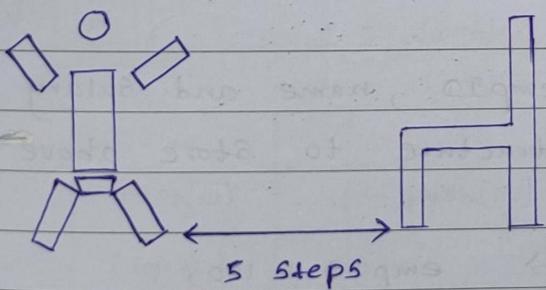
Comp computer program

Instructions + Data → Data Structure / Variable arrays.

Algorithms

- Data Structures,
- * It's a way of storing data or it's a memory arrangement.
- Algorithm,
- * Set of instructions in particular order is an algorithm.

ex:- give the instructions to 'otto' to sit on the chair.



- | | |
|--------------|---------------|
| 1) Turn left | 6) Walk |
| 2) Walk | 7) Turn Right |
| 3) Walk | 8) Turn Right |
| 4) Walk | 9) Sit |
| 5) Walk | |

Structures in 'C'

Instruction order → time and space.

→ we take 'time' as the main.

- * Structures in C // This is an user defined Data type.
- * Variable, array // This is a pre-defined Data type.

1) Variable

In a variable we can add only one data type.

ex:- int age; age.

↑	↑
DT	VN

2) Structure. (struct) ← keyword / structure tag.

```
Struct employee {  
    int age;  
    float salary;  
};
```

- we can store variables under 'struct'.
- can add multiple components in different data types.
- 'struct' is a user define data type it's a complex data structure.
- we can store multiple variables

3) array.

char arr[3]; T O M

0	1	2
---	---	---

- a) Assume we need to store empID, name and salary on each employee. Declare a structure to store above

```
Struct emp {  
    int empID;  
    char name[20];  
    float salary;  
};
```

e₁, e₂, ..;

↑

method 1

e₁ → empID = 100;
e₂ → empID = 200;

```
Struct employee {  
    int empID;  
    char name[50];  
    float salary;  
};
```

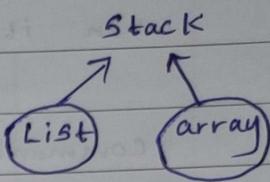
Struct employee emp1, emp2;

↑
method 2

Stack data Structure.

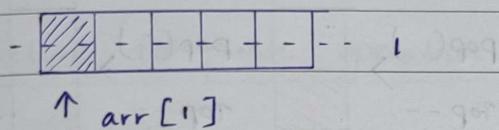
1) Stack (LIFO)

Data Structure.



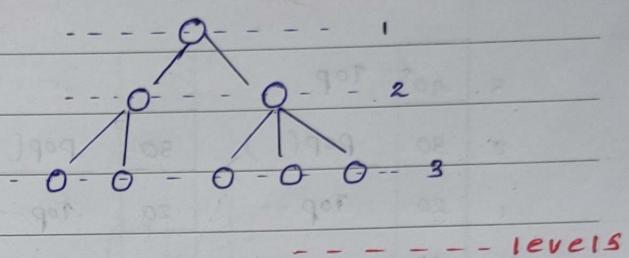
Linear

(Data allocate sequentially | one after other, It's in the same level)



non- Linear

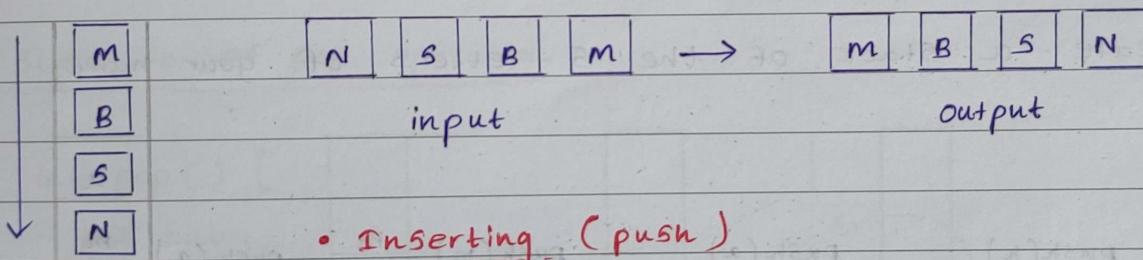
(have many levels)



* A stack is known as a data set.

* A stack can made by An array or a list.

* Stack method \rightarrow first in last out (LIFO)



Inserting - (push)

Ex:- 3							
2	$\text{push}(10)$ $(\text{top}++)$		$\text{push}(20)$		$\text{push}(30)$ $20 \leftarrow \text{top}(1)$	$30 \leftarrow \text{top}(2)$ $30 \leftarrow \text{push}(40)$	$40 \leftarrow \text{top}(3)$
1							20
0		$10 \leftarrow \text{top}(0)$		10	10		10
initial diagram		0	1	2	3		
top (-1)	arr	$10, 20, 30, 40$					

```
int top; print '0' or '1' or '2' or '3'  
arr [top]; '10' or '20' or '30' or '40'
```

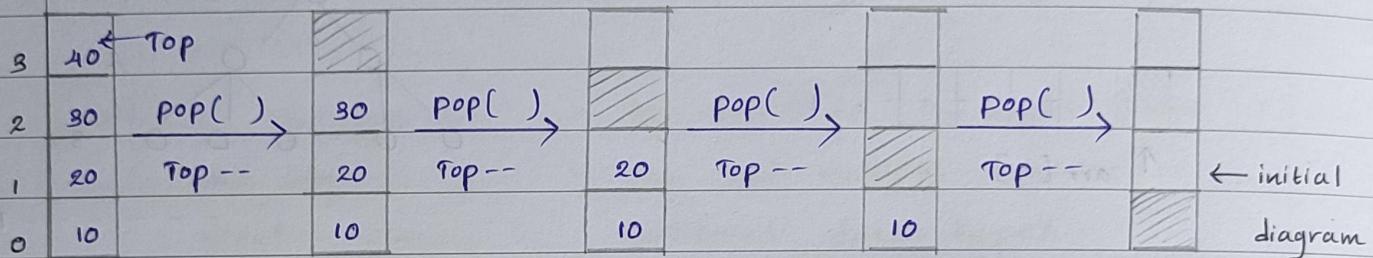
* Top is always an index.

* Inside the stack it is $0, 1, 2, 3, \dots$ ↑ ↓
 When it's outside the stack $\dots, -3, -2, -1$

command , insert \rightarrow push();

delete \leftarrow pop();

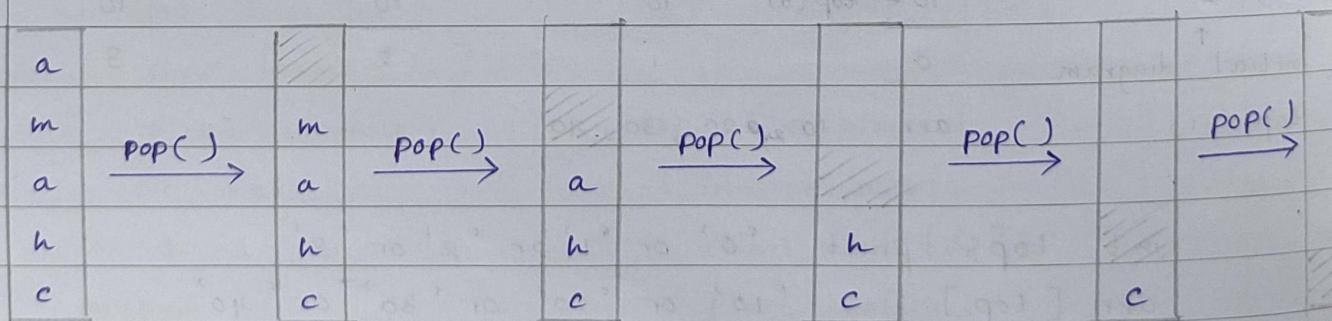
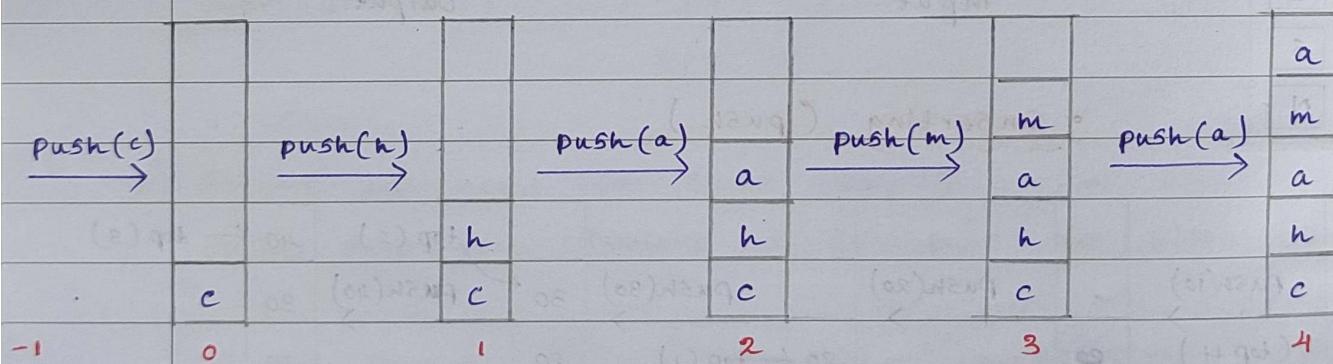
deleting (pop)



* pop() will remove the top most element.

* we cannot Delete values 40 isn't visible.

Ex:- create a stack of the 5 letters of your name.



> Stack Structure declaration.

```
# define size 6
```

```
struct Stack {
```

```
    int arr [ six ] ;
```

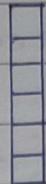
Structure arr[]

```
    int top ;
```

st. top

```
} st ;
```

Structure variable.



> Structure for push operation.

