

# Causal Inference I

*MIXTAPE SESSION*

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# Roadmap

## Directed Acyclic Graphs

- Graph notation

- Backdoor criterion

- Collider bias

- Concluding remarks

# Graphs

- Now we turn from potential outcomes modeling of causal effects to causal graphs
- Very important area, very common to see it in computer science intersections with data science, particularly tech, and often very advanced
- My focus is very narrow – I am using it mainly to help us carefully reason through design elements around matching and instrumental variables

Judea Pearl, 2011 Turing Award winner, drinking his first IPA



# Judea Pearl and DAGs

- Judea Pearl and colleagues in Artificial Intelligence at UCLA developed DAG modeling to create a formalized causal inference methodology
- They make causality concepts extremely clear, they provide a map to the estimation strategy, and maybe best of all, they communicate to others what must be true about the data generating process to recover the causal effect

## Further reading

1. Pearl (2018) The Book of Why: The New Science of Cause and Effect, Basic Books (*popular*)
2. Morgan and Winship (2014) Counterfactuals and Causal Inference: Methods and Principles for Social Research, Cambridge University Press, 2nd edition (*excellent*)
3. Pearl, Glymour and Jewell (2016) Causal Inference In Statistics: A Primer, Wiley Books (*accessible*)
4. Pearl (2009) Causality: Models, Reasoning and Inference, Cambridge, 2nd edition (*difficult*)

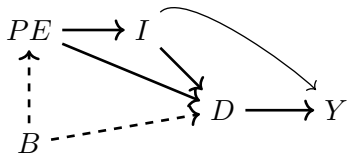
# Design vs. Model

- DAGs tend to be focused more on the theory of treatment assignment in the world
- As such it's compatible with design-based approaches
- DAGs have become extremely common in industry and machine learning, so consider my review very basic comparatively as I will use them mainly to illustrate “good vs bad controls” as well instrumental variables

# Causal model

- The causal model is sometimes called the structural model, but for us, I prefer the former as it's less alienating
- It's the system of equations describing the relevant aspects of the world
- It necessarily is filled with causal effects associated with some particular comparative statics
- Consider the following diagram representing the returns to education with simplified confounders





- $B$  is a **parent** of  $PE$  and  $D$
- $PE$  and  $D$  are **descendants** of  $B$
- There is a **direct (causal) path** from  $D$  to  $Y$
- There is a **mediated (causal) path** from  $B$  to  $Y$  through  $D$
- There are six **paths** from  $PE$  to  $Y$  but none are direct, but some of them are different in other ways

# Where do DAGs come from?

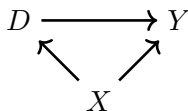
- DAGs are meant to represent “contemporary agreement among experts” – if you aren’t willing to present your DAG before a room of experts, it’s likely you shouldn’t use it at all
- Your DAG should be a reasonable approximation of  $D$  and  $Y$  parents (confounders) and direct and indirect effects of  $D$  on  $Y$
- We get ideas for DAGs from theory, models, observation, experience, prior studies, intuition, as well as conversations with domain experts

# Unconfoundedness and the backdoor criterion

- DAGs help us understand the source of problems in our observational (non-experimental) data that make inferring causality hard
- But it also can help us see a way out in some situations
- We will focus today on the unconfoundedness research design, which is best described in causal graphs with the concept of the **backdoor criterion**
- As we will see, the DAG helps you solve the problem of choosing covariates for a model to resolve selection bias, but to do so requires confidence in your DAG

# Confounding

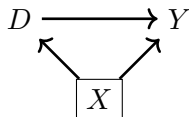
- Confounding occurs when when the treatment and the outcomes have a common parent node as that creates spurious correlation between  $D$  and  $Y$



- The *correlation* between  $D$  and  $Y$  is a biased measure of the average causal effect of  $D$  on  $Y$  because of selection bias from the confounder (ignoring for now heterogenous treatment effects bias)

# Backdoor Paths

- Confounding creates **backdoor paths** between treatment and outcome ( $D \leftarrow X \rightarrow Y$ ) – i.e., spurious correlations
  - Not the same as a collider path ( $D \rightarrow X \leftarrow Y$ )
  - and not the same as a mediator path ( $D \rightarrow X \rightarrow Y$ )
- We can “block” any particular backdoor path by conditioning on variable  $X$  so long as it is not a collider
- Once we condition on  $X$ , the correlation between  $D$  and  $Y$  estimates the causal effect of  $D$  on  $Y$
- Conditioning means calculating  $E[Y|D = 1, X] - E[Y|D = 0, X]$  for each value of  $X$  then combining (e.g., integrating) but we discuss this more later



# Blocked backdoor paths

A backdoor path is blocked if and only if:

- It contains a noncollider that has been conditioned on
- Or it contains a collider that has not been conditioned on

Note: A path which has a conditioned-on-collider can still be closed, but only with a noncollider-conditioned-on (we will see this later)

# Backdoor criterion

## Backdoor criterion

Conditioning on  $X$  satisfies the backdoor criterion with respect to  $(D, Y)$  directed path if:

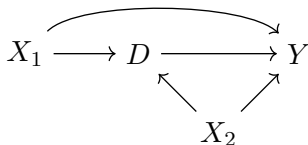
1. All backdoor paths are blocked by  $X$
2. No element of  $X$  is a collider

In words: If  $X$  satisfies the backdoor criterion with respect to  $(D, Y)$ , then controlling for or matching on  $X$  identifies the causal effect of  $D$  on  $Y$ .

