Trilinear Higgs boson coupling variations for di-Higgs production with full NLO QCD predictions in Powheg

G. Heinrich¹, S. Jones², M. Kerner³, G. Luisoni¹ and L. Scyboz¹

- $^{\rm 1}$ Max-Planck-Institut für Physik, Föhringer Ring 6, 80805 München, Germany
- ² Theoretical Physics Department, CERN, Geneva, Switzerland
- ³ Physik-Institut, Universität Zürich, Winterthurerstrasse 190, 8057 Zürich, Switzerland

E-mail: gudrun@mpp.mpg.de, s.jones@cern.ch, mkerner@physik.uzh.ch, luisonig@gmail.com, scyboz@mpp.mpg.de

Abstract. The couplings of the Higgs boson to other particles are increasingly well-measured by the ATLAS and CMS experiments. Yet there is still room for improvement in the limits set on the Higgs trilinear self-coupling, mainly due to the low cross-section for Higgs boson pair production. We present inclusive and differential results for the NLO QCD corrections to Higgs pair production with the full top-quark mass dependence, where the Higgs trilinear self-coupling is varied to non-SM values. The calculation of the two-loop virtual contributions has been performed numerically using CPUs and GPUs. The fixed-order calculation is supplemented by parton showering within the Powheg-BOX-V2 event generator, and both Pythia8 and Herwig7 parton-shower algorithms are implemented in a preliminary study of shower effects.

1. Introduction

Impressive experimental constraints have been set on the Higgs boson couplings to vector bosons and heavy fermions [1, 2, 3, 4]. The Higgs potential, in contrast, leaves more room for New Physics. In particular, the Higgs boson trilinear self-coupling λ can be experimentally constrained by exclusion limits on Higgs pair production $pp \to hh$ [5, 6]. Higher-order corrections to Higgs pair production are routinely calculated in the heavy top-quark mass limit (HTL) $m_t \to \infty$, where the top-quark degrees of freedom are integrated out [7, 8]. The NLO QCD corrections with the full top-quark mass dependence were only computed more recently [9, 10, 11]. They are based on a numerical evaluation of the two-loop contribution to $gg \to hh$ performed via sector decomposition. For non-SM values of the Higgs couplings, results were computed at NLO QCD with the full top-quark mass dependence for a class of extensions of the SM in Ref. [12].

In the following, an implementation of the full NLO QCD corrections into the Powheg-BOX-V2 event generator [13, 14, 15] is presented. In this framework, the Higgs trilinear self-coupling can be varied, as well as the top-Higgs Yukawa coupling. Total cross-sections are computed for $\sqrt{s} = 13, 14$ and 27 TeV at the (HE-)LHC. Differential results are shown for $\sqrt{s} = 14$ TeV. The fixed-order calculation is then matched to both Pythia8 [16] and Herwig7 [17] parton showers. For a more detailed description, the reader is referred to Ref. [18].

2. Description of the calculation

The calculation is based on the setup presented in Ref. [19] for the case of the SM. The leading-order amplitude has been computed analytically. The real-emission contributions were implemented in GoSam [20, 21] and interfaced to the Powheg-BoX, and the corresponding scalar one-loop amplitudes were evaluated with Ninja [22], golem95C [23, 24] and OneLOop [25] (except for the scalar four-point function, which is taken from VBFNLO [26, 27] for numerical stability reasons). The two-loop amplitude for the full-theory virtual contribution was adapted from Refs. [9, 10], which used an extension of the GoSam package. There, the integral reduction was performed with Reduze2 [28], and the integrals were numerically evaluated with SecDec3 [29]. For a fast convergence, the integration was performed within a Quasi-Monte-Carlo implementation using a rank-1 shifted lattice [30, 31]. The integrals were computed with 16 dual NVIDIA Tesla K20XM GPUs. The top-quark and Higgs masses have been set to $m_t = 173 \,\text{GeV}$ and $m_h = 125 \,\text{GeV}$. Thus, the integrals depend only on the two Mandelstam invariants \hat{s} and \hat{t} .

A grid for the two-loop amplitude was constructed in both variables using 5291 pre-sampled phase-space points. We split the amplitude in two contributions: diagrams containing the trilinear Higgs coupling are called *triangle-like*, and those that do not *box-like* (see Fig. 1 for two leading-order diagrams).



Figure 1. Triangle-like (left) and box-like (right) diagrams contribute to the full amplitude. The former contain the Higgs self-coupling, while the latter do not.

