

# Descriptive Statistics

Gov 51: Data Analysis and Politics



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# Today's Roadmap

## 1. The Question: What Does “Typical” Mean?

- ▷ Summarizing presidential approval across states

## 2. Measures of Center

- ▷ Mean, median, and when they differ

## 3. Measures of Spread

- ▷ Range, percentiles, variance, standard deviation

## 4. Weighted Statistics

- ▷ Why some observations “count” more than others

## 5. Visualizing Distributions

- ▷ Histograms and what they tell us



The Question: What Does “Typical” Mean?

# A Simple Question

What does the typical American think about the president?

Gallup and other pollsters survey Americans constantly. But:

- ▷ Different states have different opinions
- ▷ Different states have different populations
- ▷ How do we summarize all this into one number?

Today we'll use state-level presidential approval data to learn how to summarize distributions.

# Loading Our Data

```
# Load data
approval <- read.csv("state_approval.csv")

# What do we have?
dim(approval)
## [1] 50 5

head(approval, 4)
##      state abbrev approval population    region
## 1 Alabama      AL       38    5024279    South
## 2 Alaska       AK       41     733391     West
## 3 Arizona      AZ       44    7151502     West
## 4 Arkansas     AR       36    3011524    South
```

50 states, with approval rating (%) and population.

## First Look: The Raw Numbers

Here are approval ratings for a few states:

State	Approval (%)	Population (millions)
California	52	39.5
Texas	41	29.1
Wyoming	32	0.6
Vermont	57	0.6
Ohio	42	11.8

**What's the “typical” approval rating?**

Should Wyoming (0.6 million people) count the same as California (39.5 million)?



# Measures of Center

## Let's Start Simple

Before we use R, let's calculate by hand.

Here are approval ratings for 5 states:

**38, 41, 44, 36, 52**

**Calculate the mean:**

- 1.** Add them up:  $38 + 41 + 44 + 36 + 52 = 211$
- 2.** Divide by the count:  $211 \div 5 = 42.2$

The mean approval rating is 42.2%.

That's all the mean is: sum divided by count.



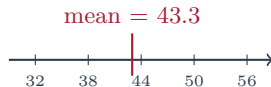
# The Mean: What R Does

The `mean()` function does exactly what we just did:

```
mean(approval$approval)
## [1] 43.26
```

For all 50 states, the mean approval is **43.3%**.

Simple, right? But there's a catch...



# The Median: The Middle Value

The **median** is the middle value when you sort the data.

```
# Sort the values
sort(approval$approval)
## [1] 32 34 34 35 35 36 36 37 37 38 38 38 39 39 39 39 40
## [18] 40 41 41 42 42 43 43 44 44 45 45 45 46 46 47 47 47
## [35] 48 48 49 49 50 50 50 51 52 52 53 56 57 58

# The median (middle value)
median(approval$approval)
## [1] 43.5
```

With 50 values, the median is the average of the 25th and 26th values.

Median = 43.5%

# Mean vs. Median: Why Both?

In our data: Mean = 43.3%, Median = 43.5%

They're almost the same! But that's not always true.

## The Mean

- ▷ Uses every value
- ▷ Sensitive to outliers
- ▷ Gets “pulled” by extreme values

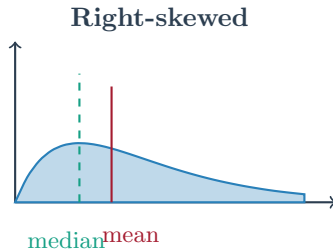
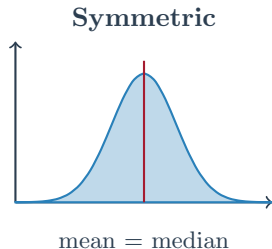
## The Median

- ▷ Only uses the middle
- ▷ Robust to outliers
- ▷ Ignores extreme values

When mean  $>$  median: distribution is right-skewed (pulled up by high values)

When mean  $<$  median: distribution is left-skewed (pulled down by low values)

# Visualizing the Difference



Income is famously right-skewed: a few billionaires pull the mean way above the median. The median household income tells you more about the “typical” American than the mean does.