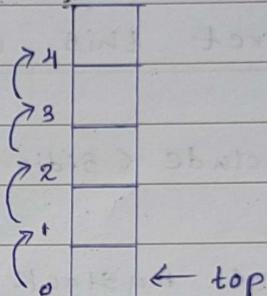
```
void push ( int element ) {
```

```
    st. top ++;
```

```
    st. arr [ st. top ] = elem;
```

```
}
```

normally in 'C' arr [top] = 10;



> Structure of pop operation

```
int pop () {
```

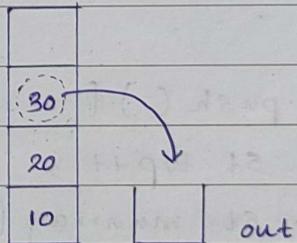
```
    int out ;
```

```
    out = st. arr [ st. top ] ;
```

```
    st. top -- ;
```

```
    return out ;
```

```
}
```



18. 10. 2022

* Array have random access variables . Struct don't have .

Array (RA)

↓

stack (RA)

> check for empty and full stack.

```
int stempty()
{
    if (st.top == -1)
        return 1;
    else
        return 0;
}
```

```
int stfull()
{
    if (st.top >= size-1)
        return 1;
    else
        return 0;
}
```

(a) correct this code.

```
#include <stdio.h>
```

```
struct mystack {
    int myarray[5];
    int top = -1;
} st;
```

int top (we don't declare element here like int top = -1;)

- void push() { void push(int element) need to add element.

st.top++;

- st.myarray[top] = ele; st.myarray[st.top] = ele;

printf ("Item Added to index %d \n", st.top);

}

- int pop(int ele) {

int out = myarray[st.top];

printf ("Popped out the item at index %d ", st.top);

} → next page.

```
int main () {
```

- st.top = -1;

push (10);

push (20);

push (30);

pop();

return 0;

}

```
int pop() {
```

int out;

out = myarray [st.top];

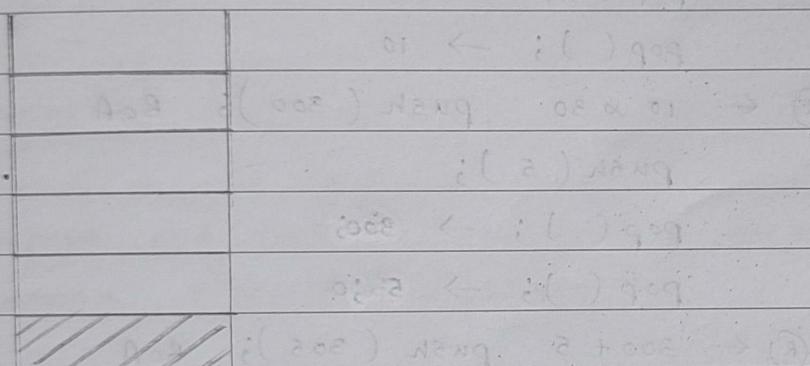
st.top --;

printf ("..... Statement")

return out;

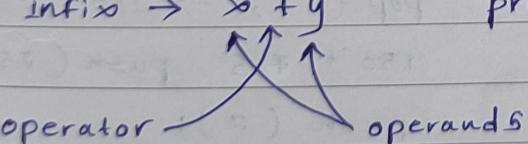
}

- * main method is alone; and all the declaration are on outside the main.



- * Stack → Evaluate postfix notifications.

infix → $x + y$



prefix $+xy$

postfix $xy+$

ex- 10 20 5 (+) (postfix)

- * In this case, these kind of equation is also solved using a stack. There are few steps for that process.

IF the operand comes first

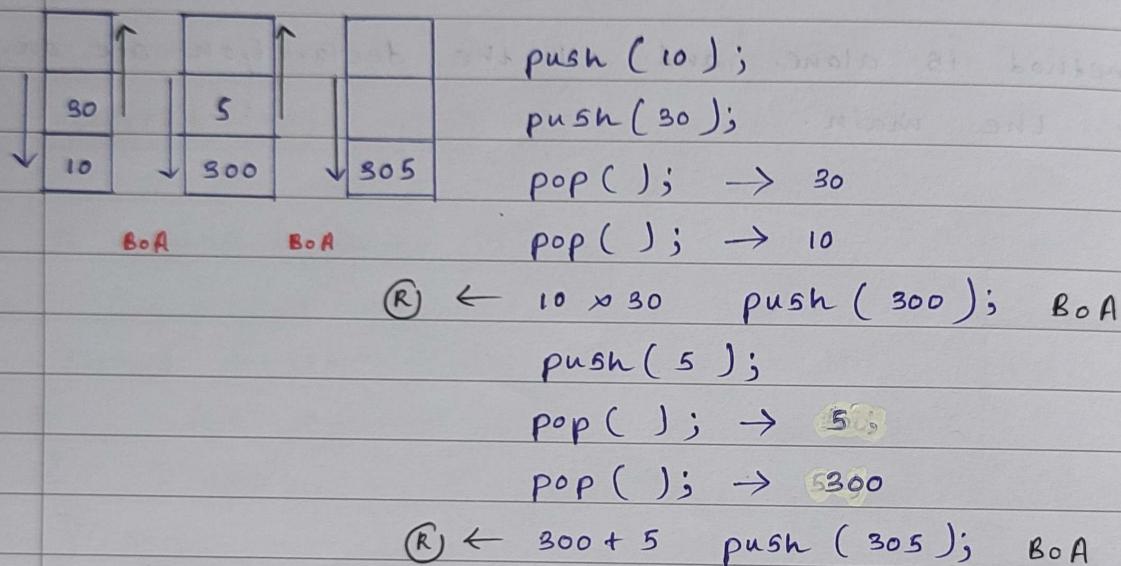
push() it to the stack.

ELSE IF the operator comes .

$\text{pop}() \rightarrow A$ } pop 2 times.
 $\text{pop}() \rightarrow B$ }

AND BoA

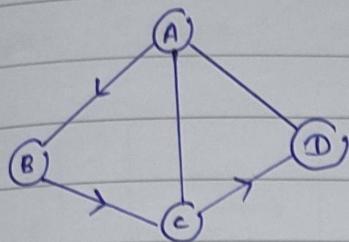
AFTER push(BoA)



ex:- 100 200 + 2 | 5 * #

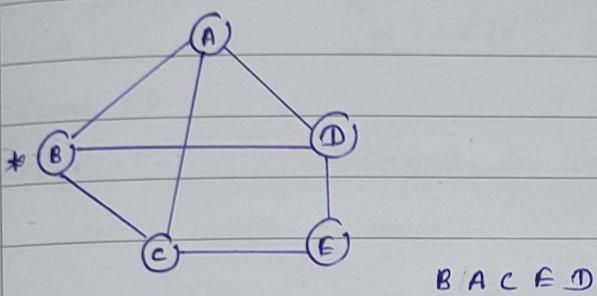
$\text{push}(100);$ $\text{pop}(); \rightarrow 150$
 $\text{push}(200);$ $150 * 5 \quad \text{push}(\#50); \quad \text{BoA}$
 $\text{pop}(); \rightarrow 200$ $\text{push}(\#);$
 $\text{pop}(); \rightarrow 100$ $\text{pop}(); \rightarrow \#$
 $100 + 200 \quad \text{push}(300); \quad \text{BoA}$ $\text{pop}(); \rightarrow 750$
 $\text{push}(2);$ $750 + \# \quad \text{push}(\#5\#); \quad \text{BoA}$
 $\text{pop}(); \rightarrow 2$
 $\text{pop}(); \rightarrow 300$
 $300 | 2 \quad \text{push}(150); \quad \text{BoA}$
 $\text{push}(5);$
 $\text{pop}(); \rightarrow 5$

Depth first Search



A, B, C, D

D
C
B
A



B A C E D

* This is commonly using in graph data structure.

2022.10.26.

Tutorial 1

- Q1) compare and contrast stacks and queues in term of adding, removing, size and emptiness.

Stacks	queues.
use 'push' command to add data. (Inserting)	Inserting element is known as the 'enqueue.' operation
use 'pop' command to remove data. (deleting)	deleting element is known as the 'dequeue'
This structure implements and follows last in first out principle (LIFO)	This structure implements and follow First In First out (FIFO) principle.
Stack is a linear form of data structure.	queue also can refer as a linear form of data structure.
User can delete and insert elements from only one side of a list	In this, a user can insert elements from only one side of the list.

2) void push (int element) {

st. top ++ ;

st. arr [st. top] = element ; }

int main () { push (7);

push (6);

push (3);

push (5);

push (9);

push (0);

}

03) pop () ; → 0

pop () ; → 9

pop () ; → 5

pop () ; → 3

push (2);

04) int st empty ()

{

if (st. top == -1)

return 1;

else

return 0 ;

}

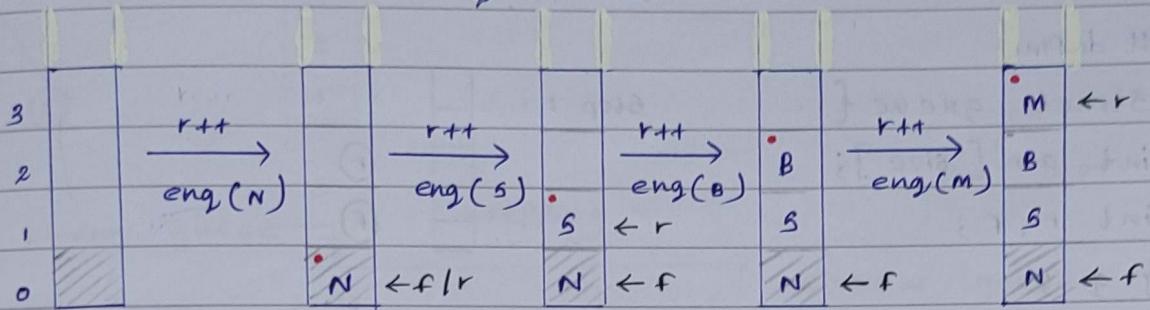
* In the queue data structure , elements are fixed and not moving when the previous element goes out . what is happening here is the 'Front' position is changing according to the relevant element .