At any order in QCD, the squared matrix-element can thus be written as a second-order polynomial in λ :

$$M_{\lambda} \equiv |\mathcal{M}_{\lambda}|^2 = \mathcal{M}_B^* \mathcal{M}_B + \lambda \left(\mathcal{M}_B^* \mathcal{M}_T + \mathcal{M}_T^* \mathcal{M}_B \right) + \lambda^2 \mathcal{M}_T^* \mathcal{M}_T . \tag{1}$$

The two-loop amplitude for an arbitrary value of λ can be reconstructed from the squared matrix-element computed for three different values of λ . In our case, we chose $\kappa_{\lambda} = \lambda_{\rm BSM}/\lambda_{\rm SM} \in \{-1,0,1\}$ and generate a new grid for the user-defined value of λ , where the amplitude for each pre-sampled phase-space point is calculated as:

$$M_{\lambda} = M_0 \cdot (1 - \lambda^2) + \frac{M_1}{2} \cdot (\lambda + \lambda^2) + \frac{M_{-1}}{2} \cdot (-\lambda + \lambda^2)$$
 (2)

The grid produced for the two-loop amplitude is fed to an interpolation framework, which interfaces the result at any phase-space point $M_{\lambda}(\hat{s},\hat{t})$ to Powheg.

3. Total and differential cross-sections for variations of the trilinear coupling

The results given below are produced using the PDF4LHC15_nlo_30_pdfas sets [32, 33, 34, 35] interfaced to Powheg via LHAPDF6 [36], with the corresponding value of α_s . The top-quark mass is renormalised in the on-shell scheme and is set to $m_t = 173 \,\text{GeV}$, as in the virtual amplitude. The mass of the Higgs boson is fixed to $m_h = 125 \,\text{GeV}$, and the top-quark and

Higgs widths are set to zero. Jets are clustered using the anti- k_T algorithm [37] as implemented in FastJet [38, 39], with a jet distance parameter of R=0.4 and a minimum transverse momentum requirement of $p_T=20 \text{ GeV}$. The central renormalisation and factorisation scales are set to $\mu_R=\mu_F=\mu_0=m_{hh}/2$. Scale uncertainties are estimated by 2-point variations $\mu_R=\mu_F=c\,\mu_0$, with $c\in\{0.5,2.0\}$.

Total cross-sections for Higgs pair production at the (HE-)LHC are shown in Table 1, for centre-of-mass energies of $\sqrt{s} = 13,14$ and 27 TeV and different values of the Higgs self-coupling $\kappa_{\lambda} = \lambda_{\rm BSM}/\lambda_{\rm SM}$. They are accompanied by their relative scale uncertainties, which are of the order $\mathcal{O}(10-20\%)$. Notably, the K-factors at 14 TeV show a sizeable dependence on the trilinear coupling κ_{λ} . In the HTL at NLO QCD, Ref. [40] suggested a variation of the K-factors with κ_{λ} of the order $\mathcal{O}(2-3\%)$. In the full theory, the K-factors are found between 1.56 and 2.15 for variations of the trilinear coupling $-5 \le \kappa_{\lambda} \le 12$, see Fig. 2.

$\lambda_{ m BSM}/\lambda_{ m SM}$	$\sigma_{ m NLO}$ @13TeV [fb]	$\sigma_{ m NLO}$ @14TeV [fb]	$\sigma_{ m NLO}$ @27TeV [fb]	K-factor@14TeV
-1	$116.71^{+16.4\%}_{-14.3\%}$	$136.91^{+16.4\%}_{-13.9\%}$	$504.9^{+14.1\%}_{-11.8\%}$	1.86
0	$62.51^{+15.8\%}_{-13.7\%}$	$73.64^{+15.4\%}_{-13.4\%}$	$275.29^{+13.2\%}_{-11.3\%}$	1.79
1	$27.84^{+11.6\%}_{-12.9\%}$	$32.88^{+13.5\%}_{-12.5\%}$	$127.7^{+11.5\%}_{-10.4\%}$	1.66
2	$12.42^{+13.1\%}_{-12.0\%}$	$14.75^{+12.0\%}_{-11.8\%}$	$59.10^{+10.2\%}_{-9.7\%}$	1.56
2.4	$11.65^{+13.9\%}_{-12.7\%}$	$13.79^{+13.5\%}_{-12.5\%}$	$53.67^{+11.4\%}_{-10.3\%}$	1.65
3	$16.28^{+16.2\%}_{-15.3\%}$	$19.07^{+17.1\%}_{-14.1\%}$	$69.84^{+14.6\%}_{-12.1\%}$	1.90
5	$81.74^{+20.0\%}_{-15.6\%}$	$95.22^{+19.7\%}_{-11.5\%}$	$330.61^{+17.4\%}_{-13.6\%}$	2.14

Table 1. Total cross-sections are given for Higgs pair production at NLO QCD at (HE-)LHC for centre-of-mass energies of $\sqrt{s} = 13,14$ and 27 TeV. The scale uncertainties are given in percent.