# Connection to Problem Set 1

In PS1, you'll calculate mean and median commute times.

**The question we'll ask:**

- ▷ Is the mean larger or smaller than the median?
- ▷ What does that tell you about the shape of the distribution?
- ▷ Does it match what you see in the histogram?

This is how you interpret data, not just calculate it.

## Now the Math

We've seen what the mean does. Here's the formula:

$$\text{Sample Mean: } \bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

- ▷  $x_i$  = each individual value
- ▷  $n$  = number of values
- ▷  $\sum$  = “add them all up”
- ▷  $\bar{x}$  = the mean (pronounced “x-bar”)

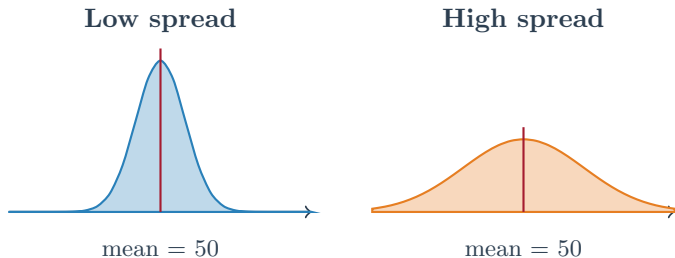
The formula just says: add up all the values, divide by how many there are.



# Measures of Spread

# Center Isn't Everything

Two datasets can have the same mean but look completely different:



**We need measures of spread:** How much do the values vary around the center?



# The Range: Simplest Measure

The **range** is just max minus min:

```
min(approval$approval)
## [1] 32

max(approval$approval)
## [1] 58

range(approval$approval)
## [1] 32 58
```

Range =  $58 - 32 = 26$  percentage points

**Problem:** The range only uses two values. One outlier can make it huge.

# Percentiles: More Robust

Percentiles tell you where values fall in the distribution:

```
quantile(approval$approval)
##      0%    25%    50%    75%   100%
##      32     39     43     49     58
```

- ▷ 0th percentile (min): 32%
- ▷ 25th percentile (Q1): 39%
- ▷ 50th percentile (median): 43.5%
- ▷ 75th percentile (Q3): 49%
- ▷ 100th percentile (max): 58%

The middle 50% of states have approval between 39% and 49%.

## Getting Specific Percentiles

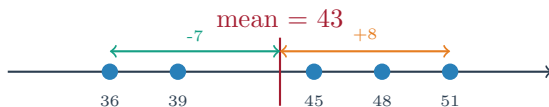
You can ask for any percentile:

```
# The 90th percentile  
quantile(approval$approval, 0.90)  
## 90%  
## 52  
  
# Multiple percentiles at once  
quantile(approval$approval, c(0.10, 0.50, 0.90))  
## 10% 50% 90%  
## 36 43 52
```

In PS1, you'll calculate the 90th percentile of commute times and write:  
"90% of commuters travel \_\_\_ minutes or less."

# Variance: Average Squared Distance from Mean

The **variance** measures how far values typically are from the mean.



## Steps:

1. Calculate each deviation:  $(x_i - \bar{x})$
2. Square them:  $(x_i - \bar{x})^2$
3. Average the squared deviations

# Why Square the Deviations?

**Problem:** Deviations add to zero!

- ▷ Some values are above the mean (positive deviation)
- ▷ Some values are below the mean (negative deviation)
- ▷ They cancel out:  $\sum(x_i - \bar{x}) = 0$

**Solution:** Square them first

- ▷ Squaring makes everything positive
- ▷ Bigger deviations get emphasized (squared distance)

There are other solutions (like absolute value), but squaring has nice mathematical properties.

## Variance in R

```
var(approval$approval)
## [1] 42.28
```

The variance is 42.28... but 42.28 *what?*

Units are “percent squared”—not very interpretable!

**Solution:** Take the square root to get back to original units.

## Standard Deviation: Variance in Original Units

The **standard deviation** is the square root of variance:

```
sd(approval$approval)
## [1] 6.50
```

The standard deviation is 6.5 percentage points.