Rear → To 'add' elements to the data structure.

Front → To 'remove' elements from the data structure.

queue

Put 'NSBM' into a queue structure.

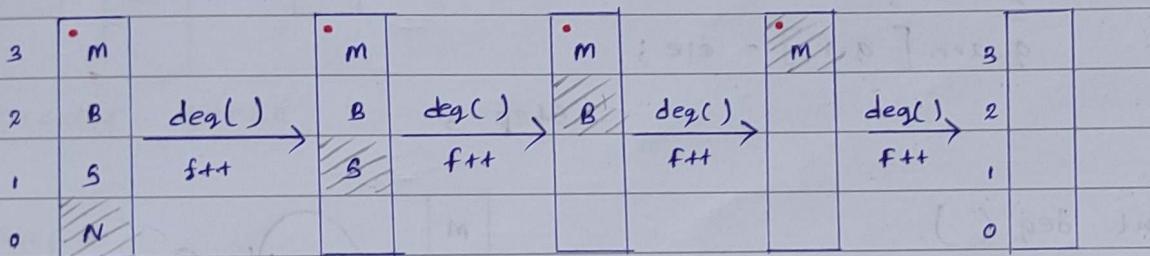


front = 0

rear = -1

enqueue → Insert

dequeue → Delete



front = 0

$f = 1$

$f = 2$

$f = 3$

$f = -1$

rear = 3

$R = 3$

$R = 3$

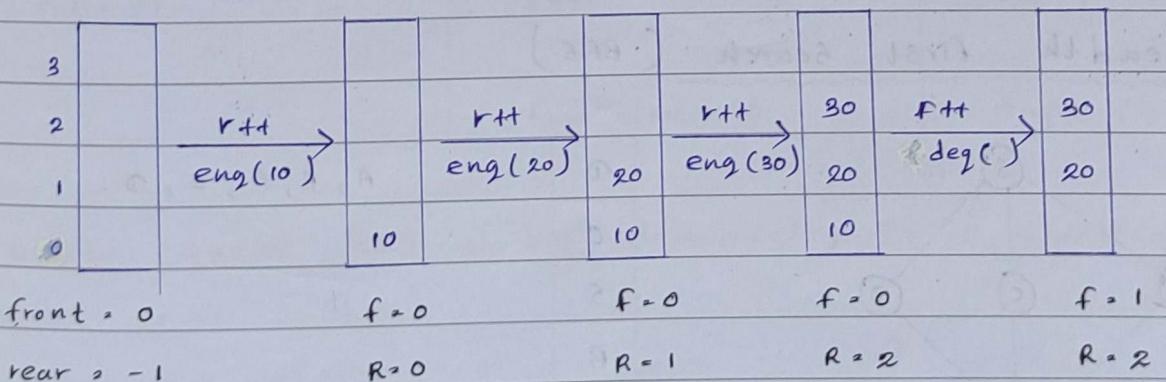
$R = 3$

$R = -1$

} empty

Q) perform these operation and get the final queue.

$Eng(10)$, $Eng(20)$, $Eng(30)$, deg .



front = 0

$f = 0$

$f = 0$

$f = 0$

$f = 1$

rear = -1

$R = 0$

$R = 1$

$R = 2$

$R = 2$

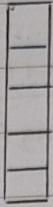
* 'Front' operation won't make any changes to the data structure.

- Q) 1) write a code for a queue of 5 elements
 2) enqueue operation.
 3) dequeue operation.

1) # define

```
struct queue {
    int arr [ size ];
    int r, f;
} q;
```

Step 1



2) void eng (int ele)

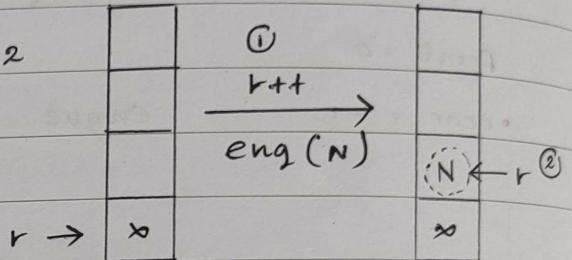
{

q.r++;

q.arr [q.r] = ele;

}

Step 2



Step 3

3) int deg ()

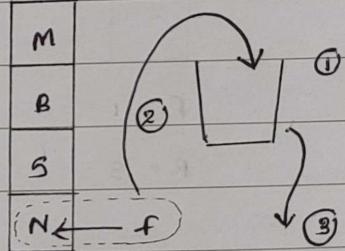
{

int out;

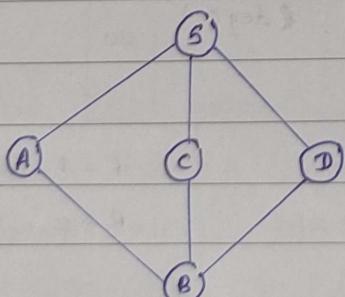
out = q.arr [q.f];

q.f++;

return out;



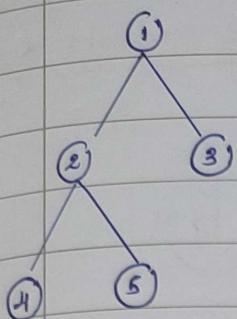
Breadth first search (BFS)



①
C
S
B
A

A, B, S, C, D.

go with an 'And operation'.



5
4
3
2
1

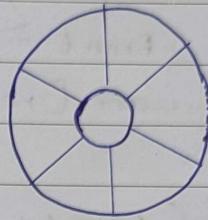
1, 2, 3, 4, 5

Linear queue

wrapping

circular queue.

50	← Rear
40	
30	
20	
10	



→ circular queue.

Step:-

- ① declare all the ② function to perform ③ function to perform elements
- enqueue.

array
 $f = -1$
 $r = -1$

Empty	Full	Full / Few
	Few elements	Empty
		Single.

* Linear queue has a big drawback, It is wasting memory.

> function to perform enque.

#include <stdio.h> ← empty

int arr[5];

int Front = -1;

int Rear = -1;

ll Function to perform enque.

void enque (int x) {

if (front == -1 && rear == -1) {

Front = rear = 0; }

arr [rear] = x; }

else if ((rear + 1) % N == front) {

printf (" queue is full "); }

else { rear = (rear + 1) % N ;

arr [rear] = x; }

> Function to perform deque;

ll Function to perform deque

Void deque () {

if (front == -1 && rear == -1) {

printf (" No elements "); }

else if (rear == front) {

printf (" .d ", arr [front])

to note

Front = -1;

rear = -1;

}

Linear Search.

0	1	2	3	4	5
10	20	30	40	50	60

Search key = 40

$A[0] == SK ? \times$

$A[1] == SK ? \times$

$A[2] == SK ? \times$

$A[3] == SK ? \checkmark$

Algorithm 5

- Search
- Sort
- Recursive
- Linear S.
- binary S.

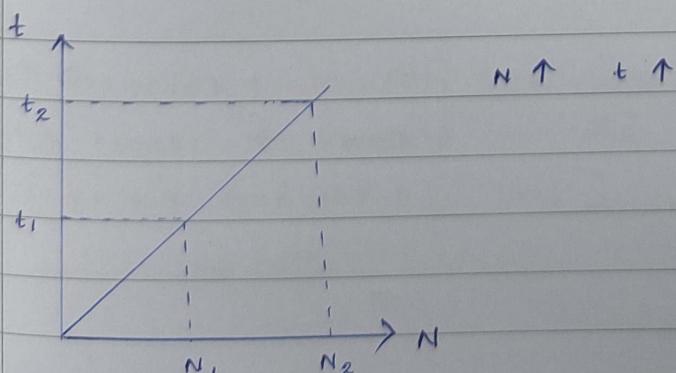
Algorithm 5

* when number of elements are increasing The search time increases. Sort Recursive.

$$\boxed{t \propto N} \uparrow \quad t - \text{time} \quad | \quad N - \text{no. of elements}$$

* we use linear search for smaller data sets. It's not good for larger data sets.

ex:-	case	10	100	1000	N
	Best	0 th , 1 st	0 th , 1 st	0 th , 1 st	0 th → index position 1 st → search
	avg.	4 th , middle	49 th , mid	499 th , mid	E → End NF → Not Found.
	worst	9 th , E/NF	99 th , E/NF	999 th , E/NF	$t_1 < t_2 < t_3$



- Algorithm for Linear Search

81021024

Set Found to false; Set position to -1; Set index to 0

while index < number of elements . and found is false.

if list [Index] is equal to search value

found = true.

position = index

end if

add 1 to index

end while

return position.

←
Linear
Search

```
int 1Search ( int arr[ ] , int BK , int N ){
```

 bool found = false;

 int position = -1;

Index Search → I Search

 int index = 0;

```
        while ( index < N && !found ){
```

 if (arr [index] == BK){

 position = index ;

 found = true ;

}

 index ++ ;

}

 return position ;

}

equal qnd?

{ found == false → True

Found → returns 'false'

{ ! found → not false (True)

for larger data for organized sorted in order sets

exam:- unsorted data set → sorted Data set.

Binary Search

* using for large data sets.

* we input organized, sorted data set in order.

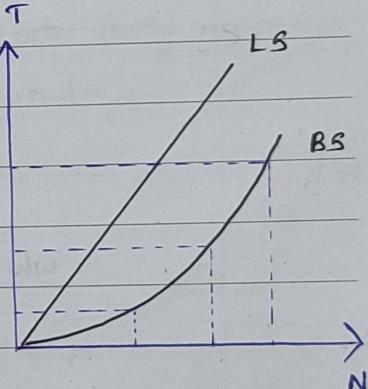
0	1	2	3	4	5
8	10	15	25	35	40

Linear Search example.

2022.11.28.

10	2	15	25	18	30	$SK = 18$
----	---	----	----	----	----	-----------

Index	List[Index]	SK	Found	position.
0	10	18	F	-1
1	2	18	F	-1
2	15	18	F	-1
3	25	18	F	-1
4	18	18	T	4
5	30	-	-	-



Algorithm of binary Search.