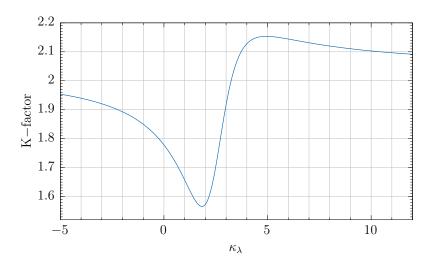


Figure 2. The dependence of the K-factor on the trilinear Higgs self-couplings κ_{λ} is given at $\sqrt{s} = 14 \,\text{TeV}$ in the full theory.

In Fig. 3, distributions of the invariant mass of the Higgs pair system m_{hh} are displayed for different values of κ_{λ} . They exhibit a characteristic dip around $m_{hh} \sim 350 \, \mathrm{GeV}$ for values of

the trilinear coupling around $\kappa_{\lambda} = 2.4$, which is not present in the SM case. This value of the trilinear self-coupling corresponds to a maximally destructive interference between triangle-like and box-like diagrams.

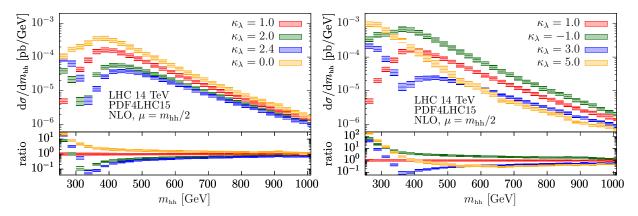


Figure 3. Distributions of the Higgs boson pair invariant mass m_{hh} for various values of κ_{λ} at $\sqrt{s} = 14 \,\text{TeV}$. The uncertainty bands are from scale variations as described in the text.

Note that since the contributions can be separated in triangle- and box-like diagrams, the top-Higgs Yukawa coupling y_t can easily be varied within the same code. A non-SM value of y_t yields in Eq. (1):

$$|\mathcal{M}_{\lambda}|^{2} = y_{t}^{4} \left[\mathcal{M}_{B}^{*} \mathcal{M}_{B} + \frac{\kappa_{\lambda}}{y_{t}} \left(\mathcal{M}_{B}^{*} \mathcal{M}_{T} + \mathcal{M}_{T}^{*} \mathcal{M}_{B} \right) + \left(\frac{\kappa_{\lambda}}{y_{t}} \right)^{2} \mathcal{M}_{T}^{*} \mathcal{M}_{T} \right] . \tag{3}$$

The cross-section can be computed by setting the correct value of the ratio κ_{λ}/y_t and of the global rescaling factor. For example, $\sigma(y_t = 1.2, \kappa_{\lambda} = 1) = (1.2)^4 \sigma(y_t = 1, \kappa_{\lambda} = 1/1.2)$. Fig. 4 shows the distribution of m_{hh} for extreme values of the top-Higgs Yukawa coupling that are still not experimentally excluded [4].

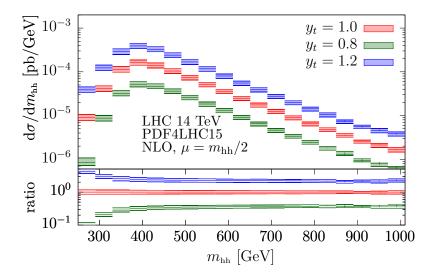


Figure 4. The distribution of the Higgs pair invariant mass m_{hh} for values of the top-Higgs Yukawa coupling $y_t \in \{0.8, 1, 1.2\}$.

4. Parton-shower matched results

We now consider NLO distributions matched to a parton shower. The Les Houches Events (LHE) [41] files produced by Powheg are used as input to the Pythia8.235 and Herwig7.1.4 parton showers. In the case of Herwig7, both the default angular-ordered \tilde{q} and the dipole showers are compared. The radiation-regulating hdamp parameter in Powheg is set to hdamp = 250 GeV. Multiple-parton interactions and hadronisation are switched off. The default tunes are used for both parton showers.