And again note that a path which has a conditioned-on-collider can still be closed, but only with a noncollider-conditioned-on

# What control strategy meets the backdoor criterion?

- List all backdoor paths from  $D$  to  $Y$ . I'll wait.

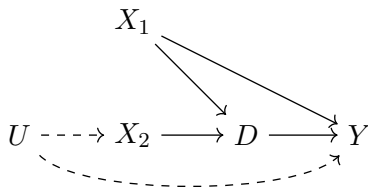


- What are the necessary and sufficient set of controls which will satisfy the backdoor criterion?



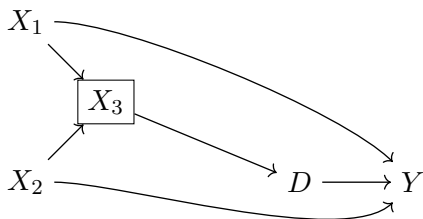
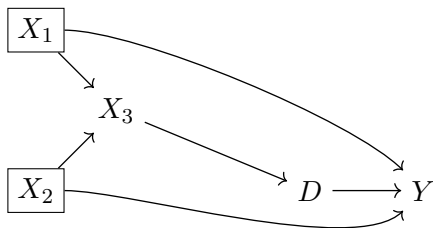
# What if you have an unobservable?

- List all the backdoor paths from  $D$  to  $Y$ .



- What are the necessary and sufficient set of controls which will satisfy the backdoor criterion?
- What about the unobserved variable,  $U$ ?

# Multiple strategies



- Conditioning on the common causes,  $X_1$  and  $X_2$ , is sufficient
- ...but so is conditioning on  $X_3$

# Collider bias

- Backdoor paths can remain open in covariate adjustment strategies through two ways:
  1. You did not close the path because you did not condition on the confounder
  2. Your conditioning variable opened up a previously closed backdoor path because on that path the variable was a **collider**
- Colliders are “bad controls” which when you control for them, *create* new previously non-existent spurious correlations (not commonly discussed, even in economics)
- This is the risk of blindly controlling for variables (“kitchen sink regressions”)

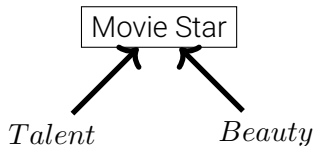
## Example 1: Movie stars

**Important:** Since unconditioned colliders block back-door paths, what exactly does conditioning on a collider do? Let's illustrate with a fun example and some made-up data

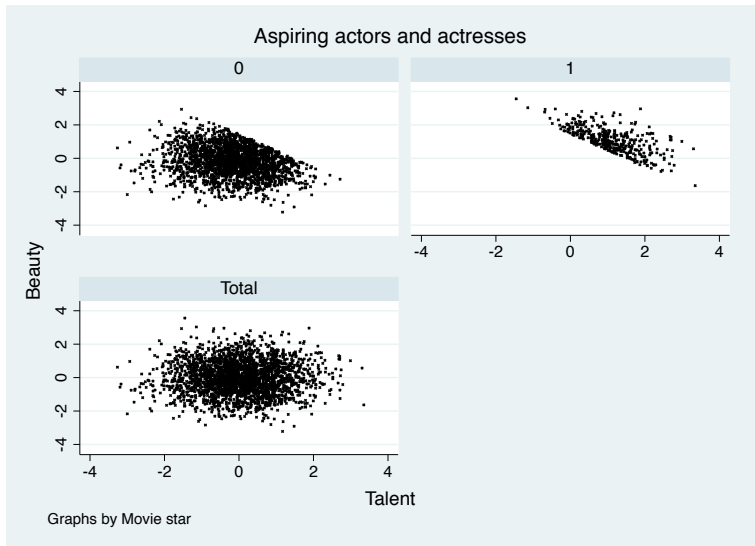
- [CNN.com](#) headline: Megan Fox voted worst – but sexiest – actress of 2009 (link)
- Are these two things actually negatively correlated in the world?
- Assume talent and beauty are independent, but each causes someone to become a movie star. What's the correlation between talent and beauty for a sample of movie stars compared to the population as a whole (stars and non-stars)?