Set first index to 0. Set last index to the last Subscript in the array. Set found to false. Set position to -1.

while found is not true and first is less than or equal to last set middle to the Subscript half-way between array [first] and array [last].

If array [middle] equals the desired value .

Set found to true .

Set position to middle .

Else if array [middle] is greater than the desired value .

Set last to middle - 1 .

ELSE

Set first to middle + 1 .

End If .

```
Int bSearch ( int A [ ] , int SK , int N ) {
```

```
    int first = 0 ;
```

```
    int last = N - 1 ;      6 - 1 = 5
```

```
    bool found = false ;
```

```
    int position = -1 ;
```

```
    while ( ! found && first <= last ) {
```

```
        int midI = first + last / 2 ;
```

```
        if ( A [ midI ] == SK ) {
```

```
            found = true ;
```

```
            position = midI ;
```

```
}
```

```
        else if ( A [ midI ] > SK ) {
```

```
            last = midI - 1 ;
```

```
}
```

```
        else {
```

```
            first = mid + 1 ;
```

```
}
```

```
}
```

```
return position ;
```

```
}
```

binary Search

To apply binary Search , array Should be sorted.

6	70
5	60
4	50
3	40
2	30
1	20
0	10

$\rightarrow \text{mid } I$

$$\text{i) } \text{mid } I = \frac{l+1}{2} = \frac{0+6}{2} = 3$$

$$A[\text{mid } I] == \text{SK?}$$

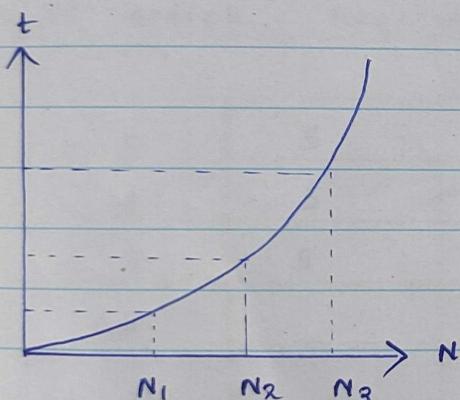
$$40 == 60 \times$$

$$\text{ii) } A[\text{mid } I] > \text{SK} \rightarrow \text{True.}$$

$I = \text{mid } I - 1 \rightarrow \text{Search only lower boundary.}$

[else] iii) Search at the up

$F = \text{mid } + 1 \rightarrow \text{Search only upper boundary.}$



$$t \propto \log x$$

$$\text{i) } 1024 = 2^{10}$$

$$\text{ii) } 100, 2^6 = 64 \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{closest is } 128$$

$$\text{So, } 100 = 2^7$$

	0	1	2	3	4	5
20:-	2	10	15	18	25	30

i)

first	last	mid \lceil	A [mid \lceil]	sk	found	position
0	5	2	15	18	F	-1
3	5	4	25	18	F	-1
3	3	3	18	18	T	3

ii) If search key was = 12,

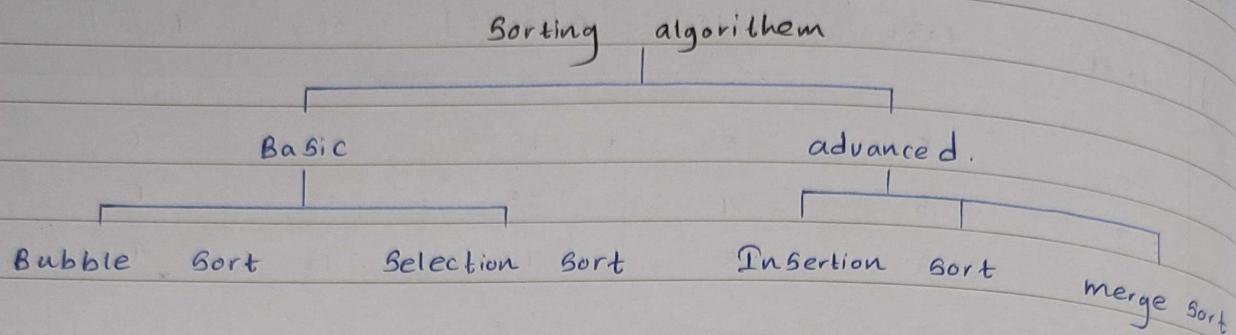
0	5	2	15	12	F	-1
0	1	0	2	12	F	-1
1	1	1	10	12	F	1
2						

iii) If search key was = 35,

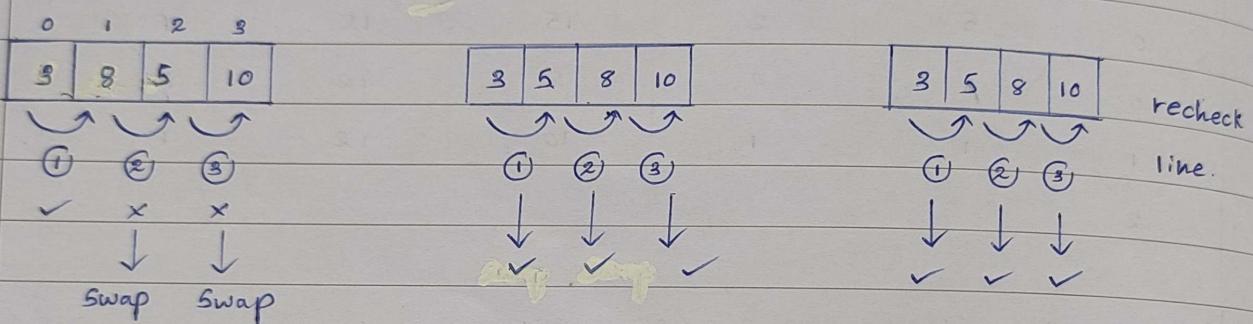
0	5	2	15	35	F	-1
3	5	4	25	35	F	-1
5	5	5	30	35	F	-1
6						

2022. 11. 30

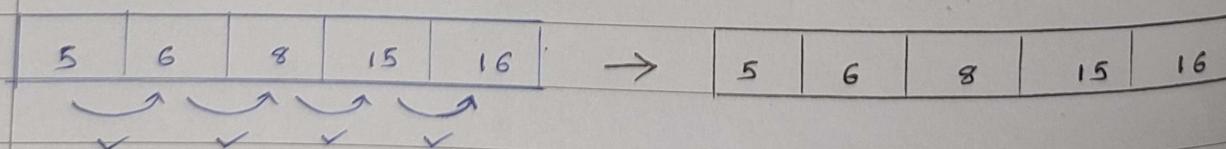
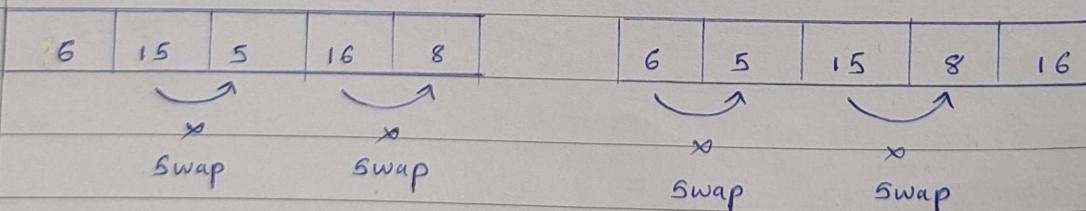
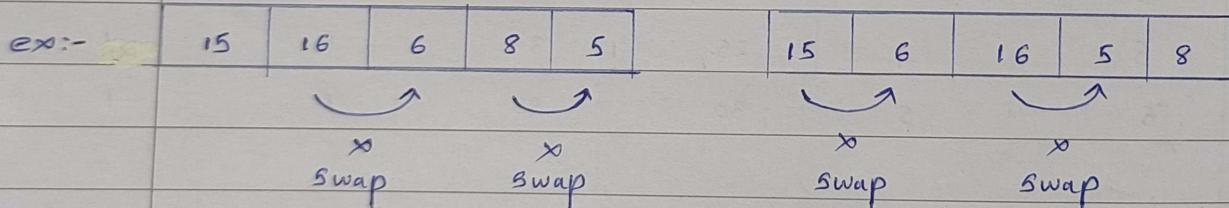
➤ Sorting algorithm.



1) Bubble Sort



→ when Swap remains false it end up the algorithm.



NO. OF PASSES = 05

No _____

A = arr

```
int i; int A [size]; int temp  
temp = A [i];  
A [i] = A [i + 1];  
A [i + 1] = temp;  
do {  
    Swap = false;  
    for ( i=0 ; i < n ; i++ ) {  
        if ( A [i] > A [i + 1] ) {  
            temp = A [i];  
            A [i] = A [i + 1];  
            A [i + 1] = temp;  
            Swap = true; }  
    }  
} while ( swap );
```

- bubble Sort -

i Assign do soon
itl , , , , (overwise)

5	3		3		3	3	5
↓	Temp		5 = Temp		Temp	↓	

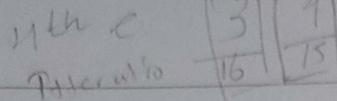
```
int temp;  
if ( arr[i] > arr[i+1] )
```

```
{  
    temp = arr[i];           arr[i] assign to temporary  
    arr[i] = arr[i+1];       value.  
    arr[i+1] = temp;         ( overwrite )  
}
```

$$12 \quad 20 \quad 18 \quad 10 \quad \rightarrow \quad 12 \quad 18 \quad 20 \quad 10 \quad \rightarrow \quad 12 \quad 18 \quad 10 \quad 20$$

Iteration	i	i + 1	A[i]	A[i + 1]	Swap
					false
①	0	1	12	20	false
	1	2	20	18	True
	2	3	20	10	True
②	0	1	12	18	false
	1	2	18	10	True
	2	3	18	12	false
X	3	4			
③	0	1	12	10	T
	1	2	12		

3 8 12 15 16



1st Iteration

0	2	11
15	8	3

2nd iteration

12	
16	8

3rd iteration 2022.1R.08 2 | 3
1) Selection Sort

Selection Sort and Insertion Sort.