Fig. 5 displays the transverse momentum of the Higgs boson pair p_T^{hh} and the separation between the two Higgs bosons $\Delta R^{hh} = \sqrt{(\eta_1 - \eta_2)^2 + (\phi_1 - \phi_2)^2}$. Considering first the distribution of p_T^{hh} , both Herwig7 parton showers (PH7- \tilde{q} and PH7-dipole) generate similar results and reproduce the fixed-order NLO prediction in the far- p_T^{hh} range. In contrast, Pythia8 agrees with Herwig7 only for small transverse momenta, while it produces much harder radiation in the tail of the distribution. The same comments apply to the ΔR^{hh} observable in the region $0 < \Delta R^{hh} < \pi$ where shower contributions are important. Large parton-shower matching uncertainties in Higgs pair production have already been emphasized in Ref. [42].

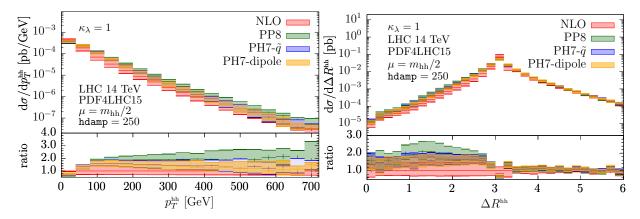


Figure 5. The transverse momentum p_T^{hh} of one (any) Higgs boson and the separation between the two Higgs bosons ΔR^{hh} are shown for the fixed-order NLO calculation and three parton showers, in the $\kappa_{\lambda} = 1$ case.

5. Conclusion

We have presented a new package for Higgs boson pair production at NLO QCD with full top-quark mass dependence. In this package, the trilinear Higgs self-coupling can be varied explicitly. Within the same code, simultaneous variations of the top-Higgs Yukawa coupling can also be produced. The public code for the Powheg-BOX-V2 event generator can be found at the website http://powhegbox.mib.infn.it in the User-Processes-V2/ggHH subdirectory. As a side note, approximations related to the HTL can be enabled for comparison purposes. We have emphasized that the full m_t -dependent NLO QCD corrections are accompanied by large K-factors. Moreover, they induce a sizeable dependence of the K-factors on the trilinear Higgs self-coupling κ_{λ} , which is not present in the HTL. We have compared fixed-order predictions at NLO QCD to parton-shower matched results. Both the Pythia8 and Herwig7 (\tilde{q} and dipole) parton showers can be matched directly to LHE files produced by Powheg. Full particle-level events can be produced with our framework, including Higgs boson decays and hadronisation.

References

- [1] Aad G et al. (ATLAS, CMS) 2016 JHEP ${f 08}$ 045 (Preprint 1606.02266)
- [2] Aaboud M et al. (ATLAS) 2018 JHEP 03 095 (Preprint 1712.02304)