# Movie star DAG

Imagine casting directors pick movie stars based on talent and beauty



Talent and beauty can become correlated even though they are independent



*Figure:* Top left figure: Non-star sample scatter plot of beauty (vertical axis) and talent (horizontal axis). Top right right figure: Star sample scatter plot of beauty and talent. Bottom left figure: Entire (stars and non-stars combined) sample scatter plot of beauty and talent.

# Sample selection?

- Notice that this is clear when we are focused on sample selection
- But even a regression that included “star” would create the issue:

$$talent_i = \alpha + \delta beauty_i + \beta star_i + \varepsilon_i$$

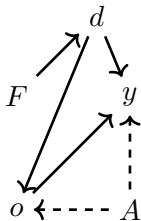
- It's not just sample selection

## Example 2: Discrimination

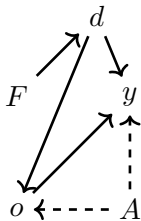
- Let's look at another example: very common for think tanks and journalists to say that the gender gap in earnings disappears once you control for occupation.
- But what if occupation is a collider, which it could be in a model with occupational sorting
- Then controlling for occupation in a wage regression searching for discrimination can lead to all kinds of crazy results *even in a simulation where we explicitly design there to be discrimination*



# DAG



$F$  is female,  $d$  is discrimination,  $o$  is occupation,  $y$  is earnings and  $A$  is ability. Dashed lines mean the variable cannot be observed. Note, by design, being a female has no effect on earnings or occupation, and has no relationship with ability. So earnings is coming through discrimination, occupation, and ability.



Mediation and Backdoor paths

1.  $d \rightarrow o \rightarrow y$
2.  $d \rightarrow o \leftarrow A \rightarrow y$

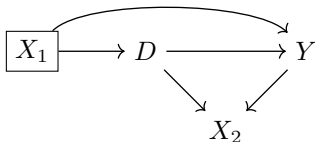
*Table:* Regressions illustrating collider bias with simulated gender disparity

Covariates:	Unbiased combined effect	Biased	Unbiased wage effect only
Female	-3.074*** (0.000)	0.601*** (0.000)	-0.994*** (0.000)
Occupation		1.793*** (0.000)	0.991*** (0.000)
Ability			2.017*** (0.000)
N	10,000	10,000	10,000
Mean of dependent variable	0.45	0.45	0.45

- Recall we designed there to be a discrimination coefficient of -1
- If we do not control for occupation, then we get the combined effect of  $d \rightarrow o \rightarrow y$  and  $d \rightarrow y$
- Because it seems intuitive to control for occupation, notice column 2 - the sign flips!
- We are only able to isolate the direct causal effect by conditioning on ability and occupation, but ability is unobserved

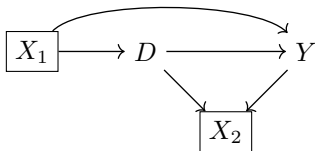
- **Colliders can be outcomes (and often those are the ones)**

→ There is only one backdoor path from  $D$  to  $Y$



→ Conditioning on  $X_1$  blocks the backdoor path

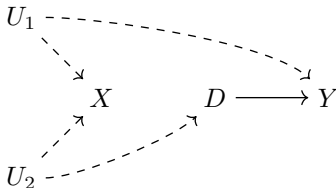
→ But what if we also condition on  $X_2$ ?



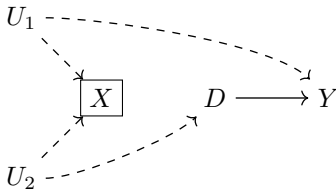
→ Conditioning on  $X_2$  opens up a new path, creating new spurious correlations between  $D$  and  $Y$

- **Colliders could be pre-treatment covariates (called M-bias because it looks like an M)**

→ Name the backdoor paths. Is it open or closed?

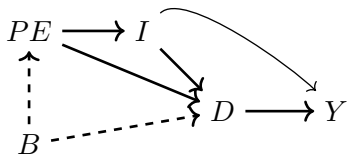


→ But what if we condition on  $X$ ?



# Testing the Validity of the DAG

- The DAG makes testable predictions
- Conditional on  $D$  and  $I$ , parental education ( $PE$ ) should no longer be correlated with  $Y$
- Can be hard to figure this out by hand, but software can help (e.g., Dagitty.net is browser based, Causal Fusion is more advanced)
- Causal algorithms tend to be DAG based and are becoming popular in industry



# Summarizing all of this

- Your dataset will not come with a codebook flagging some variables as “confounders”, “mechanisms” and “colliders” because those terms are always context specific
- Except for some unique situations that aren't generally applicable, you also don't always know statistically you have an omitted variable bias problem; but both of these are fatal for any application
- You only know to do what you're doing based on *knowledge about data generating process*.
- All identification must be guided by theory, experience, observation, common sense and knowledge of institutions
- DAGs absorb that information and can be then used to write out the explicit identifying model

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