1)

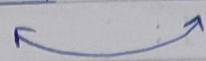
18	12	4	20	16
0	1	2	3	4

* we are assuming the minimum index have the minimum value in array.

1st Iteration → min Index → 0

min value → 18 12 4

4	12	18	20	16
---	----	----	----	----



2nd Iteration → min Index → 1

min value → 12

4	12	18	20	16
4	12	18	20	16

unchanged

3rd Iteration → min Index → 2

min value → 18 20 16

4	12	16	20	18
---	----	----	----	----



4th Iteration → min Index → 3

min value → 20 18



0	1	2	3	4	5
15	16	6	8	12	5

4	12	16	18	20
---	----	----	----	----

1st , m. Index → 0 2 5

m. value → 15 6 5

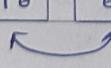
5	16	6	8	12	15
---	----	---	---	----	----



2nd , m. Index → 1 2

m. value → 16 6

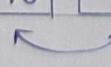
5	6	16	8	12	15
---	---	----	---	----	----



3rd , m. Index → 2 3

m. value → 16 8

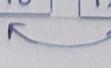
5	6	8	16	12	15
---	---	---	----	----	----



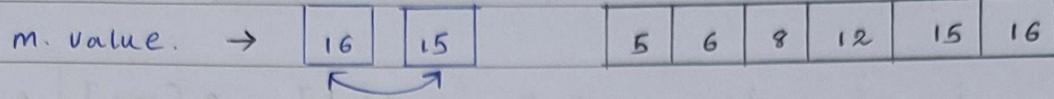
4th , m. Index → 3 4

m. value → 16 12

5	6	8	12	16	15
---	---	---	----	----	----



5th, M. Index → 4 5



➤ Code for the Selection Sort.

```
for ( i=0 ; i<n-1; i++ ) {
    int min = i;
    for ( j = i+1 ; j < n ; i++ ) {
        if ( arr[i] < arr[min] )
            min = j;
    }
    if ( min != i )
        swap ( arr[i], arr[min] );
}
```

➤ Desk check

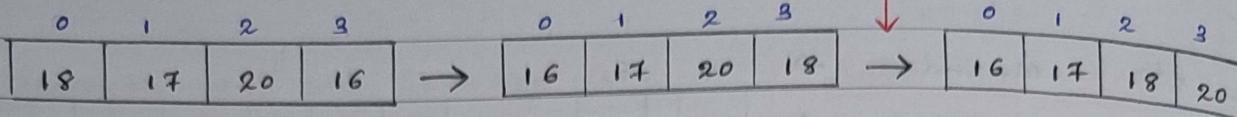
18	19	20	25
----	----	----	----

outer for loop

i	j	min I.	A[j]	A[min]	A[j] < A[min]
0	1	0	19	18	F
	2	0	20	18	F
	3	0	25	18	F
1	2	1	20	19	F
	3	1	25	19	F
2	3	2	25	20	F & T

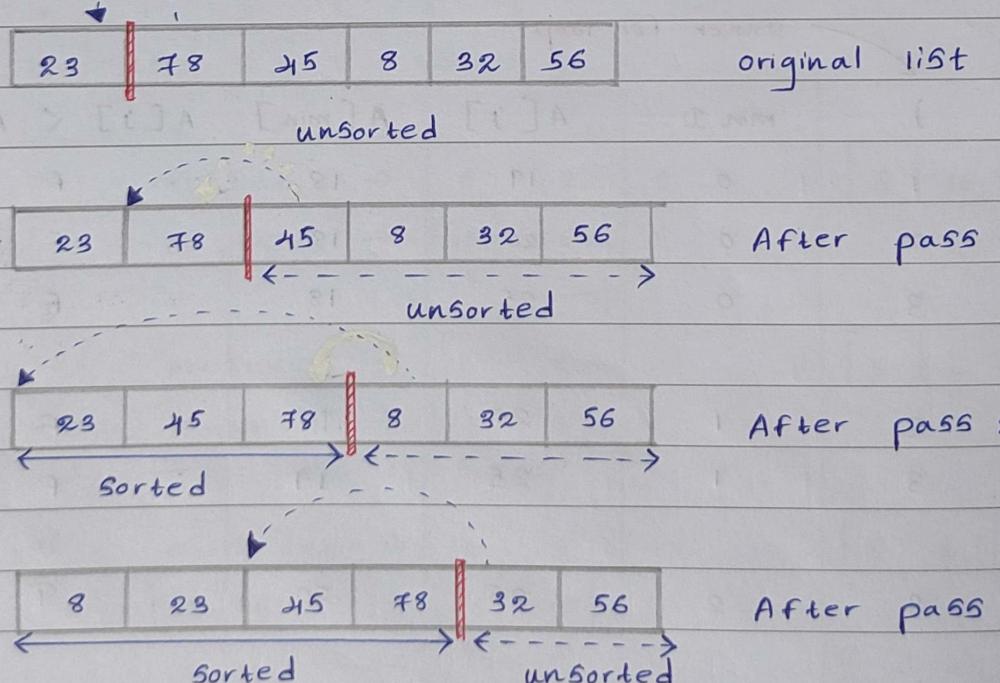
2nd (didn't swap)

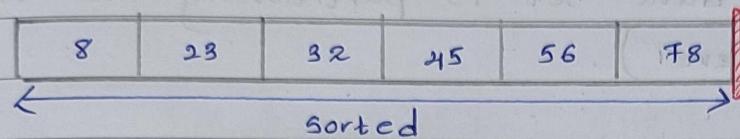
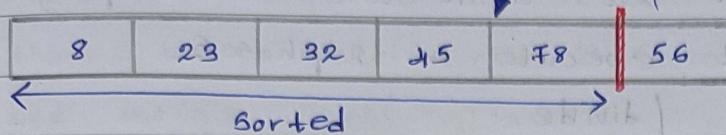
3rd



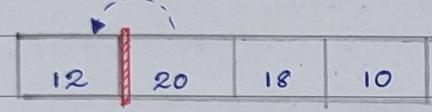
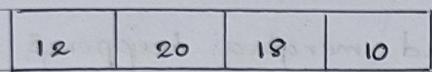
i	j	min D.	A[j]	A[min]	$A[j] < A[min]$
1st \rightarrow	0	1	0 '1'	17	18 True
		2	'1'	20	17 False
		3	'3'	16	17 True.
2nd \rightarrow	1	2	1	20	17 False
		3	1	18	17 False
3rd \rightarrow	2	3	(2) 3	18	20 True
		4	x	x	

Insertion Sorting algorithm.

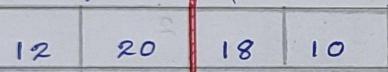




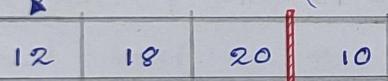
a)



original list



pass 01



pass 02



pass 03

• Insertion Sort Implementation

```
1) For (k=1 ; k< size ; k++){
    temp = A[k];
    j = k-1;
    while (j >= 0 && A[j] > temp)
    {
        A[j+1] = A[j];
        j--;
    }
    A[j+1] = temp;
```

```
2) void insert (float d[], int size){
    int i, k, l;
    float temp;
    for (k=1; k< size ; k++){
        for (i=0; i< k && d[i] <= d[k], i++);
        temp = d[k];
        for (l=k; l > i; l--)
            d[l] = d[l-1];
        d[i] = temp;
    }
}
```

Merge Sort

conquer

* Merge Sort algorithm uses divide and conquer technique merge sort execute in 2 phases.

1) Partitioning / divide

(The entire data set is partitioning into single element level)

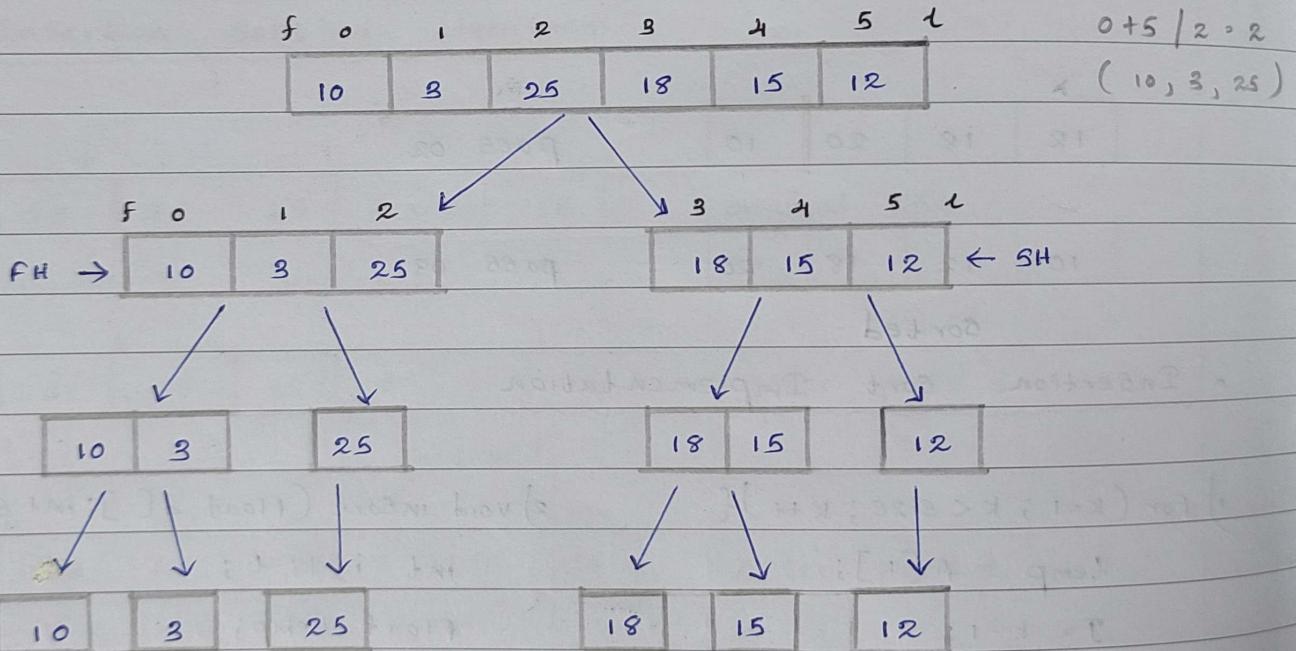
conquer

2) conquering / merge

(The actual sorting and merging happens here)