- [3] Sirunyan A M et al. (CMS) 2018 Submitted to: Eur. Phys. J. (Preprint 1809.10733)
- [4] Sirunyan A M et al. (CMS) 2018 Submitted to: Phys. Lett. (Preprint 1812.06504)
- [5] Sirunyan A M et al. (CMS) 2019 Phys. Rev. Lett. 122 121803 (Preprint 1811.09689)
- [6] ATLAS 2018 Combination of searches for Higgs boson pairs in pp collisions at 13 TeV with the ATLAS experiment. Tech. Rep. ATLAS-CONF-2018-043 CERN Geneva URL https://cds.cern.ch/record/2638212
- [7] Dawson S, Dittmaier S and Spira M 1998 Phys. Rev. D58 115012 (Preprint hep-ph/9805244)
- [8] de Florian D, Grazzini M, Hanga C, Kallweit S, Lindert J M, Maierhöfer P, Mazzitelli J and Rathlev D 2016 JHEP 09 151 (Preprint 1606.09519)
- [9] Borowka S, Greiner N, Heinrich G, Jones S, Kerner M, Schlenk J, Schubert U and Zirke T 2016 Phys. Rev. Lett. 117 012001 [Erratum: Phys. Rev. Lett.117,no.7,079901(2016)] (Preprint 1604.06447)
- [10] Borowka S, Greiner N, Heinrich G, Jones S, Kerner M, Schlenk J and Zirke T 2016 JHEP 10 107 (Preprint 1608.04798)
- [11] Baglio J, Campanario F, Glaus S, Mühlleitner M, Spira M and Streicher J 2018 (Preprint 1811.05692)
- [12] Buchalla G, Capozi M, Celis A, Heinrich G and Scyboz L 2018 JHEP 09 057 (Preprint 1806.05162)
- [13] Nason P 2004 JHEP 11 040 (Preprint hep-ph/0409146)
- [14] Frixione S, Nason P and Oleari C 2007 JHEP 11 070 (Preprint 0709.2092)
- [15] Alioli S, Nason P, Oleari C and Re E 2010 JHEP 06 043 (Preprint 1002.2581)
- [16] Sjostrand T, Ask S, Christiansen J R, Corke R, Desai N, Ilten P, Mrenna S, Prestel S, Rasmussen C O and Skands P Z 2015 Comput. Phys. Commun. 191 159–177 (Preprint 1410.3012)
- [17] Bellm J et al. 2017 (Preprint 1705.06919)
- [18] Heinrich G, Jones S P, Kerner M, Luisoni G and Scyboz L 2019 (Preprint 1903.08137)
- [19] Heinrich G, Jones S P, Kerner M, Luisoni G and Vryonidou E 2017 JHEP 08 088 (Preprint 1703.09252)
- [20] Cullen G, Greiner N, Heinrich G, Luisoni G, Mastrolia P, Ossola G, Reiter T and Tramontano F 2012 Eur. Phys. J. C72 1889 (Preprint 1111.2034)
- [21] Cullen G et al. 2014 Eur. Phys. J. C74 3001 (Preprint 1404.7096)
- [22] Peraro T 2014 Comput. Phys. Commun. 185 2771–2797 (Preprint 1403.1229)
- [23] Binoth T, Guillet J P, Heinrich G, Pilon E and Reiter T 2009 Comput. Phys. Commun. 180 2317–2330 (Preprint 0810.0992)
- [24] Cullen G, Guillet J P, Heinrich G, Kleinschmidt T, Pilon E et al. 2011 Comput. Phys. Commun. 182 2276–2284 (Preprint 1101.5595)
- [25] van Hameren A 2011 Comput. Phys. Commun. 182 2427–2438 (Preprint 1007.4716)
- [26] Arnold K et al. 2009 Comput. Phys. Commun. 180 1661-1670 (Preprint 0811.4559)
- [27] Baglio J et al. 2014 (Preprint 1404.3940)
- [28] von Manteuffel A and Studerus C 2012 (Preprint 1201.4330)
- [29] Borowka S, Heinrich G, Jones S P, Kerner M, Schlenk J and Zirke T 2015 Comput. Phys. Commun. 196 470–491 (Preprint 1502.06595)
- [30] Borowka S, Heinrich G, Jahn S, Jones S P, Kerner M and Schlenk J 2018 Comp. Phys. Comm. (Preprint 1811.11720)
- [31] Jones S P 2016 PoS **LL2016** 069 (Preprint 1608.03846)
- [32] Butterworth J et al. 2015 (Preprint 1510.03865)
- [33] Dulat S, Hou T J, Gao J, Guzzi M, Huston J, Nadolsky P, Pumplin J, Schmidt C, Stump D and Yuan C P 2016 Phys. Rev. D93 033006 (Preprint 1506.07443)
- [34] Harland-Lang L A, Martin A D, Motylinski P and Thorne R S 2015 Eur. Phys. J. C75 204 (Preprint 1412.3989)
- [35] Ball R D $et\ al.\ (NNPDF)\ 2015\ JHEP\ {\bf 04}\ 040\ (Preprint\ {\bf 1410.8849})$
- [36] Buckley A, Ferrando J, Lloyd S, Nordström K, Page B, Rüfenacht M, Schönherr M and Watt G 2015 Eur. Phys. J. C75 132 (Preprint 1412.7420)
- [37] Cacciari M, Salam G P and Soyez G 2008 JHEP ${f 04}$ 063 (Preprint ${f 0802.1189}$)
- [38] Cacciari M and Salam G P 2006 Phys. Lett. B641 57-61 (Preprint hep-ph/0512210)
- [39] Cacciari M, Salam G P and Soyez G 2012 Eur. Phys. J. C72 1896 (Preprint 1111.6097)
- [40] Gröber R, Mühlleitner M, Spira M and Streicher J 2015 JHEP 09 092 (Preprint 1504.06577)
- [41] Alwall J et al. 2007 Comput. Phys. Commun. 176 300-304 (Preprint hep-ph/0609017)
- [42] Jones S and Kuttimalai S 2018 JHEP 02 176 (Preprint 1711.03319)