**Interpretation:** On average, states are about 6.5 percentage points away from the mean approval rating.

This is the measure of spread you'll report in your summary statistics tables.

# The Formulas

**Sample Variance:**  $s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$

**Sample Standard Deviation:**  $s = \sqrt{s^2}$

Wait... why  $n - 1$  instead of  $n$ ?



# The $n - 1$ Question

**Quick intuition** (don't worry about the proof):

When we calculate variance, we first calculated the mean. That “used up” one piece of information.

- ▷ We have  $n$  data points
- ▷ But only  $n - 1$  independent pieces of information left
- ▷ This is called **degrees of freedom**

Dividing by  $n - 1$  instead of  $n$  corrects for this, giving us an unbiased estimate of the population variance.

R's `var()` and `sd()` functions use  $n - 1$  by default. That's what you want.

## The summary() Shortcut

R's `summary()` function gives you many statistics at once:

```
summary(approval$approval)
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##    32.00   39.00   43.50   43.26   49.00   58.00
```

This gives you:

- ▷ Min and Max (range)
- ▷ 1st and 3rd Quartiles (25th and 75th percentiles)
- ▷ Median (50th percentile)
- ▷ Mean

Note: `summary()` doesn't give you standard deviation—use `sd()` for that.

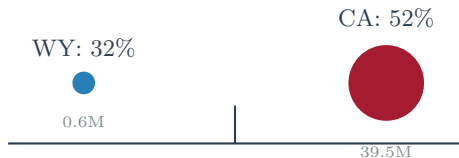


# Weighted Statistics

## Not All States Are Equal

Our mean approval (43.3%) treated every state equally.

But should Wyoming (576,000 people) count the same as California (39.5 million)?



If we want to know what the typical *American* thinks (not the typical *state*), California should count more.

# Weighted Mean

The **weighted mean** lets each observation count according to its weight:

```
# Unweighted mean (each state counts equally)
mean(approval$approval)
## [1] 43.26

# Weighted mean (weight by population)
weighted.mean(approval$approval, approval$population)
## [1] 44.52
```

- ▷ Unweighted: 43.3% (average across states)
- ▷ Weighted: 44.5% (average across people)

The weighted mean is higher because large, high-approval states (CA, NY) pull it up.

# The Weighted Mean Formula

$$\text{Weighted Mean: } \bar{x}_w = \frac{\sum_{i=1}^n w_i x_i}{\sum_{i=1}^n w_i}$$

Where  $w_i$  is the weight for observation  $i$ .

**Intuition:** Instead of each value counting once, it counts  $w_i$  times.

When all weights are equal, this reduces to the regular mean.

# Connection to Problem Set 1

In PS1, you'll use American Community Survey (ACS) data.

The ACS has a variable called PERWT (person weight):

- ▷ Each person in the survey represents many people in the US
- ▷ PERWT tells you how many

**Two calculations:**

```
# Unweighted (average in the sample)
mean(commuters$TRANTIME)

# Weighted (average in the US population)
weighted.mean(commuters$TRANTIME, commuters$PERWT)
```

You'll compare these and explain what each number represents.

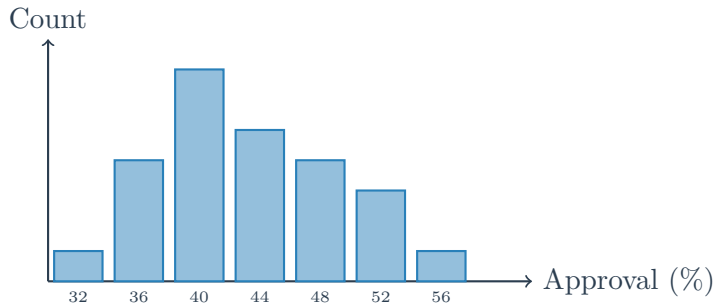


# Visualizing Distributions



# The Histogram

A **histogram** shows how values are distributed:



- ▷ X-axis: the variable (approval rating)
- ▷ Y-axis: how many observations fall in each bin
- ▷ **Shape** tells us about the distribution