1) partitioning / divide. phase.

$$n/2 \text{, balanced part } \rightarrow m = \frac{f+1}{2}$$



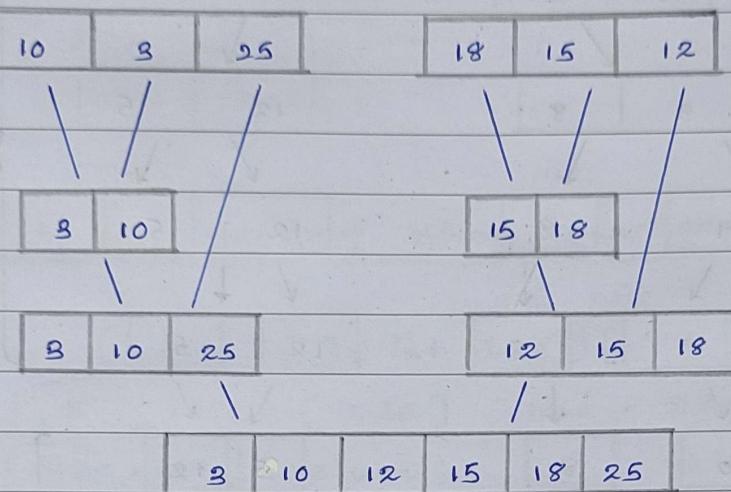
first half \rightarrow FH (arr, f, m)

Second half \rightarrow SH (arr, m+1, l)

$l > f$ (stoping criteria)

2) conquer / merge phase.

- * First we merge the first half and second half parallelly then merge the first half and second half to complete the merge sort.



first half (arr, f, m)

second half (arr, m+1, e)

merge sort (arr, f, m, m+1, e)

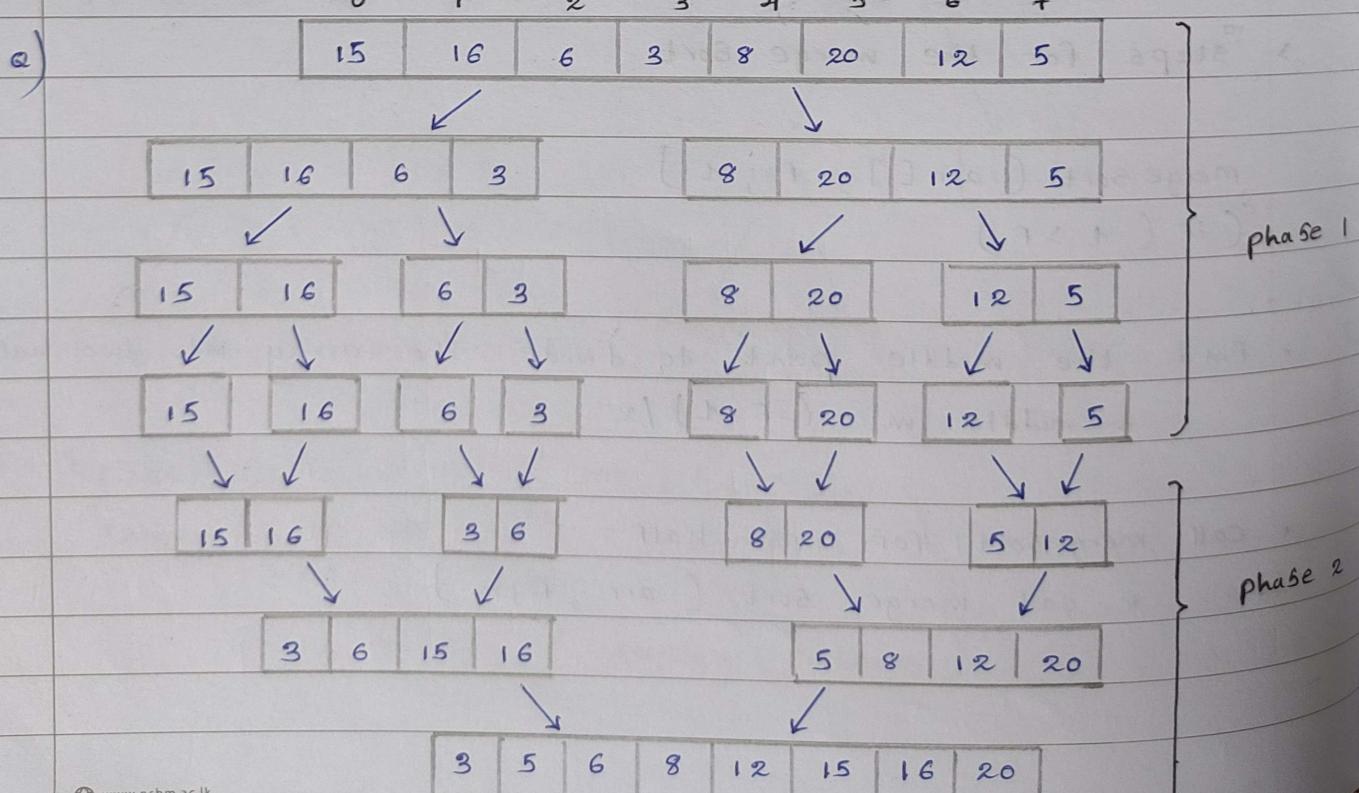
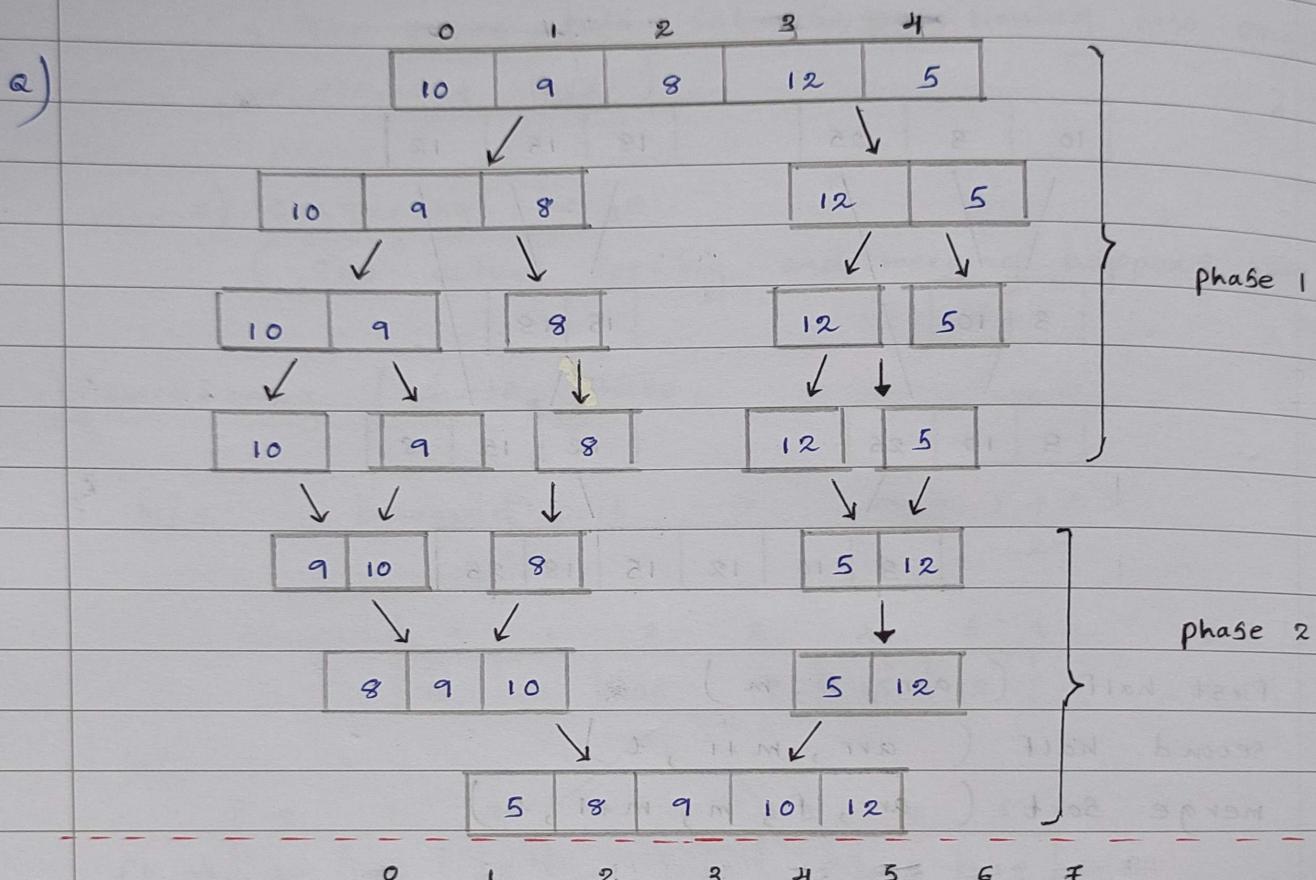
- > steps for the merge sort.

merge sort (arr[], f, e)

if (e > f)

- . find the middle point to divide the array into two halves:
 - * middle $m = (f+e)/2$
- . call mergesort for first half:
 - * call merge sort (arr, f, m)

- Call merge sort for second half:
 - * call merge sort (arr, m+1, t)
- merge the two halves sorted in steps 2 and 3:
 - * call merge (arr, f, m, t)



mSort (int d[], int l, int r) {
 if ($l < r$)
 mid = $(l+r)/2$
 mSort (d, l, mid);
 mSort (d, mid + 1, r);
 merge (d, l, mid, r);
 }

➤ merge Sort Implementing using recursion.

```
void mSort ( int d[], int size ){  

  int i, j, K , result [size] , mid = size/2;  

  if (size == 1) return;  

  mSort (d, mid);  

  mSort (&d [mid], size - mid);  

  for (K=0, i=0, j = mid, i<mid && j<size , K++)  

    result [K] = d [i] < d [j] ? d [i++] : d [j++];  

  while (i< mid) result [K++] = d [i++];  

  while (j< size) result [K++] = d [j++];  

  For (K=0 ; K< size ; K++) d [K] = result [K];  

}
```

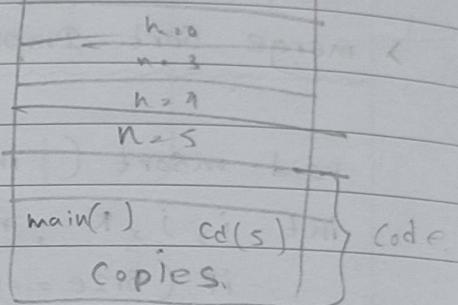
Recursion.

