$$\beta_3$$

$$\beta_1$$

$$C_3$$

$$\beta_1$$

$$C_4$$

$$C_1$$

$$C_1:(\alpha_2\to\alpha_3)\to(\alpha_1\to\alpha_2)\to\alpha_1\to\alpha_3=?\ (\mathsf{Bool}\to\mathsf{Bool})\to\beta_4$$

$$C_2:\mathsf{Int}\to\mathsf{Bool}=?\ \alpha_4\to\beta_2$$

$$C_3:\beta_1=?\ \beta_2\to\beta_3$$

$$C_5:\beta_4=?\ \alpha_4\to\beta_5$$