# Creating a Histogram in R

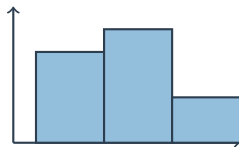
```
library(ggplot2)

ggplot(approval, aes(x = approval)) +
  geom_histogram(binwidth = 4,
                 fill = "steelblue",
                 color = "white") +
  labs(x = "Approval Rating (%)",
       y = "Number of States",
       title = "Distribution of Presidential Approval")
```

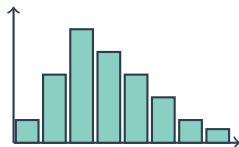
Key choices:

- ▷ **binwidth**: How wide is each bar? (Experiment!)
- ▷ **fill**: Color of the bars
- ▷ **color**: Color of the bar borders

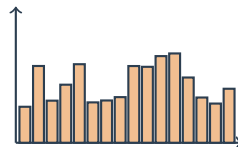
# Bin Width Matters



**Too few bins**  
Hides patterns



**Good**  
Shows shape



**Too many bins**  
Too noisy

There's no perfect answer—try different values and see what tells the clearest story.

# Describing Shape

When you look at a histogram, describe:

## Shape

- ▷ Symmetric?
- ▷ Right-skewed?
- ▷ Left-skewed?
- ▷ Bimodal?

## Center

- ▷ Where's the “middle”?
- ▷ Mean and median

## Spread

- ▷ How wide?
- ▷ Are values clustered or dispersed?

## Also note:

- ▷ Outliers (unusual values)
- ▷ Notable features (gaps, spikes)

## Example Description

Looking at our approval rating histogram:

*“The distribution of presidential approval across states is roughly symmetric, centered around 43%. Most states fall between 36% and 52% approval. There are no obvious outliers, though Vermont (57%) and Hawaii (58%) are notably high, while Wyoming (32%) and West Virginia (34%) are notably low.”*

**In PS1**, you'll write a similar description for commute times.



Putting It Together

# The Summary Statistics Table

In PS1, you'll create a table like this:

Variable	N	Mean	Std. Dev.	Min	Max
Approval (%)	50	43.3	6.5	32	58
Population (millions)	50	6.6	7.2	0.6	39.5

This table should be:

- ▷ Generated by code (not typed manually)
- ▷ Readable on its own (clear variable names, units)
- ▷ Rendered cleanly in your PDF

# Building the Table in R

```
# Calculate statistics
stats <- data.frame(
  Variable = c("Approval (%)", "Population (millions)"),
  N = c(length(approval$approval),
        length(approval$population)),
  Mean = c(mean(approval$approval),
            mean(approval$population)/1e6),
  SD = c(sd(approval$approval),
          sd(approval$population)/1e6),
  Min = c(min(approval$approval),
           min(approval$population)/1e6),
  Max = c(max(approval$approval),
           max(approval$population)/1e6)
)
```

```
# Render as a table
```

```
knitr::kable(stats, digits = 1)
```



# What You've Learned

## Concepts:

- ▷ Mean vs. median
- ▷ Skewness and shape
- ▷ Variance and standard deviation
- ▷ Degrees of freedom ( $n - 1$ )
- ▷ Weighted statistics

## R Functions:

- ▷ `mean()`, `median()`
- ▷ `min()`, `max()`, `range()`
- ▷ `var()`, `sd()`
- ▷ `quantile()`
- ▷ `weighted.mean()`
- ▷ `summary()`
- ▷ `ggplot() + geom_histogram()`



Numbers summarize. Visuals reveal. Use both.

# Looking Ahead

## Problem Set 1:

- ▷ Due Wednesday, February 11 at 11:59pm
- ▷ You now have all the statistics you need!
- ▷ Don't forget: GitHub URL in your document

## Next Week: Probability

- ▷ Foundation for everything that comes after
- ▷ Why we need it for inference

**Section this week:** Help with PS1, IPUMS setup

Questions?

Scott: Tue/Thu 3–5pm | George: Thu 2–3pm, K455 | CA: Harrison Huang