A function calling itself defining as Recursive function.

- Recursive functions : Base case / Recursive call.

- A recursive function for counting down to 0; ($n=5$)

```
Void countdown ( int num ) n ( start ) + recursion type code
{
    IF ( num == 0 ) finally delete
        print Done ! ; the all
    else code copies.
        {
            print num ; and the
            countdown ( num - 1 ) ; main ( ) function
        }
}
```



output \rightarrow 5 4 3 2 1 done.

memory allocation • While coding & running

Dynamic memory	\rightarrow	activation record	stack	heap	• Finally delete the all code copies and the main() function	$n = 0$	
action	\rightarrow				$n = 1$		
record	\rightarrow				$n = 2$		
Static / global	\rightarrow				$n = 3$		
Variables				code	$n = 4$		
					$n = 5$		
				main() cd(1) cd(2)			
				cd(3) cd(4) cd(5)			

Dynamic memory - All the things happen in runtime.

Code section - machine code is loaded in here.

03) void

(head - recursion type code)

{
In this code It's execute the last line (print num)
if . . . first. The out put generate's while deleting the
else action record.

{

countdown(num-1);
print num);

}

output = Done 1 2 3

n = 1	
n = 2	
n = 3	
main() cd(3)	
cd(2) cd(1)	

* any given recursive function has two components.

1) Base - case | Stopping condition | termination point.

2) The recursive call

(Recursive call runs towards the base case.)

a) write a function to get the factorial value of a given number.

int fact (int n) {

$$n! = (n-1)! * n$$

if (no == 0); <

$$5! = 4! * 5$$

return 1 ;

$$\hookrightarrow 3! * 4$$

else

$$\hookrightarrow 2! * 3$$

return n * fac(n-1);

$$\hookrightarrow 1! * 2$$

}

 $\hookrightarrow 0! * 1$ $\hookrightarrow 1 \text{ return.}$

factorial of

" 1 "

$n = 3$

$n * \text{fac}(n-1)$

$3 * (3-1) = 6$

$2 * (2-1) = 2$

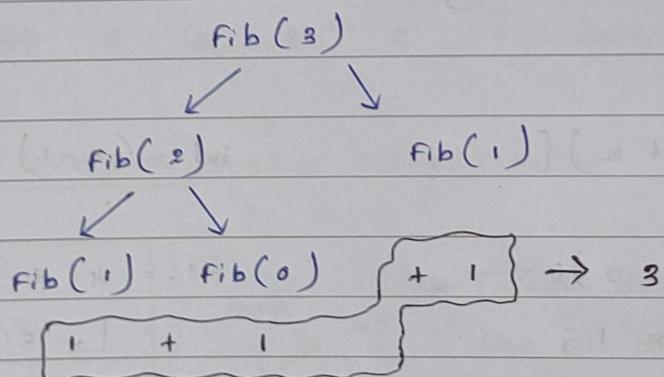
$1 * (1-1) = 0$

Fibonacci Sequence.

0 1 2 3 4 5 6 7 8 9
 1, 1, 2, 3, 5, 8, 13, 21, 34, 55

```
int fib ( int n )
if ( n <= 1 )
    return 1;
else,
    return fib( n-1 ) + fib( n-2 );
```

call tree for $n=3$:



Root
Parent
Child
Leaf
Leaves
Siblings

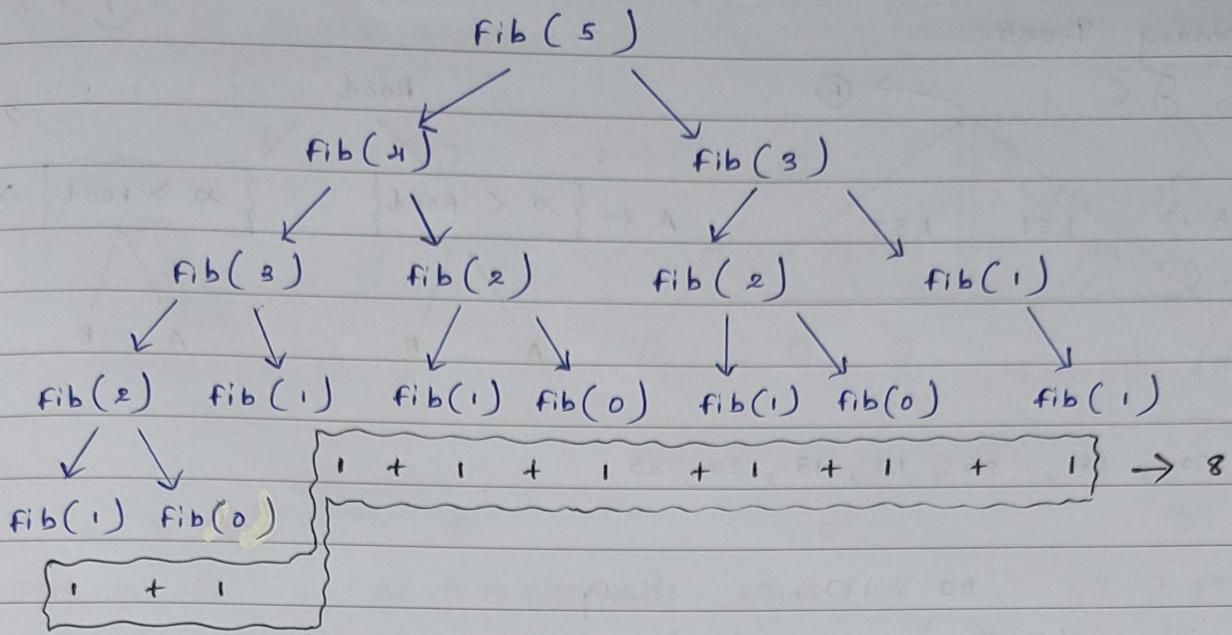
50

25

15 35 65

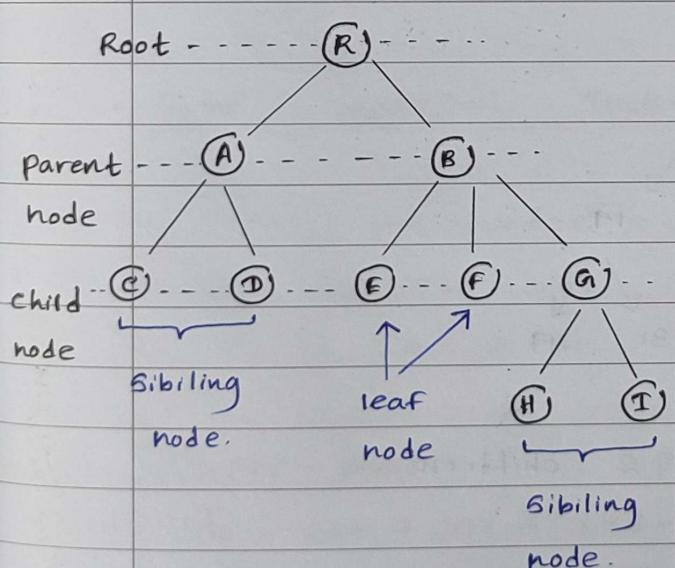
85

10



> Tree data Structure.

- A Tree is a collection of nodes and edges used to interconnect nodes.
- A node with children called parent node.
- The top most node of a tree structure is 'Root' and there is only one root for any tree structure. (supergrandparent)
- also the top most node is the starting point. (0 or more)



path \rightarrow sequence (R \rightarrow B \rightarrow G)

height \rightarrow max depth of structure.

(depth of all the nodes)

depth \rightarrow number of nodes in the path.

binary tree \rightarrow maximum of 2 children

min = 0.

multimay tree \rightarrow

leaf node \rightarrow node with no children.

normally the end point of structure.

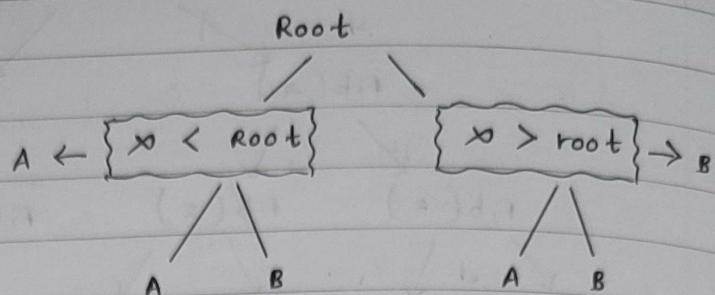
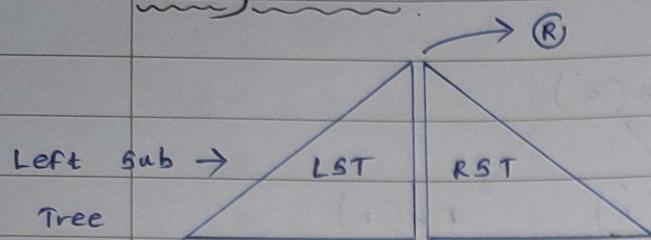
Root (R, B, G) path: R \rightarrow B \rightarrow G

① Depth of node = 3

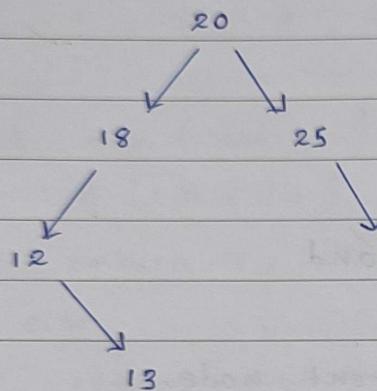
↓
(value)  www.nsbm.ac.lk

Sibling node \rightarrow nodes who have common parent nodes.

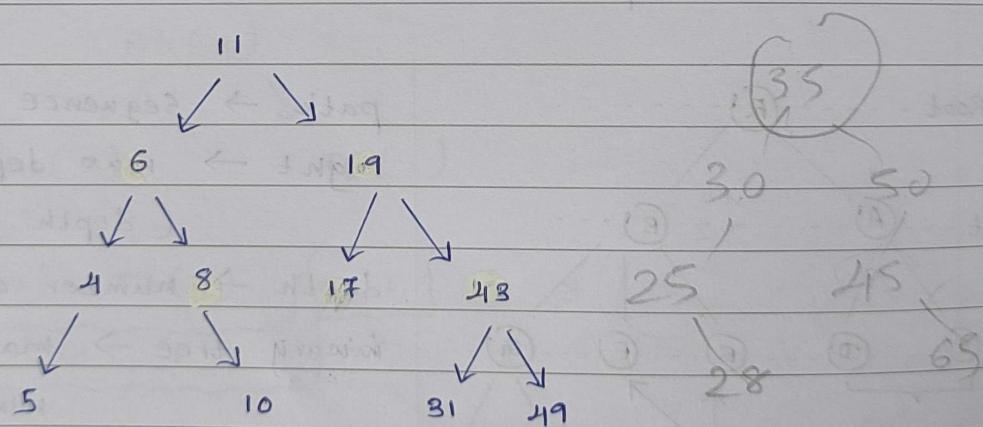
binary Trees.



01) 20, 18, 25, 12, 13, 30, 35



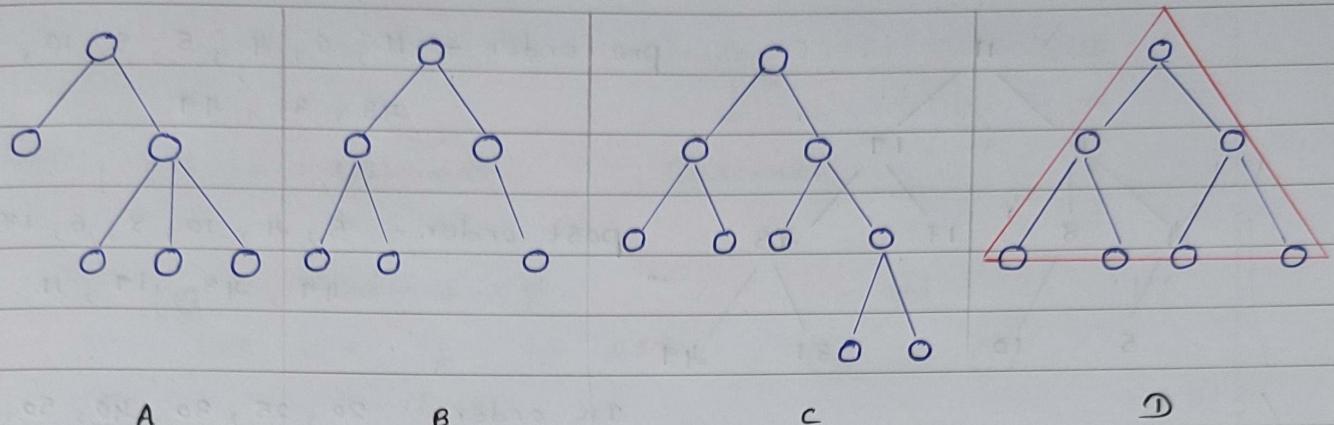
02) 11, 6, 8, 19, 4, 10, 5, 17, 43, 49, 31



• binary tree have only 0, 1 or 2 children.

• 0, 2 children
full binary
all the

• Types of binary trees



Not a BT

BT \rightarrow unbalanced

(0, 1, 2)

BT \rightarrow Full

(0, 2)

BT \rightarrow perfect

(0, 2)

Full
LSL

* binary tree is recognized as a perfect binary tree when it is a full binary tree and all the leaf nodes at the same level.

• equation for a perfect binary tree.

n - nodes

$$n = 2^h - 1$$

h - height of

$$63 = 2^6 - 1$$

PBT

• Tree Traversal Techniques

- 1) pre - order
- 2) post - order
- 3) In - order.

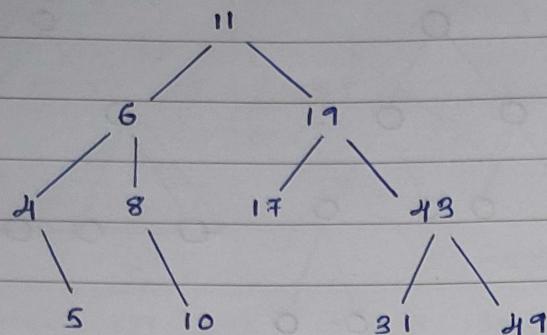
pre - order

post - order

In - order

VLR - visit if left is null move to right if not stay left	LVR - If left is null, then left is null then visit the node.	LVR - This is called left visit right
Parent first	child first	

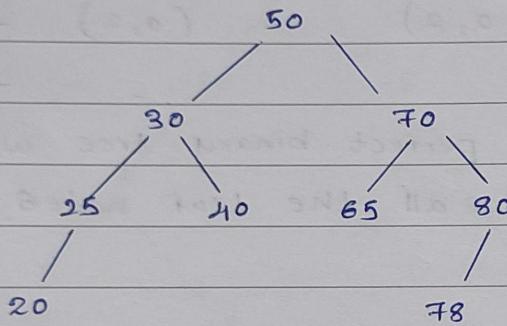
a) Find the pre-order



pre order - 11, 6, 4, 5, 8, 10, 17, 19, 17, 43, 31, 49

post order - 5, 4, 10, 8, 6, 17, 31, 49, 43, 17, 11

In order - 5, 4, 8, 10, 17, 31, 43, 49, 17, 11



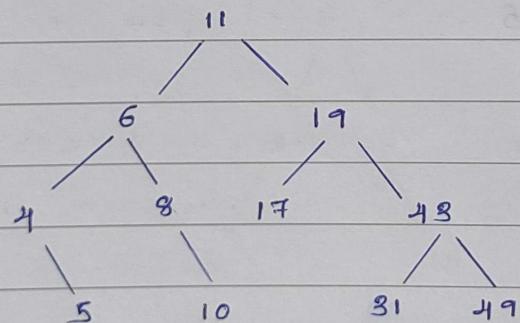
pre order - 50, 30, 25, 20, 40, 70, 65, 80, 78

post order - 20, 25, 40, 30, 65, 78, 80, 70, 50

In order - 20, 25, 30, 40, 50, 65, 70, 78, 80

2023.01.05.

ex:-

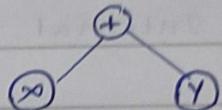


4, 5, 6, 8, 10, 11, 17, 19, 17, 43, 31, 49

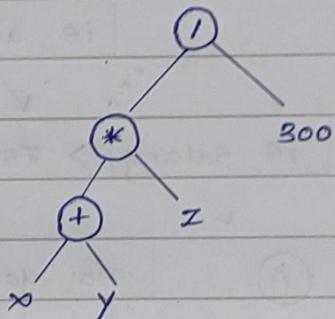
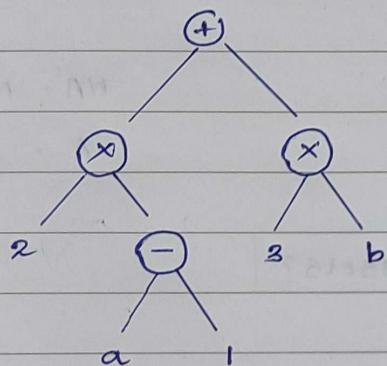
Expression tree

operand
 ↓
 Leaf / External operator
 ↓
 Internal

$x + y$
 LST ← ↓ → RST
 Root

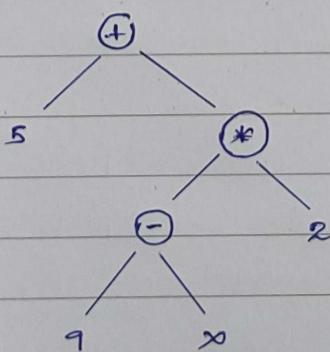


$$1) (2x(a-1) + (3 \times b)) \quad 2) ((x+y)*z) / 300$$

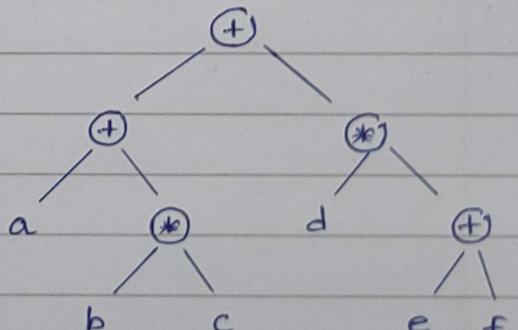


$$3) (5 + (9 - x) * 2)$$

4) Test paper question



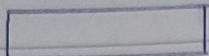
$$a + (b * c) + d * (e + f)$$



Decision Tree

Question with

y / n



Internal

Decision



External

- i) Bank loan company ,
 age > 18
 salary $> \text{f}500$ or Asset .

